

# **HHS Public Access**

Author manuscript *Macromolecules.* Author manuscript; available in PMC 2017 October 11.

Published in final edited form as:

Macromolecules. 2017 March 28; 50(6): 2477-2483. doi:10.1021/acs.macromol.6b02571.

# Poly(ethylene glycol)s in Semidilute Regime: Radius of Gyration in the Bulk and Partitioning into a Nanopore

Philip A. Gurnev<sup>†</sup>, Christopher B. Stanley<sup>‡</sup>, M. Alphan Aksoyoglu<sup>||</sup>, Kunlun Hong<sup>§</sup>, V. Adrian Parsegian<sup>||</sup>, and Sergey M. Bezrukov<sup>\*,†</sup>

<sup>†</sup>Section on Molecular Transport, Eunice Kennedy Shriver National Institute of Child Health and Human Development, National Institutes of Health, Bethesda, Maryland 20892, United States

<sup>‡</sup>Biology and Soft Matter Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, United States

<sup>§</sup>Center for Nanophase Materials Sciences, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, United States

Department of Physics, University of Massachusetts Amherst, Amherst, Massachusetts 01003, United States

# Abstract

Using two approaches, small-angle neutron scattering (SANS) from bulk solutions and nanopore conductance-fluctuation analysis, we studied structural and dynamic features of poly(ethylene glycol) (PEG) water/salt solutions in the dilute and semidilute regimes. SANS measurements on PEG 3400 at the zero-average contrast yielded the single chain radius of gyration ( $R_g$ ) over 1–30 wt %. We observed a small but statistically reliable decrease in  $R_g$  with increasing PEG concentration: at 30 wt % the chain contracts by a factor of 0.94. Analyzing conductance fluctuations of the *a*-hemolysin nanopore in the mixtures of PEG 200 with PEG 3400, we demonstrated that polymer partitioning into the nanopore is mostly due to PEG 200. Specifically, for a 1:1 wt/wt mixture the smaller polymer dominates to the extent that only about 1/25 of the nanopore volume is taken by the larger polymer. These findings advance our conceptual and quantitative understanding of nanopore polymer partitioning; they also support the main assumptions of the recent "polymers-pushing-polymers" model.

# **Graphical Abstract**

\*Corresponding Author: (S.M.B.) bezrukos@mail.nih.gov. ORCID Philip A. Gurnev: 0000-0001-9247-5027 Kunlun Hong: 0000-0002-2852-5111 Notes The authors declare no competing financial interest.



# INTRODUCTION

Understanding polymer partitioning into nanoscale cavities of different nature is important for many technological applications that include, but are not limited to, analytical chromatography, separation techniques, and purification methods. It is also critical in the qualitative interpretation and quantitative analysis of molecular interactions and biological regulation in the crowded cellular environment. This necessitates model studies with polymer solutions explored in both dilute and semidilute regimes.

Some of the early experimental investigations on polymer confinement were conducted using Vycor glass as a nanoporous medium.<sup>1–3</sup> Small-angle neutron scattering (SANS) was used to determine the structure of solution phase polymers within the confined matrix and in the bulk. While the results were insightful, certain caveats were discovered with using Vycor.<sup>3</sup> For example, polymer adsorption to the pore walls has to be considered and may require chemical treatment to passivate the Vycor surface. Also, random pore geometries complicate the analysis. It was realized that having better defined pore geometries would greatly improve these experiments and serve to more robustly test and develop theoretical approaches.

During the past 30 years it became clear that certain biological channels provide welldefined nanopores for studying both polymer partitioning<sup>4-14</sup> and its osmotic action.<sup>15-17</sup> In addition, it was shown that conductance fluctuation analysis of single nanopores allows one to study the dynamic side of polymer partitioning, which offers advantages over ensemble techniques. To the best of our knowledge, the first experiments on polymer-induced noise in the nanopore current were reported for alamethicin channels interacting with differently sized poly(ethylene glycol)s (PEGs)<sup>18</sup> and then further advanced and extended to other biological nanopores.<sup>6,19–21</sup> Highly water-soluble and "soft" PEGs proved to be most popular in partitioning studies. In particular, it was demonstrated that under appropriate conditions PEG-induced single-molecular events<sup>10</sup> can be perfectly time-resolved<sup>22</sup> and used for PEG dispersion analysis at the submonomeric resolution.<sup>23-25</sup> An interesting latest development in this single-molecule technique relates to the unexpected temperature dependence of the lifetime of a single polymer molecule trapped by the *a*-hemolysin (aHL) nanopore.<sup>26</sup> It turned out that the temperature effect can be opposite for PEGs of different molecular weights. For the relatively small PEGs (molecular weight <2000) the time was found to exponentially decrease with temperature, while increasing for the larger PEGs (molecular weight 2000 and higher).

Recently,<sup>27</sup> polymer partitioning from semidilute solutions of PEG mixtures was studied with a number of membrane-spanning  $\beta$ -barrel channels of different origin: the voltagedependent anion channel (VDAC) from outer mitochondrial membrane, bacterial porin OmpC, and channel-forming toxin aHL. PEGs of molecular weight 200 (PEG 200) and 3400 (PEG 3400), and their mixtures in different proportions, were used. The results for the mixtures were rationalized within the earlier formulated "polymers-pushing-polymers" model of nanopore partitioning,<sup>28</sup> which is based on the assumptions that the larger component of the polymer mixture, being preferentially excluded from the cavity, pushes the smaller component into the cavity, thus representing forced polymer redistribution between the bulk and the channel. Here we study polymer mixtures by using two different methods— SANS and nanopore conductance fluctuation analysis-to quantify the larger polymer parameters in the bulk and the degree of its partitioning in the pore, respectively. We show that the reduction of the PEG 3400 characteristic size with its increasing concentration in the bulk is statistically significant but small. We also demonstrate that partitioning of the larger polymer in the nanopore is negligible, below 4%, if its relative weight fraction is kept smaller than 1/2, in excellent agreement with the major assumptions of the recent study.<sup>27</sup>

# **EXPERIMENTAL SECTION**

#### Materials

The synthesis of perdeuterated PEG of MW 3900 (dPEG 3900) was achieved using a custom-made glass reactor with constrictions and break-seal techniques under high-vacuum conditions. Potassium 2-(tetrahydropyranyloxy)ethanol was used as the initiator and tetrahydrofuran as the solvent. Details of the synthesis and characterization of the dPEG are similar to previously reported.<sup>29</sup> Deuterium oxide (Cambridge Isotope Laboratories, 99.9% D) was used without further purification. *Staphylococcus aureus* aHL, PEGs of MW 200 and 3400, KCl, and HEPES for nanopore experiments were purchased from Sigma, and diphytanoylphosphatidylcholine was from Avanti Polar Lipids. The buffered KCl solutions containing various wt % of PEG 200, PEG 3400, and their mixtures were prepared in double-distilled water.

#### Small-Angle Neutron Scattering

SANS experiments were performed on the extended *Q*-range small-angle neutron scattering (EQ-SANS, BL-6) beamline at the Spallation Neutron Source (SNS) at Oak Ridge National Laboratory (ORNL). In 60 Hz operation mode, a 2.5 m sample-to-detector distance with 2.5–6.46 Å wavelength band was used<sup>30</sup> to obtain the relevant wave-vector transfer,  $Q = 4\pi \sin(\theta)/\lambda$ , where  $2\theta$  is the scattering angle. Samples were loaded into 1 mm path-length circular-shaped quartz cuvettes (Hellma USA, Plainville, NY), and SANS measurements were performed at 25 °C. Data reduction followed standard procedures using MantidPlot.<sup>31</sup> The measured scattering intensity was corrected for the detector sensitivity and scattering contribution from the solvent and empty cells and then placed on absolute scale using a calibrated standard.<sup>32</sup>

PEG solutions for SANS were prepared in 5 mM HEPES (pH 7), 1 M KCl buffer, consistent with the single-channel experiments. The SANS zero-average contrast (ZAC) condition<sup>33</sup>

was used to obtain the single PEG chain conformation over the entire concentration series. Here the scattering intensity, I(Q), can be described by

$$I(Q) = [f_{\rm D} \Delta \rho_{\rm D}^2 + (1 - f_{\rm D}) \Delta \rho_{\rm H}^2] S_1(Q) + [f_{\rm D} \Delta \rho_{\rm D} + (1 - f_{\rm D}) \Delta \rho_{\rm H}]^2 S_2(Q)$$
(1)

where  $f_D$  is the fraction dPEG,  $\rho_D$  is the dPEG contrast with H<sub>2</sub>O/D<sub>2</sub>O solvent,  $\rho_H$  is the hydrogenated PEG (hPEG) contrast with H<sub>2</sub>O/D<sub>2</sub>O solvent,  $S_1(Q)$  is the intrachain scattering, and  $S_2(Q)$  is the interchain scattering. To nullify the  $S_2(Q)$  contribution, the second term in eq 1 was set to 0 by choosing  $f_D = 0.5$  (1:1 hPEG 3400:dPEG 3900) and then solving for the appropriate D<sub>2</sub>O percentage (= 63.3% D<sub>2</sub>O). Both hPEG and dPEG have a similar degree of polymerization (DP ~ 80), which is important for the ZAC method. PEG concentrations are reported as total wt % PEG (hPEG 3400 + dPEG 3900) for the ZAC experiments. SANS curves were fit to the Debye model for Gaussian polymer chains

$$I(Q) = I(0) \frac{2(e^{-x} + x - 1)}{x^2} \quad (2)$$

where the scattering intensity, I(Q), is described by the zero-angle scattering intensity, I(0), and  $x = Q^2 R_g^2$ , where  $R_g$  is the radius of gyration.

### **Nanopore Experiments**

Bilayer lipid membranes were prepared from diphytanoylphosphatidylcholine/pentane solution using the lipid monolayer-opposition technique on a circular aperture in a Teflon partition separating two compartments of an experimental cell.<sup>20</sup> PEGs and their mixtures were added to 1 M KCl aqueous solutions. Single membrane-spanning nanopores were formed by adding 25 µg/mL stock aHL solution directly to one of the compartments. Ion current measurements were performed with an Axopatch 200B amplifier (Molecular Devices, Eugene, OR) at room temperature (~24 °C). A pair of Ag/AgCl electrodes in 15% agarose/2 M KCl bridges was used to apply transmembrane voltages and to record ion currents. A positive potential of 100 mV was applied from the side opposite to aHL addition. The output signal of the amplifier was filtered by the amplifier built-in 10 kHz Bessel filter and in-line low-pass eight-pole Butterworth filter (Model 9002; Frequency Devices, Ottawa, IL) at 15 kHz and directly saved into computer memory with a sampling frequency of 50 kHz. Amplitude and fluctuation analyses were performed using ClampFit 10.2 (Molecular Devices) and Origin 9.1 software (OriginLab, Northampton, MA).

#### Viscosity

The kinematic viscosity,  $\nu$ , of PEG 200/PEG 3400 mixtures in 5 mM HEPES (pH 7), 1 M KCl buffer was measured in duplicate or triplicate using Cannon–Fenske viscometers. Using density,  $\rho$ , measurements with a standard balance, the dynamic viscosity  $\eta (= \nu \rho)$  was then calculated.

# **RESULTS AND DISCUSSION**

#### SANS: Chain Contraction in the Semidilute Regime

We first used SANS from bulk PEG solutions to evaluate polymer chain contraction with increasing polymer concentration. To accomplish this, we took advantage of the zeroaverage contrast (ZAC) condition for SANS,<sup>33</sup> where an optical theta condition is reached to cancel out intermolecular scattering contributions and yield only the single chain scattering independent of the PEG concentration. This method also was used in previous SANS studies on polymer structure in Vycor.<sup>1-3</sup> We achieved the ZAC condition for PEG by using 1:1 hPEG 3400:dPEG 3900 and 63.3% D<sub>2</sub>O (see Experimental Section) to unambiguously determine the single polymer chain conformation over the full concentration range measured. Importantly, the same buffered salt solution was used for SANS and the nanopore polymer partitioning experiments. The SANS curves and fits to the scattering as expected from a random coil (solid lines) are shown in Figure 1A for the PEG concentration series, from 1 to 30 wt %. As a control, the I(0) values obtained from the random coil fits were normalized by I(0) at c = 1 wt %, I(0,c)/I(0,1) wt %), to compare with the wt % concentration. The direct correlation demonstrated in Figure 1B verifies that  $S_2(Q)$  in eq 1 has no contribution with only single chain scattering detected. Since hPEG 3400 and dPEG 3900 have a similar DP, we simply refer to this 1:1 mixture as "PEG 3400" below.

Figure 1C shows that the PEG 3400  $R_g$  slightly decreases with increasing polymer concentration. A linear fit to the data provided the size extrapolated to infinite dilution,  $R_{g,0} = 21.0$  Å, which matches the value at 1 wt %. As the semidilute regime is approached,  $R_g$  decreases to 19.7 Å at 30 wt %. The SANS results here provide two main observations. First, they demonstrate that even at 1 M KCl bulk polymer behavior does not change significantly, as the polymer size at infinite dilution is close to the expected value based on its length and persistence length.<sup>34</sup> This seems to be an important finding, as interactions between PEG and salt are well documented.<sup>35</sup> Second, the decrease in polymer size with increasing polymer concentration, though statistically significant, is small at ~1.3 Å. The  $R_g$  ratio between 30 and 1 wt % is about 0.94.

Previous SANS measurements<sup>36</sup> on hydrogenated PEG 3400 in D<sub>2</sub>O found a similar dilute solution  $R_g$  but with a more pronounced decrease in the "apparent"  $R_g$  with increasing polymer concentration. Going from ~3 to 16 wt %, the reported  $R_g$  decreased by more than 10 Å. As the authors of ref 36 discuss, the reason for the stronger effect is that the measured "apparent"  $R_g$  is also influenced by the onset of interpolymer interactions ( $S_2(Q)$  in eq 1), causing the measured  $R_g$  value to appear to decrease with increasing concentration. However, it is difficult to separate out the individual PEG chain  $R_g$  since interpolymer scattering contributions can become dominant. The "apparent"  $R_g$  values in this previous SANS study therefore are informing on a characteristic correlation length within the PEG solutions. By using ZAC to nullify the  $S_2(Q)$  contribution in our SANS measurements, we show that the single PEG chain  $R_g$  does decrease, but the concentration effect is more subtle. This slight decrease in the size of individual PEG chains can be partially attributed to a decrease in water activity, which reduces the solvent quality for the PEG to favor a more

compact conformation. A similar effect is observed upon raising the temperature, where PEG 3400 collapses in size due to decreased solubility.<sup>26</sup>

### Nanopore Fluctuation Analysis: Predominant Small-Chain Partitioning into the Nanopore

One of the main assumptions of the polymers-pushing-polymers model used for the analysis of the forced PEG partitioning into nanopores<sup>27</sup> was that in a mixture of smaller and larger polymers, namely, PEG 200 and PEG 3400, it is predominantly the smaller polymer that fills the pore, up to the larger polymer weight fraction of 0.5. We now show that fluctuation analysis of pore conductance in the presence of polymer mixtures allows one to check this assumption experimentally. To achieve this goal, we use single transmembrane channels or water-filled pores formed by a-hemolysin<sup>37</sup> in planar lipid bilayers.

Figure 2A displays samples of the currents through the channels before and after addition of different PEG mixtures. It shows two effects of PEG on the current: PEG addition to the membrane-bathing 1 M KCl aqueous solution reduces pore conductance and changes the noise in the ion current. Both effects depend on the composition of the polymer mixture.

Figure 2B gives the relative channel conductance in PEG 200/PEG 3400 mixtures of different composition, in which the total monomeric concentration of PEG is held constant at the 30 wt % level at a varying relative fraction  $\chi$  of PEG 3400 in the mixture, defined as  $\chi = [PEG 3400]/([PEG 3400] + [PEG 200])$ , where square brackets stand for the weight concentration. Surprisingly, channel conductance displays a non-monotonic dependence on the relative fraction of PEG 3400. It first increases with the increasing fraction of the larger PEG in the mixture, but then, after this fraction reaches about 2/3 (corresponds to 20 wt % of PEG 3400), it starts to decrease. Using the language of conductance-derived partitioning,<sup>27</sup> this can be interpreted in the following way. Substitution of smaller PEG 200 by larger PEG 3400 first leads to a decrease in partitioning which is manifested by an increase in the conductance of the pore due the reduced pore occupancy by polymer. This is an expected behavior because of the extra entropic penalty of moving larger polymer into the nanopore; but then, surprisingly, with the fraction of the larger polymer increasing, the partitioning increases again.

Figure 2C shows the results of the spectral analysis of fluctuations in the currents through the a-hemolysin nanopore in the polymer-free solutions and in the presence of the PEG 200/PEG 3400 mixtures of different small vs large polymer proportions. It is immediately seen that while for the solutions enriched with PEG 200 the noise is barely different from that of the nanopore in the absence of polymers, for the ones enriched with PEG 3400 the polymer-induced noise is quite significant. The larger polymer induces a lot of current fluctuations while the smaller one does not.

Visual examination of the data suggests that at the relative fraction of PEG 3400 not greater than  $\chi = 1/2$  (corresponding to 15 wt % PEG 3400 in the bulk) the contribution of PEG 3400 to the partitioning is negligible. Indeed, the low-frequency spectral density of current fluctuations at this relative fraction is more than 2 orders of magnitude lower than it is in pure PEG 3400 solutions,  $\chi = 1$ . Assuming that this spectral parameter reports on the

presence of PEG 3400 in the nanopore, one may conclude that this larger polymer is practically excluded from the pore at  $\chi = 1/2$ .

To obtain quantitative estimates, we need to use the available analytical approaches. One of them, deemed to be most appropriate in our case, is based on the diffusion model of channel-facilitated transport.<sup>38</sup> For the fluctuations, which are induced by equilibrium exchange of nonconductive particles between the pore and the bulk, it gives the following expression for the spectral density of current noise  $S_{f}(f)$  as a function of frequency f.

$$S_I(f) = \langle N \rangle (\Delta G)^2 V^2 S(f)$$
 (3)

where  $\langle N \rangle$  is the average number of particles in the pore, *G* is the reduction in pore conductance due to entering of one particle, *V* is the applied voltage, and *S*(*f*) is the spectral density obtained from the normalized correlation function of the number of particles in the pore *C*(*t*):

$$S(f) = 4 \int_0^\infty C(t) \cos(2\pi f t) \,\mathrm{d}t \quad (4)$$

Solutions for C(t) demonstrate that the spectral density may have a quite complex frequency behavior,<sup>39</sup> which is determined by many parameters of the pore and pore/particle interactions. However, for the low-frequency spectral limit, S(0), and particle diffusional dynamics in a cylindrical pore, the expression is simplified to<sup>38</sup>

$$S(0) = \frac{L^2}{3D} \left( 1 + \frac{3\pi}{2} \frac{Da}{D_{\rm b}L} \right) \quad (5)$$

where *L* is the channel length, *a* is the channel radius, *D* is the particle diffusivity in the channel, and  $D_{\rm b}$  is the particle diffusivity in the bulk. Because for the pore in question  $L \gg a^{37}$  and  $D_{\rm b} \gg D_{\rm s}^{20}$  the last term in the brackets can be omitted, and we obtain the following:

$$S_{I}(0) = \langle N \rangle \frac{L^{2}}{3D} (\Delta G)^{2} V^{2}$$
 (6)

It is convenient to introduce the normalized fluctuation spectra by the following expression:

$$S_{\rm rel}(f) \equiv \frac{S_I(f)}{\langle G \rangle^2 V^2} \quad (7)$$

where  $\langle G \rangle$  is the average conductance of the nanopore. As a result, we have a simple expression:

$$S_{\rm rel}(0) = \langle N \rangle \frac{L^2}{3D} \left( \frac{\Delta G}{\langle G \rangle} \right)^2 \tag{8}$$

Experimentally obtained spectra transformed according to eq 7 are shown in Figure 3A. The values of  $S_{rel}(0)$ , defined as an average of the normalized spectra in Figure 3A over the 10–300 Hz range, are given in Figure 3B.

Now, these data and eq 8 allow us to quantify the relative population of PEG 3400 in the nanopore. Indeed, assuming that  $G/\langle G \rangle$ , the normalized change in conductance due to the entrance of one PEG 3400 molecule, does not change much for the studied mixtures and that the intrachannel diffusion coefficient scales with the mixture composition similarly to its bulk counterpart and is inversely proportional to viscosity, we can estimate the average number of PEG 3400 molecules in the pore. Their average number,  $\langle N(\chi) \rangle$ , as a function of polymer composition in the bulk,  $\chi$ , can be expressed through their average number in pure PEG 3400 solutions ( $\chi = 1$ ),  $\langle N(1) \rangle$ , as

$$\frac{\langle N(\chi) \rangle}{\langle N(1) \rangle} \simeq \frac{S_{\rm rel}(0)_{\chi}}{S_{\rm rel}(0)_{\chi=1}} \frac{\eta_{\rm p}(1)}{\eta_{\rm p}(\chi)} \tag{9}$$

where  $S_{\text{rel}}(0)_{\chi}$  and  $S_{\text{rel}}(0)_{\chi=1}$  are the low-frequency spectral densities of PEG 3400-induced fluctuations at the PEG 3400 relative fraction  $\chi$  and  $\chi = 1$ , respectively, and  $\eta_p(1)/\eta_p(\chi)$  is the ratio of mixture viscosities *in the pore* at PEG 3400 relative fraction *in the bulk* indicated as arguments. As it is suggested by the conductance data in Figure 2B, PEG 3400 practically equipartitions at  $\chi = 1$ , so that its content-dependent partitioning coefficient can be defined as  $p(\chi) = \langle N(\chi) \rangle / \langle N(1) \rangle$ .

According to eq 9, in order to obtain the partition coefficient from the noise data, we need to know the intrapore viscosity ratio. We deduce the intrapore viscosity from the data on bulk dynamic viscosity measurements. These are shown in Figure 3C inset and approximated by the solid line

$$\eta(\chi) = 3.20 + 8.31\chi + 5.72\chi^{1.96}$$
 (10)

drawn through the data points, assuming that the solution viscosity in the pore is proportional to the solution dynamic viscosity, eq 10, with the larger polymer relative fraction corrected for partitioning,  $\eta_p(p(\chi)) \propto \eta(p(\chi))$ . As a result, on the basis of eq 9, we arrive at

$$p(\chi) = \frac{S_{\rm rel}(0)_{\chi}}{S_{\rm rel}(0)_{\chi=1}} \frac{\eta(1)}{\eta(p(\chi))}$$
(11)

Solving eq 11 numerically, we obtain the values of  $p(\chi)$  shown in Figure 3C. The figure demonstrates that partitioning of PEG 3400 is highly composition-dependent. Indeed, at  $\chi = 0.5$  (1:1 PEG 3400:PEG 200 solutions) it is only about  $4 \times 10^{-2}$  relative to its value in pure PEG 3400 solutions ( $\chi = 1$ ) and at  $\chi = 0.33$  PEG 3400 partitioning drops to a fraction of one percent. Partitioning increases sharply, reaching unity at  $\chi = 1$  where only the larger polymer is in solution. Here PEG 3400 is pushed into the nanopore due to high solution nonideality; in the dilute regime its partitioning is negligible.<sup>27</sup> Interestingly, in the case of the PEG 200/PEG 3400 mixture, the increase in viscosity produced by PEG 3400 relative fraction increase from  $\chi = 0.5$  to  $\chi = 1$  (corresponding to PEG 3400 concentration of 15 and 30%, respectively) is about a factor of 2 (Figure 3 inset and eq 10). This is significantly smaller than the viscosity change for pure PEG 3400 solutions at these two concentrations interpolated from the data published previously.<sup>40</sup>

# CONCLUSIONS

Structural parameters in the bulk and dynamic partitioning into a nanopore of PEG 3400 water solutions in the presence of PEG 200 and 1 M potassium chloride salt were studied by SANS from bulk solutions and by analysis of nanopore conductance fluctuations, respectively. It was demonstrated that at the increasing fraction of PEG 3400 in the PEG 3400/ PEG 200 mixtures with the total monomeric concentration of PEG kept constant at 30 wt %, partitioning of the larger polymer into the *a*-hemolysin nanopore change. Increasing PEG 3400 concentration also leads to a decrease in the characteristic chain size. However, conclusions from both our analysis of the structural features and dynamic partitioning are in excellent accord with the major assumptions of the recently formulated polymers-pushing-polymers approach.<sup>27,28</sup> Indeed, the  $R_g$  of PEG 3400 reduces from 21.0 Å (extrapolated to infinite dilution) to 19.7 Å as the polymer concentration increases from 1 to 30 wt %. This is a statistically reliable (Figure 1C) but small effect.

Partitioning of PEG 3400 grows rapidly with  $\chi$  but is estimated as negligible, specifically,  $p(\chi) = 4 \times 10^{-2}$ , for the fraction of this polymer in the mixture as large as  $\chi = 0.5$  (Figure 3C). This level of partitioning means that in comparison to  $\chi = 1$  only 4% of the polymeraccessible volume of the pore is taken up by PEG 3400; the rest of the volume is filled by the smaller PEG 200. Taking into account the 17-fold difference in their molecular weight, we conclude that the ratio of the average number of small polymer molecules in the pore to that of the large ones exceeds 400 at this and smaller PEG 3400 relative fractions. With the increasing PEG 3400 fraction, the partitioning of this larger polymer starts to dominate. Quite unexpectedly, due to a significant nonideality at  $\chi = 1$ , this large polymer fills the *a*-hemolysis pore to nearly the same degree as pure PEG 200 at its 30% concentration (Figure 2B). This means that polymer–polymer repulsive interactions overcome the cost of its confinement by the pore.<sup>11,41</sup>

We believe that these findings are important for understanding and quantifying polymer behavior in the bulk and polymer partitioning into nanopores in dilute and semidilute regimes.

# Acknowledgments

The deuterated PEG was synthesized at the Center for Nanophase Materials Sciences, which is a DOE Office of Science User Facility. A portion of this research was performed at Oak Ridge National Laboratory's Spallation Neutron Source, sponsored by the U.S. Department of Energy, Office of Basic Energy Sciences. We acknowledge laboratory support by the Center for Structural Molecular Biology, funded by the Office of Biological and Environmental Research of the U.S. Department of Energy. P.A.G. and S.M.B. were supported by the Intramural Research Program of the National Institutes of Health (NIH), Eunice Kennedy Shriver National Institute of Child Health and Human Development.

# References

- Lal J, Sinha SK, Auvray L. Structure of polymer chains confined in Vycor. J Phys II. 1997; 7(11): 1597–1615.
- Gilbert EP, Auvray L, Lal J. Structure of polyelectrolyte chains confined in nanoporous glass. Macromolecules. 2001; 34(14):4942–4948.
- 3. Nieh MP, Kumar SK, Ho DL, Briber RM. Neutron scattering study of chain conformations in the energetically neutral pores of Vycor glass. Macromolecules. 2002; 35(16):6384–6391.
- Krasilnikov OV, Sabirov RZ, Ternovsky VI, Merzliak PG, Muratkhodjaev JN. A Simple Method for the Determination of the Pore Radius of Ion Channels in Planar Lipid Bilayer-Membranes. FEMS Microbiol Lett. 1992; 105(1–3):93–100.
- Sabirov RZ, Krasilnikov OV, Ternovsky VI, Merzliak PG. Relation between Ionic Channel Conductance and Conductivity of Media Containing Different Nonelectrolytes - a Novel Method of Pore-Size Determination. Gen Physiol Biophys. 1993; 12(2):95–111. [PubMed: 7691679]
- Bezrukov SM, Vodyanoy I. Probing Alamethicin Channels with Water-Soluble Polymers Effect on Conductance of Channel States. Biophys J. 1993; 64(1):16–25. [PubMed: 7679295]
- 7. Bezrukov SM, Kasianowicz JJ. The charge state of an ion channel controls neutral polymer entry into its pore. Eur Biophys J. 1997; 26(6):471–476. [PubMed: 9404007]
- Merzlyak PG, Yuldasheva LN, Rodrigues CG, Carneiro CMM, Krasilnikov OV, Bezrukov SM. Polymeric nonelectrolytes to probe pore geometry: Application to the alpha-toxin trans-membrane channel. Biophys J. 1999; 77(6):3023–3033. [PubMed: 10585924]
- 9. Rostovtseva TK, Nestorovich EM, Bezrukov SM. Partitioning of differently sized poly(ethylene glycol)s into OmpF porin. Biophys J. 2002; 82(1):160–169. [PubMed: 11751305]
- Movileanu L, Cheley S, Bayley H. Partitioning of individual flexible polymers into a nanoscopic protein pore. Biophys J. 2003; 85(2):897–910. [PubMed: 12885637]
- Krasilnikov OV, Bezrukov SM. Polymer partitioning from nonideal solutions into protein voids. Macromolecules. 2004; 37(7):2650–2657.
- Ostroumova OS, Gurnev PA, Schagina LV, Bezrukov SM. Asymmetry of syringomycin E channel studied by polymer partitioning. FEBS Lett. 2007; 581(5):804–808. [PubMed: 17289034]
- Gurnev PA, Rostovtseva TK, Bezrukov SM. Tubulin-blocked state of VDAC studied by polymer and ATP partitioning. FEBS Lett. 2011; 585(14):2363–2366. [PubMed: 21722638]
- Oukhaled AG, Biance AL, Pelta J, Auvray L, Bacri L. Transport of Long Neutral Polymers in the Semidilute Regime through a Protein Nanopore. Phys Rev Lett. 2012; 108(8):088104. [PubMed: 22463579]
- Zimmerberg J, Parsegian VA. Polymer Inaccessible Volume Changes during Opening and Closing of a Voltage-Dependent Ionic Channel. Nature. 1986; 323(6083):36–39. [PubMed: 2427958]
- Zimmerberg J, Bezanilla F, Parsegian VA. Solute Inaccessible Aqueous Volume Changes during Opening of the Potassium Channel of the Squid Giant-Axon. Biophys J. 1990; 57(5):1049–1064. [PubMed: 2340341]

- Vodyanoy I, Bezrukov SM, Parsegian VA. Probing Alamethicin Channels with Water-Soluble Polymers - Size-Modulated Osmotic Action. Biophys J. 1993; 65(5):2097–2105. [PubMed: 7507718]
- Bezrukov, SM., Vodyanoy, I. Electrical noise of the open alamethicin channel. In: Musha, T.Sato, S., Yamamoto, M., editors. International Conference on Noise in Physical Systems and 1/f Fluctuations; Kyoto, Japan. 1991; Kyoto, Japan: Ohmsha, Ltd; 1991. p. 641-644.
- Bezrukov SM, Vodyanoy I, Parsegian VA. Counting Polymers Moving through a Single-Ion Channel. Nature. 1994; 370(6487):279–281. [PubMed: 7518571]
- 20. Bezrukov SM, Vodyanoy I, Brutyan RA, Kasianowicz JJ. Dynamics and free energy of polymers partitioning into a nanoscale pore. Macromolecules. 1996; 29(26):8517–8522.
- Bezrukov SM, Krasilnikov OV, Yuldasheva LN, Berezhkovskii AM, Rodrigues CG. Fielddependent effect of crown ether (18-crown-6) on ionic conductance of alpha-hemolysin channels. Biophys J. 2004; 87(5):3162–3171. [PubMed: 15507690]
- Krasilnikov OV, Rodrigues CG, Bezrukov SM. Single polymer molecules in a protein nanopore in the limit of a strong polymer-pore attraction. Phys Rev Lett. 2006; 97(1):018301. [PubMed: 16907416]
- Robertson JWF, Rodrigues CG, Stanford VM, Rubinson KA, Krasilnikov OV, Kasianowicz JJ. Single-molecule mass spectrometry in solution using a solitary nanopore. Proc Natl Acad Sci U S A. 2007; 104(20):8207–8211. [PubMed: 17494764]
- Rodrigues CG, Machado DC, Chevtchenko SF, Krasilnikov OV. Mechanism of KCl Enhancement in Detection of Nonionic Polymers by Nanopore Sensors. Biophys J. 2008; 95(11):5186–5192. [PubMed: 18805926]
- 25. Baaken G, Halimeh I, Bacri L, Pelta J, Oukhaled A, Behrends JC. High-Resolution Size-Discrimination of Single Nonionic Synthetic Polymers with a Highly Charged Biological Nanopore. ACS Nano. 2015; 9(6):6443–6449. [PubMed: 26028280]
- 26. Piguet F, Ouldali H, Discala F, Breton MF, Behrends JC, Pelta J, Oukhaled A. High Temperature Extends the Range of Size Discrimination of Nonionic Polymers by a Biological Nanopore. Sci Rep. 2016; 6:38675. [PubMed: 27924860]
- Aksoyoglu MA, Podgornik R, Bezrukov SM, Gurnev PA, Muthukumar M, Parsegian VA. Sizedependent forced PEG partitioning into channels: VDAC, OmpC, and alpha-hemolysin. Proc Natl Acad Sci U S A. 2016; 113(32):9003–9008. [PubMed: 27466408]
- Podgornik R, Hopkins J, Parsegian VA, Muthukumar M. Polymers Pushing Polymers: Polymer Mixtures in Thermodynamic Equilibrium with a Pore. Macromolecules. 2012; 45(21):8921–8928. [PubMed: 23226877]
- 29. Pai SS, Hammouda B, Hong KL, Pozzo DC, Przybycien TM, Tilton RD. The Conformation of the Poly(ethylene glycol) Chain in Mono-PEGylated Lysozyme and Mono-PEGylated Human Growth Hormone. Bioconjugate Chem. 2011; 22(11):2317–2323.
- Zhao JK, Gao CY, Liu D. The extended Q-range small-angle neutron scattering diffractometer at the SNS. J Appl Crystallogr. 2010; 43:1068–1077.
- 31. Arnold O, Bilheux JC, Borreguero JM, Buts A, Campbell SI, Chapon L, Doucet M, Draper N, Leal RF, Gigg MA, Lynch VE, Markvardsen A, Mikkelson DJ, Mikkelson RL, Miller R, Palmen K, Parker P, Passos G, Perring TG, Peterson PF, Ren S, Reuter MA, Savici AT, Taylor JW, Taylor RJ, Tolchenov R, Zhou W, Zikovsky J. Mantid-Data analysis and visualization package for neutron scattering and mu SR experiments. Nucl Instrum Methods Phys Res Sect A. 2014; 764:156–166.
- 32. Wignall GD, Bates FS. Absolute Calibration of Small-Angle Neutron-Scattering Data. J Appl Crystallogr. 1987; 20:28–40.
- Benmouna M, Hammouda B. The zero average contrast condition: Theoretical predictions and experimental examples. Prog Polym Sci. 1997; 22(1):49–92.
- 34. Lopez-Esparza R, Guedeau-Boudeville MA, Gambin Y, Rodriguez-Beas C, Maldonado A, Urbach W. Interaction between poly(ethylene glycol) and two surfactants investigated by diffusion coefficient measurements. J Colloid Interface Sci. 2006; 300(1):105–110. [PubMed: 16678840]
- 35. Breton MF, Discala F, Bacri L, Foster D, Pelta J, Oukhaled A. Exploration of Neutral Versus Polyelectrolyte Behavior of Poly(ethylene glycol)s in Alkali Ion Solutions using Single-Nanopore Recording. J Phys Chem Lett. 2013; 4(13):2202–2208.

- Thiyagarajan P, Chaiko DJ, Hjelm RP. A Neutron-Scattering Study of Poly(Ethylene Glycol) in Electrolyte-Solutions. Macromolecules. 1995; 28(23):7730–7736.
- Song LZ, Hobaugh MR, Shustak C, Cheley S, Bayley H, Gouaux JE. Structure of staphylococcal alpha-hemolysin, a heptameric transmembrane pore. Science. 1996; 274(5294):1859–1866. [PubMed: 8943190]
- Bezrukov SM, Berezhkovskii AM, Pustovoit MA, Szabo A. Particle number fluctuations in a membrane channel. J Chem Phys. 2000; 113(18):8206–8211.
- 39. Berezhkovskii AM, Pustovoit MA, Bezrukov SM. Effect of binding on particle number fluctuations in a membrane channel. J Chem Phys. 2002; 116(14):6216–6220.
- 40. Stojilkovic KS, Berezhkovskii AM, Zitserman VY, Bezrukov SM. Conductivity and microviscosity of electrolyte solutions containing polyethylene glycols. J Chem Phys. 2003; 119(13):6973–6978.
- Zitserman VY, Berezhkovskii AM, Parsegian VA, Bezrukov SM. Nonideality of polymer solutions in the pore and concentration-dependent partitioning. J Chem Phys. 2005; 123(14):146101. [PubMed: 16238435]



#### Figure 1.

(A) SANS curves on 1:1 hPEG 3400:dPEG 3900 in 63.3% D<sub>2</sub>O buffer. The total PEG concentration was varied as 1, 3, 5, 10, 15, 20, and 30 wt % (with the lowest and highest wt % indicated). SANS curves were fit to the Debye equation (solid lines). (B) Normalized I(0) vs wt % PEG (solid diamonds) compared to the direct wt % vs wt % PEG correlation (dashed line). (C) PEG 3400 single chain radius of gyration  $R_g$  vs wt % determined using SANS at the ZAC point. A linear fit to the data (solid line) yields the equation  $R_g$  (Å) = 21.07–0.046 (wt %).



#### Figure 2.

(A) Traces of ionic currents through single aHL nanopores in lipid bilayers at different compositions of the polymer mixtures. The events of spontaneous assembly of nanopores are manifested as upward jumps in the current. Addition of polymers decreases the current due to their partitioning into the pore. It is also seen that the increasing concentration of PEG 3400 promotes excess fluctuations. Dashed line denotes zero current. Applied voltage was 100 mV. All traces were filtered by a low-pass filter with 10 kHz cutoff frequency. (B) Average conductance of the nanopore in the presence of 30 wt % PEG as a function of the relative fraction  $\chi$  of PEG 3400. As PEG 3400 fraction grows from  $\chi = 0$ , corresponding to pure PEG 200, to about  $\chi = 2/3$ , the conductance increases, reporting on a reduced polymer partitioning into the pore. Further increase in PEG 3400 content decreases conductance increasing partitioning. (C) Power spectral densities of ion current noise in the polymer-free and polymer-containing solutions of different relative fractions  $\chi$  of PEG 3400.



## Figure 3.

(A) Power spectral densities of Figure 2C normalized by pore average conductance according to eq 7. The normalization demonstrates that the relative conductance fluctuations are increased by polymer presence for all mixtures. (B) Low-frequency spectral density,  $S(0)_{\chi}$ , as a function of polymer mixture composition characterized by the relative fraction of PEG 3400,  $\chi$ . Pores in contact with solutions of the increasing PEG 3400 content display increasing noise intensities at  $\chi > 1/3$ . (C) PEG 3400 partition coefficient as a function of mixture composition calculated according to eq 11 using dynamic viscosity data shown in the inset.