

Gradual regime shifts in fairy circles

Yuval R. Zelnik^a, Ehud Meron^{a,b}, and Golan Bel^{a,1}

^aDepartment of Solar Energy and Environmental Physics, Blaustein Institutes for Desert Research, Ben-Gurion University of the Negev, Sede Boqer Campus 8499000, Israel and ^bDepartment of Physics, Ben-Gurion University of the Negev, Beer Sheva 8410501, Israel

Edited by Simon A. Levin, Princeton University, Princeton, NJ, and approved August 19, 2015 (received for review March 4, 2015)

Large responses of ecosystems to small changes in the conditions regime shifts—are of great interest and importance. In spatially extended ecosystems, these shifts may be local or global. Using empirical data and mathematical modeling, we investigated the dynamics of the Namibian fairy circle ecosystem as a case study of regime shifts in a pattern-forming ecosystem. Our results provide new support, based on the dynamics of the ecosystem, for the view of fairy circles as a selforganization phenomenon driven by water–vegetation interactions. The study further suggests that fairy circle birth and death processes correspond to spatially confined transitions between alternative stable states. Cascades of such transitions, possible in various patternforming systems, result in gradual rather than abrupt regime shifts.

fairy circles | regime shifts | pattern formation | hybrid states | vegetation self-organization

he response of ecosystems to climate variability and anthropogenic disturbances is a fundamental aspect of ecology. Much attention has been devoted recently to large responses of ecosystems to small environmental changes or disturbances. Such responses, often termed "catastrophic regime shifts," are conceived of as abrupt transitions between two alternative stable states that occur uniformly across the ecosystem (1). Spatially extended systems can respond in different ways to varying conditions, including pattern formation (2-4) and spatially confined transitions to alternative stable states (5). When one of the alternative stable states is spatially patterned, a multitude of additional stable states can appear, each a mosaic of fixed domains that alternate between the uniform and the patterned states (4, 6, 7). The existence of such hybrid states can strongly affect the dynamics of state transitions in fluctuating environments (8) and may lead to gradual rather than abrupt shifts (5, 9). This prediction of pattern formation theory has never been tested either in a real ecosystem or in a model describing the dynamics of a specific ecosystem.

Pattern formation is widespread in natural ecosystems (3, 10), but good case models for studying gradual regime shifts are not abundant. An outstanding candidate is the Namibian fairy circle (NFC) ecosystem, which is fairly homogeneous and undisturbed, and recently has been the subject of intense research (11–17). The NFC ecosystem consists of a uniform matrix of perennial grass, punctured by circular gaps of sandy bare soil—the fairy circles that on landscape scales form nearly periodic patterns (12, 17).

Various explanations for the formation of fairy circles have been suggested, including the release of poisonous gas and the feeding habits of ants and termites (14, 17, 18). These explanations, however, have not uncovered, as of yet, the small-scale feedbacks needed to account for the emergence of the large-scale order (2, 4, 10). On the other hand, it is well established by model studies and confirmed by empirical observations that patch-scale biomass-water feedbacks can lead to regular landscape-scale vegetation patterns and that periodic gap patterns, which highly resemble fairy circle patterns, can appear from uniform vegetation in response to water stress (3, 19–22). Indeed, recent detailed comparisons of fairy circle remote sensing data and model gap patterns show high similarity in static properties, such as hexagonal symmetry and spatial correlations of fairy circle size and distance (17).

In this paper, we combine a theoretical analysis of a vegetation model, fitted to the biotic and abiotic conditions of the NFC ecosystem, with an empirical data analysis, to account for fairy circle dynamics in the NamibRand Nature Reserve from the years 2004 to 2013, thereby accomplishing two goals. The first goal is to substantiate the view of fairy circles as a pattern-formation phenomenon by complementing the current statistical evidence (11, 15, 17) with evidence based on the dynamics of the NFC ecosystem. The second goal is to demonstrate the feasibility of gradual regime shifts in the NFC ecosystem as cascades of uni-directional transitions across hybrid states.

Model

The model we use is based on the Gilad et al. vegetation model (21, 23), which captures three different mechanisms of vegetation pattern formation (24). However, applying the model to the NFC ecosystem (sandy soil, confined root zones) results in a simplified model describing the dynamics of aboveground biomass (*B*) and soil-water (*W*) areal densities. The simplified model captures a single pattern-forming feedback associated with the high rate of water uptake by the perennial grasses and the fast soil-water diffusion (relative to biomass expansion) in sandy soils. This mechanism leads to higher soil-water content in the bare fairy circles compared with the vegetation matrix (24), in agreement with reported observations (14, 15). The model equations read

$$\partial_T B = \Lambda W B (1 - B/K) (1 + EB)^2 - M B + D_B \nabla^2 B, \qquad [1]$$

$$\partial_T W = P - N(1 - RB/K)W - \Gamma WB(1 + EB)^2 + D_W \nabla^2 W.$$

In the biomass equation, Λ is the biomass growth rate coefficient, K is the maximal standing biomass, E is a measure for the root-to-shoot ratio, M is the mortality rate, and D_B represents the seed-dispersal or clonal growth rate. In the soil-water equation, P is the precipitation rate, N is the evaporation rate, R is a dimensionless factor representing a reduction of the evaporation

Significance

Combining model and empirical data analyses, we show that transitions between alternative stable states (regime shifts) in spatially extended ecosystems are not necessarily abrupt; cascades of local shifts between a multitude of stable states, composed of patterned and uniform domains, can result in global regime shifts that proceed gradually. In the Namibian fairy circle ecosystem (barren circular gaps in grasslands), such local shifts appear as fairy circle birth or death processes. This mechanism of regime shifts has never been demonstrated in a specific natural context. In addition, the results reported here further support the view of fairy circles as a self-organization phenomenon by providing a new type of evidence based on dynamical processes.

Author contributions: Y.R.Z., E.M., and G.B. designed research; Y.R.Z., E.M., and G.B. performed research; Y.R.Z. and G.B. analyzed data; and Y.R.Z., E.M., and G.B. wrote the paper.

The authors declare no conflict of interest.

This article is a PNAS Direct Submission.

¹To whom correspondence should be addressed. Email: bel@bgu.ac.il.

This article contains supporting information online at www.pnas.org/lookup/suppl/doi:10. 1073/pnas.1504289112/-/DCSupplemental.



Fig. 1. Steady states of the model. (A) Partial bifurcation diagram for a 1D system, showing the L^2 norm of the biomass vs. the precipitation rate. The steady states shown include two uniform solutions of bare soil and uniform vegetation (black), two periodic solutions of gap patterns with different wavelengths (red and green) spanning the bistability range of uniform vegetation and patterned states, and hybrid solutions representing uniform vegetation with an increasing (as the branch snakes down) number of gaps (blue). The solid (dashed) lines in the diagrams represent stable (unstable) solutions. (B) Blowup of the hybrid-state range. (C) The periodic solution corresponding to the red branch in A. (D) A hybrid solution corresponding to the lowest blue branch in B (a single missing gap) obtained with P = 102[mm/y]. (E and F) The 2D versions of the solutions shown in C and D. (G and H) Corresponding fairy circle patterns, obtained from the 2013 satellite image.

rate due to shading, Γ is the water-uptake rate coefficient, and D_W is the effective soil-water diffusivity in the lateral (X, Y) directions. The model parameters used in this study are different from those used by Getzin et al. (17) and were estimated from published data. We refer the reader to *SI Appendix* for more details on the derivation of the model and to *Materials and Methods* for details on the parameter estimations and values.

Results

We first study the stationary solutions, in one spatial dimension (1D), along the precipitation axis. Fig. 1A shows uniform solutions representing bare soil and uniform vegetation and periodic solutions representing gap patterns. Within the bistability range of uniform vegetation and gap patterns, there is a subrange with many stable hybrid states, consisting of confined domains of uniform vegetation in an otherwise periodic vegetation pattern (and vice versa; Fig. 1B). The figure further shows 1D spatial profiles of a periodic gap pattern (Fig. 1C) and of a hybrid state that describes a periodic pattern with one missing gap (Fig. 1D). The corresponding 2D patterns are shown in Fig. 1 E and F, and similar fairy circle patterns (obtained from satellite images) are shown in Fig. 1 G and H. Similarly to other models of dryland vegetation (9, 22), the model also exhibits spotted and striped patterns (SI Appendix), for lower values of precipitation.

Next, we use the model, along with high-resolution satellite images of the NamibRand area from 2004 to 2013, to suggest that fairy circle "birth" and "death" processes (appearance and disappearance of gaps) (13) correspond to transitions between hybrid states. Fig. 2*A* shows the birth of a fairy circle following a drought in 2007, whereas Fig. 2*C* shows the death of a fairy circle following a spate (a period of excess precipitation) in 2008. Fig. 2 *B* and *D* shows the same behaviors in model simulations, starting with initial conditions that mimic the initial fairy circle patterns in 2004 and applying precipitation downshift and upshift to mimic the drought and spate. The precipitation shifts were chosen to be strong enough to take the system out of the subrange of hybrid states (in opposite directions), thus inducing hybrid-state transitions.

In addition to the appearance and disappearance of gaps, Fig. 2 also shows changes in gap sizes; a moderate drought expands

the gaps, whereas a spate contracts the gaps. To gain a deeper understanding of these dynamics, we correlated fairy circle data that were extracted from satellite images with rainfall data from several meteorological stations in the NamibRand region and compared the observed correlations with those predicted by the model. Fig. 3 shows the cross-correlations between the accumulated rainfall over different time periods (integration time) and the average fairy circle size (Fig. 3A) and the fairy circle number (Fig. 3B). Analogous cross-correlations using model simulations (Fig. 3 C and D) show a qualitative agreement. The simulation results are based on averaging more than 100 regions and long time series, and therefore, they show smooth curves. Fig. 3 E and F shows the same quantities for the model simulations but averaged over fewer regions and using shorter time series. The curves in these panels resemble the curves for the real data (Fig. 3 A and B). The stronger correlations in the simulations (compared with those in the field) between the gap size and the precipitation is due to the fact that the simulated system is homogeneous, whereas the field is heterogeneous and also because the simulated precipitation is not intermittent as it is in the field. The results highlight the different time scales for changes in the size and in the number of fairy circles. For fairy circle size, the correlation magnitude is maximal for a relatively short integration time (of a few years), whereas for fairy circle number, the correlation magnitude does not decrease with time throughout the time range of available data. The different characteristics of the correlation functions suggest that the time scale for changes in the fairy circle size is much shorter than the time scale for changes in the fairy circle number.

We turn now to the question of gradual regime shifts and ask whether climate variability in the form of repeated short droughts can induce a gradual regime shift. To this end, we simulated the model equations, starting with a uniform vegetation state that is locally disturbed to form a few gaps, and using precipitation downshifts that take the system outside the hybrid-state subrange periodically in time. As Fig. 4*A* shows, such a precipitation regime drives the system toward a nearly periodic patterned state (rightmost panel) by successive shifts to hybrid states of larger gap numbers. The opposite transition is shown in Fig. 4*B*, in which a series of short spates drives the system from a nearly periodic gap



Fig. 2. Birth and death of fairy circles as hybrid-state transitions. (*A* and *C*) Satellite images showing the dynamics of the appearance/disappearance of a bare soil domain (fairy circle birth/death). (*B* and *D*) Snapshots of corresponding simulations using initial conditions derived from the 2004 satellite images shown in *A* and *C*. *B* and *D* show the simulated response to 1 y of drought/spate (P = 84[mm/y]/P = 143[mm/y]), after which the precipitation was set back to normal (P = 102[mm/y]). The time shown at the top of the satellite image (simulation) denotes the year it was captured (number of years elapsed from the beginning of the drought or the spate). The time intervals between the simulation snapshots were chosen to emphasize the short-time-scale changes in gap size. All panels show the dynamics of a region of 30 × 30 m.

pattern, through a multitude of hybrid states, to a uniform vegetation state. Systems initially in a uniform vegetation state (*SI Appendix*) or a perfectly periodic patterned state (Fig. 4C), exposed to the same series of droughts or spates, show only minor fluctuations in the biomass density and remain practically unchanged.

Discussion

We regard the model results described above and their agreement with field observations as compelling evidence for the view of fairy circles as a pattern formation phenomenon and for the existence of hybrid states in the NFC ecosystem. This evidence is based on the following grounds.

Spatial Properties. The model, adjusted to the particular context of the NFC ecosystem, predicts gap patterns that resemble the spatial distribution of fairy circles in the field, as Fig. 1 shows. Moreover, the model predictions agree with recent field observations of higher soil-water content within the fairy circles, relative to vegetated domains (14, 15).

Dynamics. Fairy circle birth and death processes can be reproduced with model simulations by temporal escapes outside the existence range of hybrid states (Fig. 2), supporting the interpretation of these processes as hybrid-state transitions.

Correlations with Precipitation. Significant correlations between the rainfall and the number and size of fairy circles indicate the importance of biomass-water interactions in the dynamics of the NFC ecosystem. These correlations and the time scales associated with them, short for size variations and long for number variations, are in agreement with the model predictions (Fig. 3). The time scale difference can be understood using pattern formation theory; gap size changes are related to the convergence to a steady state, whereas gap number changes are related to the dynamics of fronts that separate domains of uniform vegetation and gap patterns (8), structural and wavelength changes of the patterned state, and other nonlinear processes.

This evidence does not rule out alternative hypotheses (25, 26), but these hypotheses cannot be considered as satisfactory explanations of the fairy circle phenomenon unless they uncover the local feedbacks that are responsible for the emergence of largescale order and account for the correlation of fairy circle dynamics with rainfall variability. The model suggested here requires additional evidence to fully uncover the origin and dynamics of the NFC. First, measurements of the soil-water diffusivity and the dependence of the soil-water extraction rate on the vegetation density are required to support the mechanism suggested in our model. Second, the precipitation fluctuations in the field are very large and, according to the simplified model, are expected to drive the



Fig. 3. Correlations between the number and average size of fairy circles and the accumulated precipitation. All graphs show the negative covariance vs. the integration time for the accumulated precipitation (see *Materials and Methods* for precise definitions). (*A* and *C*) Correlations between average fairy circle size and accumulated rain for real data and simulation results, respectively. (*B* and *D*) Same information for the fairy circle number. Real data analyses (*A* and *B*) are based on eight satellite images (i.e., eight time points) and averaging over four regions. Simulation results (*C* and *D*) are based on 100 time points and averaging over 120 regions. Therefore, the curves for the simulation results are smoother. (*E* and *F*) Correlations for simulation data, similar to *C* and *D*, but including the same number of time points and regions as the real data. The shaded regions show the error assessment, calculated from the SD of the sample.



Fig. 4. The response of 2D patterns to periodic short droughts or spates. (*A*) A gradual regime shift from a stable hybrid state (leftmost panel) to a nearly periodic gap pattern (rightmost panel). The shift is driven by periodic 1-y droughts with P=81[mm/y], followed by 15 y of P=102[mm/y]. (*B*) The reversed shift, namely a gradual shift from a nearly periodic pattern to uniform vegetation, driven by 1-y spates with P=138[mm/y] followed by 15 y with P=102[mm/y]. The droughts/spates take the system out of the hybrid-state range (Fig. 1 *A* and *B*) and induce hybrid-state transitions in the course of which gaps appear/disappear, leading to a gradual regime shift. (*C*) When the initial pattern is strictly periodic, no regime shift takes place even though the system is subjected to the same rainfall regime as in *B*. The simulated domains are 60×56 m.

system toward one of the uniform states. We believe that accounting for the spatial heterogeneity of the ecosystem, i.e., topography, soil heterogeneity, and other factors, would result in more robust patterns in the model. Third, the exact biological origin of hybrid states in the NFC system remains unclear. Controlled field experiments of the FCs dynamics, combined with the mathematical framework suggested here, will be able to provide conclusive evidence for the hypothesis proposed here and reveal the relevant biological mechanisms. In particular, experiments in areas with different soil textures, topography, and plant species, together with manipulations of the precipitation, are expected to better clarify the relative importance of specific plant physiology and ecosystem characteristics in shaping the observed NFC dynamics.

The results presented here are not limited to the NFC ecosystem and may be observed in other pattern-forming systems. The appearance of hybrid states in systems exhibiting a bistability of uniform and patterned states implies that transitions, from uniform vegetation to a gap pattern and vice versa, may take place through successive hybrid-state transitions driven by periodic escapes outside the existence range of hybrid states. Dynamics of this type allow for spatially extended ecosystems to exhibit gradual rather than abrupt regime shifts.

Materials and Methods

Model Analysis. Vegetation pattern formation in this simplified model results from a finite wavenumber (Turing) instability of the uniform vegetation state. This instability requires strong water uptake, quantified by the parameters Γ and E, and fast soil-water transport, characterized by D_W , relative to biomass dispersal, quantified by D_B (24). The high hydraulic conductivity, typical of sandy soils, acts in favor of this condition, but field observations point toward the possible role of an additional factor: the large underground termite populations found in the NFC ecosystem (14). The underground

network of channels that the termites form may increase soil-moisture transport in the lateral directions, leading to higher effective values of D_{W} . Studying this possible termite effect is not only significant for understanding fairy circle formation, but also for understanding regime shifts, as the presence of termites may affect the existence and stability ranges of the uniform and patterned vegetation states, as well as those of the hybrid states.

The bifurcation diagram in Fig. 1 *A* and *B* was calculated using a numerical continuation method (AUTO software). The dynamics of the system was simulated using the pseudospectral method with periodic boundary conditions in Matlab, in either one or two dimensions. The simulations in Fig. 2 were made using initial conditions of steady states of the system, each derived from a region of the 2004 satellite image. That is, each of the initial conditions was derived by taking the relevant region in the original image, segmenting it into vegetation and bare soil areas, and setting the values of the biomass and soil-water areal densities to those corresponding to the uniform solutions (uniform vegetation and bare soil, respectively). The system was then integrated forward in time, with a constant value of precipitation rate, *P*, until a steady state was reached.

Parameter Estimations. In all model simulations, we used the following parameter values: $E = 7[m^2/kg]$, $K = 0.4[kg/m^2]$, M = 10.5[1/y], N = 15[1/y], $\Lambda = 0.9[(m^2/kg)/y]$, $\Gamma = 12[(m^2/kg)/y]$, R = 0.7, $D_B = 1.2[m^2/y]$, $D_W = 150[m^2/y]$. These values were either taken from data published in the literature or estimated using such data, as described below. The precipitation rate, *P*, was varied within the range 50 < P < 150[mm/y], which is similar to the range of annual rainfall in the NFC ecosystem.

The maximum standing biomass, K, was estimated based on maximal biomass densities reported for semiarid savannah grasses (27). The mortality rate, M, was estimated based on the mortality data of *Stipagrostis uniplumis* as a representative example of an abundant perennial grass in the NFC ecosystem (28). The reported mortality rate was measured under normal conditions (i.e., including all of the growth factors). The mortality rate in the model represents the natural mortality alone, and therefore, we used a higher mortality rate. The biomass diffusion parameter, D_{Br} , was estimated

based on published clonal growth and seed dispersal data (29). The value for the shading factor, *R*, was inferred from data on reduced evaporation by tree canopies (30). No relevant literature was found for the root-to-shoot parameter, *E*, for the perennial grass; the chosen value is similar to that used in an earlier study (23) for woody dryland species. The evaporation rate, *N*, was estimated using the relation N = P/W for a uniform bare soil state, where the soil-water density, *W*, was determined from water-content sampling data inside a fairy circle (14). The water-uptake rate coefficient, Γ , was inferred from differences in the levels of soil water within and outside the fairy circles, and from biomass measurements (31). The biomass growth parameter, Λ , was determined from estimates of the ratio of transpiration to dry biomass for tropical grass (32) and the previously estimated value of Γ .

Finally, the value of the soil-water diffusivity, D_{W} , was estimated using the Van Genuchten model for water retention curves (33). Using parameters corresponding to sandy soil (we used the parameters $\theta_s = 0.43$, $\theta_r = 0.0045$, $K_s = 0.297$, $\alpha_{VG} = 14.5$, n = 2.68, m = 1 - 1/n, and the reported water content of $\theta = 0.025 - 0.15$) and the values of soil-water content that correspond to those found in the field (14), we estimate D_W to be in the range $0.1 - 100[m^2/y]$. We used a value that slightly exceeds the upper limit of this range to account for the possible enhancement of lateral water transport due to the network of underground channels formed by termite populations (14). We emphasize that the model results reported here are robust and can be obtained with many different sets of parameters (*SI Appendix*).

Earth Data Analysis. We analyzed high-resolution satellite images taken over the period of 2004–2013 in the NambiRand Nature Reserve. The snapshots shown in Figs. 1 and 2 were processed from four images, captured in 2004, 2008, 2010, and 2013, whose spatial resolution is as high as 0.5[m]. The rgb data shown were derived using Pan-Sharpening with ERDAS software when rgb was available (2004, 2010, and 2013), and false-color was used for the 2008 image.

The data used for Fig. 3 were taken from monthly precipitation data and from measurements of fairy circles features using satellite images. The precipitation data were derived from interpolations of both the readings of meteorological stations within the NambiRand Nature Reserve (for the years 2000–2012) and of the NOAA data center (for the years 1990–1999) for two locations in Namibia. The numbers and sizes of the fairy circles were estimated from eight satellite images: the four previously described (from 2004, 2008, 2010, and 2013) and four others (from 2005, 2009, 2011, and 2012) taken from Google Earth data. From each of the eight images, four regions of 180 \times 180 m were chosen and analyzed. A proprietary segmentation

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algorithm, involving morphological operations and thresholding with a CLAHE algorithm, was used to identify each fairy circle. The identification results were then reviewed manually to minimize errors caused by the automatic process, and in total, about 800 fairy circles were identified and measured for each time point.

The cross-correlation measures shown in Fig. 3 were calculated by comparing the accumulated precipitation, ψ , with either the number of fairy circles, α , or the average size of a fairy circle, β . The accumulated precipitation is defined as

$$\psi_i(S) = \sum_{j=0}^{S-1} P_{(i-j-L)}.$$

Here, P_k is the precipitation at time k, L is the lag time, and S is the integration time, with all times given in number of years. To fit the rainy season in the field, we considered the annual precipitation between November 1 and the following October 31. The lag time, L, was set to zero (i.e., considering the accumulated rain during a period S ending at the end of the previous year) for the fairy circle size and L=1 for the fairy circle number; these values yield the most significant correlations between the precipitation and the fairy circle dynamics. The cross-correlation for the fairy circle as

$$C_{\alpha}(S) = \frac{\sum_{i=1}^{N} \left[\psi_i(S) - \overline{\psi(S)}\right] \cdot (\alpha_i - \overline{\alpha})}{\sqrt{\sum_{i=1}^{N} \left[\psi_i(S) - \overline{\psi(S)}\right]^2} \cdot \sqrt{\sum_{i=1}^{N} (\alpha_i - \overline{\alpha})^2}}$$

 \overline{A} stands for the average of A [$\overline{A} \equiv (1/N) \sum_{i=1}^{N} A_i$], and N is the number of time points, with the value of 8 for the observation data, and either 8 or 100 for the simulation data. The cross-correlation for the fairy circle size, $C_{\beta}(S)$, was calculated in the same manner. Dataset S1 includes all of the information that was used to generate Fig. 3.

ACKNOWLEDGMENTS. We thank Nils Odendaal, the Chief Executive Officer of the NamibRand Nature Reserve, for providing us the precipitation measurements of various meteorological stations within the reserve and Elad Eizner and Noa Levi-Ohana for help with the segmentation and analysis of the satellite data. The research leading to these results received funding from the European Union Seventh Framework Programme (FP7/2007-2013) under Grant 293825 and Israel Science Foundation Grant 305/13.

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