

*Article*



# **A Dynamic Multi-Projection-Contour Approximating Framework for the 3D Reconstruction of Buildings by Super-Generalized Optical Stereo-Pairs**

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**Abstract:** In this paper, a novel framework of the 3D reconstruction of buildings is proposed, focusing on remote sensing super-generalized stereo-pairs (SGSPs). As we all know, 3D reconstruction cannot be well performed using nonstandard stereo pairs, since reliable stereo matching could not be achieved when the image-pairs are collected at a great difference of views, and we always failed to obtain dense 3D points for regions of buildings, and cannot do further 3D shape reconstruction. We defined SGSPs as two or more optical images collected in less constrained views but covering the same buildings. It is even more difficult to reconstruct the 3D shape of a building by SGSPs using traditional frameworks. As a result, a dynamic multi-projection-contour approximating (DMPCA) framework was introduced for SGSP-based 3D reconstruction. The key idea is that we do an optimization to find a group of parameters of a simulated 3D model and use a binary feature-image that minimizes the total differences between projection-contours of the building in the SGSPs and that in the simulated 3D model. Then, the simulated 3D model, defined by the group of parameters, could approximate the actual 3D shape of the building. Certain parameterized 3D basic-unit-models of typical buildings were designed, and a simulated projection system was established to obtain a simulated projection-contour in different views. Moreover, the artificial bee colony algorithm was employed to solve the optimization. With SGSPs collected by the satellite and our unmanned aerial vehicle, the DMPCA framework was verified by a group of experiments, which demonstrated the reliability and advantages of this work.

**Keywords:**remote sensing; 3D reconstruction; super-generalized stereo-pairs; artificial bee colony algorithm

### **1. Introduction**

In recent years, there has been a dramatic proliferation of research concerned with three dimensional (3D) reconstruction of buildings by remote sensing resources. Data collected by different sensors could be used finishing this work, like optical images [\[1\]](#page-10-0), synthetic aperture radar (SAR) [\[2\]](#page-10-1), and light detection and ranging (LiDAR) [\[3\]](#page-10-2). There are also some multi-data source and multi-sensor approaches [\[4](#page-10-3)[,5\]](#page-10-4). Although higher precision 3D points of a city area can be obtained by LiDAR, it is an inadequate resource for certain applications, such as rescue and anti-terrorism reconnaissance. Undisputedly, optical images are the most adequate remote sensing resources. Super-generalized stereo-pairs (SGSPs) can be defined as two or more optical images, which have overlapping coverage areas and might have different resolutions, collected by the same or different sensors at diverse times and views. As we all know, a classic 3D reconstruction framework is based on stereo-pairs collected by spaceborne or airborne  $[6,7]$  $[6,7]$ . These stereo-pairs are required to satisfy certain restrictions (convergence angle, base-to-height ratio, etc.) to perform better stereo matching and calculation

of 3D coordinates [\[8\]](#page-11-0). However, SGSPs might not afford these restrictions, and stereo matching is undoubtedly the technical bottleneck when doing 3D reconstruction by SGSPs [\[9,](#page-11-1)[10\]](#page-11-2). People always failed to generate digital elevation/surface model of regions of buildings, and cannot do further 3D shape modeling for the buildings. Although some gradually developing products, like smart 3D and Street Factory, generate dense 3D point clouds using state-of-the-art pixel-based multi-stereo image matching [\[11\]](#page-11-3), an amount of manual correction is needed to enhance the geometric detail of 3D building models. In other words, the 3D reconstruction of buildings, using SGSPs, cannot be well achieved by traditional frameworks.  $\frac{1}{2}$  between  $\frac{1}{2}$  building models. In other words, using the 3D reconstruction of buildings, using  $\frac{1}{2}$  reconstruction of buildings, using  $\frac{1}{2}$  reconstruction of buildings, using  $\frac{1}{2}$  reconstructi

Here, we introduce a dynamic multi-projection-contour approximating (DMPCA) framework to reconstruct the 3D shape of buildings using SGSPs. to reconstruct the 3D shape of buildings using SGSPs.  $\frac{H}{\sqrt{2}}$  is a dynamic multi-produce a dynamic multi-produce and  $\frac{H}{\sqrt{2}}$  (DMPCA) framework fr

## **2. The Dynamic Multi-Projection-Contour Approximating Framework 2. The Dynamic Multi-Projection-Contour Approximating Framework**

The main framework of DMPCA is shown in Figure [1.](#page-1-0) The key idea is that in each of the specific views of SGSPs, we approximate the projection-contour of the building in the optical images by the projection-contour of a simulated 3D model of that building. Specifically, we establish an optimization to find a group of parameters of a simulated 3D model. It minimizes the total differences between projection-contour of a building in SGSPs and projection-contours of the simulated differences between projection-contour of a building in SGSPs and projection-contours of the simulated 3D model. Then, the simulated 3D model, defined by the optimized parameters, dynamically approximate the actual 3D shape of the building. there he building projection-contour of a building in SGSPs and projection-contours of the simulation-

<span id="page-1-0"></span>

**Figure 1.** The 3D reconstruction of a building based on a framework of dynamic **Figure 1.** The 3D reconstruction of a building based on a framework of dynamic multi-projection- $\frac{1}{2}$  contour approximating.

The work here is based on the hypothesis as expressed in Equation (1). Assume that a The work here is based on the hypothesis as expressed in Equation (1). Assume that a simulated 3D shape  $S_{sim}$  is close to the actual 3D shape of building  $S_{true}$ , when two or more projection-contours (PC)  $PC_{SGSPs}$  from actual images are approximated by the corresponding  $PC_{sim}$  (N is the number of images of SGSPs;  $PC_{SGSP}$  is the projection-contour of the building after imaging;  $PC_{sim}$  is the projection-contour of the building generated by  $S_{sim}$ ).

$$
S_{sim} \rightarrow S_{true}, when \qquad PC_{sim\_j} \rightarrow PC_{SGSP\_j} \qquad (1)
$$

$$
\min \quad f(\Phi_{SGSP\_j}, \Phi_{sim\_j}(\xi)) \ \ j = 1, 2, \dots, N
$$
\n
$$
\xi = \{\xi_{model}, \xi_{view\_j}\}\tag{2}
$$

We performed the optimization as expressed in Equation (2). *ΦSGSP\_j* is a feature image after We performed the optimization as expressed in Equation (2). *ΦSGSP\_j* is a feature image after binary and cutting processing of *PCSGSP\_j*. The cutting area is the minimum enclosing rectangle binary and cutting processing of *PCSGSP\_j*. The cutting area is the minimum enclosing rectangle (MER) of the projection-contour of the building. Meanwhile,  $\Phi_{sim-j}(\xi)$  is the simulated feature image after binary and cutting processing of *PCsim\_j*(*ξ*), which need to be generated from the dynamic simulated 3D model, cut by the MER of the projection-contour of building, and resampled to the same size as the corresponding  $Φ$ <sub>*SGSP\_j*</sub>.

Elements of  $\zeta$  are divided into two parts: (1) parameters of the simulated 3D basic-unit-models ξ<sub>*model*</sub>, such as length, width, and height, which define the structure of buildings; and (2) parameters of the view  $\xi_{view\_j} = \{Azimuth_{j}, Pitch_{j}\}$ , which are the imaging angle of the *j*-th image of SGSPs, defined as in Figure [1.](#page-1-0) If  $\xi_{view\_j}$  values are known, it can be preset. Moreover, if one or more Azimuth<sub>\_j</sub> and  $Pitch_{\_}$  are roughly known, we need to initial values of  $\zeta_{view\_j}$ , and optimize them to find the matching view of the corresponding SGSP for more precise generation of *Φsim\_<sup>j</sup>* (*ξ*). find the matching view of the corresponding SGSP for more precise generation of *Φsim\_j*(*ξ*). Azimuth*\_j* and Pitch*\_j* are roughly known, we need to initial values of *ξview\_j*, and optimize them to

The difference between each  $\Phi_{SGSP\_j}$  and the dynamic  $\Phi_{sim-j}(\xi)$  need to be compared whenever the parameter-vector  $\xi$  changed, and obtain the objective function  $f(\Phi_{SGSP\_j},\Phi_{sim-j}(\xi))$ . An optimized algorithm is employed to search  $\xi_{best}$  by iteration, and then use  $\xi_{model}$  of  $\xi_{best}$  to reconstruct the 3D shape of the building. shape of the building.

## *2.1. Parameterized 3D Simulated Models and Projection 2.1. Parameterized 3D Simulated Models and Projection*

To obtain the dynamic  $\Phi_{sim-j}(\xi)$ , groups of parameterized 3D models are needed. Inspired by [\[12\]](#page-11-4), some typical parameterized 3D basic-unit-models were designed that could fit most cases of ridge some typical parameterized 3D basic-unit-models were designed that could fit most cases of ridge buildings, as shown in Figure 2. Expressed by Equation (3), it is a universal model for these types of buildings, as shown in Figur[e 2](#page-2-0). Expressed by Equation (3), it is a universal model for these types of buildings. The basic-unit-model could be expanded to fit different applications if necessary. buildings. The basic-unit-model could be expanded to fit different applications if necessary.

$$
F(\xi_{model}) = F(w, l, \eta_1, \eta_2, \eta_3, \eta_4, H_g, H_c).
$$
\n(3)

<span id="page-2-0"></span>

**Figure 2.** Typical basic-unit-models.

Commonly, a simple 3D shape can be described using these basic-unit-models. A complex 3D shape needs to be described by a group of basic-unit-models in a certain topological initial state. *ξmodel* = {*ξb\_i*}, *i* = 1, 2, 3, . . . , *K*, *K* is a number of basic-unit-models.

With the parameterized 3D model, we set the entire model *ξmodel* at the center of the simulated 3D coordinate system. Then, the projection-image of the 3D model of any view could be simulated by Equation (4), using some integrated functions of 3D visualization according to the simulated imaging model *V*. For aerial images, the perspective projection model is employed, and a generalized model, such as the rational function model (RFM), is used for satellite images. Whenever the parameter *ξ* is changed, the 3D model on the screen is shown by the 3D visualization functions, and the screenshots are saved as the simulated projection.

$$
PC_{sim\_j}(\xi) = V(M(\xi_{model}), \xi_{view\_j}).
$$
\n(4)

#### *2.2. Dynamic Multi-Projection-Contour Approximating by an Artificial Bee Colony Algorithm*

In both *PCSGSP* and *PCsim*, the building areas are set to 1, while other parts are set to 0. We then cut the *MER* to obtain *ΦSGSP\_j* and *Φsim\_<sup>j</sup>* (*ξ*). *Φsim\_<sup>j</sup>* (*ξ*) is then resampled to the same size as *ΦSGSP\_j*, and Equation (5) is employed as an objective function. Similarity  $S_{\check{O}}$  or normalized similarity  $\hat{S}_{\check{O}}$  can be used to define the similarity between all *ΦSGSP\_j* and *Φsim\_<sup>j</sup>* (*ξ*) values, as expressed in Equation (6). Then, an artificial bee colony (ABC) algorithm can be employed to resolve the optimization.

The artificial bee colony algorithm groups the bee colony into three roles: employed bees (EB), onlooker bees (OB), and scout bees (SB), which are also the three phases of the algorithm. The main process is as follows:

$$
f = -S_{\Phi}(\Phi_{SGSP\_j}, \Phi_{sim\_j}(\xi))
$$
  
\n
$$
\xi = {\xi_{model}, \xi_{view\_j}} = {\{w_i, l_i, \eta_{i1}, \eta_{i2}, \eta_{i3}, \eta_{i4}, H_{ig}, H_{ic}, Azimuth_{\_,j}, Pitch_{\_,j}\}}
$$
\n(5)

$$
S_{\Phi} = \sqrt{\sum_{j=1}^{N} \left( \frac{\Phi_{SGSP\_j} \& \Phi_{sim\_j}(\xi)}{\Phi_{SGSP\_j} | \Phi_{sim\_j}(\xi)} \right)^2} \quad or \quad \hat{S}_{\Phi} = \frac{1}{N} \sqrt{\sum_{j=1}^{N} \left( \frac{\Phi_{SGSP\_j} \& \Phi_{sim\_j}(\xi)}{\Phi_{SGSP\_j} | \Phi_{sim\_j}(\xi)} \right)^2} \quad . \tag{6}
$$

#### (1) Parameter Initialization of the ABC Algorithm

Population number (*PN*), dimension of *ξ* (*D*), triggering threshold of scout bee (*TTSB*), maximum cycle number (*MCN*), or ideal fitness threshold (*IFT*) can be set for termination.

(2) Initialization of Solutions

The solution vector *ξ* is composed by all parameters to be optimized. Initiate *PN*/2 solutions *ξm*(*n*) (*m* = 1, 2, . . . , *PN*/2, *n* = 1, 2, . . . , *D*) randomly according to predefined logical ranges for each element of *ξ*. *PN*/2 failure counters *FC<sup>m</sup>* are reset for each solution.

- (3) Iteration and Modify all *PN*/2 Solutions
	- 1) The EB phase. Each EB corresponds to a solution. Each solution *ξm*(*n*) is modified by Equation (7), where  $\xi_k(n)$  is another solution in the *PN*/2 solutions,  $\lambda_m(n)$ ~U[−1, 1].

$$
\overline{\xi}_m(n) = \xi_m(n) + \lambda_m(n) \cdot (\xi_m(n) - \xi_k(n)). \tag{7}
$$

To improve the efficiency of the optimization, instead of modifying one element randomly in the original algorithm, all *D* elements of  $\zeta_m$  are modified.  $f(\zeta_m)$  and  $f(\overline{\zeta}_m)$  are compared, and the better one is reserved to update the solution of this EB. The *FC<sup>m</sup>* will add one if  $f(\xi_m) > f(\overline{\xi}_m)$ ; otherwise, it remains unchanged.

2) The recruiting probability of each EB is estimated using Equation (8).

$$
prob(m) = f(\xi_m) / \sum_{m=1}^{PN/2} f(\xi_m).
$$
 (8)

- 3) The OB phase: OB optimizes the solution found by the EB it follows. Each OB follows one EB according to recruiting probability, and the solution of that EB is modified. 1 *m* . Since better solutions having greater recruiting probability, they can be optimized more times. The modification is the same as the EB phase.
- 4) The best solution  $\xi_{best}$  is recorded. All the updated  $PN/2$  solutions are ranked according to their fitness, and  $ξ_{best}$  is recorded. Then, if the algorithm comes to the MCN or  $f(ξ_{best})$ reaches IFT, it ends.  $\xi_{model}$  of the  $\xi_{best}$  is chosen for further reconstruction.
- 5) The SB phase: SB is triggered only if  $FC_m$  reaches TTSB, the corresponding solution is *reached and a new solution will be randomly generated and the original one replaced.*  $\frac{1}{2}$  the SB phase  $\frac{1}{2}$  is the SB phase. The securities in  $\frac{1}{2}$  solution is the corresponding solution is the corresponding solution is the corresponding solution is the corresponding solution is the correspo

#### **3. Experiments** abandoned, and a new solution will be randomly generated and the original one replaced.

In the experiments, the same ABC parameters are used to fairly test the performance of the DMPCA in different SGSP cases. The programs were run in MATLAB 2015, and the computer is with Interl(R)  $\text{Core(TM)}$  i5-6200 2.3GHz and 8G RAM. Considering the computing ability and time-consuming problem, the main parameters of the ABC algorithm were set as  $PN = 10$ , *TTSB* = 50,  $\alpha = 100$ .

#### *3.1. An Analysis of 3D Reconstruction by DMPCA Using Simulated SGSPs*

Firstly, we intended to find the relationship between similarity  $S_{\check{O}}$  and the precision of firstly, we intended to find the reconstruction.

Since imaging angles of the actual remote sensor cannot be precisely controlled, we picked three typical buildings with different 3D shapes, as shown in Figure 3 and Table [1,](#page-4-1) and simulated their SGSPs with accurate imaging angles, as shown in Table [2.](#page-5-0) The resolution of the SGSPs is 1 m/pixel. For convenience, azimuth and pitch angles are defined according to the center of the buildings, as shown in the bottom-right section of Figure [1.](#page-1-0)  $\delta$  shown in the bottom-right section of  $\delta$ 

<span id="page-4-0"></span>

<span id="page-4-1"></span>**Figure 3.** Typical simulated 3D buildings. (**a**–**c**) are three single buildings with different roofs; (**d**) is a **Figure 3.** Typical simulated 3D buildings. (a–c) are three single buildings with different roofs; (**d**) is a combined one.

	W	$\eta_1$	$\eta_2$	$\eta_3$	η4	$H_G$	$H_C$
50	30	0	0	0	0	30	0
50	30	15	15	0	0	30	10
50	30	15	15	25	0	30	10
50	20	10	10	10	10	20	5
50	20	10	10	10	10	20	5
40	20	10	10	10	10	20	5

**Table 1.** Typical buildings (unit: m).

<span id="page-5-0"></span>

	Form of View: (Azimuth <sub>SGSP</sub> , Pitch <sub>SGSP</sub> )			
(0, 30)	(0, 45)	(0, 60)	(0, 75)	(0, 90)
(30, 30)	(30, 45)	(30, 60)	(30, 75)	(30, 90)
(60, 30)	(60, 45)	(60, 60)	(60, 75)	(60, 90)
(90, 30)	(90, 45)	(90, 60)	(90, 75)	(90, 90)
Special:		(150, 45)		(225, 45)

Table 2. Views of simulated images (unit: °).

Due to the symmetry of the three buildings, we picked azimuth and pitch angles of 20 regular simulated images (RSI) in  $0\text{-}90^\circ$ , and two special simulated images (SSI) are (150 $^\circ$ , 45 $^\circ$ ) and (225 $^\circ$ , 45 $^\circ$ ). Then, we chose one SSI together with any RSI to constitute SGSPs for 3D reconstruction. We compared<br><sup>1</sup> the error of reconstruction by Equation (9), where NT is the number of testing points, and we compared the actual coordinate  $(X_n, Y_n, Z_n)$  with the estimated ones  $(\hat{X}_n, \hat{Y}_n, \hat{Z}_n)$ . We first tested the minimum requirements of similarity *SÖ* for different precisions of 3D

$$
PRE = \frac{1}{NT} \sum_{n=1}^{NT} \sqrt{(\hat{X}_n - X_n)^2 + (\hat{Y}_n - Y_n)^2 + (\hat{Z}_n - Z_n)^2}
$$
(9)

We first tested the minimum requirements of similarity  $S_{\breve{O}}$  for different precisions of 3D reconstruction by our DMPCA method. It can be seen in Figure [4a](#page-5-1),b that similarity  $S_{\bullet}$ , defined by the feature-image  $\Phi$ , can be an effective restriction of the 3D shape, and higher precision requires a larger  $S_{\ddot{\mathcal{O}}}$  from the trend for different SGSP combinations. Nevertheless, in the same precision, the requirements of  $S_{\ddot{O}}$  are different for different buildings, also for different cases of SGSPs. we first tested the minimum requirements of similarity  $s_{\tilde{O}}$  for different prec

<span id="page-5-1"></span>

**Figure 4.** "Precision" versus " $S_{\Phi}$ ". "Precision" is obtained by Equation (9) with all sampled points of the roof of the buildings. "Similarity" is the average minimum  $S_\Phi$  when reconstructed by different the roof of the buildings. "Similarity" is the average minimum  $S_\Phi$  when reconstructed by different SGSPs. (**a**) has the specific view (150°, 45°), while (**b)** has the specific view (225°, 45°). SGSPs. (**a**) has the specific view (150◦ , 45◦ ), while (**b)** has the specific view (225◦ , 45◦ ).

Two views were used in the experiments of B1~B3, and the three buildings are entirely symmetrical. Furthermore, B4 was used, which is not perfectly symmetrical but was a complex building. Then, the performance of DMPCA on B4 was tested in different combination cases of three different views;  $\overline{a}$ different views;

We focused on the effects of the azimuth spans of DMPCA, and the pitch angles of input images were fixed at  $45^\circ$ . Eleven views of B4 were used, as shown in Figure 5. First, the cases of equidistant azimuth spans were considered. The initial azimuth was set to  $0^{\circ}$ , and the azimuth spans between two adjoined images were set to five cases ( $0^\circ$ ,  $30^\circ$ ,  $45^\circ$ ,  $60^\circ$ ,  $90^\circ$ , and  $120^\circ$ ), so the combinations of azimuths of the five cases were as follows: 0-30-60, 0-45-90, 0-60-120, 0-90-180, and 0-120-240. The results after 100 iterations are shown in Table [3.](#page-6-1) It could be found that, in the case of equidistant azimuth spans, a larger azimuth span produces better precision.

<span id="page-6-0"></span>

<span id="page-6-1"></span>**Figure 5.** The simulated projections of B4 in different views.  $(180,45)$  (210,45) (210,45) (210,45) (270,45) (300,45) (300,45) (300,45) (300,45) (300,45) (300,45) (300,45)

**Table 3.** Performance of DMPCA on different cases of equidistant azimuth spans.

<b>Azimuth Spans</b>	Similarity	Precision (m)
$30^\circ$	0.815	1.73
$45^{\circ}$	0.822	1.66
$60^\circ$	0.841	1.56
$90^\circ$	0.872	1.37
$120^\circ$	0.923	1.07

Moreover, also in equidistant azimuth spans, two-view cases and four-view cases were tested, similar to the above three-view cases (note that, when using four views of the 120° azimuth span, two of the four were entirely overlapped; this input case is the same as the case using three views of the 120°, but the one redundancy image deduced the optimizing process and, compared with the case using three views, obtained a worse result). It was illustrated that three views are the better choice in equidistant azimuth spans, as shown in Figure [6.](#page-6-2) choice in equidistant azimuth spans, as shown in Figure 6.  $\frac{1}{100}$  case views, obtained a worse results in was illustrated that three views are the better chere.

<span id="page-6-2"></span>

Figure 6. Results of different number of views.  $t_{\rm s}$  in a 0° initial azimuth is no better than other cases of initial azimuth. The cases of initi

According to a number of experiments, it was found the initial azimuth also has certain effects on the results, since the results of a  $0°$  initial azimuth is no better than other cases of initial azimuth. The initial azimuth was then set to 60 $^{\circ}$ , and the cases of non-equidistant azimuth spans were tested. The views a[nd](#page-7-0) results are shown in Table 4, Figures  $7$  and  $8$ . After  $100$  iterations, the  $60$ -150-300 case obtained the highest value of similarity and precision. Moreover, it can be found that similarity and precision do not increase simultaneously. precision do not increase simultaneously.

<span id="page-7-0"></span>**Table 4.** The performance of DMPCA on different cases of non-equidistant azimuth spans. **Table 4.** The performance of DMPCA on different cases of non-equidistant azimuth spans.

<b>The Azimuths</b>	Similarity	Precision (m)
60-150-180	0.930	0.8400
$60 - 150 - 210$	0.961	0.4800
$60 - 150 - 240$	0.975	0.3000
60-150-270	0.976	0.2880
60-150-300	0.988	0.1440
60-180-210	0.948	0.526
60-180-240	0.969	0.512
60-180-270	0.973	0.5115
60-180-300	0.985	0.5085

<span id="page-7-1"></span>

**Figure 7.** The results of cases (60-150-X, 45) in 100 iterations. **Figure 7.** The results of cases (60-150-X, 45) in 100 iterations. **Figure 7.** The results of cases (60-150-X, 45) in 100 iterations.

<span id="page-7-2"></span>

**Figure 8.** The results of cases (60-180-X, 45) in 100 iterations.

It can be concluded from above that the complementarity of the azimuth is the most significant<br>wefthe DMPCA mathed factor of the DMPCA method.  $s_{\text{max}}$  in Figure 9, we collected a satellite image (SI) from a vendor and two aerial images (AI1, AI2) from a vendor and two aerial images (AI1, AI2) from a vendor and two aerial images (AI1, AI2) and two actions of  $\$ 

### 3.2. 3D Reconstruction by DMPCA Using Actual Remote Sensing SGSPs

We tried to reconstruct the main building of the Harbin institute of technology (HIT). As shown in Figure [9,](#page-8-0) we collected a satellite image (SI) from a vendor and two aerial images (AI1, AI2) by our unmanned aerial vehicle. It could be found that aerial images are oblique, while satellite images are nadir-looking. We tried to reconstruct the main building of the Harbin institute of technology (HIT). As show

<span id="page-8-0"></span>











**Figure 9.** SGSPs of the main building of HIT. (**a**,**b**) are two airborne images, the resolution is about 0.4 m/pixel; (**c**) is a satellite image, the resolution is 2 m/pixel; (**d**) is the official display of the building. (**e**) is the schematic diagram of the initialized 27 topological units.

It could be found that aerial images are oblique, while satellite images are nadir-looking. Moreover, compared to AI2, SI and AI1 have similar azimuths. We combined them two by two and obtained three groups of SGSPs (SGSP1 = SI & AI1, SGSP2 = SI & AI2, SGSP3 = AI1 & AI2). Then, we reconstructed the building using the three groups of SGSPs, respectively.

The projection-contours of the building were extracted from each SGSPs using the image matting methods [13] and some manual correction. Since the building has a complex 3D shape, we initialized<br>it into 27 units  $(\xi_{t+1} = {\xi_t} \cdot \xi_{t+2})$  i = 1 2 27) as Figure 9e, including 25 outer-units and 2 inner-units it into 27 units ( $\xi_{model} = {\xi_{b\_i}}$ ,  $i = 1, 2, ..., 27$ ) as Figure [9e](#page-8-0), including 25 outer-units and 2 inner-units. For each basic unit, the horizontal parameters were resolved from the SI referring to the building extraction methods in [\[14\]](#page-11-6). Then, the height parameters of 27 basic-unit-models and view parameters extraction methods in [14]. Then, the height parameters of 27 basic-unit-models and view parameters<br>were collected to compose *ξ*. Note that we were approximating the projection-contour of the entire model of the building, not each single unit. Therefore, the objective function *f* in Equation (5) needs model of the building, not each single unit. Therefore, the objective function *f* in Equation (5) needs no no changes. were concluded to compose *ξ*. Note that we were approximating the projection-contour of the entire entire entire were collected to compose  $\xi$ . Note that we were approximating the projection-contour of the entire<br>model of the building, not each single unit. Therefore, the objective function f in Equation (5) need<br>no changes were collected to compute the component to component the projection of the projection of the projection-contour of the entire section of the projection-contour of the entire section of the entire section-contour of the ent model of the building, not each single unit. Therefore, the objective function *f* in Equation (5) needs no wordel of the building not each single unit. Therefore, the phierities function f in Equation (5) needs  $\frac{1}{\theta}$  the building, the objective function  $\frac{1}{\theta}$  in Equation (5) needs not function  $\frac{1}{\theta}$  in Equation (5) needs not function  $\frac{1}{\theta}$ were collected to compute the weight were approximate the protice of the contour of the projection  $(5)$  need model of the building, not each single unit. Therefore, the objective function *f* in Equation (5) needs no

According to the design diagram of this building, we collected the true-value of the top o the building. Each reconstructed unit was sampled into 0.1 *m* interval 3D points-cloud, and we selected building. Each reconstructed unit was sampled into 0.1 *m* interval 3D points-cloud, and we selected all the sampled points of the roof of building as testing points, to test the precision by Equation (9).<br>The contribution is the contribution of the contribution of the contribution of the contribution of the contri The results are shown in Table 5. According to the design diagram of this building, we concern the true-value of the top of building. Each reconstructed unit was sampled into 0.1 *m* interval 3D points-cloud, and we selected  $\frac{1}{2}$  and  $\frac{1}{2}$  are the constructed unit use consult into 0.1  $\mu$  is the set of the share of the constructed unit use consult into 0.1  $\mu$  is the set of the share of the colorinate of the state of the state of t building. Each reconstructed unit was sampled into 0.1 *m* interval 3D points-cloud, and we selected all the sampled points of the roof of building as testing points, to test the precision by Equation (9). changes. building. Each reconstructed unit was sampled into 0.1 *m* interval 3D points-cloud, and we selected unit was sampled into 0.1 *m* interval 3D points-cloud, and we selected unit was sampled into 0.1 *m* interval 3D pointsall the sampled points of the roof of building as testing points, to test the precision by Equation (9).



<span id="page-9-0"></span>**Table 5.** Reconstruction results obtained by different SGSPs. "Precision" is the mean PRE of the 27 basic-unit-models. Figures in the last column show the error of 3D reconstruction; the *x*-axis is the serial number of units, and the *y*-axis is PRE (unit: m). number of units, and the *y*-axis is PRE (unit: m).

The results revealed that, overall, 3D reconstruction of the building could be achieved by any of the testing cyclication of the SGSPs using our DMPCA. A larger support of the suppor hypothesis as a shown city is targer  $S_0$  produces better results, which support on reconstruction, since our since our since our since  $\rho_0$  is sufficient but not necessary for better  $\rho_0$ reconstruction, since our simulated perspective projection model cannot fit the actual imaging model perietry. The aerial 5351 5 with higher resolution produces better precision than 5351 1 and 5351 Particularly, although the precision of several units obtained by SGSP2 are poorer than that obtained by SGSP1, these units are in small proportion of the entire building, so SGSP2 obtained better mean The results revealed that, overall, 3D reconstruction of the building could be achieved by any of the three SGSPs using our DMPCA. A larger *SÖ* produces better results, which support our hypothesis as shown in Equation (1). In fact, a larger *SÖ* is sufficient but not necessary for better of the three SGSPs using our DMPCA. A larger *SÖ* produces better results, which support our hypothesis as shown in Equation (1). In fact, a larger *SÖ* is sufficient but not necessary for better reconstruction, since our simulated perspective projection model cannot fit the actual imaging projection since our simulated perspective projection, and  $\alpha$ The results revealed that, overall, 3D reconstruction of the building could be achieved by an<br>of the three SGSPs using our DMPCA. A larger  $S_{\bullet}$  produces better results, which support of<br>hypothesis as shown in Equation perfectly. The aerial SGSP3 with higher resolution produces better precision than SGSP1 and SGSP<br>Particularly, although the precision of several units obtained by SGSP2 are poorer than that obtaine of the three SGSPs using our DMPCA. A larger  $S_{\bullet}$  produces better results, which support our hypothesis as shown in Equation (1). In fact, a larger *SÖ* is sufficient but not necessary for better hypothesis as shown in Equation (1). In fact, a larger  $S_{\vec{O}}$  is sufficient but not necessary for better model in the actual imaging model perfectly. The aerial SGSP3 with higher resolution produces better precision than SGSP1 and SGSP2.<br>Particularly and that the contract of the contr precision than SGSP1. The only difference between SGSP1 and SGSP2 is the azimuth of AI1 and AI2. We think that this made SGSP2 a better complementarity with SI. This indicated that the precision of 3D reconstruction by our DMPCA framework mainly depends on the resolution and complementarity of the imaging angle of the SGSPs. Moreover, the precision of each unit, obtained by the respective SGSPs, is different. The inner-units could not be effectively restricted by the projection-contour, since there is only a little piece of part or none of the inner-units in the projection-contour. Thus, the precision of the inner-units cannot be guaranteed, which mostly depends on the pitch angle of the view. However, most of the outer-units have an ideal precision according to their inputting SGSPs.

#### **4. Discussion and Conclusions**

A dynamic multi-projection-contour approximating (DMPCA) framework was proposed in this paper. Using super-generalized stereo-pairs (SGSPs), the reconstruction of the 3D shape of a building was achieved, while traditional frameworks failed. In this framework, we resolved an optimization to find the best parameters of a certain group with a simulated 3D model, which minimizes differences between the projection-contour of a building in the actual optical images and that of the simulated 3D model. According to experiments, we found that the proposed similarity can well restrict the shape of the building. However, the similarity and precision do not increase simultaneously. There are two possible reasons: (1) our projection model is not absolutely consistent with the actual imaging model; (2) the optimizing algorithm did not find the best solution of the parameters. Moreover, the effect of azimuth spans on DMPCA were analyzed. In the equidistant azimuth spans cases, we found that a greater number of views will not produce a better result, and three views could be a suitable choice. In the non-equidistant azimuth spans cases, it was proved that the azimuth spans, which has better complementarity, can improve the performance of DMPCA, since they have better restriction of the shape. In the test of actual SGSPs, the precision of 3D reconstruction by our DMPCA mainly depends on the resolution and complementarity of the imaging angle of the SGSPs. A higher resolution and better complementarity of azimuth produce better precision.

Furthermore, to improve this work, a basic-unit-model could be better defined for greater application, and the optimized algorithm could be improved to enhance the performance.

**Author Contributions:** Y. Yan wrote the paper and conceived the main idea. N. Su designed the experiments and contributed analysis data and tools. C. Zhao and L. Wang gave advice for the main idea and the experiments. **Conflicts of Interest:** The authors declare no conflict of interest.

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