Published in final edited form as: *Nat Phys.* 2016 November ; 12(11): 1012–1016. doi:10.1038/nphys3819.

Parametric Amplification of a Superconducting Plasma Wave

S. Rajasekaran^{1,2}, E. Casandruc^{1,2}, Y. Laplace^{1,2}, D. Nicoletti^{1,2}, G. D. Gu³, S. R. Clark^{4,5,1}, D. Jaksch^{5,6}, and A. Cavalleri^{1,2,5,*}

¹Max Planck Institute for the Structure and Dynamics of Matter, Luruper Chaussee 149, 22761 Hamburg, Germany

²Center for Free-Electron Laser Science, Luruper Chaussee 149, 22761 Hamburg, Germany

³Condensed Matter Physics and Materials Science Department, Brookhaven National Laboratory, Upton, New York 11973-5000, USA

⁴Department of Physics, University of Bath, Claverton Down, BA2 7AY, Bath United Kingdom

⁵Department of Physics, Oxford University, Clarendon Laboratory, Parks Road, OX1 3PU Oxford, United Kingdom

⁶Centre for Quantum Technologies, National University of Singapore, 3 Science Drive 2, Singapore 117543, Singapore

Abstract

Many applications in photonics require all-optical manipulation of plasma waves1, which can concentrate electromagnetic energy on sub-wavelength length scales. This is difficult in metallic plasmas because of their small optical nonlinearities. Some layered superconductors support Josephson plasma waves (JPWs)2,3, involving oscillatory tunneling of the superfluid between capacitively coupled planes. Josephson plasma waves are also highly nonlinear4, and exhibit striking phenomena like cooperative emission of coherent terahertz radiation5,6, superconductormetal oscillations7 and soliton formation8. We show here that terahertz JPWs can be parametrically amplified through the cubic tunneling nonlinearity in a cuprate superconductor. Parametric amplification is sensitive to the relative phase between pump and seed waves and may be optimized to achieve squeezing of the order parameter phase fluctuations9 or single terahertz-photon devices.

Additional Information

Data Availability

Users may view, print, copy, and download text and data-mine the content in such documents, for the purposes of academic research, subject always to the full Conditions of use:http://www.nature.com/authors/editorial_policies/license.html#terms

^{*} andrea.cavalleri@mpsd.mpg.de.

Author Contributions

A.C. conceived the project together with S.R. S.R. built the THz pump-probe experimental setup, performed the measurement and analysed the experimental data with support of D.N. The simulations were performed by S.R. and E.C. with inputs from Y.L., S.R.C. and D.J. The results were discussed and interpreted by S.R., Y.L. and A.C. The sample was grown and characterized at Brookhaven by G.D.G. The manuscript was written by A.C., S.R., and D.N., with input from all authors.

The authors declare no competing financial interests. Supplementary information is available in the online version of the paper. Reprints and permissions information is available online at www.nature.com/reprints. Correspondence and requests for materials should be addressed to A.C.

The data that supports the plots within this paper and other findings of this study are available from the corresponding author on request.

Cuprates are strongly anisotropic superconductors in which transport is made threedimensional by Josephson tunneling between the Cu-O planes. Tunneling reduces the superfluid density in the direction perpendicular to the planes and hence the frequency of the plasmon to below the average pair breaking gap. Weakly damped oscillations of the superfluid sustain transverse Josephson Plasma Waves (JPWs) that propagate along the planes.

Consider a complex superconducting order parameter in the *t*th Cu-O plane $\psi_i(x, y, t) = |\psi_i(x, y, t)| \exp i\theta_i(x, y, t)$, which depends on two in-plane spatial coordinates *x* and *y* and on time *t*. For a THz-frequency optical field polarized perpendicular to the planes, excitations above the superconducting gap are negligible and the modulus of the order parameter $|\psi|^2$ (number of Cooper pairs) is nearly constant in space and time. Hence, the electrodyamics is dominated by the order-parameter phase $\theta_i(x, y, t)$. Ignoring at first the spatial dependence of the phase, the local tunneling strength can, from the Josephson equations10, be expressed in terms of an equivalent inductance, *L*, which depends on the local interlayer phase difference $\theta_{i,i+1}(t) = \theta_i(t) - \theta_{i+1}(t)$ as $L(\theta_{i,i+1}(t)) \sim L_0/\cos(\theta_{i,i+1}(t))$ (*i* and *i*+1 are the

indices for two neighboring layers). Here $L_0 = \frac{\hbar}{2eI_c}$ is the inductance at equilibrium, \hbar the reduced Planck's constant, 2e the Cooper pair charge and I_c the critical current. Denoting the

Resonance (JPR) frequency as $\omega_{JP}^{2} = \frac{1}{L(\theta_{i,i+1}(t))C} = \omega_{JP0}^{2} \cos \left[\theta_{i,i+1}(t)\right]$, where

capacitance of the Cu-O planes with a constant C, we express the Josephson Plasma

 $\omega_{JP0}^{2} = \frac{1}{L_0C}$ is the equilibrium value. Correspondingly, the oscillator strength *f* for the plasma oscillations 11 is also a function of the interlayer phase and scales as $f = f_0 \cos[\theta_{i,i+1}(t)]$. The dependence of the oscillator strength *f* on the cosine of the superconducting phase corresponds to a third order optical nonlinearity.

According to the second Josephson equation 10, the interlayer phase difference $\theta_{i,i+1}(t)$

advances in time with the time integral of the interlayer voltage drop, as $\frac{\partial \left[\theta_{i,i+1}\left(t\right)\right]}{\partial t} = \frac{2eV}{\hbar}$. For an optical field made resonant with the Josephson plasma frequency $E(t) = E_0 \sin(\omega_{JP0}t)$, the interlayer phase oscillates as $\theta_{i,i+1}(t) = \theta_0 \cos(\omega_{JP0}t)$, where E_0 is the field amplitude and

 $\theta_0 = \frac{2ed}{\hbar\omega_{_{JP0}}} E_0$ (*d* ~ 1 nm is the interlayer distance). This implies that the oscillator strength

 $f_{i,i+1}(t) = f_0 \cos\left(\theta_0 \cos\left(\omega_{JP0}t\right)\right) \approx f_0 \left(1 - \frac{\theta_0^2 + \theta_0^2 \cos\left(2\omega_{JP0}t\right)}{4}\right) \text{is modulated at a frequency } 2\omega_{JP0}, \text{ whenever the field } E_0 \text{ is large enough to make the phase excursion } \theta_0 \text{ sizeable.}$

Figure 1 provides a pictorial representation of this physics. We plot a vector that represents both the *phase difference* $\theta_{i,i+1}(t)$ (vector angle) and the *oscillator strength* $f_{i,i+1}(t)$ (vector length). This picture shows how, for small driving fields, only $\theta_{i,i+1}(t)$ oscillates at the driving frequency ω_{JP0} , whereas for larger fields these oscillations are accompanied by a $2\omega_{JP0}$ modulation of the oscillator strength $f_{i,i+1}(t)$.

Note also that the phenomena discussed above can be casted in terms of a Mathieu equation (see Supplementary Information 2). Thus, a $2\omega_{Jp0}$ modulation of the oscillator strength can serve as a pump for the parametric amplification of a second, weak plasma wave at frequency ω_{JP0} . In this paper we demonstrate experimentally this effect in La_{1.905}Ba_{0.095}CuO₄ (LBCO_{9.5}), a cuprate superconductor with the equilibrium JPR at $\omega_{JP0} \approx 0.5$ THz.

Terahertz pulses, generated with a photoconductive antenna12, were used as a weak probe of JPWs (a schematic drawing of the measurement geometry is reported in Supplementary Information 1). A typical THz-field trace13 reflected by the sample is shown in Fig. 2A. Two different measurements are displayed: one taken below (red line) and the other one above (black line) the superconducting transition temperature $T_c = 32$ K. In the superconducting state, long-lived oscillations with ~ 2 ps period were observed on the trailing edge of the pulse, indicative of the JPR at $\omega_{JP0} \cong 0.5$ THz. Figure 2B (solid red line) displays the corresponding reflectivity edge in frequency domain. The solid lines in Fig. 2C -2D are the complex dielectric permittivity $\varepsilon(\omega)$ and the loss function

 $L(\omega) = -\operatorname{Im}\left(\frac{1}{\varepsilon(\omega)}\right) = \frac{\varepsilon_2(\omega)}{(\varepsilon_1(\omega) + \varepsilon_2(\omega))^2} \cdot L(\omega) \text{ peaks at } \omega_{JP0}\text{, where the real part of the dielectric permittivity, } \varepsilon_1(\omega)\text{, crosses zero. These optical properties could be well reproduced by solving the wave equation in the superconductor in one dimension8 (see Supplementary Information 3), which yields the space and time dependent order parameter phase <math>\theta_{i,i+1}(x,t)$ (Fig. 2E) and the corresponding changes (negligible in linear response regime) of the oscillator strength $f = f_0 \cos[\theta_{i,i+1}(x,t)]$ (Fig. 2F). The reflectivity, complex permittivity, and loss function (dashed lines in Fig. 2B, 2C, and 2D, respectively), calculated from these simulations by solving the electromagnetic field at the sample surface8, are in good agreement with the experimental data.

Amplification of a weak JPW like the one above (*probe* field) was achieved by mixing it with a second, intense *pump* field, which resonantly drove the Josephson phase to large amplitudes. Quasi-single cycle THz pulses, generated in LiNbO₃ with the tilted pulse front method14 (yielding field strengths up to ~100 kV/cm), were used to excite these waves in nonlinear regime. The spectral content of these pulses extended between 0.2 and 0.7 THz, centered at the JPR frequency (see Supplementary Information 4). Note that the pump field strength used in this experiment exceeds the expected threshold to access the nonlinear

regime, defined by $\theta_0 = \frac{2eE_0d}{\hbar\omega_{_{JP0}}} \sim 1$ and corresponding in this material to field amplitudes

$$E_0 = \frac{\hbar\omega_{JP0}}{2ed} \sim 20 \text{ kV/cm}$$

In Fig. 3, we report the time-delay dependent, spectrally integrated pump-probe response of LBCO_{9.5}. Changes in the reflected probe field were measured at one specific probe sampling time ($\tau = \tau_0$), as a function of pump-probe time delay (*t*). For a system in which the optical properties are dominated by a single plasma resonance, the spectrally integrated response is proportional to the plasma oscillator strength *f*.

As shown in Fig. 3A-3B, this integrated response exhibits a reduction of the signal and oscillations at a frequency ~ $2\omega_{JP0}$. Note that the oscillation frequency did not depend on the pump electric field strength E_0 , while the frequency reduced when the base temperature of the experiment was increased, consistent with the reduction of the equilibrium ω_{JP0} (see Supplementary Information 5 and 6). The effect completely disappeared at $T > T_c$.

Hence, the theoretically predicted $2\omega_{JP0}$ modulation of the total oscillator strength f (see above) is well reproduced by the data in Fig. 3. This response could also be simulated using the space- and time-dependent sine-Gordon equation (see Fig. 3C-3D), yielding good agreement between experiment and theory (see dashed lines in Fig. 3A-3B).

Note that here we only analyze pump-probe delays $t \gtrsim 0$ ps, because the response at the earliest times suffers from perturbed free induction decay15. This effect consists in the deformation of a coherent signal, which occurs when the pump strikes the sample during the oscillatory relaxation of the probe (for $t \leq 0$ ps in our case). Perturbations of the response are particularly evident in case of long momentum relaxation times, as in superconductors.

Selected time-domain probe traces measured before and after excitation are displayed in Fig. 4. Crucially, at specific time delays the probe field is amplified (Fig. 4A), whereas at other delays it is suppressed (Fig. 4B) with respect to that measured at equilibrium.

In Fig. 5 we report the time-delay and frequency dependent loss function

 $L(t,\omega) = -\operatorname{Im}\left(\frac{1}{\varepsilon(t,\omega)}\right) = \frac{\varepsilon_2(t,\omega)}{(\varepsilon_1(t,\omega) + \varepsilon_2(t,\omega))^2}, \text{ a quantity that peaks at the zero crossing of } \varepsilon_1(t,\omega) \text{ and is always positive for a dissipative medium (i.e., a medium with } \varepsilon_2(t,\omega) > 0).$ The experimental data of Fig. 5A show that after excitation $L(\omega)$ acquires negative values around ω_{JP0} (red regions). This is indicative of a negative $\varepsilon_2(t,\omega)$ and hence amplification. The effect is strong near zero pump-probe time delay, then disappears after ~1 ps and is observed again periodically with a repetition frequency of ~ $2\omega_{JP0}$. The same effect appears also in the simulations (Fig. 5B), yielding periodic amplification at a repetition frequency of $2\omega_{JP0}$.

In Supplementary Information 7 we report additional quantitative estimates of the degree of amplification. We include a negative absorption coefficient and a reflectivity larger than 1 at $\omega \simeq \omega_p$. The extracted values are $a = (-0.090 \pm 0.003) \mu m^{-1}$ and $R = (1.042 \pm 0.008)$, respectively.

The data and theoretical analysis reported here demonstrate that terahertz JPWs can be parametrically amplified, exhibiting the expected sensitivity to the relative phase of strong and weak fields mixed in this process and the oscillatory dependence at twice the frequency of the drive.

Parametric amplification of THz light based on nonlinear optical techniques has already been shown in the past16. However, the physics demonstrated here extend beyond potential applications in photonics, directly leading to coherent parametric control of the superfluid in layered superconductors, and providing a means to manipulate the properties of the material or to probe them in new ways17.

Moreover, the ability to amplify a plasma wave could lead to single-THz photon manipulation devices that may operate above 1 K temperatures. These would exploit concepts that to date have been developed only at microwave frequencies and in the milli-Kelvin regime18–21. Finally, the parametric phenomena discussed here can also potentially be used to squeeze9,22, 23 the superfluid phase, and may lead to control of fluctuating superconductivity24, perhaps even over a range of temperatures above T_c 25,26.

Methods

Laser pulses with 100 fs duration and ~5 mJ energy from a commercial Ti:Sa amplifier were split into 3 parts (92%, 7%, 1%). The most intense beam was used to generate strong-field THz pulses with energies up to ~3 μ J via optical rectification in LiNbO₃ with the tilted pulse front technique. These were collimated and then focused at normal incidence onto the sample (with polarization perpendicular to the Cu-O planes, i.e. along the *c* axis) using a Teflon lens and a parabolic mirror, with focal lengths of 150 mm and 75 mm, respectively. The pump spot diameter at the sample position was ~2.5 mm. The pump field strength was calibrated with electro-optic sampling in a 0.2-mm-thick GaP crystal, yielding a maximum value of ~100 kV/cm (see Supplementary Information 4).

The 7% beam was used to generate the THz probe pulses with a photoconductive antenna. These had a dynamic bandwidth of 0.1-3 THz, corresponding to a time resolution of ~250 fs. The *c*-axis optical properties of the superconductor (both at equilibrium and throughout the pump-induced dynamics) were probed in reflection geometry, with a probe incidence angle of 45° and a spot diameter at the sample position of ~2 mm). The reflected probe pulses were electro-optically sampled in a 1-mm-thick ZnTe crystal, using the remaining 1% of the 800 nm beam. This measurement procedure returned the quantity E_{probe} (*t*, τ), with *t* being the pump-probe delay and τ being the electro-optic sampling time coordinate.

The sample used in our experiment was a single crystal of La_{1.905}Ba_{0.095}CuO₄ cut and polished along an *ac* oriented surface of ~3x3 mm size. Its equilibrium optical response in the superconducting state was determined by measuring the complex-valued $E_{probe}(\omega)$ (pump off) both at T < T_c and T > T_c and by referencing it to the normal-state reflectivity measured in another crystal coming from the same batch of samples27.

The spectrally integrated pump-probe traces of Fig. 3 were measured by scanning the pumpprobe delay *t* at a fixed sampling time $\tau = \tau_0$. This was chosen to be on the trailing edge of the pulse, where the JPR oscillations are present. Note that the observed dynamics, and in particular the $2\omega_{JP0}$ oscillations, did not depend significantly on the specific τ_0 value at which the scan was performed.

The frequency and time-delay dependent loss function of Fig. 5 (as well as all complex optical properties of the perturbed material) was determined by applying Fresnel equations 11 to the pump-induced changes in the reflected electric field. These were normalized by independently recording E_{probe} (t, τ) in presence and absence of the THz pump field. Note that there was no need to take into account any pump-probe penetration depth mismatch in the calculation.

$$\frac{\partial^{2}\theta_{i,i+1}\left(x,t\right)}{\partial x^{2}} - \frac{1}{\gamma}\frac{\partial\theta_{i,i+1}\left(x,t\right)}{\partial t} - \frac{\varepsilon_{r}}{c^{2}}\frac{\partial^{2}\theta_{i,i+1}\left(x,t\right)}{\partial t^{2}} = \frac{\omega_{JP0}^{2}\varepsilon_{r}}{c^{2}}sin\theta_{i,i+1}\left(x,t\right)$$

being γ a damping constant, *c* the speed of light, *e_r* the dielectric permittivity, and ω_{JP0} the equilibrium JPR frequency. This equation was solved numerically, with the THz pump and probe fields overlapping at the vacuum-superconductor interface. For more details on this topic, we refer the reader to Supplementary Information 3.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

Acknowledgments

The research leading to these results received funding from the European Research Council under the European Union's Seventh Framework Programme (FP7/2007-2013)/ERC Grant Agreement no. 319286 (QMAC). We acknowledge support from the Deutsche Forschungsgemeinschaft via the excellence cluster "The Hamburg Centre for Ultrafast Imaging - Structure, Dynamics and Control of Matter at the Atomic Scale" and the priority program SFB925. Work performed at Brookhaven was supported by US Department of Energy, Division of Materials Science under contract no. DE-AC02-98CH10886.

References

- 1. Kauranen M, Zayats AV. Nonlinear plasmonics. Nat Photonics. 2012; 6:737-748.
- Basov DN, Timusk T. Electrodynamics of high-T_c superconductors. Rev Mod Phys. 2005; 77:721– 779.
- Kleiner R, Steinmeyer F, Kunkel G, Müller P. Intrinsic Josephson effects in Bi₂Sr₂CaCu₂O₈ single crystals. Phys Rev Lett. 1992; 68:2394–2397. [PubMed: 10045384]
- Savel'ev S, Rakhmanov AL, Yampol'skii VA, Nori F. Analogues of nonlinear optics using terahertz Josephson plasma waves in layered superconductors. Nat Phys. 2006; 2:521–525.
- 5. Ozyuzer L, et al. Emission of Coherent THz Radiation from Superconductors. Science. 2007; 318:1291–1293. [PubMed: 18033881]
- 6. Hu X, Lin S-Z. Phase dynamics in a stack of inductively coupled intrinsic Josephson junctions and terahertz electromagnetic radiation. Supercond Sci Technol. 2010; 23:053001.
- 7. Dienst A, et al. Bi-directional ultrafast electric-field gating of interlayer charge transport in a cuprate superconductor. Nat Photonics. 2011; 5:485–488.
- Dienst A, et al. Optical excitation of Josephson plasma solitons in a cuprate superconductor. Nat Mater. 2013; 12:535–541. [PubMed: 23524373]
- Lü X-Y, et al. Squeezed Optomechanics with Phase-Matched Amplification and Dissipation. Phys Rev Lett. 2015; 114:093602. [PubMed: 25793814]
- 10. Josephson BD. Coupled Superconductors. Rev Mod Phys. 1964; 36:216-220.
- Dressel, M.; Grüner, G. Electrodynamics of Solids: Optical Properties of Electrons in Matter. Cambridge University Press; 2002.
- 12. Dreyhaupt A, Winnerl S, Dekorsy T, Helm M. High-intensity terahertz radiation from a microstructured large-area photoconductor. Appl Phys Lett. 2005; 86:121114.
- Thorsmølle VK, et al. C-axis Josephson plasma resonance observed in Tl₂Ba₂CaCu₂O₈ superconducting thin films by use of terahertz time-domain spectroscopy. Opt Lett. 2001; 26:1292–1294. [PubMed: 18049590]

- Hebling J, Yeh K-L, Hoffmann MC, Bartal B, Nelson KA. Generation of high-power terahertz pulses by tilted-pulse-front excitation and their application possibilities. J Opt Soc Am B. 2008; 25:B6.
- 15. Hamm P. Coherent effects in femtosecond infrared spectroscopy. Chem Phys. 1995; 200:415-429.
- Tripathi SR, et al. Terahertz wave parametric amplifier. Opt Lett. 2014; 39:1649–1652. [PubMed: 24690860]
- Hohenleutner M, et al. Real-time observation of interfering crystal electrons in high-harmonic generation. Nature. 2015; 523:572–575. [PubMed: 26223624]
- Vijay R, et al. Stabilizing Rabi oscillations in a superconducting qubit using quantum feedback. Nature. 2012; 490:77–80. [PubMed: 23038468]
- Macklin C, et al. A near-quantum-limited Josephson traveling-wave parametric amplifier. Science. 2015; :aaa8525.doi: 10.1126/science.aaa8525
- Eichler C, Salathe Y, Mlynek J, Schmidt S, Wallraff A. Quantum-Limited Amplification and Entanglement in Coupled Nonlinear Resonators. Phys Rev Lett. 2014; 113:110502. [PubMed: 25259964]
- Castellanos-Beltran MA, Lehnert KW. Widely tunable parametric amplifier based on a superconducting quantum interference device array resonator. Appl Phys Lett. 2007; 91:83509.
- 22. Almog R, Zaitsev S, Shtempluck O, Buks E. Noise Squeezing in a Nanomechanical Duffing Resonator. Phys Rev Lett. 2007; 98:78103.
- Zagoskin AM, Il'ichev E, McCutcheon MW, Young JF, Nori F. Controlled Generation of Squeezed States of Microwave Radiation in a Superconducting Resonant Circuit. Phys Rev Lett. 2008; 101:253602. [PubMed: 19113707]
- Denny SJ, Clark SR, Laplace Y, Cavalleri A, Jaksch D. Proposed Parametric Cooling of Bilayer Cuprate Superconductors by Terahertz Excitation. Phys Rev Lett. 2015; 114:137001. [PubMed: 25884134]
- 25. Bilbro LS, et al. Temporal correlations of superconductivity above the transition temperature in La_{2-x}Sr_xCuO₄ probed by terahertz spectroscopy. Nat Phys. 2011; 7:298–302.
- Corson J, Mallozzi R, Orenstein J, Eckstein JN, Bozovic I. Vanishing of phase coherence in underdoped Bi₂Sr₂CaCu₂O₈₊₆. Nature. 1999; 398:221–223.
- 27. Homes CC, et al. Determination of the optical properties of La_{2-x}Ba_xCuO₄ for several dopings, including the anomalous x=1/8 phase. Phys Rev B. 2012; 85:134510.

 $2\omega_{\text{JPO}}$

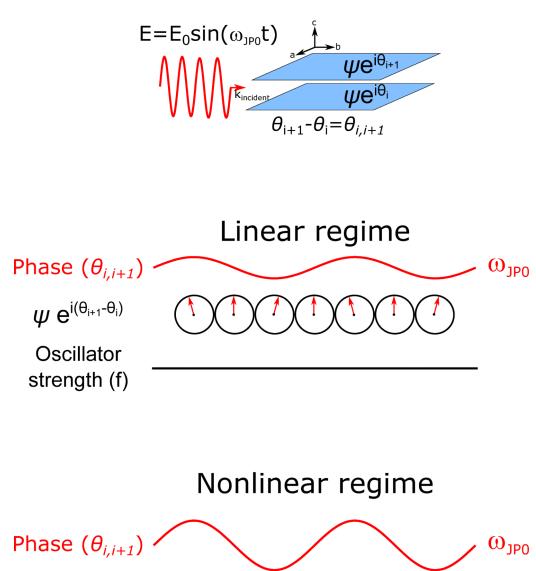


Figure 1. Schematic representation of Josephson plasma waves. Schematic time-dependent representation of JPWs in linear and nonlinear regime, in presence of a driving field $E(t) = E_0 \sin(\omega_{JP0}t)$ polarized along the out-of-plane direction of a layered superconductor. Red arrows indicate the Josephson phase while the corresponding oscillator strength *f* is represented by the black circle area. A JPW in linear regime consists

of small amplitude modulations of $\theta_{i,i+1}$ at constant oscillator strength $f \sim \omega_{JP0}^2$. In nonlinear regime, the Josephson phase oscillates at ω_{JP0} , whereas f is modulated at $2\omega_{JP0}$.

Nat Phys. Author manuscript; available in PMC 2017 January 11.

 $\psi e^{i(\theta_{i+1}-\theta_i)}$

Oscillator

strength (f)

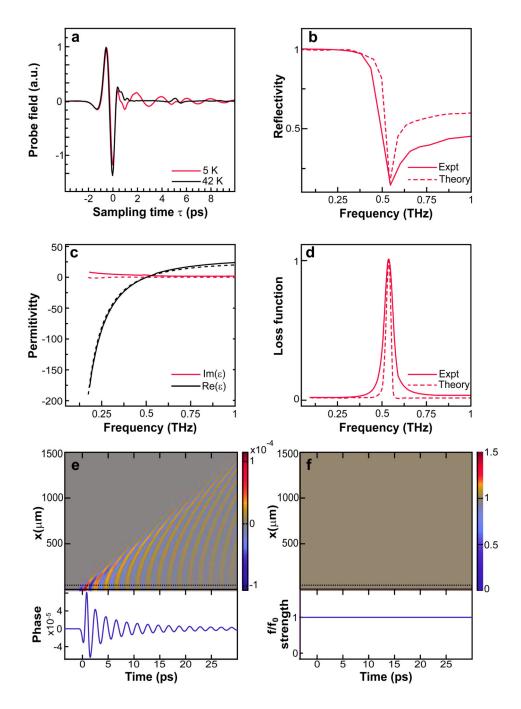
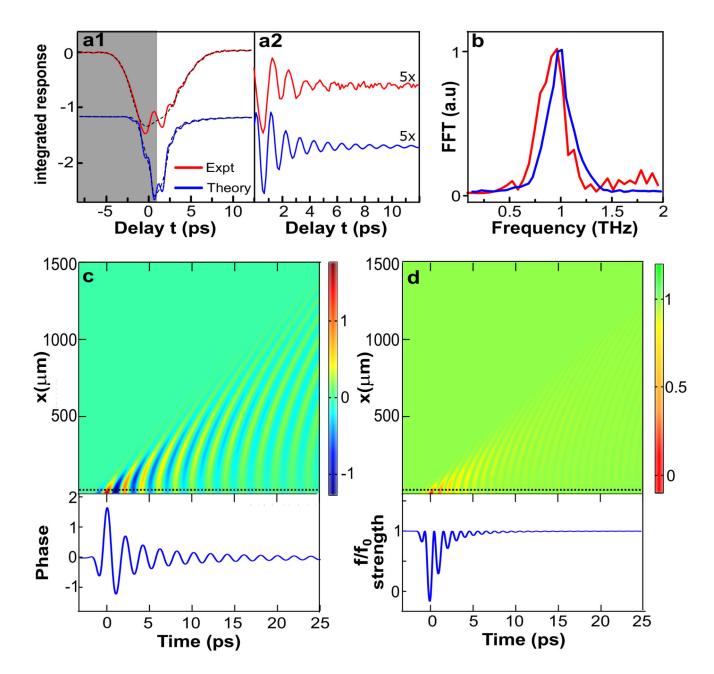


Figure 2. Linear JPWs in LBCO_{9.5}.

a, $E_{\text{probe}}(\tau)$ measured in absence of pump field both above and below $T_c = 32$ K. **b**, Frequency-dependent, *c*-axis reflectivity at T = 5 K (solid line), extracted from the $E_{\text{probe}}(\tau)$ trace of panel **a**. **c**, Corresponding real and imaginary part of the complex permittivity and (**d**) energy loss function (solid lines). Dashed lines in **b-d** were calculated by numerically solving the sine-Gordon equation in linear regime. **e**, Simulated phase $\theta_{i,i+1}(x,t)$ and (**f**) corresponding oscillator strength *f*(no change) induced by a weak probe THz field.

Horizontal dotted lines indicate the spatial coordinate *x* at which the line cuts are displayed (lower panels).

Rajasekaran et al.





a1, Normalized spectrally integrated pump-probe response $\frac{\Delta E_{\text{probe}}}{E_{\text{probe}}} (t, \tau_0=2 \text{ ps})$. Experimental data are shown along with calculations based on the sine-Gordon equation in nonlinear regime (displayed with a vertical offset). Dashed lines indicate an average reduction that accompanies the oscillations (see model). The reduction was subtracted through Fourier filtering (>0.2 THz) to obtain the oscillations shown in **a2**. The signal buildup region affected by perturbed free induction decay is shaded in grey. **b**, Fourier transform of the extracted oscillations, showing a peak at ~1 THz. **c**, Phase $\theta_{i,i+1}(x,t)$ and (**d**) corresponding oscillator strength *f* induced by a strong THz pump field, as determined by

numerically solving the sine-Gordon equation in nonlinear regime. Horizontal dotted lines indicate the spatial coordinate *x* at which the line cuts are displayed (lower panels).

Rajasekaran et al.

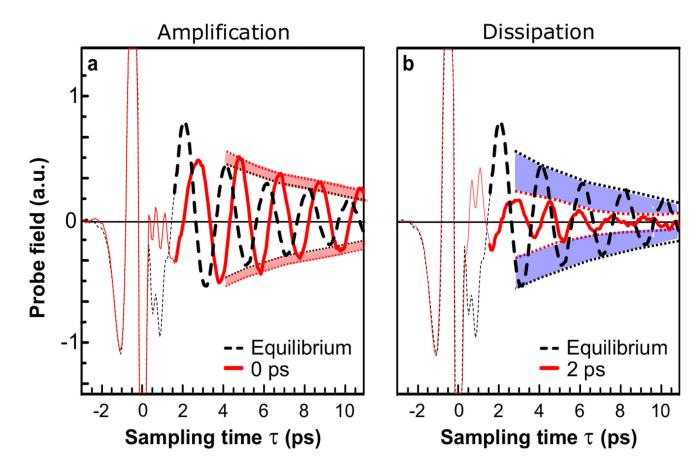
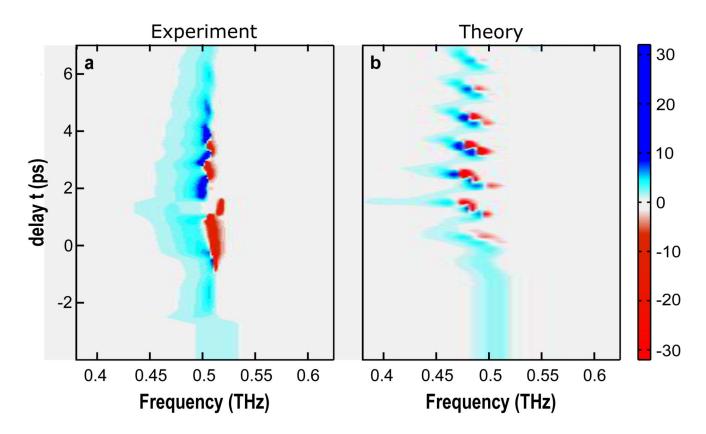
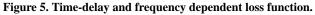


Figure 4. Amplification and suppression of plasma oscillations.

 E_{probe} (t, τ) traces measured by scanning the electro-optic sampling time τ at selected pumpprobe delays t = 0 ps and t = 2 ps. Data are shown along with the same quantity measured at equilibrium (pump off). Plasma oscillations on the trailing edge of the pulses ($\tau \gtrsim 2$ ps) are highlighted by thicker lines. Colored shadings in **a** and **b** indicate amplification and suppression of the JPW amplitude, respectively.





Time-delay and frequency dependent loss function $L(t,\omega)$ determined (**a**) experimentally and (**b**) by numerically solving the sine-Gordon equation in nonlinear regime. Note that experimental and simulated $L(\omega)$ in the region between t=-4 ps and t=-2 ps have been multiplied by a factor of 5 to be better visualized with the other data.