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Fast diffusion kurtosis imaging of fibrotic mouse kidneys

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Abstract

Diffusion kurtosis imaging (DKI) is sensitive to tissue microstructure and may therefore be useful in the diagnosis and monitoring of disease in brain and body organs. Generally, diffusion MRI (dMRI) in the body is challenging due to heterogeneous body composition that can cause image artifacts due to chemical shifts and susceptibility differences. Additionally, the abdomen has a strong presence of physiological factors (e.g. breath, heartbeat, blood flow), which may severely reduce image quality, especially when echo-planar imaging is employed as is typical in dMRI. Collectively, these challenging measurement conditions impede the use and exploration of DKI in the body. This impediment is further exacerbated by the traditionally large amount of data required for DKI and low signal-to-noise ratio at the b-values needed to effectively probe the kurtosis regime. Recently introduced fast DKI techniques reduce the challenge of DKI in the body by lowering the data requirement substantially so that e.g. triggering and breath hold techniques may be applied for the entire DKI acquisition without causing unfeasible scan times. One common pathologic condition where body DKI may be of immediate clinical value is kidney fibrosis, which causes a progressing change in organ microstructure. With its sensitivity to microstructure, DKI is an obvious candidate for a non-invasive evaluation method. We present preclinical evidence that the rapidly obtainable tensor-derived mean kurtosis (\bar{W}) distinguishes moderately fibrotic kidneys from healthy controls. The presence and degree of fibrosis are confirmed by histology, which also indicates fibrosis as the main driver behind the DKI differences observed between groups. We therefore conclude that fast kurtosis is a likely candidate for an MRI based method for detection and monitoring of renal fibrosis. We provide protocol recommendations for fast renal DKI in humans based on a b-value optimization performed using data acquired at 3T in normal human kidney.

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Introduction

Chronic Kidney Disease (CKD) has increasing incidence and fibrosis (the accumulation of extracellular matrix) is a common denominator of different pathological processes in development of CKD (1). Currently, biopsy is the only method to diagnose and monitor microstructural pathology in CKD but biopsy is both prone to sampling errors and may give complications due to its invasiveness. A promising method for non-invasive detection and monitoring of renal fibrosis and CKD is diffusion MRI (dMRI) which utilizes sequence sensitivity to water diffusion to indirectly assess tissue microstructure.

A basic measure is the apparent diffusion coefficient (ADC) which is the diffusivity $D(\hat{n})$ observed along a direction \hat{n} . In the past decade, dMRI has been used to investigate renal diseases in several studies and generally they report a reduction in the ADC in diseased kidneys (2), CKD (3–5), diabetic (6,7), chronic parenchymal disease (2,8), and transplanted kidneys (9–11). ADC has also been correlated to both glomerular filtration rate and the degree of fibrosis of the tissue (12). However, the results in the past studies show great discrepancy due to the lack of consensus in the measurement schemes (different b-values) as pointed out by different research groups (13–16). Inappropriate choice of b-values may cause measurements to be contaminated by intravoxel incoherent motion (IVIM) effects (17,18) from perfusion and filtration in the kidney, which will skew ADC estimates. Moreover, basic dMRI metrics such as the ADC might not be the most sensitive diffusion marker to detect fibrosis and more advanced diffusion techniques now offer parameters sensitive to more aspects of the microstructure. Diffusion Tensor Imaging (DTI) with the parameter Fractional Anisotropy (FA) reflects the directional variation of the water diffusion, where zero indicates isotropic diffusion and one indicates diffusion in only one direction. Hindrances and restrictions from tissue microstructure cause diffusion to be non-Gaussian which is not captured by DTI. To describe this effect, Diffusion Kurtosis Imaging (DKI) was proposed a decade ago (19) and is widely held to sensitively reflect tissue microstructure (16) complementary to basic dMRI and DTI. DKI is a simple extension of the DTI model and inclusion of non-Gaussian effects has been shown to improve diffusion tensor estimates and cause estimated diffusion metrics to show less b-value dependency (20). Typical implementations of DKI rely on large data sets for parameter estimation causing both long measurement and post-processing time. This has held back the exploration of DKI in everyday clinical application although evidence is growing that DKI offers valuable diagnostic information (21–24) (see also literature surveys in (25,26)). Recently proposed methods allow DKI to be performed within a clinically relevant timescale (as little as one minute including post-processing) (26–28), making DKI compatible with even the acute clinical setting. In body imaging, dMRI is prone to artifacts due to the use of echo-planar read-out in a body region, which contains many tissue types with different chemical shifts, magnetic susceptibilities, and the acquisition of sufficient high quality data to allow DKI analysis is a challenge. Until now, two studies of DKI in normal human kidneys have

been published (29,30). The two studies both report a larger FA for medulla than in cortex. However, they report opposite results for mean diffusivity (MD) and mean kurtosis (MK). Huang et al. is in agreement with most studies that MD in cortex is larger than in medulla (29), but for MK there exist no relevant studies to compare to. Pentang et al. and Huang et al. use a traditional DKI protocol with 30 directions, but a different range of b-values: (0, 300, 600 s/mm²) and (0, 500, 1000 s/mm²) respectively. A recent study shows DKI to be valuable in assessing clear cell renal carcinoma in patients where DKI based 7 b-values (range 0–2000 s/mm²) and three encoding directions was found to quantitatively characterize different renal tumor grades (31). Even though this shows promise for the use of DKI in diagnostics of renal disease, the lack of a standard protocol could potentially cause conflicting findings and non-comparable absolute values. Particularly, the choice of b-values is critical since the presence of flow in renal tissue may cause IVIM effects to influence DWI and DKI estimates from low b-value measurements and the choice of b-value scheme is therefore important for unaffected parameter estimates. A preclinical report by Boor et al. (32) concludes that ADC does not reflect kidney fibrosis, because the ADC measured in fibrotic kidney cortex *in vivo* is lower than in healthy kidney cortex and *ex vivo* it is opposite. In the same vein, preclinical studies can provide a basis for interpretation of clinical DKI of renal fibrosis by investigating how the fibrosis affects the DKI metrics in the absence of physiological effects.

Here we set out to do exactly this: using fixed kidneys from wild type (WT) mice and a transgenic (Tg) mouse model of CKD we compare diffusion metrics estimated with the fast DKI method (the 1-9-9 protocol from (28)) to estimates from a traditional DKI protocol using a larger data acquisition. The MRI measurements are performed on a 9.4T Bruker scanner. Good agreement is found between metrics from the two methods and dMRI metrics FA and mean kurtosis are found to differ between the two groups (WT and Tg). Quantitative histology was then performed on the kidneys to confirm the presence of fibrosis in the Tg group and assess fibrosis severity, tissue porosity, and cell density. The histology indicates that fibrosis is the main driver behind the DKI differences between groups. In this manner, we can establish how fibrosis affects the DTI/DKI metrics in the absence of physiological effects such as flow of blood and urine in the kidney tissue. Having established the fast kurtosis method's sensitivity to renal fibrosis we proceed to offer an optimized measurement strategy for use of the fast kurtosis measurement scheme in the study of human kidney disease. We propose a strategy for circumventing contamination from IVIM effects in the estimation. The optimized fast kurtosis scheme is then demonstrated on a basic data set acquired in normal human kidney at 3T.

1 Methods

1.1 Theory

In DKI the logarithm of the diffusion weighted signal is written as (19):

$$\log S(b, \hat{n}) = -bn_i n_j D_{ij} + \frac{b^2}{6} n_i n_j n_k n_l \bar{D}^2 W_{ijkl} + O(b^3), \quad (1)$$

where b is the magnitude of diffusion weighting applied along $\hat{n}=(n_x, n_y, n_z)$. Here subscripts label Cartesian components (e.g. $i = x, y, z$) and our notation implies summation over repeated indices as e.g. $n_i n_j D_{ij} = \sum_{ij} n_i n_j D_{ij}$ for the diffusion tensor D . As in (19) the rank-4 kurtosis tensor W is defined in terms of spin displacement moments:

$$W_{ijkl} = \frac{\langle R_i R_j R_k R_l \rangle - \langle R_i R_j \rangle \langle R_k R_l \rangle - \langle R_i R_k \rangle \langle R_j R_l \rangle - \langle R_i R_l \rangle \langle R_j R_k \rangle}{4\bar{D}^2 \Delta^2}, \quad (2)$$

where $R = r(\Delta) - r(0)$ is the spin displacement and Δ the diffusion time. In (26) we defined the tensor derived apparent kurtosis, $W(\hat{n})$, in analogy to the apparent diffusion constant

$$D(\hat{n}) = \hat{n}^T D \hat{n} = n_i n_j D_{ij} \quad (3)$$

as

$$W(\hat{n}) = \hat{n} \hat{n}^T W \hat{n} \hat{n}^T = n_i n_j n_k n_l W_{ijkl} \quad (4)$$

With this definition we defined a mean kurtosis, \bar{W} , as the mean of the kurtosis tensor i.e. its average over all directions (S_2 is the sphere):

$$\begin{aligned} \bar{W} &= \frac{1}{4\pi} \int_{S_2} d\hat{n} W(\hat{n}) = \frac{1}{5} \langle W, \mathbb{I} \rangle \\ &= \frac{1}{5} (W_{xxxx} + W_{yyyy} + W_{zzzz} + 2W_{xxyy} + 2W_{xxzz} + 2W_{yyzz}) \equiv \frac{1}{5} \text{Tr}(W) \end{aligned} \quad (5)$$

where \mathbb{I} is the fully symmetric isotropic tensor (33), $\langle A, B \rangle = A_{ijkl} B_{ijkl}$ denotes the Frobenius inner product, and Tr is the trace. Thus, in this definition the mean kurtosis \bar{W} can be viewed as the isotropic part of the kurtosis tensor and is equal to 1/5 of the projection $\langle W, \mathbb{I} \rangle$ of the kurtosis tensor W onto \mathbb{I} , using the inner product.

On the basis of Eq. (5), \bar{W} may be estimated from $W(\hat{n})$ along nine distinct directions, $\hat{n}^{(i)}$, $\hat{n}^{(i+)}$ and $\hat{n}^{(i-)}$ ($i=1,2,3$), defined in Table 1 (26):

$$\bar{W} = \frac{1}{15} \left(\sum_{i=1}^3 W(\hat{n}^{(i)}) + 2 \sum_{i=1}^3 W(\hat{n}^{(i+)}) + 2 \sum_{i=1}^3 W(\hat{n}^{(i-)}) \right) \quad (6)$$

Using these directions with Eq. (1) and performing the same linear combination of the log signal as in Eq. (6), we get:

$$\frac{1}{15} \left(\sum_{i=1}^3 \log S(b, \hat{n}^{(i)}) + 2 \sum_{i=1}^3 \log S(b, \hat{n}^{(i+)}) + 2 \sum_{i=1}^3 \log S(b, \hat{n}^{(i-)}) \right) = -b\bar{D} + \frac{1}{6} b^2 \bar{D}^2 \bar{W} \quad (7)$$

where $\bar{D} = \text{Tr}(\mathbf{D}) / 3$ is the mean diffusivity. In (26,27) this formed the basis for robust estimation of \bar{D} and \bar{W} from 13 diffusion weighted images: 1 at $b=0$, three directions ($\hat{x}, \hat{y}, \hat{z}$) at $b=1 \text{ ms}/\mu\text{m}^2$ and the nine directions at $b=2.5 \text{ ms}/\mu\text{m}^2$. This strategy was therefore referred to as the 1-3-9 acquisition scheme for fast estimation of mean kurtosis. Recently, this strategy was extended so that \bar{D} , \bar{W} and also FA can be estimated from 19 images. These images are acquired as 1 at $b=0$, and the nine directions at two different non-zero b -values, b_1 and b_2 . For this reason it is referred to as the 1-9-9 acquisition scheme (28). Such an acquisition allows the use of eq. (7) to form a set of two equations with two unknowns (\bar{D} and \bar{W}):

$$\begin{aligned} A_1 &\equiv \frac{1}{15} \left(\sum_{i=1}^3 \log S(b_1, \hat{n}^{(i)}) + 2 \sum_{i=1}^3 \log S(b_1, \hat{n}^{(i+)}) + 2 \sum_{i=1}^3 \log S(b_1, \hat{n}^{(i-)}) \right) = -b_1 \bar{D} + \frac{1}{6} b_1^2 \bar{D}^2 \bar{W} \\ A_2 &\equiv \frac{1}{15} \left(\sum_{i=1}^3 \log S(b_2, \hat{n}^{(i)}) + 2 \sum_{i=1}^3 \log S(b_2, \hat{n}^{(i+)}) + 2 \sum_{i=1}^3 \log S(b_2, \hat{n}^{(i-)}) \right) = -b_2 \bar{D} + \frac{1}{6} b_2^2 \bar{D}^2 \bar{W} \end{aligned} \quad (8)$$

so that a 1-9-9 estimate for \bar{D} is given by :

$$\bar{D}_{199} = (b_1^2 A_2 - b_2^2 A_1) / (b_1 b_2^2 - b_2^2 b_1) \quad (9)$$

an FA estimate is then available as:

$$FA_{199} = \sqrt{\frac{3}{2} \frac{\text{var}(D(\hat{n}))}{\text{var}(D(\hat{n})) + 6/15 \bar{D}_{199}^2}} \quad (10)$$

and \bar{W} is obtained from:

$$\bar{W}_{199} = 6b_1 b_2 (A_1 b_2 - A_2 b_1) (b_1 - b_2) / (A_1 b_2^2 - A_2 b_1^2)^2 \quad (11)$$

where $D(\hat{n})$ is obtained from the data as described previously (28), and var denotes the variance, here taken over the nine directions \hat{n} . In addition to the estimation of FA at a minimal increase in scan time and virtually no cost in post-processing time (no fitting required), one major benefit of this approach is increased robustness to experimental imperfections as shown in (28).

The 1-9-9 strategy requires a stable estimate of the unweighted tissue signal $S(b=0)$. In some regions of the kidney, the presence of IVIM effects is too large to ignore in the analysis. The IVIM model describes the signal as:

$$S(b) = S_0 \cdot (f_{IVIM} F_{perf} + (1 - f_{IVIM}) \cdot F_{diff}) \quad (11)$$

where S_0 is the unweighted signal intensity from all tissue, f_{IVIM} is the volume fraction of the incoherent perfusion compartment and F_{perf} the corresponding signal attenuation. Similarly, F_{diff} is the signal attenuation of the true diffusion in the tissue compartment which makes up the remaining volume. For the 1-9-9 strategy to work in vivo we therefore need an estimate of the unweighted signal intensity of the tissue compartment alone: $S_0 \cdot (1 - f_{IVIM})$. For kurtosis estimation in regions where f_{IVIM} is large, we propose to obtain this intensity from fitting the one-dimensional DKI signal equation to a series of 3–4 measurements at varying b-values outside of the IVIM regime ($b > 0.2 \text{ ms}/\mu\text{m}^2$) along a direction already included in the 1-9-9 scheme (e.g. one of the x,y,z directions). These 5–6 data points can be fitted to the one-dimensional DKI signal equation to obtain an estimate of the unweighted tissue signal without the IVIM compartment. This estimate would then constitute the $S(b=0)$ needed for the 1-9-9 estimation. If more than one direction is acquired, the intensity estimates from each direction should be averaged to reduce the influence of tissue anisotropy.

1.2 Animals

1.2.1 Mouse Model—We used the previously described RenTGF- β mouse strain expressing mutated porcine transforming growth factor β (TGF- β) under control of the Ren-1^c promoter ($n = 8$) (34). The mice demonstrate glomerular lesions exclusively within the kidneys and show thickening of glomerular basement membrane, deposition of extracellular matrix, increased glomerular volume, and reduced glomerular filtration rate (35). Sex- and age-matched wildtype (WT) littermates were used as control animals ($n = 8$). The animal experiment was approved and performed under guidelines given by the Danish Animal Experiments Inspectorate (2014-15-2934-01047).

1.2.2 Sample preparation for preclinical MRI—All animals were euthanized and perfusion fixed using phosphate buffered saline (PBS) with 4% paraformaldehyde (PFA). Kidneys were then excised and stored in 4% PFA for weeks. Prior to imaging, each kidney was washed in PBS for 24 hrs to improve MRI signal by removal of excess fixative. For imaging, the kidney was placed in a tube with fluorinert (FC-770, 3M) in a manner so that the sample could not move. Imaging was performed on a Bruker Biospec 9.4 T animal system equipped with the Bruker BGA12S-HP gradients (660 mT/m) and a bore-mounted 15 mm quadrature coil (Bruker Biospin).

1.3 Preclinical MRI

The imaging protocol consisted of several scans. Firstly, a fast, low contrast GE scan covering the entire kidney was acquired for volumetry. For the remaining study, 10 central slices were identified and used as geometry for the remaining scans: full DKI protocol, fast

kurtosis estimation, and reference anatomical scans for region-of-interest (ROI) placement. The reference scan used for ROI placement was acquired at the same resolution, slice positions and thicknesses as both diffusion data sets. A reference scan with higher in-plane resolution was also acquired to aid in ROI placement. ROIs were placed at cortex (CO), outer stripe of outer medulla (OS), inner stripe of outer medulla (IS) and inner medulla (IM). The imaging parameters for each scan series are given below.

1.3.1 Volumetrics—A 3D FLASH of 100 μm isotropic resolution was acquired in 8 min with TE = 3.6 ms, TR = 100 ms, 1 average, and flip angle 40 degrees. A low contrast scan with short echo time was chosen to avoid image distortions caused by potential microscopic air bubbles on the sample surface.

1.3.2 Anatomical reference scans—Gradient echo (FLASH) images covering the most medial regions of kidney were acquired. Images with 150 $\mu\text{m} \times 150 \mu\text{m}$ in-plane resolution and slice thickness 200 μm were acquired using imaging parameters TE = 25 ms, TR = 500 ms and 25 averages. High resolution images were also acquired with 60 μm in-plane resolution with 45 averages.

1.3.3 Traditional DKI protocol—Data was collected using diffusion weighted spin echo EPI with 16 segments and a bandwidth of 278 kHz, 2 dummy scans. The encoding scheme was constructed using a 12 direction spherical design (36) at each of 8 b-values 0, 0.5, 0.8, 1.0, 1.5, 2.0, 2.5, 3.0 $\text{ms}/\mu\text{m}^2$ and diffusion times $\delta/ = 6/14$ ms. TE = 26.3 ms, TR = 6250 ms and 4 averages. The resolution was 150 $\mu\text{m} \times 150 \mu\text{m}$ in-plane, slice thickness 200 μm with a scan time of 8.32 hrs.

1.3.4 Kurtosis estimation using the 1-9-9 scheme—Imaging was performed as for the traditional DKI protocol but instead acquiring the nine directions stated in Table 1 at b-values 0, 1, and 2.5 $\text{ms}/\mu\text{m}^2$, 8 averages. Total scan time 2.24 hrs.

1.4 Human MRI

Diffusion weighted data was acquired in normal human kidney using a 3T whole-body clinical MRI scanner (Magnetom Trio, Siemens Medical Systems, Erlangen, Germany) using a combination of a spine-coil and a body-flex-coil. For the b-value optimization, we acquired a single medial slice of the kidneys during breath holding with a single-shot EPI sequence with parameters: TE = 116 ms, TR = 2000 ms, acceleration factor of 2, slice thickness 4 mm and in-plane resolution of 2 mm \times 2 mm. Diffusion was only sampled along a single direction because we assume isotropic diffusion in the kidney cortex, which is the region our b-value optimization is focussed on. A rather dense sampling was performed at low b-values to assess the presence of IVIM effects. The b-values acquired were 0, 50, 100, 150, 200, 300, 400, 500, 1000, 1500, 2000, 2500 s/mm^2 .

Additional human data was acquired with the fast kurtosis protocol using optimized b-values obtained from analysis of the single direction DWI data described above. Imaging parameters for this data set were: TE = 116 ms, TR = 2000 ms, acceleration factor of 2, slice thickness 5 mm and in-plane resolution of 3 mm \times 3 mm, b-values were 0, 0.5, 1.75 $\text{ms}/\mu\text{m}^2$. Data was

acquired from a single medial slice of the kidneys during one breath hold using single-shot EPI. Data from each kidney was recorded separately to improve slice positioning.

1.5 Histology

Mice kidneys were halved lengthwise and moved to 30% (w/v) sucrose solution (Merck Millipore) for cryoprotection and moulded in Tissue-Tek ® (Sakura Finetek, USA). Coronal slices (5 µm) were cut at –20°C using a Leica CM1900 cryostat (Leica Biosystems) and the sections were stored at –20°C until use. Sirius red was used to stain collagen fibers and haematoxylin as a nuclear and counterstain. Images were acquired on a light microscope and automated image analysis was performed to calculate nuclear and fibrosis percentage using Matlab™ to escape from the subjective bias. Unstained regions of the tissue sections were also calculated as percentage of interstitial, vessel and lumen space in Matlab™.

1.5.1 Tissue staining—Two sections from each kidney were stained with Sirius red stain (Direct red 80, Sigma Aldrich, St. Louis, MO) and counterstained with haematoxylin, according to a previously described protocol (37,38).

1.5.2 Light microscopy—Histological sections were imaged with an Olympus BX 51TF microscope (Japan) and a digital camera, DP70 (Olympus). Whole tissue section montages were acquired with a 4x objective lens, and high-resolution images were acquired with a 60×/1.35 oil objective lens. High-resolution images were acquired from five anatomical regions: CO, OS, IS, IM and pelvis (P) of each tissue section of the kidney.

1.5.3 Kidney image analysis for fibrosis—Images were processed using in-house analysis tools implemented in Matlab™. Full details of the quantitative histology techniques can be found in (39). Briefly, rgb color images were first converted into L*a*b color space to scale the luminosity of each image with maximum luminosity and subsequently reconverted into 'rgb' format. Red and green channels were separately adjusted with local image contrast enhancement and were again combined into 'rgb' format with the blue channel nulled. After contrast enhancement, decorrelation stretch was performed to enhance the color difference in an image, while keeping the mean and variance the same. After this procedure, the pixels associated with fibrosis were captured as a narrow range of rgb values objectively. Finally, all the pixels were counted automatically and normalized with the total area of the image to get the fibrosis percentage of the tissue.

1.5.4 Kidney image analysis for interstitial, vessel and lumen space—The volume fraction of the interstitial, vessel and lumen space was estimated semi-automatically using a thresholding technique to select nearly white or unstained pixels. The threshold was chosen after observation of multiple random images. The resulting binary image allows estimation of the volume fraction of the collected interstitial, vessel and lumen space as the percentage of unstained pixels (value = 1) in the image.

1.5.5 Kidney image analysis for nuclear percentage—Contrast enhanced images were used to count the number of pixels associated with nuclear percentage of the kidney tissue. A binary image was created by choosing an objectively selected range of pixel values

associated with nucleus in the images. Small structures were then removed by an area opening operation and holes of the binary images of nucleus were filled with ‘imfill’ function of Matlab™. All the pixels associated with nucleus were counted and normalized by area of the image to get the nuclear percentage of the image.

1.5.6 Statistical analysis of histology—A two-sample t-test was performed in Matlab™ on the percentage values associated with fibrosis, interstitial space and nucleus for WT and Tg and p-values less than 0.05 were considered significant.

1.6 MRI data analysis

1.6.1 Full kurtosis model estimation—The full tensors D and W were estimated from a constrained iterative linear least squares fit (40) to Eq. (1). Two iterations were used to reach a stable fit. From the tensors D and W , \bar{D} , FA, and \bar{W} were obtained. These values serve as ground truth estimates in our evaluation of the fast kurtosis technique. The traditional mean kurtosis (MK) was also evaluated using a non-linear least squares direction-wise fit as recommended in (41) (ver. 2.6 accessed on Feb. 23rd 2016) for DKI data sets with 15 or fewer encoding directions such as ours.

1.6.2 Fast scheme (1-9-9) estimation—The nine $b = 0$ images were averaged and used in the analysis along with the 18 images from the non-zero b-value scans. The 1-9-9 estimates of \bar{D} , FA, and \bar{W} were then obtained from the data as described above (Eqs. (9), (10), and (11)).

1.6.3 ROI analysis of MRI data—ROIs were placed on the anatomical reference scans with the same resolution as the DWI scans but using the anatomical scan with high in-plane resolution as aid. In this manner, the four regions, CO, OS, IS, and IM were identified in each kidney. The pelvis (P) could not be consistently defined on the images. Figure 3C shows examples of the four ROIs.

1.6.4 Volumetrics—Volumetry was performed using semi-automatic clustering-based segmentation in ITK-snap (42). Total kidney volume was then calculated by multiplication of the voxel count and the MRI voxel volume.

Two Tg kidneys were found to have been poorly fixed (probably due to the fibrosis) and the MRI data was therefore sub-standard hindering reliable parameter estimation. These kidneys were therefore excluded from the analysis of the DWI data but were included in the volumetric analysis.

1.6.5 Human MRI data analysis and numerical b-value optimization—The single direction DWI data from human kidney were used to determine optimal values for b_1 and b_2 for clinical 1-9-9 acquisition. This data set was used the basis for a numerical b-value optimization procedure using Rician noise propagation. The procedure has also been described for brain tissue in (28). For the present purpose we assume isotropic tissue so that $\bar{D} = D(\hat{n})$ and $\bar{W} = W(\hat{n})$ meaning that data acquired along one direction is sufficient for the optimization. This assumption is valid in kidney cortex where FA is low but may apply to more regions of the kidney as FA is generally reported to be <0.4 in most of the organ

(15,43,44). Prior to analysis, data was smoothed using a Gaussian kernel with FWHM = 1.75 x voxel size. An ROI was drawn in kidney cortex (N = 170 voxels) and the mean dMRI signal in this ROI was fitted to Eq. (1) to estimate \bar{D} and \bar{W} and the unweighted tissue signal intensity $S_0 \cdot (1 - f_{IVIM})$. This fit was performed on a subset of the acquired b-values, $b = [0.2, 0.3, 0.4, 0.5, 1.0, 1.5]$ ms/ μm^2 where remaining b-values were excluded due to IVIM effects at low b-values and $b > 1.5$ ms/ μm^2 was excluded in order to satisfy the criterion $b < 3/(\bar{D} \bar{W})$. The estimated diffusion coefficient and kurtosis were $\bar{D} = 2.43 \mu\text{m}^2/\text{ms}$ and $\bar{W} = 0.66$. Based on the criteria above, these values indicate that the highest b-value should be less than 1.9 ms/ μm^2 . SNR in the smoothed $b = 0$ image was approximately 50; this manner of measuring the SNR is applied because smoothed data will be employed in the fast kurtosis calculation. Using these parameter values Eq. (1) was used to generate 1-9-9 data sets with varying combinations of b_1 and b_2 . Then, Gaussian noise was added in quadrature to match an SNR of 50 at $b = 0$. The magnitude of the resultant signal was then used to obtain 1-9-9 estimates of \bar{D} , and \bar{W} using Eqs. (9) and (11). This was repeated 1000 times, after which the mean absolute error and variance over noise realizations were calculated. This procedure was repeated on a densely sampled grid of values of (b_1, b_2) from 0–3 ms/ μm^2 .

2 Results

2.1 Fast kurtosis imaging

The mean kurtosis definition employed in the fast kurtosis techniques (\bar{W}) (26–28) differs slightly from the traditional mean kurtosis metric MK (19). In brain tissue, the two definitions have been shown to give very similar values (26,45,46), and we find that this is also the case in kidney. In figure 1, we compare the tensor based estimate of the mean kurtosis (\bar{W}) to traditional MK in each voxel of a WT kidney (panel 1A). The correlation between the two is shown in figure 1B. The linear correlation coefficient was 0.96 ($p \ll 0.01$). Across all samples the linear correlation was 0.94 ± 0.05 with no difference between WT and Tg kidneys.

Examples of maps of \bar{D} , FA, and \bar{W} obtained from the full DKI model and from the 1-9-9 protocol are given in figure 2. The maps are shown for a WT kidney in panel A–C and a Tg kidney in panel G–I. The correlations between the two different estimates of each parameter are shown in panels D–F for the WT and in panels J–L for the Tg. The correlation for FA is generally poor due to the overall low FA values in the kidney tissue (see discussion). However, high FA regions in the Tg kidney are captured by the 1-9-9 estimate of FA.

The estimates of \bar{D} , FA, and \bar{W} for both the full model and the 1-9-9 protocol are compared between WT and Tg in four regions of the kidneys: CO, OS, IS, and IM, an example of the ROIs are found in figure 3C for both WT and Tg kidneys. In figure 3 panel A, examples of the high-resolution anatomical scans are shown and in panel B two examples of histological slices are shown for comparison. The changes in the tissue structure of the WT and Tg kidneys are clearly apparent in both the MRI image and the histological image. The estimates of \bar{D} and \bar{W}_{199} in each of the four ROIs of the WT and the Tg agree very well and do not show any significant differences between the fibrotic and the control kidneys (figure 3D and 3G). However, in figure 3D and 3G we observe a tendency for \bar{D} to monotonically

increase from cortex towards the inner medulla in Tg kidneys (the difference between both CO and IM and CO and IS are significant for Tg for both \bar{D} and \bar{D}_{199}), which is not the case in WT kidneys. The kurtosis estimates, \bar{W} and \bar{W}_{199} also agree well, and were significantly different between WT and Tg in two regions in the medulla (IS and IM), figure 3E and 3H. In figure 3F and 3I, FA and FA₁₉₉ of the four ROIs are compared. The full estimate of FA shows significant changes in all three ROIs of the medulla (OS, IM, and IM) whereas FA₁₉₉ generally does not agree well with true FA and only shows significant changes in IS and IM.

2.2 MR-based volumetrics

The volumetric analysis shows Tg kidneys to have very different sizes as compared to WT. The mean volume of WT kidneys was $V_{WT} = 0.28 \pm 0.04 \text{ cm}^3$ and for Tg kidneys $V_{Tg} = 0.17 \pm 0.02 \text{ cm}^3$. This is in agreement with observations from previous work (34,47). The volumes are significantly different with $p = 8.3e-05$.

2.3 Histology

The results from our quantitative histology are shown in figure 4. Panel 4A gives examples of the five regions investigated with histology in a WT kidney. Panel 4B shows the mean fibrotic percentage in each of the five regions in WT and Tg kidneys. Significant increase in fibrosis is seen in P ($p < 0.01$), IS ($p < 0.01$), OS ($p = 0.02$), and CO ($p < 0.05$). A modest increase in fibrosis was apparent in the IM layer but was not significant. Overall, the degree of fibrosis in the Tg animals was moderate. The porosity of the tissue was evaluated as the volume fraction of the collected interstitial, vessel, and lumen space and shows significant increase only in the IS layer of the fibrotic kidney ($p < 0.01$), although a general increase in interstitial space and lumen was observed in Tg in comparison of WT. There were no significant alterations in nuclear volume fraction in any layer of Tg in comparison of WT.

2.4 b-value optimization for a clinical 1-9-9 protocol in human kidney

The region of kidney cortex used for b-value optimization is shown in Fig. 5A where the region is outlined in red and overlaid on the $b=0$ image. Fig 5B shows the DKI fit to the signal decay curve, errorbars are 1 standard deviation wide. We also indicate how the fit allows us to extrapolate to a $b=0$ signal intensity free of IVIM contributions (blue marker). This estimate of $S_0 \cdot (1 - f_{IVIM})$ is seen to be lower than the measured $b=0$ signal indicated by the green data point. This analysis gives us an estimate of f_{IVIM} in kidney cortex of 0.08, indicating that for fast kurtosis estimation aimed at kidney cortex, the $b=0$ image may be used directly with little loss of precision.

The results of the b-values optimization for the 1-9-9 protocol on the human kidney 3T data are shown in figure 6. The error on \bar{D} is below 10% in a large range of combinations of b_1 and b_2 values. The region where the error on \bar{W} is below 10% is much narrower and taking into account the critical SNR decrease at high b-values and the upper bound on the highest b-value of $1.9 \text{ ms}/\mu\text{m}^2$, we suggest $b_1 = 0.5 \text{ ms}/\mu\text{m}^2$ and $b_2 = 1.75 \text{ ms}/\mu\text{m}^2$, a combination which at SNR = 50 offers estimates of an error on \bar{D} of 7% and \bar{W} of 11%. These errors decrease to 4% and 7% respectively for SNR = 75. Fig. 7 shows estimates of \bar{D} and \bar{W} obtained with the 1-9-9 protocol at these b-values in both kidneys from one human subject.

3 Discussion

The main result of this study is that the fast and compact DKI scan protocols presented in ref. (26–28) are feasible for studying kurtosis in kidneys. This conclusion is based on our findings that the tensor-derived mean kurtosis (\bar{W}) is strongly correlated to traditional MK (figure 1, linear correlation coefficient of 0.96) and that regional \bar{D} is significantly different between WT and Tg groups. We therefore expect that diagnostic value of the traditional MK indicated by the few initial studies published (29,30) is very likely to also be contained in the rapidly obtainable \bar{W} . This result is of great value, because the fast acquisition schemes merely require acquisition of 13 or 19 diffusion weighted images allowing the use of breath hold imaging for the full acquisition which is unfeasible with the data requirement of traditional DKI acquisitions. However, prior to these techniques being applied in the clinic, preclinical assessment of their sensitivity to various stages of fibrosis is needed. We have investigated the fast kurtosis method from (28) in fixed murine kidneys from WT animals and a Tg model of kidney fibrosis. Histology confirms that the Tg kidneys are fibrotic to a moderate degree and the difference between the WT kidneys and Tg kidneys is also evident in organ size. This is to be expected as the overall development and growth of the Tg animals are affected by their illness.

By performing our study in fixed kidneys, we are able to compare the diffusion metrics in WT and in Tg fibrotic kidney tissue without physiological effects such as flow affecting the parameter estimates. In this manner - and by supplemental histology - we are able to establish the isolated effect of moderate fibrosis on the investigated metrics (\bar{D} , FA, \bar{W}). In short, we find that fibrosis causes FA and \bar{W} to decrease significantly in IS and IM and that for the case of \bar{W} these differences are detected reliably with the 1-9-9 protocol (figure 3 panels E,H). In the case of FA, significant changes were seen in OS, IS, and IM using the full DKI data set. FA₁₉₉ did not provide a very good estimate of true FA in the kidney because of the low anisotropy of the tissue. This is in agreement with the FA₁₉₉ behaviour observed in low FA tissue in brain in (28). Nevertheless, although the FA₁₉₉ values deviate from the true values, the 1-9-9 estimate of FA did show significant differences between WT and Tg in two of the three regions where true FA was altered, namely IS and IM (fig. 3F,I). The significant change of FA in medulla in diseased kidneys as compared to control has also been observed in the study by Gaudio et al, (8). For Tg kidneys we find a decreased corticomedullary FA differentiation (only significant between CO and IM ($p = 0.022$)). This reduction in FA is probably caused by tubular atrophy. In WT kidneys, FA increases from CO towards the medulla, figure 3F, this is also observed in other studies such as (15,29,30,44,48), and Chuck et al. (15) showed that it is independent of b-value scheme.

The kurtosis estimates, \bar{W} and \bar{W}_{199} , are compared between WT and Tg in figure 3E and 3H in the four different ROIs. For both kurtosis estimates, there is a significant difference between WT and Tg in two ROIs in the medulla (IS and IM).

For the kurtosis estimates, \bar{W} and \bar{W}_{199} , we find significant differences between CO and OS ($p = 0.011/0.0089$) in WT. The kurtosis is found to be smaller in OS than in CO in agreement with the *in vivo* results by Pentang et al. (30). In Tg kidneys, \bar{W} and \bar{W}_{199} of CO is significantly different to all three ROIs in medulla.

No significant difference in \bar{D} between groups was found with either technique. This is in agreement with the conclusions of Boor et al. (32) where apparent diffusivity was found to be insensitive to renal fibrosis. Gaudiano et al (8) investigated a broad range of patients with impaired renal function and also reported no significant difference in ADC in both cortex and medulla between groups. However, several *in vivo* studies report significant reduction of ADC in the cortex of a diseased kidney (2,3,7,9,49). These conflicting findings may be due to differences in measurement schemes e.g. choice of b-values and how data analysis is performed. The presence of IVIM effects at low b-values would skew ADC or \bar{D} estimates considerably. Avoiding these effects is possible by appropriate choice of b-values. One further way to improve DTI parameter estimates is by including kurtosis effects in the analysis (20). Consistency in data collection and analysis would strongly aid in clarifying the diagnostic value of DTI and DKI parameters in renal fibrosis. We therefore recommend that the fast kurtosis technique (either the 1-3-9 version from (26,27) or the 1-9-9 version from (28) which is used here) should be employed in future DKI studies of kidney fibrosis. The use of a series of low b-values >0.2 to estimate the unweighted tissue signal as described in the theory section might be one way to achieve this but requires registration of the data prior to analysis which in our experience is prone to errors when combining data sets from separate breath holds. Alternatively, the fast kurtosis techniques could be combined with free-breathing navigator triggered techniques as demonstrated in (44). In such cases, higher spatial resolution than presented here would be achievable and the strategy for IVIM free estimation could be built into the acquisition for estimation in regions where IVIM effects are large. The fast kurtosis protocol would then be modified to include acquisition of 3–4 b-values in the IVIM-free low b-value regime (e.g. between $0.2\text{--}0.4\text{ ms}/\mu\text{m}^2$) along one or more directions already included in the nine directions required for fast kurtosis estimation. These images would then replace the one $b=0$ image employed in the original scheme and allow an estimate of the unweighted tissue signal alone ($S_0 \cdot (1 - f_{IVIM})$). If this estimate is obtained along more than one direction the averaged value should be used in the 1-9-9 processing to reduce the effect of tissue anisotropy on the tissue signal estimate. By employing these techniques investigators will obtain an accurate estimate of \bar{D} and \bar{W} (and FA with 1-9-9) from few diffusion weighted images and with rapid post processing. The compactness of the 1-9-9 protocol facilitates the use of breath hold techniques and the use of navigator to improve image quality, which might cause prohibitive scan times in traditional DKI acquisitions. By appropriate choice of b-values the fast estimation can be performed without fitting thereby avoiding bias introduced by analysis techniques which can be significant (50,51). Our b-value optimization based on data from normal human kidney yields the values of $b_1 = 0.5\text{ ms}/\mu\text{m}^2$ and $b_2 = 1.75\text{ ms}/\mu\text{m}^2$ in line with the recommendations by Rosenkrantz et al. in (16) for traditional DKI in the body. The 1-9-9 protocol was shown to be very robust to experimental imperfections in (28) which is a major benefit when imaging in the body where imaging conditions are far from ideal. Histology showed our *ex vivo* samples to be moderately fibrotic. Further work is needed to show if the DKI techniques are sensitive enough to detect milder degrees of fibrosis *in vivo* or if the technique is useful only beyond a certain stage of fibrosis severity. The proposed protocol might also be useful in detection and diagnosis of other renal diseases e.g. in kidney tumors as demonstrated in (31). If successful in the clinical monitoring of kidney diseases, the compactness of the fast kurtosis protocol would even make it a candidate for combined PET-

MR investigation of renal function, providing structural and physiological organ parameters from the same scan session.

In conclusion, we have demonstrated that the tensor-based mean kurtosis \bar{W} is sensitive to kidney fibrosis *ex vivo* and can be reliably estimated in kidney tissue with the fast kurtosis technique. The method is compact enough to allow clinically feasible renal DKI even when triggering and breath hold techniques are employed. We therefore recommend the fast kurtosis technique be assessed for clinical investigation of renal fibrosis and offer optimized b-values for parameter estimation.

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Abbreviations

MRI	Magnetic Resonance Imaging
DWI	Diffusion Weighted Imaging
DKI	Diffusion kurtosis imaging
dMRI	diffusion MRI
CKD	Chronic Kidney Disease
ADC	Apparent Diffusion Coefficient
IVIM	IntraVoxel Incoherent Motion
DTI	Diffusion Tensor Imaging
FA	Fractional Anisotropy
MD	Mean Diffusivity
MK	Mean Kurtosis
WT	Wild Type
Tg	Transgenic
PBS	Phosphate Buffered Saline
GE	Gradient Echo

ROI	Region-Of-Interest
CO	Cortex
OS	Outer Stripe of outer medulla
IS	Inner Stripe of outer medulla
IM	Inner Medulla
P	Pelvis
TE	Echo Time
TR	Repetition Time
EPI	Echo Planar Imaging

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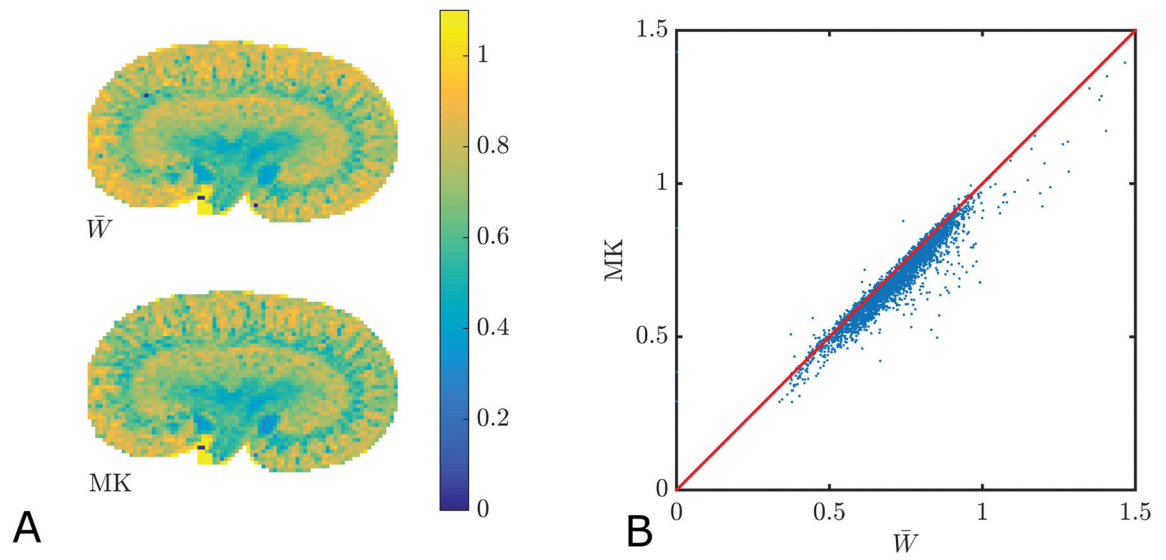


Fig. 1. Comparison of tensor based mean kurtosis (\bar{W}) and traditional mean kurtosis MK. Maps of the two parameters are shown in A and a plot with their correlation is displayed in B. The linear correlation coefficient is 0.96 ($p \ll 0.01$). Across all samples the linear correlation is 0.94 ± 0.05 .

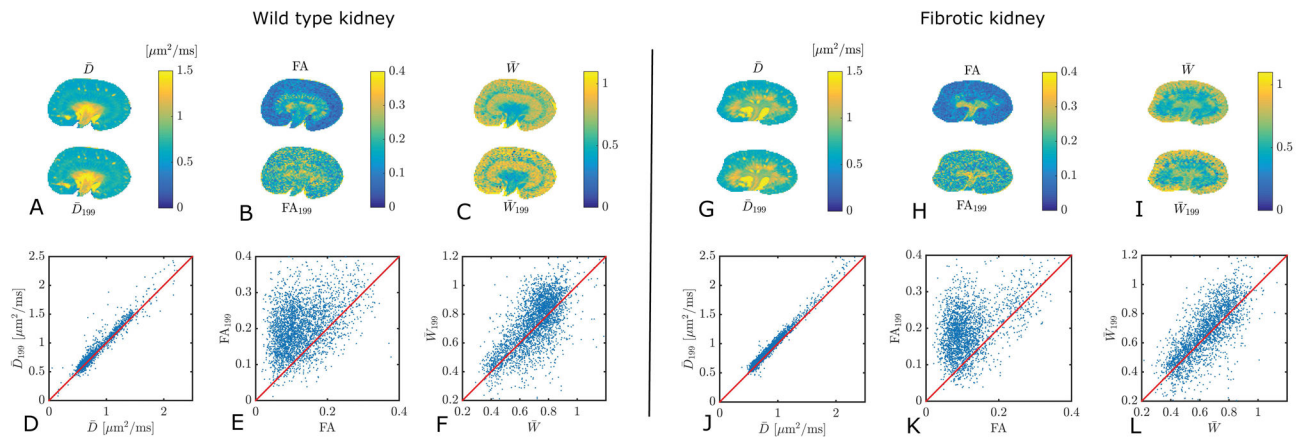


Fig. 2. Comparison of maps of \bar{D} , FA, and \bar{W} obtained from fits to a large data set and with the 1-9-9 protocol. Panels A–C show these estimates from WT murine kidney. The correlations between the two estimates of each parameter are shown in panels D–F. Similarly, panels G–I show parameter maps from Tg murine kidney, and correlations in J–L. The correlation strengths are 0.97 (D), 0.46 (E), 0.61 (F), 0.99 (J), 0.45 (K), 0.76 (L).

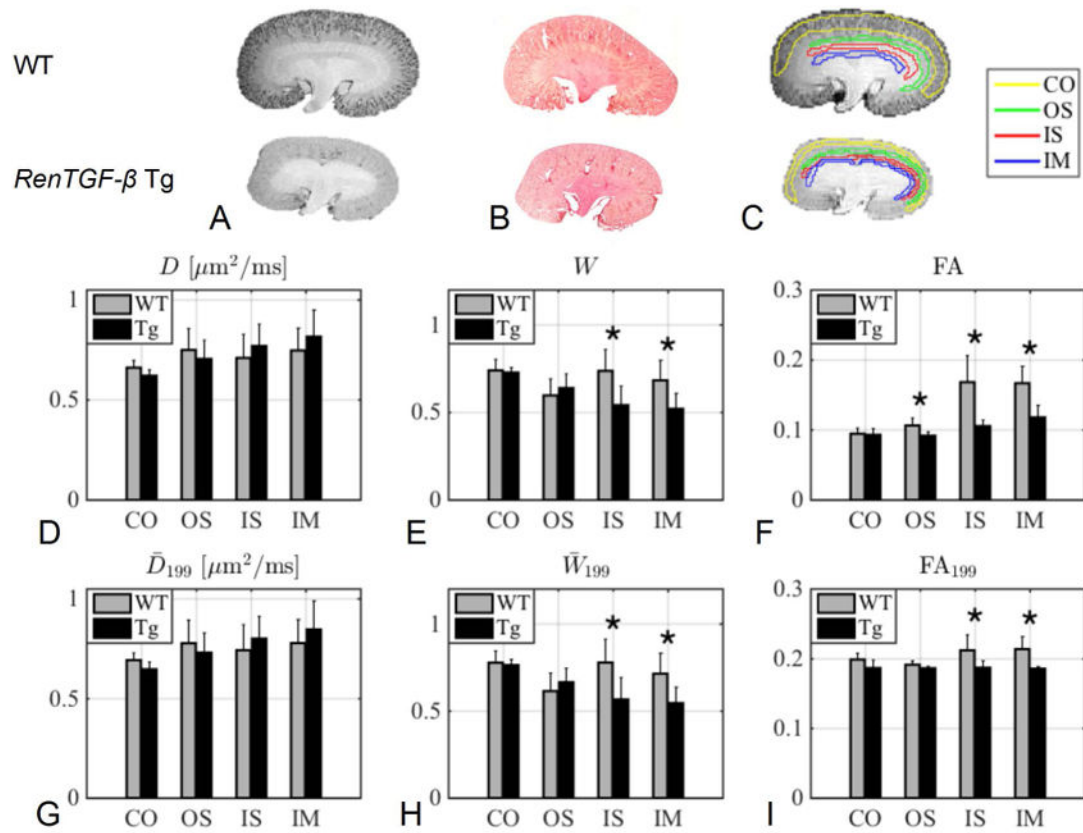
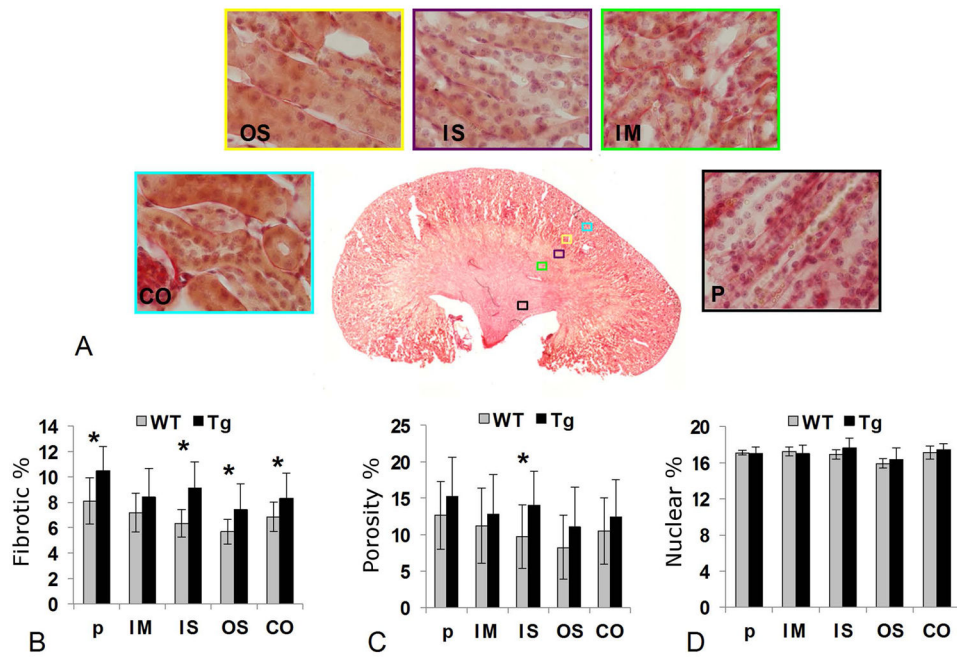


Fig. 3.

Column A and B show a high resolution anatomical image and a histology section of both a WT and a Tg kidney. Column C shows an example of the four ROIs (CO: cortex, OS: outer stripe of outer medulla, IS: inner stripe of outer medulla and IM: inner medulla) on WT and Tg kidneys. The bar plots in D–E shows a comparison of the mean values in the four ROIs in the WT kidneys and Tg kidneys from parameters obtained from the full DKI model and the bar plots in G–I shows the corresponding plots for the 1-9-9 estimates. The asterisk (*) indicates significance (< 0.05) from a two sample t-test. E: IS ($p = 0.029$), IS: ($p = 0.021$), F: OS ($p = 0.022$), IS ($p = 0.0058$), IM ($p = 0.0043$), H: IS ($p = 0.025$), IM ($p = 0.028$) and I: IS ($p = 0.045$), IM ($p = 0.0074$).

**Fig. 4.**

In A, five ROIs are shown in a histology section of a WT kidney: pelvis (P), inner medulla (IM), inner stripe of outer medulla (IS), outer stripe of outer medulla (OS) and cortex (CO). The bar plot in B shows a comparison of the fibrosis in % for WT and Tg. The bar plot in C shows an estimate of the porosity (the combined interstitial, vessel and lumen space) in WT and Tg and the final bar plot in D shows a count of the nuclei in the ROIs in WT and Tg which gives a estimate of the cell density.

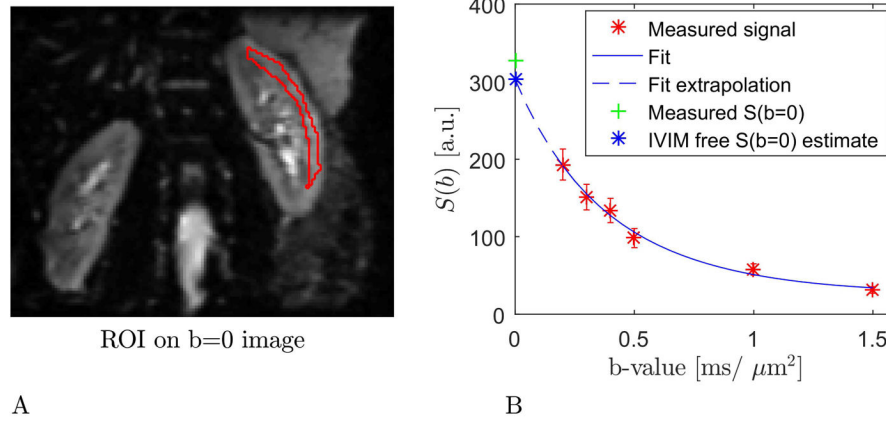
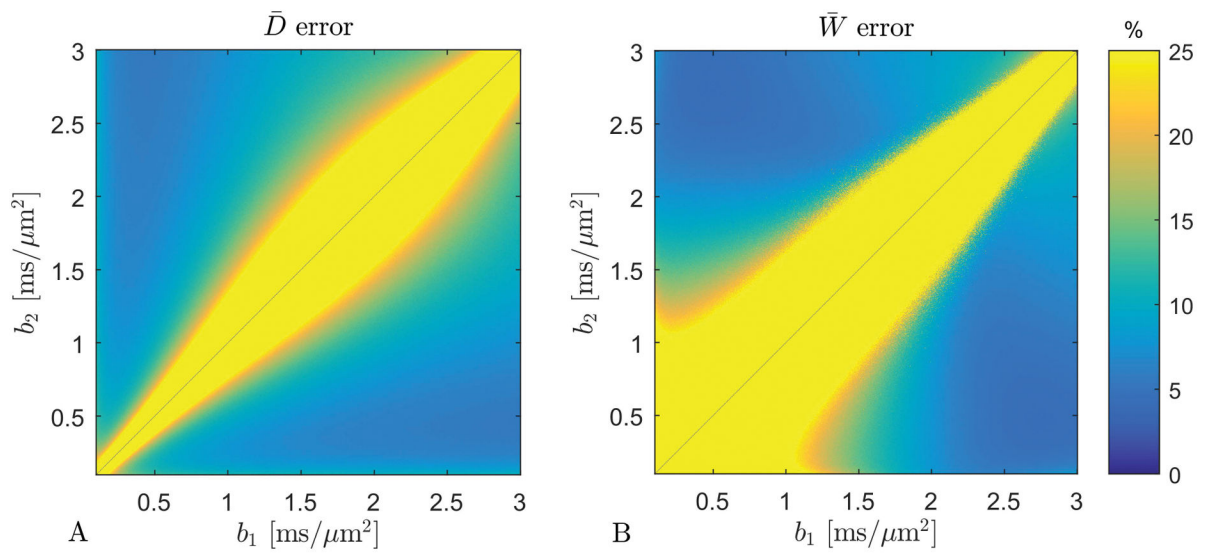


Fig 5. The region of kidney cortex used for b-value optimization is shown in panel A where the region is outlined in red and overlaid on the $b=0$ image. Panel B shows the DK1 fit to the average signal decay curve from the region in panel A. Errorbars are 1 standard deviation wide. The figure also indicates how the fit allows extrapolation to a $b=0$ signal intensity free of IVIM contributions (blue marker).

**Fig. 6.**

The estimate error for \bar{D} (panel A) and \bar{W} (panel B) for SNR = 50. For $b_1 = 0.5 \text{ ms}/\mu\text{m}^2$ and $b_2 = 1.75 \text{ ms}/\mu\text{m}^2$ the error on \bar{D} and \bar{W} is 7% and 11%, respectively. For SNR = 75 these errors decrease to 4% and 7% (data not shown).

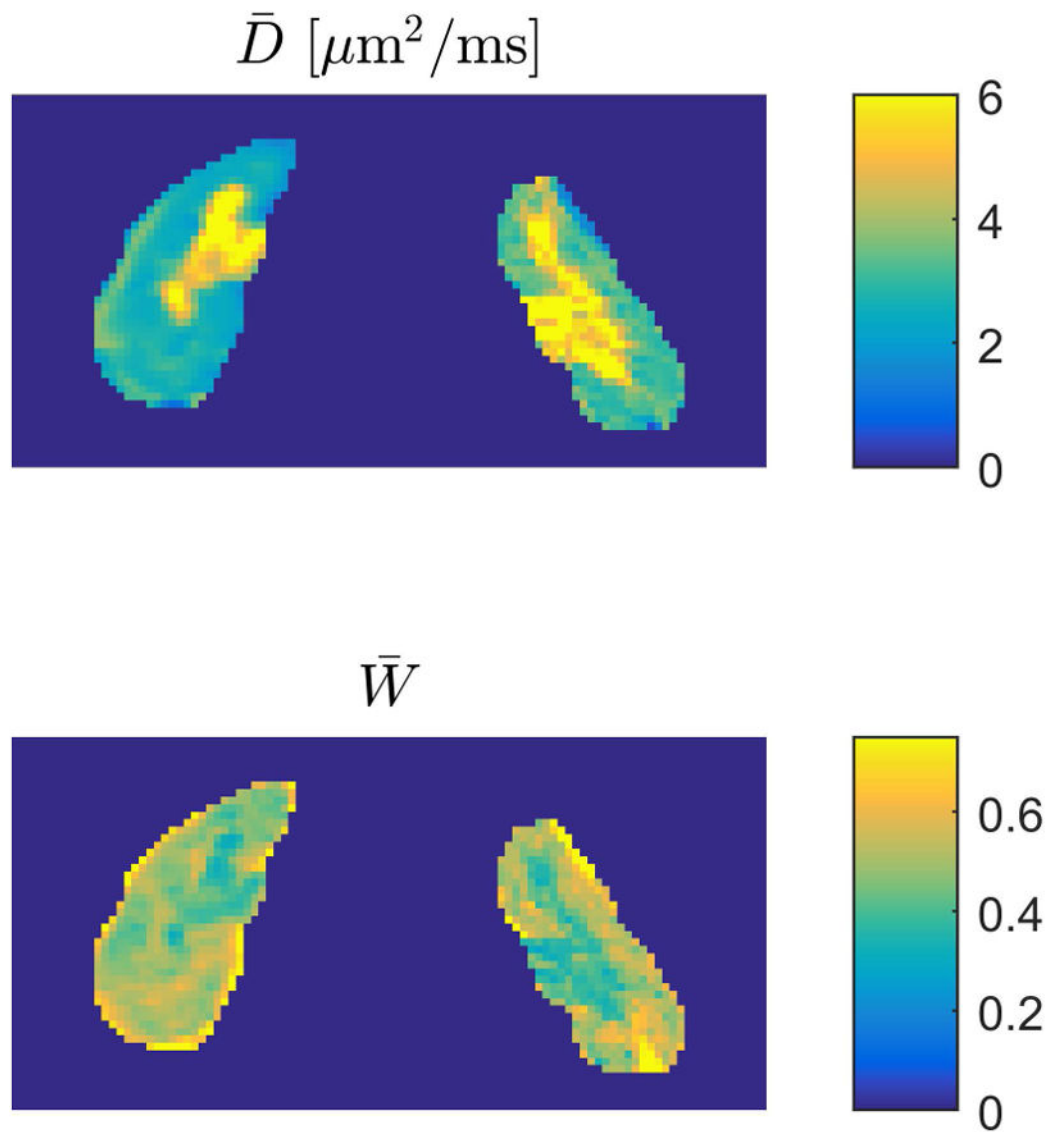


Fig. 7. Estimates of \bar{D} (upper panel) and \bar{W} (lower panel) obtained with the 1-9-9 protocol at the optimal b-values suggested here. Estimates are shown for both kidneys from one human subject.

Table 1

The nine directions in the compact notation used in the manuscript and stated as normalized vectors.

Direction	x-component	y-component	z-component
n^1	1	0	0
n^{1+}	0	$1/\sqrt{2}$	$1/\sqrt{2}$
n^{1-}	0	$1/\sqrt{2}$	$-1/\sqrt{2}$
n^2	0	1	0
n^{2+}	$1/\sqrt{2}$	0	$1/\sqrt{2}$
n^{2-}	$1/\sqrt{2}$	0	$-1/\sqrt{2}$
n^3	0	0	1
n^{3+}	$1/\sqrt{2}$	$1/\sqrt{2}$	0
n^{3-}	$1/\sqrt{2}$	$-1/\sqrt{2}$	0

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