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Quantum transport of two-species Dirac fermions in dual-gated three-dimensional topological insulators

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Topological insulators are a novel class of quantum matter with a gapped insulating bulk, yet gapless spin-helical Dirac fermion conducting surface states. Here, we report local and non-local electrical and magneto transport measurements in dual-gated BiSbTeSe₂ thin film topological insulator devices, with conduction dominated by the spatially separated top and bottom surfaces, each hosting a single species of Dirac fermions with independent gate control over the carrier type and density. We observe many intriguing quantum transport phenomena in such a fully tunable two-species topological Dirac gas, including a zero-magnetic-field minimum conductivity close to twice the conductance quantum at the double Dirac point, a series of ambipolar two-component half-integer Dirac quantum Hall states and an electron-hole total filling factor zero state (with a zero-Hall plateau), exhibiting dissipationless (chiral) and dissipative (non-chiral) edge conduction, respectively. Such a system paves the way to explore rich physics, ranging from topological magnetoelectric effects to exciton condensation.

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A three-dimensional (3D) topological insulator (TI) is characterized by an insulating bulk band gap and gapless conducting topological surface states (TSS) of spin-helical massless two-dimensional (2D) Dirac fermions^{1,2}. Such surface states are topologically non-trivial and protected by time-reversal symmetry, thus immune to back scattering. The potential novel physics offered by this system, such as topological magnetoelectric (TME) effects^{3,4}, Majorana fermions⁵ and effective magnetic monopoles⁶, has drawn intense interest. One of the most iconic transport signatures for 2D Dirac electronic systems is the half-integer quantum Hall effect (QHE) in a perpendicular magnetic field (B), as first observed in graphene^{7,8} and later also studied in HgTe^{9,10}. The Landau levels (LLs) of 2D Dirac fermions have energies $E_N = \text{sgn}(N)v_F(2eB\hbar|N|)^{1/2}$, where sgn is the sign function, N is the LL index (positive for electrons and negative for holes), v_F is the Fermi velocity, e is the elementary charge and \hbar is the Planck's constant h divided by 2π . The zeroth LL at $E_0 = 0$ is equally shared between electrons and holes, giving rise to the half-integer shift in the quantized Hall conductivity $\sigma_{xy} = g(N + 1/2)e^2/h$, where g is the number of degenerate species of Dirac fermions (for example, $g = 4$ for graphene, and $g = 1$ for TSS with a single Dirac cone). This $1/2$ can also be related to the Berry-phase due to the spin or pseudospin locking to the momentum of Dirac fermions⁷⁻¹⁰.

In most commonly studied TI materials such as Bi₂Se₃, Bi₂Te₃ and other Bi/Sb-based chalcogenides, it is often challenging to observe characteristic TSS transport (particularly QHE) due to bulk conduction caused by unintentional impurity doping. Only very recently has well-developed QHE arising from TSS been observed in exfoliated flakes from BiSbTeSe₂ (BSTS) single crystals¹¹ and molecular beam epitaxy grown (Bi_{1-x}Sb_x)₂Te₃ or Bi₂Se₃ thin films^{12,13}. In this work, we fabricate dual-gated¹⁴⁻¹⁶ TI devices from exfoliated BSTS thin flakes with undetectable bulk carrier density and conduction at low temperature¹¹. Such a dual-gating structure is also promising for exploring exciton condensation proposed for TIs¹⁷ and topological quantum phase transitions induced by displacement electric field¹⁸.

In our dual-gated BSTS devices, the independent, ambipolar gating of parallel-conducting top and bottom surfaces realize two independently controlled species of 2D Dirac fermions, allowing us to investigate such interesting transport phenomena as the minimum conductivity of TSS at Dirac point (DP), and two-species (two-component) Dirac fermion QHE of electron + electron, electron + hole and hole + hole types, involving various combinations of top and bottom surface half-integer filling factors ν_t and ν_b , respectively. When $(\nu_t, \nu_b) = (-1/2, 1/2)$ or $(1/2, -1/2)$, there's an intriguing $\nu = 0$ state characterized by zero-Hall plateau and a large longitudinal resistance peak^{11,12}, attributed to the formation of dissipative and non-chiral edge states. We also perform non-local transport measurements and compare them with the normal local measurements in our dual-gated 3D TI devices in the quantum Hall (QH) regime to probe the nature of edge-state transport for both standard QH states and the novel $\nu = 0$ dissipative QH-like state. We further demonstrate that the dissipative edge states at $\nu = 0$ have temperature-independent conductance, revealing that the transport in such a quasi-one-dimensional (1D) dissipative metallic edge channel could evade standard localization.

Results

Transport properties at zero and low magnetic field.

Qualitatively, similar data are measured in multiple samples, while results from a typical sample A (channel length $L = 9.4 \mu\text{m}$, width $W = 4.0 \mu\text{m}$, with $\sim 100 \text{ nm}$ -thick BSTS and 40 nm -thick h-BN as top-gate dielectric, see schematic in Fig. 1a) are

presented below unless otherwise noted. The h-BN as a substrate or gate dielectric is known to preserve good electronic properties for graphene, resulting from the atomic flatness and relatively low density of impurities in h-BN¹⁹. The carrier densities of the top and bottom surface of the BSTS flake are tuned by top-gate voltage V_{tg} and back-gate voltage V_{bg} , respectively.

Figure 1b,c shows the double-gated electric field effect measured at $T = 0.3 \text{ K}$. The longitudinal resistivity ρ_{xx} ($= R_{xx} \times W/L$, with R_{xx} being longitudinal resistance) at magnetic field $B = 0 \text{ T}$ (Fig. 1b) and Hall resistivity ρ_{xy} ($= R_{xy}$, Hall resistance) at $B = 1 \text{ T}$ (Fig. 1c) are plotted in colour scale as functions of both top and bottom gate voltages (V_{tg} and V_{bg}). The extracted field effect and Hall mobilities are typically several thousands of $\text{cm}^2 \text{V}^{-1} \text{s}^{-1}$. A minimum carrier density $n^* \sim 9 \times 10^{10} \text{ cm}^{-2}$ per surface can be extracted from the maximum Hall coefficient (absolute value) $\sim 3.5 \text{ k}\Omega \text{ T}^{-1}$ (when both surfaces are slightly n-type or p-type) measured in Fig. 1c. A set of exemplary V_{tg} -sweeps with $V_{bg} = 3 \text{ V}$ is shown in Fig. 1c inset. By adjusting V_{tg} (or V_{bg}), the device can be gated through a R_{xx} peak, identified as the charge-neutrality DP of the top (or bottom) surface, marked by the blue (or red) dashed lines in Fig. 1b. Gating through the DP, the carriers in the corresponding surface change from hole-like to electron-like (that is, ambipolar), as evidenced by Hall measurements (Fig. 1c). The slight deviation of the two lines from being perfectly vertical and horizontal arises from the weak capacitive coupling between the top (bottom) surface and the back (top) gate¹⁶. The crossing of these two lines corresponds to the double DP (both surfaces tuned to DP), where ρ_{xx} ($\sigma_{xx} = 1/\rho_{xx}$) reaches a global maximum (minimum). Within the gate voltage range used, the carriers predominantly come from the TSS and we observe relatively good particle-hole symmetry in the transport properties (for example, the symmetrical appearance of ρ_{xx} on both sides of DP in each surface in Fig. 1b and the similar absolute values of the positive and negative maximum Hall coefficient in Fig. 1c).

We have studied six dual-gated BSTS devices with different thicknesses (t) and aspect ratios (L/W). These devices are measured at low temperatures ($T < 2 \text{ K}$) and the results are repeatable after multiple thermal cycles. When both surfaces are tuned to DP, the minimum 2D conductivity σ_{min} at $B = 0 \text{ T}$ exhibits relatively constant value $(3.8 \pm 0.1)e^2/h$ for all the devices measured (with the uncertainty representing 90% confidence interval), whose thicknesses range from ~ 50 to $\sim 200 \text{ nm}$ and L/W range from 1.3 to 3.5 (Fig. 1d). Our observation indicates that the conductivity at the DP for each major surface (top or bottom) is $\sim 2e^2/h$ (one unit of conductance quantum), within the range of values ($2 \sim 5 e^2/h$) reported by Kim *et al.*¹⁴ on thin flakes of Bi₂Se₃ ($\sim 10 \text{ nm}$). The better consistency over multiple samples in our dual-gated BSTS devices may be attributed to the more insulating bulk (whose conduction is immeasurably small at low temperature) and uniformity of the exfoliated BSTS flakes, which are sandwiched between SiO₂ and h-BN to achieve better device stability. The minimum conductivity at DP has also been discussed in graphene with considerable interest²⁰⁻²⁵.

The experiments in graphene revealed that the minimum conductivity is strongly affected by carrier-density inhomogeneities (puddles) induced by disorder or near graphene^{24,25}, such as the adsorbates or charged impurities in the substrates. In 3D TIs, one source of impurities likely relevant to the observed quasi-universal minimum conductivity in our dual-gated BSTS devices could be bulk defects (located near surface)^{26,27}, such as those revealed in scanning tunnelling microscopy studies²⁸.

Two-component QHE. For the rest of the paper, we focus on the transport phenomena in the QH regime under a high magnetic

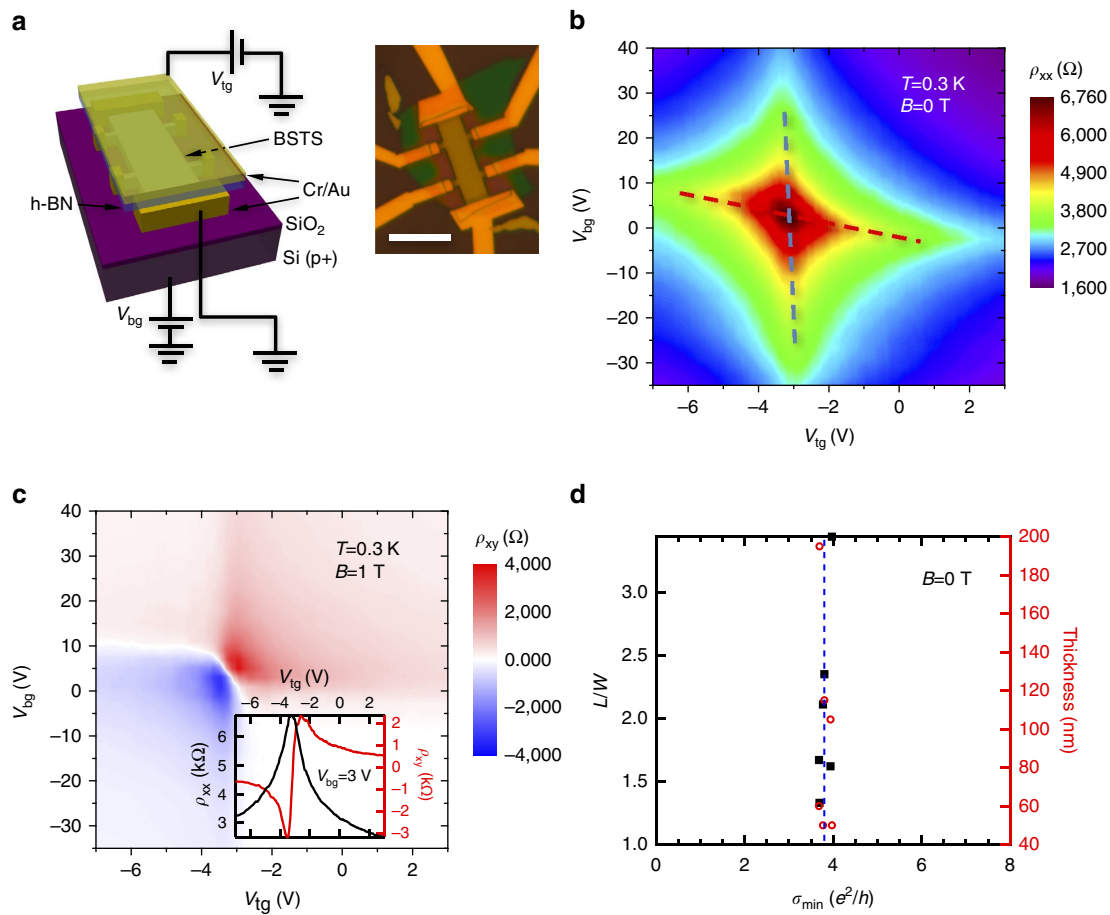


Figure 1 | Device configuration and dual-gated field effect at zero and low magnetic field. (a) Device schematic. Inset is an optical microscope image of a typical dual-gated BSTS device before depositing the top-gate metal; Scale bar, 10 μm . (b,c) show 2D maps of ρ_{xx} at $B=0$ T and ρ_{xy} at $B=1$ T as functions of V_{tg} and V_{bg} on sample A. The blue (red) dashed lines in **b** are guides to the eye for the top (bottom) surface DP. The 2D map is generated by data measured from V_{tg} -sweeps at a series of V_{bg} values, with one example at $V_{bg}=3$ V shown in the inset of **c**. (d) Zero-magnetic-field minimum conductivity σ_{min} (bottom axis) measured in six dual-gated samples at low temperature (<2 K) plotted as a function of the sample thickness (data in circles) and 2D aspect ratio (L/W , data in squares). The vertical dashed line indicates $3.8e^2/h$.

field B perpendicular to the top and bottom surfaces. Figure 2a,c shows in colour scales the longitudinal conductivity $\sigma_{xx} (= \rho_{xx}/(\rho_{xx}^2 + \rho_{xy}^2))$ and Hall conductivity $\sigma_{xy} (= \rho_{xy}/(\rho_{xx}^2 + \rho_{xy}^2))$ for Sample A as functions of V_{tg} and V_{bg} at $B=18$ T and $T=0.3$ K. The colour plots in Fig. 2a,c divide the (V_{tg}, V_{bg}) plane into a series of approximate parallelograms, centred around well-developed or developing QH states with vanishing or minimal σ_{xx} (Fig. 2b) and quantized σ_{xy} in integer units of e^2/h (Fig. 2d). These QH parallelograms are bounded by approximately (but slightly tilted) vertical and horizontal lines, which represent the top and bottom surface LLs, respectively. By increasing (decreasing) either V_{tg} or V_{bg} to fill (exhaust) one LL on the top or bottom surface, σ_{xy} increases (decreases) by e^2/h , taking consecutive quantized values of $\nu e^2/h$, where integer $\nu = \nu_t + \nu_b = N_t + N_b + 1$. The $N_{t(b)}$ is the corresponding top (bottom) surface LL integer index that can be adjusted by top (back) gate to be of either Dirac electrons or holes. In Fig. 2d, different fixed V_{bg} values (from -17 to 40 V) set ν_b around consecutive half integers $-3/2, -1/2, 1/2, 3/2$ and $5/2$ (such that the bottom surface contributes $\sigma_{xy}^b = \nu_b e^2/h$ to the total σ_{xy}), explaining the vertical shift of e^2/h at QH plateaux of consecutive V_{tg} -sweeps.

It is also notable that in Fig. 2, there are a few states with zero-quantized Hall conductivity ($\sigma_{xy}=0$, manifesting as white regions in Fig. 2c, separating the electron-dominated regions in red and the hole-dominated regions in blue) and non-zero σ_{xx}

minimum, marked by equal and opposite half-integer values of ν_t and ν_b thus total $\nu=0$, for example $(\nu_t, \nu_b) = (-1/2, 1/2), (1/2, -1/2)$ and $(3/2, -3/2)$. These states with total $\nu=0$, exhibiting zero-Hall plateaux (see also Fig. 2d), have non-zero σ_{xx} minimum (Fig. 2a,b) but very large R_{xx} maximum (see next, Fig. 3).

Non-local transport at $\nu=0$ states. To further characterize the observed QH and $\nu=0$ states, we have performed non-local transport measurements of $R_{nl} (= V_{nl}/I, I$ is the current and V_{nl} is the non-local voltage, see the schematic measurement setup in the inset of Fig. 3b) as functions of V_{tg} and V_{bg} at $B=18$ T and $T=0.3$ K and compared the results with the standard (local) measurements of the longitudinal resistance R_{xx} (Fig. 3a). It is intriguing that unlike other QH states typified by a zero or minimum in R_{xx} , the states with $\nu = \nu_t + \nu_b = 0$ (labelled by (ν_t, ν_b) in Fig. 3a with $\nu_t = -\nu_b = \pm 1/2$ or $\pm 3/2$) are accompanied by a R_{xx} maximum. The best-developed $\nu=0$ states are those at $(\nu_t, \nu_b) = (-1/2, 1/2)$ or $(1/2, -1/2)$, where R_{xx} reaches ~ 220 k Ω ($\rho_{xx} \sim 100$ k Ω), exceeding the resistance quantum ($h/e^2 = \sim 25.8$ k Ω) by an order of magnitude. The non-local R_{nl} also becomes very large (~ 100 k Ω) and the similar order of magnitude as R_{xx} at these two $\nu=0$ states, while negligibly small at other (ν_t, ν_b) QH states (see Fig. 3b and also the representative cuts in Fig. 3c).

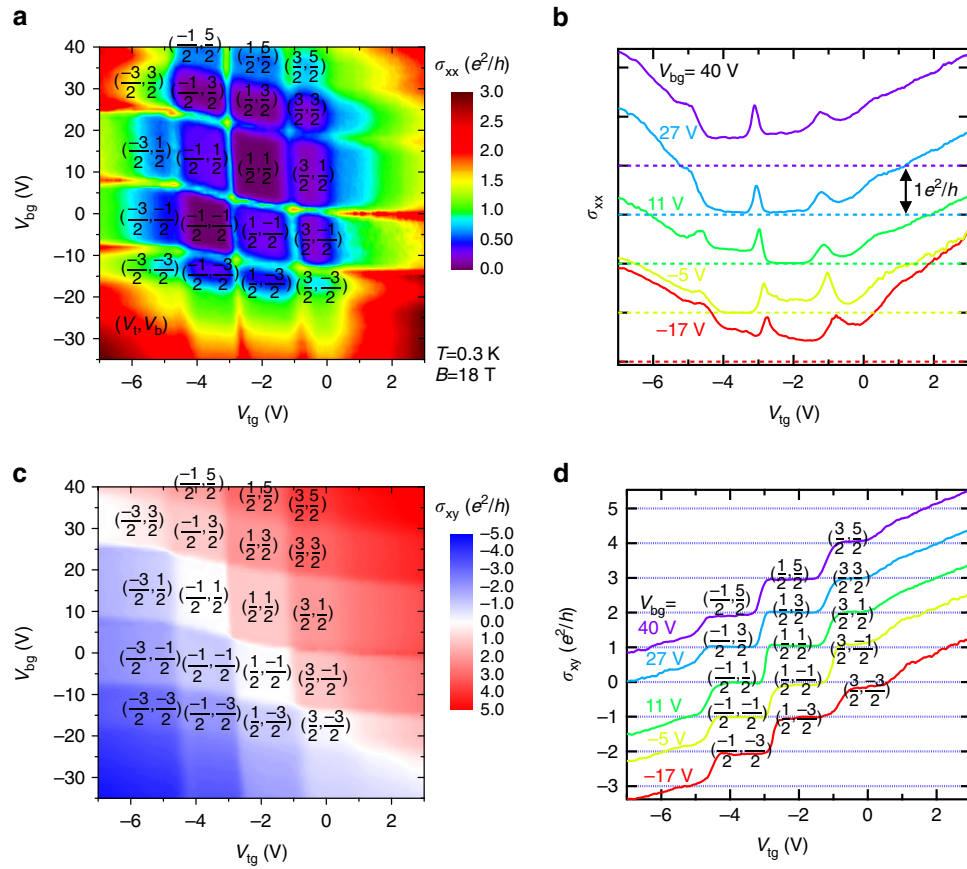


Figure 2 | QHE modulated by top and bottom gates. (a) σ_{xx} and (c) σ_{xy} , shown as 2D colour maps, as functions of V_{tg} and V_{bg} at $B = 18$ T and $T = 0.3$ K in the sample ‘A’, with representative cuts at 5 different values of V_{bg} shown in **b** and **d**. The (ν_t, ν_b) labels (top, bottom) surface filling factors for corresponding quantum Hall states. The σ_{xx} curves in **b** are shifted vertically (in consecutive step of e^2/h) for clarity (the corresponding zero σ_{xx} levels are indicated by the same-coloured horizontal dashed lines).

The simultaneously large local and non-local resistance at $\nu = 0$ states in the QH regime has been reported in other 2D electron-hole systems^{29,30} and understood in a picture of dissipative edge channels. We emphasize that the pronounced R_{nl} signal cannot be explained from R_{xx} by a classical Ohmic non-local resistance from the stray current connecting the remote leads. Such a contribution ($\sim \rho_{xx} e^{-\pi L/W}$) would decay exponentially with L/W ($= 2.4$ in our case), and be three orders of magnitude smaller than the local R_{xx} (which is the case at $B = 0$ T, Supplementary Fig. 1). As another comparison, the middle panel of Fig. 3c shows the cuts in Fig. 3a,b at $V_{bg} = 3$ V, crossing the double-DP (also zeroth LL) of both top and bottom surfaces at $(\nu_t, \nu_b) = (0, 0)$, where we observe a relatively large peak in R_{xx} but significantly smaller R_{nl} . Such a result is consistent with the ‘extended’ state transport (at the center of zeroth LL) as the current flows through the bulk of the 2D surface.

From the colour plots in Figs 2 and 3, the parallelogram centred around $(\nu_t, \nu_b) = (-1/2, 1/2)$ state is enclosed by boundaries representing $N_t = 0$ and -1 , $N_b = 0$ and 1 LLs. Similarly, the $(\nu_t, \nu_b) = (1/2, -1/2)$ state is bound by $N_t = 0$ and 1 , $N_b = 0$ and -1 LLs. We conclude that such a $\nu = 0$ state can exist when the potential difference V between top and bottom surfaces (equivalently the energy separation between top and bottom surface DPs) is in the range of $0 < |V| < 2E_{0-1}$ ($\cong 2 \times 50$ meV at $B = 18$ T, where E_{0-1} is the $0-1$ LL separation of TSS Dirac fermions¹¹). The large energy scale of E_{0-1} can help make the $\nu = 0$ and $\nu = \pm 1$ QH states observable at significantly elevated temperatures as demonstrated below.

Temperature dependence of the $\nu = 0$ and ± 1 states. We have studied the temperature (T) dependence of the QHE and $\nu = 0$ states from 0.3 K to 50 K at $B = 18$ T (Fig. 4). At each temperature, the bottom surface density is tuned by V_{bg} to set ν_b near $1/2$ (dashed lines) or $-1/2$ (solid lines), and the peaks in local R_{xx} and non-local R_{nl} corresponds to the $(\nu_t, \nu_b) = (-1/2, 1/2)$ or $(1/2, -1/2)$, respectively (Fig. 4a,b, detailed raw data are shown in Supplementary Fig. 2). The R_{xx} peaks ($> \sim 150$ k Ω) are seen to be more robust up to the highest temperature ($T = 50$ K) measured, while R_{nl} peaks decrease rapidly (approximately linearly in T , shown in Fig. 4c) with increasing T and is nearly suppressed above 50 K. We also show the T -dependence of σ_{xx} and σ_{xy} at $(\nu_t, \nu_b) = (-1/2, 1/2)$, $(1/2, -1/2)$, $(1/2, 1/2)$ and $(-1/2, -1/2)$ in Fig. 4e,f. The σ_{xy} maintains good quantization at $\nu e^2/h$ ($\nu = 0, \pm 1$) up to $T = 50$ K, while σ_{xx} increases with T (the gate-dependent σ_{xx} and σ_{xy} traces at different temperatures are shown in Supplementary Fig. 3). The σ_{xx} for $\nu = \pm 1$ states is found to show thermally activated behaviour at high temperatures¹¹, where the finite σ_{xx} is attributed to the thermally excited 2D surface or 3D bulk carriers. Such carriers can shunt the edge-state transport and suppress the non-local R_{nl} response at high T (ref. 29). We also note that the σ_{xx} versus T curves for $\nu = 0$ and $\nu = \pm 1$ states follow the similar trend and have approximately constant separation. We find the averaged separation $\Delta\sigma_{xx} = 1/2 \times (\sigma_{xx}(-1/2, 1/2) + \sigma_{xx}(1/2, -1/2) - \sigma_{xx}(1/2, 1/2) - \sigma_{xx}(-1/2, -1/2))$ to be largely T -independent with a value of $(0.27 \pm 0.01)e^2/h$, which we attribute to the conductivity of the quasi-1D dissipative edge channel.

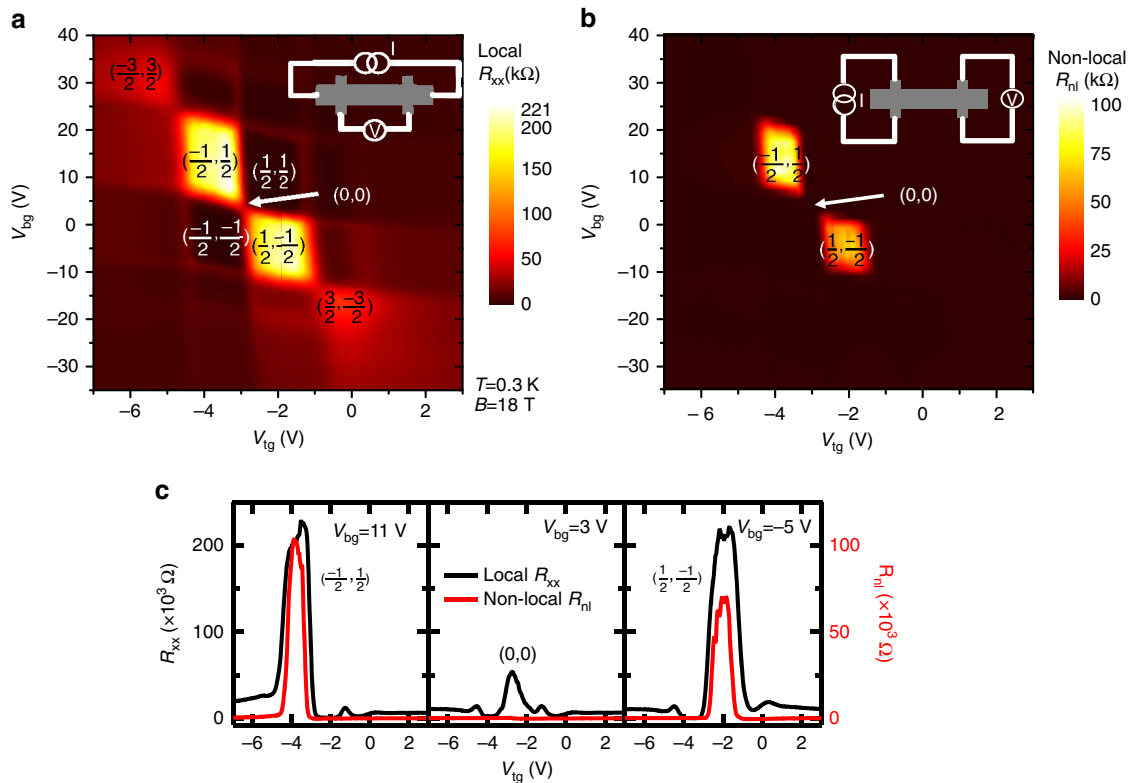


Figure 3 | Local and non-local resistance in dual-gated TI in high magnetic field. (a) Local resistance R_{xx} and (b) non-local resistance R_{nl} measured in sample A as functions of V_{tg} and V_{bg} at $B=18$ T and $T=0.3$ K, with insets showing the measurement setup schematics. (c) A few representative cuts of a and b at different values of V_{bg} . Filling factors for the local R_{xx} peaks are labeled in each sub-panel.

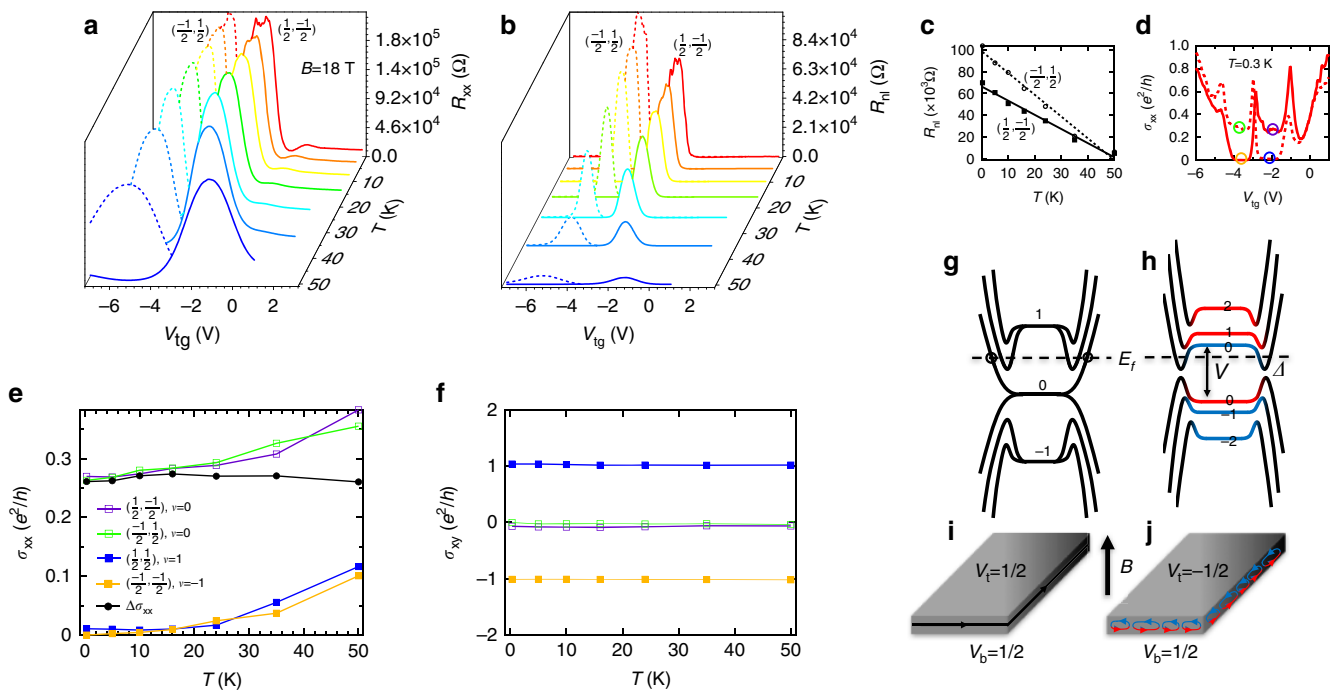


Figure 4 | Temperature dependence and illustrative schematics of the QHE and $\nu = 0$ state in TI. (a) R_{xx} and (b) R_{nl} measured in sample ‘A’ as functions of V_{tg} for different temperatures at $B=18$ T, where V_{bg} is chosen to set ν_b at $1/2$ (dashed lines) and $-1/2$ (solid lines), respectively. (c) The R_{nl} value at $(\nu_t, \nu_b) = (-1/2, 1/2)$ and $(1/2, -1/2)$ shows approximately linear dependence on temperature. (d) σ_{xx} versus V_{tg} (with the same two values of V_{bg} chosen in a and b) at $T=0.3$ K as an example, with each highlighted circle corresponding to a state in e plotted with corresponding coloured symbols. (e) σ_{xx} and (f) σ_{xy} of $\nu = +1, -1$ and 0 states as functions of temperature. In e, we also plot $\Delta\sigma_{xx}$ (difference between averaged $\nu = 0$ states’ σ_{xx} and averaged $\nu = \pm 1$ states’ σ_{xx}), which barely changes with T . (g,h) Schematics of surface band structure (energy spectrum) in high magnetic field, showing LLs from top and bottom surfaces (blue and red) in the middle of the sample transitioning into side surface sub-bands at sample edge, and (i,j) edge states in a slab-shaped sample for $\nu=1$ and $\nu=0$ states. The dashed line indicates a representative Fermi level E_f and circles in g label chiral edge modes.

Discussions

In our measurement setup, the contacts connect to the top, bottom and side surfaces, all of which are probed simultaneously. The side surface only experiences an in-plane field and can be viewed as a quasi-1D domain boundary that separates the top and bottom surfaces with B pointing outward and inward, respectively, thus can support QH edge states³¹. When the top and bottom surfaces are doped to the same carrier type (either n or p), the corresponding QH edge states (on the side surface) would have the same chirality and give the observed total $\sigma_{xy} = ve^2/h = (v_t + v_b)e^2/h$, restricted to integer multiples of e^2/h . When the two surfaces have opposite carrier types but one of them dominates, well-defined QH states with $v = v_t + v_b$ may still be observed, such as the $(-1/2, 3/2)$ state with $\sigma_{xy} = (-1/2 + 3/2)e^2/h = e^2/h$ and vanishing ρ_{xx} . Previous studies in InAs/(AlSb)/GaSb heterostructure-based electron-hole systems^{32,33} also revealed QH effect with $R_{xy} = h/(ve^2) = h/(v_e - v_h)e^2$ (v_e and v_h are electron and hole-filling factors, both are positive integers) and vanishing R_{xx} when the AlSb barrier (separating electron and hole gases) is sufficiently thin to enable electron-hole hybridization. Despite the phenomenological similarities, our QH system is distinctive in the sense that the spatially separated electrons and holes residing on the top and bottom surfaces have half-integer filling factors, and the hybridization only happens at the side surface.

We show the schematic energy spectrum when the two surfaces are degenerate with $V = 0$ (refs 34–36) in Fig. 4g, which depicts the Fermi energy E_f inside the $0 - 1$ LL gap and corresponds to the $(1/2, 1/2)$ QH state. For a relatively thick sample such as ours (~ 100 nm) magnetic length $l_B = (\hbar/eB)^{1/2} \cong 6$ nm at $B = 18$ T); however, it has been suggested that even in the presence of well-quantized LLs, a standard TI Hall measurement would exhibit deviations from perfectly quantized values due to conduction through the side surfaces^{31,34–36}. On the other hand, it has also been suggested that when net chiral modes exist (Fig. 4g,i show one such net chiral mode), the QH effect may be restored by the local equilibrium between non-chiral edge modes³⁷, possibly explaining the good quantization in σ_{xy} and vanishing ρ_{xx} (also R_{nl}) observed in our experiments.

For the $(v_t, v_b) = (-1/2, 1/2)$ or $(1/2, -1/2)$ state, the carrier density on the top and bottom surfaces are opposite. Since E_f is within the LL gap on both the surfaces, the finite residual σ_{xx} and large R_{nl} we observed are indicative of dissipative edge transport. We show a schematic energy spectrum³⁸ of this $v = 0$ state with V slightly smaller than E_{0-1} in Fig. 4h, where the Fermi level E_f resides between the $N_t = -1$ and 0 LL of top surface (marked in blue), thus $v_t = -1/2$, and also between the $N_b = 0$ and 1 LL of bottom surface, thus $v_b = 1/2$. Overall, such energy spectrum represents a $(v_t, v_b) = (-1/2, 1/2)$ and $v = 0$ state. The E_f crosses an even number (only two shown in this illustrative example in Fig. 4h) of counter-propagating edge modes (arising from sub-bands of the quasi-1D side surface). The disorder can cause scattering and local equilibrium between the counter-propagating modes, giving rise to non-chiral dissipative transport (depicted by a series of conducting loops that can hop between adjacent ones in Fig. 4j) on the side surface with a large and finite resistance. While the energy spectrum (Fig. 4h) is expected to have a gap (Δ) near the edge (due to the hybridization between top (marked with blue) and bottom (red) surface zeroth LLs and approximately the finite-size confinement-induced gap $\cong hv_f/t \cong 10$ meV opened at DP of the side surface³⁸), we did not observe a truly insulating state with vanishing σ_{xx} and diverging R_{xx} (Figs 2a and 4a). This is likely due to the disorder potential (spatial fluctuation of DP²⁸) comparable or larger than Δ and thus smearing out this gap (effectively E_f always crosses the non-chiral edge modes). It would be an interesting question for future studies to clarify whether the

weak T -dependence (at $T < \sim 50$ K) of the observed conductance (Fig. 4e), similar to the behaviour reported in InAs/GaSb based electron-hole systems³⁹, may indicate an absence of localization^{40–43} in such quasi-1D resistive edge channels.

Several recent theories have pointed out that the $v = 1/2 - 1/2 = 0$ state in the TI QH system may bring unique opportunities to realize various novel physics. It has been suggested that both the $v = 0$ state in TI QHE and an analogous quantum anomalous Hall (QAH) state with zero-Hall-conductance plateau in a magnetic-doped TI around the coercive field can be used as platforms to observe the TME effect^{44,45}, where an electric (magnetic) field induces a co-linear magnetic (electric) polarization with a quantized magnetoelectric polarizability of $\pm e^2/2h$. A zero-Hall-plateau state has been recently observed in the QAH case in ultrathin (few-nm-thick) films of $\text{Cr}_x(\text{Bi,Sb})_{2-x}\text{Te}_3$ at low temperature (< 1 K) (refs 46,47). In comparison, our samples have much larger thickness ($> \sim 50$ nm, suggested to be preferable for better developed TME effect^{45,48}), and our $v = 0$ state survives at much higher temperatures (~ 50 K). It has also been proposed that excitonic condensation and superfluidity can occur in thin 3D TIs at the $v = 0$ state in QH regime⁴⁹ (in addition to the at-zero B field¹⁷) induced by spontaneous coherence between strongly-interacting top and bottom surfaces. In future studies, much thinner samples are likely needed to investigate the possibility of such exciton superfluidity.

Methods

Sample preparation. 3D TI single crystals BiSbTeSe₂ (BSTS) were grown by the vertical Bridgman technique¹¹. BSTS flakes (typical thickness ~ 50 – 200 nm) are exfoliated (Scotch tape method) onto highly doped Si (p+) substrates (with 300 nm-thick SiO₂ coating), and lithographically fabricated into Hall bar-shaped devices with Cr/Au contacts. A thin flake of hexagonal boron nitride (h-BN, typical thickness ~ 10 – 40 nm) is transferred¹⁹ on the BSTS flake to serve as a top-gate dielectric and a top-gate metal (Cr/Au) is deposited afterwards. The thickness of BSTS and h-BN flakes are measured by atomic force microscopy.

Transport measurement. Transport measurements are performed with the standard lock-in technique using a low-frequency (< 20 Hz) excitation current of 20 nA in a helium-4 variable temperature system (with base temperature down to 1.6 K) or a helium-3 system equipped with magnetic fields (B) up to 18 T (down to 0.3 K).

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Author contributions

Y.P.C supervised the research. I.M. synthesized the crystals. Y.X. fabricated the devices, performed the transport measurements and analysed the data. Y.X. and Y.P.C wrote the paper.

Additional information

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