# Inferring the Frequency Spectrum of Derived Variants to Quantify Adaptive Molecular Evolution in Protein-Coding Genes of Drosophila melanogaster

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**ABSTRACT** Many approaches for inferring adaptive molecular evolution analyze the unfolded site frequency spectrum (SFS), a vector of counts of sites with different numbers of copies of derived alleles in a sample of alleles from a population. Accurate inference of the high-copy-number elements of the SFS is difficult, however, because of misassignment of alleles as derived vs. ancestral. This is a known problem with parsimony using outgroup species. Here we show that the problem is particularly serious if there is variation in the substitution rate among sites brought about by variation in selective constraint levels. We present a new method for inferring the SFS using one or two outgroups that attempts to overcome the problem of misassignment. We show that two outgroups are required for accurate estimation of the SFS if there is substantial variation in selective constraints, which is expected to be the case for non-synonymous sites in protein-coding genes. We apply the method to estimate unfolded SFSs for synonymous and nonsynonymous sites in a population of *Drosophila melanogaster* from phase 2 of the *Drosophila* Population Genomics Project. We use the unfolded spectra to estimate the frequency and strength of advantageous and deleterious mutations and estimate that  $\sim$ 50% of amino acid substitutions are positively selected but that <0.5% of new amino acid mutations are beneficial, with a scaled selection strength of  $N_e s \approx 12$ .

KEYWORDS adaptation; distribution of fitness effects; Drosophila; site frequency spectrum (SFS)

OST protein sequences are strongly conserved between closely related species, which suggests that most amino acid—changing mutations are selectively removed from populations (Graur and Li 2000). The nature of the selective forces acting on the mutations that become fixed between species is central to a variety of questions in population genetics. These include understanding the maintenance of variation within species, determining the causes of variation in nucleotide diversity across the genome, and discerning the nature of evolutionary adaptation. Evidence for pervasive selection in the genome comes from observations of positive correlations between nucleotide diversity at putatively neutrally evolving sites and the rate of recombination (Begun

and Aquadro 1992) and negative correlations between local genomic diversity and the presence of functional elements (such as protein-coding exons or conserved noncoding elements) (Cai *et al.* 2009; Hernandez *et al.* 2011; Lohmueller *et al.* 2011; Halligan *et al.* 2013; Enard *et al.* 2014; Deinum *et al.* 2015). These correlations are likely to be caused by natural selection acting on functional sites in the genome reducing diversity at linked sites, but the precise nature of the selective forces involved is unresolved because both selective sweeps owing to positive selection and background selection caused by purifying selection can contribute to these patterns.

One approach to discriminating between the contributions of neutral, deleterious, and advantageous substitutions to molecular evolution is based on the McDonald-Kreitman (MK) test (McDonald and Kreitman 1991), which compares within-species polymorphism to between-species divergence. Initially conceived as a test of departure from neutrality in a specific gene, it was subsequently adapted to estimate the proportion of substitutions driven to fixation by positive selection between species for a class of sites in the genome (Fay et al. 2002; Smith and Eyre-Walker 2002). It does not,

Copyright © 2016 by the Genetics Society of America doi: 10.1534/genetics.116.188102

Manuscript received February 10, 2016; accepted for publication April 18, 2014; published Early Online April 20, 2016.

Supplemental material is available online at www.genetics.org/lookup/suppl/doi:10. 1534/genetics.116.188102/-/DC1.

<sup>1</sup>Address for correspondence: School of Biological Sciences, University of Edinburgh Charlotte Auerbach Road, Edinburgh, EH9 3FL, United Kingdom. E-mail: peter.keightley@ed.ac.uk however, directly provide information on the rate of occurrence of advantageous mutations or on the magnitude of their selective effects. Furthermore, the approach is compromised if there has been a demographic change that alters the fixation probability of selected alleles (either advantageously or disadvantageously), the signature of which is not captured by analysis of the polymorphism data (Eyre-Walker 2002).

Other ways of combining polymorphism and divergence data or focusing on polymorphism data only to infer genomewide selection may be more fruitful. Andolfatto (2007) and Macpherson et al. (2007) showed that there is a negative correlation between synonymous site polymorphisms and nonsynonymous divergence in Drosophila, and they used this information to estimate the strength of selection and frequency of adaptive protein evolution. Both studies concluded that there is widespread adaptive evolution, but estimates of the strength of selection and frequency of adaptive substitution depended on the size of the genomic window considered in the analyses. A related approach fits a population genetics model to mean reductions in diversity observed around nonsynonymous sites that have experienced a substitution between related species (Sattath et al. 2011). This does not depend on the use of a specific window size. The best-fitting model suggests that there is substantial variation in the fitness effects of adaptive amino acid substitutions in Drosophila, potentially shedding light on the different results of Andolfatto (2007) and Macpherson et al. (2007).

We have previously described an approach that attempts to simultaneously infer the rate and strength of deleterious and beneficial mutations occurring in a class of sites in the genome that exploits the shape of the unfolded site frequency spectrum (uSFS) (Schneider et al. 2011). The uSFS is a vector of counts of nucleotide sites with *j* copies of the derived allele, where  $0 \le j \le n$ , and *n* is the number of gene copies in the sample (i.e., including sites fixed for ancestral or derived alleles). By using the uSFS, information for inferring the strength of selection can come mainly from current polymorphisms within a focal species rather than divergence from an outgroup species. The first step is to infer demographic parameters using the SFS for quasi-neutrally evolving sites, such as synonymous sites. Conditioning on the estimates of the demographic parameters, selection parameters are estimated for a selected site class SFS (e.g., for nonsynonymous sites). These parameters describe the distribution of fitness effects (DFE) for deleterious mutations and the frequency of occurrence and strength of selection for one or more classes of advantageous mutations. Inferring adaptive evolution parameters requires that there is an excess of high-frequency derived variants above and beyond that expected from demographic change and from negative selection acting on the bulk of mutations.

Applying the method of Schneider *et al.* (2011) or any method that uses the frequencies of high-frequency derived variants therefore depends on accurate inference of the uSFS. Inference of the uSFS is potentially compromised, however, by misassignment of the ancestral state, and this tends to

affect high-frequency elements of the SFS disproportionately (Fay and Wu 2000; Baudry and Depaulis 2003; Hernandez et al. 2007; Glémin et al. 2015). Current methods for inferring the uSFS rely on a single outgroup (Hernandez et al. 2007). Schneider et al. (2011) also described a method for inferring the uSFS, but we have recently determined that this tends to overestimate the frequency of high-frequency derived variants (Halligan et al. 2013). Here we present a new method for inferring the uSFS using information from one or two outgroup species, which we thoroughly test by simulations. We apply this method to a recent wholegenome polymorphism data set for protein-coding genes from a sample of Drosophila melanogaster genomes originating from a Rwanda population close to their ancestral range. By use of the inferred uSFS, we estimate the frequencies and effects of deleterious and advantageous amino acidchanging mutations.

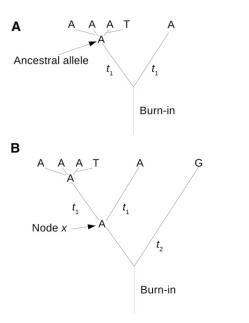
#### **Materials and Methods**

#### Inferring the uSFS: basic assumptions

A focal species is sequenced at multiple sites in a cohort of individuals sampled from a population. The possibility of more than two alleles segregating at a site in the focal species is disregarded. The consequences of this simplification are investigated in the simulations described later, which allow multiallelic sites. To infer the uSFS, we need to compute probabilities for the possible states of the alleles ancestral to the observed alleles in the focal species (Figure 1A). We compute these probabilities using information from a single gene copy, assumed to be randomly sampled at each site, from either one or two outgroup species. Polymorphisms in the common ancestor of the outgroup(s) and the focal species are disregarded; bias introduced by violating this assumption is investigated using the simulations. Initially, we assume that all types of base substitution are equally frequent. Distinct transition and transversion rates are subsequently incorporated. The consequences of violating the equalmutation-rates assumption in the basic method are explored by the simulations.

#### Single-outgroup, single-mutation-rate parameter

Here we illustrate the approach for inferring the uSFS assuming a single outgroup and a single evolutionary divergence parameter *K*. This is the divergence between the allele ancestral to the observed allele(s) in the focal species and a single outgroup (Figure 1A). We do not need to consider mutations from the ancestral allele to the observed segregating alleles in the focal species. In this and the methods that follow (*i.e.*, that allow different transition and transversion rates and two outgroups), a two-stage approach is implemented. First, the evolutionary divergence parameter(s) is estimated by maximum likelihood (ML). Second, assuming perfect knowledge of divergence parameter(s), the elements of the uSFS are estimated one by one by ML.



**Figure 1** Example of a site at which four copies are sequenced in the focal species, where A is the major allele and the ancestral allele and T is the minor allele. (A) A single outgroup has the same state as the ancestral allele. (B) There are two outgroups and an internal node x. Time  $t_2$  is the total number of generations from x to outgroup 2.

#### Single outgroup stage 1: ML estimation of K

Assume that the data consist of counts of numbers of different alleles observed in a sample of n copies in the focal species (n=4 gene copies in Figure 1 and Table 1, for example) and a single copy from an outgroup species. Let K be the expected number of mutations distinguishing the allele ancestral to these four gene copies and the outgroup. Defining  $y_i$  as the allelic configuration observed at site i in the focal species and the outgroup, and assuming independence among sites, the likelihood of the data for all sites combined is

$$L = \prod_{i=1}^{\text{sites}} p(y_i|K) \tag{1}$$

If the focal species is monomorphic, there are two possible configurations of alleles  $(y_1 \text{ and } y_2)$  (Table 1), and there are three configurations if the focal species is polymorphic  $(y_3, y_4, \text{ and } y_5)$  (Table 1). Noting the symmetry of configurations  $y_3$  and  $y_4$ , Equation 1 therefore can be rewritten as

$$L \propto p(y_1|K)^{z_{1,0}} p(y_2|K)^{z_{2,0}} \prod_{j=1}^{n/2} \left[ p(y_3|K)^{z_{3,j}+z_{4,j}} p(y_5|K)^{z_{5,j}} \right]$$
 (2)

where  $z_{x,j}$  is the number of sites showing the configuration with subscript x, given that there are j minor allele copies in the focal species.

Assuming that the number of mutations m is Poisson distributed with probability P(m|K), the probability of configuration  $y_x$ , given divergence K, is

$$p(y_{\mathbf{x}}|K) = \sum_{\mathbf{m}=0}^{\infty} q_{\mathbf{x},\mathbf{m}} P(\mathbf{m}|K)$$
 (3)

where  $q_{x,m}$  is the conditional probability for allelic configuration  $y_x$  given that there are m mutations (Table 1). In practice, we considered only up to two mutations in the summation in Equation 3. Simulations with K up to 20% suggested that allowing more than two mutations had a negligible effect on estimates of K or the SFS elements.

To understand the table, note, for example, the probability  $q_{1,0}$  of observing configuration  $y_1=1$  if there have been no mutations; it is not possible to observe configuration  $y_1$  if there has been one mutation (i.e.,  $q_{1,1}=0$ );  $q_{1,2}=1/3$  because if there had been two mutations, nucleotide A could have mutated to any other nucleotide and then must have mutated back to A. The natural log likelihood with respect to K, i.e.,  $\log(\text{Equation 2})$ , was maximized by the Golden Search Algorithm (Press  $et\ al.\ 1992$ ).

## Single outgroup stage 2: ML estimation of the uSFS elements given K

The approach is to find the ML estimate of the proportion of probability density  $\pi_i$  attributable to the major allele being ancestral vs. the minor allele being ancestral for each element of the SFS while assuming the fixed ML estimate of K from stage 1. There are therefore n/2 + 1 ML estimates to be made. To compute the likelihood of  $\pi_i$ , we need to consider sites for which there are j copies of one allele and n - jcopies of a different allele in the sample of n copies. For invariant sites (j = 0), there are  $z_{1,0}$  and  $z_{2,0}$  sites that have allelic configurations  $y_1$  and  $y_2$ , respectively (Table 1). For variant sites  $(j \neq 0)$ , there are three possible allelic configurations  $(y_3, y_4, \text{ and } y_5)$  (Table 1), but sites where the outgroup allele is different from the copies observed in the focal species (configuration  $y_5$ ) provide no information about the uSFS and so can be disregarded. Note that these sites do contribute to the estimate of K. We therefore have  $z_{3,j}$  and  $z_{4,i}$  sites with the two informative configurations. The likelihood for variant sites that have j minor alleles in the focal species is

$$\begin{split} L(j) & \propto \Bigg\{ \sum_{m=0}^{\infty} \left[ q_{3,m}^{\text{maj}} P(m|K) \right] \pi_{j} + \sum_{m=0}^{\infty} \left[ q_{3,m}^{\text{min}} P(m|K) \right] (1-\pi_{j}) \Bigg\}^{z_{3,j}} \\ & \times \Bigg\{ \sum_{m=0}^{\infty} \left[ q_{4,m}^{\text{maj}} P(m|K) \right] \pi_{j} + \sum_{m=0}^{\infty} \left[ q_{4,m}^{\text{min}} P(m|K) \right] (1-\pi_{j}) \Bigg\}^{z_{4,j}} \end{aligned} \tag{4}$$

where the superscript maj (min) on q implies that the ancestral allele is the major (minor) allele (Table 1). The likelihood for invariant sites in the focal species is

$$L(0) \propto \left\{ \sum_{m=0}^{\infty} \left[ q_{1,m}^{maj} P(m|K) \right] \pi_0 \right\}^{z_{1,0}} \left\{ \sum_{m=0}^{\infty} \left[ q_{2,m}^{min} P(m|K) \right] (1-\pi_0) \right\}^{z_{2,0}} \tag{5}$$

We considered only up to two mutations in the summations in Equations 4 and 5. Log likelihood with respect to each  $\pi_j$  was maximized by the Golden Search Algorithm.

Table 1 Five possible configurations  $(y_1, ..., y_5)$  of numbers of copies of alleles at a site observed in the focal species and the outgroup for the case of four copies sampled in the focal species

Observed state				Conditional probability		
Configuration	Focal species	Outgroup	m = no. of mutations	$q_{x,m}^{maj}$	$q_{x,m}^{min}$	$oldsymbol{q}_{x,m} = oldsymbol{q}_{x,m}^{maj} + oldsymbol{q}_{x,m}^{min}$
<i>y</i> <sub>1</sub>	AAAA	А	0	1	0	1
			1	0	0	0
			2	1/3	0	1/3
<i>y</i> <sub>2</sub>	AAAA	T	0	0	0	0
			1	0	1	1
			2	0	2/3	2/3
<i>y</i> <sub>3</sub>	AAAT	Α	0	1	0	1
			1	0	1/3	1/3
			2	1/3	2/9	5/9
<i>y</i> <sub>4</sub>	AAAT	T	0	0	1	1
			1	1/3	0	1/3
			2	2/9	1/3	5/9
<i>y</i> <sub>5</sub>	AAAT	C	0	0	0	0
			1	2/3	2/3	4/3
			2	4/9	4/9	8/9

There is either no copy or a single copy of a minor allele present in the focal species (T in this case). Assuming that there are from m = 0 to m = 2 mutations between the ancestral allele of the alleles present in the focal species and the outgroup (Figure 1), the conditional probabilities  $q_{x,m}^{maij}$  and  $q_{x,m}^{min}$  of observing configuration x given that the ancestral allele is the major or minor allele, respectively, are shown.

This method can be adapted to infer uSFS elements where different transition and transversion rates have been estimated (Supplemental Material, File S1 and Table S1) and where there are two outgroups (File S1 and Table S2).

#### Simulations

We assessed the performance of the uSFS inference procedures using Monte Carlo simulations, which incorporate the possibility of polymorphisms in the population ancestral to the focal and outgroup species and unequal transition/transversion rates. We analyzed data sets containing large numbers of sites specifying the allelic states for n copies sampled from the population of a focal species and single copies sampled from populations of one or two outgroup species. The simulated populations were diploid and of constant population size N =100. We generally assumed that the neutral diversity  $\theta$  = 0.01 by setting the mutation rate per site per generation to  $\mu = \theta/4N$ . We simulated unlinked nucleotide sites that could be in one of four states (A, T, C, or G). An ancestral population was initiated with equal frequencies of the four nucleotides and allowed to evolve to mutation-drift equilibrium for 20N burn-in generations. A site of an individual was mutated with probability  $\mu$  each generation by randomly altering its current nucleotide state. In general, the probability of a transition mutation was equal to  $1/(1 + 2/\beta)$ , where  $\beta > 1$ implies that there is transition/transversion mutation bias. In the case of a single outgroup, two separate populations were each evolved for  $t_1$  generations after the burn-in to produce a focal population and the outgroup population (Figure 1A). When simulating two outgroups, an outgroup 2 population was evolved for  $(t_1 + t_2)/2$  generations, and a second population was evolved for  $(t_2 - t_1)/2$  generations up to node x (Figure 1B). Two populations then were each evolved from the node x population for  $t_1$  generations to produce a focal population and an outgroup 1 population.

In many simulations, we assumed that all sites evolve neutrally. We also simulated variation in the rate of substitution among sites caused by variation in the strength of purifying selection. A fraction *C* of sites was contributed by selectively constrained sites. Any allele that was different in state from the wild-type allele that arose at such sites was designated as mutant and had a selective disadvantage *s*/2. Effects on fitness were multiplicative. Fertility selection was carried out by sampling individuals for reproduction with replacement in proportion to their relative fitness.

We quantified bias (in percent) affecting estimates of elements of the SFS as the percentage deviation from the true value of that element. We also estimated the scaled root mean square error (RMSE in percent) for elements of the SFS. RMSE incorporates variance among estimates (because one method might produce less variable estimates of SFS elements about the true values than another) and is also influenced by bias:

$$RMSE = 100 \times \frac{\sqrt{\frac{1}{r} \sum (\hat{Y}_i - Y_i)^2}}{\sum Y_i / r},$$
 (6)

where  $\hat{Y}_i$  is the estimate for an SFS element from simulation replicate i,  $Y_i$  is the corresponding true value of that element, and r is the number of simulation replicates.

*D. melanogaster polymorphism data:* We obtained polymorphism data from an African population of *D. melanogaster* comprising 17 Rwandan haploid genomes (RG18N, RG19, RG2, RG22, RG24, RG25, RG28, RG3, RG32N, RG33, RG34, RG36, RG38N, RG4N, RG5, RG7, and RG9) that have been estimated to have the lowest levels of admixture with European populations (<3%) (see Pool *et al.* 2012, Figure 3b]. We downloaded FASTQ files from the *Drosophila* Population Genomics Project (DPGP; http://www.dpgp.org/dpgp2/candidate/). We further masked any regions of the

African samples with evidence of admixture from European populations using the admixture coordinates reported by Pool et al. (2012). Following Pool et al. (2012), sites with a Burrows-Wheeler alignment (BWA) quality score below Q =31 (equivalent to a Phred score of 48 and approximately equivalent to one error per 100 kb) also were masked. This produced the Q31 data set, which is the focus of most of the analysis. We also analyzed a more stringently filtered Q41 data set. From the FASTQ files, we extracted protein-coding regions using gene annotations from FlyBase v5.33 (www. flybase.org) and made FASTA files containing all samples (17 copies), and we excluded genes within non-crossing-over regions (see Campos et al. 2012). For each D. melanogaster gene with multiple transcripts, we chose one transcript at random. We included as outgroups the orthologous genes of D. simulans (r2.01) and D. yakuba (r1.3), obtained from the D. melanogaster–D. simulans–D. yakuba gene alignments of Hu et al. (2013), from which we selected the coding regions corresponding to our selected transcripts.

## Estimating the DFE and rate and strength of adaptive mutations along with the frequency of adaptive substitutions

Assuming the inferred unfolded uSFSs for two outgroups and with no transition/transversion bias, we estimated parameters of the DFE and adaptive mutations by the ML method described by Schneider et al. (2011), which is incorporated into the software DFE-alpha (Keightley and Eyre-Walker 2007), with the following modifications: we first fitted a three-epoch demographic model to the neutral (i.e., synonymous) uSFS, allowing two changes of population size, first from  $N_1$  to  $N_2$  and then from  $N_2$  to  $N_3$  at times  $t_2$  and  $t_3$ , respectively, while also fitting parameters specifying the fractions of unmutated sites  $(f_0)$  and sites fixed by drift  $(f_{2N})$ . By fitting this model to the DPGP synonymous uSFS, we found that high-frequency elements were underpredicted. The estimated uSFS for synonymous sites contains a small uplift in the last element, which cannot be explained under the demographic and mutational model fitted. This uplift could reflect hitchhiking with selected amino acid variants or positive selection on synonymous variants. Alternatively, it could be caused by residual misassignment of low-frequency variants. We assumed that such processes also affected the nonsynonymous uSFS and would lead to upwardly biased estimates of positive selection parameters if not corrected.

In a similar manner to that described by Glémin *et al.* (2015), which follows the approach of Eyre-Walker *et al.* (2006), we therefore corrected elements of the nonsynonymous uSFS  $N_j$  using the deviations of the observed elements  $S_j$  from the fitted elements  $E_j$  of the synonymous uSFS:

$$N_{j}^{'} = \frac{N_{j}}{1 + (S_{j} - E_{j})/E_{j}}$$
 for  $j = 0..n$  (7)

We assessed goodness of fit by comparing fitted uSFSs to observed uSFSs using a  $\chi^2$  statistic, but because the numbers

of sites in derived class j and ancestral class n-j are non-independent, we did not perform formal significance tests.

Conditioning on the values of the parameters fitted to the synonymous SFS, parameters specifying the effects and relative frequencies of deleterious and advantageous mutations were fitted by ML to the corrected nonsynonymous uSFS. We either assumed that the fitness effects of deleterious mutations were drawn from a gamma distribution (which is specified by a shape and a scale parameter) or, following Kousathanas and Keightley (2013), that there were  $n_{\rm d}$  fixed classes of deleterious mutations, where the fitness effect and frequency of class i are  $s_{\rm d,i}$  and  $p_{\rm d,i}$ , respectively. We fitted  $n_{\rm a}$  classes of advantageous mutations, where the fitness effect and frequency of class j are  $s_{\rm a,j}$  and  $p_{\rm a,j}$ , respectively, such that

$$\sum_{i}^{n_{d}} p_{d,i} + \sum_{j}^{n_{a}} p_{a,j} = 1$$
 (8)

The gamma DFE represents a single, continuously variable class of deleterious mutations.

To find maximum-likelihood estimates (MLEs), we carried out runs with large numbers of combinations of random starting values. We estimated 95% confidence limits for the proportion of adaptive mutations and their selective strength from profile likelihoods on the basis of drops in log likelihood of 2 units from their respective MLs (Cole *et al.* 2014). For each point in each profile likelihood, we used the highest likelihood obtained from 20 runs using different starting values sampled around the MLEs. Estimates of  $\alpha$ , the proportion of adaptive substitutions, and  $\omega_a$ , the rate of adaptive substitution relative to the rate of neutral substitution, were obtained as described by Schneider *et al.* (2011).

#### Data availability

The authors state that all data necessary for confirming the conclusions presented in this article are represented fully within the article. The code for uSFS inference is available at www.homepages.ed.ac.uk/pkeightl/.

#### Results

#### Simulations: single outgroup

To investigate the performance of the uSFS inference procedure under circumstances where the data closely conform to the assumptions of the model, we simulated a focal population and a single outgroup with nucleotide divergence K=0.1, no transition/transversion bias ( $\beta=1$ ), and no selection. We assumed that  $\theta=4N_{\rm e}\mu=0.01$  so that  $\theta<< K$  and few polymorphic sites in the focal species are also polymorphic in the ancestral population prior to the split between the focal species and the outgroup. Figure 2 shows the true uSFS (calculated using knowledge of the ancestral state for each site) and the uSFSs inferred using the single-outgroup method described here and the method of Schneider *et al.* (2011). The new approach is therefore capable of estimating the

uSFS with little bias on average, including high-frequency elements of the SFS. The method of Schneider *et al.* (2011) tends to overestimate high-frequency SFS elements, presumably because polymorphic sites having an outgroup allele inconsistent with either allele present in the focal species are misassigned. Our approach appears to give nearly unbiased estimates of the uSFS elements as long as the divergence to the outgroup is K < 0.3 (Figure S1).

We extended the method to include the estimation of separate transition and transversion rate parameters (File S1 and Table S1). This was tested by simulations of neutrally evolving sites and also produces nearly unbiased estimates of the uSFS in the presence of transition/transversion mutational bias (Figure S2A). The single-rate-parameter method also produces reasonably unbiased estimates of the uSFS as long as the transition/transversion mutation bias  $\beta < 2$  (Figure S2B).

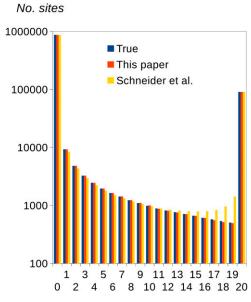
#### Simulations: two outgroups, neutrally evolving sites

We then compared the performances of the uSFS inference procedures allowing one or two outgroups. The results suggest that there is a clear benefit from using a second outgroup in terms of lower variance among replicates (lower RMSE) (Figure 3) but potentially a cost in terms of higher bias (*i.e.*, there is a tendency for underestimation of the high-frequency SFS elements), especially if the divergence from the second outgroup is small (Figure 3).

### Simulations: variable strength of purifying selection among sites

We then investigated the performance of the uSFS inference procedures in the presence of variation in the substitution rate and diversity among sites caused by purifying selection. We simulated this variation by assuming that a fraction C of sites is subject to negative selection (see *Materials and Methods*), the remainder evolving neutrally. We found that with  $C \approx 0.85$  and Ns = 10 (so that mutant alleles rarely become fixed), and divergence, diversity, and the shape of the SFS simulated are similar to what we observe in the D. melanogaster polymorphism data for nonsynonymous sites, although in this case we assume a constant population size.

We compared the accuracy of the inferred uSFS using one or two outgroups, focusing on the high-copy-number elements of the SFS, which are hardest to estimate accurately. We assumed a neutral divergence between the focal species and the first outgroup of  $K_1 = 0.1$  (which is similar to the D. melanogaster -D. simulans divergence) and a neutral divergence between the internal node and the second outgroup of  $K_2 = 0.15$ . The results suggest that there is a clear benefit in terms of both reduced bias and reduced RMSE from using the information from a second outgroup (Figure 4 and Figure S3). Using information from a single outgroup, however, can lead to serious overestimation of the high-copy-number SFS elements (as much as 15% in the cases shown). Presumably, the benefit of using a second outgroup applies when there are other sources of variation



No. derived allele copies

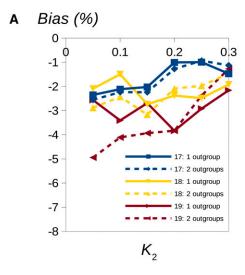
**Figure 2** True uSFS (from simulation) and estimated uSFSs computed by the present method and by the method of Schneider *et al.* (2011), both using a single outgroup. Twenty copies were sampled at each site of the focal species. Diversity  $\theta = 4N\mu = 0.01$ , and divergence between the focal species and the outgroup was K = 0.1. There were eight replicate simulations, each with  $10^6$  sites, resulting in a negligible sampling variance for elements of the estimated uSFSs.

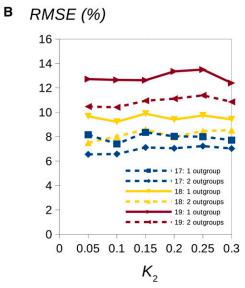
in the substitution rate among sites, such as variation in the mutation rate.

## Inference of uSFSs and frequency and strength of adaptive molecular evolution in the D. melanogaster proteome

We applied the uSFS inference procedure to the polymorphism data set of protein-coding genes of the *D. melanogaster* DPGP phase 2. Using two outgroups (*D. simulans* and *D. yakuba*), we inferred uSFSs for four- and zerofold sites (Figure 5). As expected, nucleotide diversity at zerofold sites is substantially lower than that at fourfold sites, and there is an enrichment of zerofold singletons, consistent with negative selection acting on many nonsynonymous sites.

Given the inferred SFSs, we then applied the approach of Schneider *et al.* (2011) to estimate the rate of occurrence and selective strength of adaptive amino acid mutations. We fitted parameters of a three-epoch demographic model to the synonymous-site data (Table S3 and Figure S4); this model fit much better than a two-epoch model (log-likelihood difference = 221) and suggests that there was a population-size bottleneck followed by a population expansion. There is, however, an appreciable deviation between the observed and fitted synonymous uSFSs, particularly affecting the last element [Figure S4;  $\chi^2(16) = 138$ ]. We assumed that misinference also would affect the nonsynonymous uSFSs, potentially leading to spurious estimates of adaptive molecular evolution. We therefore corrected the nonsynonymous

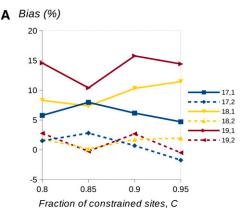


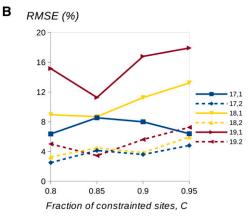


**Figure 3** Estimated bias (%) (A) and RMSE (B) for estimates of uSFS elements 17, 18, and 19 plotted against divergence  $K_2$  between node x and outgroup 2 (see Figure 1) for the case of 20 copies sampled at each site of the focal species. Positive and negative percent bias imply over- or underestimation of the SFS element, respectively. The solid and dotted lines show inferences using one or two outgroups, respectively. The divergence between the focal species and outgroup 1 was  $K_1 = 0.1$ , and the diversity in the focal species was  $\theta = 0.01$ . There was no transition/ transversion bias. In each of 160 replicates,  $10^5$  sites were simulated.

uSFSs using the deviation between the observed and fitted synonymous uSFSs, as described in *Materials and Methods*. Uncorrected and corrected nonsynonymous uSFSs are shown in Figure S5.

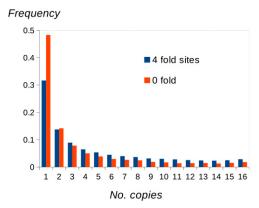
Given the demographic parameter estimates from the synonymous site data, we then estimated parameters of the DFE for deleterious mutations and the proportion  $p_a$  and scaled selection strength acting on one or more classes of adaptive mutations  $N_e s_a$ , assuming that the DFE is constant through time. Several models had similar levels of statistical support (Table 2). The best-fitting model gives an excellent fit to the data [Figure S5;  $\chi^2(16) = 16.9$ ] and consisted of





**Figure 4** One- vs. two-outgroup comparison in the presence of variation among sites in selective constraints. The panels show bias (A) and RMSE (B) in the last three elements of the uSFS. For example, the label 17,1 refers to the bias/RMSE affecting element 17 with a single outgroup. A fraction C of sites was simulated with scaled selection coefficient Ns = -10, and the remainder evolve neutrally. A total of  $10^5$  sites were simulated per replication and 240 replicates. The divergence parameters for neutral alleles were  $K_1 = 0.1$  and  $K_2 = 0.15$ .

four classes of mutational effects: two classes of deleterious mutations, a class of neutral mutations, and a single class of advantageous mutations. There is substantial support for models with adaptive mutations ( $\Delta \log L = 93$  between the best-fitting model and the same model excluding adaptive mutations). Assuming the four-class model, MLEs of the proportion of advantageous mutations and the scaled strength of selection acting on them are  $p_a = 0.0045$  [approximate upper 95% confidence interval (CI) = 0.012] and  $N_e s_a = 11.5$  (approximate lower 95% CI = 5), respectively. Because we assume that the inferred SFSs are known with certainty, these 95% CIs are likely to be underestimates. Note that  $p_a$  and  $s_a$ are hard to estimate separately, but their product is well estimated. Other models that explain the data almost as well (gamma DFE, three classes of mutational effects) give somewhat different ML estimates of  $p_a$  and  $N_e s_a$ , but the products of  $p_a \times N_e s_a$  are of similar magnitude (Table 2). Fitting additional classes of mutations (advantageous or deleterious) did not lead to a further increase in log likelihood. We then estimated the frequency of adaptive substitutions  $\alpha$  and the rate



**Figure 5** Unfolded SFSs for zero- and fourfold sites of *D. melanogaster* protein-coding genes inferred using two outgroups (*D. simulans* and *D. yakuba*).

of adaptive substitution relative to that of neutral substitution  $\omega_a$  from the proportions and fixation probabilities of the advantageous, neutral, and deleterious mutation classes. The estimates are  $\alpha=0.57$  and  $\omega_a=0.096$  for the four-class model, but these are sensitive to the model assumed (Table 2).

#### Discussion

There were three main motivations for this study. First, we had determined that a previously described method to infer the uSFS (Schneider et al. 2011) tends to overestimate highfrequency SFS elements. Second, using parsimony for inferring ancestral states of high-frequency elements of the SFS is problematical because the corresponding low-frequency elements usually involve a far greater number of sites, and these tend to be misassigned as high-frequency elements, potentially leading to an overestimation of the frequency of alleles under positive selection. Third, large, genome-wide polymorphism data sets offer the opportunity to investigate the frequency and strength of ongoing adaptive molecular evolution using a method also described by Schneider et al. (2011), but this requires accurate inference of the uSFS. The development of this approach was motivated by inconsistent results emerging from the application of variants of the MK test, such as the methods of Welch (2006), DFE-alpha (Eyre-Walker and Keightley 2009), and DoFE (based on Eyre-Walker et al. 2006).

These methods all estimate the frequency of adaptive substitutions in a set of loci by contrasting polymorphism data in a focal species with divergence from an outgroup species. For example, many estimates of the proportion of adaptive amino acid substitutions  $\alpha$  in plants are negative, some significantly, at face value, implying that there is little adaptive protein evolution (Gossmann *et al.* 2010). The true value of  $\alpha$  cannot be negative, however, and this result may reflect the presence of widespread population structure in plant species, which distorts the SFS and could bias estimates of  $\alpha$  downward. Some estimates of  $\alpha$  in great apes are also negative (Good *et al.* 2013). A clear example of inconsistency comes

Table 2 ML estimates of parameters from DFE-alpha for three different models

	ML estimates					
Parameter	Four classes	Three classes	Gamma			
β	_	_	0.35			
$p_{d1}$	0.88	0.89	1			
$N_{\rm e}s_{\rm d1}$	<b>-177</b>	-167	-2120			
$p_{d2}$	0.076	0.10	_			
$N_{\rm e}s_{\rm d2}$	-2.8	-1.4	_			
$p_{d3}$	0.039	_	_			
$N_{\rm e}s_{\rm d3}$	0	_	_			
$p_{a}$	0.0045	0.0093	0.0031			
$N_{\rm e}s_{\rm a}$	11.5	6.7	17			
α	0.57	0.89	0.68			
$\omega_{\text{a}}$	0.096	0.14	0.091			
$\Delta \log L$	0	-0.6	-2.1			

The models assume that there are four or three classes of mutational effects or a gamma DFE. The difference in log likelihood ( $\Delta \log L$ ) is the difference from the best-fitting model. The parameters of the model are as follows:  $\beta$  = shape of gamma distribution;  $p_{\rm di}$  = proportion of deleterious mutations in category i;  $N_{\rm e}S_{\rm di}$  = scaled selection coefficient for deleterious mutations in category i;  $p_{\rm a}$  = proportion of adaptive mutations;  $N_{\rm e}S_{\rm a}$  = scaled selection coefficient for adaptive mutations;  $\alpha$  = proportion of amino acid substitutions fixed by positive selection; and  $\omega_{\rm a}$  = rate of adaptive amino acid substitution relative to the neutral substitution rate.

from a reciprocal analysis of genome-wide polymorphism data in murid rodents, where an estimate of  $\alpha$  in wild house mice using divergence from the rat is strongly and significantly positive, *i.e.*,  $\alpha \approx 0.3$  (Halligan *et al.* 2013), whereas an estimate using polymorphisms within wild brown rats and divergence from the mouse is strongly and significantly negative, *i.e.*,  $\alpha \approx -0.3$  (Deinum *et al.* 2015). The negative estimate presumably reflects a recent population bottleneck in the brown rat, leading to overprediction of the number of fixed, slightly deleterious mutations.

In contrast to MK-based methods, the method of Schneider et al. (2011) uses information on polymorphism data within a species to infer ongoing adaptive molecular evolution. It can be set up to use no information from sites fixed for the derived allele, but we did not do that here. By simulations, we investigated the circumstances under which accurate inference of the uSFS is possible. The most important potential source of misinference we identified is variation in the substitution rate, affecting the joint spectrum of polymorphisms in the focal species and divergence(s) from the outgroup(s). This could either be due to variation in the mutation rate between different kinds of sites or variation between sites in selective constraints or adaptive potential. In principle, it is possible to account for some components of variation in the mutation rate by explicit modeling (e.g., transition/transversion bias). Selection that varies among sites appears to be a more important issue, however, and is more difficult to model. Our simulations show that with a single outgroup only, high-copynumber uSFS elements are potentially seriously overestimated if there is variation in selective constraints among sites. This is so because the divergence between the ancestral allele and the outgroup is computed as an average across sites, but this will be lower than the divergence at the subset of unconstrained sites, so multiple hits are undercorrected at these sites. Our simulation results suggest that incorporating a second outgroup substantially corrects this problem, allowing accurate estimation of the uSFS. It should be feasible to extend our approach to include multiple outgroups, although there are presumably diminishing returns and potential biases from adding more distant outgroups. Incorporating data from multiple linked SNPs in a region also might add further information, although the rapid decay of linkage disequilibrium with distance between markers in *Drosophila* (Mackay *et al.* 2012) means that this would be of limited use.

We applied our new uSFS inference approach to the D. melanogaster DPGP phase 2 data for protein-coding genes, and several aspects of the results are noteworthy. The inferred uSFS for synonymous sites contains a small but appreciable uplift in the last element (Figure S4). With the demographic and mutational models fitted by DFE-alpha, however, it is not possible to obtain an uplift in the fitted uSFS. The apparent increase in the frequency of high-copynumber derived synonymous alleles could be genuine and explained, for example, by hitchhiking with linked selected amino acid variants or selection on synonymous variants (Zeng 2010; Clemente and Vogl 2012; Lawrie et al. 2013). If the uplift is an effect of selection on linked sites, we can assume that this also affects the nonsynonymous uSFS. This is the rationale for correcting the nonsynonymous uSFS based on the deviation from the fitted and observed synonymous uSFS. Alternatively, it could be caused by residual misassignment of low-frequency variants. We investigated whether this might be due to sequencing errors by analyzing a more stringent set of SNPs (Q41). The inferred uSFSs are extremely similar to the uSFSs analyzed (Q31) (Figure S6), suggesting that sequencing errors in DPGP are not an important source of misinference. We corrected the nonsynonymous uSFS based on the deviation from the fitted and observed synonymous uSFS.

Fitting the demographic parameters estimated from synonymous sites and then estimating selection parameters by ML resulted in a close fit to the corrected nonsynonymous uSFS (Figure S5), but several alternative models also give excellent fits (Table 2). Taking the best-fitting model at face value, the results therefore imply that there is a major contribution from adaptive amino acid substitutions to protein evolution in D. melanogaster, i.e.,  $\alpha \approx 0.5$ . This figure is consistent with several studies employing variants of the MK test to estimate the frequency of adaptive protein evolution (Fay et al. 2002; Smith and Eyre-Walker 2002; Welch 2006; Andolfatto 2007; Eyre-Walker and Keightley 2009; Campos et al. 2014). The estimated selective effects of adaptive mutations are also consistent with estimates for the more common, weakly selected of the two classes inferred by Sattath et al. (2011) based on changes in diversity around substituted nonsynonymous sites. However, Sattath et al. (2011) estimated that only about 13% of amino acid substitutions cause selective sweeps, arguing that this low value could reflect a prevalence of partial sweeps. However, Schneider et al.

(2011) used information from high-frequency polymorphisms, which is most relevant for inferring the ongoing strength of selection and the frequency of relatively weakly selected variants. This is so because strongly selected mutations are expected to be relatively rare and sweep rapidly to fixation, leaving little detectable footprint in the uSFS.

#### **Acknowledgments**

We are grateful to two anonymous referees for helpful comments. We also thank the UK Biotechnology and Biological Sciences Research Council for support.

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Communicating editor: W. Stephan

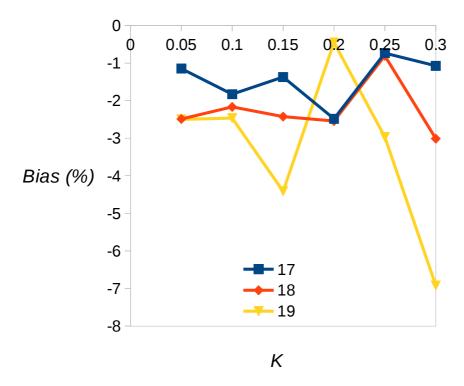
# **GENETICS**

**Supporting Information** 

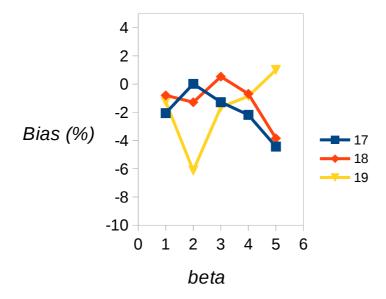
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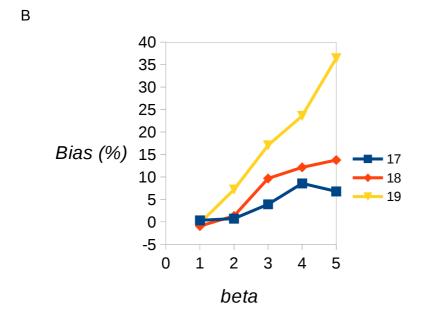
Inferring the Frequency Spectrum of Derived Variants to Quantify Adaptive Molecular Evolution in Protein-Coding Genes of Drosophila melanogaster

Peter D. Keightley, José L. Campos, Tom R. Booker, and Brian Charlesworth



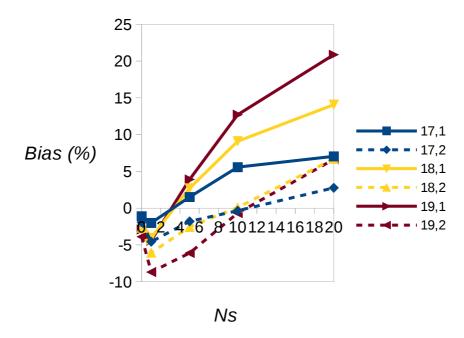
**Figure S1**. Bias (%) as average deviation from true values of estimates for the last three elements of the uSFS (i.e., number of copies of the derived allele = 17, 18 or 19) as a function of divergence (K) between the focal species and an outgroup. 20 copies were sampled at each site of the focal species, and one from a single outgroup. Diversity  $\theta = 4N\mu = 0.01$ . There was no transition:transversion bias.  $10^5$  sites were simulated in each of 160 replicates.

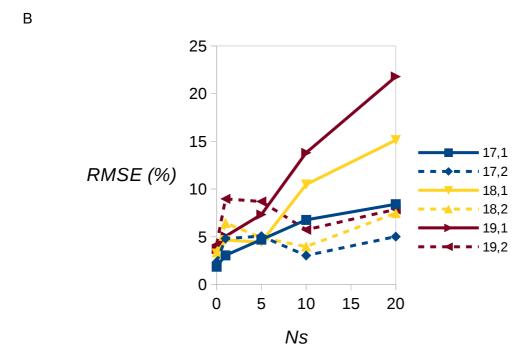




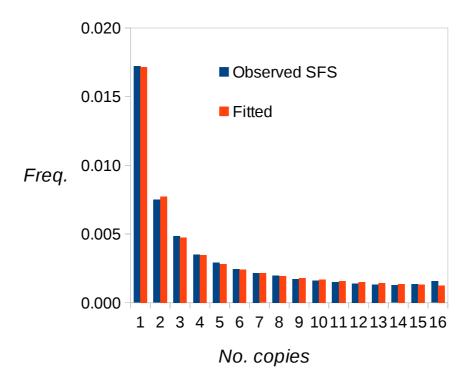
**Figure S2**. Bias (%) as average deviation from true values for estimates of the last three elements of the uSFS (i.e., number of copies of the derived allele = 17, 18 or 19) as a function of the transition:transversion mutation rate bias parameter, *beta*. 20 copies were sampled at each site of the focal species, diversity =  $\theta = 4N\mu = 0.01$ , and the divergence between the focal species and a single outgroup = K = 0.1.  $10^5$  sites were simulated in each of 32 replicates. A: analysis using method incorporating separate transition and transversion rates. B: analysis using single rate parameter method.



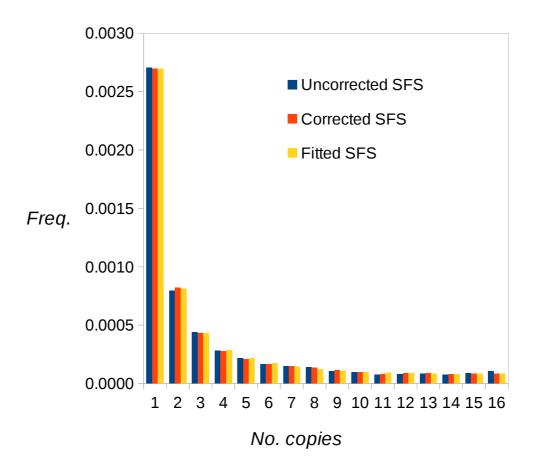




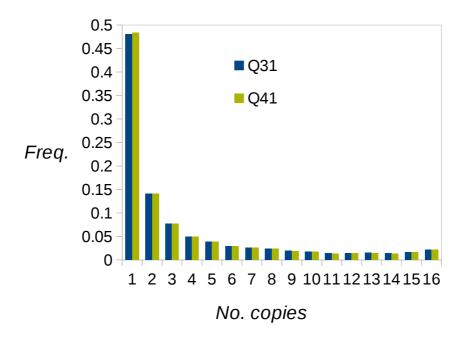
**Figure S3**. One *versus* two outgroup comparison where a subset of sites are subject to negative selection. Bias (A) and RMSE (B) in the last three elements of the uSFS. For example, 17,1 refers to the bias/RMSE affecting element 17 with one outgroup. A fraction C = 0.9 of sites had scaled selection coefficient (*Ns*) and the remainder evolved neutrally.  $10^5$  sites were simulated per replication and 240 replicates. The divergences for neutral alleles were  $K_1 = 0.1$  and  $K_2 = 0.15$ .



**Figure S4**. Comparison of synonymous uSFS from a three-epoch model estimated by DFE-alpha (fitted) to the observed uSFS in Drosophila.



**Figure S5**. Comparison of nonsynonymous uSFS estimated by DFE-alpha (fitted) to the observed uncorrected uSFS and the corrected uSFS in Drosophila.



**Figure S6**. Uncorrected nonsynonymous uSFSs for the DPGP data inferred using two SNP quality thresholds (Q31 and Q41).

Table S1 Configurations and conditional probabilities for the case of transition/transversion bias.

Observed state			Conditional probability			
Config	Focal species	Outgroup	т	$q_{_{x},m}^{^{maj}}$	$q_{x,m}^{min}$	$q_{x,m} = q_{x,m}^{maj} + q_{x,m}^{min}$
<b>y</b> 1	AAAA	Α	0	1	0	1
			1	0	0	0
			2	$K_{ts}^2 + 2K_{tv}^2$	0	$K_{ts}^2 + 2K_{tv}^2$
<b>y</b> <sub>2</sub>	AAAA	Т	0	0	0	0
			1	0	K <sub>ts</sub>	K <sub>ts</sub>
			2	0	$2K_{tv}^2$	2K <sub>tv</sub> <sup>2</sup>
<b>y</b> <sub>3</sub>	AAAA	С	0	0	0	0
			1	0	K <sub>tv</sub>	K <sub>tv</sub>
			2	0	4K <sub>ts</sub> K <sub>tv</sub>	$4K_{ts}K_{tv}$
<b>y</b> <sub>4</sub>	AAAG	Α	0	1	0	1
			1	0	K <sub>ts</sub>	K <sub>ts</sub>
			2	$K_{ts}^2 + 2K_{tv}^2$	2K <sub>tv</sub> <sup>2</sup>	$K_{ts}^2 + 4K_{tv}^2$
<b>y</b> <sub>5</sub>	AAAG	G	0	0	1	1
			1	K <sub>ts</sub>	0	K <sub>ts</sub>
			2	2K <sub>tv</sub> <sup>2</sup>	$K_{ts}^2 + 2K_{tv}^2$	$K_{ts}^2 + 4K_{tv}^2$
<b>y</b> <sub>6</sub>	AAAG	С	0	0	0	0
			1	2K <sub>tv</sub>	2K <sub>tv</sub>	4K <sub>tv</sub>
			2	4K <sub>ts</sub> K <sub>tv</sub>	4K <sub>ts</sub> K <sub>tv</sub>	8K <sub>ts</sub> K <sub>tv</sub>
<b>y</b> <sub>7</sub>	AAAC	Α	0	1	0	1
			1	0	K <sub>tv</sub>	K <sub>tv</sub>
			2	$K_{ts}^2 + 2K_{tv}^2$	2K <sub>ts</sub> K <sub>tv</sub>	$K_{ts}^2 + 2K_{ts}K_{tv} + 2K_{tv}^2$
<b>y</b> 8	AAAC	С	0	0	1	1
			1	K <sub>tv</sub>	0	K <sub>tv</sub>
			2	2K <sub>ts</sub> K <sub>tv</sub>	$K_{ts}^2 + 2K_{tv}^2$	$K_{ts}^2 + 2K_{ts}K_{tv} + 2K_{tv}^2$
<b>y</b> <sub>9</sub>	AAAC	G	0	0	0	0
			1	$K_{ts} + K_{tv}$	$K_{ts} + K_{tv}$	$2K_{ts} + 2K_{tv}$
			2	$2K_{ts}K_{tv}+2K_{tv}^2$	$2K_{ts}K_{tv}+2K_{tv}^2$	$4K_{ts}K_{tv}+4K_{tv}^{2}$

Nine possible configurations  $(y_1...y_9)$  of numbers of copies of alleles at a site observed in the focal species and the outgroup for the case of four copies sampled in the focal species. There are either zero or one copy of a minor allele present in the focal species. Assuming that there are from m = 0 to 2 mutations, the conditional probabilities  $q_{x,m}^{maj}$  and  $q_{x,m}^{min}$  of observing configuration x, given that the ancestral allele is the major or the minor allele, respectively, are shown as a function of the rates of transition and transversion substitution,  $K_{ts}$  and  $K_{tv}$ , respectively.

Table S2 Configurations and conditional probabilities for the case of two outgroups.

	Observed state			Conditional probability			
Config	Focal sp.	Outgroup 1	Outgroup 2	m	$q_{x,m}^{maj}$	$q_{x,m}^{min}$	$q_{x,m} = q_{x,m}^{maj} + q_{x,m}^{min}$
<b>y</b> <sub>1</sub>	AAAA	Α	А	0	1	0	1
				1	0	0	0
				2	$2K_1^2/3 + K_2^2/3$	0	$2K_1^2/3 + K_2^2/3$
<b>y</b> <sub>2</sub>	AAAA	Т	А	0	0	0	1
				1	K₁/3	0	K <sub>1</sub> /3
				2	$2K_1^2/3 + 2K_1K_2/3$	0	$2K_1^2/3 + 2K_1K_2/3$
<b>y</b> 3	AAAA	Α	Т	0	0	0	1
				1	K₂/3	0	K₂/3
				2	$2K_1^2/3 + 2K_2^2/3$	0	$2K_1^2/3 + 2K_2^2/3$
<b>y</b> <sub>4</sub>	AAAA	Т	Т	0	0	0	1
				1	K₁/3	0	K₁/3
				2	$2K_1^2/3 + 2K_1K_2/3$	0	$2K_1^2/3 + 2K_1K_2/3$
<b>y</b> 5	AAAA	Т	С	0	0	0	1
				1	0	0	0
				2	$4K_1^2/3 + 8K_1K_2/3$	0	$4K_1^2/3 + 8K_1K_2/3$
<b>y</b> 6	AAAT	Α	A	0	1	0	1
				1	0	K₁/3	K₁/3
				2	$2K_1^2/3 + K_2^2/3$	$2K_1^2/9 + 2K_1K_2/9$	$8K_1^2/9 + 2K_1K_2/9 + K_2^2/3$
<b>y</b> 7	AAAT	Т	Т	0	0	1	1
				1	K₁/3	0	K₁/3
				2	$2K_1^2/9 + 2K_1K_2/9$	$2K_1^2/3 + K_2^2/3$	$8K_1^2/9 + 2K_1K_2/9 + K_2^2/3$
<b>y</b> 8	AAAT	Α	Т	0	0	0	0
				1	K₂/3	K₁/3	$K_1/3 + K_2/3$
				2	$2K_1^2/9 + 2K_2^2/9$	$2K_1^2/9 + 2K_1K_2/9$	$4K_1^2/9 + 2K_1K_2/9 + 2K_2^2/9$
<b>y</b> 9	AAAT	Т	A	0	0	0	0
				1	K₁/3	<i>K</i> ₂/3	$K_1/3 + K_2/3$
				2	$2K_1^2/9 + 2K_1K_2/9$	$2K_1^2/9 + 2K_2^2/9$	$4K_1^2/9 + 2K_1K_2/9 + 2K_2^2/9$
<b>y</b> 10	AAAT	Α	С	0	0	0	0
				1	2K₂/3	0	2K <sub>2</sub> /3
				2	$4K_1^2/9 + 4K_2^2/9$	$4K_1^2/9 + 8K_1K_2/9$	$8K_1^2/9 + 8K_1K_2/9 + 4K_2^2/9$
<b>y</b> 11	AAAT	Т	С	0	0	0	0
				1	0	2K₂/3	2K <sub>2</sub> /3
				2	$4K_1^2/9 + 8K_1K_2/9$	$4K_1^2/9 + 4K_2^2/9$	$8K_1^2/9 + 8K_1K_2/9 + 4K_2^2/9$
<b>y</b> <sub>12</sub>	AAAT	С	А	0	0	0	0
				1	2K₁/3	0	2K <sub>1</sub> /3
				2	$4K_1^2/9 + 4K_1K_2/9$	$4K_1^2/9 + 8K_1K_2/9$	$8K_1^2/9 + 12K_1K_2/9$
<b>y</b> 13	AAAT	С	Т	0	0	0	0
				1	0	2K <sub>1</sub> /3	2K <sub>1</sub> /3
				2	$4K_1^2/9 + 8K_1K_2/9$	$4K_1^2/9 + 4K_1K_2/9$	8K <sub>1</sub> <sup>2</sup> /9 + 12K <sub>1</sub> K <sub>2</sub> /9
<b>y</b> 14	AAAT	С	С	0	0	0	0
				1	2K <sub>1</sub> /3	2K <sub>1</sub> /3	4K <sub>1</sub> /3
				2	$4K_1^2/9 + 4K_1K_2/9$	$4K_1^2/9 + 4K_1K_2/9$	$8K_1^2/9 + 8K_1K_2/9$
<b>y</b> 15	AAAT	С	G	0	0	0	0
				1	0	0	0
				2	$4K_1^2/9 + 8K_1K_2/9$	$4K_1^2/9 + 8K_1K_2/9$	$8K_1^2/9 + 16K_1K_2/9$

Table S3 ML estimates of demographic parameters from DFE-alpha.

Parameter	ML estimates
$N_2/N_1$	0.30
$N_3/N_1$	0.70
$t_2/N_2$	3.2
<i>t</i> <sub>3</sub> /N <sub>3</sub>	0.28

Inference of evolutionary rates and uSFS elements allowing different transition and transversion rates

Stage 1. Analogously to equation (2), the likelihood equation for the allelic configurations (Table S1) as a function of the transition and transversion rates ( $K_{ts}$  and  $K_{tv}$ , respectively) is:

$$\begin{split} L &\propto p(y_1|K_{ts},K_{tv})^{z_{1,0}} p(y_2|K_{ts},K_{tv})^{z_{2,0}} p(y_3|K_{ts},K_{tv})^{z_{3,0}} \\ &\prod_{i=1}^{n/2} \left[ p(y_4|K_{ts},K_{tv})^{z_{4,j}+z_{5,j}} p(y_6|K_{ts},K_{tv})^{z_{6,j}} p(y_7|K_{ts},K_{tv})^{z_{7,j}+z_{8,j}} p(y_9|K_{ts},K_{tv})^{z_{9,j}} \right] \end{split}$$

where

$$p(y_x|K_{ts},K_{tv}) = \sum_{m=0}^{\infty} q_{x,m} P(m|K_{ts}+2K_{tv}),$$

 $q_{x,m}$  is the conditional probability given in Table S1 and  $P(m \mid x)$  is the Poisson probability function for m events with parameter x. Likelihood was maximized using the Simplex algorithm (Press et al. 1992).

Stage 2. Analogously to equation (4), the likelihood equation for the allelic configurations, given the evolutionary rates, as a function of the site frequency spectrum elements with derived allele count j = 1 to n - 1 is:

$$L(j) \propto \prod_{i=4,5,7,8} \left[ \sum_{m=0}^{\infty} \left( q_{i,m}^{\textit{maj}} P(m | K_{ts} + 2K_{tv}) \right) \pi_j + \sum_{m=0}^{\infty} \left( q_{i,m}^{\textit{min}} P(m | K_{ts} + 2K_{tv}) \right) (1 - \pi_j) \right]^{z_{i,j}},$$

where index *i* refers to the configurations in Table S1. Likelihood was maximized by the Golden Search algorithm (Press et al. 1992).

Inference of evolutionary rates and uSFS elements allowing two outgroups

Stage 1. The likelihood equation for the allelic configurations (Table S2) as a function of the lengths of the branches ( $K_1$  and  $K_2$ , Figure 1) is:

$$L \propto \prod_{i=1}^{5} \rho(y_{i}|K_{1},K_{2})^{z_{i,0}} \prod_{j=1}^{n/2} \left( \prod_{i=6,8,10,12} \rho(y_{i}|K_{1},K_{2})^{z_{i,j}+z_{i+1,j}} \rho(y_{13}|K_{1},K_{2})^{z_{13,j}} \rho(y_{14}|K_{1},K_{2})^{z_{14,j}} \right),$$

where

$$p(y_x|K_1,K_2) = \sum_{m=0}^{\infty} q_{x,m} P(m|2K_1+K_2),$$

 $q_{x,m}$  is the conditional probability given in Table S2 and  $P(m \mid x)$  is the Poisson probability function for m events parameter x. Likelihood was maximized using the Simplex algorithm (Press et al. 1992).

Stage 2. The likelihood equation for the allelic configurations, given the branch lengths  $K_1$  and  $K_2$ , as a function of the site frequency spectrum elements with derived allele count j = 1 to n - 1 is:

$$L(j) \propto \prod_{i=6}^{13} \left[ \sum_{m=0}^{\infty} (q_{i,m}^{maj} P(m|2K_1 + K_2)) \pi_j + \sum_{m=0}^{\infty} (q_{i,m}^{min} P(m|2K_1 + K_2)) (1 - \pi_j) \right]^{z_{i,j}},$$

where index *i* refers to configurations in Table S1. Likelihood was maximized by the Golden Search algorithm (Press et al. 1992).