



# Emergent chirality in the electric polarization texture of titanate superlattices

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Chirality is a geometrical property by which an object is not superimposable onto its mirror image, thereby imparting a handedness. Chirality determines many important properties in nature—from the strength of the weak interactions according to the electroweak theory in particle physics to the binding of enzymes with naturally occurring amino acids or sugars, reactions that are fundamental for life. In condensed matter physics, the prediction of topologically protected magnetic skyrmions and related spin textures in chiral magnets has stimulated significant research. If the magnetic dipoles were replaced by their electrical counterparts, then electrically controllable chiral devices could be designed. Complex oxide BaTiO<sub>3</sub>/SrTiO<sub>3</sub> nanocomposites and PbTiO<sub>3</sub>/SrTiO<sub>3</sub> superlattices are perfect candidates, since “polar vortices,” in which a continuous rotation of ferroelectric polarization spontaneously forms, have been recently discovered. Using resonant soft X-ray diffraction, we report the observation of a strong circular dichroism from the interaction between circularly polarized light and the chiral electric polarization texture that emerges in PbTiO<sub>3</sub>/SrTiO<sub>3</sub> superlattices. This hallmark of chirality is explained by a helical rotation of electric polarization that second-principles simulations predict to reside within complex 3D polarization textures comprising ordered topological line defects. The handedness of the texture can be topologically characterized by the sign of the helicity number of the chiral line defects. This coupling between the optical and novel polar properties could be exploited to encode chiral signatures into photon or electron beams for information processing.

chirality | electric polarization | topological textures | resonant soft X-ray diffraction | second-principles calculations

Superlattices composed of thin layers of ABO<sub>3</sub> perovskite oxides have attracted substantial interest in recent years because of the exotic phenomena that emerge (1–3) entirely from interfacial or confinement effects and the competition between various energies, leading to topological features such as vortex structures. Electric polarization vortices were theoretically predicted in BaTiO<sub>3</sub> quantum dots and nanowires (4), where the local dipoles continuously rotate to minimize depolarizing fields. Such rotational structures have recently been experimentally observed in PbTiO<sub>3</sub>/SrTiO<sub>3</sub> superlattices (5), an intensively studied system since the emergence of improper ferroelectricity in short-period superlattices (6). The so-called “polar vortex” phase is characterized by the spontaneous formation of tube-like textures with laterally alternating clockwise and counterclockwise rotations of electric polarization (7). Such a polar configuration would be potentially chiral (8, 9) with natural optical activity (10) if additional symmetry lowering were permitted.

We have discovered that the polar textures in PbTiO<sub>3</sub>/SrTiO<sub>3</sub> superlattices indeed exhibit emergent chirality, the fingerprints of which are imprinted onto its interactions with polarized light. Here, chirality of the polar textures is observed as circular dichroism in the

resonant soft X-ray diffraction (RSXD) pattern, i.e., as the difference in diffracted intensities when the circular polarization of incident X-rays is reversed. Atomistic simulations of the superlattices reveal a complex energy surface. The symmetry of some atomic configurations is lowered to a chiral structure, directly related to the appearance of an antiparallel axial polarization at the cores of neighboring polar tubes, which is consistent with the experimentally observed circular dichroism. Within this framework of chiral polarization tubes, these axially polarized cores may be regarded as topological line defects (11). Moreover, the ordering of these chiral line defects within the 3D polar texture leads to a helical rotation of electric polarization along the ordering direction (Fig. S1).

## Results and Discussion

(PbTiO<sub>3</sub>)<sub>n</sub>/(SrTiO<sub>3</sub>)<sub>n</sub> superlattices were grown epitaxially by pulsed laser deposition on DyScO<sub>3</sub> (001)<sub>pc</sub> substrates (*pc* indicates pseudocubic indices) as described previously (*Materials and Methods*). For *n* = 10 to 16, the balance of elastic, electrostatic,

## Significance

Many natural structures exhibit chirality that is essential to their functional interactions, yet the chiral electronic structures found in condensed matter systems have been primarily limited to magnetic materials. Notably, the electric dipole equivalent of magnetic skyrmions has remained conspicuously elusive. However, recent theoretical predictions and experimental observations of the continuous rotation of electric polarization in titanate superlattices suggests that such complex oxide nanocomposites are ideal candidates for realizing chiral electric dipole configurations. Here we present the results from superlattices of PbTiO<sub>3</sub> and SrTiO<sub>3</sub> using a combination of resonant soft X-ray diffraction and second-principles simulations. We observe chiral arrays of polar line defects, spontaneously formed by the complex interactions in these artificial superlattices constructed from two nonchiral lattices.

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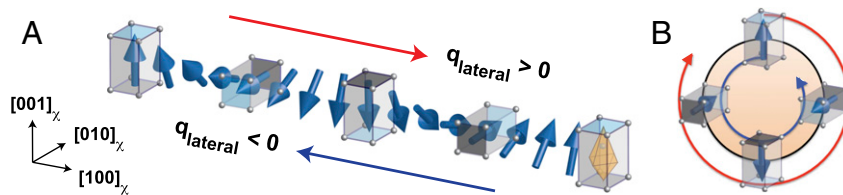
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**Fig. 2.** Mirrored diffraction vectors detect opposite rotational patterns in chiral textures. RSXD is sensitive to anisotropic  $\text{TiO}_6$  distortions, so that a helical rotation of the electric polarization can produce RSXD peaks with antisymmetric XCD. (A) Conical blue arrows indicate the direction of polarization, which rotates helically along the lateral direction,  $[100]_x$ . The distorted perovskite cell is depicted for several orientations, as is the distorted  $\text{TiO}_6$  octahedron for an up-polarized unit cell. (B) The cyclic modulation of polarization for this same helix is highlighted by folding the lateral dimension into a circle. The diffraction vector with  $q_{\text{lateral}} > 0$  (red arrow) senses a clockwise helical rotation of polarization, whereas the diffraction vector with  $q_{\text{lateral}} < 0$  (blue arrow) detects a counterclockwise rotation.

dependent on the particular geometry of each diffraction experiment (25). However, these components can be principally distinguished via their azimuthal dependence, in particular by the reversal (or not) of XCD. We next demonstrate that the azimuthal pattern of XCD (Fig. 3A) measured in the  $q_{\text{lateral}} = \pm q_{X\text{-pair}}$  diffraction peaks from  $\text{PbTiO}_3/\text{SrTiO}_3$  superlattices is indicative of the chiral electric dipole configuration in the textured arrays, and that it is also distinct from that of other systems whose XCD is dominated by dynamical effects. Finally, we have also confirmed that XCD is essentially negligible (*XCD of Ordered Phases*, Fig. 4, and Fig. S2) in thinner  $(\text{PbTiO}_3)_n/(\text{SrTiO}_3)_n$  superlattices (e.g.,  $n = 4$ ), which have no curled polar structure but which still possess periodic arrays of ferroelectric  $a$  domains that exhibit resonant diffraction peaks (*Phase Coexistence*). Thus, the dramatic difference in XCD between samples with and without curled polar textures directly points to the chiral structure of the arrays, rather than dynamical effects, as the primary origin of XCD.

The helical polarization structure depicted in Fig. 2A and its inherent broken mirror symmetry along  $q_{\text{lateral}}$  will produce a resonant ATS diffraction pattern whose peaks,  $q_{\text{lateral}} = \pm q_{\text{helix}} = \pm 2\pi/d_{\text{helix}}$  ( $d_{\text{helix}}$  is the period of the helix), have opposite XCD, similar to Fig. 1B. The twofold symmetry of the helix implies that its diffraction pattern after a  $180^\circ$  rotation is indistinguishable from the diffraction pattern of the original orientation. Notably, however, because  $q_{\text{lateral}}$  is fixed to the sample (by construction), the peak with positive dichroism in the original orientation is located at  $q_{\text{lateral}} = +q_{\text{helix}}$  whereas, after rotation, it is located at  $q_{\text{lateral}} = -q_{\text{helix}}$ . We observe similar behavior from the  $\text{PbTiO}_3/\text{SrTiO}_3$  polar arrays, as seen in Fig. 3.

Fig. 3A shows that, for a single diffraction spot with  $q_{\text{lateral}} = +q_{X\text{-pair}}$ , XCD is large and positive (red) across a range of azimuths,  $\phi_{\text{spot}}$  near  $+90^\circ$ . XCD in that same spot is strongly negative (blue) for  $\phi_{\text{spot}}$  near  $-90^\circ$ , and, in between these extremes, the XCD tends toward zero at  $\phi_{\text{spot}}$  near  $0^\circ$  or  $180^\circ$ . Similar azimuthal patterns were measured for multiple diffraction spots from the polar arrays (*Materials and Methods*), and have been overlaid in Fig. 3A to highlight this commonality via judicious selection of the origin,  $\phi_{\text{spot}} = 0^\circ$ . Here the azimuth,  $\phi_{\text{spots}}$ , has been defined for each diffraction spot, to measure the in-plane projection of its scattering vector relative to the projection of incident X-rays onto the sample surface (dashed green line in Fig. 3B). The cartoon in Fig. 3B illustrates the data in Fig. 3A, to emphasize that either diffraction spot exhibits positive XCD (red disk) when its in-plane scattering vector is  $+90^\circ$  from the dashed green reference line. This condition is fulfilled for  $q_{\text{lateral}} = +q_{X\text{-pair}}$  (thick black arrow, parallel to  $[100]_x$ ) in Fig. 3B, Left and also by a  $180^\circ$  azimuthal rotation of the sample for  $q_{\text{lateral}} = -q_{X\text{-pair}}$  (thick gray arrow, antiparallel to  $[100]_x$ ) in Fig. 3B, Right. For a fixed sample orientation, however, the mirrored diffraction spots ( $q_{\text{lateral}} = \pm q_{X\text{-pair}}$ ) have XCD with opposite polarity, as in Fig. 1B. Indeed, the inversion of XCD polarity with reversal of  $q_{\text{lateral}}$  persists at all azimuths, as deduced from Fig. 3A, and is a defining feature that points toward the chiral origin of this XCD signal.

This azimuthal pattern of XCD in the polar array diffraction spots is functionally similar to that of the ideal electric polarization helix. In the reference frame of the diffractometer, this twofold rotation of the sample results in a similar (albeit not identical) XCD diffraction pattern from the polar texture. An immediate implication of this XCD pattern is that the electric polarization of the chiral array must possess a broken mirror symmetry along  $q_{\text{lateral}}$ , with an additional restriction that the electric polarization texture must be considerably unchanged by a  $180^\circ$  azimuthal rotation. These constraints extracted from experimental results help to identify the most likely candidate structures calculated from second-principles atomistic simulations, which are discussed in *Calculation of Polarization Textures*.

The XCD pattern of  $\text{PbTiO}_3/\text{SrTiO}_3$  superlattices is not perfectly antisymmetric with respect to azimuth, largely because the magnitude is smaller for azimuths with negative XCD. This indicates that the chiral arrays do not perfectly mimic the ideal helix in their polarization configuration. This might arise, in part, due to a skewing of the atomic positions, which leads to a systematic asymmetric offset (i.e., buckling) of the polar core positions, as seen in Fig. S3. Skewed profiles of periodic structures are well known to produce asymmetric intensity in the mirrored diffraction spots of, e.g., surface gratings made of patterned lines with asymmetric cross-section (26). Dynamical effects might also partially contribute to the XCD signal, causing it to deviate from an idealized antisymmetric azimuthal pattern. In studies where dynamical modulation of dichroism [either XCD or X-ray linear dichroism (XLD)] in the diffraction peaks was found to be significant (20, 21), the azimuthal patterns possess twofold symmetry or else mirror symmetry that deviates only slightly from twofold symmetry (Fig. S4). This is in stark contrast to the inversion of XCD polarity that we observe with a  $180^\circ$  azimuthal rotation.

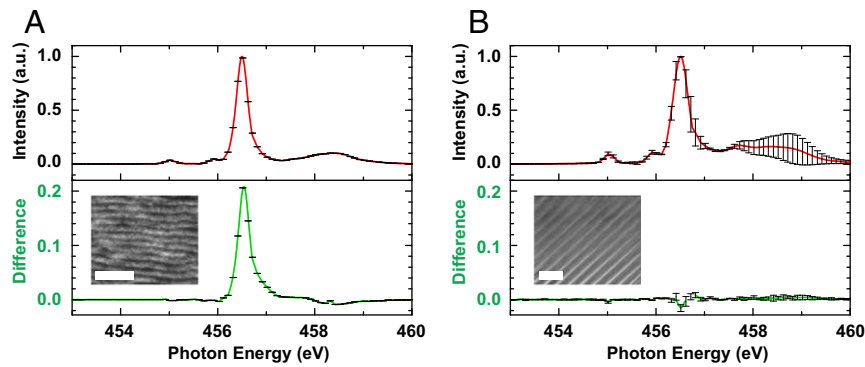
Our current analysis focuses on the general trend that positive XCD is observed at positive azimuths, while negative XCD is measured at negative azimuths. Other features of the azimuthal pattern in Fig. 3A could be manifestations of dynamical effects (*Azimuthal XCD and Chirality*), including fine intensity modulations and a notable imbalance of intensity between the azimuthal lobe of positive XCD and the lobe with negative XCD. Regardless, these two primary lobes of XCD with opposite polarization are clearly visible in the azimuthal pattern, even though some regions of the azimuthal circle are inaccessible due to geometrical constraints of the experimental setup. Based on this distinct azimuthal pattern, we can rule out dynamical effects as the principal source of XCD in the polar array diffraction spots. Also, in the absence of magnetic order, we conclude that XCD in these diffraction patterns is primarily the result of a chiral configuration of electric polarization in the curled textures of  $\text{PbTiO}_3/\text{SrTiO}_3$  arrays.

### Calculation of Polarization Textures

To ascertain more specifically the structure that produces the observed XCD signal, we have performed second-principles







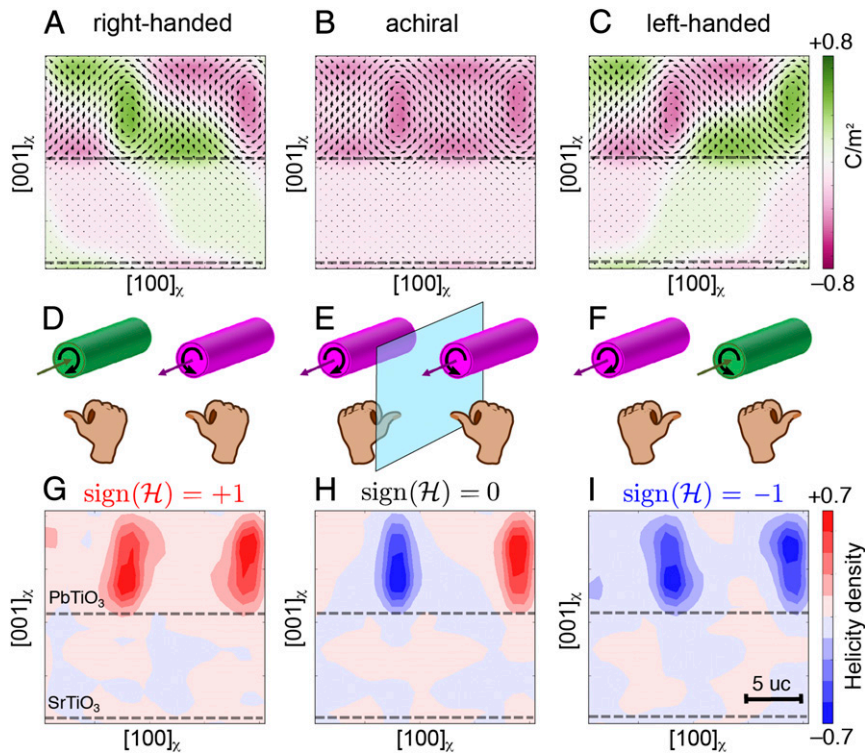
**Fig. 4.** Resonance profiles for  $(\text{PbTiO}_3)_n/(\text{SrTiO}_3)_n$  superlattices through the titanium  $L_3$  edge at (A)  $q_{\text{lateral}} = +q_{x, \text{pair}}$  for  $n = 14$  and (B)  $q_{\text{lateral}} = +q_{a, \text{domain}} = +2\pi/d_{a, \text{domain}}$  for  $n = 4$ , where  $d_{a, \text{domain}} \sim 70$  nm. (Upper) The polarization-averaged diffraction intensity (red) for both X-ray helicities, and (Lower) XCD (green). Insets show planar view HR-STEM images of (A) an array of polar cores ordered along  $[100]_x$  (horizontal scale bar: 50 nm) and (B) an array of ferroelectric  $a$  domains ordered along  $[110]_x$  (horizontal scale bar: 200 nm). Superlattices with chiral polar arrays exhibit strong XCD in A that is characteristic of the chiral arrangement of electric polarization in the texture. In superlattices with smaller layer thickness, the polarization arranges into periodic  $a$  domains only, with no chiral structure and correspondingly negligible XCD.

## Materials and Methods

**Deposition and Structural Characterization of Thin Film Superlattices.** Superlattices of  $(\text{SrTiO}_3)_n/(\text{PbTiO}_3)_n$  were synthesized on  $\text{DyScO}_3(110)_O$  substrates by pulsed laser deposition. Here  $n$  refers to the thickness in unit cells of respective materials oriented along the  $[001]_{pc}$  (pseudocubic) direction, defined relative to the orthorhombic substrate as  $[001]_{pc} // [110]_O$ ;  $[100]_{pc} // [\bar{1}10]_O$ ; and  $[010]_{pc} // [001]_O$ . Superlattice films were grown (*Synthesis and Structural Characterization*) to a total thickness of 100 nm and were monitored throughout using Reflection High Energy Electron Diffraction (RHEED) in situ characterization;

they exhibited Frank–van der Merwe growth mode. Various characterization techniques such as XRD, Rutherford back scattering (RBS), and TEM were employed to ensure structural and chemical homogeneity of superlattice films (5). For each superlattice, the lateral period of the counterrotated pair of polar cores ( $d_{x, \text{pair}}$ ) is well defined, ranging from  $\sim 8$  nm ( $n = 10$ ) to 11.4 nm ( $n = 16$ ).

**Detecting Chirality by RSXD.** Synchrotron-based resonant diffraction experiments were performed at the Advanced Light Source, using the scattering endstation at beamline 4.0.2. Polarization and photon energy of the X-ray source



**Fig. 5.** Second-principles calculations of electric polarization textures and their topological properties for  $n = 10$ . (A–C) Three different local minima, degenerate in energy. Each texture contains a pair of counterrotated cores yet has different chiral properties. Black arrows indicate the local dipoles, projected onto the  $(010)_x$  plane. A large axial component of the polarization along  $\pm[010]_x$ , represented by the green and magenta domains, is observed. (D–F) Simplified cartoon with cylinders representing the cores and arrows that show their rotational and axial polarization components. A right-hand rule reveals the chirality of each cylinder. By curling one's fingers in the direction of polar rotation around the core, the thumb points (anti-)parallel to the axial polarization for a (left-) right-handed core. (G–I) Maps of helicity. When the handedness of the two cores is the same, the system as a whole is chiral and the enantiomers can be distinguished by the sign of the integrated helicity ( $\mathcal{H}$ ). Results obtained at temperature of 10 K.

were tuned by an elliptically polarizing undulator. Intensity of X-rays scattered by the sample were measured using an in-vacuum CCD, and background dark counts were removed (*RSXD Measurements*). The CCD detector was also used to record X-ray absorption spectra via fluorescence (*RSXD Measurements*) and monitor small shifts in the diffraction peak position as a function of photon energy due to dynamical scattering effects (*RSXD Peak Shifts* and Fig. S9).

Resonance profiles were measured by tuning the photon energy through the titanium  $L_{3,2}$  edges (~450 eV to 470 eV), while sample and detector angles were adjusted to maintain the Bragg condition for each energy. The satellite features have an out-of-plane modulation along  $\ell$ , commensurate with the superlattice peaks observed in a specular  $(\theta-2\theta)$  XRD scan. The Bragg condition in Fig. 1C is  $(+q_{x, \text{pair}}, n_{SL} = 3)$ ; i.e., the lateral component of the wavevector was set to  $+q_{x, \text{pair}}$  and the out-of-plane component was set to the third-order superlattice peak (and the axial component was zero). All spectra have been corrected for the energy-dependent intensity of the incoming beam ( $I_0$ ) and are normalized to the maximum intensity of the polarization-averaged spectrum, after subtracting the nonresonant intensity in the preedge region (*RSXD Measurements*).

Line cuts through reciprocal space were measured at fixed photon energy, while adjusting sample and detector angles to vary  $q_{\text{lateral}}$  ( $q_{\text{out-of-plane}}$ ) at a fixed value of  $q_{\text{out-of-plane}}$  ( $q_{\text{lateral}}$ ). Fig. 1B shows a line cut parallel to  $q_{\text{lateral}}$  with fixed  $q_{\text{out-of-plane}}$  corresponding to  $n_{SL} = 3$ . Data were normalized to the average intensity at  $q_{\text{lateral}} = \pm q_{x, \text{pair}}$  for the polarization-averaged curve. Photon energy was fixed at the most intense feature in the resonance profile, identified as having  $t_{2g}$  character (~456.5 eV).

All measurements were performed with nearly 100% circularly polarized X-rays. Data were collected in pairs, with helicity of the circular polarization reversed for each energy (resonance profiles) or momentum vector (reciprocal space line cuts). XCD (*RSXD Measurements*) was calculated as the difference of the scattered intensity for the two helicities; subtraction was performed after normalizing the scattered intensities.

Azimuthal data in Fig. 3A were collected from three diffraction spots, two of which were  $q_{\text{lateral}} = \pm q_{x, \text{pair}}$  for the primary ordering direction,  $[100]_x // [001]_0$  (*Azimuthal XCD Measurements* and Fig. S10 A–C). The third diffraction spot was  $q_{\text{lateral}} = +q_{x, \text{pair}}$  for the secondary ordering direction,  $[100]_x // [\bar{1}10]_0$ . The sample azimuth ( $\Phi$ ) was adjusted to vary the azimuth ( $\phi_{\text{spot}}$ ) of each diffraction spot, as depicted in Fig. S10 D–F. XCD resonance profiles were collected at each azimuth, then normalized and fitted by a reference spectrum (*Azimuthal XCD Measurements*).

The chirality map in Fig. 1D displays the XCD measured in the primary diffraction spot,  $q_{\text{lateral}} = +q_{x, \text{pair}}$  with  $\phi_{\text{spot}}$  fixed near  $+90^\circ$ . XCD intensity was recorded at fixed diffraction geometry while scanning the sample, with the effect of rastering the X-ray beam across the surface of the sample.

**Second-Principles Simulations of  $\text{PbTiO}_3/\text{SrTiO}_3$  Superlattices.** The superlattice potentials are identical to those used in ref. 28. We assume in-plane lattice constants of  $a = b = 3.901 \text{ \AA}$  and  $\gamma = 90^\circ$ . To counteract the underestimate of the lattice constant due to the well-known overbinding error of the local density approximation, which is the first-principles theory used to compute the parameters of our model, an external expansive hydrostatic pressure of  $-11.2 \text{ GPa}$  is imposed.

For computational feasibility, we have focused on a simulation supercell made from a periodic repetition of  $2n \times n \times 2n$  elemental perovskite unit cells, sufficiently large to simulate domains in the  $n = 10$  superlattice. We solved the models by running Monte Carlo simulations typically comprising 10,000 thermalization sweeps, followed by 40,000 sweeps to compute thermal averages. We ran Monte Carlo simulated annealings down to very low temperatures to perform structural relaxations and find the ground state or metastable solutions. Additional details of the simulation parameters and the resulting structures are discussed in *Second-Principles Calculations*.

Local polarizations are computed within a linear approximation of the product of the Born effective charge tensor times the atomic displacements from the reference structure positions divided by the volume of the unit cell. From the complex polarization texture, we can compute the helicity density as proposed by Moffatt (31). A detailed description of the helicity calculations and the polar texture chirality is found in *Helicity of Calculated Polarization Textures*.

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