



# Metastability and avalanche dynamics in strongly correlated gases with long-range interactions

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Edited by Steven M. Girvin, Yale University, New Haven, CT, and approved February 7, 2018 (received for review December 5, 2017)

**We experimentally study the stability of a bosonic Mott insulator against the formation of a density wave induced by long-range interactions and characterize the intrinsic dynamics between these two states. The Mott insulator is created in a quantum degenerate gas of 87-Rubidium atoms, trapped in a 3D optical lattice. The gas is located inside and globally coupled to an optical cavity. This causes interactions of global range, mediated by photons dispersively scattered between a transverse lattice and the cavity. The scattering comes with an atomic density modulation, which is measured by the photon flux leaking from the cavity. We initialize the system in a Mott-insulating state and then rapidly increase the global coupling strength. We observe that the system falls into either of two distinct final states. One is characterized by a low photon flux, signaling a Mott insulator, and the other is characterized by a high photon flux, which we associate with a density wave. Ramping the global coupling slowly, we observe a hysteresis loop between the two states—a further signature of metastability. A comparison with a theoretical model confirms that the metastability originates in the competition between short- and global-range interactions. From the increasing photon flux monitored during the switching process, we find that several thousand atoms tunnel to a neighboring site on the timescale of the single-particle dynamics. We argue that a density modulation, initially forming in the compressible surface of the trapped gas, triggers an avalanche tunneling process in the Mott-insulating region.**

quantum gas | metastability | avalanche dynamics | cavity QED | extended Bose-Hubbard model

**W**hen found in a metastable state or phase, a system resides in a condition differing from its state of least energy for an extended period. Examples for long-lived metastable phases are found in magnetized materials, glasses, and crystals like diamond, as well as in macromolecules (1–3). In many solid-state systems, metastability can be described by a first-order phase transition (4), yet the less accessible switching dynamics and their associated timescales are crucial to gain insights into the mechanisms of structure formation.

Ultracold atoms emerge as a promising tool to study questions related to metastability in quantum many-body systems, due to the precise knowledge and high level of control over the underlying Hamiltonian. Indeed, metastable states, many-body localization, and first-order phase transitions have recently attracted theoretical (5–10) and experimental interest (11–16). The presence of long-range interactions is of particular importance to induce and influence metastability, since it makes decay processes like nucleation and phase separation energetically costly, resulting in increased lifetimes of higher-energy states, as recently observed in Rydberg excitation clusters (17). The consequences are even more severe in systems with long-range interactions decaying slower than  $1/r^d$ , where  $r$  is the interparticle distance and  $d$  is the dimensionality of the system, as a separation into independent clusters is no longer possible. The lifetime of metastable phases then scales with the system size and diverges in the thermodynamic limit (18, 19).

Here we study a trapped bosonic quantum gas with strong short-range interactions in which all atoms are also coupled

to each other through global-range interactions. Increasing the strength of the global coupling triggers a switching process that results in a rearranged atomic distribution and self-consistent potential. The timescale during which this process takes place is intrinsically determined by the many-body dynamics of the gas and is continuously monitored in the experiment.

In our experiment the global interactions arise from the coupling of a Bose–Einstein condensate (BEC) to a single mode of an optical high-finesse cavity (20, 21). With the atomic gas trapped in a 3D optical lattice we can simultaneously control short-range interactions and push the system into a strongly correlated regime (Fig. 1B). The phase diagram of the system is schematically shown in Fig. 1C. It was recently determined experimentally (22, 23) and studied theoretically (24–32). In the thermodynamic limit a first-order phase transition from a Mott insulator (MI) (33, 34) to a charge-density wave (CDW) state has been predicted (27, 28, 30, 32).

## Toy Model

To achieve a basic understanding of our system we study a toy model with Hamiltonian  $\hat{\mathcal{H}} = \frac{1}{2} U_s \sum_{i \in e, o} \hat{n}_i (\hat{n}_i - 1) - \frac{1}{K} U_l \hat{\Theta}^2$ , i.e., an extended Bose-Hubbard model where we have neglected tunneling for simplicity. We consider the situation of a fixed number of atoms  $N$  in a box potential, with  $K = N$  lattice sites and an average filling per lattice site of  $\langle \hat{n}_i \rangle = 1$ .  $U_s$  and  $U_l$  denote the strength of short- and global-range interactions, respectively. The global-range interaction term favors a particle imbalance between even and odd lattice sites. It is characterized by the imbalance operator  $\hat{\Theta} = \sum_{i \in e} \hat{n}_i - \sum_{i \in o} \hat{n}_i$ , where  $\hat{n}_i$  counts the number of atoms on lattice site  $i$  and the subindexes  $e$  and  $o$  denote even and odd lattice sites, respectively.

## Significance

**Most structured matter, whether in the form of solids or macromolecules, is found in metastable states. Metastability, as well as the transition processes between metastable states, is ubiquitous in nature, but challenges our tools to describe such complex quantum systems. Using a quantum gas, we assemble a synthetic quantum many-body system featuring metastability. The essential ingredient is a global interaction that couples superfluid shells of the system with a metastable Mott insulator in its core. We study in real time the self-induced switching of the core to a different density configuration, a process reminiscent of the folding between discrete structures encountered in the study of macromolecules.**

Author contributions: L.H., N.D., M.L., T.D., and T.E. designed research; L.H., N.D., and M.L. performed research; L.H., N.D., and M.L. analyzed data; and L.H., N.D., M.L., T.D., and T.E. wrote the paper.

The authors declare no conflict of interest.

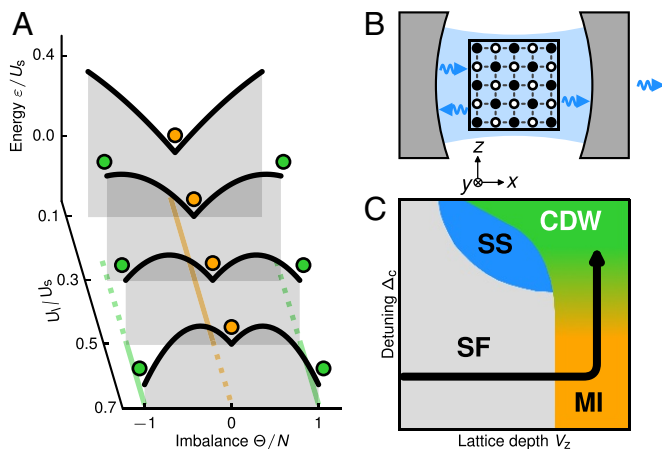
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This article contains supporting information online at [www.pnas.org/lookup/suppl/doi:10.1073/pnas.1720415115/-DCSupplemental](http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.1720415115/-DCSupplemental).

Published online March 8, 2018.



**Fig. 1.** Metastability and system overview. (A) Mean-field results from the toy model. In the presence of short-range interactions  $U_s$  and global-range interactions  $U_l$  atoms placed in a lattice potential can show metastable behavior. States (indicated by circles) can be protected by an energy barrier and the present state of the system depends on its history, leading to hysteresis. The Mott insulator (orange line) and the charge density wave (green lines) are stable (solid), metastable (dashed), or unstable. (B) Our system consists of a Bose-Einstein condensate coupled to a single mode of an optical resonator in the presence of 3D optical lattices. The atoms can create a particle imbalance  $\Theta$  by arranging in a checkerboard pattern which maximizes scattering of photons from a  $z$  lattice (not shown) into the resonator mode. (C) Schematic phase diagram of the system with a superfluid (SF, gray), a lattice supersolid (SS, blue), a Mott insulator (MI, orange), and a charge-density wave (CDW, green) phase. The shaded region between the MI and CDW indicates a region of hysteresis between the phases. The black arrow illustrates the experimental sequence: We prepare the atoms in the SF phase and ramp up the 3D optical lattices to increase  $U_s$ , which brings the system into the MI phase. Subsequently, we carry out a detuning ramp toward cavity resonance which increases  $U_l$ .

We obtain the average ground-state energy per particle  $\varepsilon = \langle \hat{H} \rangle / N$  as a function of the imbalance  $\Theta = \langle \hat{\Theta} \rangle$  for varying  $U_l/U_s$  (Fig. 1A and *Derivation of the Extended Bose-Hubbard Toy Model*). When global-range interactions are weak ( $U_l/U_s < 0.25$ ), the free-energy landscape has a single global minimum at imbalance  $\Theta = 0$  corresponding to an MI with exactly one atom on every lattice site. For  $U_l/U_s > 0.5$  global-range interactions dominate and we find an insulating ground state with a modulated density distribution which we denote CDW. Since the discrete even-odd symmetry of the lattice is broken, the energy landscape shows two global minima at  $\Theta/N = \pm 1$ . In the region around  $U_l/U_s \approx 0.5$  this model shows metastable behavior (31, 32). Here the MI state is a local minimum in the free-energy landscape, separated from the CDW states by an energy barrier, which results from the competition between strong interactions of short- and global-range character.

### System Description

We load a BEC of  $(15-25) \times 10^3$   $^{87}\text{Rb}$  atoms into a harmonic potential centered at the position of the cavity mode. The cloud is split into about 70 weakly coupled 2D layers using an optical lattice of  $(26.2-30.7) E_R^{671}$  depth along the  $y$  axis at wavelength  $\lambda_y = 671.0$  nm (*Calculation of Atomic Density Distributions*). We specify lattice depths in units of the recoil energy  $E_R^\lambda = h^2/(2m\lambda^2)$  for the wavelength  $\lambda$ , where  $h$  denotes Planck's constant and  $m$  is the atomic mass of  $^{87}\text{Rb}$ . The 2D layers are exposed to a square lattice composed of a free-space lattice in the  $z$  direction and an intracavity optical standing wave along the  $x$  direction which is externally applied through the cavity mirrors (Fig. 1B) at wavelengths  $\lambda_x = \lambda_z = 784.7$  nm. In all exper-

iments, the depths of these lattices are tuned simultaneously such that  $V_x \approx V_z$  (*Lattice Calibrations*), but due to the special role of the  $z$  lattice we refer to  $V_z$  throughout the paper. The  $z$  lattice mediates global-range atom-atom interactions of tunable strength  $U_l \propto V_z/\Delta_c$  via off-resonant scattering into the optical resonator mode (21) (*Strength of Effective Atom-Atom Interactions of Global Range*). Here  $\Delta_c$  is the detuning of the frequency of the laser forming the  $z$  lattice from cavity resonance. We estimate a final filling of at most two atoms per lattice site at the center of the cloud in the MI phase. We monitor in real time the flux of photons leaking out of the cavity, using a heterodyne detector (35). The flux is converted into an imbalance  $\Theta \propto \sqrt{n_{\text{ph}}}$ , where  $n_{\text{ph}}$  represents the mean intracavity photon number. For further information on the system see ref. 23 and *Supporting Information*.

### Metastability and Hysteresis

A common method to probe a system for the presence of metastable states is to prepare it in a well-defined state, to provide excess energy, and to observe which states it relaxes to. We accordingly implement such a metastability measurement where we prepare the cloud in an MI state by slowly ramping up the lattices at an initial detuning  $\Delta_c/2\pi = -50$  MHz that corresponds to a negligible strength of global-range interactions  $U_l$ . Subsequently, to provide energy to the system, we quench the initial detuning within 20 ms to a variable endpoint of  $\Delta_c^f$  closer to cavity resonance. The quench increases  $U_l$  while  $U_s$  stays unchanged. Following the quench the system evolves while all experimental parameters are kept constant. A schematic of this sequence is shown in Fig. 1C. We observe that the imbalance  $\Theta$  rises during or after the quench until it settles at a steady-state level  $\bar{\Theta}$ , defined as an average over 10 ms taken 30 ms after finishing the quench (Fig. 2D).

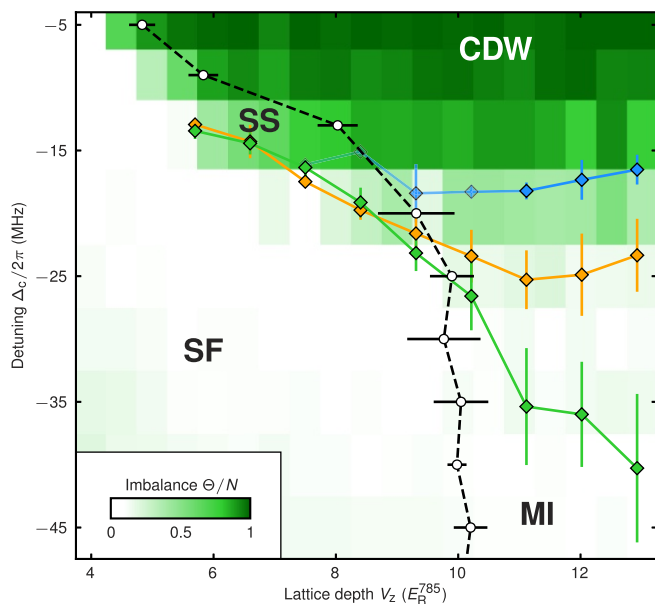
Repeating the experiment, we measure the imbalance  $\bar{\Theta}$  as a function of the final detuning  $\Delta_c^f$  (Fig. 2A-C). Far from resonance ( $\Delta_c^f/2\pi < -24$  MHz), where the strength of global-range interactions is weak, the system consistently ends up at low imbalances (orange) in an interval of  $0 < \bar{\Theta} < 7 \times 10^3$  atoms. Quenching the detuning closer to resonance ( $\Delta_c^f/2\pi \geq -19.5$  MHz), where the strength of global-range interactions is higher, the system is never found to end up within this imbalance interval. We now observe consistently higher imbalances (green) of  $\bar{\Theta} > 7 \times 10^3$  atoms. The two well-separated imbalance intervals (Fig. 2A) coexist for final detunings in an intermediate region ( $-24$  MHz  $\leq \Delta_c^f/2\pi \leq -19.5$  MHz) where the system ends up in a state either of low or of large average imbalance  $\bar{\Theta}$  (*Evaluation of the Metastability Measurement*).

We attribute the observation of two distinct imbalance distributions in our system to the existence of two metastable states. Their separation signals the presence of an energy barrier between the states which does not allow for a continuous connection between them. Our observation of a constant imbalance level after equilibration (Fig. 2D) shows that the final state is long-lived and hence can be either metastable or stable. Monte Carlo simulations for the closed version of the system indeed predict metastable states (32). We observe that this metastability is preserved in our system despite its open character due to the dissipative cavity, which could lead to a fast decay of metastable states.

Metastable behavior in a many-body system is usually associated with hysteresis at phase transitions. When a control parameter is slowly varied back and forth across a critical point, the final state of the system depends on its history. The direct observation of hysteresis provides an indication for the stability of metastable states with respect to parameter changes. We perform such a hysteresis measurement by preparing our system in the MI phase at a lattice depth of  $V_z = 12.9 E_R^{785}$  and again at







**Fig. 6.** Previously extracted transition points superimposed on a phase diagram of the system. Results from the hysteresis measurement: Orange and green diamonds indicate the thresholds where an imbalance is created and where it vanishes during detuning ramps, respectively. The center of the imbalance jump is shown in blue, where transparency indicates the probability of occurrence of the jump. For details on the measurement of the phase diagram, see *Phase Diagram Measurement: Data Evaluation*. White data points and the associated black dashed line indicated the loss of coherence, from left to right, which we infer from the measured BEC fraction, and green tiles indicate states with nonzero imbalance. We identify a superfluid (SF), a lattice supersolid (SS), an MI, and a CDW phase. This experiment was performed with  $16(1) \times 10^3$  atoms at maximum lattice depths of  $(V_x, V_y, V_z) = (15.7 E_R^{785}, 26.2 E_R^{671}, 12.9 E_R^{785})$ . For further details see ref. 23 and *Phase Diagram Measurement: Data Evaluation*. Error bars are SD (*Phase Diagram Measurement: Data Evaluation* and Fig. 5A).

the parity of the CDW state, indicated by a well-defined and constant phase of the measured light field (40), shown in Fig. 4C. We attribute the initial imbalance increase (i) to a rearrangement of surface atoms. From the experimental parameters of the metastability measurement, we theoretically estimate a number of surface atoms of  $N_{\text{surf}} \approx (4-8) \times 10^3$  (*Calculation of Atomic Density Distributions*), which is in agreement with the initial imbalance increase (i). Photons scattered at these atoms into the cavity mode generate an energy offset  $\delta_{\text{off}}$  between even and odd sites (Fig. 5B). This offset eventually drives the bulk system from a metastable MI to a CDW state, which we link to the fast imbalance jump (ii). However, we do not observe an imbalance jump when ramping the detuning back to the starting value in ramp II (Fig. 3), which we mainly attribute to the cloud being heated.

### Microscopic Dynamics and Energy Redistribution During the Imbalance Jump

A simplified microscopic picture of the imbalance dynamics following the detuning quench is sketched in Fig. 5A, where the system is broken into a collection of coupled double wells. In the initial MI state, bulk atoms occupy both sites of each double well. This state is labeled  $|1, 1\rangle$ , where  $|n_e, n_o\rangle$  denotes the filling on the even and odd sites, respectively. Here, on-site interactions of strength  $U_s/2\pi = 2.2(1)$  kHz provide an energy barrier for neighboring atoms, thus suppressing tunneling into a  $|2, 0\rangle$  state. The barrier softens but persists as surface atoms generate an imbalance  $\Theta$  and a site offset  $\delta_{\text{off}}$ . Monitoring the flux of photons leaking from the cavity, we observe  $\delta_{\text{off}}/2\pi = 1.6(2)$

kHz just before the imbalance jump (ii) happens (*Extraction of the Even-Odd Particle Imbalance  $\Theta$  and Site Offset  $\delta_{\text{off}}$  from the Measured Photon Flux*). The harmonic trapping potential causes an additional site offset of  $0 \text{ kHz} \leq \delta_{\text{trap}}/2\pi \leq \delta_{\text{trap}}^{\text{max}}/2\pi = 0.6$  kHz, increasing from the center outward. When  $\delta_{\text{off}} + \delta_{\text{trap}}^{\text{max}} \approx U_s$ , the outermost bulk atoms start resonantly tunneling to their neighboring lattice sites. They further increase  $\Theta$  and  $\delta_{\text{off}}$ , successively allowing more and more atoms to resonantly tunnel. The imbalance jump (ii) thus results from an avalanche of resonant tunneling processes of bulk atoms which stops only once  $\delta_{\text{off}} - \delta_{\text{trap}}^{\text{max}} > U_s$ . Indeed, we find  $\delta_{\text{off}}/2\pi = 2.7(3)$  kHz at the end of the jump.

We describe each resonant tunneling process by a Landau-Zener transition, shown in Fig. 5A. The  $|1, 1\rangle$  and  $|2, 0\rangle$  states are coupled with strength  $\sqrt{2}t$ , where the tunneling  $t$  is bosonically enhanced by a factor of  $\sqrt{2}$ . We find an upper bound for the probability of adiabatic Landau-Zener transfer of about 60%, which is determined by the measured rate of change of  $\delta_{\text{off}}$  during the imbalance jump, shown in Fig. 5B. As all experimental parameters are held constant after the quench, the site offset  $\delta_{\text{off}}$  is solely tuned by the reordering atoms. The timescale and (non)adiabaticity of the Landau-Zener transitions is thus inherently determined by the system evolving nonlinearly due to the presence of the global-range interactions.

At the beginning of the imbalance jump (ii), the ground state of the system is the CDW state. The bulk is, however, still in the MI state, which is now a highly excited state of energy  $E_1$ . During the imbalance jump (ii) each double well in the bulk evolves via nonadiabatic Landau-Zener transfers to a superposition of  $|1, 1\rangle$  and  $|2, 0\rangle$  states. On top of the imbalance created previously by superfluid surface atoms, the redistributing bulk increases the imbalance further, allowing the system to lower the excitation energy by  $\Delta E$ . We infer  $\Delta E = 7.7(2.1)$  MHz from the imbalance jump (ii) in the metastability measurement (*Extraction of the Change in Excitation Energy  $\Delta E$  from the Measured Photon Flux*) (Fig. 5C). This process is sketched using our toy model, where a symmetry-breaking field is present due to the imbalance created by superfluid surface atoms.

To study the energy budget of the system we consider two scenarios. If the system was closed, the total energy could not change, and the reduction in excitation energy  $\Delta E$  would be balanced by an increase in kinetic energy of the system. Since our system is inherently open, the energy could also be dissipated by leaking cavity photons. We make use of the spectrum of these photons to distinguish the two cases. We estimate the number of scattered photons during the imbalance jump (ii) to be about  $12(3) \times 10^3$  (*Number of Photons Scattered During the Imbalance Jump*), where each photon would have to dissipate at least  $0.6(3)$  kHz of energy. This would leave a notable signature in the photon spectrum, which is not observed. While our heterodyne detection cannot rule out processes where only few photons dissipate all of the energy, such a collective scattering process seems unlikely. Hence we conclude that the excitation energy released during the jump (ii) remains in the system and is transformed into kinetic and interaction energy (*Energy Stored in the Superfluid Surface and the Insulating Bulk During the Imbalance Jump*).

### Phase Diagram

The observation of metastable states, a coexistence of phases, and a jump in the order parameter are typical features of first-order phase transitions. We thus want to relate our observations to a phase diagram of the system measured as in ref. 23 (Fig. 6). Here, we superimpose the thresholds extracted in the hysteresis measurement on the phase diagram.

The threshold for the creation of an imbalance (orange diamonds in Fig. 6) coincides with the appearance of an imbalance

in the phase diagram (green tiles in Fig. 6). The center position of the fast jump (blue diamonds in Fig. 6) is located within a region of intermediate imbalance present in the phase diagram at  $\Delta_c/2\pi \approx -20$  MHz (light green tiles in Fig. 6). The threshold for the disappearance of an imbalance (green diamonds in Fig. 6) extends deep into the MI region (white tiles in Fig. 6). The associated blue and green lines enclose an area where the MI and the CDW phases can coexist and where hysteresis is observed. In addition, we find the parameter regime where the system can fall into either of the two final states in the metastability measurement (Fig. 24) to lie close to the blue line (Fig. 6).

## Conclusion and Outlook

Using the unique real-time access of our experiment, we observed long-lived metastable phases and hysteretic behavior at a first-order quantum phase transition between an MI and a CDW phase. Owing to the nonlinearity stemming from the global-range interactions, the system develops its own timescale when

quenched across the phase transition. The resulting dynamics of spatially reordering atoms point to an avalanche of resonant tunneling processes taking place, which render the transition out of the metastable state inherently nonadiabatic. The observed lack of energy dissipation during the transition poses questions about the thermalization of the final state. Our work provides a unique approach to study dynamics and thermalization processes in open quantum many-body systems.

**ACKNOWLEDGMENTS.** We acknowledge insightful discussions with Frederik Görg, Sebastian Huber, Katrin Kröger, Gabriel T. Landi, Giovanna Morigi, Helmut Ritsch, André Timpanaro, Päivi Törmä, Sascha Wald, and Wilhelm Zwerger. We acknowledge funding from Synthetic Quantum Many-Body Systems (a European Research Council advanced grant) and the European Union Collaborative Project Thermodynamics of Mesoscopic Quantum Systems (Grant 618074). We also acknowledge State Secretary for Education, Research and Innovation support for Horizon2020 project Quantum Simulations of Insulators and Conductors; Swiss National Science Foundation support for National Center of Competence in Research Quantum Science and Technology; and German–Austrian–Swiss Lead Agency process DACH project “Quantum Crystals of Matter and Light.”

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