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The risk of incomplete personal protection coverage in vector-borne disease

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Personal protection (PP) techniques, such as insecticide-treated nets, repellents and medications, include some of the most important and commonest ways used today to protect individuals from vector-borne infectious diseases. In this study, we explore the possibility that a PP intervention with partial coverage may have the counterintuitive effect of increasing disease burden at the population level, by increasing the biting intensity on the unprotected portion of the population. To this end, we have developed a dynamic model which incorporates parameters that describe the potential effects of PP on vector searching and biting behaviour and calculated its basic reproductive rate, R_0 . R_0 is a well-established threshold of disease risk; the higher R_0 is above unity, the stronger the disease onset intensity. When R_0 is below unity, the disease is typically unable to persist. The model analysis revealed that partial coverage with popular PP techniques can realistically lead to a substantial increase in the reproductive number. An increase in R_0 implies an increase in disease burden and difficulties in eradication efforts within certain parameter regimes. Our findings therefore stress the importance of studying vector behavioural patterns in response to PP interventions for future mitigation of vector-borne diseases.

1. Introduction

The collective human mortality rate due to vector-borne diseases is estimated to be more than 1.5 million per annum [[1](#page-5-0)]. Important examples include malaria, dengue, leishmaniasis, yellow fever, Lyme disease and the West Nile virus [[2](#page-5-0)–[5\]](#page-5-0).

One of the most important measures of the risk of infectious disease outbreak is the basic reproductive rate, R_0 . R_0 measures the average number of secondary infections caused by a single infection in a naive host population. R_0 thus establishes a threshold criteria for disease invasion; a disease has the potential to invade a population if $R_0 > 1$, and is unable to persist when R_0 < 1 [[6](#page-5-0)–[9\]](#page-5-0). In general, the higher R_0 is, the more difficult it will be to eradicate the disease [[6](#page-5-0)]. In this study, we explore how personal protection (PP) interventions that protect a portion of individuals in the community affect R_0 .

We use PP to refer broadly to interventions that operate at the individual or household level (rather than the community level), whether or not they kill the vectors in addition to their individualistic protection. Examples include the use of medication, personal use of insect repellent and bednets, including insecticide-treated nets (ITN) [\[10](#page-5-0)-[14](#page-5-0)]. Residual spraying of households can also be considered as PP by our definition, if application decisions are made at the household level.

In most applied interventions, only a portion of the population receives or uses a suggested treatment. Although PP provides direct benefits to protected individuals, its population-level effects can be complex and may not always be beneficial in cases where its coverage is not complete. For example, the use of insect repellents by only a part of the population (the treated group, TG) can increase the number of bites on untreated individuals (untreated group, UTG), as repelled vectors seek alternative hosts [[15\]](#page-5-0). When bites are concentrated in a fraction of the host population, the disease risk of the entire population, as represented by R_0 , may increase [[11,16](#page-5-0)-[22](#page-5-0)]. The fact

Figure 1. The different possible effects of PP given to the TG on the disease risk of the UTG and the entire host population. Solid and dashed arrows denote whether the outcome is obligatory or not, respectively. (Online version in colour.)

that certain treatments which benefit the TG may indirectly harm the UTG is of interest, since it raises ethical concerns that may limit their usage. An even more troubling scenario is when a PP harms the UTG to such a degree that the overall net effect is an increase in disease risk for the entire population. The possible outcomes of a partial treatment coverage given to a population are summarized in figure 1.

In this study, we apply a model that was originally designed to analyse a system with two host species and one vector species [[20,23,24](#page-5-0)] to a single host population divided into two different groups, the TG and the UTG, and develop it to account for possible effects of PP on vector biting patterns. The goal is to analyse how partial PP coverage affects R_0 under different assumptions about the vector behavioural patterns, in particular, its response to ITN, bednets and insect repellents. The analysis of R_0 identified the conditions under which partial PP coverage will either increase or decrease it.

2. Model outlines

We explore how the basic reproductive number, R_0 , depends on individual-level treatment with variable coverage rates of the host population. To calculate R_0 , we modified a previously developed modelling framework [[20,24\]](#page-5-0) originally designed for multiple host species, to consider different host types—specifically hosts receiving (TG) and not receiving (UTG) PP treatments. We chose this model because it is a relatively simple framework that includes the details we need to explore the effects of PP on R_0 . Our model considers only one host species: in particular, we do not account here for the possibility that vectors divert from biting human hosts to bite domestic animals or other non-human targets.

The model quantifies the dynamics of the susceptible, infected and removed compartments of the TG and the UTG (denoted by the subscripts T and U, respectively). By using the next-generation-operator technique, we calculate the expression of R_0 from the model equations [\[7\]](#page-5-0) (see the electronic supplementary material for the model description and equations):

$$
R_0 = V \left(\frac{k_{\rm T}^2 p_{\rm T} q_{\rm T}}{N_{\rm T} \delta_{\rm T} d} + \frac{k_{\rm U}^2 p_{\rm U} q_{\rm U}}{N_{\rm U} \delta_{\rm U} d} \right) = \frac{V}{d} \left(\frac{k_{\rm T}^2 g_{\rm T}}{N_{\rm T}} + \frac{k_{\rm U}^2 g_{\rm U}}{N_{\rm U}} \right). \tag{2.1}
$$

In equation (2.1), $g_i = p_i q_i / \delta_i$ is the transmission ability of host group i ($i = T$ or U), defined as the product of probability of transmission to a vector p_i , probability of transmission from a vector q_i and the infectiousness duration $(1/\delta_i)$ see [table 1](#page-2-0) for parameters definitions) [\[20](#page-5-0)]. V and d are the density and the death rate of the vector, respectively, k_i is the vector biting rate (number of bites per vector per unit time) on hosts belonging to group *i*, and N_i is host group *i* density. In equation (2.1), we assumed frequency-dependent biting (i.e. the biting rate of an individual vector is independent of the host total population density, $N = N_T + N_U$, see the electronic supplementary material). In general, the assumption of frequency-dependent biting leads to a decrease in R_0 when host population size increases while vector density remains constant, since bites are then distributed on more host individuals, thus reducing the frequency at which individual hosts are bitten [[25,26\]](#page-5-0). Similar expressions of R_0 have been obtained in the past for both, metapopulation [[16\]](#page-5-0) and multi-host models [\[20](#page-5-0),[26\]](#page-5-0). The current model builds on these by modelling the factors affecting the biting rates k_i , as elaborated below.

We adapt a 'classical' saturated (Holling type II) functional response to calculate vector biting rates on each type of host [\[27](#page-5-0)-[29](#page-5-0)]. The type II functional response is a wellknown model that has been successfully applied to various consumer – resource systems [[30\]](#page-5-0), and which provide a natural basis to model the way vector bites are distributed as a function of searching efficiencies, host densities and handling times with respect to each group. Under these assumptions (see the electronic supplementary material), it can be shown that the vector biting rate on host group *i*, k_i [[27,28,30](#page-5-0)] is given by:

$$
h_i = h_{i1} + h_{i2} + \frac{1 - \beta_i}{\beta_i} h_{i2},
$$
\n(2.2*a*)

$$
A_i = a_i \beta_i \tag{2.2b}
$$

and $k_i = \frac{A_i N_i}{A_T h_T N_T + A_U h_U N_U}$ $(2.2c)$

where

$$
\beta_i = 1 - \exp\left(\frac{-h_{i2}}{b_i}\right). \tag{2.3}
$$

In equation (2.2*a*), h_{i1} ($i = T$ or *U*), the post-biting handling time, is the time the vector spends in handling host i after it has been successfully bitten. Biologically, h_{i1} may include the time the vector needs for (a) resting and digesting the blood meal, (b) egg production, (c) searching for a proper incubation site and (d) laying eggs. h_{i2} is the pre-biting handling time, that is, the time the vector is occupied by an individual host when flying around and trying to locate a biting site. h_i in equation $(2.2a)$ represents the total handling time, that is, the average time the vector needs to spend in handling a single bite from hosts in group *i*; h_i is a weighted sum of the time the vector spends in handling a successful bite ($h_{i1} + h_{i2}$ = the pre- and the post-handling times) and associated in unsuccessful attempts (h_{i2} = the pre-biting handling time, equation (2.2*a*)). β_i (equation (2.3)) is the probability that a biting attempt on a host from group i will be successful. We assumed that the pre-biting time h_{i2} is exponentially distributed with mean, b_{i} , the protection time, which measures the mean time it takes the vector to achieve a successful bite on group *i*. A_i in equation (2.2b) represents the general searching efficiency, that is the average biting rate the vector has when foraging in a population of unit density $(N_i = 1)$ neglecting all handling

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times (i.e. when $h_{i1} = h_{i2} = 0$), thus, a_i can be interpreted as the attractiveness of group i to the vectors.

To model treatments that may kill the vectors, we assume that the killing acts to decrease the vector longevity, or alternatively, increase its death rate, d (provided that its life expectancy is exponentially distributed) [[31\]](#page-5-0). As a simple approximation for simulation purposes, we assume that d depends bilinearly on the time the vector is exposed to the pesticide, h_{T2} , and the TG coverage rate x:

$$
d = d_0 + \eta h_{\text{T2}} x. \tag{2.4}
$$

where, d_0 is the basal vector death rate without the killing treatment, and η is a constant representing the treatment killing efficiency; it is zero when the treatment does not kill the vector and positive when it does. From the above, $N_T = xN$, $N_u = (1 - x)N$, where N is the total host population density $(N = N_T + N_U)$. With the aid of equations (2.1)–(2.4), $R₀$ can be written as:

$$
R_0(x) = \frac{V(x) e^{-dL} [g_T A_T^2 x + g_U A_U^2 (1 - x)]}{dN [A_T h_T x + A_U h_U (1 - x)]^2}
$$

=
$$
\frac{r e^{-(d_0 + \eta h_{T2} x)L} [g_T A_T^2 x + g_U A_U^2 (1 - x)]}{(d_0 + \eta h_{T2} x)^2 N [A_T h_T x + A_U h_U (1 - x)]^2}
$$
(2.5)

where $V(x)$ is the vector population size when a proportion x of the population is treated. In cases where the treatment does not kill the vectors, $V(x)$ is expected to be constant (assuming that the vector population is at equilibrium), when $\eta > 0$, $V(x)$ may decrease with x (it can be, of course, that a treatment, such as ITN, does not substantially affect the vector population size) [\[31](#page-5-0)]. From the model equations (electronic supplementary material, equation S1), the vector equilibrial population is r/d , where r is the vector's fixed birth rate that is assumed to be limited by other factors in the habitat (e.g. incubation sites, etc.). The expression r/d enables us to calculate the decrease in the vector population size due to the killing effect of ITN via d in equation (2.4). We add the factor $exp(-dL)$ to equation (2.1) and obtain equation (2.5) to account for the decrease in R_0 due to a possible vector latency period, L. This factor represents the probability that an infected vector will survive the fixed latent period, L, and becomes infectious [[6](#page-5-0),[31](#page-5-0)]. Definitions of all model parameters can be found in table 1.

Every PP can be characterized by different sets of the model parameters (e.g. A_T , A_U , h_T , h_U , etc.; see also table 1 and equation (2.5)). In this research, we will concentrate mainly on the effects of bednets, ITN, and insect repellents used by individuals, on R_0 . The main goal of this study is to explore the conditions under which these PP techniques will reduce R_0 below its value in an otherwise untreated population, i.e. solving the inequality:

$$
R_0(x) < R_0(0), \tag{2.6}
$$

Figure 2. The dependence of R_0 on coverage rate. Purple horizontal line: R_0 for a naive (untreated) population (i.e. $R_0(x = 0)$). Blue line: $h_T = 0.5$, $h_U = 0.25$, $A_T = A_U = 0.1$ and $x_t = -2$ (see the electronic supplementary material). R_0 decreases with every TG proportion thus any PP coverage is beneficial to the population. Red and black lines: $A_T = 0.1$, $A_U = 5$, $h_T = 0.5$, $h_{\text{U}} = 0.06$ and $x_{\text{t}} = 0.96$ and $A_{\text{T}} = 0.1$, $A_{\text{U}} = 5$, $h_{\text{T}} = 0.5$, $h_{\text{U}} = 0.03$, and $x_t = 0.75$, respectively. R_0 decreases with every TG proportion $x > x_t$ and increases with $x < x_t$. In all graphs $g_T = g_U$, $\eta = 0$ and $R_0(x = 0) =$ $r g_{\sf U}$ exp($-d_{\sf 0} L$)/ $(d_{\sf 0}^2 N h_{\sf U}^2) = r g_{\sf T}$ exp($-d_{\sf 0} L$)/ $(d_{\sf 0}^2 N h_{\sf U}^2) = 1.5$. When $R_{\sf 0} < 1$, the disease is extinguished. (Online version in colour.)

where $R_0(x)$ is R_0 when a proportion x of the population is treated (equation (2.5)) and $R_0(0) = R_0(x = 0) = resp(-d_0L)$ $g_u/(d_0^2 N h_U^2)$ (equation (2.5)).

3. Results

3.1. General consideration

In general, the response of R_0 to PP coverage takes two main forms depending on model parameters (figure 2): (i) the net effect of the PP always decreases R_0 , or (ii) PP increases R_0 if the TG proportion is below a certain threshold x_t , and decreases R_0 thereafter (figure 2). A detailed analysis of equation (2.5), including an expression of the threshold x_t for $\eta = 0$ can be found in the electronic supplementary material. When R_0 is near 1, an increase in it will generally result in an increased population morbidity.

Figure 2 demonstrates that for the chosen parameters, R_0 can reach 2.70 for coverage of 80%, exceeding the value for the untreated population by more than 80% ($R_0(x = 0) =$ 1.5). As such an increase can lead to dramatic rise in disease burden, we will explore how common PP techniques affect the model parameters, and consequently $R_0(x)$, thus enabling us to link between different PP and the behaviour of $R_0(x)$ exemplified in figure 2.

3.2. The dependency of R_0 on the use of bednets, insecticide-treated nets and insect repellents

Insect repellents may affect the time the vector spends in trying to bite a host from the treated group, once located, h_{T2} (the prebiting time); the vector may spend less time in trying to bite a host with repellent, or alternatively, it may spend more time around a host with repellent in trying to locate an untreated skin area. The repellent also increases the protection time, b_T , and it may also make the host less attractive from a distance, thus decreasing a_T (equation (2.2b)). Likewise, bednets may affect h_{T2} ; they can increase or decrease it, depending on whether nets cause the vectors to give up a protected host quickly, or alternatively, cause them to spend more time in trying to find holes or proximal body parts. Nets also increase b_T , the protection time. If bednets are also impregnated with insecticide (ITN), they also increase η , and consequently the killing rate, d (equation (2.4)). [Figure 3](#page-4-0) illustrates how the form of $R_0(x)$ (the dependency of R_0 on coverage rate, x, as exemplified in figure 2) varies over the parameter space of h_{T2} , b_{T} and η . To the best of our knowledge, there are insufficient data available to estimate these parameters with accuracy. We therefore use upper bounds of several days for h_{T2} and b_T —the life expectancy and egg production time of many vectors species [[32\]](#page-5-0). We have also set $d_0 = 0.088 \text{ d}^{-1}$ and $L = 0.1 d^{-1}$, the death rate and the latency period of typical Anopheles spp. (malaria vectors) [\[6,31\]](#page-5-0). We have chosen a range of η between 0 (bed nets without killing effect) and 0.3. When $\eta = 0.3$, the vector equilibrial population, r/d (equation (2.5)) decreases by 23%, an upper bound for a population decrease due to ITN according to a field study on Anopheles albimanus [[33\]](#page-5-0). [Figure 3](#page-4-0) is thus intended to point out on general principles, not to provide quantitative information.

[Figure 3](#page-4-0) shows parameter ranges where partial PP coverage can increase R_0 (yellow area). The border between the green and the yellow areas shows critical values of the prebiting and protection times (h_{T2} and b_{T_f} respectively). For example, when $\eta = 0.03$ and the pre-biting time, $h_{T2} = 0.39$ days ([figure 3](#page-4-0)b), there exists a critical value of the TG protection time, $b_{\text{To}} = 1.7$ days, for which PP reduces R_0 at any coverage level if the protection time is less than b_{Tc} (green area), but increases R_0 below a threshold coverage level when the protection time is longer than b_{Tc} (yellow area). Thus, if it is harder for the vectors to successfully bite treated hosts (i.e. b_T increases), the disease risk for the entire population may increase when R_0 is near the threshold value of 1. This is because when b_T is long, vectors are more likely to be diverted from treated to untreated hosts, concentrating more bites per capita on the UTG.

Other parameters behave similarly. When pre-biting time h_{T2} is large, R_0 decreases for every coverage rate (green zone), and if it is large enough (e.g. $h_{T2} > h_{T2c} = 1.17d$, [figure 3](#page-4-0)a), this decrease is independent of the value of b_T . The killing parameter, η , has a critical value as well; the higher it is, the wider the parameter range of b_T and h_{T2} under which R_0 decreases for every PP coverage. If a PP intervention has very strong killing ability (i.e. η is high), then it can decrease R_0 irrespective of the coverage rate over the whole range of h_T and b_T we studied (in the simulations of [figure 3,](#page-4-0) this occurs, for example, when η > 11, data not shown).

4. Discussion

In this study, we have investigated the effects of partial PP coverage and found that under some circumstances, it is plausible that partial coverage with popular PP techniques used today, such as ITN, bednets and repellents, can lead to substantial increases in the reproductive number, R_0 . This result is similar to the diversity amplification effect which occurs due to vector preference towards specific host

Figure 3. The effect of PP with various vector pre-biting, h_{D} , and protection, b_{L} times, respectively, and killing ability, η (all times are in days) on the qualitative behaviour of R_0 as function of the proportion of the treated group within the population. In green: the treatment always decreases R_0 . In yellow, the treatment increases R_0 below a threshold coverage rate, and decreases R_0 above it. In all simulations, $g_{\rm T}=g_{\rm U}$, $h_{\rm T1}=$ 3, $h_{\rm U}=$ 3, $a_{\rm T}=a_{\rm U}$, $L=$ 0.1 d $^{-1}$, $d_0=$ 0.088 d $^{-1}$, i.e. the treatment does not affect the host transmission ability and the attractiveness to vectors. (Online version in colour.)

species in a two-species community [[20\]](#page-5-0). In both cases, an increase in R_0 occurs when vectors divert from one host group (TG or less preferred host species) to the other (the UTG or the preferred host species).

Previous models have pointed out the potential negative effects that partial bednet coverage can have due to diversion of vectors from the TG to the UTG, when combined with low killing efficiency [[11,21,34](#page-5-0)]. The effects estimated, however, were very low, particularly at the level of the entire population [\[11,31](#page-5-0),[32\]](#page-5-0). It has also been speculated that total population morbidity could increase with increased bednet coverage in a case where bednets were combined with vaccines that could affect the population immunity of specific vulnerable host groups [[35\]](#page-5-0). Field studies, however, praise the use of ITN for their success in reducing malaria incidence, or in decreasing other important metrics of disease risk (e.g. entomological inoculation rate, human biting rate and vector population) [[36](#page-5-0)–41].

This study is the first to systematically explore the effect of partial PP coverage on R_0 over a wide range of plausible parameters, and the first to find a potential for substantial increase in population-level risk; when R_0 is near its threshold (i.e. 1), any increase in it is expected to lead an increased population-level morbidity. It is important to note, however, that when morbidity and force of infection are high, an increase in R_0 caused by protecting part of the population will not always be expected to increase population-level morbidity, since the effects of increasing R_0 would be outweighed by the direct effect of protecting part of the population. Yet, the increase in R_0 in these cases may still lead to an increased risk in a portion of the population.

Our model makes the subtle yet important distinction between protection and diversion [\[11,21,31\]](#page-5-0). In previous studies, both diversion and protection have been related to the probability that a vector will give up a protected host and turn to look for another victim [[11,21,31](#page-5-0)]. In the present framework, however, diversion is equivalent to the time duration the vector spends in trying to bite a protected host, h_{T2} , that is, its pre-biting time. The shorter the pre-biting time, h_{T2} , the stronger the diversion effect of the respective PP. The protection, b_T , in our model, is equivalent to the mean time the vector needs for a successful biting attempt of a protected host, irrespective of the time the vector actually spends in that attempt (h_{T2}) . In our study therefore, protection and diversion are two independent properties, and hence may be affected differently by different PP interventions. Figure 3 demonstrates the counterintuitive dependency of R_0 on protection due to this differentiation; a more protective PP can increase R_0 when the vector pre-biting handling time, h_{T2} , is short, and the coverage rate is below a certain threshold. For longer h_{T2} , however, every PP coverage reduces R_0 (figure 3). Consequently, an increase in R_0 may therefore occur due to a change in the vector foraging behaviour. If vectors switch quickly on encountering nets (or on encountering ITNs), the pre-biting time, h_{T2} , will decrease, and consequently R_0 will increase for some levels of coverage (assuming high enough protection times, figure 3). Such a change of the vector behaviour is realistic. Avoiding landing on ITNs and spending less time in trying to bite protected individuals are traits that can increase vector longevity and fitness, and thus may spread within the population relatively fast. Changes in vector behaviour correlated with ITN usage have already been observed: mosquitoes change their activity time, host species (from human to livestock) and feeding site (indoor or outdoor) within several years in high coverage areas [[39,42](#page-6-0)–[45\]](#page-6-0). Unfortunately, to the best of our knowledge, there are no field or laboratory measurements regarding the time allocation used by vectors while foraging for potential hosts.

This study expands on previous work by supplementing simulation-based exploration of the various effects of PP on disease burden with analytical results on R_0 , thus increasing generality and providing a better mechanistic understanding [[46\]](#page-6-0). Our results are most applicable to cases where R_0 is near its threshold (i.e. 1). Under such circumstances, an increase in morbidity may occur for PP partial coverage rates if certain vector behavioural patterns exist, especially a decrease in its pre-biting handling time. This study, therefore, stresses the

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importance of field research on the vector's time allocation to foraging for potential hosts and its relation to the PP techniques widely used today for future elimination and mitigation of vector-borne infectious diseases.

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