

Determining hydrodynamic forces in bursting bubbles using DNA nanotube mechanics

Rizal F. Hariadi^a, Erik Winfree^b, and Bernard Yurke^{c,1}

^aApplied Physics, California Institute of Technology, Pasadena, CA 91125; ^bBioengineering, California Institute of Technology, Pasadena, CA 91125; and ^cDepartment of Materials Science and Engineering, Boise State University, Boise, ID 83725

Edited by Eric D. Siggia, The Rockefeller University, New York, NY, and approved September 4, 2015 (received for review December 24, 2014)

Quantifying the mechanical forces produced by fluid flows within the ocean is critical to understanding the ocean's environmental phenomena. Such forces may have been instrumental in the origin of life by driving a primitive form of self-replication through fragmentation. Among the intense sources of hydrodynamic shear encountered in the ocean are breaking waves and the bursting bubbles produced by such waves. On a microscopic scale, one expects the surface-tension-driven flows produced during bubble rupture to exhibit particularly high velocity gradients due to the small size scales and masses involved. However, little work has examined the strength of shear flow rates in commonly encountered ocean conditions. By using DNA nanotubes as a novel fluid flow sensor, we investigate the elongational rates generated in bursting films within aqueous bubble foams using both laboratory buffer and ocean water. To characterize the elongational rate distribution associated with a bursting bubble, we introduce the concept of a fragmentation volume and measure its form as a function of elongational flow rate. We find that substantial volumes experience surprisingly large flow rates: during the bursting of a bubble having an air volume of 10 mm³, elongational rates at least as large as $\dot{\epsilon} = 1.0 \times 10^8 \text{ s}^{-1}$ are generated in a fragmentation volume of $\sim 2 \times 10^{-6} \text{ }\mu\text{L}$. The determination of the elongational strain rate distribution is essential for assessing how effectively fluid motion within bursting bubbles at the ocean surface can shear microscopic particles and microorganisms, and could have driven the self-replication of a protobiont.

DNA nanotechnology | polymer dynamics | hydrodynamics

Functioning like a giant heat engine between the high-temperature heat bath of the sun and the low-temperature heat bath of outer space, the earth's atmosphere generates wind and rain with intense fluid flows. The mechanical stresses produced by these hydrodynamic flows are among the environmental stresses that biological organisms must cope with. Organisms often exploit these stresses and fluid flows, most notably to aid reproduction. A well-known example at the macroscopic scale is the wind dispersal of spores, seeds, and pollen. Less well-known, fragmentation resulting from fluid-flow-induced stress is used by a number of marine organisms as a means of vegetative reproduction, such as macrophyte algae (1) and sponge and coral colony (2, 3) propagation by storm-induced fragmentation. Can analogous mechanical forces facilitate vegetative reproduction at the micro-scale? Current evidence is at best indirect: Filamentous cyanobacteria are known to fragment under environmental stress (4, 5), suggesting that prokaryotes may use fluid-flow-induced fragmentation as a means of clonal reproduction and dispersal as well.

Several origin-of-life hypotheses invoke processes in which environmentally produced microscale mechanical forces drive self-replication through fragmentation. Oparin proposed that fragmentation of coacervates may have constituted a primitive form of self-replication allowing for Darwinian evolution by natural selection (6). More concretely, Cairns-Smith proposed that life arose from mineral crystals that replicated by fragmentation into new seed crystals, thereby propagating genetic information consisting of the patterns of defects within the mother crystal (7–9).

Szostak's group also proposed that division of protocells (having a lipid bilayer) can be driven by fluid flow (10–12). Inspired by Cairns-Smith's proposal, Schulman, Yurke, and Winfree used DNA tile self-assembly to construct a self-replicating system in which fragmentation was induced by intense elongational flow at a constriction in a flow channel (13). This synthetic system is analogous to an in vitro system in which exponential growth of prions is driven via fragmentation by mechanical shearing of amyloid fibrils (14). Similarities between regeneration (self-healing) and asexual reproduction in modern organisms have led some to postulate fragmentation-and-regeneration as a primordial form of reproduction (15).

To effectively shear microscopic objects such as bacteria or protobionts, fluid flows must exhibit high-velocity gradients over the length scale of the object. Such small-scale high-velocity-gradient flows occur naturally in breaking ocean waves that produce whitecaps (16). Within these waves, the highest velocity gradients are expected to occur in the films of bursting bubbles due to the rapid acceleration produced by surface tension forces acting on the small fluid mass. Moreover, bursting bubbles can generate mechanical stresses of sufficient intensity to be biologically relevant to organisms living in the sea surface microlayer (neuston) (17). As a technological example, cell death at the air–liquid interface during the sparging of bioreactors to enhance oxygen diffusion has been attributed to bubble bursting (18).

The fluid flows most effective at shearing small free-floating objects are those that exhibit strain deformation. In such flows, a rod-shaped object will tend to align itself along the direction of maximum fluid extension. In this orientation the rod experiences the greatest tensile stress and is most susceptible to fragmentation.

Significance

The hydrodynamic forces within bursting bubbles are of interest for their relevance to small-scale fluid mechanics, bioreactor efficiency, pollutant degradation, and the origin of life. However, despite the 150-year history of their study, the strengths of flows within bursting bubbles are only hypothetically known. Here, we show that DNA nanotubes—architecturally similar to biological microtubules—are fragmented during the bubble bursting process. Further, by analyzing the resulting fragment lengths, we characterize the spectrum of elongational flow rates, revealing that surprisingly strong tensile forces can be generated—in principle sufficient to fragment filamentous cyanobacterial chains, lipid vesicle protocells, genomic DNA, and other long polymeric molecules residing within or near the disintegrating liquid film.

Author contributions: R.F.H., E.W., and B.Y. designed research; R.F.H. and B.Y. performed research; R.F.H., E.W., and B.Y. contributed new reagents/analytic tools; R.F.H., E.W., and B.Y. analyzed data; and R.F.H., E.W., and B.Y. wrote the paper.

The authors declare no conflict of interest.

This article is a PNAS Direct Submission.

Freely available online through the PNAS open access option.

¹To whom correspondence should be addressed. Email: bernard.yurke@boisestate.edu.

This article contains supporting information online at www.pnas.org/lookup/suppl/doi:10.1073/pnas.1424673112/-DCSupplemental.

In a given fluid element, the rate of fluid extension—i.e., the rate at which two points in the fluid separate, divided by the distance between them—has a maximum that is referred to as the elongational rate and is here denoted by $\dot{\epsilon}$. A useful way to conceptualize the meaning of $\dot{\epsilon}$ is to consider the case when it is constant. In this case, the time it takes for the fluid element to double its length is $t_b = \ln(2)/\dot{\epsilon}$.

Fig. 1 shows a mechanism by which rod-shaped objects within bursting fluid films can be fragmented. As the hole produced in the bubble film expands, its circumference increases (Fig. 1*B*). Due to this, fluid elements near the hole's edge will experience elongation in the direction perpendicular to the velocity of the hole edge. As shown in Fig. 1*C* and *D*, rod-shaped structures within the bubble film will align along the circumference of the expanding hole. If the tension generated along the length of the structure exceeds its tensile strength, the structure will fragment (Fig. 1*E*).

The elongational rates generated by this mechanism can be estimated using a model of film hole dynamics, for a film of uniform thickness. Initially considered by Dupré (19), Rayleigh (20), and Ranz (21), then corrected by Culick (22) and Taylor (23), the model treats the rupture as a circular hole that propagates outward with the film fluid accumulating in a toroid at the hole perimeter. From momentum balance, the hole propagates outward with a constant speed $v = \sqrt{2\sigma/\rho\delta}$, where σ is the surface tension of the film, ρ is the fluid density, and δ is the film thickness. The elongational rate of the circumference is given by $\dot{\epsilon} = v/r$, where r is the hole radius. The volume of fluid subjected to elongational rates greater than $\dot{\epsilon}$, in this simple model, is given by $V_f(\dot{\epsilon}) = \pi\delta r^2 = 2\pi\sigma/\rho\dot{\epsilon}^2$, which is, surprisingly, independent of film thickness. Such volumes provide a natural way to characterize the ability of a bursting bubble to fragment objects suspended within the bubble film that will shear under given elongational rate $\dot{\epsilon}$. Importantly, $V_f(\dot{\epsilon})$ can be defined in a model-independent way as the volume of fluid that experiences elongational rates greater than $\dot{\epsilon}$ during the course of bubble bursting. We will refer to such volumes as fragmentation volumes.

Although easiest to explain, the Culick and Taylor model does not describe the only type of elongational flow that can be

generated within a bursting bubble; therefore the estimate for $V_f(\dot{\epsilon})$ based on this model should be considered a loose lower bound for the true value. In fact, only half the surface-tension energy released is converted into the kinetic energy of the outward motion of the fluid (24). This suggests that the other half of the surface-tension energy must be dissipated within the film near the edge of the hole. For fluids with low viscosity, such as water, this implies that there are intense small-scale fluid flows near the edge of the hole (18) in addition to those illustrated in Fig. 1. Hydrodynamic instabilities, particularly with larger bubbles, can occur along the perimeter, resulting in fingering and the formation of droplets (25). Also, particularly for small bubbles, the expanding hole produces an inward propagating wave at the bottom surface of the bubble that forms a jet that may launch droplets (26, 27). High-flow gradients are expected in the region where these jets pinch to form droplets. A recent discussion of droplet production during bubble bursting in ocean-like (i.e., not soapy) water was given by Lhuissier and Villermaux (28).

As discussed by Lhuissier and Villermaux, at the instant the bubble bursts it possesses a cap of uniform thickness that, at a well-defined edge, joins with the bulk fluid in a region where the thickness rapidly increases with distance from the center of the bubble (Fig. 14). The critical thickness at which bubble films spontaneously burst depends on the bubble radius (28), increasing from 0.05 to 30 μm as the bubble radius increases from 1 to 20 mm. For an object such as a microorganism to be fully impacted by the mechanical stresses produced by bubble bursting, it would have to reside in the cap film or close to the cap boundary; that is, its thinnest dimension would have to be smaller than the film thickness. Nevertheless, mechanical stresses produced by bursting bubbles are among the stresses that microorganisms, particularly those that occupy the niche consisting of the neuston or sea surface microlayer (29–31), must cope with. We hypothesize that protobionts, small enough to be suspended within the bubble film, also occupied this niche and used these stresses to facilitate replication. However, little work seems to have been done to characterize the elongational rates produced during the bursting of a bubble that would facilitate assessing whether forces of sufficient magnitude are generated.

In this study the fragmentation of DNA nanotubes is used to characterize both the magnitude of the elongational rates produced and the volume of fluid subjected to these elongational rates during bubble bursting. These nanotubes are constructed from short DNA oligomers referred to as single-stranded tiles, which each have four sequence domains by which a given oligomer binds with four neighboring oligomers via Watson–Crick base pairing. Thus, whereas each DNA oligomer is held together by covalent bonds, the entire tube assembly is held together by the supramolecular interactions that enable two complementary single-stranded oligomers to form duplex DNA. Base sequences of the oligomers are designed so that the axes of the duplex DNA are parallel to the long axis of the tube. The supramolecular Watson–Crick bonds between neighboring single-stranded tiles are much weaker than the covalent bonds of the phosphate backbone of a single-stranded tile (32). Under sudden tension along the axis of the duplex DNA (33), the tensile force at which the supramolecular bonding fails is referred to as the overstretching force f_c , which has a value of about 65 pN (34, 35). For a tube in which there are n duplex strands in cross-section, the tensile force will be $T_c = nf_c$. For the tubes used in the experiments reported here, $n = 7$ (SI Appendix, Fig. S1) and consequently the tubes fragment when subjected to tensile forces in excess of 455 pN. The tubes have a radius of 4 nm, a persistence length of 5 μm (36), and a length distribution that peaks at 5 μm at the start of the experiment (SI Appendix, Fig. S2; see Fig. 3*B* and *G*).

Some of these tubes will be trapped in the bubble film and will be subjected to elongational forces in the manner illustrated in Fig. 1. Although nanotubes will necessarily also be subject to

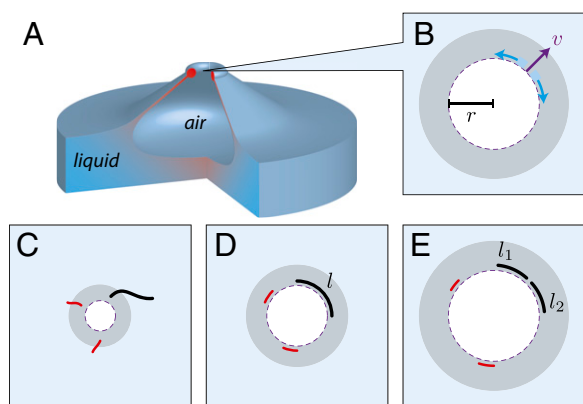


Fig. 1. DNA nanotubes fragmentation by bursting bubbles. Side (*A*) and top (*B*) views of a bubble filled with air bursting on a water surface. Color gradient loosely corresponds to the expected magnitude of the hydrodynamic forces. (*B*–*E*) As the hole travels outward driven by surface tension, the liquid film is accumulated into a growing toroidal rim (gray rings). The enlargement of the hole produces elongational flow, with rate $\dot{\epsilon} = v/r$, which is tangential to the perimeter where r is the hole radius and v is the outward velocity of the hole perimeter. The two blue arcs are the two volume elements of the bursting film. (*C* and *D*) As the hole expands, the fluid flow orients DNA nanotubes (black, red). (*D* and *E*) The elongational flow breaks sufficiently long DNA nanotubes (black) of length l into fragments of length l_1 and l_2 due to tension applied to the nanotube by the elongational fluid flow. Short nanotubes (red) are not fragmented due to insufficient build-up of tension.

compressive fluid flows, they are not fragile under compression. The junctions at which a given single-stranded tile connects with two neighboring tiles are flexible, allowing the tube to crumple and then straighten when the compressive forces are relieved. This collapse into a coil configuration followed by stretching has been studied for other stiff linear biopolymers and synthetic fibers in hydrodynamic flows near stagnation points (33, 37, 38). Generally, the tubes will crumple under the compressive flow and reorient and stretch along the axis of the elongational flow (Movie S1 and SI Appendix, section 10). A further complication is that Brownian motion will tend to counteract the alignment produced by the elongational flow. However, as will be shown, under the conditions in which our DNA nanotubes break, the Péclet number—which is the ratio of the active transport rate to the diffusive transport rate—is in excess of 1.4×10^4 , indicating that diffusive misalignment of the nanotubes plays a negligible role in our experiments. Due to the viscous stresses exerted on the DNA nanotube as it reorients along the direction of maximum extension flow, the tension experienced by the tube will be greatest at the center of the tube and will be greater for longer tubes, scaling as $T \propto \dot{\epsilon} l^2 / \ln(l/2R)$, where l is the tube length and R the tube radius (34). If the tensile force is exceeded, the tube will break into two fragments of nearly equal length. If the elongational flow continues to intensify so that the two fragments experience a tension at their centers that exceeds the tensile force, each of these in turn will fragment into two shorter pieces of equal length. This cascading process will continue until the elongational rate reaches its maximum value.

DNA nanotubes are well-suited to serve as probes of hydrodynamic flows within bubble films for three reasons. First, their fragmentation in elongational flows has already been extensively characterized (34). Second, they are highly soluble in water and do not exhibit a surfactant-like tendency to stick to the air–water interface, unlike many proteins. Third, it is straightforward to measure histograms of nanotube lengths using fluorescence microscopy. Here, from the evolution of the DNA nanotube fragment length during the course of bubbling, we were able to determine the fragmentation volumes for elongational rates over five orders of magnitude, although our experimental techniques were not able to distinguish where the DNA nanotubes were broken within the bubble. Our findings suggest that, via bubbles, ocean waves provide a source of strong mechanical forces at the micron-scale mechanical stresses that ocean surface-dwelling microbes must cope with, that may be involved in the natural breakdown of pollutants, and that would have been available for protobionts to use as a means of driving self-replication.

Results

Fig. 2 shows the experimental setup and molecular design.

DNA Nanotubes. For the experiments, DNA nanotubes with monodisperse diameter and bond strength were used (32, 34). These tubes were self-assembled from 7 DNA oligomers (Fig. 2D and SI Appendix, Fig. S1), as described in *Materials and Methods*. The tubes seldom grow longer than 20 μm and have a persistence length of over 5 μm (36), making them more amenable to theoretical analysis than a reptating polymer. For the experiments here, they can be regarded as rigid rods that break when an axial tensile force of 455 pN is applied (34).

Bubble Production at Constant Rate and Precise Bubble Size. Bubbles were generated by flowing air through buffer solution containing DNA nanotubes (Fig. 2). Air was supplied via a motorized syringe pump equipped with a 60-mL syringe [26.70-mm inner diameter (ID)]. To minimize evaporation, the air was delivered via polyethylene tubing, 0.58-mm ID, and was bubbled through a humidifier consisting of a 15-mL centrifuge tube filled to 13.5 mL with the assay buffer [$1 \times$ TAE (40 mM Tris-acetate and 1 mM EDTA) with 12.5 mM MgCl_2]. Two stainless steel capillaries,

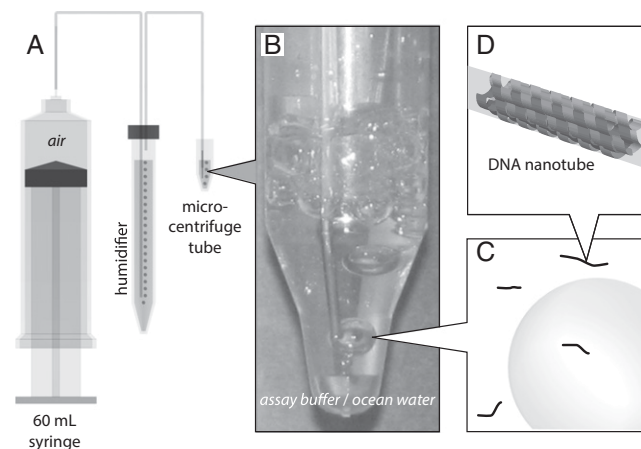


Fig. 2. Bubbles production apparatus. (A) Schematic of apparatus. (B) Sample, housed in a microcentrifuge tube, to which air is being delivered. For scale, the OD of the upper section of the microcentrifuge tube is 1.1 cm. (C) Bubbles and 7-helix nanotubes (not to scale) are in the solution. (D) Schematic of the 7-helix nanotube used in this experiment (SI Appendix, Fig. S1 and Table S1).

passing through the cap and cemented with silicone aquarium sealant, served as feedthroughs for air to and from the airtight humidifier chamber. The bubbles were generated at the end of a stainless steel capillary, 0.635-mm outer diameter (OD) and 0.432-mm ID, connected to the end of the polyethylene tubing that was pointed downward into the sample fluid (Fig. 2B). To minimize the amount of synthetic DNA used, the sample, typically consisting of 100 μL of fluid, was housed in a 2.0-mL microcentrifuge tube (Fig. 2B). The nose of the tube has a 4-mm ID and a depth of 6 mm. The tapered region flares out to a 1-cm ID.

Bubbles of different size were obtained by varying the airflow rate. Two airflow rates, 1.8 and 18 mL/min, were used in the experiments. A bubble volume V_b of 5.32 mm^3 at the slower airflow rate (1.8 mL/min) was determined from photographs of bubble production at the end of the capillary tube in a flat-walled flask containing assay buffer. The height and width of the bubbles were measured and the volumes were computed under the assumption that the bubbles are oblate spheroids. At the slower flow rate, individual bubbles reached the surface and burst before the arrival of subsequent bubbles. Larger bubbles were produced at the higher flow rate. By counting the number of bubbles produced over a known time interval at a given airflow rate, the ratio of the volume of the bubbles produced at 18 and 1.8 mL/min was measured to be 1.74 ± 0.26 . From this ratio, a bubble volume V_b of 9.26 mm^3 was inferred for the higher flow rate (18 mL/min). At this bubbling rate, the sample chamber contained multiple bubbles at any one time, i.e., a foam, as shown in Fig. 2B. A mean bubble lifetime of ~ 2 s was determined for both buffer and ocean water based on an estimate of the number of bubbles in the sample chamber divided by the rate of bubble production. This lifetime is intermediary between that of pure (distilled) water and saturated soap bubbles, indicating the presence of surfactant in highly dilute amounts, typical of tap water or water found in nature, such as river water, ocean water, and rain puddles (28). Due to drainage, bubble lifetime is related to the film thickness at bursting; for similar-sized bubbles bursting individually in tap water, Lhuissier and Villermaux (28) report thickness on the order of 100 nm.

Bubble Bursting Driven Fragmentation of DNA Nanotubes in Assay Buffer or in Ocean Water. To follow the fragmentation of the DNA nanotubes by bubbling, two experiments were performed in assay buffer and in ocean water at the 18-mL/min airflow rate. For the experiment in ocean water, a control sample was left undisturbed to assess the stability of the DNA nanotubes in ocean water

(SI Appendix, Fig. S3 A and B). At the beginning of the run, the mean fragment length of the DNA nanotube control sample was determined to be $7.01 \pm 0.41 \mu\text{m}$. At the end of 1 h, the mean fragment length in the undisturbed sample was measured to be $6.88 \pm 0.42 \mu\text{m}$, which is statistically indistinguishable from the initial value.

The experiment in assay buffer consisted of two runs. In the first run, 1- μL volumes were drawn at time points when $V_a = 0$, 60, and 240 mL of air had passed through the sample. In the second run, the data were acquired at $V_a = 0$, 9, 18, 36, 72, 180, and 360 mL. Representative total internal reflection fluorescence (TIRF) microscopy images taken from the second run samples are shown in Fig. 3 A, C, and E along with the corresponding length histograms (Fig. 3 B, D, and F). The data of both runs were treated as a homogeneous set (SI Appendix, Fig. S2). For the experiment in ocean water, samples were withdrawn at $V_a = 0$, 60, 120, and 360 mL (Fig. 3 G-I and SI Appendix, Fig. S3).

The evolution of DNA nanotube length distributions was quantified by measuring individual nanotube lengths in fluorescence images (34). DNA nanotubes were covalently labeled with Cy3 fluorophores at uniform density (1 Cy3 every 7 nm, SI Appendix, Fig. S1). As a consequence, the relation between emitted photons and fragment length is expected to be linear. By measuring the photons emitted by each nanotube and the contour length of the longest nanotube in each image, the length of each nanotube can be inferred directly from the photon counts, even for nanotubes whose length is less than the diffraction-limited resolution of the microscope (Materials and Methods).

The length distributions (Fig. 3 and SI Appendix, Figs. S2 and S3) show a decrease in mean fragment length $\langle l \rangle$ with increasing bubble bursting. After 20 min, when 360 mL of air had been bubbled through the sample, the mean fragment length was measured to be $1.04 \pm 0.07 \mu\text{m}$ and $1.02 \pm 0.10 \mu\text{m}$ for the experiments in assay buffer and ocean water, respectively. The decrease in mean fragment length showed that a substantial amount of tube fragmentation had occurred. Moreover, the assay buffer and ocean water histograms indicated that DNA nanotube fragmentation proceeds similarly in the two fluids.

Under shearing, the sum of tube lengths l_i should remain conserved. This was tested by measuring the total tube length per image for the samples extracted during the run in assay buffer at different time points. Fig. 4A shows that l_i remains constant as a function of the air volume that has passed through the sample, V_a . Because $l_i = N \langle l \rangle$, where N is the total number of nanotubes and $\langle l \rangle$ is the mean tube length, the time independence of l_i allows one to infer the population ratio $P_g = N/N_0$, where N_0 is the initial number of nanotubes, via $P_g = \langle l \rangle_0 / \langle l \rangle$, where $\langle l \rangle_0$ is the initial mean tube length. P_g , inferred by this method, is plotted as a function of V_a in Fig. 4B. There is a sevenfold increase in the number of nanotubes by the time an air volume of 360 mL has passed through the sample. The curves are the result of a global best fit of the theory presented in the Model for Extracting the Fragmentation Volume section to the experimentally measured tube length distributions.

To determine the smallest tube fragments that were produced, the concentration of tubes $c(l, t)$ in the length range $0 < l < \Delta_{bin}$ for $\Delta_{bin} = 1, 1/2, 1/4, 1/8, 1/16, \text{ and } 1/32 \mu\text{m}$ was tabulated at different V_a . In Fig. 4C, we plotted $c(0 < l < \Delta_{bin}, t) / \Delta_{bin}$, which is the observed nanotube concentration normalized to the bin of size Δ_{bin} . For $\Delta_{bin} \geq 1/16 \mu\text{m}$ and larger, this quantity grows substantially with V_a , whereas for $\Delta_{bin} = 1/32 \mu\text{m}$ the data remain relatively fixed, indicating that fragments as short as $1/16 \mu\text{m}$ are produced. A comparison of the curves of Fig. 4C with that of the results of a global best fit of the theory presented in the model section to the experimentally measured tube length distributions is given in SI Appendix, Fig. S7.

In previously reported experiments (34), we have shown that the suddenly applied fluid elongational rate $\dot{\epsilon}$ required for mid-point scission of an initial nanotube of length l to produce two fragments that have identical length of $l/2$ is

$$\dot{\epsilon}(l) = \frac{4T_c \ln(l/2R)}{\pi\eta l^2}, \quad [1]$$

where R is the tube radius, η is the viscosity of the fluid, and the tension T_c required to break the tube is given by $T_c = n f_c$, where n

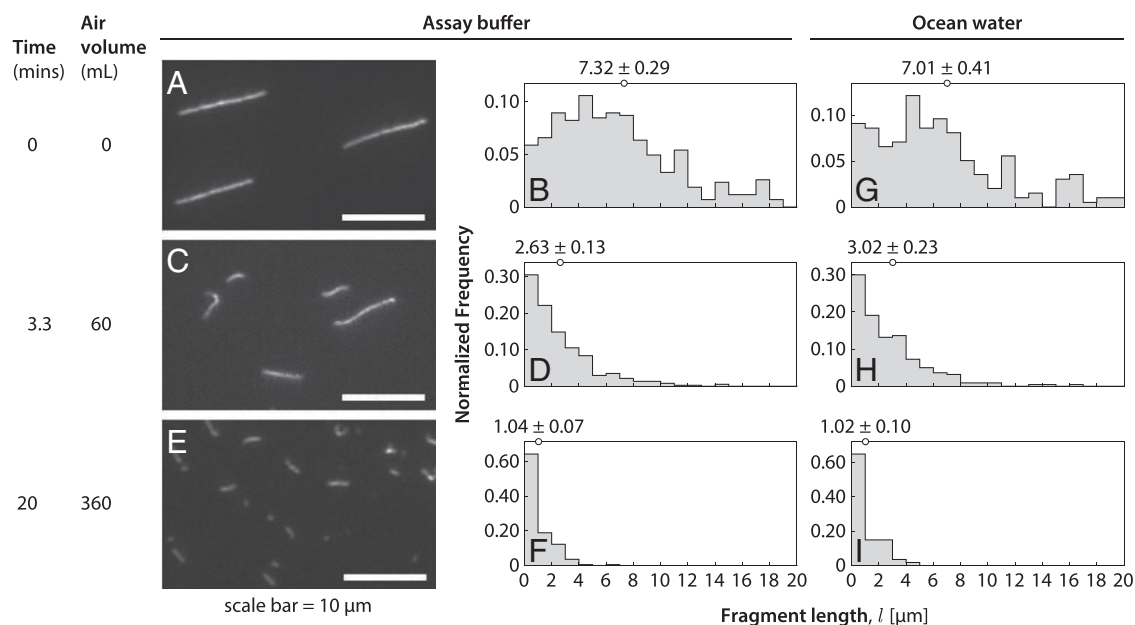


Fig. 3. Nanotube length distributions for bubble bursting experiments in assay buffer or in ocean water. Fluorescence microscopy images and fragment length distributions of DNA nanotubes withdrawn from a sample with an initial volume of 100 μL after 0 mL (A and B), 60 mL (C and D), and 360 mL (E and F) of air had passed through the sample at a flow rate of 18 mL/min. The mean tube length $\langle l \rangle$ for each distribution is given at the top of each histogram. Nanotube length distribution in bubble bursting experiment with ocean water after 0 mL (G), 60 mL (H), and 360 mL (I) of air.

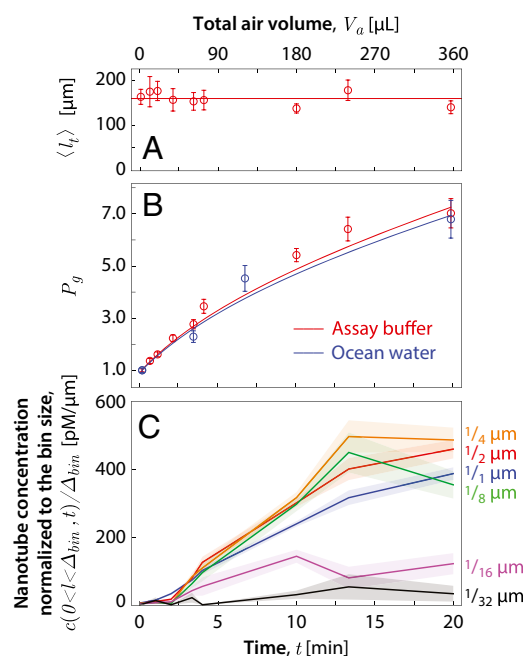


Fig. 4. DNA-nanotube fragmentation data as a function of the bubbling exposure time at a flow rate of 18 mL/min. (A) Total tube length per microscope field of view. The horizontal line represents a constant total tube length of 159 μm per image. Error bars show the SEM. (B) Plot of the population ratio P_g for experiments in assay buffer (red) and in ocean water (blue). The lines are the Bayesian fit to the experiments in assay buffer (red) and in ocean water (blue) based on the theory described in the model section. (C) Plot of the nanotube concentration per tube length $c(l, t) / \Delta_{bin}$ in the length range $0 < l < \Delta_{bin}$ for $\Delta_{bin} = 1, 1/2, 1/4, 1/8, 1/16,$ and $1/32 \mu\text{m}$. (See *SI Appendix, Fig. S2* for detailed histograms.)

is the number of duplex DNA strands along the circumference of the tube (*SI Appendix, Fig. S1*) and $f_c = 65 \text{ pN}$ is the critical force to overstretch a DNA helix (35). Note that the tension required to break the tube does not depend on the length of the duplex DNA segments that link successive tiles along the tube axis. This is because when stress is applied on a time scale that is short compared with that over which base pairs disassociate due to Brownian fluctuations, the strain will distribute uniformly along the linker duplex segments. All base pairs will break at once when this strain reaches the value where overstretching occurs. For our tubes, $n = 7$ and $R \approx 4 \text{ nm}$. The observation of $1/16\text{-}\mu\text{m}$ tube fragments implies that tubes as short as $1/8 \mu\text{m}$ are broken in two via the hydrodynamic flows generated within the bubbles of the experiment of Figs. 3 and 4. Taking $\eta = 1.0 \times 10^{-3} \text{ Pa}\cdot\text{s}$, Eq. 1 indicates that elongational flow rates at least as large as $\dot{\epsilon} = 1.0 \times 10^8 \text{ s}^{-1}$ are generated during bubble rupture.

Fragmentation Is Little Affected by the Bubble Production Rate. To show that fluid flow associated with bubble inflation and transport was not primarily responsible for the tube fragmentation, we repeated the experiment in assay buffer at an order of magnitude slower flow rate of 1.8 mL/min (*SI Appendix, Fig. S4*). The mean tube length when 60 mL of air had passed through the sample was $2.32 \pm 0.13 \mu\text{m}$. If, as presumed by our simple theoretical estimate based on film hole dynamics, a fixed amount of fragmentation occurs each time a bubble bursts, then the same amount of fragmentation should be apparent in samples that experienced the same number of bubbles. Because of the different size bubbles at the two flow rates, 60 mL of air at the slower flow rate generates the same number of bubbles as 104 mL of air at the faster flow rate. Interpolating between measured values for the faster flow rate of 18 mL/min (Fig. 3 and *SI Appendix, Fig. S2*)

yields a mean fragment length of 1.88 μm . This is only 20% shorter than found at the slower airflow rate, despite the 10-fold faster airflow rate, supporting a dominant role for bubble bursting rather than other hydrodynamic flows in the observed fragmentation processes. Furthermore, the similar degree of fragmentation in bubbles bursting individually at the surface (as for the slower flow rate) or in the context of a foam (as for the higher flow rate) suggests that the relevant hydrodynamic effects are similar for these two contexts.

Eliminating Bubble Bursting on the Water–Air Interface Suppresses Fragmentation. The assumption that fluid flows associated with bubble bursting are primarily responsible for tube breakage was confirmed by the suppression of tube fragmentation through the addition of 200 μL of heptane to the sample vial to form a fluid layer on top of the assay buffer. Air bubbles rising through this layer would leave the hydrophilic DNA in the aqueous phase. The aqueous fluid flows associated with this process are also reduced because of viscous coupling of the buffer with the heptane at the interface (39–41). The mean tube length when 60 mL of air was bubbled through the sample at 18 mL/min was $6.03 \pm 0.50 \mu\text{m}$ (*SI Appendix, Fig. S5*), which is similar to the initial mean tube length $7.32 \pm 0.29 \mu\text{m}$ and large compared with the mean tube length $2.63 \pm 0.13 \mu\text{m}$ measured at $V_a = 60 \text{ mL}$ for the experiment of Fig. 3 and *SI Appendix, Fig. S2*.

Decreasing Surface Tension also Suppresses Fragmentation. Finally, we demonstrated that fluid flows associated with bubble bursting are primarily responsible for tube breakage by reducing tube fragmentation through the addition of 2 mM of the surfactant SDS to the assay buffer. The surfactant reduces the surface tension, increases surface viscosity effects (42), and increases the bubble lifetime. These effects inhibit nanotube breakage by reducing surface-tension-driven flow velocities and by reducing the film fluid volume through film drainage. The foam produced during this experiment necessitated using a 300- μL sample volume. Even then it was necessary to periodically stop the airflow to allow the foam to subside. Because of the $3\times$ greater volume, the mean tube length $\langle l \rangle = 6.23 \pm 0.5 \mu\text{m}$ at $V_a = 180 \text{ mL}$ for this experiment (*SI Appendix, Fig. S6*) should be compared with the $\langle l \rangle = 2.63 \pm 0.13 \mu\text{m}$ at $V_a = 60 \text{ mL}$ for the experiment of Fig. 3 and *SI Appendix, Fig. S2*. Reducing the surface tension suppresses the breakage of the nanotubes. In agreement with previously published reports (43, 44), we verified that DNA nanotubes are stable in SDS buffer by constructing a length histogram of a control sample that was incubated in SDS buffer for 30 min without airflow. The final mean tube length $7.45 \pm 0.54 \mu\text{m}$ was found to be statistically indistinguishable from the initial mean tube length $7.65 \pm 0.58 \mu\text{m}$, indicating the stability of DNA nanotubes in SDS buffer (*SI Appendix, Fig. S6*).

Model for Extracting the Fragmentation Volume. The results we have presented show that bursting bubbles will fragment DNA nanotubes and document how the fragment distribution in a fixed volume of fluid changes as a function of time as the fluid is cycled through the bursting bubbles. To apply these results more generally, one would like to know the number N of objects of a particular type that would be broken in a bubble if they are present in the fluid at concentration c and if an elongational rate of $\dot{\epsilon}$ was required to break them. The proportionality factor between N and c is the fragmentation volume $V_f(\dot{\epsilon})$; that is, $N = V_f(\dot{\epsilon})c$. The fragmentation volume is the sum of all of the fluid volume elements whose elongational rate has exceeded $\dot{\epsilon}$ at some point during the bubble rupture process. The fragmentation volume characterizes the fragmentation process for a single pass through a bubble. However, during the course of our experiments, a given nanotube or its fragments will have passed through bubbles multiple

times. This complicates the determination of $V_f(\dot{\epsilon})$ from the data. We will now describe how the time evolution of the DNA nanotube length distribution can be processed to extract $V_f(\dot{\epsilon})$.

Let $c(l, t)$ denote the concentration distribution of tubes of length l as a function of time t , such that in the limit $\Delta l \rightarrow 0$, $c(l, t)\Delta l$ is the concentration of tubes having lengths in the interval from $l - \Delta l/2$ to $l + \Delta l/2$ at a given time. The time evolution of the experimentally determined $c(l, t)$ contains information on how effectively a bubble can break a tube of length l . To extract the fragmentation volume from these data, a model is crafted for the case where the bubbles all have the same volume V_b , are produced a constant rate γ , and the sample volume V_s remains sufficiently well mixed that $c(l, t)$ can be regarded as constant over the sample volume. For the experiments reported here, $c(l, t)$ is expected to be uniform because the sample volume is small and well mixed by the fluid motion produced as the bubbles rise to the surface.

Let $r_f(l)$ be the rate with which tubes of length l are fragmented upon bursting of a bubble and let $r_b(l, l')$ be the rate per unit tube length that tubes of length l are produced from tubes of length l' upon bursting of a bubble. Then, the rate of change of $c(l, t)$ is given by

$$\frac{dc(l, t)}{dt} = -\gamma r_f(l)c(l, t) + \gamma \int_0^{\infty} r_b(l, l')c(l', t)dl', \quad [2]$$

where γ is the rate at which bubbles are produced (i.e., \dot{V}_a/V_b). Note that the lower limit of integration could have been set to l because $r_b(l, l') = 0$ for $l > l'$ because producing a new fragment of length l requires breakage of a tube longer than l . Because the total tube length per unit volume remains constant as the tubes are broken into shorter sections, one must have

$$\int_0^{\infty} l r_f(l)c(l, t)dl = \int_0^{\infty} l \int_0^{\infty} r_b(l, l')c(l', t)dl'dl. \quad [3]$$

The rate $r_f(l)$ is inversely proportional to V_s because this determines the frequency with which a given tube of length l will be within the vicinity of a bursting bubble. We thus write

$$r_f(l) = \frac{V_f(l)}{V_s}, \quad [4]$$

where the fragmentation volume $V_f(l)$ characterizes the effectiveness with which a bursting bubble breaks a tube of length l . Here, $V_f(l)$ is used as shorthand for $V_f(\dot{\epsilon}(l))$, where $\dot{\epsilon}(l)$ indicates the minimum elongational rate required to break tubes of length l . Similarly, we write

$$r_b(l, l') = n(l, l') \frac{V_f(l')}{V_s}, \quad [5]$$

where $n(l, l')$ is the mean number of tubes of length l per unit tube length produced by the fragmentation of a tube of length l' .

In principle, the functions $V_f(l)$ and $n(l, l')$ could be obtained through numerical calculation of the hydrodynamic flows of bursting bubbles and numerical calculation of the breakage of tubes within these hydrodynamic flows. To our knowledge, the requisite hydrodynamical calculations to determine $V_f(l)$ and $n(l, l')$ have not been carried out. The aim of the analysis here is to determine $V_f(l)$ using a plausible model for $n(l, l')$ in conjunction with our experimental data.

Imagine a small tube in the vicinity of a bubble that has begun to burst. The elongational flow rate of the fluid element the tube is imbedded in will increase over time. When the tension at the center

of the tube exceeds the tensile strength of the tube, the tube will break into two fragments of equal length. If the elongational rate continues to increase so that the tension at the center of the two shorter tubes exceeds the tube tensile strength, then again each of these two shorter tubes will break into two smaller tubes of equal length. At long times the fluid motions produced by the bursting bubble will dissipate, the bifurcation cascade will terminate, and the elongational flow rates within the fluid element containing the tube fragments will return to zero. One thus expects the fragmentation process to be a cascade of bifurcations. In the model for this case, which we call the “full cascade model,” $n(l, l')$ is given by

$$n(l, l') = \sum_{m=1}^{\infty} 2^m p_m(l') \delta(l - l'/2^m), \quad [6]$$

where $p_m(l)$ is the conditional probability that a tube of length l has broken into 2^m fragments given that it has broken, the delta function ensures that $l' = 2^m l$, and the multiplier in front of the delta function is the number of fragments produced by a cascade of m bifurcations.

This is, of course, an idealization. Because of microscopic disorder, tubes are not expected to break exactly in half. However, our experience in modeling imperfections in tube breakage by hydrodynamic flows in another context indicates that the results are insensitive to the inclusion of such disorder in the modeling (34). More seriously, the assumption that the tube lengths are small compared with the length scale over which the elongational flow rate varies is likely to be violated in our experiments. Our longest tubes exceed 20 μm , which is likely to be substantially greater than the bubble film thickness. In this case, we expect a long tube to fragment into tubes having a distribution of lengths rather than into 2^m tubes of equal length. As an extreme case one might imagine that the tubes only break in two. This choice results in the “single bifurcation model,” which uses

$$n(l, l') = 2\delta(l - l'/2). \quad [7]$$

We show in *SI Appendix*, Figs. S7–S9 and sections 3–6 that the single bifurcation model does not fit the data as well as the full cascade model. This indicates that the $c(l, t)$ data have the power to distinguish between models of $n(l, l')$ and suggests that Eq. 6 is a satisfactory approximation for our experiments.

As shown in *SI Appendix*, section 3, Eq. 2, using Eqs. 4–6, yields the full cascade model:

$$\frac{dc(l, t)}{dt} = -\frac{\gamma V_f(l)}{V_s} c(l, t) + \frac{\gamma}{V_s} \sum_{m=1}^{\infty} 2^{2m} [V_f(2l) - V_f(l)] c(2^m l, t). \quad [8]$$

Note that because shorter tubes require higher fluid elongational rates to break and very short tubes require a very high elongational rate to break, $V_f(l)$ is a monotonically increasing function

$$V_f(l) \geq V_f(l') \quad \text{for } l \geq l' \quad [9]$$

and

$$\lim_{l \rightarrow 0} V_f(l) = 0. \quad [10]$$

Eqs. 8–10 define the model of tube breaking used in the analysis.

It has been experimentally observed that DNA nanotubes can join end-to-end (45). To assess the effect end-joining might have on attempts to extract $V_f(l)$ from the data, a more complete model incorporating end-joining of DNA nanotubes was considered. This

“end-to-end joining model” considers the full cascade of bifurcations and is given by

$$\frac{dc(l,t)}{dt} = -\frac{\gamma V_f(l)}{V_s} c(l,t) + \frac{\gamma}{V_s} \sum_{m=1}^{\infty} 2^{2m} [V_f(2l) - V_f(l)] c(2^m l, t) - \int_0^{\infty} k(l,l') c(l,t) c(l',t) dl' + \int_0^l k(l',l-l') c(l',t) c(l-l',t) dl', \quad [11]$$

where $k(l,l')$ is the second-order rate constant for the joining of two tubes, one of length l , the other of length l' to a tube of length $l+l'$. The first integral on the right-hand side gives the rate of loss of tubes of length l due to joining with another tube. The second integral on the right-hand side gives the rate of production of tubes of length l due to the joining of a tube of length l' with a tube of length $l-l'$. It is straightforward to show that total tube length is conserved in this more complete model, that is,

$$\frac{d}{dt} \int_0^{\infty} lc(l,t) dl = 0. \quad [12]$$

The full cascade model also satisfies this condition because condition 3 was imposed in building the model.

There are few data available on the rate constant $k(l,l')$. Using the expression for the Stokes drag on a rod of length l and radius r , the relationship between mobility and diffusion, and the relation between diffusion constants and reaction rates for diffusion-controlled reactions (46, 47), we modeled this rate constant as

$$k(l,l') = \kappa \frac{12k_B T}{\eta} \left(\frac{\ln(l/R)}{l/R} + \frac{\ln(l'/R)}{l'/R} \right), \quad [13]$$

where R is the tube diameter, $0 < \kappa < 1$ accounts for the fraction of productive collisions, k_B is the Boltzmann constant, and T is the absolute temperature [see *SI Appendix, section 7* for details, including a comparison with the result of Hill (48)]. With $\kappa = 1$, this expression is an upper bound for diffusion-controlled end-joining.

However, it is known that DNA hybridization is not diffusion-controlled, i.e., the majority of collisions are unproductive (49). Based on hybridization rate constants measured for 10-mers (50), we estimated a reference value of $\kappa_{ref} = 2.2 \times 10^{-4}$ (*SI Appendix, section 7*). Using the methods described below to extract $V_f(l)$ from the experimental data, and assuming various values for κ , we found that there was minimal change in the quality of fit (< 5%) and in the inferred fragmentation volumes (< 20% for $1/4 \mu\text{m} \leq l \leq 18 \mu\text{m}$ and < 10-fold for $l = 1/8 \mu\text{m}$) for $0 \leq \kappa/\kappa_{ref} \leq 1.2$, but the quality of fit was 3.3-fold worse for $\kappa/\kappa_{ref} \sim 12$. From this we concluded both that κ_{ref} is a reasonable estimate and that neglecting end-joining is satisfactory for analysis of the experiment. Consequently, most of the data analysis was carried out using the full cascade model rather than the end-to-end joining model. The analysis was facilitated by the fact that Eq. 8 can be solved analytically given V_f in look-up table form and knowledge of $c(l,0)$. The solutions are presented in *SI Appendix, section 4*.

Data Analysis for Extracting the Fragmentation Volume. The experimentally measured tube length distribution at $t=0$ obtained by partitioning the measured tube lengths in $1/32\text{-}\mu\text{m}$ -wide bins served as the initial value data (*SI Appendix, Fig. S2*). A stochastic search method was used to find a piecewise linear and continuous $V_f(l)$, constrained to start at zero and to be monotonic so as to satisfy Eqs. 9 and 10, which resulted in the best fit (weighted mean-

squared error) between the measured concentration distribution $c(l,t)$ and the computed concentration distribution $c_c(l,t)$. The fitness function, as well as other details of the data analysis process, is given in *SI Appendix, section 6*. For the full cascade model, Eqs. 8–10, the best-fit computed concentration distribution compared with the measured concentration distribution is shown in *SI Appendix, Figs. S7 and S8* for the assay buffer and in *SI Appendix, Fig. S10* for the case of ocean water. The results of extracting V_f from the buffer and ocean water data using the full cascade model are shown in Fig. 5. One sees that the fragmentation volume functions $V_f(l)$ for the buffer and ocean water overlap within the uncertainty of the fit. Using Eq. 1, V_f can be expressed as a function of the elongational flow rate $\dot{\epsilon}$, as indicated by the x-axis labels above the figure.

In the large l region (as defined below), the plot of Fig. 5 does not depend on $n(l,l')$ and is thus model independent, making the values for V_f extracted in this region particularly robust. This follows from the fact that our initial tube length distributions fall off rapidly for large l so that the distribution effectively cuts off at a maximum tube length l_m . Consequently, new tubes with lengths in the region $l_m/2 < l \leq l_m$ will not be produced, and the change in $c(l,t)$ as a function of time will only be due to loss of tubes from this part of the distribution through tube breakage. In this region, the length distribution simply decays exponentially with the decay constant $\gamma V_f(l)/V_s$, as per the first term of Eq. 8. Hence, in this interval a fit to the exponential decay of $c(l,t)$ suffices to extract V_f , as is shown in Fig. 5 and *SI Appendix, Fig. S11*. The theory we have presented is necessary to extract V_f in the region $0 \leq l < l_m/2$ because here the dynamics is complicated by the addition of new tubes from the breakage of tubes of length $l_m/2 < l \leq l_m$.

As an aside, note that rod-like DNA nanostructures could be fabricated with well-defined lengths (43, 51) and designed to split exactly in the middle by introducing a “weak spot” with fewer

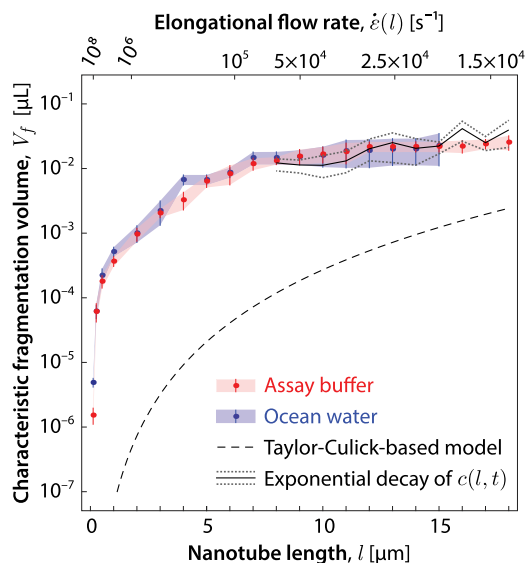


Fig. 5. Characteristic fragmentation volume V_f for tubes in the length bin interval $l \pm 1 \mu\text{m}$ for assay buffer (red) and ocean water (blue) data. The best-fit V_f function for assay buffer is similar to the best-fit V_f function for ocean water, which indicates that DNA nanotube fragmentation occurs in a similar fashion in the two liquids. The simple theoretical estimate of V_f using the Culick and Taylor model of film hole dynamics (black dashed line) falls below our data, as expected, due to the neglect of hydrodynamic effects within bursting bubbles that are not easily modeled. For sufficiently long nanotubes ($l > 8 \mu\text{m}$), the best-fit V_f for assay buffer data (blue) is similar to the V_f values (solid black line \pm gray dotted lines) extracted from the exponential decay of $c(l,t)$ (*SI Appendix, Fig. S11*). Error bars represent SEM (*SI Appendix, section 6.4*).

helices in the cross-section. Such structures could be used to determine $V_f(l)$ for the length l of the structure simply by monitoring the exponential decay due to breakage, because the possibility of breakage at multiple locations can be discounted. However, compared with using tile-based DNA nanotubes that have a broad length distribution, this approach has the disadvantage that, for a given nanostructure, V_f can only be determined at one l .

Some insight into where most of the fragmentation is occurring can be obtained by considering the size of V_f . The data of Fig. 5 suggest that $V_f(l)$ approaches an asymptotic value of $2.6 \times 10^{-2} \mu\text{L}$ for large l . The bubbles in this experiment have an air volume equivalent to a sphere of radius 1.3 mm. For bubbles of this size, surface tension rather than gravity dominates in determining the bubble shape. These bubbles in isolation rest largely below the water surface and maintain a nearly spherical shape with a small cap protruding above the water surface that is 100 nm thick as measured by Lhuissier and Villermaux (28). The depth of the bubble foam formed under the fast bubbling rate is roughly three bubble diameters thick (Fig. 2B). Pushed up by the buoyancy of the bubbles below, the bubbles near the top of the film can be expected to protrude higher and have cap films and foam facet films with areas somewhat larger than that of an isolated bubble. However, one expects the film thickness to be comparable to that of an isolated bubble due to similar surface-tension-driven film draining. A generous overestimate of $1.1 \times 10^{-3} \mu\text{L}$ for the film volume per bubble is obtained by multiplying half the bubble surface area by 100 nm. The 20-fold discrepancy with the measured fragmentation volume implies either that the film is considerably thicker than 100 nm—perhaps due to the context of the foam—or that substantial fragmentation occurs outside the cap region, i.e., in the meniscus where the film thickness increases, in the interstices between bubbles of a foam, or in the bulk.

As indicated in the Introduction, a crude estimate for V_f associated with fluid stretching along the length of the perimeter can be obtained from the Taylor–Culick model of film hole dynamics, where the volume of fluid swept up by the hole before the elongational rate falls below a particular value $\dot{\epsilon}$ is given by $V_f = 2\pi\sigma/\rho\dot{\epsilon}^2$. Using Eq. 1, one obtains $V_f = 1.4 \times 10^9 \text{m}^{-1} \times l^4 / \ln^2(l/2R)$, where we have used $\rho = 1 \text{g/cm}^3$ and $\sigma = 73 \text{dyn/cm}$ for the density and surface tension of water, and l is the nanotube length. This relationship is plotted as a dashed line in Fig. 5.

As we have already mentioned, within this model, energy conservation requires that half the surface-tension energy released must be dissipated within the toroid, suggesting the existence of additional microscale fluid flows within the toroid (18, 24) that must be taken into account to accurately predict V_f . In addition, an accurate calculation would require taking into account the geometry of a bubble contacting a water surface (26), which differs from that of a planar film of uniform thickness, and mechanisms that give rise to instabilities and droplet spray along the hole perimeter (28, 52). In summary, the V_f of the Taylor–Culick-based model, plotted in Fig. 5, is a loose lower bound above which the data must lie.

By computing the Péclet number Pe , we can now confirm that misalignment of the nanotube from the direction of the elongational flow due to Brownian motion is not significant. In the present case, Pe can be taken to be the ratio of the elongational rate to the rotational diffusion constant $Pe = \dot{\epsilon}/D_r$ (53), where the rotational diffusion constant is given by $D_r = 3k_B T \ln(l/R) / \pi\eta l^3$ (54) and l is the length of the tube before scission. Therefore, the Pe number for nanotubes that experience midpoint scission can be estimated based on the experimentally measured length-dependent $\dot{\epsilon}$ (Eq. 1), from which we see that Pe increases monotonically with tube length l . For the range of nanotubes in Figs. 4 and 5 that experience substantial fragmentation ($l \geq 1/8 \mu\text{m}$), Pe was estimated to be $>1.4 \times 10^4$. By analyzing torques within the fluid (47, 55), we showed that Pe is the inverse of the mean-

squared angular deviation of the nanotube axis from the elongational direction and therefore $\sqrt{\langle\theta^2\rangle} < 8.3 \times 10^{-3} \text{rad}$ (SI Appendix, Eq. S88 and section 8). Taken together, the high Pe number and small $\langle\theta^2\rangle$ indicate that the effects of diffusional reorientation are expected to be negligible.

Discussion

Our experiments indicate that DNA nanotube fragmentation can serve as a probe of elongational flows generated at small scales in time-varying complex fluid flows, where imaging of tracer particles would be impractical. We have used DNA nanotube fragmentation to probe the elongational rates in the fluid flows generated by bursting bubbles in aqueous solutions, including ocean water. The DNA nanotube fragment distributions we have measured indicate more intense elongational flow rates than those predicted using the Culick (22) and Taylor (23) model. A more accurate model will have to take into account small-scale hydrodynamic flows occurring within the bubble film. The ability of a bursting bubble to fragment objects suspended within the bubble film has been characterized by the fragmentation volume $V_f(\dot{\epsilon})$, which is the volume of fluid subject to elongational rates in excess of $\dot{\epsilon}$. Although our data for two different bubble sizes did not reveal a strong size dependence of the fragmentation volume, further exploration using a wider range of bubbles sizes could be illuminating. In addition, it will depend on surface tension, viscosity, and the presence of surfactants. The exploration of these dependencies is left to future work. However, when these dependencies are sufficiently well known, the fragmentation volume can be used to determine the rate with which small objects will be broken, by passage through bubbles, in bodies of water ranging from oceans to bioreactors, provided the concentration of the objects, their susceptibility to elongational flows [i.e., $\dot{\epsilon}(l)$], and the size spectrum rate for the bubble production are known.

Whether biological organisms use the energy available in bursting bubbles to aid clonal reproduction and dispersal is not known. However, measurements of the tensile strength of microorganisms suggest that this is a possibility. For example, Stocks and Thomas (56) have measured a tensile strength of $T = 1.0 \mu\text{N}$ for the filamentous bacterium *Saccharopolyspora erythraea* grown in a fermentation tank. A hypha diameter of 180 nm and a mean hypha length of 60 μm was reported for this organism. Using these numbers, Eq. 1 yields $\dot{\epsilon} = 1.8 \times 10^6 \text{s}^{-1}$ for the elongational rate needed to break these hypha in two. This is two orders of magnitude below the maximum elongational rates inferred from DNA nanotube breakage (Fig. 5).

Protobionts may have used the energy available in bursting bubbles to induce cell division without the need for complicated molecular machinery. In SI Appendix, section 9, we present a calculation [using the tensile strength of an analogous substance (57)] that estimates that the tubular vesicle investigated by Szostak's group (10–12) can be broken into 1- μm sections under an elongational rate of $\dot{\epsilon} = 2.5 \times 10^6 \text{s}^{-1} \times n$, where n is the number of lamella in the vesicle. This is also well within the range of $\dot{\epsilon}$ that we have inferred for bursting bubbles. Bursting bubbles therefore provide ample hydrodynamic forces to drive this protocell division process.

Bursting bubbles are also capable of fragmenting covalently linked polymers such as duplex DNA. Using 6 nN as the suddenly applied force needed to break a covalent bond (58–60) and 1 nm as the radius for duplex DNA, one finds from Eq. 1 that an elongational rate of $1.0 \times 10^8 \text{s}^{-1}$ is able to fragment duplex DNA into sections 0.33 μm long. Long-chain synthetic polymers, in which the monomer units are covalently linked together by a single bond, have a radius that is typically less than half that of duplex DNA and can thus be fragmented into segments as small as those of duplex DNA. It is conceivable that bursting bubbles may play some role in degrading plastics and biomaterials within

the ocean (61) and may aid in the dispersal of natural and man-caused oil slicks (62).

Our use of self-assembled DNA nanostructures to probe hydrodynamic flows within bursting bubbles suggests that DNA nanotechnology can provide tools to explore hydrodynamics at short length scales and fast time scales that would be difficult to investigate by other means. Among the other intense transient ocean fluid flows that are effective in shearing small objects in modern oceans and that may have aided reproduction of the protobiont are those associated with rain impacts on the ocean surface and with whitecap formation during wave breaking. DNA-based probes may serve as useful tools to characterize the fragmentation potential of these fluid flows as well, particularly because, as our experiments have shown, such probes can function in ocean water.

Materials and Methods

DNA Nanotubes. The design and characterization of the nanotubes is discussed in ref. 32. A stock solution of DNA nanotubes was prepared by mixing 7 DNA strands (Integrated DNA Technologies, Inc.; *SI Appendix, Table S1 and Fig. S1*) at equimolar concentration of 3.50 μM in a buffer consisting of 1 \times TAE (40 mM Tris-acetate and 1 mM EDTA), pH 8.3 with 12.5 mM Mg-acetate and then slowly annealing from 90 $^{\circ}\text{C}$ to room temperature ($\sim 25^{\circ}\text{C}$) over the course of a day in a Styrofoam box. The nanotube stock solution was then diluted by a factor of 20 for the experiments, which were performed at room temperature.

Imaging. The images were acquired with a custom-built prism-based TIRF upright microscope, as described in refs. 32, 34. A solid-state green laser (GCL-025, 25 mW, Crystalaser) equipped with an adjustable power supply (CL2005, CrystaLaser) provides the excitation beam at 532 nm. The excitation light was filtered with a 532-nm laser filter (Z532/10 \times , Chroma). The filtered excitation beam passed through a quarter-wave plate (Thorlabs) to produce a circularly polarized light wave, which effectively has uniform polarization to counter the fluorescence dependence on the relative orientation between fluorophore and the polarization of excitation light. Two mirrors (Thorlabs) were used to guide the illumination beam to the field of view below the imaging optics. Another mirror (Thorlabs) and a 15-cm focusing lens (CVI Laser Optics) steered the excitation beam onto a Suprasil 1 right-angle prism (CVI Laser Optics) at $\sim 0^{\circ}$ from the horizon to produce a weakly focused illumination spot directly below the objective. We calculated that the incoming angle between the incoming laser and the normal vector of the microscope slide is sufficiently larger than critical angle for evanescent wave to occur at the interface between glass and liquid, where the sample and focal plane of the objective are located.

DNA nanotubes resided inside a glass capillary tube that was optically coupled with the prism by a thin layer of immersion oil. The emitted photons were captured by a 60 \times 1.2-N.A. water immersion objective (Nikon) and focused to the electron multiplier CCD camera (C9100-02, Hamamatsu) by a 20-cm lens tube (double achromat, CVI Laser Optics). The combination of the high brightness and photostability of Cy3-labeled DNA nanotubes, low

background from RCA-cleaned microscope slides, and efficient light collection produce images with high signal-to-noise ratio.

Nanotube Length Measurement. Following a procedure previously reported (32, 34) for the microscopy assay, a 1- μL volume of fluid was withdrawn and immediately diluted by a factor of 40 in buffer. A 5- μL volume of this diluted sample was then deposited between an RCA-cleaned (63) microscope slide and RCA-cleaned coverslip and then imaged. We found that DNA nanotubes stuck readily to this surface.

Contour lengths of Cy3-labeled DNA nanotubes were analyzed using ImageJ (64). Nanotube detection was performed manually. The maximum pixel intensity in each detected feature was used to exclude aggregates of DNA nanotubes and colocalized DNA nanotube fragments. Moreover, all features whose maximum pixel intensities were above the saturation level of the camera were excluded from the length measurement. For each detected nanotube, the number of emitted photons Φ_{NT} was measured as a proxy for the contour length l . Briefly, two rectangular region of interests R_1 and R_2 were selected manually to satisfy these criteria: (i) the nanotube of interest was the only detected feature inside R_1 and (ii) R_1 was well inside R_2 . Then, the mean local background φ_B was calculated by $\varphi_B = (\Phi_2 - \Phi_1)/(A_2 - A_1)$, where Φ_1 and Φ_2 are the sum of all pixel intensities in R_1 and R_2 , respectively, and A_1 and A_2 are the areas of regions R_1 and R_2 , respectively. The number of photons emitted by a nanotube was determined to be $\Phi_{NT} = \Phi_1 - \varphi_B A_1$. Finally, in each image, the contour length and photon numbers of the longest nanotube (whose length, $l > 3 \mu\text{m}$, could be easily measured) provided a calibration factor for the linear conversion of Φ_{NT} to l . This technique is robust to the curvature of DNA tubes and to the image sharpness. Moreover, the photon-counting method allows for the determination of nanotube lengths even for fragments that are not optically resolved.

In other experiments, our prism-based TIRF microscope proved capable of detecting single Cy3 molecules. Despite this sensitivity, here we obtained very low false-positive detection rates with our experimental procedure, as indicated by the counts of short nanotubes at early times (before 2 min of bubbling) that are plotted in Fig. 4C. On the other hand, we cannot exclude the possibility that some DNA nanotubes, e.g., those shorter than 1/32 μm , did not stick as readily to the RCA-cleaned glass, or were not counted due to photobleaching. However, the constancy of total measured tube length (Fig. 4A) suggests that this effect was not significant. Furthermore, if our experimental methods undercounted short nanotubes, then an even larger maximal elongational rate could be inferred than what we have reported here, making our reported value a lower bound.

Ocean Water. The ocean water was collected from a rock breakwater in San Buenaventura State Beach in Ventura, California. For use in the experiments, a 1-mL sample of ocean water was filtered through a Millex-GP filter unit (Millipore, 0.22- μm pore size) using a syringe.

ACKNOWLEDGMENTS. The authors gratefully acknowledge Rebecca Schulman, Damien Woods, Paul Rothmund, Carter Swanson, Manu Prakash, John O. Dabiri, and Sandra Troian for helpful discussions. This work was supported by the National Science Foundation through Grants EMT-0622254, NIRT-0608889, CCF-0832824 (The Molecular Programming Project), and CCF-0855212.

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