

ARTICLE

DOI: 10.1038/s41467-018-03703-0

OPEN

Dual-comb spectroscopy of laser-induced plasmas

Jenna Bergevin¹, Tsung-Han Wu¹, Jeremy Yeak², Brian E. Brumfield³, Sivanandan S. Harilal³, Mark C. Phillips³ & R. Jason Jones¹

Dual-comb spectroscopy has become a powerful spectroscopic technique in applications that rely on its broad spectral coverage combined with high frequency resolution capabilities. Experiments to date have primarily focused on detection and analysis of multiple gas species under semi-static conditions, with applications ranging from environmental monitoring of greenhouse gases to high-resolution molecular spectroscopy. Here, we utilize dual-comb spectroscopy to demonstrate broadband, high-resolution, and time-resolved measurements in a laser-induced plasma. As a demonstration, we simultaneously detect trace amounts of Rb and K in solid samples with a single laser ablation shot, with transitions separated by over 6 THz (13 nm) and spectral resolution sufficient to resolve isotopic and ground state hyperfine splittings of the Rb D₂ line. This new spectroscopic approach offers the broad spectral coverage found in the powerful techniques of laser-induced breakdown spectroscopy (LIBS) while providing the high-resolution and accuracy of cw laser-based spectroscopies.

¹College of Optical Sciences, University of Arizona, 1630 E University Blvd, Tucson, AZ 85721, USA. ²PM&AM Research, Tucson, AZ 85719, USA. ³Pacific Northwest National Laboratory, Richland, WA 99352, USA. Correspondence and requests for materials should be addressed to R.J.J. (email: rjjones@optics.arizona.edu)

Laser-induced plasmas provide a versatile and non-contact means to apply the powerful tools of optical spectroscopy in the analysis of solid materials. When the intensity of an incident laser pulse is sufficiently high, a plasma is generated, ablating a small amount of material above the sample surface. The resulting ions, atoms, and molecules within the evolving plasma plume can be detected optically using either emission or absorption techniques. The most common optical spectroscopy technique for laser ablation plumes is optical emission spectroscopy, typically called laser-induced breakdown spectroscopy (LIBS)^{1,2}. In this technique, the emission spectrum from electronically excited ions, atoms, and molecules is recorded. LIBS has had a significant impact in a broad range of fields. For example many geological applications exist for studying the composition of rocks, minerals, and soils³, including the planetary exploration of Mars by the NASA rover Curiosity⁴. LIBS has also been applied for the characterization of nuclear materials and their isotopic concentrations⁵, needed for monitoring nuclear waste and nuclear fuel production for its use in both civilian and military applications. Other applications are found in areas ranging from pharmaceutical quality control⁶, monitoring of industrial processes⁷, forensic science⁸, and for trace detection of nanoparticles used in medical applications⁹, to name a few.

In this work, we apply the technique of dual frequency comb spectroscopy to optically probe laser-induced plasmas. Dual-comb spectroscopy (DCS) has become a valuable tool for broadband and high-resolution spectroscopic measurements. We demonstrate the potential impact of this approach in the analysis of solid materials by simultaneously detecting trace amounts of Rb and K in solid samples using a single laser ablation shot while still providing sufficient spectral resolution to observe the isotopic and ground state hyperfine splittings of the Rb D₂ line. The broadband, sensitive, and high spectral and temporal resolution of this approach can enable the capability to optically identify and track multiple atomic, ionic, and molecular species present in the dynamic plasma environment.

Results

Laser ablation spectroscopy. To obtain the maximum amount of information about the composition of a solid sample via optical probing of a laser ablation plume, it is desirable to utilize a large spectral bandwidth so that multiple ionic, atomic, molecular, and continuum transitions can be identified. At the same time, a high spectral resolution is needed to distinguish closely spaced transitions, to resolve small isotopic shifts, to measure intrinsic linewidths of transitions, and to minimize spectral interferences from multiple species. Other desirable aspects of an optical spectroscopic measurement are rapid detection, time and space resolution, and simultaneous acquisition of multiple wavelengths. Unfortunately, it is difficult to satisfy all requirements simultaneously and thus compromises must be made based on available spectroscopic instrumentation.

In LIBS, a dispersive spectrograph combined with an intensified-CCD (ICCD) camera is often used to record the optical emission. It is straightforward to measure time-gated emission spectra from laser ablation plasmas with the ICCD. However, this technique requires a trade-off in spectral bandwidth versus spectral resolution based on diffraction grating selection and ICCD array size. Thus, a low- to moderate-resolution spectrum can be obtained over a large spectral bandwidth, or a high-resolution spectrum can be obtained over a reduced spectral bandwidth. For example, a typical LIBS spectrum measured using a 0.5 m Czerny-Turner spectrograph with 2400 g/mm grating could provide a spectral resolution of ≈ 20 pm with ≈ 5 nm spectral bandwidth. If the emission intensity

is high enough, spectra may be obtained from single ablation shots without additional averaging.

A fundamental limitation of optical emission spectroscopy is the requirement for electronic excitation to generate a measurable emission signal. The relative populations of ionized atoms, neutral atoms, and molecules vary as the plasma evolves, and are highly dependent on the ablation conditions. Nevertheless, for any given transition the emission intensity increases with excitation temperature that is higher at earlier times in the plasma evolution. Unfortunately, higher temperature and electron density at early times in plasma evolution also leads to increased spectral linewidths, primarily via Stark broadening². Linewidths are decreased at later times in the plasma evolution, but the emission intensity also decreases at these times. Thus, for optical emission spectroscopy techniques, maximizing signal intensity and minimizing spectral linewidths are conflicting requirements.

Absorption spectroscopy techniques applied to laser ablation plumes measure lower-state populations and thus do not rely on electronic excitation of species. As a result, absorption may probe later times in the plasma evolution during which temperatures are cooler and spectral linewidths are correspondingly narrower. For the conditions used here (ns ablation pulses, low background pressures), the plasma emission lifetime typically lasts a few microseconds. However, the presence of ground state atomic neutrals can last several hundreds of microseconds.

Absorption spectroscopy using broadband incoherent sources and a dispersive spectrograph has been used for probing laser ablation plumes, but suffers the same limitations on spectral bandwidth and resolution as optical emission spectroscopy¹⁰. Tunable cw lasers provide a means to probe laser ablation plumes via laser absorption spectroscopy (LAS)^{11–16} or laser-induced fluorescence (LIF)^{15–20}. The spectral linewidths of cw lasers (<10 MHz) are much smaller than the intrinsic linewidths of most transitions. As a result, spectra may be measured in the laser ablation plume by LAS or LIF without effects of instrumental broadening. For example, atomic absorption spectral linewidths measured in laser ablation plumes can be <2 GHz (2 pm)^{14,19,20}. However, when performing LAS or LIF using cw lasers, the laser wavelength must be stepped or scanned across an absorption feature to record a spectrum. The scanning requirement places a limit on the spectral bandwidth that may be acquired in a given time period for LAS or LIF. Moreover, acquisition typically occurs over multiple ablation pulses while the laser is scanned, making single-shot measurements impractical. Performing multiplexed wavelength measurements on a single ablation shot would provide great benefits in noise reduction, consistent plasma conditions over all wavelengths, and increased spectral coverage.

Dual-comb spectroscopy. Femtosecond (fs) frequency combs offer a new and powerful tool for probing laser ablation plasmas. Frequency combs have revolutionized the field of precision frequency spectroscopy and enabled the development of next-generation atomic clocks based on optical transitions²¹. Frequency combs are based on the ability to generate trains of optical pulses with a well-defined phase between subsequent pulses. This pulse-to-pulse phase coherence results in an optical spectrum consisting of narrow comb teeth separated precisely by the pulse repetition rate (e.g. 100 MHz). Furthermore, the absolute optical frequency of each comb tooth can be determined with high accuracy. Given the short pulse durations that can be obtained directly from many laser systems (<10 fs), the bandwidth of these optical frequency combs can easily extend beyond 100 nm. In addition, thanks to the high peak powers provided by the pulses, nonlinear frequency conversion techniques can be utilized to extend the frequency comb coverage to over an optical octave²².

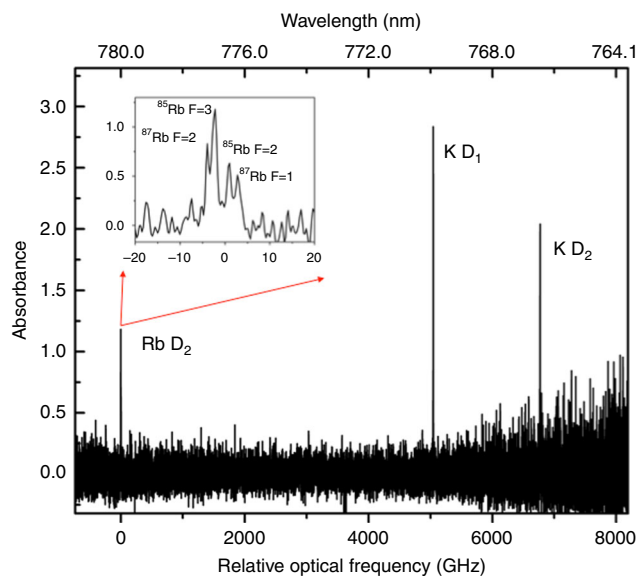


Fig. 2 Broadband single-shot absorption measurement of the laser-induced plasma. The absorption spectrum of the Rb D_2 line and K D_1 and D_2 lines, separated by over 6 THz, are simultaneously observed from a calibrated sample of SRM610 NIST glass following the laser ablation pulse. The inset shows a zoomed-in view of the $5S_{1/2}$ – $5P_{3/2}$ Rb D_2 line, demonstrating the ability of DCS to simultaneously provide high spectral resolution by resolving the four absorption peaks from the Rb D_2 ground state hyperfine structure and isotopic shift of ^{85}Rb versus ^{87}Rb . Optical resolution: 0.53 GHz (1 pm), Δf_{rep} : 520 Hz, pressure: 51 torr. Labels indicate Rb isotope and ground state hyperfine level of the transition

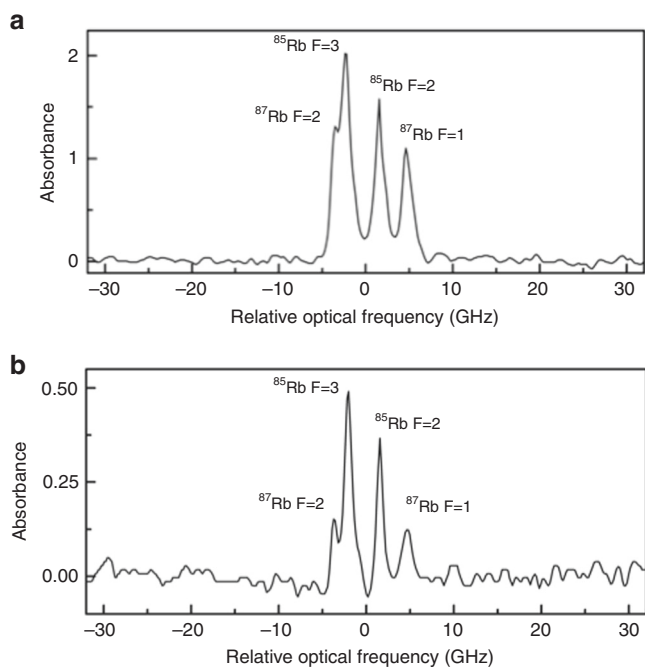


Fig. 3 Comparison of Rb cell versus laser plasma absorption spectrum. Simultaneous measurement of the Rb D_2 lines from the **a** laser-induced plasma and **b** Rb cell. Each spectrum is the average of three laser ablation shots. The calculated measurement resolution was 0.18 GHz (0.4 pm). Δf_{rep} : 140 Hz, pressure: 1 torr

Discussion

The broadband and high-resolution spectrum of multiple atomic species measured in a single laser ablation shot as demonstrated

here using DCS would be extremely difficult to achieve using other techniques. For example, in LIBS, obtaining sufficient spectral resolution to resolve intrinsic spectral linewidths in a laser ablation plume presents significant challenges and requires very large spectrographs, further reducing spectral bandwidth. Intrinsic LIBS emission linewidths of atomic transitions are often <10 pm, especially for heavy elements such as U^{32,33}. Approaches have been used to increase spectral resolution in LIBS measurements, such as combining a Fabry–Perot etalon with a spectrograph^{32,34}. Echelle spectrographs³³ are capable of measuring broad spectral bandwidths at high spectral resolution. For example, an echelle spectrograph using a CCD can measure over a spectral bandwidth of 200–1000 nm at a resolving power of 44,000, corresponding to a spectral resolution of 5–20 pm³³, which would still be insufficient to measure the Doppler-limited linewidths and hyperfine splittings demonstrated here. In addition, the low optical throughput of such instruments can make some LIBS measurements challenging, especially when time-resolved or single-shot measurements are desired.

In LAS or LIF measurements that use cw lasers to achieve high spectral resolution, the limited scanning range presents a serious constraint on optical bandwidth. For example, an external cavity diode laser operating at 780 nm may provide 50 GHz of mode-hop-free tuning range which is usually only enough to measure the absorption spectrum of a single transition at a time. LAS and LIF also face challenges when applied to laser plasma measurements due to the highly transient and spatially varying plasma environment. The characteristics and shot-to-shot repeatability of the laser plasma (e.g. density, temperature, species evolution) depend critically on multiple factors, including sample surface conditions and possible multi-shot modifications, pulse energy, pulse duration, background pressure and composition to name a few^{2,35}. Variations in ablation properties during acquisition with a cw laser over multiple shots can lead to noise in the absorption spectrum or uncertainties in spectral parameters due to changing plasma physical conditions, especially at higher ambient pressures. Techniques have been developed to reduce the effects of this shot-to-shot ablation noise using differential absorption¹⁴ or signal normalization by emission²⁰. However, in the DCS measurements demonstrated here, all frequencies of the fs comb interact with the plasma simultaneously. The noise seen when scanning a tunable laser over multiple ablation shots can in principle be minimized with DCS. Even if ablation properties change over multiple ablation shots, this noise will appear as spectrally flat in DCS, which can be averaged more effectively than in tunable LAS.

The signal-to-noise (s/n) of the absorption spectrum demonstrated here can be further improved using a variety of standard techniques already implemented in other DCS experiments. For example, a reference beam can be used to differentiate background noise from the measured absorption signal³⁶. In the current experiments, a time-interleaved reference beam is inherently available from the probe pulses arriving in between laser ablation shots when there is no plasma present. Modifications in the current timing electronics and data acquisition processing can use the information from these temporal slices of the pulse train to subtract out residual background noise and improve the detection sensitivity.

The initial experiments reported here were performed with relatively long integration times considering the highly transient nature of laser-produced plasmas. However, the changes in plasma properties are more drastic at early times of its evolution, and much less during the delayed temporal window of the present measurements. This enabled the measurement of relatively narrow lineshapes not severely limited by the Stark or excessive Doppler broadening that occurs at shorter timescales. In the

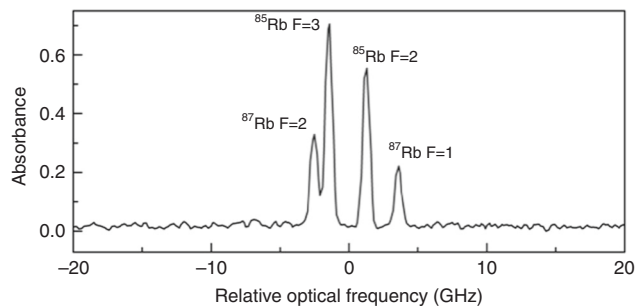


Fig. 4 Doppler-limited absorption spectrum of Rb D₂ lines. The spectrum from the gas cell shows the ground state hyperfine splitting of both ⁸⁵Rb and ⁸⁷Rb. The spectrum is the average of 200 measurements with a calculated measurement resolution of 0.13 GHz

current experiment, we are also able to simultaneously detect the Rb and K transitions with a time window down to only ≈ 10 μ s. In this case, the broadband spectrum (not shown) looks nearly identical to that as shown in Fig. 2. However, the hyperfine and isotopic shift of the Rb D₂ line is not resolved due to the reduced measurement-limited spectral resolution. Increasing Δf_{rep} can improve the time-resolution without sacrificing optical resolution. However, this comes at the cost of detection sensitivity and measurement spectral bandwidth³⁷. Probing the plasma with increased time-resolution utilizing higher repetition rate laser sources can be helpful in future work to study the dynamic evolution of the ionic, atomic, and molecular species within the plasma.

In conclusion, we have demonstrated DCS of laser-induced plasmas. We simultaneously measure trace amounts of Rb and K in a single laser ablation shot while resolving the hyperfine and isotopic shift of the Rb D₂ line with sub-GHz level resolution. The spectral resolution, broad spectral coverage, and rapid measurement capability of DCS can enable identification and tracking of multiple ionic, atomic, and molecular species in the evolving plasma. The spectral coverage of DCS can be easily extended to almost any portion of the electromagnetic spectrum. For example, with use of nonlinear optical fibers for supercontinuum generation, DCS laser systems can measure optical spectra spanning 100's of nanometers²². Further spectral coverage can be achieved with sum²⁸ and difference frequency generation³⁸, and even intra-cavity high harmonic generation^{39,40} to the vacuum and extreme-ultraviolet. Our approach to time-resolved DCS can also be applied to study other dynamic systems such as kinetics in chemical reactions²⁹ and pulsed-detonation combustion⁴¹. The results demonstrated here lay the ground work for future studies exploiting the properties of the fs frequency comb to probe laser-induced plasmas, with the potential to impact a wide range of applications in the optical analysis of solid materials.

Methods

Experimental set-up. The dual-comb system used here was provided by PM&AM Research (model PMAM-780-TR-DCS-0.120 GHz) and was developed in a collaborative effort to investigate isotopic ratios of radiological materials utilizing laser-induced plasmas. It is composed of two Kerr lens mode-locked Ti:sapphire lasers each pumped at 4.5 W from a common 532 nm laser source to minimize pump-induced noise between the oscillators. The spectrum of both lasers was centered near 780 nm with bandwidths spanning 760–800 nm, adjustable with the use of intracavity prisms. The approximately 120 MHz repetition rate of each laser could be adjusted using translation stages and piezo-electric transducers (PZTs) attached to each cavity end mirror. The repetition rate difference between the lasers, Δf_{rep} , was typically set between 100 and 500 Hz. To establish phase coherence between the comb modes near 780 nm, a free-running but slow drifting monolithic DBR laser at 780 nm was used (Vescent D2-100) as a transfer oscillator. The cw laser was locked directly to Comb 1 using fast servo electronics fed back to the cw laser current to lock the beatnote between the two lasers, f_{b1} , to a stable RF reference. The beatnote between a mode of Comb 2 and the cw laser, f_{b2} , was also detected.

Due to the linewidth of the cw laser, direct stabilization of f_{b2} to an RF reference was insufficient to establish phase coherence between modes of Comb 1 and Comb 2 near 780 nm. To eliminate the contribution of noise from the transfer oscillator, Comb 2 was stabilized to the difference between the beatnotes, $f_{b1} - f_{b2}$ ⁴² using a second fast PZT in Comb 2. This enabled an effectively tight phase lock between Comb 1 and Comb 2 for the modes near 780 nm that was independent of noise from the cw laser, and sufficient for averaging over multiple interferograms for time scales on the order of 1 s. For the Doppler-limited linewidths measured here, no additional locking of either comb offset frequency was needed.

Rb cell reference. To demonstrate the performance of the DCS system and to serve as a real-time reference for the plasma-based experiment, we first measured the Rb D₂ transitions near 780 nm in a 7-cm long glass cell containing a natural abundance of Rb atoms (72% ⁸⁵Rb and 28% ⁸⁷Rb). The pulse trains from each fs comb were combined before the Rb cell on a beam splitter and detected with a silicon photodiode after diffracting off a grating (see Fig. 1). The grating was used to improve the retrieved signal-to-noise levels by eliminating shot-noise contributions from unused portions of the laser spectrum³⁷. The resulting interferograms were recorded in the time domain with a 12-bit data acquisition card at 125 Ms/s. The Rb absorption spectrum shown in Fig. 4 is the result of 200 recorded interferograms that were individually Fourier transformed and then averaged in the frequency domain. For this data set, with $\Delta f_{\text{rep}} = 500$ Hz, the 1.8 ms acquisition time per interferogram provided a 130 MHz (0.3 pm) optical resolution. Both Rb isotopes and their ground state hyperfine splittings are easily resolved, limited by Doppler broadening from the room temperature gas cell.

Data availability. All relevant data that supports our experimental findings is available from the corresponding author upon reasonable request.

Received: 9 November 2017 Accepted: 6 March 2018

Published online: 28 March 2018

References

- Musazzi, S. & Perini, U. *Laser-Induced Breakdown Spectroscopy: Theory and Applications*, Vol. 182 (Springer, New York, 2014).
- Hahn, D. W. & Omenetto, N. Laser-induced breakdown spectroscopy (libs), part i: Review of basic diagnostics and plasma-particle interactions: still-challenging issues within the analytical plasma community. *Appl. Spectrosc.* **64**, 335A–366A (2010).
- McMillan, N. J., Rees, S., Kochelek, K. & McManus, C. Geological applications of laser-induced breakdown spectroscopy. *Geostand. Geoanal. Res.* **38**, 329–343 (2014).
- Maurice, S. et al. The chemcam instrument suite on the mars science laboratory (msl) rover: Science objectives and mast unit description. *Space Sci. Rev.* **170**, 95–166 (2012).
- Martin, M. Z., Allman, S., Brice, D. J., Martin, R. C. & Andre, N. O. Exploring laser-induced breakdown spectroscopy for nuclear materials analysis and in-situ applications. *Spectrochim. Acta Part B: At. Spectrosc.* **74**, 177–183 (2012).
- Myakalwar, A. K. et al. Laser-induced breakdown spectroscopy-based investigation and classification of pharmaceutical tablets using multivariate chemometric analysis. *Talanta* **87**, 53–59 (2011).
- Everton, S. K., Hirsch, M., Stravroulakis, P., Leach, R. K. & Clare, A. T. Review of in-situ process monitoring and in-situ metrology for metal additive manufacturing. *Mater. Des.* **95**, 431–445 (2016).
- Lennard, C., El-Defar, M. M. & Robertson, J. Forensic application of laser-induced breakdown spectroscopy for the discrimination of questioned documents. *Forensic Sci. Int.* **254**, 68–79 (2015).
- Sancey, L. et al. Laser spectrometry for multi-elemental imaging of biological tissues. *Sci. Rep.* **4**, 6065 (2014).
- Rivière, M. & Chéron, B. Analysis of relaxing laser-induced plasmas by absorption spectroscopy: toward a new quantitative diagnostic technique. *Spectrochim. Acta Part B: At. Spectrosc.* **65**, 524–532 (2010).
- King, L., Gornushkin, I., Pappas, D., Smith, B. & Winefordner, J. Rubidium isotope measurements in solid samples by laser ablation-laser atomic absorption spectroscopy. *Spectrochim. Acta Part B: At. Spectrosc.* **54**, 1771–1781 (1999).
- Liu, H., Quentmeier, A. & Niemax, K. Diode laser absorption measurement of uranium isotope ratios in solid samples using laser ablation. *Spectrochim. Acta Part B: At. Spectrosc.* **57**, 1611–1623 (2002).
- Miyabe, M. et al. Absorption spectroscopy of uranium plasma for remote isotope analysis of next-generation nuclear fuel. *Appl. Phys. A* **112**, 87–92 (2013).

14. Taylor, N. & Phillips, M. Differential laser absorption spectroscopy of uranium in an atmospheric pressure laser-induced plasma. *Opt. Lett.* **39**, 594–597 (2014).
15. Miyabe, M. et al. Laser ablation absorption spectroscopy for isotopic analysis of plutonium: spectroscopic properties and analytical performance. *Spectrochim. Acta Part B: At. Spectrosc.* **134**, 42–51 (2017).
16. Bushaw, B. A. & Anheier, N. C. Isotope ratio analysis on micron-sized particles in complex matrices by laser ablation-absorption ratio spectrometry. *Spectrochim. Acta Part B: At. Spectrosc.* **64**, 1259–1265 (2009).
17. Smith, B., Quentmeier, A., Bolshov, M. & Niemax, K. Measurement of uranium isotope ratios in solid samples using laser ablation and diode laser-excited atomic fluorescence spectrometry. *Spectrochim. Acta Part B: At. Spectrosc.* **54**, 943–958 (1999).
18. Harilal, S. S., LaHaye, N. L. & Phillips, M. C. Two-dimensional fluorescence spectroscopy of laser-produced plasmas. *Opt. Lett.* **41**, 3547–3550 (2016).
19. Harilal, S. S., LaHaye, N. L. & Phillips, M. C. High-resolution spectroscopy of laser ablation plumes using laser-induced fluorescence. *Opt. Express* **25**, 2312–2326 (2017).
20. Phillips, M. C. et al. Two-dimensional fluorescence spectroscopy of uranium isotopes in femtosecond laser ablation plumes. *Sci. Rep.* **7**, 3784 (2017).
21. Cundiff, S. T. & Ye, J. Colloquium: femtosecond optical frequency combs. *Rev. Mod. Phys.* **75**, 325–342 (2003).
22. Okubo, S. et al. Ultra-broadband dual-comb spectroscopy across 1.0–1.9 μm . *Appl. Phys. Express* **8**, 082402 (2015).
23. Foltynowicz, A. et al. Optical frequency comb spectroscopy. *Faraday Discuss.* **150**, 23–31 (2011).
24. Coddington, I., Newbury, N. & Swann, W. Dual-comb spectroscopy. *Optica* **3**, 414–426 (2016).
25. Rieker, G. B. et al. Frequency-comb-based remote sensing of greenhouse gases over kilometer air paths. *Optica* **1**, 290–298 (2014).
26. Coddington, I., Swann, W. C. & Newbury, N. R. Coherent multiheterodyne spectroscopy using stabilized optical frequency combs. *Phys. Rev. Lett.* **100**, 013902 (2008).
27. Bernhardt, B. et al. Cavity-enhanced dual-comb spectroscopy. *Nat. Photonics* **4**, 55–57 (2010).
28. Potvin, S. & Genest, J. Dual-comb spectroscopy using frequency-doubled combs around 775 nm. *Opt. Express* **21**, 30707–30715 (2013).
29. Fleisher, A. J. et al. Mid-infrared time-resolved frequency comb spectroscopy of transient free radicals. *J. Phys. Chem. Lett.* **5**, 2241–2246 (2014).
30. Baker, C. et al. In situ probing of mode-locked vertical-external-cavity-surface-emitting lasers. *Opt. Lett.* **40**, 5459–5462 (2015).
31. Asahara, A. & Minoshima, K. Development of ultrafast time-resolved dual-comb spectroscopy. *APL Photonics* **2**, 041301 (2017).
32. Morgan, P. K., Scott, J. R. & Jovanovic, I. Hybrid interferometric/dispersive atomic spectroscopy of laser-induced uranium plasma. *Spectrochim. Acta Part B: At. Spectrosc.* **116**, 58–62 (2016).
33. Cremers, D. A. et al. Monitoring uranium, hydrogen, and lithium and their isotopes using a compact laser-induced breakdown spectroscopy (libs) probe and high-resolution spectrometer. *Appl. Spectrosc.* **66**, 250–261 (2012).
34. Effenberger, A. J. & Scott, J. R. Practical high-resolution detection method for laser-induced breakdown spectroscopy. *Appl. Opt.* **51**, B165–B170 (2012).
35. Russo, R. E. Laser ablation. *Appl. Spectrosc.* **49**, 14A–28A (1995).
36. Coddington, I., Swann, W. & Newbury, N. Coherent dual-comb spectroscopy at high signal-to-noise ratio. *Phys. Rev. A* **82**, 043817 (2010).
37. Newbury, N. R., Coddington, I. & Swann, W. Sensitivity of coherent dual-comb spectroscopy. *Opt. Express* **18**, 7929–7945 (2010).
38. Schliesser, A., Picqué, N. & Hänsch, T. W. Mid-infrared frequency combs. *Nat. Photonics* **6**, 440–449 (2012).
39. Jones, R. J., Moll, K. D., Thorpe, M. J. & Ye, J. Phase-coherent frequency combs in the vacuum ultraviolet via high-harmonic generation inside a femtosecond enhancement cavity. *Phys. Rev. Lett.* **94**, 193201 (2005).
40. Gohle, C. et al. A frequency comb in the extreme ultraviolet. *Nature* **436**, 234–237 (2005).
41. Rein, K. D. et al. Multispecies absorption spectroscopy of detonation events at 100 kHz using a fiber-coupled, time-division-multiplexed quantum-cascade-laser system. *Appl. Opt.* **55**, 6256–6262 (2016).
42. Kuse, N., Ozawa, A. & Kobayashi, Y. Comb-resolved dual-comb spectroscopy stabilized by free-running continuous-wave lasers. *Appl. Phys. Express* **5**, 112402 (2012).

Acknowledgements

This material is based upon work supported by the Air Force Office of Scientific Research under award number FA9550-15-1-0091, the National Nuclear Security Administration, Defense Nuclear Nonproliferation R&D Office, and the Department of Energy under Award Number DE-SC0004311 and Physics, Materials and Applied Mathematics Research L.L.C. The Pacific Northwest National Laboratory is operated for the U.S. Department of Energy (DOE) by the Battelle Memorial Institute under Contract No. DE-AC05-76RL01830. J.B. would like to thank the UA/NASA Space Grant Program for funding during the course of this research.

Author contributions

J.B. and T.-H.W. contributed equally to this work. R.J.J., T.-H.W., J.Y., M.C.P., and S.S.H. conceived the experiments. Experiments were performed by R.J.J., J.B., T.-H.W., J.Y., and M.C.P. R.J.J., J.B., T.-H.W., J.Y., M.C.P., B.E.B., and S.S.H. contributed to the analysis of the data and interpretation of the results. R.J.J., J.B., M.C.P., and S.S.H. wrote the manuscript with comments from all authors.

Additional information

Supplementary Information accompanies this paper at <https://doi.org/10.1038/s41467-018-03703-0>.

Competing interests: The authors declare no competing interests.

Reprints and permission information is available online at <http://npg.nature.com/reprintsandpermissions/>

Publisher's note: Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.



Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit <http://creativecommons.org/licenses/by/4.0/>.

© The Author(s) 2018