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A Recurrent Network Model of Somatosensory Parametric Working Memory in the Prefrontal Cortex

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Abstract

A parametric working memory network stores the information of an analog stimulus in the form of persistent neural activity that is monotonically tuned to the stimulus. The family of persistent firing patterns with a continuous range of firing rates must all be realizable under exactly the same external conditions (during the delay when the transient stimulus is withdrawn). How this can be accomplished by neural mechanisms remains an unresolved question. Here we present a recurrent cortical network model of irregularly spiking neurons that was designed to simulate a somatosensory working memory experiment with behaving monkeys. Our model reproduces the observed positively and negatively monotonic persistent activity, and heterogeneous tuning curves of memory activity. We show that fine-tuning mathematically corresponds to a precise alignment of cusps in the bifurcation diagram of the network. Moreover, we show that the fine-tuned network can integrate stimulus inputs over several seconds. Assuming that such time integration occurs in neural populations downstream from a tonically persistent neural population, our model is able to account for the slow ramping-up and ramping-down behaviors of neurons observed in prefrontal cortex.

Introduction

The physical world is described in terms of continuous (analog) quantities, such as space, direction, time, velocity and frequency. Through evolution, animals and humans must have developed the mental ability not only to encode analog physical quantities as sensory stimuli, but also to remember such quantities by virtue of an active internalized representation in working memory. A basic question in neuroscience is how analog physical stimuli are represented and stored in memory in the brain. Starting in the 1980s,

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We dedicate this paper to the memory of Patricia S. Goldman-Rakic, a friend and colleague whose prescience and enthusiasm have shaped research in working memory and the prefrontal cortex.

Supplementary Material

Supplementary material can be found at: <http://www.cercor.oupjournals.org>

neurophysiologists have investigated this question, with a focus on spatial information. In a delayed response task, an animal is required to remember the spatial location of a sensory cue across a delay period of a few seconds. Neurons in the parietal cortex (Gnadt and Anderson, 1989; Chafee and Goldman-Rakic, 1998) and prefrontal cortex (Funahashi *et al.*, 1989; Rainer *et al.*, 1998) show persistent activity that is correlated with memory maintenance during the delay period. Mnemonic neural activity is selective to spatial locations, quantified by a bell-shaped tuning. That is to say, a given neuron shows an elevated delay in activity only for a relatively narrow range of positional cues, and the spatial information is encoded by ‘what’ neurons fire significantly during the memory period. A similar coding strategy is also used by the neural system that encodes and predicts an animal’s head direction (see Sharp *et al.*, 2001; Taube and Bassett, 2003).

More recently, another form of working memory for analog quantities was discovered in a somatosensory delayed response experiment (Romo *et al.*, 1999; Brody *et al.*, 2003). In this task, the monkey is trained to compare the frequencies of two vibrotactile stimuli separated in time by a delay of 3–6 s; therefore the behavioral response requires the animal to hold in working memory the frequency of the first stimulus across the delay period. It was found that neurons in the inferior convexity of the prefrontal cortex show persistent activity during the delay, with the firing rate of memory activity varying monotonically with the stimulus frequency. Therefore, the stimulus is encoded by the firing rates at which all neurons discharge spikes. Similarly, in the oculomotor system that maintains a fixed eye position between quick saccades, persistent neuronal activity is proportional to the eye position (Robinson, 1989; Aksay *et al.*, 2000). We emphasize that the meaning of tuning curve for delay period activity is profoundly different from that of responses to sensory inputs. Conventionally, the stimulus selectivity of neuronal firing *during stimulus presentation* is quantified by a tuning curve. For example, the higher the input intensity, the larger the neural response. By contrast, in a working memory task, the mnemonic neural activity is measured *after the transient stimulus is withdrawn*, during the delay period. If a working memory network exhibits a family of delay period activity that is monotonically tuned to a feature of the transient stimulus, this entire family of mnemonic activities with different firing rates must be all realizable under exactly the same external conditions (during the delay when external inputs are absent). How a cortical network, for example in the prefrontal cortex, can be capable of such a feat presents an intriguing open question in neuroscience.

Persistent neural activity during working memory is generated internally in the brain, either by recurrent circuit mechanisms (Lorente de Nó, 1933; Goldman-Rakic, 1995) or by intrinsic cellular mechanisms (Camperi and Wang, 1998; Egorov *et al.*, 2002). According to the attractor model of persistent activity (Amit, 1995; Wang, 2001), a neural assembly has a resting state at a low firing rate, as well as a stable active (‘attractor’) state at an elevated firing rate that is self-sustained by reverberative excitation. Recently, this idea has been extended to the realm of working memory of an analog physical quantity, and tested rigorously using biophysically based recurrent network models. In models of spatial working memory, the spatial locations are encoded by a continuum of ‘bell-shaped’ localized persistent states (‘bump attractors’) (Camperi and Wang, 1998; Compte *et al.*,

2000; Gutkin *et al.*, 2001; Tegnér *et al.*, 2002; Ermentrout, 2003; Renart *et al.*, 2003a). In neural integrators in the oculomotor circuit, persistent firing rate of each neuron varies linearly with the gaze position (Cannon *et al.*, 1983; Robinson, 1989). As a result, if rates of different neurons are plotted against each other, they fall on a straight line in the ‘firing-rate space’. This observation led to the theoretical concept of ‘line attractors’ (Seung, 1996).

It was recognized (Cannon *et al.*, 1983; Seung *et al.*, 2000a,b) that very fine tuning of synaptic feedback is necessary to create such monotonically tuned neural integrators in models. The feedback must be finely tuned, so that if the firing rate of a neuron is altered by a transient input, then the resulting change in synaptic feedback to the neuron is exactly the amount required to maintain the new firing rate. Any mis-tuning of the feedback results in an exponential decay or growth of firing rates away from the desired memory state to one of a few stable levels. The drift occurs with a persistence time proportional to the synaptic time constant divided by the fractional error in the tuning (Seung *et al.*, 2000b), such that synaptic weights must be tuned to one part in a hundred if the desired network time constant (10 s) is 100-fold longer than the synaptic time constant (100 ms).

Koulakov *et al.* (2002) recently proposed a mechanism without the fine-tuning requirement. The idea is to combine many robust, bistable groups to form a system with multiple stable states. If there are enough bistable units, which switch to persistent active states following transient stimuli of different strengths, the summation of neural units’ outputs will become indistinguishable from a continuous quantity that encodes the stimulus feature. Such an integrator or memory device is similar to the stable digital memory of a computer (which can simulate analog quantities). One salient feature of the Koulakov model is that each individual neuron’s tuning curve of delay period activity displays a significant jump in the firing rate between the resting state and active memory states. Whether this prediction is consistent with experimental data from neural integrators (Aksay *et al.*, 2000; Nakamagoe *et al.*, 2000) remains unclear.

In this paper, we present a new model of persistent activity monotonically tuned to an analog stimulus feature. Our model was designed to reproduce the prefrontal neural activity in the vibrotactile delayed matching-to-sample experiment (Romo *et al.*, 1999; Brody *et al.*, 2003). Conceptually, this model is similar to that of Seung *et al.* (2000a), and we present a mathematically precise description of what is meant by the requirement of network fine-tuning for this class of working memory models. Furthermore, in order to apply our model to the prefrontal cortex during parametric working memory, we elaborated on existing models in several important ways. First, we used large neural networks (12 000 neurons), appropriate for cortical circuits, in contrast to the oculomotor neural models with only tens of neurons. Secondly, our model has a locally structured circuit architecture, whereas in Seung *et al.*’s model (Seung *et al.*, 2000a) synaptic connections are globally determined by a gradient-descent optimization algorithm. Thirdly, noise is absent in the models of Seung *et al.* (2000a) and Koulakov *et al.* (2002), and the robustness of network behavior against noise was not assessed. Cortical neurons receive a large amount of background noise inputs, which are taken into account in our model. Fourthly, in both integrator models (Seung *et al.*, 2000a; Koulakov *et al.*, 2002), neurons are silent in the resting state. By contrast, prefrontal neurons show spontaneous activity at low rates prior to stimulus presentation, and our model

reproduces such spontaneous neural activity in the resting state. Fifthly, our model includes both excitatory and inhibitory neural populations. Finally, we propose a two-network model that reproduces both positively and negatively monotonic neurons which have been observed experimentally in prefrontal neurons.

Materials and Methods

Network Architecture

Our network model represents a cortical local circuit composed of a number (typically two sets of 12) of neural groups or ‘columns’ (Fig. 1). The two halves of the network represent the two sets of cells that receive either positively monotonic or negatively monotonic transient input from neurons in S2 (Salinas *et al.*, 2000). Each neural group (labeled by $i = 1, 2, \dots, 12; 1^*, 2^*, \dots, 12^*$) contains 400 excitatory cells and 100 inhibitory cells, so we simulate $12 \times 2 \times 500 = 12\,000$ cells in total. With such a large number of neurons per column, the instantaneous firing rate of the group is a meaningful quantity that encodes the information in the network. Individual spike times are noisy, and any data for a single neuron are only uncovered by averaging over many trials.

The connectivity from group j to group i , $W_{j \rightarrow i}$, is structured such that synaptic connections are stronger between cells within a column than between two columns. The strong recurrent excitation within a column means that each column is close to being bistable — that is, the self-excitation within a column is not enough to raise the firing rate when all cells are in the spontaneous state, but is almost enough to maintain a high firing rate if the cells are given transient excitation. The strengths of connections with other groups is key to the maintenance of higher firing rates, and to obtaining a large number of different stable states. The neurons within a column are all connected identically (all-to-all), so receive identical recurrent input. They are only differentiated by the background noise they receive.

The connection strength between two neural groups decays exponentially with the difference in their labels, as shown in Figure 1 for the E-to-E connections between excitatory cells. All connections with inhibitory cells (E-to-I, I-to-E and I-to-I) are strongest within a column and decay symmetrically between columns. The E-to-E network architecture has a ‘high-to-low’ asymmetry, in the sense that if $j > i$, then $W_{i \rightarrow j} < W_{j \rightarrow i}$. This results in a gradient of effective excitability across the network, with the groups with the lowest labels being most excitable. Such a distribution of excitability is important for the network to show a graded response to a range of stimuli.

A fixed gradient of intrinsic thresholds (produced by a range of leak conductances for example) can be used to generate a range of excitabilities to external stimuli. Both Koulakov *et al.* (2002) and Seung *et al.* (2000a) used such a network. Koulakov *et al.* included symmetric connectivities between neurons of differing thresholds, but with very low strength, such that the feedback to a neuron within a group was significantly greater than the feedback to a neuron from its effect on other neurons with different thresholds. Hence, the concept of Koulakov *et al.*’s network is one of a discrete set of bistable groups, each of which switch to an excited state following a different magnitude of input.

In Seung *et al.*'s network, far more feedback comes to a cell through its connections to other cells (apart from the most excitable cell, which is bistable while all others are silent). In Seung *et al.*'s line attractor network, asymmetrical connections are necessary, with stronger synaptic weights from low- to high-threshold neurons. This is because the whole network is designed to have a linear input–output relation. When just one cell (the lowest threshold) is firing, the change in output comes solely from that cell, so connections from that cell are strong. When all neurons are firing, the same change in input causes all cells to increase in output. For the total change in output to be the same, the output from higher threshold cells must be progressively smaller. Hence high-to-low connections are weaker than low-to-high.

In all three cases, a range of excitabilities is used to ensure that a wide range of inputs leads to different responses in the network. A single bistable group of neurons can only distinguish whether a stimulus is greater or lower than its single threshold. A range of thresholds allows for more stimuli to be distinguished. In the prefrontal cortex, it is unlikely that there are columns or neural groups with large systematic differences in their intrinsic excitability. Hence we use systematic differences in the synaptic strengths between populations (which are readily altered through learning mechanisms) to create groups of neurons that require different strengths of stimulus for their firing rate to deviate strongly from their spontaneous rate. Such a network results in stronger connections from higher threshold to lower threshold neurons. This is evident, as it is the extra excitation arising from the stronger synaptic weights from higher-threshold populations that causes low-threshold populations to be more readily excited by external input. Since silent cells cannot influence the activity of other cells, however strong the connections, this effect is absent without spontaneous activity. Such is the case in the other models (Seung *et al.*, 2000a; Koulakov *et al.*, 2002).

Our complete model contains two such networks connected by reciprocal inhibition (Fig. 1). The model receives input from two types of cells, which mimic the outputs of two neuronal types in cortical area S2 that show responses to vibrotactile stimuli (but not persistent delay activity). The positively monotonic cells increase their firing rate with larger stimulus frequency, while negatively monotonic cells act oppositely (Salinas *et al.*, 2000). We assume that the two types of transient inputs from S2 project to the two different networks in our model. This assumption automatically leads to both positively and negatively monotonic tuning of the PFC cells in our model.

Single Neurons and Synapses

In the spiking network model, we simulate the individual cells as leaky integrate-and-fire neurons (Tuckwell, 1988). All inputs to a cell are given in terms of excitatory or inhibitory conductances, which give rise to currents that are integrated over time in the membrane potential. Once the membrane potential reaches a threshold, the cell fires an action potential and the membrane potential is reset to a fixed value for a refractory time, before temporal integration continues. The full dynamical equations are presented in the Supplementary Material.

Our network makes the simplification that afferent input reaches cells through AMPA receptor-mediated (AMPA) synapses of 2 ms time constant, while recurrent activity is

transmitted purely through the slower NMDA receptors (NMDARs), with 100 ms time constant. The importance for working memory of the relative abundances and strengths of AMPARs and NMDARs has been investigated elsewhere (Wang, 1999; Compte *et al.*, 2000), showing the deleterious effect of a large ratio of AMPARs to NMDARs in recurrent synapses. Here, we utilize the slow time-constant of NMDARs in recurrent connections to enhance the time-constant of the entire network (Seung *et al.*, 2000b).

All excitatory, recurrent synapses exhibit short-term presynaptic facilitation and depression (Varela *et al.*, 1997; Hempel *et al.*, 2000). We implement the scheme described by Matveev and Wang (2000), which assumes a docked pool of vesicles containing neurotransmitter, where each released vesicle is replaced with a time constant, τ_d . The finite pool of vesicles leads to synaptic depression, as when the presynaptic neuron fires more rapidly than vesicles are replaced, no extra excitatory transmission is possible. Such synaptic depression contributes to stabilizing persistent activity at relatively low rates, strongly enhancing the postsynaptic effect of NMDAR saturation. For example, a synapse with 16 docking sites and a docking time constant of 0.5 s has a maximum rate of vesicle release of 32 per second. Such saturation in the recurrent excitation reduces the excitatory feedback significantly, even for firing rates of <20 Hz. This allows the network to have stable states of persistent activity with relatively low firing rates (e.g. 15 Hz), where the incremental increase in feedback excitation is already diminishing as the firing rate rises.

Synaptic facilitation helps to stabilize the network to noise, because brief fluctuations in activity do not get transmitted through recurrent excitatory synapses — in particular, the resting, spontaneous state of each group is more stable. Whereas the cues of 0.5 or 1 s duration, which cause a response in the network, elicit many action potentials and facilitate the synapses in a group that is driven into the active persistent state. Note that our network is not designed to use the longer time constants of the facilitating synapses as the basis of temporal integration (Shen, 1989).

Stimulus

The stimulus to the network is modeled by fast synaptic excitation mediated by AMPA receptors, with a maximum conductance of 3 nS. The sensory stimulus frequency, s , is expressed in terms of the rate, λ , of the presynaptic Poisson spike train. Here specifically, we used $\lambda = 5s$, with s ranging from 10 to 40 Hz (the flutter range). When the positively monotonic cells receive the lowest stimulus input, the negatively monotonic cells receive the highest, and vice versa. Hence the negatively monotonic cells receive a stimulus of approximately $(50 - s)$ Hz, where s is the vibrational stimulus frequency. Note that for a given cue, the stimulus is of the same strength to all neurons with the same sign of tuning.

In the last section, where we analyze the ability of the network to integrate a stimulus over longer periods of time, we apply the Poisson input to the positively monotonic neurons only.

Experimental Data

The experimental data we compared with our model were taken from extracellular recordings from microelectrodes in the inferior convexity of the prefrontal cortex in

macaque monkeys, as described elsewhere (Romo *et al.*, 1999; Brody *et al.*, 2003). The task was a delayed comparison of vibrational frequency, which required the monkey to remember the ‘flutter’ frequency of an initial vibrotactile stimulus on its finger, during the 3 or 6 s delay period. In this paper, we present some examples of spike trains from single neurons that exhibited persistent stimulusdependent activity throughout the delay.

Data Analysis

Unless otherwise stated, all firing-rate histograms and tuning curves for the simulations were calculated from single neurons separately, averaged over ten simulations with different seeds in the random number generator for external noise. We used a Gaussian smoothing of time window 150 ms before binning spikes to generate the histograms. For model simulations, tuning curves were obtained with an average firing rate of between 3 and 6 s after the offset of the stimulus. The tuning curves for the experimental data contain an average firing rate of between 0.5 and 2.5 s after the offset of the stimulus for a 3 s delay protocol, and between 0.5 and 5.5 s after the end of the stimulus for a 6 s delay protocol. We did not use the initial and final 0.5 s of the delay, because different activity during the stimulus or response could affect the data in these time intervals after smoothing.

Results

Monotonically Tuned Persistent Activity

The neural spiking in our model is compared with that seen during the delay period of the somatosensory delayed-frequency comparison experiment of Romo (Romo *et al.*, 1999; Brody *et al.*, 2003). The experiment consists of an initial somatosensory vibrational stimulus of fixed (0.5 or 1 s) duration followed by a delay period (of 3–6 s), then a second stimulus of identical duration but different frequency to the first. The monkey must indicate which stimulus frequency is the greater, a task which requires memory of the initial stimulus frequency during the delay. The monkey is able to perform the task, and indeed, Romo’s group observed neurons whose firing rates vary monotonically with stimulus frequency, persistently during the delay. Such neurons could subserve the mnemonic function necessary for the task. By careful adjustment of the connectivity strengths between neural groups, our model network reproduces such persistent neural activity. The issue of fine-tuning of parameters will be discussed later.

The tuned model was simulated with a stimulation protocol similar to that used in the experiment. The network is initially in a resting state, where most excitatory neurons fire in the range of 1–8 Hz. A transient (1 s) stimulus is introduced to all the neurons in the network, with an intensity assumed to be proportional to the vibrational frequency in the experiment (see Materials and Methods). Neurons increase their spike discharges in response to the stimulus, which leads to reverberative excitation through recurrent connections. This intrinsic synaptic excitation is able to sustain persistent activity after the stimulus offset. Our network is in two halves, each half corresponding to neurons that receive either positively monotonic or negatively monotonic input from S2. S2 contains such oppositely tuned cells, which do not show persistent activity (Salinas *et al.*, 2000).

Figure 2 shows the activities of two representative neurons. In Figure 2a, a single neuron shows delay period activity that monotonically increases with the stimulus frequency. This neuron belongs to the first half of our network model which receives a stronger input with a higher stimulus frequency. The larger transient neural responses recruit more recurrent excitation which can sustain persistent activity at a higher rate. In contrast, the neuron in Figure 2b shows a monotonically decreasing tuning of its mnemonic activity. This neuron belongs to the second half of our network model, which receives less inputs with a higher stimulus frequency, hence the recruited recurrent excitation as well as the resulting persistent activity is lower.

Our model simulations (Fig. 2) can be compared with the experimentally observed neural activity in the prefrontal cortex during the vibrotactile experiment (Fig. 3). The model neurons fire most strongly during the transient response to stimulus, then settle to a persistent rate which is monotonically dependent on the stimulus frequency (middle panels). The tuning curves (lower panels) are clearly monotonic and demonstrate parametric working memory. The average firing rates of neurons in the interval between 2 and 5 s after the end of the stimulus exhibit a quasi-linear or sigmoidal dependence on stimulus frequency.

Different neural groups have different activation thresholds, and show persistent activity at different rates for a given stimulus. This is similar to the models of Seung *et al.* (2000a) and Koulakov *et al.* (2002). In these cases, neurons have different intrinsic input thresholds for spike discharges. In the present model, the synaptic connections are asymmetrical (Fig. 1; see Materials and Methods). As a result, neural groups receive progressively more overall recurrent excitation from left to right across the network. This way, neural group 1 has the lowest threshold and group 12 has the highest threshold, when driven by external inputs. This range of excitability allows the network to have a range of responses to varying stimuli. Because the tuning is monotonic, the stimulus frequency is encoded and stored in memory not by what neurons fire significantly, but at what rates all neurons fire. Because of background noise, and because the network is sensitive to parameter tuning (see below), even the averaged population firing rate of an individual neural column shows significant temporal fluctuations. The memory of the stimulus is better maintained by persistent activity pooled across the entire network of all neural groups.

The experimentally observed tuning curves of prefrontal neurons are very diverse; some are linearly tuned with the vibration frequency, others show sigmoid-shaped tuning (Fig. 4A). Our model reproduces to a large degree this diversity of tuning curves of single neurons (Fig. 4B). Our model has four types of neurons, both positively and negatively monotonic types of pyramidal cells and interneurons. The interneurons have different intrinsic properties (see Supplementary Material), as they are designed to be fast-spiking and generally have a higher firing rate than pyramidal cells. We found that the tuning curves of interneurons are more linear than those of pyramidal cells. This can be explained by the fact that interneurons receive broad excitation from the pyramidal cells; averaging over a few hard sigmoid functions yields a more linear function.

Robustness to Heterogeneity

A key issue in evaluating the biological feasibility of our network is a determination of its robustness to variations of the parameters. The key parameters that we tuned were the connection strengths. To assess the effects of mis-tuning, we multiplied the synaptic strengths $W_{i \rightarrow j}$ by $(1 + \eta_g^{i \rightarrow j})(1 + \eta_n^{i \rightarrow j})$ where $\eta_g^{i \rightarrow j}$ is sampled for each group of neurons, drawn from a Gaussian distribution with standard deviation σ_g , while $\eta_n^{i \rightarrow j}$ is sampled separately for each neuron, drawn from a Gaussian of standard deviation σ_n . The leak conductances also varied, with a standard deviation of 1.2 nS (i.e. $\pm 3\%$).

We found that the more deleterious way to mis-tune is to scale up or down all the connection strengths for a particular neural group ($\sigma_g > 0$). We find that 5% population heterogeneity causes a clear drift in firing rates to a few stable persistent states. The network loses its ability to discriminate many different inputs, and a large gap in firing rates (typically up to 15–20 Hz) opens up for some neurons when the stimulus is strong enough to propel the network from one discrete stable state to another. The time constant for drift is still long (2–3 s), but that is diminished enough to limit the network's ability to distinguish >3 or 4 stimulus strengths after 6 s. A less damaging variation is to scale up or down all connections to individual neurons separately and randomly ($\sigma_g = 0$ and $\sigma_n > 0$). Indeed, the mnemonic ability of the network is maintained with a 10% variation in synaptic strengths for each individual neuron, while the heterogeneity in the inter-group connection strength is $\pm 1\%$. The firing rates after different stimuli remain separate throughout the delay period of 6 s and neuronal responses are qualitatively indistinguishable from those presented in Figures 2 and 4. Such heterogeneity within a population does lead to a greater variety of tuning curves, as, unlike the homogeneous case, heterogeneity allows tuning curves to be different for each of the 100 inhibitory or 400 excitatory cells within a population.

Such stability to heterogeneity within a population may not be a surprise. Assuming that neurons are uncorrelated or weakly correlated, heterogeneities of single neurons can be averaged out across a large neural population. Indeed, a 10% variation of individual neuronal properties results in only an $\sim 0.5\%$ variation in the average properties of 400 neurons. However, our results do indicate that with the large numbers of neurons available in the cortex, tuning of single neuronal parameters no longer needs to be extremely precise.

Mean-field Analysis of Model Networks

To elucidate the precise requirements for parametric working memory behavior, we carried out mathematical analysis of the mean-field approximation of our biophysically based spiking model. The mean-field approach (Amit and Brunel, 1997; Hansel and Sompolinsky, 1998; Brunel, 2001; Brunel and Wang, 2001; Renart *et al.*, 2003b) is to replace quantities such as synaptic conductances by their averages, ignoring their fluctuations due to individual spikes. The mean-field approximation is useful, as it allows us to describe a whole population of spiking neurons with their average activity. Hence, we can rapidly solve for the stable states of the system, and observe how those states change as a function of parameters like the connection strengths, or intrinsic excitability. A detailed account of the mean field equations can be found in the Supplementary Material. We found that the mean-field calculations are confirmed qualitatively by simulations of the original spiking model,

but an adjustment of parameters is necessary to match precisely the behaviors of the two models quantitatively.

To help understand the results of our mean-field analysis, let us first consider schematically one neural group with recurrent excitation. When the recurrent strength $W_{E \rightarrow E}$ is above a critical value, a bistability between the resting spontaneous state and an active persistent state is produced by strong recurrent excitation. The bistability persists over a range of applied excitation, determined by the excitatory synaptic drive conductance, g_{App} , to the neurons. This is illustrated schematically in Figure 5, where the network behavior is shown on the plane of the two parameters $W_{E \rightarrow E}$ and g_{App} . While $W_{E \rightarrow E}$ is a measure of the recurrent excitation, multiplying feedback from within the neural group, g_{App} is a constant excitatory drive, which would arise, for example, from other neural groups. A change in intrinsic parameters which alters the firing thresholds of neurons, will shift the whole diagram along the axis of g_{App} . In particular, the larger the leak conductance, g_L , the larger the required drive, g_{App} , to achieve firing threshold and bistability.

With $W_{E \rightarrow E}$ far above the critical value (point A on the left panel of Fig. 5), the bistability range of g_{App} is wide and the behavior is robust. However, there is a large gap in the firing rates between the active and resting states (right panel of Fig. 5). In order to realize a quasi-continuum of firing rates, $W_{E \rightarrow E}$ should be as close to the critical value as possible (the point B, which is called a ‘cusp’ in the theory of dynamical systems). However, in this case the value of g_{App} must be precisely tuned (Seung *et al.*, 2000b). Moreover, for a single neural group, the quasicontinuous range of firing rates is actually quite small (a few Hertz), largely determined by the properties of a single neuron’s input–output relation (Brunel, 2001). The range of response should be increased for two reasons. First, a wider range allows a wider range of stimulus strengths to be encoded by the network. Secondly, if neurons encode the stimulus over a large range of firing rates, the sensitivity of the network is increased, as different stimuli cause larger changes in firing rates that are more easily decoded. The limited range can be increased by utilizing a large number of interconnected neural groups with different thresholds. The recruitment of each new neural group increases the excitatory drive to, hence activity of, those already active neural groups, leading to a much larger quasi-continuous range of persistent firing rates.

The mean-field analysis of our complete two-network model demonstrates a large number of stable states over a very narrow range of synaptic drive (Fig. 6). Our model network has as many cusps as the number of excitatory neural groups, and tuning the whole network to a continuous attractor requires an alignment of cusps so that the system can be tuned to all of them at once. The ideal vertical line of Figure 5 becomes wavy on a fine scale when many neural groups are combined to make a continuum. It is the nearness of the system to many cusps that allows the stable states to be close together, and results in a long time constant for drift following any stimulus. If connections within the system are varied randomly, the cusps are no longer aligned, but as there are a large number of cusps, the system will still be near a few of them and typically have more than one stable state. Hence, random mis-tuning does not cause a severe detriment to the network properties. However, a global mis-tuning (such as a global scaling of all synapses) will result in drifts of firing rates as described in previous work (Seung *et al.*, 2000a,b).

Time Integration

A line attractor network converts a transient input into a persistent output which is proportional to the input amplitude, so in that sense it performs an integration of the input. However, if the computation is truly mathematical integration, neurons should also be able to integrate over time, i.e. the firing rate of persistent activity should reflect the time duration of an input stimulus. To assess the temporal properties of integration by our network, we carried out a series of trials where the strength and frequency of the stimulus were fixed but the duration of the stimulus changed.

The results presented in Figure 7 show that the network can integrate an input slowly in time, over many s (Fig. 7A). Equivalent slow integration is observed in the mean-field network described in the previous section. Such a slow time course of integration is remarkable given that the longest biophysical time constant of the model is 100 ms. Once the stimulus ends, the network maintains a level of activity that is monotonically dependent on the stimulus duration (Fig. 7B). Optimal time integration occurs provided that the input strength is not too small (below a critical threshold) or too large (beyond which saturation occurs).

The threshold and saturation effects imply that the integration is not 'pure' in the sense that if average firing rates are plotted as a function of the product of stimulus frequency and duration, they do not fall on a universal curve. A doubling of the stimulus duration with a halving of the frequency, in general produces a smaller response. Experimental tests of the temporal scaling properties of integration in both the oculomotor system and working memory system would be illuminating.

Ramping Neurons

Finally, we investigated the issue of diversity of neural responses observed in the somatosensory discrimination experiment. During the delay period, persistent activity of many prefrontal-cortical neurons is not tonic, but evolves slowly over time. Some neurons tune to the stimulus early in the delay, others late in the delay. Moreover, average rates of some neurons ramp down or ramp up. The two types of temporal dependence are correlated with each other, but are not identical. Here, we investigate the two subtypes of neurons, which do not necessarily show any stimulus dependence, but whose average rates ramp up or ramp down during the delay. These are only two kinds of time dependence, out of a greater variety reported by Brody *et al.* (2003).

To generate such neurons, we extended our model to include three sets of neurons (each having 12 neural groups), each structured like the positively monotonic half of our previous network (Fig. 8A, upper right). The first neural population shows tonic persistent activity during the delay, as in our original model, but at a saturated rate that is independent of stimulus strength (Fig. 8A, upper left). It is assumed that the first neural population sends excitatory projections to the second population which integrates the inputs slowly in time, as in the previous subsection. Consequently, the second neural population shows slow ramp-up spike discharges during the delay period (Fig. 8A, lower right). Furthermore, the second and third neural populations are reciprocally connected by inhibition (Constantinidis *et al.*,

2002). The transient stimulus activates the third neural population and, as the second neural population ramps up over a few s, the third population is progressively inhibited; therefore its activity ramps down during the delay (Fig. 8A, lower left). Similarly, the initial activity of the third population delays the ramping up of the second population in a closely matched tug-of-war that is resolved by the extra tonic input from the first to the second population. Note that these ramping behaviors occur during the delay, while there is no applied stimulus.

Experimentally it was found that the rate of evolution of time-dependent neurons is plastic. For example, when the delay duration is doubled from one block of trials to another (say, from 3 s to 6 s), the ramping slope of delay activity is roughly reduced by a factor of 2, so that a ramping neuron reaches the same final activity level at the end of the delay (Brody *et al.*, 2003). Our model (Fig. 8A, upper right) suggests a synaptic mechanism for such plasticity. Since ramping neurons integrate inputs from the tonic neural population, the ramp slope depends on the strength of synapses between the two neural populations. Indeed, when this synaptic conductance is reduced by one-third (from g_1 to $2g_1/3$) the time course of a ramping neuron is delayed and slowed (Fig. 8B, left panel). However, if the timescale is compressed by a factor of two, the ramping time course becomes superposable with that in the control case (Fig. 8B, right panel), similar to the experimental observations (Brody *et al.*, 2003).

Discussion

In this paper we presented a large-scale cortical network model (with 12 000 neurons) for parametric working memory. The main results are threefold. First, our model reproduces the salient neural activity data from monkey prefrontal cortex in a somatosensory delayed discrimination experiment (Romo *et al.*, 1999; Brody *et al.*, 2003). A model with two inhibitorily coupled networks reproduces positively and negatively monotonic neurons, and a diversity of tuning curves of memory activity. Secondly, we show that there is a trade-off between robust network behavior with large jumps in the tuning curves, and fine-tuned network behavior with a quasi-continuum of attractor states. The fine-tuning of our model is mathematically identified to be a precise alignment of cusps in the bifurcation diagram of the network. This is also true for the model of Seung *et al.* (2000a) (data not shown). Thirdly, we show that the finely tuned network can integrate stimulus inputs over many s, even though single neurons and synapses operate at timescales of 10–100 ms. Assuming that such time integration occurs in downstream neural populations that receive inputs from a tonically persistent neural population, our model is able to reproduce the ramping-up and and ramping-down behaviors of some time-dependent neurons observed in the prefrontal cortex (Romo *et al.*, 1999; Brody *et al.*, 2003).

The key to the ability of a neural network to encode monotonically and remember a continuous quantity, and integrate inputs in the mathematical sense, is to achieve an effective time constant of many seconds. At least three biological implementations of such integration are conceivable.

First, single neurons and synapses may possess mechanisms with very long intrinsic time constants, such as synaptic facilitation (Shen, 1989) or intracellular calcium release from

stores (Loewenstein and Sompolinsky, 2002). Alternatively, a single neuron could tune positive internal feedback (from calcium channels) to generate a longer cellular time constant from its faster intrinsic mechanisms (Durstewitz, 2003). Recently, Egorov *et al.* (2002) reported experimental evidence for a slow (seconds) integration process in single neurons of the rat layer V entorhinal cortex. The underlying mechanisms remain to be elucidated.

Secondly, a network may contain a number of bistable and independently switchable neural groups (Koulakov *et al.*, 2002). The continuous variable can then be encoded by the number of neural groups that are switched on; and such a digital code can be close to a continuous representation if the number of neural groups is large. However, this scenario predicts significant gaps in the tuning curves of memory neurons, due to the jumps between the resting state and active persistent states, that are not seen in neural data from working memory experiments. It remains to be seen whether gaps in the firing rate could be rendered insignificant with biophysically realistic mechanisms.

Thirdly, a network can be tuned judiciously toward a continuum of attractor states (Seung, 1996; Seung *et al.*, 2000a). Our simulations show that a finely tuned model compares favorably with the experimental data, without large gaps in the tuning curves of mnemonic neural activity. The inherent problem of a trade-off between robustness to noise and heterogeneity versus a continuum of stable states is ameliorated by the cross-inhibition between positively and negatively monotonic groups, as well as the large number of neurons in the system. In our network there are a total of 24 excitatory neural groups, each with strong recurrent feedback adjusted to be at the ‘cusp’ to produce a continuous attractor over a small range of inputs (Figs 5 and 6). With 24 continuous attractors available, the whole network is able to be in the vicinity of several of them robustly. Near the attractor states the effective time constant of the network is much longer than the intrinsic cellular or synaptic time constants (Seung *et al.*, 2000b).

In the brain, fine-tuning of a recurrent network is likely to be accomplished by some activity-dependent homeostatic mechanisms (Marder, 1998; Turrigiano *et al.*, 1998; Turrigiano, 1999; Turrigiano and Nelson, 2000; Renart *et al.*, 2003a). For example, consider a neural group with excitatory feedback (shown in Fig. 5). Assuming that regulatory processes (operating at timescale of days) stabilize the long-term firing rate of neurons at ~8–15 Hz (the ‘goal’ or ‘target’ rate), then the network will be naturally tuned to the narrow parameter region near the cusp (with continuous attractor states). Figure 6 emphasizes that for the tuned system shown, the average firing rate can only be in the range of 8–15 Hz if the conductance offset, g_{App} (in this case zero) exactly matches the position of the vertical line. Hence a coarse monitoring of average firing rate (Turrigiano, 1999; Turrigiano and Nelson, 2000) could lead to a very fine tuning of neuronal parameters.

Such a homeostatic mechanism would combat and compensate any mis-tuning of cellular or synaptic parameters, so that the network would be stabilized near the cusp in spite of parameter mis-tuning. Theoretical work suggests that such a homeostatic mechanism works effectively in a continuous attractor model for spatial working memory (Renart *et al.*,

2003a). It would be interesting to see whether the same kind of ideas can be applied to parametric working memory models.

It can be noted from Figure 5 that tuning a system to a cusp requires adjustment of two parameters. Durstewitz (2003) has suggested that as well as mean firing rate, a cell could monitor its variance in activity as a second parameter to tune. Noting that the variance is typically maximal at a line attractor, where fluctuations are not damped, Durstewitz suggests that a neuron can utilize such information. Further experimental work will be very useful to demonstrate the feasibility of such cellular tuning processes.

With appropriate network connectivity (Fig. 8) our model can reproduce cells which have a delay from the end of the stimulus until they begin to ramp up. Moreover, the length of delay and rate of ramping-up can be scaled in time by modification of synaptic strengths. Other mechanisms could produce delays, such as utilizing slow currents within neurons, but there are no known mechanisms whereby such intrinsic currents could change their time constants. Durstewitz (2003) has suggested a similar synaptic learning mechanism, but where the strength of input from other cells affects a neuron's intrinsic ramping rate. Experimentally, whether a change in the duration of the delay does give rise to the kind of synaptic modification suggested by our model is not known and remains to be studied in the future.

As well as a time variation of average firing rates, neurons in the prefrontal cortex can also exhibit a time variation in their tuning to the stimulus. The two behaviors are correlated, because when the average firing rate is very low, there is typically little stimulus dependence, as a strong stimulus dependence would cause a range of firing rates across stimuli, resulting in an average firing rate that differs significantly from the spontaneous rate. However, during the delay some neurons can maintain a near constant, typically high average firing rate, while the spread of firing rates is large only early or late in the delay. We speculate that a strategy similar to the one we outlined above could generate many of these other types of time-dependent behavior observed experimentally.

To conclude, we would like to emphasize that, at present, it remains unproven that the continuous attractor paradigm is a necessary and accurate description of spatial or parametric working memory circuits. Because of experimental constraints, typically only a relatively small number (<10) of stimuli are used in working memory experiments, such as the oculomotor response task (Funahashi *et al.*, 1989) or the somatosensory discrimination task (Romo *et al.*, 1999). Moreover, even if a large number of discrete stimuli are sampled, animals tend to categorize these values when possible, and avoid the difficult task of memorizing a continuous quantity (Hernandez *et al.*, 1997). Hence, further experiments are desirable to rigorously test whether the internal representation of an analog stimulus in working memory is truly continuous.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

Acknowledgments

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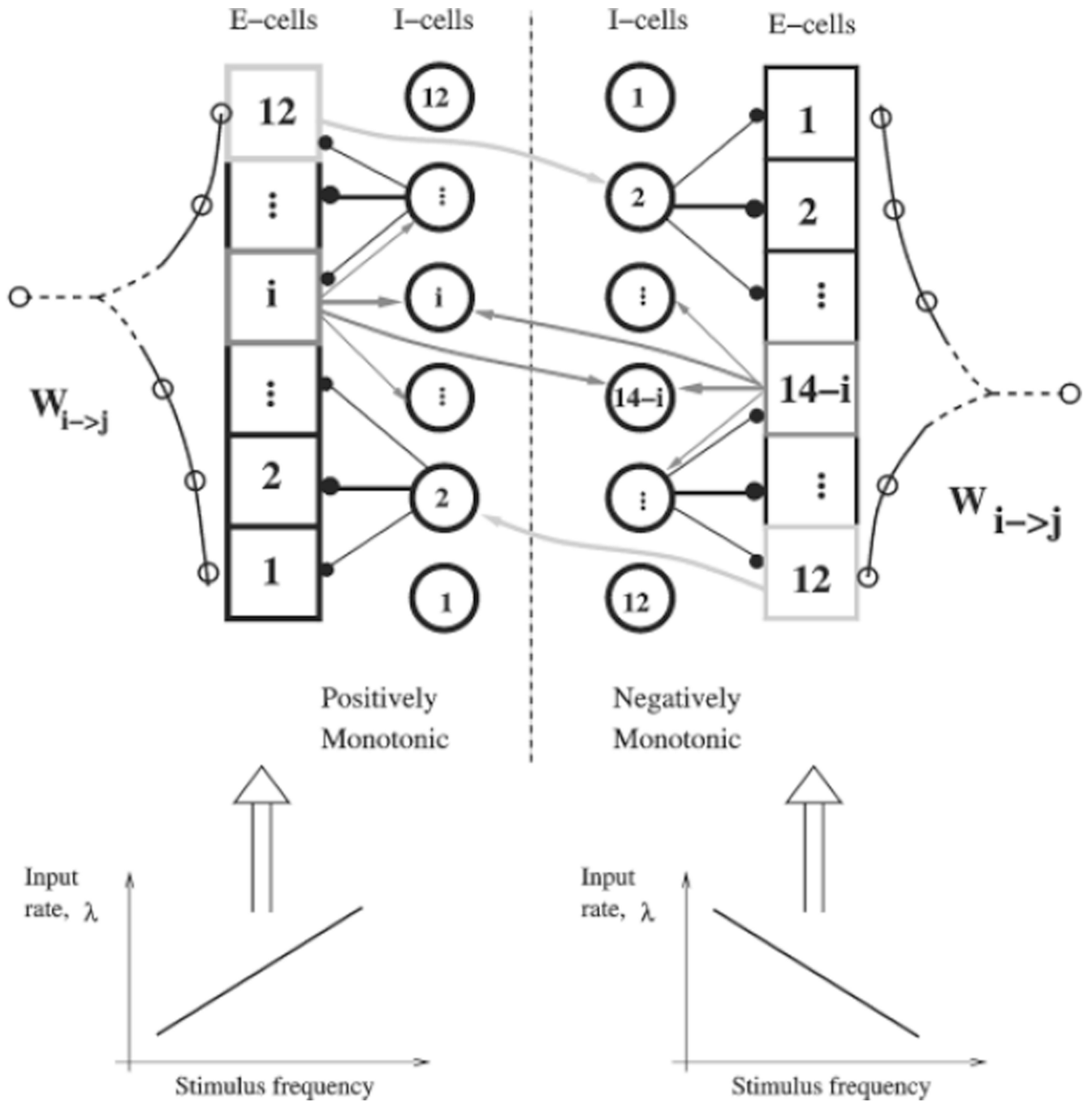


Figure 1. Schematic model architecture with asymmetric connectivity. Two mirror networks of positively and negatively monotonic neurons receive transient input respectively from positively and negatively tuned neurons in S2. Each network has an excitatory pyramidal cell population (squares) and an inhibitory interneuron population (circles). Neurons are divided into 12 groups per network. Synaptic connections are stronger within the same group than between two groups. The connectivity is asymmetrical, so that the activation threshold by stimulus is the lowest for neural group 1 and highest for neural group 12.

Populations of inhibitory interneurons are shown as circles. The two networks interact through pyramid-to-interneuron connections, resulting in cross-inhibition. See text for more details.

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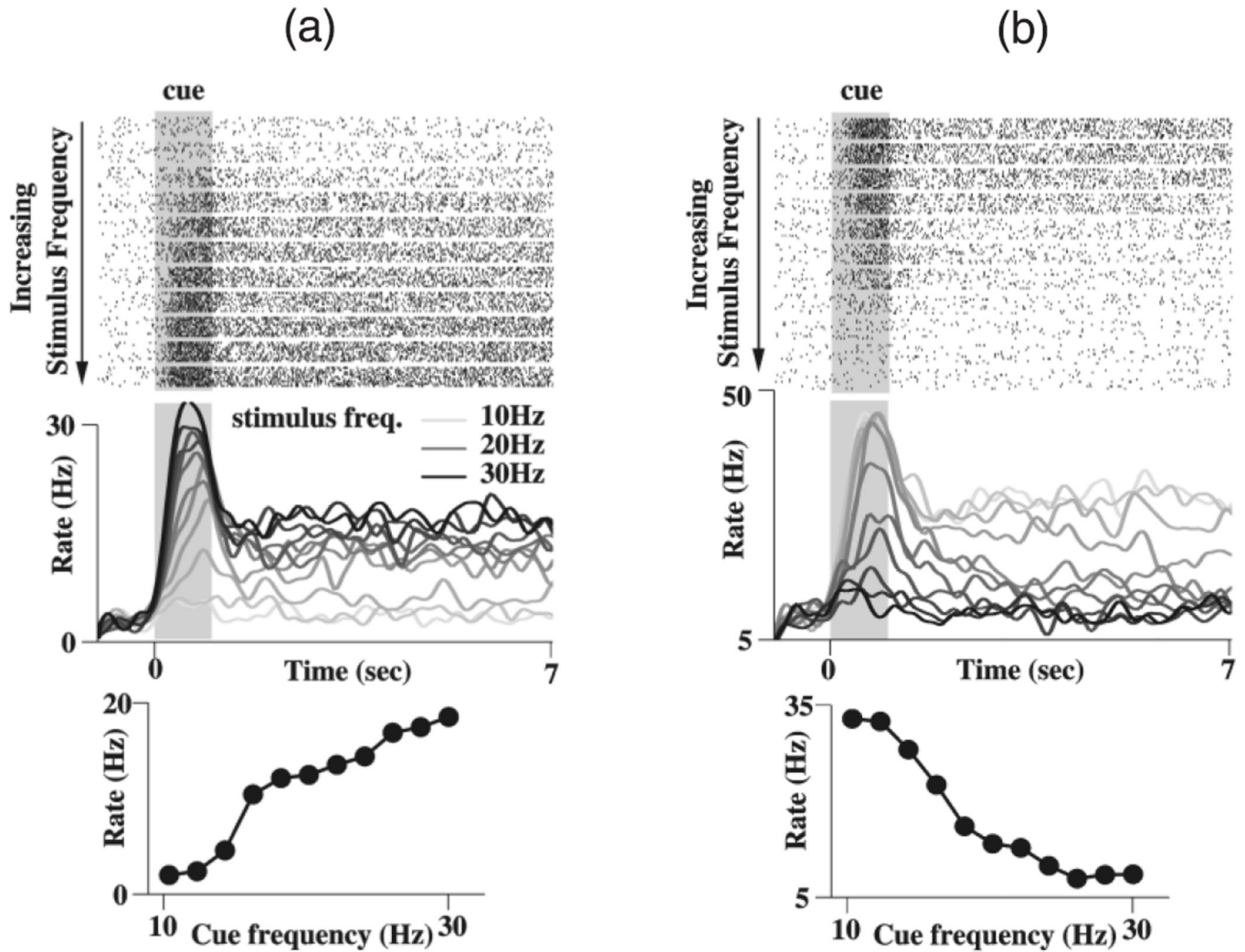


Figure 2. Persistent neural activity of the parametric working memory model. (a) A positively monotonic, excitatory cell. Top panel: rastergrams, showing spikes in blocks of 10 trials, each block corresponding to a fixed stimulus frequency. The cell initially fires spikes at a few Hertz spontaneously. A transient stimulus (shaded) produces a large response, followed by persistent activity after the stimulus offset. The firing rate of both the transient response and persistent activity increases with the stimulus frequency. Middle panel: trial-averaged neural firing rate, where darker shades of gray represent increasing stimulus frequency. Bottom panel: the tuning curve shows the average rate in the last 5s of the delay period following each stimulus. (b) A negatively monotonic inhibitory interneuron, same plots as (a).

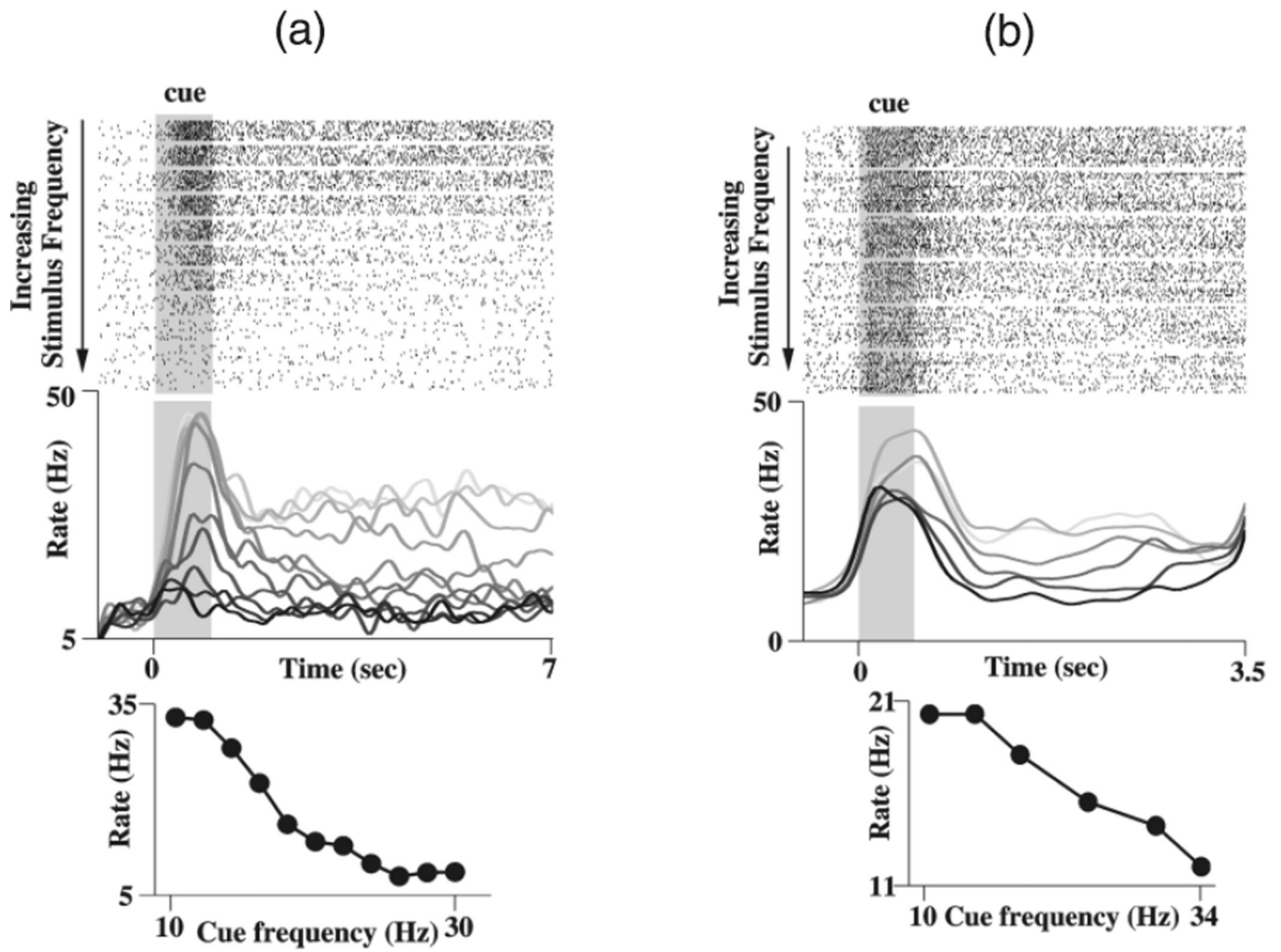


Figure 3. Sustained delay activity of prefrontal cortical neurons recorded from macaque monkeys during parametric working memory. (a) A positively monotonic neuron. (b) A negatively monotonic neuron. Same format as Figure 2

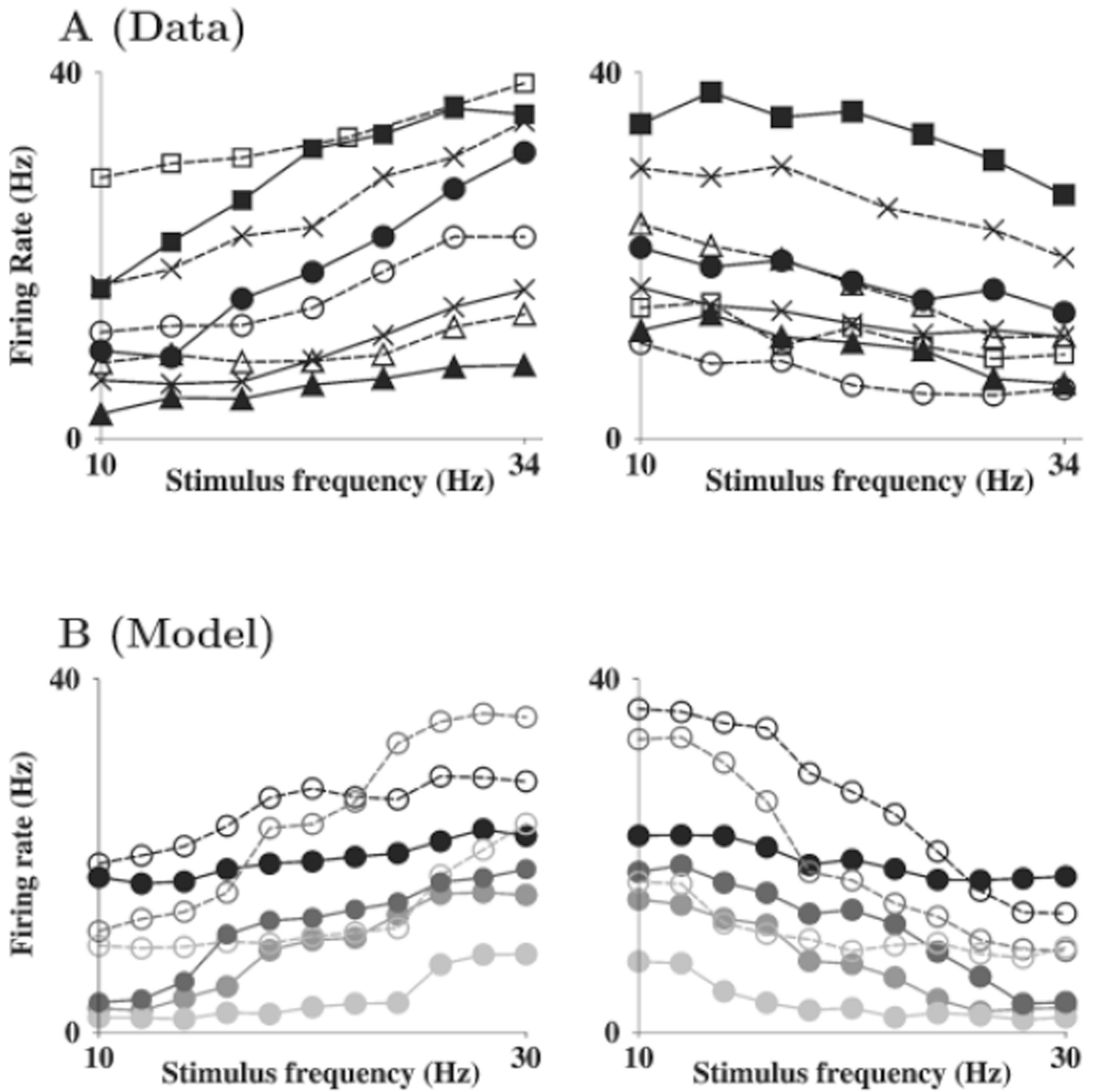


Figure 4. Diversity of tuning curves of persistent neural activity in prefrontal neurons and our model. (A) Examples of positively monotonic (left) and negatively monotonic (right) tuning curves from the experimental database. (B) Examples chosen to indicate the full variety of tuning curves from model simulations. Note the quasi-continuous nature of the curves, with small rate jumps. Filled circles: excitatory cells; open circles: interneurons.

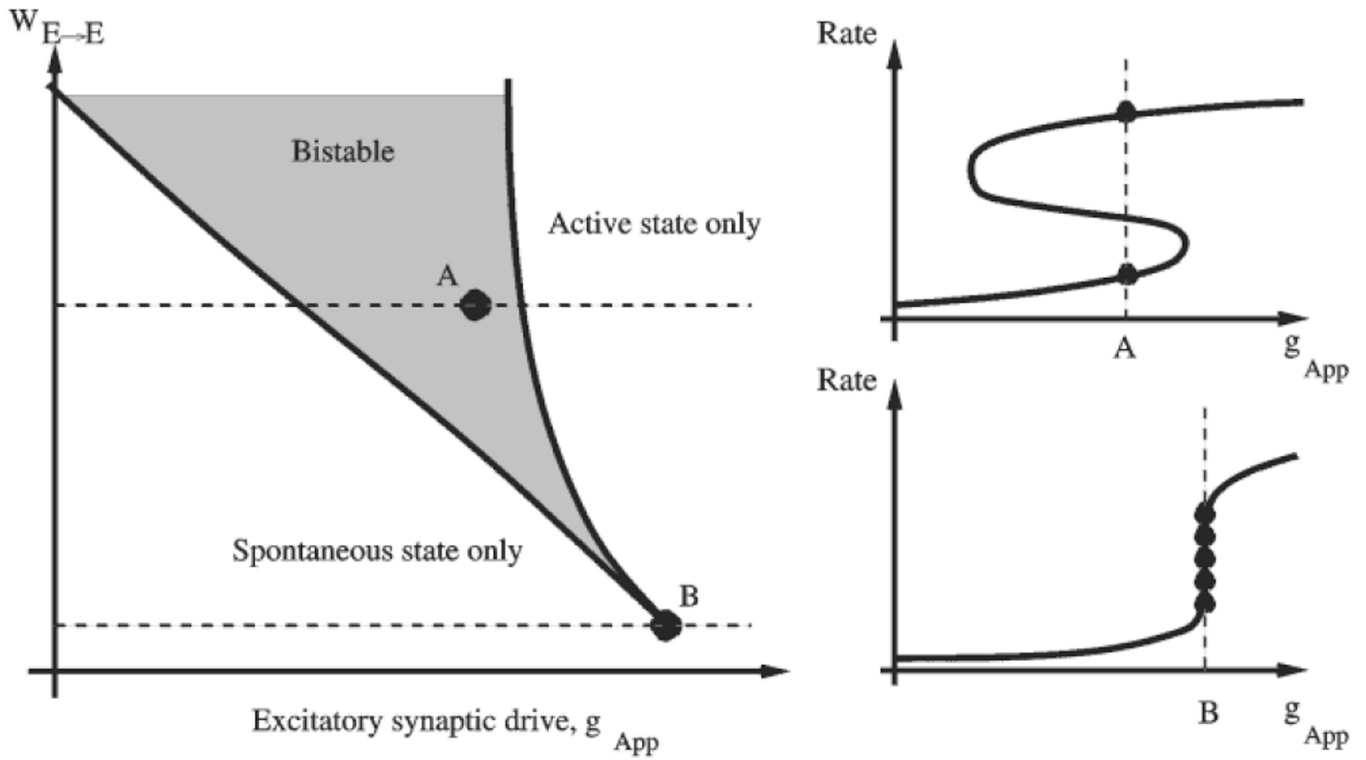


Figure 5.

Fine-tuning of parametric working memory model. Schematic illustration of a neural group with recurrent excitation. Left panel: network behavior as a function of the recurrent strength $W_{E \rightarrow E}$ and applied excitatory input, g_{App} . When $W_{E \rightarrow E}$ is above a critical value (e.g. point A), a bistability between a resting state and an active persistent state occurs in a range of g_{App} . This range shrinks to zero at the critical value of $W_{E \rightarrow E}$, point B, which is called a ‘cusp’. Right panel: there is a trade-off between robust bistability but with a large gap in the firing rates of the two stable states (upper figure) and fine-tuning to the cusp where there can be a continuous range of firing rates (lower figure).

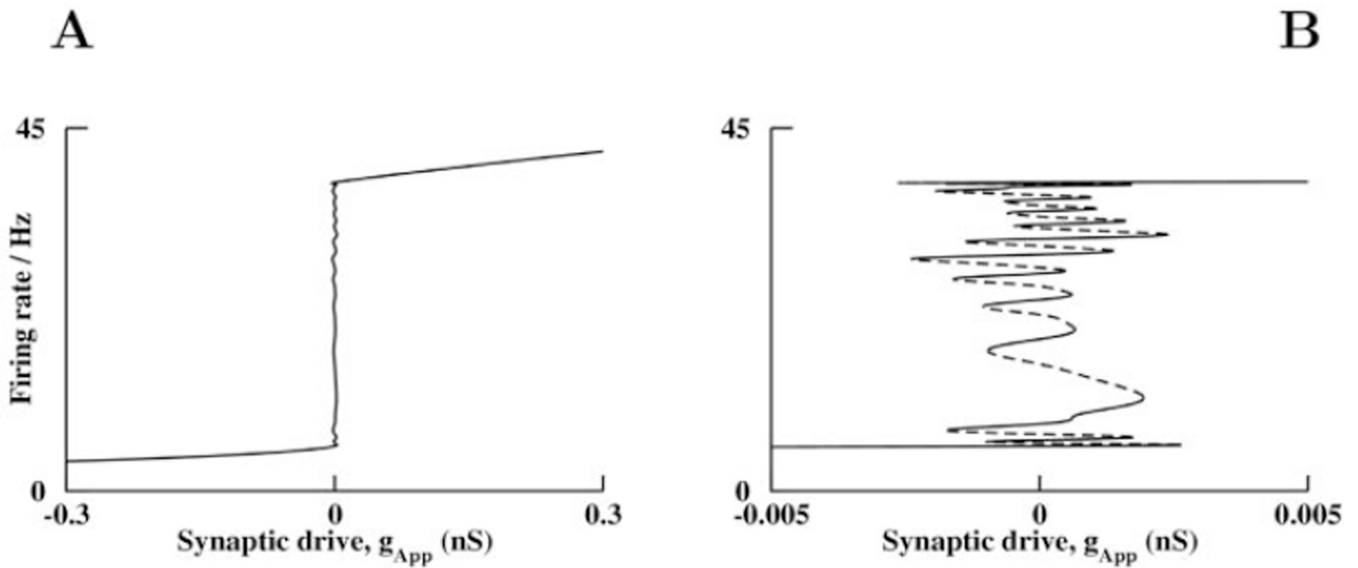


Figure 6.

Bifurcation diagram of the finely tuned parametric working memory model, as a function of applied synaptic drive conductance, g_{App} . Synaptic drive is an offset conductance for demonstration purposes, that we add to the positively monotonic neurons and subtract from the excitatory input to negatively monotonic neurons. A negative drive means the positively monotonic neurons have reduced synaptic excitation. A shift in any intrinsic neuronal parameter has a similar effect on the system. All the stable states are computed using the mean field theory for the entire network of twelve positively monotonic and twelve negatively monotonic, excitatory and inhibitory, neural groups. These persistent states are plotted as the firing rates of cells in neural group 3. (A) A quasi-continuum of stable firing rates is possible with correct tuning of applied synaptic drive. (B) An enlargement of the region near the quasi-continuous attractor indicates a discrete number of stable persistent states close to the number of neural groups, with small changes in firing rate between states. Portions of the curve with negative slopes are the branches of unstable states (dashed lines).

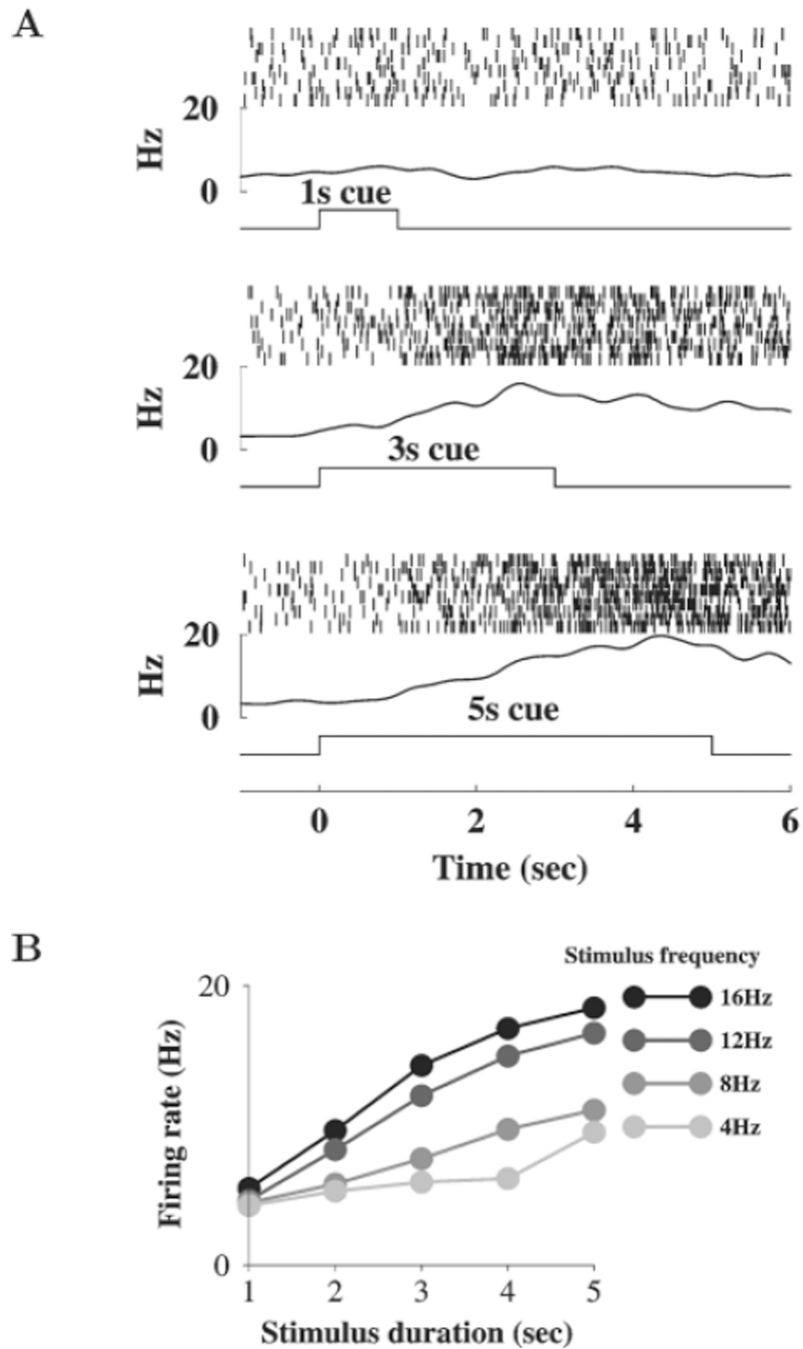


Figure 7.

Time integration of a stimulus with different duration and amplitude. (A) The network can integrate a stimulus over a long time (1, 3 and 5 s), as shown by the rastergrams and population firing rates. (B) The firing rate of persistent activity (averaged between 3 and 6 s after the stimulus offset) is plotted as a function of stimulus duration, different curves correspond to different stimulus frequencies (4, 8, 12 and 16 Hz, with increasingly darker shades of gray). Note that linear dependence on the time duration of the stimulus occurs for moderate input strengths.

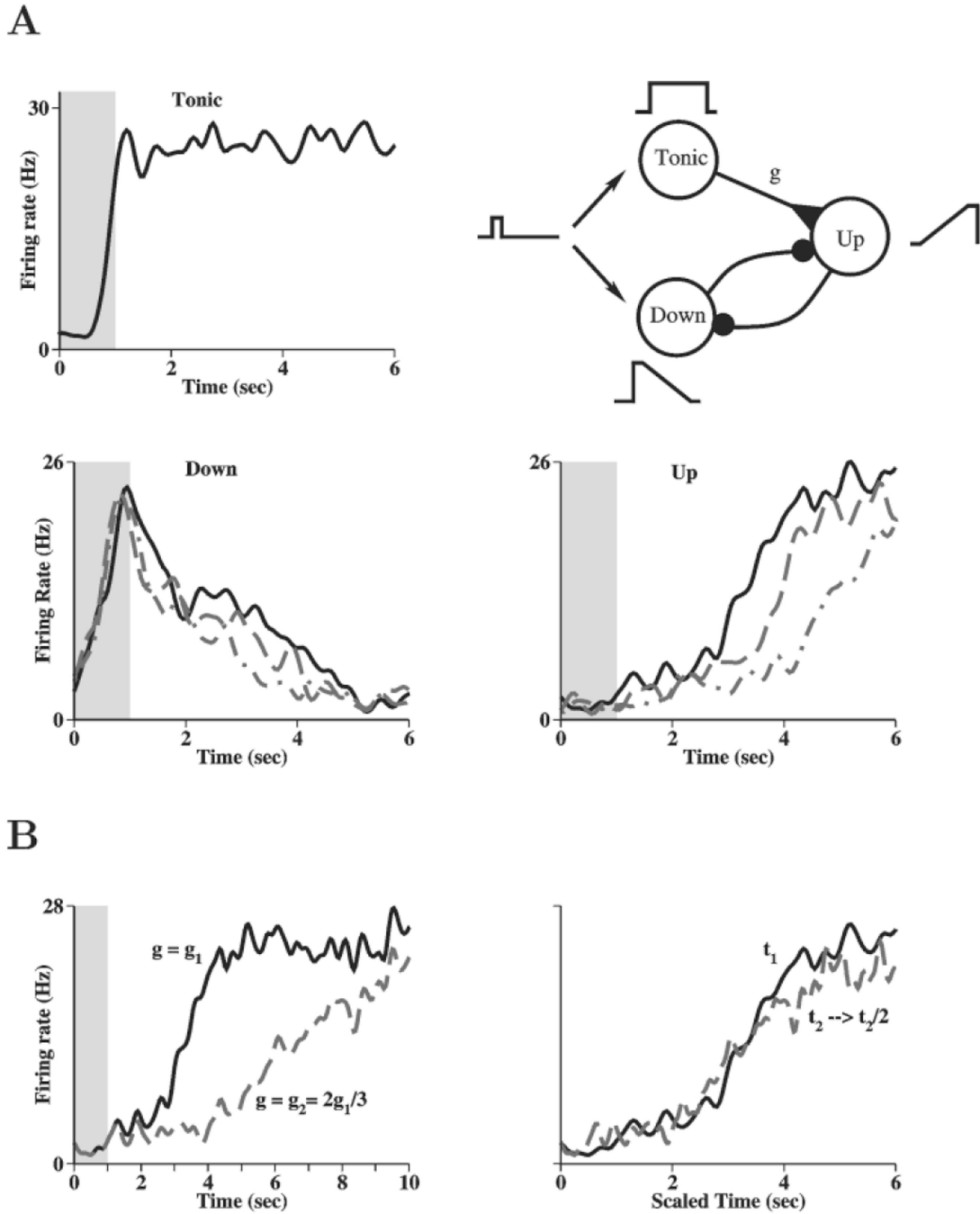


Figure 8. Diversity of delay period activity: tonic, early and late neurons. (A) Schematic diagram of an extended model with three neural populations (all are positively monotonic with the stimulus frequency). The first network (Tonic) shows tonic persistent activity and projects with strength g to a second network (Up), which integrates the inputs slowly to generate ramping-up activity during the delay. The third network (Down) displays a transient activation by the stimulus, and ramping-down time course of delay period activity due to the progressive inhibition from population 2. The trial-averaged firing rates for three different

cells from each type of network are shown for 5 s following the stimulus frequency. (*B*) Neurons in population 2 ramp-up with a slope and a delay that depend on the input synaptic strength. Left panel: control (black, solid), and when the synaptic strength, g , from the tonic population 1 is reduced by one-third (gray, dashed). Right panel: when the time is scaled by half for the gray, dashed curve, the two time courses closely resemble each other.