Optical π phase shift created with a single-photon pulse

Daniel Tiarks, Steffen Schmidt, Gerhard Rempe, Stephan Dürr*

A deterministic photon-photon quantum logic gate is a long-standing goal. Building such a gate becomes possible if a light pulse containing only one photon imprints a phase shift of π onto another light field. We experimentally demonstrate the generation of such a π phase shift with a single-photon pulse. A first light pulse containing less than one photon on average is stored in an atomic gas. Rydberg blockade combined with electromagnetically induced transparency creates a phase shift for a second light pulse, which propagates through the medium. We measure the π phase shift of the second pulse when we postselect the data upon the detection of a retrieved photon from the first pulse. This demonstrates a crucial step toward a photon-photon gate and offers a variety of applications in the field of quantum information processing.

INTRODUCTION

Photons are interesting as carriers of quantum information because they hardly interact with their environment and can easily be transmitted over long distances. A deterministic photon-photon gate could be used as the central building block for universal quantum information processing (QIP) (1). Such a gate can be built if a "control" light pulse containing only one photon imprints a π phase shift onto a "target" light pulse (2). Because the interaction between optical photons in vacuum is extremely weak, an effective interaction between photons must be mediated by matter to create the required phase shift. Physical mechanisms that yield a large target phase shift created by a single control photon are difficult to find. One promising strategy is to couple an optical resonator to an atom, an atomic ensemble, or a quantum dot (3–7). Another possible implementation is electromagnetically induced transparency (EIT) (8), but for EIT with low-lying atomic states, the single-photon phase shifts measured to date are on the order of 10^{-5} rad (9–11), which is much too small. Building a photon-photon gate by applying a small controlled phase shift to an ancillary coherent pulse with a large mean photon number has been proposed (12), but the best performance achieved so far (11) produced a phase shift of 18 μrad at a single-shot resolution for a measurement of the ancilla phase of 50 mrad, which is several orders of magnitude away from the goal. However, the combination with Rydberg states makes EIT very appealing (13–18).

So far, three experiments (3, 4, 16) demonstrated an optical phase shift per photon between π/10 and π/3; only one experiment (6) reached π. However, none of the schemes used in these experiments is applicable to deterministic optical QIP. Two of these experiments (6, 16) measured self-phase modulation of a single continuous wave (CW) light field, but deterministic optical QIP requires that one light field controls another. The other two experiments (3, 4) measured cross-phase modulation (XPM), which is created by one CW light field for another CW light field. However, an extension of these XPM experiments from CW light to a single photon, which must inherently be pulsed, is hampered by the fact that to spectrally resolve the two pulses, the pulses would need a duration that exceeds the typical time scale of the XPM, given by the resonator decay time. Moreover, there is a

no-go theorem (19–21) that claims that it is impossible to achieve deterministic optical QIP on the basis of a large single-photon XPM.

Here, we show that the shortcomings of the existing experiments can be overcome by storing a control light pulse in a medium, letting a target light pulse propagate through the medium, and eventually retrieving the stored control excitation, similar to a proposal by Gorshkov et al. (14). Storage and retrieval circumvent the no-go theorem because it only applies to two simultaneously propagating light fields. We measure the controlled phase shift, that is, by how much the presence of the control pulse changes the target pulse phase. We harvest the strong interactions in Rydberg EIT to create a large controlled phase shift. The incoming control pulse contains 0.6 photons on average. We obtain a controlled phase shift of 3.3 ± 0.2 rad, which was postselected upon the detection of a retrieved control photon.

RESULTS

The experiment begins with the preparation of a cloud of typically 1.0×10^5 ^{87}Rb atoms at a temperature of typically 0.5 μK in an optical dipole trap (see Materials and Methods), which creates a box-like potential along the z axis, somewhat similar to the experiment by Kuga et al. (22). We create Rydberg EIT with the beam geometry shown in Fig. 1A. The 780-nm signal beam propagates along the z axis. This is an attenuated laser beam with Poissonian photon number distribution. The mean photon number in this beam is $\langle n_c \rangle = 0.6$ for the control pulse and $\langle n_t \rangle = 0.9$ for the target pulse. A 480-nm EIT-coupling beam used for the control pulse counterpropagates the signal beam. Another 480-nm EIT-coupling beam used for the target pulse copropagates with the signal beam. The coupling light power P_c is $(P_{c,c}, P_{c,t}) = (70, 22)$ mW for control and target. The waists ($1/e^2$ radii of intensity) are $(w_s, w_{c,c}, w_{c,t}) = (8, 21, 12)$ μm. Using the methods described by Baur et al. (23), we estimate coupling Rabi frequencies of $(\Omega_{c,c}, \Omega_{c,t})/2\pi = (18, 18)$ MHz. The coupling beams address principal quantum numbers $n_c = 69$ and $n_t = 67$ (Fig. 1B). This pair of states features a Förster resonance with a van der Waals coefficient of $C_6 = 2.3 \times 10^{23}$ atomic units (au) (17). The timing sequence is shown in Fig. 1C.

Signal light transmitted through the atomic cloud is coupled into a single-mode optical fiber (omitted in Fig. 1A) to suppress stray light.

Max-Planck-Institut für Quantenoptik, Hans-Kopfermann-Straße 1, 85748 Garching, Germany.
*Corresponding author. E-mail: stephan.duerr@mpq.mpg.de
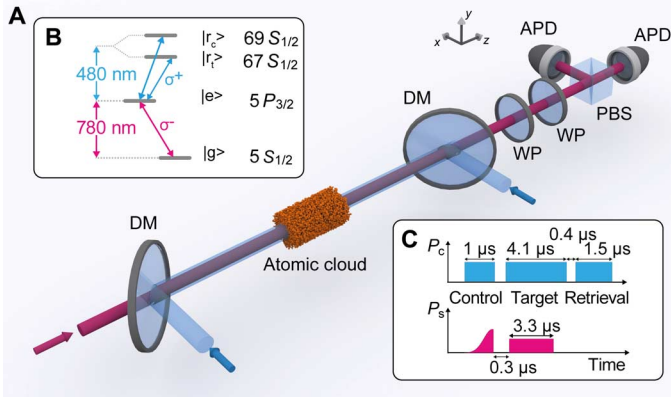
Fig. 1. Experimental procedure. (**A**) Scheme of the experimental setup. Signal light (red) illuminates an atomic gas. Two additional beams (blue) provide EIT-coupling light, one copropagating and the other counterpropagating the signal light. Dichroic mirrors (DMs) overlap and separate the beams. The polarization of transmitted signal light is measured using wave plates (WPs), a polarizing beam splitter (PBS), and avalanche photodiodes (APDs). (**B**) Level scheme. The 780-nm signal light couples states $|g\rangle = |5S_{1/2},$ $F = 2, m_F = -2\rangle$ and $|e\rangle = |5P_{3/2}, F = 3, m_F = -3\rangle$. The 480-nm EIT-coupling light couples states $|e\rangle$ and $|r\rangle = |nS_{1/2}, F = 2, m_F = -2\rangle$, with $n_c = 69$ and $n_t = 67$ for control and target pulse, respectively. (**C**) Timing sequence of input powers of coupling light P_c and signal light P_s. The control pulse is stored in the medium, the target pulse propagates through the medium picking up a π phase shift if a control excitation was stored, and, eventually, the control excitation is retrieved.

The polarization of the light is then measured using a PBS and two APDs. The polarization measurement basis is selected using WPs in front of the PBS. The probability of collecting and detecting a transmitted signal photon is 0.25.

As shown in Fig. 1B, the target signal light is σ^--polarized. To measure the phase shift that it experiences, we add a small σ^+-polarized component. This component serves as a phase reference because the phase shift that it experiences can be neglected because it is smaller by a factor of 15 than that for σ^-. Hence, a phase shift of the σ^- component can be detected as a polarization rotation of transmitted target signal light (see Materials and Methods). Consider a target input polarization state $|\psi_{in}\rangle = c_+|\sigma^+\rangle + c_-|\sigma^-\rangle$ with amplitudes c_+ and c_-. Depending on whether 0 or 1 control excitations are stored, the output state will be

$$|\psi_{out,0}\rangle \propto (c_+|\sigma^+\rangle + c_- e^{-OD_0/2} e^{i\varphi_0}|\sigma^-\rangle) \otimes |0\rangle \qquad (1)$$

$$|\psi_{out,1}\rangle \propto (c_+|\sigma^+\rangle + c_- e^{-OD_1/2} e^{i\varphi_1}|\sigma^-\rangle) \otimes |1\rangle \qquad (2)$$

where OD_j and φ_j are the optical depth and the phase shift experienced by $|\sigma^-\rangle$, given that j control excitations are stored. The goal is to achieve $\varphi_1 - \varphi_0 = \pi$.

Figure 2 (A and B) shows the measured EIT spectra of the transmission e^{-OD_0} and the phase shift φ_0 of the signal light in the absence of control pulse recorded with 1.0×10^5 atoms at a peak density of $\rho = 1.8 \times 10^{12}$ cm^{-3}. To model these quantities, we note that the electric
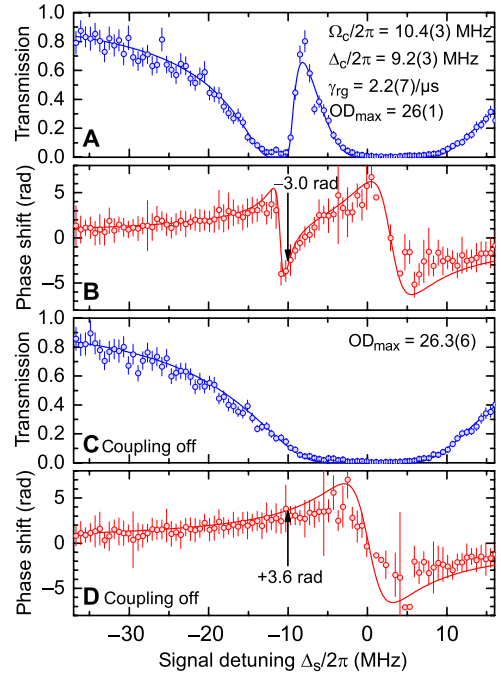

Fig. 2. Rydberg-EIT spectra without control pulse. (**A** and **B**) The transmission e^{-OD_0} and phase shift φ_0 of the target signal beam are shown as a function of the signal detuning Δ_s. The line in (A) shows a fit based on Eq. (3). The line in (B) shows the expectation from Eq. (3) for the parameter values obtained in (A). For further experiments, we choose $\Delta_s/2\pi = -10$ MHz (arrow), which is near the minimum of φ_0. (**C** and **D**) For reference, similar spectra are shown in the absence of coupling light. All error bars in this article represent a statistical uncertainty of ±1 SD.

susceptibility for EIT in a ladder-type level scheme, calculated analogously to the finding of Fleischhauer *et al.* (*8*), is

$$\chi = i\chi_0 \Gamma_e \left(\Gamma_e - 2i\Delta_s + \frac{|\Omega_c|^2}{\gamma_{rg} - 2i(\Delta_c + \Delta_s)} \right)^{-1} \qquad (3)$$

where $\Gamma_e = 1/(26$ ns$)$ is the population decay rate of state $|e\rangle$; γ_{rg} is the dephasing rate between $|g\rangle$ and $|r\rangle$; Ω_c is the coupling Rabi frequency; $\Delta_s = \omega_s - \omega_{s,res}$ and $\Delta_c = \omega_c - \omega_{c,res}$ are the single-photon detunings of signal and coupling light, respectively; and $\chi_0 = 2\rho|d_{eg}|^2/\epsilon_0\hbar\Gamma_e$ is the value of $|\chi|$ for $\Omega_c = \Delta_s = 0$, where ϵ_0 is the vacuum permittivity, d_{eg} is the electric dipole matrix element for the signal transition, and ρ is the atomic density. Propagating through a medium of length L yields an optical depth of $OD = k_s L Im(\chi)$ and a phase shift of $\varphi = k_s L Re(\chi)/2$, where k_s is the vacuum wave vector of the signal light. The best-fit values obtained from Fig. 2A agree fairly well with the expectations from the atomic density distribution, the coupling light intensity, and the value of γ_{rg} measured at this density by Baur *et al.* (*23*). For later reference, Fig. 2 (C and D) shows the spectra in the absence of coupling light.

We now turn to the effect of adding a control pulse on φ. Note that unlike the target pulse, the control pulse is operated at $\Delta_s = \Delta_c = 0$ to optimize storage efficiency. The combined efficiency for storage and
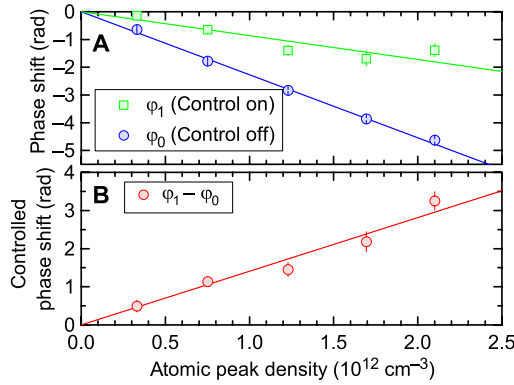
Fig. 3. Controlled phase shift. (**A**) The phase shift φ_0 in the absence of a control pulse (blue circles) depends linearly on atomic density, so does the phase shift φ_1 in the presence of a control pulse (green squares) but with a different slope because of Rydberg blockade. (**B**) The difference between the two phase shifts yields the controlled phase shift $\varphi_1 - \varphi_0$, which is equal to 3.3 ± 0.2 rad for the rightmost data point. The lines show linear fits.

retrieval of the control pulse is 0.2 for negligible delay between storage and retrieval, and it drops to 0.07 after 4.5 µs in the absence of target light. The probability of storing more than one control excitation is suppressed by Rydberg blockade. Exploring what limits the efficiency is beyond the present scope. For dephasing due to thermal motion, we expect a $1/e$ time of $\approx$30 µs, indicating that other decoherence mechanisms dominate.

Figure 3 shows a measurement of the controlled phase shift $\varphi_1 - \varphi_0$ at $\Delta_s/2\pi = -10$ MHz. Clearly, a controlled phase shift of π is reached. The φ_1 data (green) were postselected upon the detection of a retrieved control excitation to eliminate artifacts from imperfect storage efficiency. To change the density, we varied the atom number loaded into the trap, which had little effect on the atomic temperature. The first 0.8 µs of the target pulse is ignored in Fig. 3 because transmission and phase show some transient, partly caused by the different group delays of $|\sigma^-\rangle$ and $|\sigma^+\rangle$.

There is a quantitative connection between Figs. 2 and 3. This is because when a control pulse is stored, Rydberg blockade pushes the EIT feature to very different frequencies (see Materials and Methods), so that, over the relevant frequency range, the blockaded part of the medium will take on the value of χ corresponding to Fig. 2D. If one excitation blockaded the complete medium, then the reference spectrum measured in Fig. 2D would match φ_1. At $\Delta_s/2\pi = -10$ MHz, the lines in Fig. 2 (B and D) would then predict a controlled phase shift of $\varphi_1 - \varphi_0 = 6.6$ rad. In our experiment, the blockade region has a length of $2R_b$, where the blockade radius R_b (17) is estimated to be $R_b = |C_6/\hbar\Delta_T|^{1/6} = 14$ µm, with the full width at half maximum (FWHM) of the EIT transmission feature $\Delta_T/2\pi = 3.7$ MHz extracted from Fig. 2A. With $L = 61$ µm (see Materials and Methods), we expect a controlled phase shift of $\varphi_1 - \varphi_0 = (2R_b/L)6.6$ rad = 3.0 rad. This agrees fairly well with the measurement in Fig. 3B, where the linear fit displays a controlled phase shift of 2.5 rad at $\rho = 1.8 \times 10^{12}$ cm^{-3}.

For the fidelity achievable in a future quantum gate, how well the phase coherence between the σ^+ and σ^- components of the target signal light is maintained when creating the controlled π phase shift will

be crucial. This can be quantified in terms of the visibility V (see Materials and Methods). For the rightmost data point in Fig. 3, the polarization tomography from which we extract φ_1 yields $V = 0.75 \pm 0.14$.

DISCUSSION

To summarize, we implemented a scheme in which a control pulse containing one photon imprinted a phase shift onto a target light field and measured a controlled phase shift of 3.3 rad. Our implementation offers a realistic possibility to be extended to building a photon-photon quantum gate in a future application. Because the $|\sigma^+\rangle$ polarization is no longer needed as a phase reference when operating the gate, the polarization state of the target signal pulse would immediately be available as one of the qubits. We emphasize that the phase coherence properties of this qubit have already been explored in our present work by measuring the visibility. The control qubit could be a dual-rail qubit (24, 25) consisting of two beams propagating parallel to each other in the same atomic cloud with a relative distance larger than the blockade radius, such that the target beam overlaps with only one of the rails. On the input and output side, the dual-rail qubit could be conveniently mapped onto a polarization qubit such as that presented by Choi et al. (26). A related experiment was simultaneously performed at the Massachusetts Institute of Technology (27).

MATERIALS AND METHODS

Optical dipole trap
The dipole trap consists of a horizontal laser beam with a wavelength of 1064 nm, a waist of 140 µm, and a power of 3.2 W. This causes negligible axial confinement along the z axis and a measured radial trapping frequency of 90 Hz. In addition, we used two light beams with wavelengths of 532 nm, waists of 25 µm, and powers of 0.10 W each. These "plug" beams perpendicularly intersect the dipole-trapping beam and provide a box-like potential along the z axis. The distance between the centers of the two plug beams is $\Delta z = 120$ µm. After carefully leveling the direction of the 1064-nm beam relative to gravity, the overall configuration creates a medium that is, to a good approximation, axially homogeneous. Using a polarizability of $\alpha = 711$ au (28) for the $5S$ state at 1064 nm, where 1 au is equal to 1.649×10^{-41} J(m/V)^2, we estimated a radial root mean square cloud size of $\sigma_r = 12$ µm. Using $\alpha = -250$ au (29) for the $5S$ state at 532 nm, we estimated an axial FWHM cloud size of $L = 61$ µm. Note that L is smaller than Δz because the atomic temperature is much lower than the barrier height created by the plug beams. The radial inhomogeneity of the medium has little effect because $w_s < \sigma_r$. A magnetic field of $\approx$100 µT was applied along the z axis to stabilize the orientation of the atomic spins. The two plug beams were generated by sending one light beam into an acousto-optic modulator driven with the sum of two sinusoidal radio frequency (rf) fields, thus generating two first-order diffracted output light beams. This makes Δz and, hence, L, easily adjustable by changing the frequencies of the rf fields.

The dipole trap was loaded from a magnetic trap. Before the transfer, the atomic cloud was cigar-shaped with the x axis as the symmetry axis. After the transfer, the cloud remained cigar-shaped but with the z axis as the symmetry axis. This transfer from one elongated trap into another perpendicularly elongated trap is nontrivial. It turns out that

the atom number fluctuations added by the transfer are minimized, if we first slowly ramp up another 1064-nm dipole-trapping beam propagating along the y axis, which forces the cloud into an almost spherical shape during transfer. Second, we slowly ramped up the dipole-trapping beam along the z axis together with the plug beams. Third, we slowly ramped down the magnetic trap, and finally, we slowly ramped down the dipole-trapping beam along the y axis.

The 480-nm coupling light created a repulsive potential, which was added to the dipole trap potential. The coupling light was on for only a few microseconds, and the experiment was repeated every 100 μs. This low-duty cycle was chosen because it made the effect of the repulsive potential negligible, as in Tiarks et al. (17) and Baur et al. (23).

Polarization tomography and visibility

To measure the phase shift φ_j in Eqs. (1) and (2), we performed tomography of the output polarization state of the target signal light. To this end, the experiment was repeated many times for any given set of experimental parameters. In each repetition, one of three polarization measurement bases was chosen. These bases were horizontal/vertical (H/V), diagonal/antidiagonal (D/A), and left/right circular (L/R). Combination of these measurements yields the normalized Stokes parameters S_{HV}, S_{DA}, and S_{LR}, where $S_{kl} = (P_k - P_l)/(P_k + P_l)$ and P_k is the light power in polarization k. The normalized Stokes parameters contain the complete information about the polarization state of the light. We expressed the normalized Stokes vector in spherical coordinates as $(S_{HV}, S_{DA}, S_{LR}) = S_0 (\sin \vartheta \cos \varphi, \sin \vartheta \sin \varphi, \cos \vartheta)$. Hence, we obtained radius S_0, polar angle ϑ, and azimuth φ. We chose the amplitudes c_+ and c_- of the input state of the signal polarization to be real and positive. Hence, the azimuth φ equals, modulo 2π, the phase shift φ_j in Eqs. (1) and (2). Thus, the tomography yields φ_j.

Alternatively, one could, in principle, determine the azimuth φ by measuring in many bases with linear polarizations, which include various angles α with the horizontal polarization. In this case, one would expect to measure a transmitted power $P_\alpha = P_{total}[1 + V \cos(\varphi - 2\alpha)]/2$ with $P_{total} = P_H + P_V$ and fringe visibility $V = S_0 \sin \vartheta$.

From our polarization tomography measurements, we extracted a visibility $V = \sqrt{S_{HV}^2 + S_{DA}^2}$. The visibility characterizes the phase coherence properties of the polarization of the target signal pulse. The ratio of c_+ and c_- in the input polarization was chosen to maximize V for the measurement of φ_1.

Sign of the Rydberg-blockade shift

If the propagating target excitation and the stored control excitation have a relative distance r, then their van der Waals potential is $V = -C_6/r^6$. For small r values, this creates Rydberg blockade. In our experiment, the positive sign of C_6 implies an attractive van der Waals interaction, which lowers the energy of the Rydberg pair state. At fixed detuning Δ_c of the EIT-coupling laser, the EIT feature is therefore shifted to smaller signal detuning Δ_s, that is, further to the left in Fig. 2B. This is advantageous because there is no radius r at which the left side of the EIT feature, where the phase shift is large and positive, would appear at $\Delta_s/2\pi = -10$ MHz. Hence, when r continuously decreases from infinity to near zero, $\text{Re}(\chi)$ as a function of radius starts out at the value relevant for Fig. 2B and monotonically approaches the value relevant for Fig. 2D. This avoids the Raman resonance, as discussed by Gorshkov et al. (14).

Had we reversed the signs of Δ_s and Δ_c, then for decreasing r, $\text{Re}(\chi)$ would first overshoot to large positive values at the Raman resonance

before settling down to the value relevant for Fig. 2D. Integration of $\text{Re}(\chi)$ over distance would then yield a reduced controlled phase shift, which is undesirable. We experimentally tested this and found that the controlled phase shift was indeed reduced by a factor of roughly 1.5. A similar asymmetry under a simultaneous sign reversal of Δ_s and Δ_c was observed by Firstenberg et al. (16).

REFERENCES AND NOTES

1. M. A. Nielsen, I. L. Chuang, Quantum Computation and Quantum Information (Cambridge Univ. Press, Cambridge, 2000).
2. G. J. Milburn, Quantum optical Fredkin gate. Phys. Rev. Lett. 62, 2124–2127 (1989).
3. Q. A. Turchette, C. J. Hood, W. Lange, H. Mabuchi, H. J. Kimble, Measurement of conditional phase shifts for quantum logic. Phys. Rev. Lett. 75, 4710–4713 (1995).
4. I. Fushman, D. Englund, A. Faraon, N. Stoltz, P. Petroff, J. Vučković, Controlled phase shifts with a single quantum dot. Science 320, 769–772 (2008).
5. V. Parigi, E. Bimbard, J. Stanojevic, A. J. Hilliard, F. Nogrette, R. Tualle-Brouri, A. Ourjoumtsev, P. Grangier, Observation and measurement of interaction-induced dispersive optical nonlinearities in an ensemble of cold Rydberg atoms. Phys. Rev. Lett. 109, 233602 (2012).
6. J. Volz, M. Scheucher, C. Junge, A. Rauschenbeutel, Nonlinear π phase shift for single fibre-guided photons interacting with a single resonator-enhanced atom. Nat. Photonics 8, 965–970 (2014).
7. A. Reiserer, N. Kalb, G. Rempe, S. Ritter, A quantum gate between a flying optical photon and a single trapped atom. Nature 508, 237–240 (2014).
8. M. Fleischhauer, A. Imamoglu, J. P. Marangos, Electromagnetically induced transparency: Optics in coherent media. Rev. Mod. Phys. 77, 633–673 (2005).
9. H.-Y. Lo, Y.-C. Chen, P.-C. Su, H.-C. Chen, J.-X. Chen, Y.-C. Chen, I. A. Yu, Y.-F. Chen, Electromagnetically-induced-transparency-based cross-phase-modulation at attojoule levels. Phys. Rev. A 83, 041804 (2011).
10. B.-W. Shiau, M.-C. Wu, C.-C. Lin, Y.-C. Chen, Low-light-level cross-phase modulation with double slow light pulses. Phys. Rev. Lett. 106, 193006 (2011).
11. A. Feizpour, M. Hallaji, G. Dmochowski, A. M. Steinberg, Observation of the nonlinear phase shift due to single post-selected photons. Nat. Phys. 11, 905–909 (2015).
12. K. Nemoto, W. J. Munro, Nearly deterministic linear optical controlled-NOT gate. Phys. Rev. Lett. 93, 250502 (2004).
13. A. K. Mohapatra, T. R. Jackson, C. S. Adams, Coherent optical detection of highly excited Rydberg states using electromagnetically induced transparency. Phys. Rev. Lett. 98, 113003 (2007).
14. A. V. Gorshkov, J. Otterbach, M. Fleischhauer, T. Pohl, M. D. Lukin, Photon-photon interactions via Rydberg blockade. Phys. Rev. Lett. 107, 133602 (2011).
15. Y. O. Dudin, A. Kuzmich, Strongly interacting Rydberg excitations of a cold atomic gas. Science 336, 887–889 (2012).
16. O. Firstenberg, T. Peyronel, Q.-Y. Liang, A. V. Gorshkov, M. D. Lukin, V. Vuletić, Attractive photons in a quantum nonlinear medium. Nature 502, 71–75 (2013).
17. D. Tiarks, S. Baur, K. Schneider, S. Dürr, G. Rempe, Single-photon transistor using a Förster resonance. Phys. Rev. Lett. 113, 053602 (2014).
18. H. Gorniaczyk, C. Tresp, J. Schmidt, H. Fedder, S. Hofferberth, Single-photon transistor mediated by interstate Rydberg interactions. Phys. Rev. Lett. 113, 053601 (2014).
19. J. H. Shapiro, Single-photon Kerr nonlinearities do not help quantum computation. Phys. Rev. A 73, 062305 (2006).
20. J. H. Shapiro, M. Razavi, Continuous-time cross-phase modulation and quantum computation. New J. Phys. 9, 16 (2007).
21. J. Gea-Banacloche, Impossibility of large phase shifts via the giant Kerr effect with single-photon wave packets. Phys. Rev. A 81, 043823 (2010).
22. T. Kuga, Y. Torii, N. Shiokawa, T. Hirano, Y. Shimizu, H. Sasada, Novel optical trap of atoms with a doughnut beam. Phys. Rev. Lett. 78, 4713–4716 (1997).
23. S. Baur, D. Tiarks, G. Rempe, S. Dürr, Single-photon switch based on Rydberg blockade. Phys. Rev. Lett. 112, 073901 (2014).
24. D. Paredes-Barato, C. S. Adams, All-optical quantum information processing using Rydberg gates. Phys. Rev. Lett. 112, 040501 (2014).
25. M. Khazali, K. Heshami, C. Simon, Photon-photon gate via the interaction between two collective Rydberg excitations. Phys. Rev. A 91, 030301 (2015).
26. K. S. Choi, H. Deng, J. Laurat, H. J. Kimble, Mapping photonic entanglement into and out of a quantum memory. Nature 452, 67–71 (2008).
27. K. M. Beck, M. Hosseini, Y. Duan, V. Vuletić, "Large conditional single-photon cross-phase modulation," http://arxiv.org/abs/1512.02166.
28. M. Marinescu, H. R. Sadeghpour, A. Dalgarno, Dynamic dipole polarizabilities of rubidium. Phys. Rev. A 49, 5103–5104 (1994).
29. M. Saffman, T. G. Walker, K. Mølmer, Quantum information with Rydberg atoms. Rev. Mod. Phys. 82, 2313–2363 (2010).