



Chemotaxis and autochemotaxis of self-propelling droplet swimmers

Chenyu Jin^a, Carsten Krüger^a, and Corinna C. Maass^{a,1}

^aDepartment Dynamics of Complex Fluids, Max Planck Institute for Dynamics and Self-Organization, Am Fassberg 17, 37077 Goettingen, Germany

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Chemotaxis and autochemotaxis play an important role in many essential biological processes. We present a self-propelling artificial swimmer system that exhibits chemotaxis as well as negative autochemotaxis. Oil droplets in an aqueous surfactant solution are driven by interfacial Marangoni flows induced by micellar solubilization of the oil phase. We demonstrate that chemotaxis along micellar surfactant gradients can guide these swimmers through a microfluidic maze. Similarly, a depletion of empty micelles in the wake of a droplet swimmer causes negative autochemotaxis and thereby trail avoidance. We studied autochemotaxis quantitatively in a microfluidic device of bifurcating channels: Branch choices of consecutive swimmers are anticorrelated, an effect decaying over time due to trail dispersion. We modeled this process by a simple one-dimensional diffusion process and stochastic Langevin dynamics. Our results are consistent with a linear surfactant gradient force and diffusion constants appropriate for micellar diffusion and provide a measure of autochemotactic feedback strength vs. stochastic forces. This assay is readily adaptable for quantitative studies of both artificial and biological autochemotactic systems.

artificial swimmers | chemotaxis | autochemotaxis | microfluidics

Locomotion of living bacteria or cells can be random or oriented. Oriented motion comprises the various “taxis” strategies by which bacteria or cells react to changes in their environment (1). Among these, chemotaxis is one of the best-studied examples (2, 3): Cells and microorganisms are able to sense certain chemicals (chemoattractants or chemorepellents) and move toward or away from them. This is an essential function in many biological processes, e.g., wound healing, fertilization, pathogenic species invading a host, or colonization dynamics (4, 5). When the chemoattractant or chemorepellent is produced by the microorganisms themselves, the system exhibits positive or negative autochemotaxis. Thus, chemotaxis provides a mechanism of interindividual communication. Modeling such communication strategies is key to understanding the collective behavior of microorganisms (6–8) as well as flocks of animals like fire ants (9, 10).

To model the swimming motion of microorganisms, various self-propelling artificial swimmer systems have been developed based on different mechanisms. Generally, there are two classes of swimmers: systems driven by and aligning with external fields (11–14), including chemotactic gradients, and self-propelled swimmers, which move autonomously in homogeneous environments (15–21). Many autonomous swimmers additionally react to external fields, e.g., phototactic gradients (22).

Biological autochemotactic systems exhibit very complex behaviors (23, 24), where physical effects are intermingling with effects from various bioprocesses such as cell migration, metabolism, and division. To untangle these effects, there have been some design proposals for artificial systems, such as in ref. 25, and simulations on the dynamics of simple autochemotactic microswimmers (26–30). Studies exist on collective effects like autochemotaxis-induced clustering (31–33), but generally, there is still a lack of well-controllable and quantifiable experimental realizations of autochemotactic artificial swimmers. We demon-

strate chemotaxis and autochemotaxis in microfluidic geometries for a highly symmetric and tunable artificial model swimmer system: self-propelling oil droplets in an aqueous surfactant solution (15, 34, 35).

The quantitative study of chemotaxis with traditional methods such as micropipette assays has been limited to observational studies (36, 37), as experimental conditions such as gradient strength are difficult to set in such geometries. Using microfluidic techniques, experimental conditions can be much better controlled; e.g., a linear gradient can be generated and kept constant, or even fast switched (38, 39), the object distribution can be easily analyzed (40), and the objects can be tracked individually (41–43). In this paper we present a microfluidic assay for the quantitative study of autochemotaxis. We have not only observed autochemotaxis reproducibly, but also been able to directly measure system parameters like diffusion constants. This enables further quantitative experimental studies on the dynamics of simple autochemotactic swimmers.

Self-Propelling Droplet Swimmers

When an oil droplet dissolves in a surfactant solution, oil molecules will continuously migrate into the surfactant micelles until the entire droplet is solubilized. The final equilibrium state of the system is a homogeneous micellar nanoemulsion, composed of a mixture of empty micelles, oil-filled micelles, and free surfactant molecules at the critical micelle concentration (CMC). The droplet locomotion is caused by a self-sustained Marangoni flow due to the inhomogeneous interfacial surfactant coverage and only observable in the nonequilibrium state of solubilization (Fig. 1) (35). While incorporating oil molecules, micelles grow in size, incorporating free surfactant molecules from the aqueous phase and increasing the total area of oil–water interfaces in the system. A boundary layer forms around the droplet with a

Significance

Chemotaxis and autochemotaxis are key mechanisms in the dynamics of microorganisms, e.g., in the acquisition of nutrients and in the communication between individuals, as well as influencing their collective behavior. However, chemical signaling and the natural environment of biological swimmers are generally complex, such that control parameters are hard to single out and quantify experimentally. Here, artificial systems with biomimetic features can provide vital insights. We present a well-controllable droplet swimmer system exhibiting both chemotaxis and negative autochemotaxis, as well as microfluidic assays to observe, control, and quantify these effects. Fundamental properties of the system can be derived by a simple analytical model.

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¹To whom correspondence should be addressed. Email: corinna.maass@ds.mpg.de.

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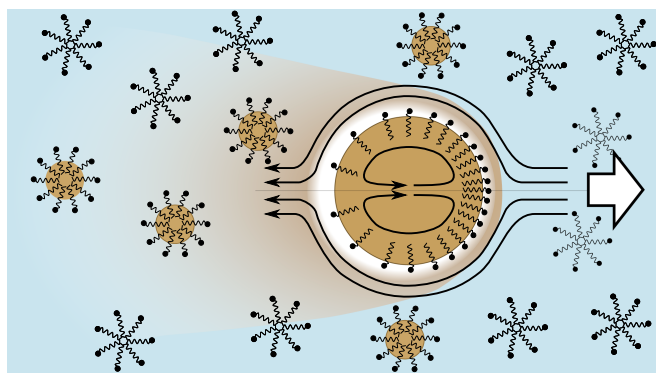


Fig. 1. Schematic drawing of a droplet swimmer moving in surfactant solution. Due to the micellar solubilization of the oil phase, filled micelles disperse from the droplet into the solution, as shown by the yellowish shadow. Close to the droplet the free surfactant molecules are depleted, as shown by the white circle. When the droplet moves, it encounters more empty micelles in the front and leaves more filled micelles behind. The inhomogeneous interfacial surfactant coverage on the droplet then starts the Marangoni flow and sustains the motion. Drawing is not to scale.

reduced density of free surfactant that in turn depletes the surfactant coverage of the droplet interface. This depletion is counteracted by the disintegration of empty micelles approaching the droplet either via diffusion or, if the droplet is moving, via advection. Advection will lead to more available empty micelles in front of the droplet and a trail of filled micelles behind it. In consequence, the depletion at the droplet apex is less pronounced and the resulting Marangoni flow will drive the droplet farther forward toward even more empty micelles. At sufficiently high surfactant concentrations, small fluctuations in the droplet position or surfactant density are sufficient to start sustained self-propulsion. In flow equilibrium, set by the balance of Marangoni forces and viscous dissipation, the swimmer moves at a constant speed controlled by the global surfactant concentration.

The system presented in this study uses the ionic surfactant tetradecyltrimethylammonium bromide (TTAB); the oil phase consists of the nematic liquid crystal 4-pentyl-4'-cyano-biphenyl (5CB). Nematic droplet swimmers of pure 5CB exhibit a strong curling instability (44) in their propulsion, which is absent in isotropic droplets. For this study, we use only isotropic droplets, either by keeping the ambient temperature above the nematic-isotropic transition at $T_{NI} = 35^\circ\text{C}$ or by substituting a mixture of 5CB and 1-Bromopentadecane (BPD) with a volume ratio of 10:1. Henceforth, we refer to the respective droplet types using the notations 5CB and 5CB/BPD. Droplets are mass produced in microfluidic flow-focusing devices with high monodispersity (<5%) and sizes adjustable between 30 μm and 100 μm . The observation time is on the order of hours. Droplet speed and trajectory persistence are well controllable via temperature and surfactant concentration (44). The droplet propulsion is initiated at surfactant concentrations above 4 wt% TTAB.

Chemotactic Maze Solving

Following the argument above, an external gradient of surfactant, i.e., empty micelles, will result in an alignment of the Marangoni flow with the gradient direction; as a result the droplet swimmer will move toward higher surfactant concentrations. This behavior is typical for chemotaxis: The swimmer has no preferred direction in a homogeneous medium, yet moves directionally in the presence of a chemical gradient.

To demonstrate the chemotactic nature of our droplet swimmers, we used a design inspired by Lagzi et al. (11) consisting of two reservoirs connected by a microfluidic maze (Fig. 2). Chemoattractant released at the exit spreads into the maze, with

the local concentration depending on the path distance to the exit. By moving up gradients, swimmers will then prefer the shortest path, as shown in chemotactic experimental systems (11, 12) and simulations (45).

To initiate droplet propulsion, the maze is filled with a micellar TTAB solution at 5 wt%. Directly after the droplet swimmers (5CB/BPD) are released into the entrance reservoir, solid TTAB is added to the exit reservoir, acting as a chemoattractant. The TTAB gradually dissolves and spreads into the maze via convective diffusion, i.e., significantly faster than simple micellar diffusion. Thus, there will be a positive gradient along the optimum path through the maze, attracting the swimmers, whereas dead ends and detours will feature negative gradients, repelling the swimmers back toward the shortest path. In a control experiment, we pre-filled the maze again with a 5 wt% TTAB solution, but added no solids, such that the overall concentration was homogeneous.

Fig. 2 shows results from our experiment. In Fig. 2A, we imaged the surfactant spreading inside the maze qualitatively by mixing the solid TTAB with the fluorescent Nile Red dye, which is insoluble in water and therefore comoves with the surfactant micelles. The still image in Fig. 2A is taken 60 min after the release of solid TTAB; the additional surfactant has spread to the maze entrance and its concentration decreases along side branches.

Fig. 2C and D shows the trajectories of swimmers in a gradient (Fig. 2C) and a control experiment (Fig. 2D) during a 90-min time interval. The trajectories are color coded by time from blue to red. In the presence of a surfactant gradient, (Fig. 2C), the trajectory density is highest along the shortest path, with detours occurring primarily in the first 20 min, before the surfactant has spread sufficiently. In the control experiment without a gradient (Fig. 2D), the swimmers move freely and explore the entire maze, with no correlations in time.

Fig. 2B compares trajectory lengths between gradient and control experiments for all swimmers that successfully traversed the maze, sorted by the time at which they entered the maze.

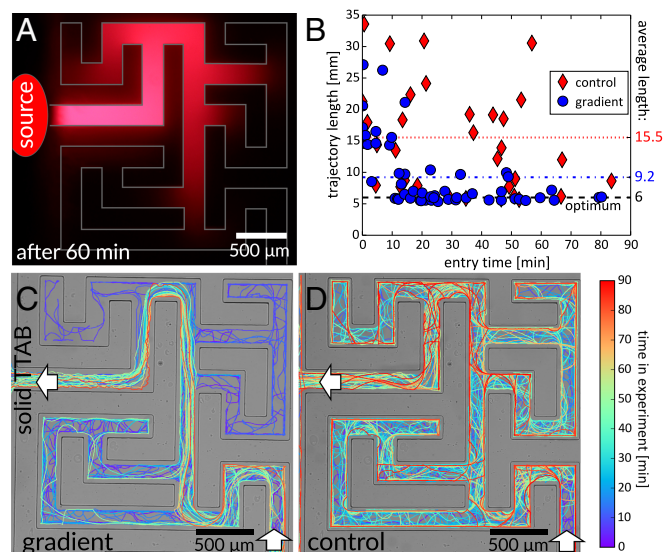


Fig. 2. Maze solving by chemotactic droplet swimmers. White arrows indicate maze entrance and exit. (A) Solid TTAB mixed with fluorescent Nile Red spreading in the maze; distribution after 60 min. "Source" marks the point of release (the excitation LED was shaded in this area to improve contrast). (C and D) Trajectories with and without TTAB gradient. We selected only swimmers that passed both entrance and exit points. Line colors correspond to the time in the experiment. In C, detours are mostly for early times (purple) whereas in D there is no correlation. (B) Plot of path lengths vs. entry time, compared with the shortest path length (6 mm) (Movies S1–S3).

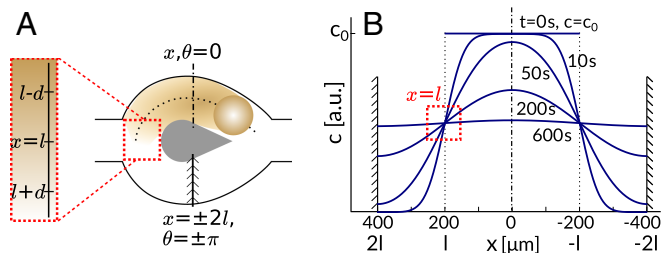


Fig. 5. (A) Schematic drawing of a bifurcation. The trail of a swimmer fills the top branch and diffuses into the bottom branch around the pillar. The bifurcation is mapped to a fixed radius polar coordinate $x = (2l/\pi) \cdot \theta$ with the origin at the top of the bifurcation and $x = l$ at its entrance. (B) Trail dispersion, characterized by the concentration profile of micellar-solubilized oil molecules c , approximated by 1D diffusion from a step function between reflecting boundaries, with calculated profiles from 0 s and 600 s. Red dotted rectangle marks the gradient at $x = l$.

In our circular pillar approximation, the diffusion problem is symmetric around $x = 0$, and we neglect diffusion into the main channel at $x = \pm l$. The gradient evolution at $x = l$ can be mapped onto the problem of 1D diffusion between two reflecting or periodic boundaries at $x = \pm 2l$ (Fig. 5B). The concentration profile in the region $-2l \leq x \leq 2l$ evolving over time from a step function $c(-l \leq x \leq l) = c_0$ is (47)

$$c(x, t) = \frac{c_0}{2} \sum_{n=-\infty}^{\infty} \left(\operatorname{erf} \left(\frac{(4n+1)l-x}{\sqrt{4D_f t}} \right) - \operatorname{erf} \left(\frac{(4n-1)l-x}{\sqrt{4D_f t}} \right) \right), \quad [1]$$

where D_f denotes the diffusion coefficient of the filled micelles, which are the carriers of the solubilized oil. We provide a full derivation in the [Supporting Information](#).

Using parameters appropriate to our experimental system [$l \approx 200 \mu\text{m}$, $D_f \approx 100 \mu\text{m}^2 \cdot \text{s}^{-1}$ (48)], we calculate and plot examples of concentration profiles at different times in Fig. 5B. We expect the anticorrelation between the choices of two consecutive swimmers to decay in time, depending on the decrease of the gradient at $x = l$. In the long time limit, after the environment in the two branches becomes homogeneous again, the choice of a swimmer between the two branches should be completely random, i.e., independent of the choice of the previous swimmer.

The swimmers make their choice at the entrance $x = l$ under both the gradient force and the stochastic force. In all experiments, we did not observe swimmers reversing direction once past the bifurcation. This indicates that the choice is made within a small region $x \in [l-d, l+d]$, as sketched in Fig. 5A, with d on the order of the droplet diameter or channel width, and on a timescale τ much shorter than the timescale t of the trail dispersion. Hence, the motion of the swimmer $x(\tau)$ during the decision process can be approximated as a 1D Brownian motion under a constant gradient force between two absorbing boundaries at $l \pm d$, described by the following overdamped Langevin equation:

$$\frac{dx}{d\tau} \Big|_{x=l} = \kappa \partial_x c + \sqrt{2D} \Gamma(\tau). \quad [2]$$

Here, κ is a linear coefficient quantifying the sensitivity to the chemorepellent gradient $\partial_x c$. Because the chemorepellent is self-produced, κ corresponds to the autochemotactic feedback strength used in the literature (26–30). Note that κ is not identical to the chemotactic strength as applicable to the maze experiments, which is based on a gradient in empty micelles. $\Gamma(\tau)$ is a normalized Gaussian noise term with $\langle \Gamma(\tau) \rangle = 0$, $\langle \Gamma(\tau), \Gamma(\tau + \Delta\tau) \rangle = \delta(\Delta\tau)$. The velocity of the active swimmer is not included in Eq. 2, as the branch choice direction is orthogonal to the

incoming swimmer. D denotes the diffusion coefficient of a passive swimmer and is presumably larger than the Stokes–Einstein value of $k_B T / 6\pi\eta r$, because the micellar solubilization process provides an additional source of stochastic noise.

The position of the swimmer $x(\tau)$ can be written as

$$x(\tau) - l = \kappa \partial_x c \tau + \sqrt{2D} B^\circ(\tau), \quad [3]$$

where $B^\circ(\tau)$ is a standard Brownian motion process and $x(0) = l$.

The probability \mathcal{P} of anticorrelated branch choices between two consecutive swimmers is then the probability that the biased Brownian motion process $x(\tau)$ reaches $l + d$ before $l - d$ (49):

$$\mathcal{P} = \frac{1 - \exp(-2\xi)}{\exp(2\xi) - \exp(-2\xi)}, \quad \xi = -\frac{\kappa \cdot d}{2D} \partial_x c. \quad [4]$$

In our data analysis, we record events of correlated branch choices between consecutive swimmers as $\mathcal{C} = 1$ and anticorrelated choices as $\mathcal{C} = -1$. If the interaction of a swimmer and a pillar contains several passages, i.e., the swimmer orbits the pillar, we consider only the last passage of the preceding swimmer and the first passage of the following swimmer. To study the time-dependent decay of the (anti)correlation, we bin the experimental result according to the time interval Δt between the preceding swimmer leaving the bifurcation and the following swimmer entering it. Using Eq. 4 with a concentration gradient $\partial_x c$ at $x = l$, $t = \Delta t$, the average correlation between the choices of consecutive swimmers is

$$\langle \mathcal{C} \rangle = -1 \cdot \mathcal{P} + 1 \cdot (1 - \mathcal{P}) = \tanh(\xi(\Delta t)). \quad [5]$$

The statistical result for $\langle \mathcal{C} \rangle$ from a series of branch-choosing experiments is shown in Fig. 6. Because some microfluidic bifurcations can be biased due to fabrication errors, we accepted only results from bifurcations where the overall preference for a single branch was less than 75%. The bias-corrected dataset contains 4,160 correlation events, omitting 283 rejected events. The data are binned by the time interval Δt ; the average correlation $\langle \mathcal{C} \rangle$ of each bin is plotted vs. the corresponding average Δt (blue bars). To account for the steep correlation decay for short times and decreasing statistics for long times, we use a constant number of events (100 swimmer pairs) per bin, resulting in an increasing range of time intervals, indicated by the bar width.

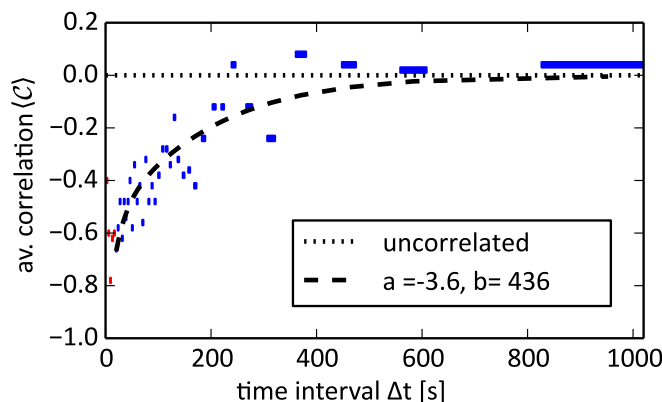


Fig. 6. Correlation $\langle \mathcal{C} \rangle$ between branch choices of consecutive swimmers vs. the time interval Δt between passages. Data were binned by Δt using 100 events per bin and then averaged (the corresponding Δt range is marked by the bar width). $\langle \mathcal{C} \rangle$ decorrelates with increasing Δt , with the limits of $\langle \mathcal{C} \rangle \in [-1, 0]$ for perfect anticorrelation (-1) and no correlation (0). The parameters $a = -3.6 \pm 0.2$ and $b = (4.3 \pm 1.2) \times 10^2 \text{s}$ for the fitted $\langle \mathcal{C} \rangle = \tanh(\xi)$ were derived by fitting ξ using Eqs. 5–7. Correlation data for $\Delta t < 10 \text{s}$ (red bars) were omitted from the fitting to rule out hydrodynamic drag effects. Supplementary data on the effects of TTAB concentration and channel geometry are provided in Figs. S2 and S3.

When Δt is small, the choices of swimmers show a clear anticorrelation up to -0.8 ; i.e., 90% of the following swimmers choose the branch that the preceding swimmer did not pass. As Δt increases, this average anticorrelation decreases to values close to zero; i.e., swimmers enter branches randomly and independent of the preceding swimmer.

With Eq. 5, ξ can be easily calculated from the anticorrelation data. We truncate the concentration profile from Eq. 1 to the $n = 0, \pm 1$ terms and fit ξ with

$$\xi = -\frac{a}{\sqrt{t}}(2\exp(-b/t) - 1 - 2\exp(-4b/t) + \exp(-9b/t)), \quad [6]$$

with two parameters, a prefactor a and a time constant b :

$$a = \frac{\kappa}{D} \cdot \frac{\beta d}{4vwh\sqrt{\pi D_f}}, \quad b = \frac{l^2}{D_f}. \quad [7]$$

The corresponding function for the average correlation $\langle C \rangle$ is then plotted in Fig. 6 as black dashes.

With $b \approx 436$ s from fitting the experimental data and $l \approx 200$ μm , we calculated $D_f \approx 92$ $\mu\text{m}^2 \cdot \text{s}^{-1}$, which agrees with calculated and literature values ($D_f \approx 100$ $\mu\text{m}^2 \cdot \text{s}^{-1}$) (48). In our expression for a in Eq. 7, all quantities except the autochemotactic coupling strength κ and the droplet diffusion coefficient D can be measured or calculated independently. We can therefore use a as a direct measure of the strength of chemotactic vs. stochastic forces, κ/D .

Conclusion and Summary

We studied a system of self-propelled droplets that exhibits chemotaxis comparable to that of biological systems. The motion of the oil-in-water droplets is driven by a Marangoni flow, which is caused by a self-sustained interfacial tension gradient during the solubilization of the droplet in a micellar surfactant solution. In a homogeneous solution, the swimmers show no directional preference, whereas they move up surfactant gradients, i.e., gradients in empty micelles, whose effect we have used to guide them through microfluidic mazes.

A related effect is trail avoidance by negative autochemotaxis, due to gradients of oil-filled micelles in the wake of a droplet. We have studied this effect quantitatively, observing anticorrelated branch choices between consecutive droplets in microfluidic channel bifurcations. We could model the time-dependent correlation decay analytically, assuming a force on the droplets proportional to the local empty micelle gradient.

Fitting our data yielded two system parameters: a time constant b depending on the micellar diffusion timescale and a lin-

ear prefactor a , containing the secretion rate β and the strength of (auto)chemotaxis κ over stochastic force D . In biological systems, where various physical effects and bioprocesses are intertwined, these parameters are often difficult to measure independently. Microfluidic assays as presented above can provide reproducibly quantitative experimental data for statistics and comparative studies. In our droplet swimmer system, we will use insights from this study to predict and control autochemotactic effects in more complicated geometries and to compare the swimmer dynamics with theoretical models (26–30).

Materials and Methods

Chemicals. We obtain 5CB, BPD, TTAB, and Nile Red from commercial suppliers (Synthon Chemicals and Sigma-Aldrich) and use them as is.

Microfluidic Devices. We fabricate microfluidic devices using standard soft lithography procedures: We create photomasks in a 2D AutoCad application and have them printed as a high-resolution emulsion film by an external company (128,000 dots per inch; JD Photo-Tools). A Si wafer (Wafer World Inc.) is spin coated with a negative photoresist (SU-8; Micro Resist Technology) in a clean room environment. UV light exposure through a photomask and subsequent chemical development produce a master wafer containing the microstructures.

We then use the master wafer in a polymer molding step to cast the microstructure into PDMS (polydimethylsiloxane; Sylgard 184; Dow Corning). After degassing and heat curing at 75 °C for 2 h, we peel the PDMS replica off the wafer, cut it into single pieces, and punch in fluid inlets and outlets. We then seal the molded PDMS blocks from below by glass slides. Covalent bonding between PDMS and glass is achieved by pretreating all surfaces in an air plasma (Pico P100-8; Diener Electronic GmbH + Co. KG) for 30 s.

We produce droplets in standard flow-focusing microfluidic devices, mounting syringes (Braun) on a precision microfluidic pump (NEM-B101-02B; Cetoni GmbH) and connecting them to the inlets and outlets with Teflon tubing (39241; Novodirect GmbH). To create oil-in-water emulsions, we first activate the originally hydrophobic PDMS surfaces by a 1:1 volumetric mixture of $\text{H}_2\text{O}_2/\text{HCl}$, then fill the channels with a silanization solution [$(\text{C}_2\text{H}_5\text{O})_n\text{C}_7\text{H}_{15}\text{O}_4\text{Si}$] for 30 min, and finally rinse them with milli-Q water.

During experiments, we introduce a concentrated droplet stock solution into microfluidic devices, using standard pipettes.

Image Recording and Analysis. We record swimmers (still images and movies) on an Olympus IX-73 optical microscope connected to a commercial digital camera (Canon EOS 600D) at four frames per second. Images are processed (swimmer tracking and trajectory analysis) using software written in-house in Python/openCV.

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