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Nitric Oxide Release by Deoxymyoglobin Nitrite Reduction During Cardiac Ischemia: A Mathematical Model

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Abstract

Interactions between cardiac myoglobin (Mb), nitrite, and nitric oxide (NO) are vital in regulating O2 storage, transport, and NO homeostasis. Production of NO through the reduction of endogenous myocardial nitrite by deoxygenated myoglobin has been shown to significantly reduce myocardial infarction damage and ischemic injury. We developed a mathematical model for a cardiac arteriole and surrounding myocardium to examine the hypothesis that myoglobin switches functions from being a strong NO scavenger to an NO producer via the deoxymyoglobin nitrite reductase pathway. Our results predict that under ischemic conditions of flow, blood oxygen level, and tissue pH, deoxyMb nitrite reduction significantly elevates tissue and smooth muscle cell NO. The size of the effect is consistent at different flow rates, increases with decreasing blood oxygen and tissue pH and, in extreme pathophysiological conditions, NO can even be elevated above the normoxic levels. Our simulations suggest that cardiac deoxyMb nitrite reduction is a plausible mechanism for preserving or enhancing NO levels using endogenous nitrite despite the ratelimiting O_2 levels for endothelial NO production. This NO could then be responsible for mitigating deleterious effects under ischemic conditions.

Keywords

myoglobin nitrite reductase; myocardial infarction; mass transport; arteriole model

1. Introduction

Myoglobin (Mb) is an intracellular oxygen binding protein that has a variety of important functions in O_2 storage and delivery. Mb has been shown to substantially contribute to nitric oxide (NO) – a powerful paracrine vasodilator - homeostasis in the heart (Flögel et al., 2010). In normoxia, Mb is a strong scavenger of NO. However, in hypoxic conditions, deoxygenated myoglobin (deoxyMb) has been shown to enzymatically reduce nitrite to NO.

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It is hypothesized that this is one of several nitrite reduction pathways in the body that provides a mechanism for the body to generate NO during conditions when oxygendependent endothelial nitric oxide synthase (eNOS) production falls (Faassen et al., 2010; Hendgen-Cotta et al., 2010).

Myoglobin nitrite reduction has been shown to reduce ischemic damage, mitigate ischemia/ reperfusion injury, and reduce myocardial infarction size through NO release in animal and human heart studies (Hendgen-Cotta et al., 2008; Rassaf et al., 2007; Shiva et al., 2007; Totzeck et al., 2012a). The ability of myocardial Mb to effectively produce NO from nitrite in vivo has been challenged by its high affinity to oxygen, which reduces the availability of deoxyMb. However, endogenous nitrite, relatively high in tissue, has been shown to be sufficient to reduce ischemic damage, although the mechanism by which NO does this is not fully understood (Flögel et al., 2010; Totzeck et al., 2012b). Myoglobin deficient animals have been shown to be more susceptible to ischemic damage (Flögel et al., 2010; Rassaf et al., 2007), and myoglobin deficient animals with overexpressed inducible NOS have developed cardiac hypertrophy, ventricular dilatation, and fibrosis (Wunderlich et al., 2003). Due to experimental limitations, there are relatively few physiological human studies on cardiac Mb nitrite reduction (Ormerod et al., 2011; Webb et al., 2004). However, in vivo and in vitro studies have reported therapeutically beneficial uses of myocardial nitrite in treating ischemia through NO release in animals such as rats and mice, (Baker et al., 2007; Rassaf et al., 2014; Shiva et al., 2007; Tiravanti et al., 2004; Zweier et al., 2010) horses (Totzeck et al., 2012b), and fish (Pedersen et al., 2010). It is thought that Mb scavenges NO during normoxic conditions to maintain homeostasis and prevent deleterious transient NO effects, but releases NO during ischemic conditions such as low flow, low blood PO_2 , and low pH in order to inhibit cardiac respiration, reduce reactive oxygen species generation, and vasodilate cardiac vessels (Hendgen-Cotta et al., 2008; Rassaf et al., 2007).

Previous mathematical models have considered the effect of myoglobin as a scavenger on NO transport in microcirculatory vessels and the effects of myoglobin, nitrite, and NO reactions (Buerk, 2001; Kavdia et al., 2002; Kavdia and Popel, 2004; Tsoukias, 2008), but have not quantified the relative importance of deoxymyoglobin releasing NO from tissue nitrite in ischemic conditions relative to Mb scavenging of NO during normal oxygen and flow. The NO producing capabilities of cardiac Mb have previously been estimated using simple reaction kinetics calculations (Kim-Shapiro and Gladwin, 2014), without considering the effect of mass transport inside an arteriole environment. We have previously modeled (Liu et al., 2016) the effect of the deoxyhemoglobin nitrite reductase pathway on blood nitrite, but the deoxymyoglobin pathway is active on tissue nitrite and has different reaction kinetics. There is a need for mathematical models to analyze this scavenger and producer mechanism of myoglobin to explain the experimental effectiveness of cardiac tissue nitrite in releasing NO under ischemic conditions. The goal of this study is to determine the effectiveness of deoxyMb nitrite reductase during ischemia compared to its NO scavenging behavior under normoxic conditions. For this purpose, we developed a mathematical model for a cardiac arteriole and surrounding tissue to investigate the effect of deoxyMb nitrite reduction of endogenous nitrite in releasing NO during ischemia.

2. Model Development

2.1. Description of mathematical model

NO and O₂ transport were considered in a cardiac arteriole and surrounding myocardial tissue, modeled as a cylindrical vessel with surrounding tissue. Coupled nonlinear partial differential equations were written in cylindrical coordinates and solved for steady-state conditions by finite element numerical methods using the software COMSOL v5.1 (COMSOL, Inc., Burlington, MA), similar to our previous approach (Buerk et al., 2011; Liu et al., 2016). The model has concentric cylindrical layers: (i) red blood cell (RBC) core, (ii) a RBC-free plasma layer, (iii) endothelium, (iv) vascular wall, and (v) perivascular cardiac tissue (Fig. 1). All model layers were assumed to have homogenous properties with uniform species reactions within.

Concentration gradients were assumed to be axisymmetric and axial diffusion was assumed to be negligible. Blood flow was assumed to be well-developed and laminar. At steady state, the governing mass transport equation therefore simplifies to Eq. (1):

$$
0=D_i\left[\frac{1}{r}\frac{\partial}{\partial r}\left(r\frac{\partial C_i}{\partial r}\right)\right]-V_z\frac{\partial C_i}{\partial z}\pm\sum R_i\tag{1}
$$

where D, C, and R are the diffusivity, concentration, and reactions of the species, i , corresponding to NO and O_2 . The axial flow velocity v_z is given by Poiseuille flow. Table 1 lists the dimensions and physical constants in the model.

2.2. Nitric oxide

Coupled NO-O₂ transport models have been developed previously by us (Chen, 2006; Lamkin-Kennard et al., 2004; Liu et al., 2016) and others (Kavdia et al., 2002; Tsoukias, 2008) and our approach here is similar. Endothelial nitric oxide synthase (eNOS) in layer 3 was assumed to uniformly produce NO with a linear shear stress dependence and $O₂$ dependent Michaelis-Menten kinetics (Eq. 2). All other substrates and co-factors were assumed to be in abundant supply.

$$
R_{NO} = R_{NO_{\text{max}}} \left(\frac{P_{O_2}}{P_{O_2} + K_m} \right) \left(\frac{\tau_W}{\tau_{\text{ref}}} \right) \tag{2}
$$

where K_m is the Michaelis-Menten constant and τ_{ref} is the reference value used by Chen et al. (Chen et al., 2011) R_{NOmax} was calculated so that at baseline flow (centerline velocity = $1000 \mu m s^{-1}$), NO production matches the solely O₂-dependent Michaelis-Menten values used by Buerk (Buerk, 2001). Shear stress was calculated as a function of flow using the laminar pipe flow wall shear stress equation (Eq. 3):

$$
\tau_w = \mu_\text{b} \frac{2_{v_{\text{max}}}}{r_{\text{vessel}}} \quad (3)
$$

where μ _b - the dynamic viscosity of blood - was calculated using the modified microvessel viscosity equation by Pries et al. (Pries et al., 1994) NO is scavenged by hemoglobin in layer 1 and by oxymyoglobin in layer 5 with first order rate constants λ_b and λ_{Mb} , respectively. The Hb scavenging constant λ_b has been estimated around 100-750 s⁻¹ at a systemic hematocrit of 45%, and our chosen value of 382.5 s^{-1} falls within these values (Buerk, 2009; Carlsen and Comroe, 1958; Tsoukias and Popel, 2003). In layers 4 and 5, NO reacts with soluble guanylyl cyclase (sGC) with first order scavenging rate constant λ_t . NO is also produced by enzymatic myoglobin reduction of endogenous cardiac nitrite (described below).

2.3. Oxygen

RBC-rich layer 1 was assumed to have uniform, constant $O₂$ delivery which was independently varied from severe anoxia to typical normoxia levels (0.1-120 Torr). The lower end of this range represents levels of oxygen representative of extreme ischemic events such as acute myocardial infarction, where flow and $O₂$ are nearly entirely restricted, compared to more mild physiological hypoxia levels around 20 Torr (Faassen et al., 2010). The amount of O_2 consumed by eNOS is twice that of NO produced. Oxygen consumption in the vascular wall and tissue was reversibly inhibited through inhibition of cytochrome oxidase by NO in a modified Michaelis-Menten equation (Eqs. 4 and 5) as modeled by Buerk (Buerk, 2001).

$$
R_{O_2} = R_{O_2 \text{max}} \frac{P_{O_2}}{P_{O_2} + \text{AppK}_m}
$$
 (4)

$$
AppK_m = K_m^* \left(1 + \frac{C_{NO}}{27 \, nM} \right) \quad (5)
$$

where K_{m}^{*} is assumed to be 1 Torr for these simulations.

2.4. Myoglobin and Mb nitrite reductase

Myoglobin and nitrite were assumed to be uniformly present and constant in the perivascular cardiac tissue (layer 5), and quantified with experimentally reported values for healthy adult humans (Table 1). Cardiac tissue nitrite levels vary depending on factors such as dietary habits and lifestyle (e.g. tobacco consumption, exercise), but have been shown to be around 20 μM (Faassen et al., 2010; Hendgen-Cotta et al., 2008). The oxymyoglobin saturation curve was defined using Eq. (6):

$$
Y_{O_2} = \frac{P_{O_2}}{P_{50} + P_{O_2}} \tag{6}
$$

where P_{50} is 2.31 Torr.

Oxygenated myoglobin ($MbO₂$) scavenges NO as in Eq. (7) with second order rate constant λ_{Mb} (Ascenzi and Brunori, 2001).

$$
MbO_2+NO \xrightarrow{\lambda_{Mb}} \text{metMb}+NO_3^- \quad (7)
$$

Deoxygenated myoglobin reduces nitrite as a function of nitrite and deoxyMb concentration with second order rate constant k_{Mb} . This rate constant has been experimentally reported in the range of 12.0-12.86 M⁻¹ s⁻¹ at 37°C and pH = 7.4, changing ten-fold with each unit pH change (Gladwin and Kim-Shapiro, 2008; Hendgen-Cotta et al., 2010; Shiva et al., 2007). This nitrite reduction behavior is quantified as Eq. (8):

$$
R_{NO} = k_{Mb} \left(10^{7.4-pH} \right) \left[\text{nitrite} \right] \left[\text{deoxyMb} \right] \tag{8}
$$

where k_{Mb} is 12.4 M⁻¹ s⁻¹. Postischemic cardiac tissue pH levels have been measured as low as 5.5, from a normal pH around 7-7.4 (Buerk et al., 2003; Zweier et al., 2010, 1999). All other secondary reactions between myoglobin, NO, and other nitroso species are assumed to be negligible as experimental evidence has shown that Eqs. 7 and 8 are the primary reactions affecting functional NO from nitrite reduction (Rassaf et al., 2007; Shiva et al., 2007).

2.5. Boundary conditions

Zero mass fluxes were assumed for all species at the center of the blood vessel $(r = 0)$ and at the outermost boundary of layer 5 $(r₅)$ in Eq. (9):

$$
D_i \frac{\partial C_i}{\partial r} = 0 \text{ at } r = 0, r_5 \quad (9)
$$

The mass flux of a species exiting one layer is assumed to equal the mass flux entering the adjacent layer e.g. for the lumen boundary (r_2) in Eq. (10):

$$
-D_i \frac{\partial C_i}{\partial r_{\text{lumen}}}\n=Di \frac{\partial C_i}{\partial r_{\text{endothelium}}\n\tag{10}
$$

2.6. Numerical methods

The model was solved in COMSOL v5.1 at steady state with relative accuracy of 1×10^{-6} to predict concentration profiles across the arteriolar domain $(0 < r < 130 \mu m)$ and averaged across the smooth muscle cell (SMC) region (layer 4) and perivascular tissue region (layer 5) at the arteriole midline ($z = 150 \,\mu$ m). Simulations were performed with and without tissue nitrite present in layer 5 while varying blood $PO₂$, blood flow rates, and tissue pH to determine the effect of deoxyMb nitrite reductase in producing NO during ischemic conditions. Simulations done at zero blood oxygen and flow were not feasible due to solver limitations, so 0.1 Torr and 1% centerline v_{max} (10 μ m s⁻¹) were used to simulate almost complete ischemic blockage.

3. Results

Ischemia leads to a deficiency in blood $PO₂$, which monotonically decreases tissue $PO₂$, averaged across layer 5 (Fig. 2A). A decrease in blood PO from normoxic levels (around 120 Torr) to near anoxic levels (0.1 Torr) leads to a decrease in average tissue $PO₂$ from 50.1 to 0.1 Torr, respectively (Fig. 2A inset). This change in tissue PO_2 affects the saturation percentage of perivascular tissue myoglobin as in Eq. 6 (Fig. 2B).

Without the contribution of tissue nitrite, ischemic decreases in blood $PO₂$ (and tissue $PO₂$) lead to decreases in NO across the computational domain (Fig. 3). A decrease in blood $PO₂$ from 120 to 1 Torr leads to a decrease in peak NO at the endothelium-SMC boundary ($r = 15$) μm) from 45.6 to 8.28 nM, respectively. Tissue NO is <5 nM at all blood oxygen values without tissue nitrite due to strong myoglobin scavenging.

Ischemic decreases in flow also lead to changes in NO availability. Without tissue nitrite reduction, decreasing flow and blood $PO₂$ down to near zero values (0.1 Torr, 1% flow) both lead to a decrease in averaged SMC NO in the $15 < r < 25$ µm region (Fig. 4). Changes in tissue pH from ischemia have little effect on the shear- and O_2 - dependent NO produced by eNOS in layer 3.

With the added effect of tissue nitrite reduction by deoxyMb, there is a significant increase in NO, increasing in effect at lower blood PO_2 (1 vs. 10 Torr) and lower pH (Figs. 5A and 5B, respectively). The increase in NO is greatest in magnitude at the tissue and SMC regions but relatively minor in the blood and plasma layers. The effect is significant at the SMC region for all flow values and stronger at the lower limit of $pH = 5.5$ (Fig. 6B) versus $pH =$ 6.85 (Fig. 6A). There was little effect on the $PO₂$ profiles with the incorporation of tissue nitrite reduction; variations in average tissue $PO₂$ between no nitrite and nitrite for all flow and pH cases were <1 Torr (not shown).

The absolute elevation of both average SMC NO (Fig. 7A) and average tissue NO (Fig. 7B) by tissue nitrite is consistent at different flow values, but relatively higher at low flow because of the decrease in NO availability at lower shear stress. The elevation in NO is also higher in the tissue region than the SMC region, and higher as tissue pH decreases. Table 2 summarizes the changes in NO between the no nitrite and nitrite cases for various ischemic conditions at baseline flow.

4.1. Discussion

The results of our simulations suggest that in conditions of cardiac ischemia resulting in low blood PO2, low flow, and low pH, reduction of endogenous nitrite by deoxymyoglobin can significantly elevate both tissue and smooth muscle cell NO. Our computational model is the first attempt to explicitly model the interplay between myoglobin scavenging of NO at normoxia and its opposing role of producing NO from tissue nitrite under certain conditions. As blood PO_2 falls from normoxic to hypoxic and near anoxic levels (Fig. 2A), tissue PO_2 levels can drop to levels inside the range of the P_{50} of Mb (Fig. 2B), where the concentration of deoxyMb rapidly increases. This in turn leads to a significant increase in deoxyMb nitrite reduction, while simultaneously decreasing the scavenging NO by MbO₂.

Similarly, decreases in flow and blood $PO₂$ comparable to levels found during extreme cardiac ischemia, such as during a myocardial infarction, lead to significant shortages in NO production by eNOS (Figs. 3 and 4) (Gladwin and Kim-Shapiro, 2008; Rassaf et al., 2007). At extreme levels of ischemia (1% v_{max} , 1 Torr), there is almost zero NO across the arteriolar radius when there is no tissue nitrite. These results are consistent with previous mathematical models studying the effect of flow and blood oxygen levels on NO availability without compensatory nitrite reduction pathways (Chen, 2006; Tachtsidis et al., 2011; Tsoukias, 2008). Additionally, the presence of Mb in perivascular cardiac tissue at strongly scavenges NO; there is ≤ 1 nM NO in the tissue region at all conditions in our modeled cardiac arteriole at normoxia (Fig. 3) due to the high rate constant of the Mb-NO reaction (Eq. 7). Previous models show a similar reduction in NO in vascular SMC due to myoglobin scavenging with almost complete NO scavenging at the SMC-tissue border, but they did not model any recovery via deoxyMb nitrite reductase (Kavdia, 2006; Kavdia and Popel, 2004). It has been postulated that cardiac muscle Mb serves to protect the region from transient increases in cytosolic NO from nitric oxide synthase in the endothelium, the sarcoplasmic reticulum, and the mitochondria by inactivating excess NO (Blomberg et al., 2004; Flögel et al., 2001). In contrast, Mb will switch to becoming an NO producer at extremely low oxygenation and flow conditions, when $O₂$ -dependent eNOS production is limited.

When the effect of deoxyMb nitrite reduction of endogenous tissue nitrite is considered, our simulations predict that low blood flow and $PO₂$ conditions result in significantly elevated NO across the endothelium, SMC, and tissue regions, in increasing order of magnitude (Fig. 5). This NO elevation effect is consistent at different flow values, but relatively more powerful at low flow conditions because of the lower baseline NO from shear-stressdependent production (Fig. 6). Both blood PO₂ and flow rates will decrease during ischemia. Similarly, lowering pH values from normal (6.85) to severely ischemic heart values will

significantly increase the elevation of nitrite-derived NO (Fig. 7). The dependence of Mb nitrite reduction on pH has been experimentally shown to be very high (10-fold change in reaction rate for every unit pH change) and another factor in the large elevation of tissue and SMC NO following cardiac ischemia (Shiva et al., 2007; Totzeck et al., 2012a; Trochu et al., 2000). With the combination of very low flow, blood $PQ₂$, and tissue pH that could occur during severe ischemia (e.g. 10 μ m s⁻¹, 1 Torr, 5.5 tissue pH), NO elevations in blood and tissue can reach the 30-50 nM range, which is comparable to or even surpasses the steady state predictions at normal, non-ischemic conditions (Table 2).

These results are in agreement with experimental evidence showing that nitrite reduction by deoxyMb is a significant producer of NO in cardiac muscle in ischemic and hypoxic conditions (Rassaf et al., 2007; Shiva et al., 2007; Webb et al., 2004). Functionally significant levels (>5 nM) of NO produced by deoxyMb are detected with subendocardium oxygen levels around 2-5 Torr (Shiva et al., 2007), and NO production measured indirectly through NO-heme accumulation was appreciable only with hypoxia and levels of nitrite application similar to our simulation concentrations (20 μM) (Rassaf et al., 2007). Direct reporting of NO generation rates by deoxyMb during ischemia is rare due to experimental difficulties, but estimates from analysis of human and mice Mb are around 1-5 nM s-1 (Totzeck et al., 2012b; Zweier et al., 2010). In addition, Mb nitrite production of NO has been shown to significantly decrease myocardial infarction size and reduce ischemic injury or ischemia/reperfusion injury in animal experiments (Hendgen-Cotta et al., 2008; Shiva et al., 2007; Totzeck et al., 2012b; Webb et al., 2004). It is not exactly understood how this released NO reduces ischemic damage or mitigates ischemia-reperfusion injury. It has been hypothesized that the release of NO by deoxyMb during ischemia could downregulate cardiac energy consumption via reduced contractility and oxygen consumption. Additionally, the released NO can serve to reduce reactive oxygen species generation or inhibit adhesion molecule expression and platelet aggregation (Gladwin and Kim-Shapiro, 2008; Hendgen-Cotta et al., 2008; Lamkin-Kennard et al., 2004; Rassaf et al., 2007). Nitritederived NO from deoxyMb has been demonstrated to inhibit cellular respiration in myocardial infarctions, but it is not yet understood exactly how NO escapes autocapture by secondary reactions with myoglobin species such as deoxyMb and metMb (Hendgen-Cotta et al., 2008; Webb et al., 2004). It has been proposed that the proximity of nitrite-derived NO to mitochondria (specifically, cytochrome c oxidase binding to inhibit respiration) allows this NO to escape autocapture (Shiva et al., 2007; Totzeck et al., 2012a), or that in vivo conditions result in scavenging rates of NO by these secondary reactions that are sufficiently low to allow escape (Blomberg et al., 2004; Gladwin and Kim-Shapiro, 2008). This elevation of NO leads to downregulation of cardiac contractile function and energy metabolism (Hendgen-Cotta et al., 2010). This effect, known as short-term hibernation, leads to a dampening of high energy phosphates and oxygen consumption, and can potentially restore myocardial energy balance (Faassen et al., 2010; Heusch et al., 2005). Without an elevation of NO, ischemic conditions would lead to a depletion of NO which could exacerbate the condition by causing (or enhancing) vasoconstriction (Heusch et al., 2005; Trochu et al., 2000).

4.2. Model limitations

There are limitations to our model approach that could affect our predictions of NO bioavailability. We have assumed that the primary reactions involving Mb and NO are the $MbO₂$ scavenging reaction (Eq. 7) and the deoxyMb nitrite reduction reaction (Eq. 8). There are second-order reactions involving NO and other nitrogen oxide species and different states of Mb (oxyMb, metMb, and deoxyMb) that could affect nitrite-NO interactions which we have not included in our model, but should have less significant effects than the deoxyMb nitrite reduction pathway (Eich et al., 1996; Flögel et al., 2010). There is uncertainty regarding the various parameters reported by experimental sources used in this model. Myoglobin concentrations and reaction rates have been primarily estimated in animal models due to experimental limitations in human studies (Rassaf et al., 2007; Totzeck et al., 2012a, 2012b). Human Mb is unique because it has $Cys¹¹⁰$, which has been shown to form S-nitroso-myoglobin (S-NO-Mb) during nitrite reduction and extend the lifetime of nitritederived NO (Rayner et al., 2005; Witting et al., 2001). This pathway has been hypothesized to enhance the transport of NO produced by cardiac Mb but since it has not been fully elucidated, is not present in this model. Since released NO is scavenged by Mb but might be preserved by S-NO-Mb, our model provides a worst case scenario for Mb nitrite reduction during ischemia, and may underestimate the effect in humans. The sensitivity analysis (Fig. 8) shows that tissue nitrite concentration, Mb nitrite reduction reaction rate, $MbO₂$ scavenging of NO, and Mb P_{50} have a strong influence on the released NO from tissue nitrite. All of these factors impact the O_2 saturation of myoglobin, which significantly affects nitrite-released NO.

We have also constructed our model with independent flow and blood $PO₂$ input parameters, but these two conditions would be linked in vivo. We (Chen, 2006; Chen et al., 2011; Lamkin-Kennard et al., 2004) and others (Kavdia et al., 2002; Tsoukias et al., 2004) have examined the dynamics of red blood cell profiles, flow, and blood oxygen in the microcirculation through mathematical modeling, and incorporating these mechanisms is an area of potential future study. Models of oxygen transport in more complex microcirculatory networks, which could more fully characterize the interactions of microvascular hypoxia, blood flow, and O₂ transport, have been reviewed by Goldman (Goldman, 2008). However, NO transport and hypoxic nitrite production in these networks has not been as extensively modeled. We have previously studied coupled oxygen and NO transport in paired arteriolevenule (Chen et al., 2007) and branching microcirculation environments (Chen et al., 2011), and plan to incorporate Mb nitrite reduction to extend these models. Infused nitrite into the bloodstream releasing NO has also been shown to have cytoprotective and vasodilatory effects, although the mechanism is not fully understood (Liu et al., 2015; Lundberg et al., 2008). Our model also does not simulate O_2 consumption as a function of contractile activity, which has been postulated to be part of the cytoprotective effects of cardiac nitrite reduction (Flögel et al., 2010; Heusch et al., 2005). Recently, low-dosages (physiological levels) of nitrite infused into the bloodstream have been shown to reduce the effects of myocardial infarction, which is a phenomena that could be added to the model for future study (Ingram et al., 2013). In addition, reactive oxygen and nitrogen species have a significant effect on ischemic damage and ischemia/reperfusion injury, and mathematical modeling of the role of Mb nitrite reduction in these complex reactions is another area of

potential study (Kavdia, 2006; Powers et al., 2014). There are also numerous other nitrite reductase pathways that have been identified as significantly active under hypoxic or ischemic conditions, and would likely add to the magnitude of the effects predicted here. These pathways include proteins such as xanthine oxidoreductase, cytochrome P_{450} , and aldehyde oxidase (Faassen et al., 2010; Li et al., 2008). These other pathways have been shown to be effective in producing nitrite-derived NO in different organs and muscle vessels of the body depending on their enzyme compositions, including the heart (Zweier et al., 2010). Modeling these other tissue nitrite mechanisms is an area of potential future analysis. However, the deoxyMb nitrite reduction pathway alone has been shown be significant in elevating NO (Totzeck et al., 2012b).

4.3. Conclusion

Our mathematical model illustrates that while cardiac myoglobin serves as a strong scavenger of NO during normal conditions of flow or blood $PO₂$, the deoxyMb nitrite reduction pathway can have a significant physiological effect on NO production during ischemic conditions. This effect is most pronounced at the lowest blood $PO₂$ and tissue pH conditions and in some cases results in SMC and tissue NO above the normoxic levels. NO elevation is consistent at different flow rates, but relatively higher at lower flow due to the decreased baseline NO. Since we have demonstrated that cardiac tissue nitrite-derived NO can be significant, an important area of potential future study is modeling the in vivo observation that nitrite-derived NO can reduce cellular respiration and cardiac tissue oxygen consumption. Nevertheless, our results support experimental observations of the effectiveness of myoglobin nitrite reductase in releasing NO in the cardiac muscle during ischemic events and provide insight into mechanisms by which myocardial nitrite reduces myocardial infarction injury.

Acknowledgments

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Highlights

- **•** In normoxia, oxygenated Mb is a strong scavenger of NO to maintain homeostasis.
- **•** During ischemia, deoxygenated Mb can significantly generate NO from tissue nitrite.
- NO elevation is highest at the lowest blood PO₂ and tissue pH conditions.
- This effect is consistent at different flow rates, but relatively higher at low flow.
- **•** This released NO could be responsible for mitigating deleterious ischemic effects.

Figure 1.

Schematic diagram of a radially concentric cylindrical model of a small cardiac arteriole and perivascular tissue. The layer radii are: (1) 13 μm, (2) 1 μm, (3) 1 μm, (4) 10 μm, and (5) 105 μm.

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Figure 2.

Effect of blood PO2 changes on (**A**) PO2 profiles across the arteriolar radius and (**B**) myoglobin oxygen binding. (Inset) Average tissue $PO₂$ on the perivascular tissue region (25 $\langle r < 130 \text{ }\mu\text{m} \rangle$ for various blood PO₂ concentrations. The vertical dashed lines mark boundaries between the five radial model layers labeled above the graph.

Figure 3.

NO concentration profiles across the computational domain for various blood $PO₂$ concentrations (indicated next to the corresponding peak) without cardiac nitrite. The vertical dashed lines mark boundaries between the five radial model layers labeled above the graph.

Figure 4.

Average NO concentration in the smooth muscle cell region ($15 < r < 25 \mu m$) as a function of blood PO₂ concentrations without cardiac nitrite for various blood flow rates. Blood flow is varied from maximum centerline velocities of 1000 to 10 μ m s⁻¹. There is no significant difference between different tissue pH values on these data.

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between the five radial model layers labeled above the graph.

Figure 5.

Effect of deoxyMb nitrite reductase on NO concentrations across the computational domain at low blood PO_2 values (A) 1 Torr and (B) 10 Torr at pH values of 6.85, 6, and 5.5. The baseline NO profile is the condition with zero tissue nitrite (as in Fig. 3). The vertical dashed lines mark boundaries between the five radial model layers labeled above the graph.

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Figure 6.

Effect of myocardial tissue nitrite reductase on average NO concentration in the smooth muscle cell region ($15 < r < 25 \mu m$) as a function of blood PO₂ for tissue pH values of (A) 6.85 and (\bf{B}) 5.5. The higher section of blood PO₂ is omitted because the change in average SMC NO between blood PO_2 values of 35 and 120 Torr is <1 nM.

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Figure 7.

Effect of myocardial deoxyMb nitrite reductase on average NO concentration as a function of blood PO2 compared against the baseline no nitrite values in (**A**) the smooth muscle region ($15 < r < 25 \mu m$) and (**B**) the perivascular tissue region ($25 < r < 130 \mu m$) for tissue pH values of 6.85, 6, and 5.5. There is no significant difference in these data at different flow values. The higher section of blood $PO₂$ is omitted because the average SMC NO between blood PO_2 values of 20 and 120 Torr is <1 nM.

Figure 8.

Sensitivity analysis showing the effect of minor variations $(\pm 5\%)$ in model parameters (listed at right) on relative differences in average NO in the smooth muscle cell region (15 < $r < 25 \mu m$) for blood PO₂ = 1 Torr and baseline flow and pH.

NO concentrations below 1 pM are reported as zero NO concentrations below 1 pM are reported as zero