

Flexural Rigidity and Shear Stiffness of Flagella Estimated from Induced Bends and Counterbends

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ABSTRACT Motile cilia and flagella are whiplike cellular organelles that bend actively to propel cells or move fluid in passages such as airways, brain ventricles, and the oviduct. Efficient motile function of cilia and flagella depends on coordinated interactions between active forces from an array of motor proteins and passive mechanical resistance from the complex cytoskeletal structure (the axoneme). However, details of this coordination, including axonemal mechanics, remain unclear. We investigated two major mechanical parameters, flexural rigidity and interdoulet shear stiffness, of the flagellar axoneme in the unicellular alga *Chlamydomonas reinhardtii*. Combining experiment, theory, and finite element models, we demonstrate that the apparent flexural rigidity of the axoneme depends on both the intrinsic flexural rigidity (EI) and the elastic resistance to interdoulet sliding (shear stiffness, k_s). We estimated the average intrinsic flexural rigidity and interdoulet shear stiffness of wild-type *Chlamydomonas* flagella in vivo, rendered immotile by vanadate, to be $EI = 840 \pm 280 \text{ pN} \cdot \mu\text{m}^2$ and $k_s = 79.6 \pm 10.5 \text{ pN/rad}$, respectively. The corresponding values for the *pf3; cnk11-6* double mutant, which lacks the nexin-dynein regulatory complex (N-DRC), were $EI = 1011 \pm 183 \text{ pN} \cdot \mu\text{m}^2$ and $k_s = 39.3 \pm 6.0 \text{ pN/rad}$ under the same conditions. Finally, in the *pf13A* mutant, which lacks outer dynein arms and inner dynein arm *c*, the estimates were $EI = 777 \pm 184 \text{ pN} \cdot \mu\text{m}^2$ and $k_s = 43.3 \pm 7.7 \text{ pN/rad}$. In the two mutant strains, the flexural rigidity is not significantly different from wild-type ($p > 0.05$), but the lack of N-DRC (in *pf3; cnk11-6*) or dynein arms (in *pf13A*) significantly reduces interdoulet shear stiffness. These differences may represent the contributions of the N-DRCs (~40 pN/rad) and residual dynein interactions (~35 pN/rad) to interdoulet sliding resistance in these immobilized *Chlamydomonas* flagella.

INTRODUCTION

Motile cilia and flagella are whiplike cellular organelles (~5–50 μm in length and ~200 nm in diameter) that bend actively to propel cells or move fluid or other materials (Fig. 1, *a* and *b*) (1). Motile cilia and flagella play a wide range of important roles in developmental and physiological processes, such as determination of left-right asymmetry, cerebrospinal fluid flow, mucociliary clearance, sperm swimming, and egg transport in fallopian tubes (1). Ciliary dysfunction is known or suspected in a number of genetic and acquired disorders (ciliopathies) including primary ciliary dyskinesia (2,3), chronic obstructive pulmonary disease (4), asthma (5), and otitis media (2). However, the complexity of the coupling between structure-function and mechanics-biochemistry in ciliary bending has precluded the mechanistic understanding required for

rational development of diagnosis and treatment of ciliary dysfunction.

The ciliary microtubular cytoskeleton (axoneme) is a complex structure composed of >600 structural proteins (6). A typical axoneme (Fig. 1 *c*) consists of nine microtubule doublets that surround a central pair of singlet microtubules. These microtubule beams are interconnected by circumferential nexin-dynein regulatory complex (N-DRC) and radial spokes. In addition, motor protein dyneins form an array of cross bridges between neighboring outer doublets and exert forces (powered by ATP hydrolysis) that cause sliding of one doublet relative to the other (7). This interdoulet sliding is then converted to bending deformation of the axoneme as all microtubule beams are interconnected. The active motor forces are counterbalanced by both internal resistive forces from the axoneme and external viscous fluid drags (8). As a result, the axoneme undergoes coordinated propagation of bending deformations that are critical for motility.

Many details of this coordinated motion, including the role of axonemal mechanics, remain unclear. To date, only a

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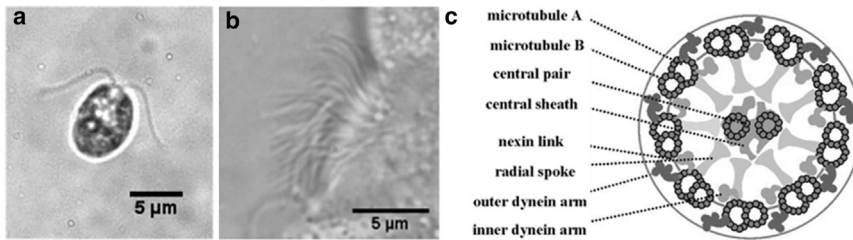


FIGURE 1 (a and b) Video micrographs of *Chlamydomonas* flagella (a) and human airway epithelial cilia (b). (c) Schematic of the normal flagellar axoneme in cross section (from Ibañez-Tallon et al. (1)). The “9+2” axoneme consists of nine outer microtubule doublets surrounding a central pair of single microtubules. These beam-like components are interconnected by radial spokes and nexin-dynein regulatory complexes (N-DRC). Interdoublet sliding is driven by dynein motor proteins.

limited number of studies directly measure the mechanical properties of the axoneme. Two mechanical parameters that are critical for characterizing the elastic behavior of the axoneme during bending are: 1) the flexural rigidity, EI , defined as the product of the Young’s modulus, E , and the area moment of inertia, I ; and 2) the interdoublet shear stiffness, k_s , defined as the elastic resistance to interdoublet sliding. In a previous study (9), the flexural rigidity of echinoderm sperm flagella, measured by bending with a flexible glass microneedle, was estimated to be in the range of $EI \sim 300\text{--}1500 \text{ pN}\cdot\mu\text{m}^2$. In sea urchin sperm studied with the same method, flexural rigidity was estimated to be $800 \text{ pN}\cdot\mu\text{m}^2$ (10). Using magnetic beads as mechanical probes, the flexural rigidity of human bronchial epithelial cilia was estimated to be $EI = \sim 620 \text{ pN}\cdot\mu\text{m}^2$ on average (11). Unlike a simple elastic beam, the axoneme is a complex bundle of interconnected microtubule doublets. The elastic resistance to interdoublet sliding, as well as the flexural rigidity, is needed to characterize its bending mechanics. The interdoublet shear stiffness of the axoneme is manifested through a characteristic phenomenon: the distal counterbend response to proximal bending (12–14). During large bending deformation, induced by a glass needle in the proximal portion of a sea urchin sperm flagellum, the distal portion of the flagellum exhibited a bend with the opposite curvature; this is referred to as the “counterbend” (13). By incorporating a shear-stiffness term in the classic elastic beam theory to analyze the counterbend curvature, the authors estimated both the intrinsic flexural rigidity ($EI = 100 \text{ pN}\cdot\mu\text{m}^2$) and shear stiffness ($k_s = \sim 6 \text{ pN/rad}$) in sea urchin sperm flagella (13).

The ciliary axoneme is a highly conserved structure with similar protein composition and morphology between mammalian cilia and flagella of the unicellular alga, *Chlamydomonas reinhardtii* (15). Because of the considerable genetic and structural homology with human cilia, *Chlamydomonas* flagella have been used as a model system to investigate mechanisms of primary ciliary dyskinesia and other ciliopathies (16). The cumulative longitudinal shear forces on isolated *Chlamydomonas* axonemes have previously been measured (17); an effective cumulative spring constant was estimated to be $\sim 2 \text{ pN/nm}$ per $1 \mu\text{m}$ of axoneme (17), which for an effective diameter of 180 nm corresponds to $k_s = \sim 65 \text{ pN/rad}$ (13). However, the relationship between the bending compliance of the axoneme and its intrinsic flexural rigidity and interdoublet shear stiffness remains un-

clear, as do the contributions of the different structural components.

In this study, we combine experiment, theory, and modeling to investigate how the overall stiffness of *Chlamydomonas* flagella depends on both the flexural rigidity (attributable to microtubule doublets) and the interdoublet shear stiffness (from interconnecting components). The tip compliance of individual flagella was measured with the optical tweezers, while the interplay between bending and interdoublet shearing was probed by the counterbend induced by a microneedle. We estimated the average intrinsic flexural rigidity (EI) and interdoublet shear stiffness (k_s) in wild-type flagella, in the flagella of the *pf3;cnk11-6* mutant that lacks the N-DRC, and exhibits enhanced tubulin turnover at doublet tip (18–22), and in the flagella of *pf13A* mutants, which lack outer dynein arms and inner dynein arm *c* (23,24). We found that in both wild-type and mutant flagella the apparent flexural rigidity of the axoneme is greatly affected by elastic resistance to interdoublet sliding. Reductions in interdoublet shear stiffness, but not intrinsic flexural rigidity, were detected in both mutants using this approach, allowing us to estimate other contributions of N-DRC to shear stiffness.

MATERIALS AND METHODS

Cell culture and preparation

Wild-type (Strain CC-124), *pf3; cnk11-6* mutant (Strain CC-1026), and *pf13A* mutant (Strain CC-2492) cells were obtained from *Chlamydomonas* Resource Center at the University of Minnesota. Strain construction was performed using standard methods of mating and tetrad dissection (25). Genotypes were verified by PCR and sequencing of the mutations involved (26). In particular, the strain CC-1026 carries a second mutation (*cnk11-6*) in addition to the *pf3* mutation (19) that results in longer flagella (19). *Chlamydomonas* cells were grown in modified Sager and Granick medium (25,27). All measurements were taken using nonbeating flagella with stable length. To suppress dynein activity (and beating), before all experiments, vanadate (Sigma, St. Louis, MO) was added to the medium, at a final concentration of 3 mM to block dynein activity (28). This concentration rendered all cells immotile within 5 min. The loss of motility was similar at higher concentrations of 4 and 5 mM; at 2 mM, cells remained motile for up to 10 min.

Measurement of tip compliance with optical tweezers

The tip compliance (ratio of displacement to force) of *Chlamydomonas* flagella was measured with an optical tweezers system (29). Briefly, an

optical trap and a micropipette controlled by a piezoelectric stage with nanometer resolution were positioned in an experimental chamber just above the objective of an inverted microscope (Fig. 2). Latex beads of 4.5 μm in diameter (Bangs Laboratories, Fishers, IN) were washed twice in PBS without Ca^{2+} and Mg^{2+} (Cambrex BioSciences, Walkersville, MD) containing 0.1% or 1% (w/v) BSA (bovine serum albumin; Fisher Scientific, Pittsburgh, PA) and mixed with the cells. Beads were coated with antibody targeted to flagellar membrane glycoproteins FMG-1 (30) to ensure frequent adhesion between the bead and the flagellum. A coated bead was trapped in an infrared laser focused by the objective. Trap stiffness was calibrated by applying controlled viscous drag forces to trapped beads, whose deflection was recorded and quantified with NanoTrack, a custom-written MatLab script (29). A cell was manipulated into the opening of the micropipette where it was firmly held by suction with one flagellum pointing upwards or downwards. The micropipette was driven toward the bead at 2.5 $\mu\text{m}/\text{s}$, paused for 0.1 s, then retracted at constant speed (Fig. 2, *a-c* and *a'-c'*). Bead deflection was tracked with NanoTrack; cell body displacement was calculated from the speed and duration of motion. The applied pulling force, F , was the product of the trap stiffness and bead deflection; the deflection of the flagellar tip, δ , was the difference between the displacements of the bead and cell body (Fig. 2 *d*). The tip compliance $C = \delta/F$.

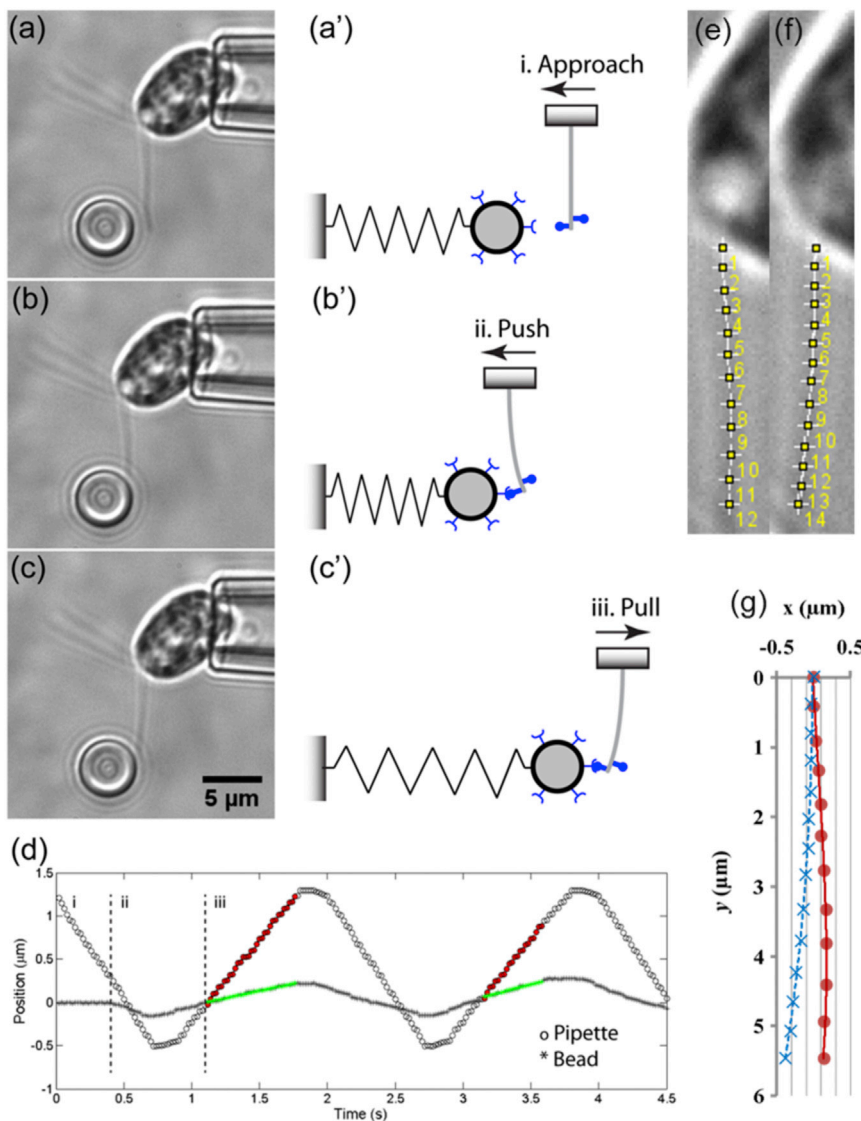


FIGURE 2 Measurement of the apparent flexural rigidity of the flagellar axoneme with optical tweezers. Video micrographs (*a-c*) and corresponding schematics (*a'-c'*) show the flagellum approaching, pushing, and pulling on a trapped bead. The trapped bead functions as a mechanical spring. The cell body was firmly held by micropipette suction and oriented such that force was applied perpendicularly to the flagellar axis. Adhesion between the bead and the flagellum was ensured by coating the bead with antibodies to FMG-1. (*d*) Typical tracking curves for relative pipette and bead positions (two pulling cycles are shown). Pulling forces on the flagellum were calculated from the product of the bead displacement (green curve) and the laser trap stiffness. Flagellar deflections were calculated from the difference between the displacements of the micropipette (red curve) and the bead (green curve). (*e* and *f*) Manual tracking of the flagellar length before (*e*) and after (*f*) bending in (*a*) and (*c*), respectively. (*g*) Superimposition of the tracked flagellar length in (*e*) and (*f*) showing that potential pivoting at the flagellar base is negligible compared with the induced bending close to the tip. To see this figure in color, go online.

Probing the interdoublet shear stiffness through the counterbend response

The effective shear stiffness of *Chlamydomonas* flagella was measured in a microprobe-based manipulation system. The cell body was firmly held by micropipette suction with one flagellum under microscope focus. A thin glass microneedle was driven by a 3D hydraulic micromanipulator (Narishige-US, East Meadow, NY) to approach and bend the flagellum at an intermediate length (Fig. 3, *a* and *b*). The flagellum reverses its curvature distal to the imposed bend beyond the forcing point; this is the counterbend response (Fig. 3 *b*). This behavior is consistent with a simple mechanical model in which doublets are interconnected by elastic elements. Sliding displacement between doublets will result in a local shear force that is proportional to the shear angle relative to the base, θ , modulated by the shear stiffness, k_s (in pN/rad). This effect is explained in the subsections below.

Data analysis: bending of beams with flexural rigidity and interdoublet shear stiffness

To estimate both the intrinsic flexural rigidity and the shear stiffness of the flagellum, we analyze data from both the tip compliance (optical tweezers)

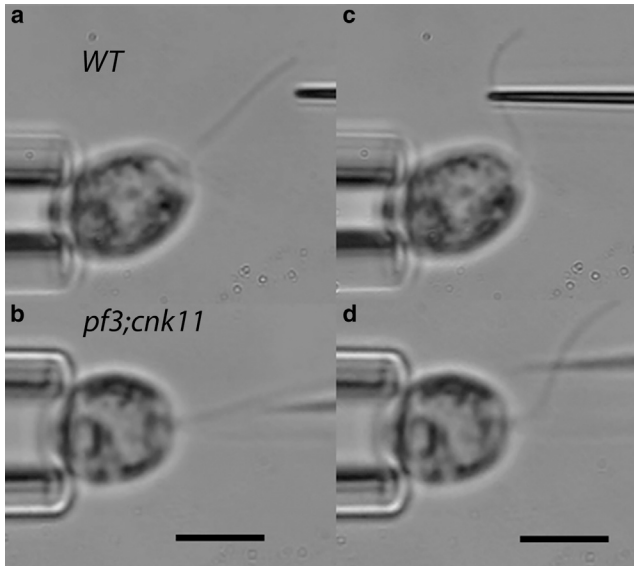


FIGURE 3 Estimation of the ratio of interdoublet shear stiffness to flexural rigidity from the counterbend response of the flagellar axoneme. Video micrographs show a flagellum (*a* and *b*) approached by, and (*c* and *d*) manipulated slowly with, a glass microprobe controlled by a hydraulic micromanipulator. The cell body was firmly held by micropipette suction. A bend of the flagellum is induced by the probe close to the base and is accompanied by a counterbend distal to the probe. Top row (*a* and *c*): wild-type (WT). Bottom row (*b* and *d*): *pf3; cnk11-6* double mutant. Scale bars, 5 μm .

and counterbend experiments in terms of the deflection of a slender beam with flexural rigidity EI ($\text{pN}\cdot\mu\text{m}^2$) and resistance to shear deformation k_s (pN/rad), in response to point-loading at either the tip or near the midpoint (Fig. 4). The base is considered fixed (zero angular compliance). The fixed-base approximation is justified by consistent observations of negligible changes in the angle at the base during flagellar bending examples (e.g., see Fig. 3) in which large bending angles were observed distally.

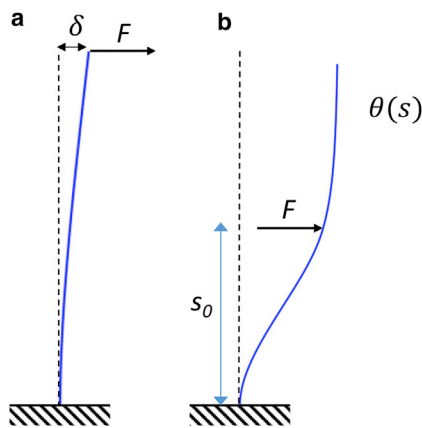


FIGURE 4 Mathematical models of the tip compliance and counterbend experiments. (*a*) A load, F , applied at the tip produces a deflection, δ . The tip compliance $C = \delta/F$ depends on both intrinsic flexural rigidity EI and shear stiffness k_s . (*b*) A load, F , applied near the midpoint (at $s = s_0$) produces a bend-counterbend shape described by the angle $\theta(s)$, which depends on the load amplitude, the location of the load, and on the ratio $\beta^2 = k_s/EI$. To see this figure in color, go online.

Analytical solution for flagellar deflection due to tip loading

The deflection, δ , at the tip of a fixed-free, slender (Euler-Bernoulli) beam with length L and flexural rigidity EI , but no shear stiffness, when a lateral force, F , is applied at the free end, is (31):

$$\delta = FL^3/3EI. \quad (1)$$

This theory must be extended to handle the flagellum, in which there is elastic resistance to shear. For quasi-static bending, equilibrium between moments from bending, shear resistance, and the external force must be maintained:

$$EI \frac{\partial^2 \theta}{\partial s^2} - k_s \theta = -F. \quad (2)$$

A general solution to Eq. 2 is

$$\theta(s) = \frac{F}{k_s} + c_1 e^{\beta s} + c_2 e^{-\beta s}, \quad (3)$$

where $\beta = \sqrt{k_s/EI}$ (in μm^{-1}), and c_1 and c_2 are constants. The two boundary conditions are zero shear angle at the fixed base, $s = 0$:

$$\theta(0) = 0, \quad (4)$$

and zero moment (thus zero curvature) at the tip, $s = L$:

$$\left. \frac{\partial \theta}{\partial s} \right|_{s=L} = 0. \quad (5)$$

Using these two boundary conditions, we can solve for the two constants and obtain the solution for the shear angle

$$\theta(s) = \frac{F}{k_s} \left(1 - \frac{e^{\beta s}}{e^{2\beta L} + 1} - \frac{e^{-\beta s}}{e^{-2\beta L} + 1} \right). \quad (6)$$

Finally, the small deflection of the flagellar tip caused by the force is given by

$$\delta = \int_0^L \theta ds = \frac{FL}{k_s} \left(1 - \frac{1}{\beta L} \cdot \frac{e^{\beta L} - e^{-\beta L}}{e^{\beta L} + e^{-\beta L}} \right). \quad (7)$$

The tip compliance $C = \delta/F$ is thus:

$$C = \frac{L}{k_s} \left(1 - \frac{1}{\beta L} \cdot \frac{e^{\beta L} - e^{-\beta L}}{e^{\beta L} + e^{-\beta L}} \right). \quad (8)$$

The tip compliance depends on length, L , which is measured, as well as the shear stiffness, k_s , and the flexural rigidity, EI , both of which are unknown. Accordingly, counterbend experiments were performed to provide complementary information about the ratio $\beta^2 = k_s/EI$, as described in the next section.

Remark 1. The apparent flexural rigidity (\overline{EI}) of a beam with both flexural rigidity and shear stiffness can be calculated from the measured deflection (by analogy to Eq. 1) as:

$$\overline{EI} = \frac{FL^3}{3\delta}. \quad (9)$$

The ratio of apparent (\overline{EI}) to true flexural rigidity (EI), depends on both the parameter β and the length (L):

$$\frac{\overline{EI}}{EI} = \frac{\beta^3 L^3}{3 \left(\beta L - \frac{e^{\beta L} - e^{-\beta L}}{e^{\beta L} + e^{-\beta L}} \right)}. \quad (10)$$

If $\beta L \ll 1$ (for very small shear stiffness), Eq. 10 predicts $\overline{EI} \approx EI$ as expected.

Remark 2. It can be shown (see Appendix A in the [Supporting Material](#)) that the apparent flexural rigidity \overline{EI} should increase with length for a flagellum fixed at the base. A similar analysis can be performed for a flagellum loaded in “three-point bending”, as in Okuno et al. (28). Importantly, the apparent flexural rigidity \overline{EI} calculated from a three-point bending experiment will generally be different from (lower than) the corresponding value of \overline{EI} calculated from the compliance of a tip-loaded, fixed-free flagellum with the same intrinsic properties (see Appendix A and [Fig. A2](#) in the [Supporting Material](#)).

Analytical solution for flagellar shape in the counterbend experiment

An analytical solution for the shape of the counterbend has been presented recently in Gadêlha et al. (32); it is summarized here in terms of the current nomenclature. The equations of equilibrium (13) between bending and shearing that govern the quasi-static shape of the counterbend, in regions proximal and distal to the point of force application, respectively, are:

$$EI \frac{\partial^2 \theta}{\partial s^2} - k_s \theta = -F, \quad s < s_0, \quad (11a)$$

$$EI \frac{\partial^2 \theta}{\partial s^2} - k_s \theta = 0, \quad s \geq s_0, \quad (11b)$$

where EI is intrinsic flexural rigidity (without the overbar) attributable to the microtubule doublets and central pair.

A general solution to Eqs. 11a and 11b is

$$\theta(s) = \theta_1(s) = \frac{F}{k_s} + c_1 e^{\beta s} + c_2 e^{-\beta s}, \quad s < s_0; \quad (12a)$$

$$\theta(s) = \theta_2(\gamma) = d_1 e^{\beta \gamma} + d_2 e^{-\beta \gamma}, \quad s \geq s_0, \quad \gamma = s - s_0. \quad (12b)$$

Four boundary conditions are required to specify the shape of the flagellum. Two boundary conditions ensure zero angular deflection at the fixed end and zero moment at the free end of the flagellum:

$$BC_1 : \theta_1|_{s=0} = 0, \quad (13)$$

$$BC_2 : \left. \frac{\partial \theta}{\partial s} \right|_{s=L} = \left. \frac{\partial \theta_2}{\partial \gamma} \right|_{\gamma=\gamma_0} = 0, \quad (\gamma_0 = L - s_0). \quad (14)$$

The two remaining conditions ensure continuity of angle and curvature at the point of force application:

$$BC_3 : \theta_1|_{s=s_0} = \theta_2|_{\gamma=0}, \quad (15)$$

$$BC_4 : \left. \frac{\partial \theta_1}{\partial s} \right|_{s=s_0} = \left. \frac{\partial \theta_2}{\partial \gamma} \right|_{\gamma=0}. \quad (16)$$

These boundary conditions lead to algebraic equations that determine the four coefficients (c_1, c_2, d_1, d_2) for given values of F/k_s , β , and s_0 (see Appendix B in the [Supporting Material](#)).

Parameter estimation

First, the parameter β^2 was estimated from counterbend images by fitting the analytical solution (Eqs. 12a and 12b) to the observed flagellar shapes.

Points on the flagellum were selected manually and fitted with a polynomial function for the shear angle, $\theta(s)$, in terms of the axial position, s ([Fig. 5, a](#) and [b](#)), using a previously developed algorithm (33). Numerical optimization (fminsearch; MATLAB, The MathWorks, Natick, MA) was used to find the ratio $\beta^2 = k_s/EI$ (13) and the value of s_0 that minimized the sum of the squared residual error between the analytical solution (Eqs. 12a and 12b) and the observed shear angle at 50 equally spaced points on the flagellum ([Fig. 5, c](#) and [d](#)). The fitting algorithm was validated on data from simulations of Eqs. 11a and 11b (COMSOL, Burlington MA; [Fig. 5, e–h](#)). Estimates were rejected if the squared error of the fitted solution exceeded 2% of the variance of the data, or if the optimized value of s_0 differed from the initial visual estimate s_0 by >10%. Each successful counterbend experiment produced a separate estimate of β^2 , denoted $(\beta^2)^{(n)}$ ($n = 1, 2, \dots, N$). For wild-type cells, $N = 12$ estimates of β^2 were obtained; for *pf3*; *cnk11-6*, $N = 8$, and for *pf13A*, $N = 11$.

Second, data from the tip compliance experiments, consisting of flagellar compliance (measured by optical tweezers) and length, were then used to estimate the physical parameters EI and k_s . In each mutant, the expression for the compliance of the flagellum as a function of length (Eq. 8) was fitted to data from all optical tweezers studies by minimizing the squared residual error between the predicted compliance (Eq. 8) and the data. Because different flagella were used in counterbend and tip compliance experiments, for each estimate $(\beta^2)^{(n)}$ ($n = 1, 2, \dots, N$) from the counterbend experiments in a given mutant, a separate fit was performed to the ensemble of compliance data from that mutant ([Fig. 6](#)). Each such fit produced an independent estimate of $EI^{(n)}$, and a corresponding estimate of $k_s^{(n)} = (\beta^2)^{(n)} EI^{(n)}$.

Third and finally, statistical analysis of β^2 , EI , and k_s estimates was performed using one-way ANOVA followed by multiple comparisons (Tukey-Kramer; MATLAB, The MathWorks). Normal distributions are assumed, and probability $p < 0.05$ was used as the threshold for statistical significance.

RESULTS

The counterbend response indicates shear resistance to interdouplet sliding

When bending was induced by a glass probe close to the base, each flagellum exhibited a counterbend distal to the probe ([Figs. 3](#) and [5](#)). Fitting Eqs. 12a and 12b to each flagellar shape provided an estimate of the ratio of the interdouplet shear stiffness to the intrinsic flexural rigidity ([Fig. 6](#)). For the wild-type flagella ($N = 12$), this ratio is $\beta^2 = 0.111 \pm 0.054 \mu\text{m}^{-2}$; for the *pf3*; *cnk11-6* flagella ($N = 8$) $\beta^2 = 0.041 \pm 0.012 \mu\text{m}^{-2}$; and for the *pf13A* flagella ($N = 11$), $\beta^2 = 0.061 \pm 0.028 \mu\text{m}^{-2}$ ([Fig. 6](#)). Differences between wild-type and *pf3*; *cnk11-6* ($p = 0.0012$) and between wild-type and *pf13A* ($p = 0.0124$) are statistically significant.

Estimates of intrinsic flexural rigidity and interdouplet shear stiffness from tip compliance

We obtained estimates of EI and k_s in each flagella type by fitting Eq. 8 to all the measured values of compliance C from the optical tweezers experiments ([Fig. 2](#)), using each estimate of β^2 from the counterbend experiments in the corresponding flagella type ([Fig. 6](#)). The theoretical expression (Eq. 8) provides reasonably good fits ([Fig. 7](#)) to the compliance data for all values of β^2 , supporting our postulate that

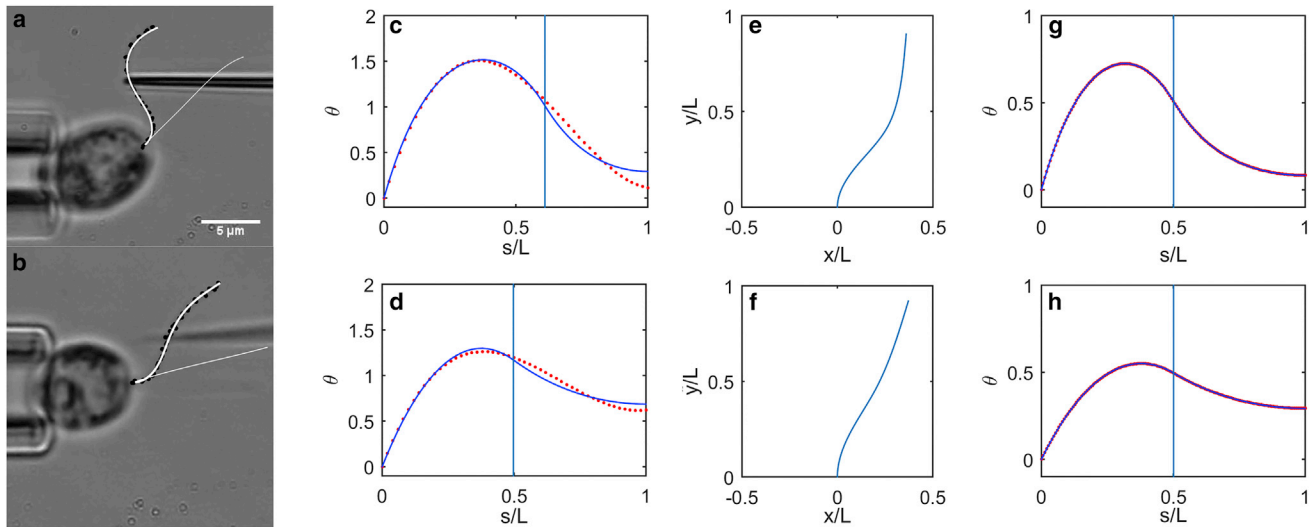


FIGURE 5 Examples of analytical solutions fitted to counterbend data from (a–d) experiment and (e–h) simulation. (a) Flagellum of wild-type *Chlamydomonas* (Fig. 3, a and c) with manually picked points (black dots) and a polynomial curve (thick white line) fitted to these points. The flagellum before bending is also shown (thin white line). (b) Flagellum of *pf3; cnk11-6* *Chlamydomonas* (Fig. 3, b and d) with manually picked points (black dots) and a polynomial curve (white) fitted to these points. (c) Values of $\theta(s)$ (red dots) from polynomial curve fit in (a), and fitted solution (blue curve; Eqs. 12a and 12b) with $\beta^2 = 0.202$, $(\beta L)^2 = 25.5$. (d) Values of $\theta(s)$ (red dots) from a polynomial curve fit in (b), and a fitted solution (blue curve; Eqs. 12a and 12b) with $\beta^2 = 0.053$, $(\beta L)^2 = 5.0$. (e) Simulated shape of a beam with $(\beta L)^2 = 25$. (f) Simulated shape of a beam with $(\beta L)^2 = 5$. (g) Values of $\theta(s)$ at 50 equally spaced points on flagellum (red dots) from simulation with $(\beta L)^2 = 25$ and fitted solution (blue curve; Eqs. 12a and 12b). (h) Values of $\theta(s)$ (red dots) from simulation with $(\beta L)^2 = 5$ and fitted solution (blue curve; Eqs. 12a and 12b). To see this figure in color, go online.

the length-dependency of the compliance reflects both flexural rigidity and interdoublet shear stiffness. Statistical results are shown in Fig. 8.

The intrinsic flexural rigidity (attributed to the microtubule components) of the axoneme is estimated to be $EI = 840 \pm 280 \text{ pN}\cdot\mu\text{m}^2$ for wild-type flagella, $EI = 1011 \pm 183 \text{ pN}\cdot\mu\text{m}^2$ for the *pf3;cnk11-6* mutant, and $EI = 777 \pm 184 \text{ pN}\cdot\mu\text{m}^2$ for *pf13A* flagella, with no significant difference ($p > 0.05$) between any pair of groups (Fig. 8). On the other hand, the interdoublet shear stiffness of the axoneme differs markedly between these cell types: $k_s = 79.6 \pm 10.5 \text{ pN/rad}$ for the wild-type flagella, $k_s = 39.3 \pm 6.0 \text{ pN/rad}$ for the *pf3; cnk11-6* flagella, and

$k_s = 43.3 \pm 7.7 \text{ pN/rad}$ for the *pf13A* flagella. Statistically significant differences ($p < 0.0001$) in k_s are observed between the wild-type flagella and each mutant (Fig. 8), but not between the two mutants. The reduction in shear stiffness in *pf3; cnk11-6* flagella is consistent with the loss of the circumferential linkages of N-DRC between doublets in this mutant. The reduction in shear stiffness in the *pf13A* mutant is consistent with a loss of shear resistance due to dynein arms that apparently contribute even though

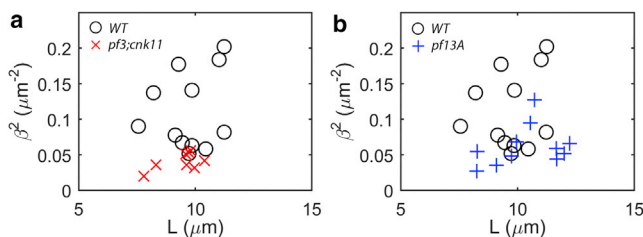


FIGURE 6 Analysis of the counterbend images yields the ratio of shear stiffness to flexural rigidity of the axoneme ($\beta^2 = k_s/EI$); individual estimates of β^2 are shown for (a) wild-type (WT) and *pf3; cnk11-6* flagella, and (b) WT and *pf13A* flagella. A statistically significant difference ($p = 0.0012$) between wild-type ($\beta^2 = 0.111 \pm 0.054 \mu\text{m}^2$) and the *pf3; cnk11-6* mutant ($\beta^2 = 0.041 \pm 0.012 \mu\text{m}^2$). The difference between WT and *pf13A* ($\beta^2 = 0.061 \pm 0.028$) is also statistically significant ($p = 0.012$). To see this figure in color, go online.

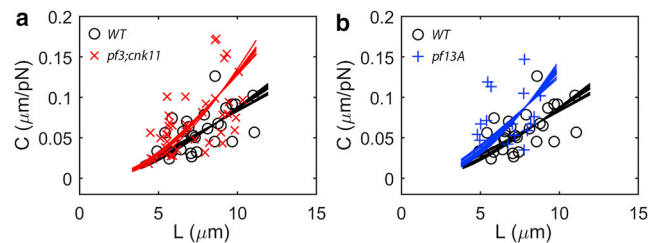


FIGURE 7 Flexural rigidity and shear stiffness are estimated from tip compliance and flagellar length by fitting the theoretical compliance-length relationship (Eq. 8) to data from the optical tweezers experiment. Each data point represents the tip compliance of an individual flagellum of either the (a) wild-type (WT) or *pf3; cnk11-6* mutant, or (b) WT or *pf13A* mutants. Each curve shows the theoretical compliance-length relationship (Eq. 8) for an estimate of β^2 from a specific counterbend experiment in the corresponding flagella type, using the value of k_s (or equivalently, EI) that minimizes the total squared residual error. The mean (\pm SD) fraction of the variance explained by these curve fits is $R^2 = 0.89 \pm 0.01$ in wild-type ($N = 12$ curve fits), $R^2 = 0.76 \pm 0.01$ in *pf3; cnk11-6* ($N = 8$), and $R^2 = 0.79 \pm 0.01$ in *pf13A* ($N = 11$). To see this figure in color, go online.

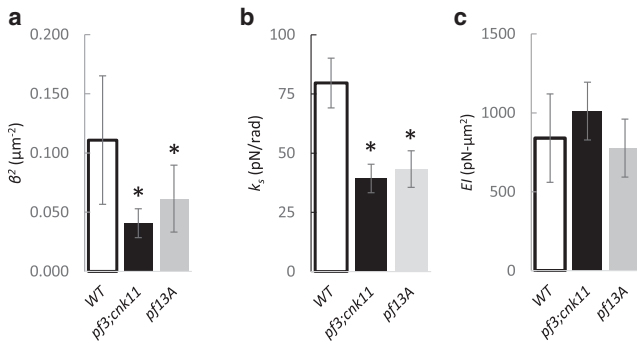


FIGURE 8 (a–c) Estimates of the intrinsic flexural rigidity and the shear stiffness of the axoneme obtained by fitting tip compliance data from optical tweezers studies to Eq. 8, using estimates of β^2 from each counterbend experiment. Asterisks denote statistically significant differences ($p < 0.05$, Tukey-Kramer multiple comparisons) compared to wild-type; p -values for the comparisons with wild-type are given below. The average intrinsic flexural rigidity and interdoublet shear stiffness of the wild-type axoneme are $EI = 840 \pm 280 \text{ pN}\cdot\mu\text{m}^2$ and $k_s = 79.6 \pm 10.5 \text{ pN/rad}$, respectively. The corresponding values for the *pf3; cnk11-6* double mutant are $EI = 1011 \pm 183 \text{ pN}\cdot\mu\text{m}^2$ (NS, $p = 0.240$) and $k_s = 39.3 \pm 6.0 \text{ pN/rad}$ ($p < 0.0001$). The corresponding values for the *pf13A* mutant are $EI = 777 \pm 184 \text{ pN}\cdot\mu\text{m}^2$ (NS, $p = 0.785$) and $k_s = 43.3 \pm 7.7 \text{ pN/rad}$ ($p < 0.0001$).

the cells are in media containing high concentrations of vanadate.

We also estimated the apparent flexural rigidity (Eq. 10, Appendix A in the Supporting Material) of wild-type, *pf3; cnk11-6*, and *pf13A* flagella. The mean (\pm SD) values of the apparent flexural rigidity were $\overline{EI} = 2978 \pm 1636 \text{ pN}\cdot\mu\text{m}^2$ ($L = 7.7 \pm 1.7 \mu\text{m}$) in wild-type flagella, $2155 \pm 1389 \text{ pN}\cdot\mu\text{m}^2$ ($L = 7.2 \pm 1.9 \mu\text{m}$) in *pf3; cnk11-6*, and $1733 \pm 1121 \text{ pN}\cdot\mu\text{m}^2$ ($L = 6.8 \pm 1.4 \mu\text{m}$) in *pf13A*. There was no statistically significant difference between any two groups. However, the apparent flexural rigidity showed a dependence on the flagellar length: the longer the flagellum, the larger the apparent flexural rigidity (Appendix A and Fig. A3 in the Supporting Material). This length-dependence of \overline{EI} confirms the importance of shear stiffness (Appendix A and Fig. A2 in the Supporting Material). Performing two complementary measurements, such as tip compliance and counterbend, is necessary to estimate the intrinsic flexural rigidity.

DISCUSSION

The propulsive effectiveness of motile cilia and flagella relies on coordinated interactions between the mechanics and biochemistry of the axoneme. In this study, we probed two major mechanical parameters of the axoneme: the intrinsic flexural rigidity from the microtubules (outer doublets and central pair), and the interdoublet shear stiffness from interconnecting components. We developed a method, which, to our knowledge, is novel for determining the intrinsic mechanical properties of the axoneme, based on a combination

of experiment and theory. Analytical expressions and finite element simulations (Appendix D and Fig. D2 in the Supporting Material) of a simplified structural model of the axoneme together demonstrate that the compliance, the apparent flexural rigidity, and the counterbend response of the axoneme all depend on the elastic resistance to interdoublet sliding.

We interpret the intrinsic flexural rigidity of the axoneme, EI , as due to the flexural rigidity of the beamlike components of the axoneme, presumably the outer microtubule doublets and the central pair. By analyzing experimental data based on our extended beam theory, we determined the average intrinsic flexural rigidity of the axoneme to be $840 \pm 280 \text{ pN}\cdot\mu\text{m}^2$ for the wild-type axoneme (Fig. 8), and not significantly different in the two mutants ($EI = 1011 \pm 183 \text{ pN}\cdot\mu\text{m}^2$ in *pf3; cnk11-6* flagella and $EI = 777 \pm 184$ in *pf13A*). These EI values are similar to a previous estimate of $900 \text{ pN}\cdot\mu\text{m}^2$ for sea urchin sperm (28). For comparison, the flexural rigidity of individual microtubules was previously measured to be $\sim 20\text{--}30 \text{ pN}\cdot\mu\text{m}^2$ (34,35) (we note that other estimates are in the range of $5\text{--}8 \text{ pN}\cdot\mu\text{m}^2$ (36,37)). Because the axoneme contains ~ 20 microtubules (18 combined into 9 outer doublets and 2 from the central pair), the combined overall flexural rigidity for the axoneme is at least 20 times of that for a single microtubule. If we accept the larger estimates of microtubule stiffness in the literature (34,35) the current estimates of intrinsic flexural rigidity ($\sim 800\text{--}1000 \text{ pN}\cdot\mu\text{m}^2$) in *Chlamydomonas* flagella appear reasonable, considering that the bending stiffness of microtubule doublets should be larger than the sum of the bending stiffness from two individual microtubules (the area moment of inertia of the doublet is the sum of the area moments of inertia of two, almost-complete, microtubules relative to their own longitudinal axes, plus an additional amount due to the distance of the individual microtubule axes from the common parallel axis).

While the difference in EI between wild-type and *pf3; cnk11-6* flagella is not statistically significant, a small increase in the intrinsic flexural rigidity of *pf3; cnk11-6* flagella could reflect the effects of altered microtubule doublet ultrastructure. Axonemes of *pf3* mutants exhibit reduced levels of tektin, a filament protein that associates closely with tubulins in doublet microtubules (18–22). Microtubule doublets in the *cnk11* strain also exhibit altered tubulin dynamics (19) that mirror the effects of Taxol treatment (38).

The average interdoublet shear stiffness, k_s , was estimated to be $k_s = 79.6 \pm 10.5 \text{ pN/rad}$ for the wild-type flagellum, immobilized by vanadate in vivo. This shear stiffness includes the contributions of the N-DRC, as well as contributions of the radial spokes and any dynein arms that are not completely inactivated by vanadate. To estimate the contributions of individual components, we also measured k_s in flagella of *Chlamydomonas* mutants with specific axonemal defects. The interdoublet shear stiffness of *pf3; cnk11-6* flagella was $k_s = 39.3 \pm 6.0 \text{ pN/rad}$

(Fig. 8), which is significantly less than that of the wild-type flagella ($p < 0.0001$). Previous studies have shown that the *pf3* and *pf3; cnk11-6* mutants lack the N-DRC. A plausible interpretation of our current results is that the contribution of the N-DRC to the shear stiffness is the difference between the k_s estimates in wild-type and *pf3; cnk11-6*:

$$k_s^{(\text{NDRC})} = k_s^{(\text{WT})} - k_s^{(\text{pf3})} \approx 40 \text{ pN/rad.} \quad (17)$$

This estimate of $k_s^{(\text{NDRC})}$ is larger than an estimate of ~ 6 pN/rad for demembrated sea urchin sperm axoneme obtained in a previous study (13). Notably, the counterbends observed in the prior study correspond to values of $\beta^2 = k_s/EI = 0.03\text{--}0.08 \mu\text{m}^{-2}$ (13), which are very similar to the values of β^2 found in this study. Thus this study and the prior study (13) agree with respect to the ratio of shear stiffness to flexural rigidity, but differ with respect to the total stiffness. In other previous work, Minoura et al. (17) measured the cumulative interdoublet longitudinal shear resistance, K_L , by applying longitudinal shear forces on isolated *Chlamydomonas* axonemes. This elastic constant was estimated by the authors to be $K_L = 2 \pm 0.8$ pN/nm per 1- μm section of the axoneme (17). To compare this to the current estimates of shear stiffness due to N-DRC (~ 40 pN/rad), we invoke Eq. D8 (see Appendix D in the Supporting Material) with $w = 180$ nm (following Pelle et al. (13)), and confirm that the data from Minoura et al. (17) are consistent with a value of $k_s = 65 \pm 26$ pN/rad.

Studies with the *pf13A* mutant address the contribution of residual dynein activity to the shear stiffness of flagella in the wild-type and *pf3;cnk11-6* mutant cells. Although a very high concentration of vanadate is present in the medium that contains the cells, and ATP is likely maintained at normal levels in the flagellum (~ 1.2 mM (39)), rendering flagella immotile, some dynein interactions with the microtubule doublets appear to remain and to resist shear. The difference (~ 35 pN/rad) between the k_s values in wild-type flagella and *pf13A* flagella is a plausible estimate of the stiffness provided by the outer and inner dynein arms that are missing in the *pf13A* mutant, but present in wild-type flagella. We note that the *pf13A* mutant retains inner dynein arms that may resist shear.

It is not clear why the interdoublet shear stiffness might differ between *Chlamydomonas* flagella and sea urchin sperm flagella, but differences in estimates of k_s might partly be due to structural differences in the two axonemes. For example, the N-DRC in *Chlamydomonas* has a bifurcated structure with two apparent interfaces with the B doublet microtubule, whereas one of the bifurcated heads of N-DRC from sea urchin sperm appears shorter and is possibly noninteracting (40). Thus the N-DRC in *Chlamydomonas* flagella may provide relatively more resistance to the interdoublet sliding than it does in sea urchin sperm. Also, although the overall structures of the radial spokes are similar between *Chlamydomonas* flagella and sea urchin

sperm flagella (40), studies have shown that the radial spokes in *Chlamydomonas* flagella are structurally heterogeneous (41). Unlike flagella of other species with three regular radial spoke components (RS1, RS2, and RS3) that share the same structure, *Chlamydomonas* flagella have only two complete radial spoke components, RS1 and RS2, per axonemal repeat. The RS3S structure is structurally distinct in length, morphology, and anchoring to the microtubule doublets (41). In addition, radial spokes (RS1 and RS2) in *Chlamydomonas* flagella appear to be thicker and possess larger anchoring heads (Fig. 3, G and H, in Barber et al. (41)) than those in sea urchin sperm (Fig. 3 f in Nicastro et al. (42)). It seems counterintuitive that *Chlamydomonas* flagella, with fewer radial spokes, exhibit higher shear stiffness than sea urchin sperm flagella, but possible differences in interactions between N-DRCs and doublets may cause differences in resistance to interdoublet sliding. The possibility that true differences in flexural rigidity and interdoublet shear stiffness exist between different species warrants further study.

We note that the apparent flexural rigidity of *Chlamydomonas* flagella, \overline{EI} , as measured by optical tweezers, ranged from ~ 1000 to 4000 pN $\cdot\mu\text{m}^2$ for flagellar lengths from 4 to 10 μm (Appendix A and Fig. A3 in the Supporting Material). The magnitude of the apparent flexural rigidity is comparable to, but generally higher than, previous measurements on sperm flagella (9,10,13) and airway epithelial cilia (11), all of which fell in the range of 300–1500 pN $\cdot\mu\text{m}^2$. Some variations in measured values might result from structural differences among sperm flagella, mammalian cilia, and algal flagella (7,42–44). However, shear stiffness, flagellar length, loading, and boundary conditions all affect estimates of \overline{EI} (Appendix SA). Our analysis confirms that when shear stiffness is significant, the apparent flexural rigidity of the flagellum, whether estimated by tip bending or three-point bending (28), depends on all these parameters (Appendix A and Fig. A2 in the Supporting Material). Thus measurements of bending stiffness or tip compliance should be complemented by independent measurements to assess the specific roles of flexural rigidity and shear stiffness.

CONCLUSIONS

In this study, we have developed an approach which, to our knowledge, is novel, combining two experimental protocols and corresponding theory, to quantify the intrinsic mechanical properties of the axoneme in *Chlamydomonas* flagella. These biophysical parameters are essential to investigations based on modeling and simulation (12,13,45). In particular, during ciliary beating, active dynein forces are balanced by both internal elastic forces within the axoneme and external viscous fluid drag (8,33). The intrinsic biomechanical properties are critical to accurate estimation of active forces generated by dynein motors (8). This study thus represents progress toward the long-term goal of quantitative

understanding of axonemal mechanics and function, which may ultimately lead to the development of novel diagnostic and therapeutic methods.

SUPPORTING MATERIAL

Supporting Materials and Methods and six figures are available at [http://www.biophysj.org/biophysj/supplemental/S0006-3495\(16\)30299-5](http://www.biophysj.org/biophysj/supplemental/S0006-3495(16)30299-5).

AUTHOR CONTRIBUTIONS

P.V.B., S.K.D., J.-Y.S., and G.X. designed research; G.X., K.S.W., and R.J.O. performed experiments and analyzed data; G.X. and P.V.B. developed the theory and model; and G.X., P.V.B., and S.K.D. wrote the article.

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