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Local interactions and self-organized spatial patterns stabilize microbial cross-feeding against cheaters

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Mutualisms are ubiquitous, but models predict they should be susceptible to cheating. Resolving this paradox has become relevant to synthetic ecology: cooperative cross-feeding, a nutrient-exchange mutualism, has been proposed to stabilize microbial consortia. Previous attempts to understand how cross-feeders remain robust to non-producing cheaters have relied on complex behaviour (e.g. cheater punishment) or group selection. Using a stochastic spatial model, we demonstrate two novel mechanisms that can allow cross-feeders to outcompete cheaters, rather than just escape from them. Both mechanisms work through the spatial segregation of the resources, which prevents individual cheaters from acquiring the resources they need to reproduce. First, if microbe dispersal is low but resources are shared widely, then the cross-feeders self-organize into stable spatial patterns. Here the cross-feeders can build up where the resource they need is abundant, and send their resource to where their partner is, separating resources at regular intervals in space. Second, if dispersal is high but resource sharing is local, then random variation in population density creates small-scale variation in resource density, separating the resources from each other by chance. These results suggest that cross-feeding may be more robust than previously expected and offer strategies to engineer stable consortia.

1. Introduction

Mutualisms are common [[1](#page-11-0)]. For example, cooperative cross-feeding, a nutrientexchange mutualism that is ubiquitous among microbes, has been observed in communities including the open ocean (diatoms and bacteria exchanging vitamin B-12 for carbon [\[2\]](#page-11-0)), and the gut microbiomes of animals such as humans (bacteria exchange acetate for xylose [[3](#page-11-0)]), bees (bacteria exchange lactate for pyrimidines and B-vitamins [[4](#page-11-0)]) and termites (bacteria exchange hydrogen for vitamins [[5](#page-11-0)]). However, models suggest that many mutualisms will be susceptible to cheaters, who receive the benefit of a mutualism without paying the cost of helping their partner [\[1,6](#page-11-0)–[9](#page-11-0)]. For example, many metabolites are costly to produce [\[10,11\]](#page-11-0); therefore, if cross-feeders share resources freely, then individuals may benefit from not making resources. Left unchecked, each species will evolve towards non-production until the mutualism collapses [[7,12](#page-11-0),[13\]](#page-11-0). Thus, why cross-feeding and other mutualisms are robust to cheating is a long-standing question [[1](#page-11-0)]. In this paper, we examine mechanisms that allow cross-feeders to resist cheaters.

Cheaters in a cross-feeding mutualism may require resources from multiple mutualists [[14\]](#page-11-0). This is unusual among mutualisms: for example, in pollination mutualism, cheaters never require both nectar and pollen transportation. We

suspect that cheaters who rely on multiple mutualists are more common among microbes. Microbes produce a variety of public goods and services, including environmental detoxification [[15\]](#page-11-0), biofilm formation [\[16](#page-11-0)] extracellular products [\[17](#page-11-0)], and, of course, cross-feeding resources [[2](#page-11-0)–[5](#page-11-0)]. Thus, it is feasible that microbes could cheat at multiple functions. This work will thus help us understand how microbial mutualisms differ from non-microbial mutualisms.

Space is thought to be important for allowing crossfeeding and other mutualisms to persist [[9](#page-11-0),[18,19\]](#page-11-0). Many studies have shown that mutualisms can persist by becoming segregated from cheaters [[8,9,13,14](#page-11-0),[20](#page-11-0)-[23\]](#page-12-0). Segregation typically occurs when individuals have long-term interactions within small groups [\[13,14,20,21](#page-11-0)]. This phenomenon can be understood using the multilevel selection framework [\[12](#page-11-0),[24\]](#page-12-0): individual cheaters will have an advantage within a group; however, groups with too many cheaters will collapse, and groups with few cheaters will tend to form new groups. Thus, whether cheaters dominate depends on the relative importance of an individual-level and group-level selection. Group selection that maintains cooperation has been called partner fidelity feedback [\[23](#page-12-0)].

Partner fidelity feedback relies on two key properties of space. First, interactions must be local (resources are shared within a group or small neighbourhood), so cheaters strongly affect their neighbours. If interactions are widespread and diffuse, then an individual's contribution will have little effect on others, and there will not be an immediate consequence of cheating. Second, microbes must have long-term interactions, ideally across generations; otherwise, a cheater could damage a local community and then leave (or disperse its offspring away) without consequences.

Though most studies have focused on partner fidelity feedback, space may promote cross-feeding in other ways. For example, mutualists can become segregated from the cheaters if cheaters disperse farther than mutualists [\[8\]](#page-11-0). However, these results still rely on the mutualists becoming segregated from the cheaters, rather than other aspects of the spatial structure. As far as we know, no studies have examined how spatial factors can allow cross-feeders to become competitively superior to cheaters.

Understanding how cross-feeding persists is of practical use in synthetic ecology. A goal of synthetic ecology is to grow multi-species consortia of engineered microbes [\[18](#page-11-0),[25,26\]](#page-12-0). One proposed strategy for stabilizing coexistence is to make the microbes cross-feed, so they rely on one another [\[27](#page-12-0) –[30\]](#page-12-0). However, if there is selection for nonproduction, then such consortia may be short-lived. Some have proposed to counter this selective pressure using active behaviours that harm cheaters, such as quorum sensing or cheater punishment [\[31](#page-12-0)]. However, such behaviours may be challenging to engineer (but see [\[32](#page-12-0)]) and could themselves be selected against [\[18](#page-11-0)]. This problem has lead some to ask whether simpler and more passive mechanisms—such as those relying on population dynamics alone—are possible [[18\]](#page-11-0).

Here we use a stochastic spatial model to study how spatial processes affect whether cross-feeders can be robust to cheaters. As expected, we find that if cross-feeders have loose, short-term associations, then they are susceptible to cheating, and if they have tight, long-term associations, then they persist via partner fidelity feedback. Additionally, we demonstrate two novel ways that space can stabilize

mutualism: cross-feeding can be stabilized by long-term associations, even when interactions are diffuse; and they can be stabilized by localized interactions, even when interacting with random partners. Both mechanisms are driven by population dynamics alone, without the need for complex behaviours. They allow the cross-feeders to be competitive dominants, rather than fugitive species who persist by escaping from cheaters.

2. Model summary

We modelled microbes competing for sites on a lattice ([figure 1\)](#page-2-0). Our consortium contains cross-feeding species 1 and 2 that produce resources 1 and 2, respectively, and a cheater that produces neither resource ([figure 1](#page-2-0)a). Each cross-feeder produces quantity Q of its shared resource, and shares it equally with every individual within d_{res} sites in each direction (known as a Moore neighbourhood of distance d_{res} [[33\]](#page-12-0)), [figure 1](#page-2-0)b. Thus, the concentration of each resource at a site x , R_{1x} and R_{2x} for resources 1 and 2, will equal Q times the number of species 1 and 2 microbes within d_{res} sites in any direction, i.e.

$$
R_{1x} = \frac{Q}{(2\ d_{\text{res}} + 1)^2 - 1} \sum_{y \in d_{\text{res}}} N_{1y}
$$

and
$$
R_{2x} = \frac{Q}{(2\ d_{\text{res}} + 1)^2 - 1} \sum_{y \in d_{\text{res}}} N_{2y}
$$
 (2.1)

where the summation is over the $(2d_{res} + 1)^2 - 1$ sites within d_{res} sites of x, and N_{1v} and N_{2v} are 1 if a site y is occupied by a species 1 or 2 microbe (respectively) and 0 otherwise ([figure 1](#page-2-0)b). Sharing resources uniformly is not a perfect representation of diffusion, because the resources are not concentrated at the source; however, it is a common simplifying assumption in stochastic spatial models because it is a tractable way to represent neighbourhood interactions [\[33](#page-12-0)].

We assume that each microbe's reproductive rate is determined by the rarer essential resource (i.e. Liebig's Law of the minimum [\[27](#page-12-0),[34\]](#page-12-0)). Thus, a microbe that is constrained by resource 1 limitation will not benefit from additional of resource 2. There is evidence for this in some primary producer systems [\[35](#page-12-0)]; we are not aware of tests in cross-feeding bacteria. We assume each cross-feeder makes enough of its own resource that that resource is never limiting. Thus, a cross-feeder produces offspring at a rate equal to its birth rate (b_1 or b_2) times the availability of the resource it does not make (R_{1x} or R_{2x} at site x) [[27,36\]](#page-12-0). Therefore, during a time period of length Δt , a species 1 microbe will produce an average of $b_1R_{2x}\Delta t$ offspring, and a species 2 microbe will produce an average of $b_2R_{1x}\Delta t$ offspring. The cheater has a higher birth rate (i.e. $b_0 > b_1$ and b_2), but because it does not produce either resource, its reproductive rate is proportional to the rarer essential resource. Thus, during a time period of length Δt , a cheater microbe will produce an average of b_0 min(R_{1x} , R_{2x}) Δt offspring. Therefore, the cheater has a higher reproductive rate than at least one cross-feeder at every site, and if both resources are similarly abundant, it will have a higher birth rate than both cross-feeders.

When a microbe reproduces, its offspring disperses to a random site in a Moore neighbourhood of d_{mic} ([figure 1](#page-2-0)c). If that site is empty, the microbe survives, but if the site is occupied, then the microbe dies [[33\]](#page-12-0). Thus, if E_x is the fraction

3

Figure 1. Model structure. (a) Species 1 and 2 produce resource 1 and 2, respectively. The cheater (species 0) produces neither resource. (b) Microbes take up resources from neighbours within a Moore neighbourhood of distance d_{res} (i.e. all sites within d_{res} sites in any direction, including diagonal). Here, the starred individual gains resource 2 from the five species 2 microbes within two sites; thus, $R_{2x} = 5Q/24$. (c) Newly born microbes disperse to a random site within a Moore neighbourhood of distance d_{mic} and survive if that site is empty. Here, offspring of the starred individual will survive if they disperse into one of the three adjacent sites that are unoccupied; thus, $E_x = 3/8$.

of sites near x that are unoccupied, then a species 1 microbe will produce an average of $b_2R_{1x}E_x\Delta t$ offspring in Δt units of time. Empty sites act as a proxy for all other limiting resources besides resource 1 and 2 in our model.

All microbes die at density-independent rate δ , immediately freeing their site. Unused resources are degraded or removed from the system each time step.

2.1. Model analysis

We analysed the effect of cheaters by determining if they could invade an established pair of cross-feeders and either displace or coexist with them. As we show below, the system crashes in the absence of either cross-feeder, as expected in an obligate mutualism [[36\]](#page-12-0); thus, our methods differed slightly from a traditional invasion analysis. Instead, we allowed species 1 and 2 to establish and then introduced a small number of cheaters. Cheaters were introduced once, but at high enough density that extinction from demographic stochasticity was unlikely [[37\]](#page-12-0). We determined whether, after thousands of generations, the species coexisted (i.e. all species persisted), the cross-feeders displaced the cheaters (i.e. the cheater went extinct while the cross-feeders persisted) or the community crashed (i.e. all species went extinct).

Most of our analysis was done using simulations. Details as to how the model was implemented are described in appendix A. We also considered a mean field version of this model, which we analysed using differential equation (appendix B). Additional analyses on the spatial properties of the community are reported in appendix C.

3. Results

The two parameters that determine the impact of space are resource sharing distance, d_{res} , and microbe dispersal distance, d_{mic} . Resource sharing distance determines how diffuse the interactions are. A low d_{res} means microbes have strong interactions with few neighbours and a high d_{res} means microbes have diffuse interactions with many neighbours. Microbe dispersal determines partner associations. Low d_{mic} means offspring will not disperse far, and will therefore have similar neighbours as their parents. In this case, there is a strong connection between a microbe's density and the local conditions, because microbes will build up in good areas. High d_{mic} means that microbes will have random neighbours and that local abundance is due to random dispersal rather than local conditions.

Our model produced four qualitatively different outcomes, depending on whether d_{res} and d_{mic} were large or small ([figure 2](#page-3-0)). We explain each case separately.

3.1. Non-spatial dynamics (high d_{res} and d_{mic})

If resources are shared over long distances and offspring disperse far (high d_{res} and d_{mic}), then microbes have weak interactions with many random neighbours, so spatial processes have little effect. Our simulations suggest that in this case, cheaters always collapse the cross-feeding community ([figure 2](#page-3-0)).

By assuming that $d_{res} \rightarrow \infty$ and $d_{mic} \rightarrow \infty$, we derive a mean-field model to understand the well-mixed case (appendix B). This acts as a baseline for understanding how space alters community dynamics. Well-mixed communities are highly susceptible to cheaters (figures [2](#page-3-0), [3](#page-4-0) and [5\)](#page-6-0). A wellmixed community with cross-feeders but not cheaters has at most two stable equilibria—extinction and coexistence ([figure 3](#page-4-0)a). The shared resources create a positive feedback [[28,36\]](#page-12-0): if cross-feeders are rare, then each will be too resource-limited to reproduce, and their densities will decline further; however, if cross-feeders are common enough, then sufficient resources will be produced, and the cross-feeders will grow until they are limited by space ([figure 3](#page-4-0)b). The cheater can invade a community of cross-feeders, because both resources are readily available and the cheater has a higher birth rate ([figure 3](#page-4-0)c, appendix B). As the cheaters become abundant, they displace the cross-feeders, until the cross-feeders become too resource limited to reproduce, and the consortium crashes [\(figure 3](#page-4-0)d).

3.2. Partner fidelity feedback (low d_{res} and d_{mic})

If microbes share resources with a few neighbours and have short-range dispersal (low d_{res} and d_{mic}), then a microbe's resource production has a strong impact on the local conditions and species will tend to build up in favourable

Figure 2. Community patterns as a function of resource sharing and microbe dispersal distances. Each square represents a community 5000 time units after a cheater was introduced. Communities that are all white are those in which the cheater drove everyone extinct. Repeated simulations gave consistent results, except that the stripes have different orientations each time, and communities with moderate d_{res} and d_{mic} sometimes randomly go extinct. Here, $b_1 = b_2 = 0.6$, $b_0 = 0.7$, $\delta = 0.15$, $Q = 6.5$, and the domain is 200 \times 200 sites. (Online version in colour.)

locations. In this case, cross-feeding is stabilized by partner fidelity feedback (i.e. strong group selection [\[12](#page-11-0)]). Here, local communities behave similarly to the global community in the non-spatial case: individual cheaters will reproduce and grow if they are surrounded by cross-feeders; however, as the cheaters become locally abundant, they will displace the cross-feeders, become too resource-limited to reproduce, and cause the local population to crash. Cross-feeders can persist when there is a dynamic spatio-temporal mosaic, where groups of cross-feeders bud off and grow into empty sites, temporarily escaping the cheaters (figure $4a$, c , electronic supplementary material, movie A1). Thus, cheaters have a within-group competitive advantage [\(figure 4](#page-5-0)b and [6](#page-6-0)), but groups of cross-feeders have an advantage ([figure 7](#page-7-0)).

3.3. Pattern formation (high d_{res} and low d_{mic})

If offspring disperse short distances (low d_{mic}) but resources are shared over long distances (high d_{res}), then microbes will build up where the conditions are most favourable, but individuals will have little impact on local resource levels. Group selection has little effect here: a cheater could build up in a good environment without consequences (at least until a huge area collapses). Nonetheless, our simulations show that cross-feeders are robust to cheaters under these conditions (figures 2 and [5](#page-6-0)), showing that a novel mechanism is occurring.

This novel mechanism occurs because when d_{mic} is low and d_{res} is high, cross-feeders self-organize into regular spatial patterns [\[38](#page-12-0)] (figures 2 and [4](#page-5-0)d; electronic supplementary material, movie A2). Both striped and spotted patterns are possible (figure 2). These patterns form because the resource a cross-feeder produces is most abundant where the producer is not. To see this, consider a species 1 (blue) stripe in [figure 4](#page-5-0)d. The resource they produce is shared over a distance slightly more than the width of a stripe, so most of the resource 1 is produced locally rather than being shared from neighbouring stripes. However, the species 1 stripe is surrounded by two species 2 (green) stripes, each of which produces resource 2 that is shared across most of the blue stripe. Thus, resource 2 will be more abundant in a species 1 stripe (figure $4e$). Because species 1 is limited by resource 2, it has a higher reproductive rate in the middle of its own stripe. Similarly, species 2 has a higher reproductive rate in its own stripe. Because of local dispersal, each population builds up where it grows best, thus providing positive feedback that reinforces the regular spatial pattern.

Cheaters cannot persist in areas with a shortage of either resource, because they will have a lower reproductive rate than one of the cross-feeders. For example, a cheater in the core of a species 1 stripe will be limited by resource 1, whereas a species 1 microbe in that area will be limited by the more abundant resource 2 (figures [4](#page-5-0)e and [8](#page-8-0)). If this effect outweighs the cheater's inherent birth rate advantage, then the cheater will have a lower reproductive rate than the species 1 microbes and will be excluded from the core. The only place that cheaters have a competitive advantage is at the interface between stripes or spots, because both resources are similarly abundant there ([figure 4](#page-5-0)e). Thus, there may be some group-level selection at the edges between

Figure 3. Results of the mean-field model. (a) A system without cheaters will have at most three equilibria: a stable extinction equilibrium, a stable positive equilibrium and an unstable equilibrium separating them. (b) If the cross-feeders begin at a density above the unstable equilibrium, they will converge on the positive equilibrium. If they begin below the unstable equilibrium, they go extinct. (c) If a cheater is introduced, the positive equilibrium becomes unstable, and no new equilibria are created. (d) Thus, cheaters drive the cross-feeders extinct and then die off. In each figure, $b_1 = b_2 = 0.6$, $b_0 = 0.7$, $Q = 4$ and $\delta = 0.15$. (Online version in colour.)

stripes; however, cross-feeders gain an individual-level advantage over much of the environment [\(figure 8\)](#page-8-0). Thus, spatial pattern formation can allow the cross-feeders to coexist with, or even exclude the cheater [\(figure 2](#page-3-0)).

A similar pattern occurs when spots form: blue spots are blue because they receive green resources from four neighbours, and the cheater dominates between the spots (because resource densities are similar), electronic supplementary material, movie A4.

3.4. Neighbour uncertainty (low d_{res} and high d_{mic})

If offspring disperse long distances (high d_{mic}), but resources are shared over short distances (low d_{res}), then microbes will interact with a small, random subset of the community and their associations will be completely different from their offspring. Group selection has little effect here: a cheater will depress the growth rates of its neighbours and a crossfeeder will increase the growth rates of its neighbours, but the offspring of both will experience totally different conditions. Thus, a cheater could degrade a local community without its offspring suffering the consequences. Nonetheless, simulations again show that cross-feeders can persist under these conditions (figures [2](#page-3-0) and [5\)](#page-6-0), showing that another novel mechanism is occurring.

This novel mechanism, which we call neighbour uncertainty, occurs because highly localized interactions will cause resources to segregate, even if associations are completely random. If resources are shared over short distances, then small-scale variation in population density will lead to small-scale variation in resource availability [[39\]](#page-12-0). For example, if microbes receive resource from eight neighbours (i.e. $d_{res} = 1$) and species 1 occupies 20% of sites, this does not mean that every microbe will have 1.75 species 1 neighbours; instead, some will have two or three, others will have one or zero. As a result, many sites will have less of resource 1 or resource 2 by chance (figure $4g,h$). Such variation hurts cheaters, because they need to obtain both resources from neighbours to reproduce. Intuitively, imagine that microbes are distributed randomly, and that each resource is at above-average concentration in half of the sites; in this case, individual cheaters will benefit in the 25% of sites where both compounds are at above-average concentration, but be hindered in the 75% of sites where at least one resource at below-average concentration. Thus, on average the cheater will be hindered. This effect is strongest when $d_{res} = 1$, because resource variation is highest, but it still occurs at larger d_{res} : [figure 8](#page-8-0) shows that that the cheater is harmed by resources being separated when $d_{\text{mic}} \geq 9$ and $d_{\text{res}} \leq 5$, and [figure 9](#page-8-0) shows that this effect is not due to spatial structure. Neighbour uncertainty does not harm the cross-feeders: species 1 will benefit in areas where compound 2 is abundant and be hindered where compound 2 is rare, but there is little effect on average. Therefore, most cheaters will be more resource

Figure 4. Microbe and resource distribution under each mechanism. (a) The distribution of microbes with localized interactions ($d_{\text{res}} = 9$) and dependable associations ($d_{\text{mic}} = 7$). (b) The relative density of resources at each site in a. Green and blue areas (lighter and darker areas if in greyscale) indicate that species 1 and 2 has an advantage, respectively (i.e. because $b_0/b_2 \approx 1.13$). (c) Temporal dynamics in the black square in a. (d–f) are analogous to $a-c$, but with diffuse interactions ($d_{\text{res}} = 25$) and but dependable associations ($d_{\text{mic}} = 3$). Cheaters could not persist here. ($g - i$) are analogous to $a - c$, but with localized interactions $(d_{res} = 3)$ and random associations ($d_{mic} = 15$). Parameters are the same as [figure 2.](#page-3-0) (Online version in colour.)

limited than most of the cross-feeders. When this effect is strong enough, the cheater will be at a competitive disadvantage relative to the cross-feeder in most sites (figure 4h). Thus, this mechanism can allow the cross-feeders to exclude or coexist with cheaters [\(figure 2](#page-3-0) and 4i).

4. Discussion

How mutualisms such as cross-feeding persist in a world of cheating is a fundamental problem of evolutionary ecology. Spatial factors are often seen as an important explanation [\[9,18,19\]](#page-11-0). Studies to date have focused on how spatial factors can allow cross-feeders to escape from cheaters [\[8,9](#page-11-0),[13](#page-11-0),[14,20](#page-11-0)–[22\]](#page-11-0). Here, we show two novel mechanisms by which cross-feeding is maintained by space. Both mechanisms create individual-level selection for cross-feeding, and can allow cross-feeders to outcompete cheaters ([figure 2](#page-3-0)). These results thus parallel models of within-species cooperator/ cheater dynamics, which suggest spatial factors can cause 'cooperative' traits to be beneficial for selfish reasons [\[40,41](#page-12-0)].

First, if microbes can build up where conditions are most beneficial to them but have weak, large-scale interactions, then cross-feeders will become self-organized into regular stripes or spots (figure 4d). Each individual stripe or spot has a local shortage of one resource, which limits the growth of cheaters (figure 4e). A few previous studies have shown pattern formation in a mutualist –exploiter system [[8,20](#page-11-0)]; however, in those models the mutualists persisted by escaping their cheaters, rather than outcompeting them.

Figure 5. Robustness to cheaters. We calculated the maximum birth rate (b_0) that a cheater could have without driving a community of cross-feeder extinct. The larger this number is, the more robust the community is to cheaters. Each simulation was run with $b_1 = b_2 = 0.6$, $\delta = 0.15$, $Q = 6.5$ and a community size of 200×200 sites.

Figure 6. Whether cross-feeders and cheaters partition sites. We correlated the cheater's reproductive rate (B_{0x}) with each cross-feeder's reproductive rate (B_{1x} and B_{2v} across all sites for each community in microbes in [figure 2](#page-3-0). Cells display the average of both correlations. Values close to 1 indicate that sites were generally good or bad for every species. Values close to 0 indicate that many sites were good for a cross-feeder but bad for the cheater.

This mechanism seems most likely to occur in biofilm systems, especially if shared compounds can diffuse across many fixed microbes. Indeed, many biofilms have been shown to form patterns [[42\]](#page-12-0).

Second, if microbes have strong interactions with a few neighbours, but those neighbours are random, then cheaters will often experience a local shortage of one resource [\(figure 4](#page-5-0)h). This harms the cheater, because not synthesizing any essential resources is a poor strategy when resources are uncertain. A recent study suggested a similar phenomenon in a model where microbes had random, long-term interactions [\[14](#page-11-0)]. This mechanism seems most likely to occur in systems that are well-mixed (e.g. the open ocean) and where compounds quickly degrade (so compound densities vary).

Pattern formation and neighbour uncertainty work in fundamentally the same way: the two essential resources are separated in space, leaving individual cheaters limited by one resource and at a disadvantage relative to one of the cross-feeders. Each mechanism achieves this effect by different means. Under pattern formation, population dynamics arrange the cross-feeders such that there is regular, large-scale variation in resource density [\(figure 4](#page-5-0)e). Under neighbour uncertainty, localized interactions create random, small-scale variation in resources ([figure 4](#page-5-0)h), without the need for self-organization. Thus, artificially mixing the system will harm cross-feeders that persist via pattern formation, but not those that persist via random localized interactions ([figure 9\)](#page-8-0). In fact, neighbour uncertainty appears

Figure 7. Whether microbes are near the resources they need. (a) We calculated the reproductive rate of each cross-feeder at each site (i.e. B_{1x} or B_{2x}), using the communities in [figure 2.](#page-3-0) We subtracted the mean of this value across all sites from the mean in only sites where that microbe was found. If this difference was positive, then randomly moving a microbe would reduce its reproductive rate. Each result is the average value for both cross-feeders. (b) We calculated the same value for each cheater (i.e. B_{0x}). Communities without cheaters are labelled with an X, because we could not measure the effect of sites they occupy if they are absent. (c) We subtracted the values in b from those in a. When that difference was positive, it indicated that the cross-feeders were more likely to be in favourable locations, compared to the cheater.

Figure 8. Amount that the cheater was limited because the resources were separated. We calculated the cheater's average reproductive rate (B_{0x} , averaged across all sites) for each community in [figure 2](#page-3-0). We divided this value by what the average would have been if under well-mixed conditions (i.e. $d_{\text{res}} \rightarrow \infty$). Lower values indicate that the cheater was highly limited because each resource was found in different areas, and higher values indicated that both resources tended to have similar values. The cross-feeders have a birth rate disadvantage of $b_2/b_0 \approx 0.88$; therefore, if the cheater and cross-feeders are coexisting, we expect the cheater's reproductive rate to be reduced by about 12% (less if spatial structure is important, [figure 7\)](#page-7-0).

Figure 9. Amount that a cheater would benefit if spatial structure was disrupted. We calculated the cheater's average reproductive rate (B_{0x} , averaged over all sites) for each community in microbes in [figure 2.](#page-3-0) We then randomly rearranged the microbes, and re-measured the mean of B_{0x} . The heat map shows how much the mean of B_{0x} increased in the rearranged community, and thus quantifies how much spatial structure hindered the cheaters.

to function whenever d_{res} is small, and thus works in tandem with partner fidelity feedback [\(figure 6\)](#page-6-0).

The second difference between these mechanisms is how dependably cross-feeders find themselves in favourable locations. Under pattern formation, individuals of species 1 are almost always in areas beneficial to species 1 (figures [4](#page-5-0)d and [7\)](#page-7-0); thus, cross-feeders can exclude cheaters when the effect of resource limitation is weak. Under neighbour uncertainty, individuals of species 1 are equally likely to be in areas beneficial to species 1 or species 2 (figures [4](#page-5-0)g and [7](#page-7-0)); thus, the effect of resource limitation on the cheaters must be much stronger for the cross-feeders to maintain dominance. This is why cheaters are excluded in [figure 4](#page-5-0)d, but not [figure 4](#page-5-0)g, even though resource limitation is similar in both communities (figure 8).

Like any model, our results are based on the specific assumptions we used, such as uniform dispersal and cheaters being limited by the rarest resource (i.e. Liebig's Law). The critical assumptions needed to produce neighbour uncertainty are (i) microbes interact with a small number of neighbours, (ii) the microbes associate randomly, and (iii) a cheater who is limited by one resource gains less benefit from taking up the other resource. Thus, we expect neighbour uncertainty to be robust to our assumptions: any resource

sharing kernel should produce ingredient (i) if it is shortranged, any rapid and random movement should produce ingredient (ii) [\[39](#page-12-0)], and many concave uptake functions should produce ingredient (iii). Our model assumed that resource levels quickly equilibrate, rather than building up when not used. It is not clear whether this assumption increased or decreased the between-site variation in resource density. If it decreased between-site variation, then a model with slower resource removal could actually have stronger effect of neighbour uncertainty.

The critical assumptions needed to produce pattern formation are (a) microbes disperse short distances, (b) a cheater who is limited by one resource gains less benefit from the other resource and (c) the resource sharing kernel must be shaped such that it is better to be at an intermediate distance from two partners than right next to one partner. Ingredients (a) and (b) should be easy to produce, but some sharing kernels will probably not produce (c); for example, preliminary simulations suggest that Gaussian kernels may not have that property. We expect that if (c) does not hold, then patterns will not be stable because the most abundant resource in a stripe or spot will be the one produced by the microbes there. Future studies should determine how robust this mechanism is to different resource sharing kernels.

Both novel mechanisms work because cheaters need both resources. Thus, we suspect that if a cheater only needed only one resource, and could make the other resource without sharing it, then the novel mechanism will fail. It is not unreasonable to assume that microbes cannot produce a resource without sharing it: many microbes excrete compounds to maintain homeostasis, and all microbes excrete compounds when they lyse [\[11](#page-11-0)]. More generally, detoxification, biofilm production and many other microbial functions produce some public benefit [\[11](#page-11-0)]. Thus, we feel the assumption that cheaters need both mutualists is valid for some microbial mutualisms (though unlikely for non-microbial mutualisms). Future studies should examine how leaky traits must be for our mechanisms to function.

Our results suggest novel ways that cross-feeding can be maintained by population dynamics alone. However, many active behaviours have also been proposed to explain how cross-feeding persists [[31](#page-12-0)]. For example, mutualisms can be maintained if mutualists can choose their partners [[7](#page-11-0)], provide fewer resources to cheaters [[6](#page-11-0)] or actively punish cheaters [[43\]](#page-12-0). It is likely that both behavioural and population dynamics mechanisms act in real populations. Future work should examine if such active behaviours would enhance or undermine pattern formation and neighbour uncertainty.

In addition to providing two novel explanations for how cross-feeding is maintained, our work suggests strategies for making synthetic consortia robust against non-producing cheaters. Pattern formation and random local interactions do not require complex behaviours like quorum sensing, and will be more temporally stable than partner fidelity feedback ([figure 4](#page-5-0); electronic supplementary material, movies A1, A2 and A3). Many of the technologies needed to produce these effects have already been developed. For example, gels, semi-permeable membranes and microfluidic devices can stop microbes from moving without stopping them from sharing compounds [\[44](#page-12-0)]; these could be used to generate spatial patterns. Similarly, microfluidic devices have been developed which partition consortia into small groups by injecting them into tiny droplets [\[45](#page-12-0)]; these could be used to generate random local interactions. Future work should examine what are effective ways to implement these mechanisms in synthetic consortia.

Data accessibility. Code and data available at the Dryad Digital Repository [\(http://dx.doi.org/10.5061/dryad.s1v3801\)](http://dx.doi.org/10.5061/dryad.s1v3801) [[46\]](#page-12-0).

Authors' contributions. C.A.K. conceived the research. S.M.S. and C.A.K. developed the model. E.K.J. and S.M.S. wrote code and performed simulations. S.M.S. performed mathematical analysis in the supplementary material. All authors contributed to writing the manuscript.

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Appendix A. Model implementation

Most results were generated using simulations. The community is modelled on a grid (typically 200×200 sites) with periodic boundary conditions. Each site can be empty or contain a single microbe of any type. Each time step in a simulation represents Δt units of time (typically 0.1). During each time step, we determine if empty sites become occupied by new microbes and if occupied sites become empty via a microbe dying. We assume that both events occur simultaneously.

An empty site became filled if a nearby microbe gives birth and disperses its offspring there. The average number of offspring produced in a given time step, B_{jx} for species j at site x , is

$$
B_{1x} = b_1 R_{2x} \Delta t,
$$

\n
$$
B_{2x} = b_2 R_{1x} \Delta t
$$

\nand
$$
B_{0x} = b_0 \min(R_{1x}, R_{2x}) \Delta t.
$$
 (A1)

The probability that a site x became filled with an individual of species *j* was therefore $1/[(2 d_{\text{mic}} + 1)^2 - 1] \sum_{y \in d_{\text{mic}}} N_{jy}B_{jy}$. We selected values of Δt such that this average was much less than 1 to minimize the possibility that multiple microbes colonize a site in the same time step (such effects were ignored).

Microbes die in each time step with probability $\delta \Delta t$. Microbes can reproduce during the time step they die. A site cannot be recolonized the same time step it becomes empty, and a microbe cannot die during the time step it was born; such events do not have an effect when Δt is small.

The simulation was written in Java and interfaced through R, and some of the analysis was performed in Matlab.

For [figure 2,](#page-3-0) we initiated a community with 3000 individuals of each cross-feeder (7.5% of sites occupied). This was enough to allow the cross-feeders to persist for these parameters in the absence of cheaters. After 20 000 time steps (2000 time units or approximately 300 generations), we introduced 150 cheater individuals (0.375% of sites) at random locations, displacing any individuals there. We then ran the simulation for an additional 50 000 time steps to approach a steady state. [Figure 4](#page-5-0) was generated using similar methods, except that the cheater was introduced after 5000 time steps and then the simulation was run for an additional 30 000

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time steps. [Figure 4](#page-5-0) displays the spatial distribution at 29 400 time steps, in order to show the population in [figure 4](#page-5-0)a as it was transitioning between a boom and a bust (at 30 000 time steps, there are few empty locations, but the population is about to crash in many localities, making the figure less illustrative). The neighbour uncertainty case (figure $4g-i$) was run for 50 000 time steps, because it took longer for the community to equilibrate. Movies of each can be found in the electronic supplementary material.

Appendix B. Analytical results

B.1. Derivation of mean field model

Under mean-field conditions, the finite rate of increase of an individual of species j (i.e. its geometric growth rate), λ_i is $\lambda = 1 + \text{birth–death}$. This expression simplifies to

$$
\lambda_j = 1 + B_j(1 - N_1 - N_2 - N_0) - \delta \Delta t, \tag{B1}
$$

where B_i is the average number of times that species *j* reproduces (equation $(A 1)$) and N_i is the fraction of sites held by species *j*. In this appendix, we use N_i and B_i without the *x* to represent the mean of N_{xi} and B_{xi} across space. The parenthetical term is the fraction of sites that are empty. Taking the limit of (B 1) as $\Delta t \rightarrow 0$ results in the continuous-time model

$$
\frac{dN_1}{dt} = N_1(b_1QN_2(1 - N_1 - N_2 - N_0) - \delta),
$$
\n
$$
\frac{dN_2}{dt} = N_2(b_2QN_1(1 - N_1 - N_2 - N_0) - \delta)
$$
\nand\n
$$
\frac{dN_0}{dt} = N_0(b_0Q\min(N_1, N_2)(1 - N_1 - N_2 - N_0) - \delta).
$$
\n(B2)

For the analysis used to generate [figure 3,](#page-4-0) we make the additional simplifying assumption that $b_1 = b_2$ and $N_1 = N_2$ (which we call N_{1-2}), to reduce the model dimensionality to aid intuition. With this assumption of species symmetry, we can model both cross-feeders with a single equation, and (B 2) simplified to

$$
\frac{dN_{1-2}}{dt} = N_{1-2}(b_2QN_{1-2}(1-2N_{1-2}-N_0) - \delta)
$$
\nand\n
$$
\frac{dN_0}{dt} = N_0(b_0QN_{1-2}(1-2N_{1-2}-N_0) - \delta).
$$
\n(B3)

We justify this symmetry assumption below.

B.2. Stability of mean-field model

We will conduct most of the analysis on equation (B 2) (i.e. without the symmetry assumption), though add that assumption when needed.

If the cheater is absent, this system will have one of three equilibria. This system always has an extinction equilibrium

$$
N_1^* = N_2^* = 0. \tag{B4}
$$

Additionally, when birth rates and compound production are sufficiently high relative to death rates, then it will have two positive equilibria,

$$
(N_1^*, N_2^*) = \left(\frac{b_1 \pm \sqrt{b_1/b_2}\sqrt{b_1b_2 - 4\delta(b_1 + b_2)/Q}}{2(b_1 + b_2)}, \frac{b_2 \pm \sqrt{b_2/b_1}\sqrt{b_1b_2 - 4\delta(b_1 + b_2)/Q}}{2(b_1 + b_2)}\right)
$$
(B5)

If $b_1 = b_2$, these simplify to

$$
N_1^* = N_2^* = \frac{1}{4} \pm \sqrt{\frac{1}{16} - \frac{\delta}{2b_1Q}}
$$
 (B6)

which exists whenever $Qb_1 > 8\delta$. Thus, N_1 and N_2 approach equality when $b_1 = b_2$ and the cheater is absent, which justifies our symmetry assumption that $N_1 = N_2$.

At the extinction equilibrium, the Jacobian matrix is

$$
J = \begin{bmatrix} -\delta & 0\\ 0 & -\delta \end{bmatrix},
$$
 (B7)

which is always stable. At a positive equilibrium, the Jacobian matrix is

$$
J = \begin{bmatrix} -b_1 N_2^* & -2b_1 N_2^* - b_1 N_1^* \\ -2b_2 N_1^* - b_2 N_2^* & -b_2 N_1^* \end{bmatrix}.
$$
 (B8)

Plugging in $(B 5)$, we find that the smaller positive equilibrium is unstable but the larger positive equilibrium is stable (if they exist). Thus, this system has multiple stable equilibria.

Next, we show that the cheater will inevitably crash the system.

No positive equilibrium can exist in a system with the cheater. To see this, we will assume that one does exist and arrive at a contradiction. We assume WLOG that $N_1^* \le N_2^*$. If a positive equilibrium exists, then $dN_2/dt = 0$ and $N_2^* > 0$. In this case, we can rearrange species 2's growth equation to

$$
QN_1^*(1 - N_1^* - N_2^* - N_0^*) = \frac{\delta}{b_2}.
$$
 (B9)

Substituting this into the cheater's growth rate (when min $(N_1^*, N_2^*) = N_1^*$, we find that

$$
\frac{dN_0}{dt} = N_0^* \left(b_0 \frac{\delta}{b_2} - \delta \right).
$$
 (B10)

This is positive whenever $N_0 > 0$, by our assumption that $b_0 > b_2$. Thus, because $dN_0/dt > 0$ when $dN_2/dt = 0$ and each species has a positive density, a positive equilibrium with all three species cannot exist.

The equilibrium $(N_1^*, N_2^*, N_0^*) = (N_1^* > 0, N_2^* > 0, 0)$ cannot be stable, because if $dN_1/dt = 0$ and $dN_2/dt = 0$, then the cheater must have a positive growth rate (as shown above). The extinction equilibrium has Jacobian matrix

$$
J = \begin{bmatrix} -\delta & 0 & 0 \\ 0 & -\delta & 0 \\ 0 & 0 & -\delta \end{bmatrix}.
$$
 (B11)

Thus, only the extinction equilibrium, $(N_1^*, N_2^*, N_0^*) = (0,0,0)$, is stable.

If we assume that $b_1 = b_2$ and $N_1 = N_2$, then we can reduce our system to a two-dimensional system, shown in [figure 3.](#page-4-0) In this case, we have a closed, bounded, twodimensional system with no internal equilibria; therefore, no limit cycle exists. Because the system is bounded, does not contain a closed loop, and contains no other stable equilibria, the extinction equilibrium is globally stable. Hundreds of computer simulations across a variety of parameters suggest that the same results hold when $b_1 \neq b_2$.

Appendix C. Additional analysis of spatial patterns

Here we present an additional analysis of the spatial patterns observed in our simulations.

For [figure 5](#page-6-0), we used a bisection method to calculate the maximum birth rate b_0 a cheater could have without driving the cross-feeders extinct. We checked values between $b_0 = 0.6$ (equal to b_1 and b_2) and 2.4. For each value of b_0 , we allowed the cross-feeders to reach an equilibrium, introduced a small number of cheaters, and determined if the cross-feeders persisted after 20 000 time steps. If the cross-feeders persisted at a given b_0 , then we checked if they persisted at a b_0 half way between this and the lowest b_0 where they did not persist; if the cross-feeders did not persist, then we checked if they persisted at a b_0 half way between this and the highest b_0 where they did persist. We repeated this for eight trials, reaching an accuracy of $1.8 \times 2^{-8} \approx 0.007$. We measured the minimum b_0 needed to invade using the same method, and the results were similar. Two simulations runs showed extremely similar results, suggesting that stochastic extinctions had only a minor effect on our estimates of b_0 .

Figures [6](#page-6-0)-9 were generated using the communities in [figure 2.](#page-3-0) We used the final distribution of microbes (those displayed) and ignored communities which collapsed. To test whether sites that were favourable to the cross-feeders were also favourable to the cheater (figure 6), we correlated B_{0x} with B_{1x} and with B_{2x} across each site. [Figure 6](#page-6-0) shows the mean of these two correlations. Results were similar for the correlation between B_{0x} and $1/2$ $(B_{1x} + B_{2x})$, though the correlations were higher. To test whether microbes were more likely to be in favourable spots ([figure 7](#page-7-0)), we calculated the mean of probability of reproduction in sites where the microbe could be found and compared to its probability of reproduction averaged across all sites [[47\]](#page-12-0). To determine how much the cheater was harmed because the resources were in different areas (figure 8), we calculated the mean of $min(R_{1x}, R_{2x})$ across all sites and divided this by the mean of R_{1x} and R_{2x} across all sites. The denominator here represented the mean-field level of resource levels, and thus the ratio shows how much variation in resources harms the cheater. To test the effect of spatial structure [\(figure 9\)](#page-8-0), we randomly reorganized each of the communities. After reorganization, we tested how much the cheater's mean probability of reproduction $(B_{0x}$ averaged across all sites) changed. Because B_{1x} and B_{2x} are linear functions of species 2 and 1 densities, mean values of B_{1x} and B_{2x} did not change when the microbes were reorganized.

References

- 1. Bronstein JL. 2001 The exploitation of mutualisms. Ecol. Lett. 4, 277– 287. ([doi:10.1046/j.1461-0248.](http://dx.doi.org/10.1046/j.1461-0248.2001.00218.x) [2001.00218.x\)](http://dx.doi.org/10.1046/j.1461-0248.2001.00218.x)
- 2. Bertrand EM et al. 2015 Phytoplankton bacterial interactions mediate micronutrient colimitation at the coastal Antarctic sea ice edge. Proc. Natl Acad. Sci. USA 112, 9938-9943. ([doi:10.1073/pnas.](http://dx.doi.org/10.1073/pnas.1501615112) [1501615112\)](http://dx.doi.org/10.1073/pnas.1501615112)
- 3. Rivière A, Gagnon M, Weckx S, Roy D, De Vuyst L. 2015 Mutual cross-feeding interactions between Bifidobacterium longum subsp. longum NCC2705 and Eubacterium rectale ATCC 33656 explain the bifidogenic and butyrogenic effects of arabinoxylan oligosaccharides. Appl. Environ. Microbiol. 81, 7767 – 7781. [\(doi:10.1128/AEM.02089-15\)](http://dx.doi.org/10.1128/AEM.02089-15)
- 4. Kwong WK, Engel P, Koch H, Moran NA. 2014 Genomics and host specialization of honey bee and bumble bee gut symbionts. Proc. Natl Acad. Sci. USA 111, 11 509–11 514. ([doi:10.1073/pnas.1405838111\)](http://dx.doi.org/10.1073/pnas.1405838111)
- 5. Rosenthal AZ, Matson EG, Eldar A, Leadbetter JR. 2011 RNA-seq reveals cooperative metabolic interactions between two termite–gut spirochete species in co-culture. $ISME$ J. 5, 1133 - 1142. [\(doi:10.1038/ismej.2011.3\)](http://dx.doi.org/10.1038/ismej.2011.3)
- 6. Steidinger BS, Bever JD. 2014 The coexistence of hosts with different abilities to discriminate against cheater partners: an evolutionary game-theory approach. Am. Nat. 183, 762–770. [\(doi:10.1086/675859\)](http://dx.doi.org/10.1086/675859)
- 7. Foster KR, Kokko H. 2006 Cheating can stabilize cooperation in mutualisms. Proc. R. Soc. B 273, 2233 – 2239. [\(doi:10.1098/rspb.2006.3571](http://dx.doi.org/10.1098/rspb.2006.3571))
- 8. Wilson WG, Morris WF, Bronstein JL. 2003 Coexistence of mutualists and exploiters on spatial landscapes. Ecol. Monogr. 73, 397– 413. ([doi:10.](http://dx.doi.org/10.1890/02-0297) [1890/02-0297\)](http://dx.doi.org/10.1890/02-0297)
- 9. Yamamura N, Higashi M, Behera N, Wakano JY. 2004 Evolution of mutualism through spatial effects. J. Theor. Biol. 226, 421– 428. [\(doi:10.1016/](http://dx.doi.org/10.1016/j.jtbi.2003.09.016) [j.jtbi.2003.09.016\)](http://dx.doi.org/10.1016/j.jtbi.2003.09.016)
- 10. Akashi H, Gojobori T. 2002 Metabolic efficiency and amino acid composition in the proteomes of Escherichia coli and Bacillus subtilis. Proc. Natl Acad. Sci. USA 99, 3695-3700. ([doi:10.1073/pnas.](http://dx.doi.org/10.1073/pnas.062526999) [062526999](http://dx.doi.org/10.1073/pnas.062526999))
- 11. Morris JJ. 2015 Black queen evolution: the role of leakiness in structuring microbial communities. Trends Genet. 31, 475 – 482. ([doi:10.1016/j.tig.2015.](http://dx.doi.org/10.1016/j.tig.2015.05.004) [05.004](http://dx.doi.org/10.1016/j.tig.2015.05.004))
- 12. West SA, Griffin AS, Gardner A, Diggle SP. 2006 Social evolution theory for microorganisms. Nat. Rev. Microbiol. 4, 597 – 607. [\(doi:10.1038/](http://dx.doi.org/10.1038/nrmicro1461) [nrmicro1461](http://dx.doi.org/10.1038/nrmicro1461))
- 13. Boyle RA, Williams HTP, Lenton TM. 2012 Natural selection for costly nutrient recycling in simulated microbial metacommunities. J. Theor. Biol. 312, 1 – 12. [\(doi:10.1016/j.jtbi.2012.07.018\)](http://dx.doi.org/10.1016/j.jtbi.2012.07.018)
- 14. Oliveira NM, Niehus R, Foster KR. 2014 Evolutionary limits to cooperation in microbial communities. Proc. Natl Acad. Sci. USA 111, 17 941– 17 946. [\(doi:10.1073/pnas.1412673111\)](http://dx.doi.org/10.1073/pnas.1412673111)
- 15. Jeffrey Morris J, Papoulis SE, Lenski RE. 2014 Coexistence of evolving bacteria stabilized by a

shared black queen function. Evolution 68, 2960– 2971. ([doi:10.1111/evo.12485\)](http://dx.doi.org/10.1111/evo.12485)

- 16. Klayman BJ, Volden PA, Stewart PS, Camper AK. 2009 Escherichia coli 0157:H7 requires colonizing partner to adhere and persist in a capillary flow cell. Environ. Sci. Technol. 43, 2105– 2111. [\(doi:10.1021/](http://dx.doi.org/10.1021/es802218q) [es802218q](http://dx.doi.org/10.1021/es802218q))
- 17. Cordero OX, Ventouras L-A, DeLong EF, Polz MF. 2012 Public good dynamics drive evolution of iron acquisition strategies in natural bacterioplankton populations. Proc. Natl Acad. Sci. USA 109, 20 059 – 20 064. [\(doi:10.1073/pnas.1213344109](http://dx.doi.org/10.1073/pnas.1213344109))
- 18. Escalante AE, Rebolleda-Gomez M, Benitez M, Travisano M. 2015 Ecological perspectives on synthetic biology: insights from microbial population biology. Front. Microbiol. $6, 1-10$. ([doi:10.3389/fmicb.2015.00143\)](http://dx.doi.org/10.3389/fmicb.2015.00143)
- 19. Nowak MA. 2006 Five rules for the evolution of cooperation. Science 314, 1560– 1563. [\(doi:10.](http://dx.doi.org/10.1126/science.1133755) [1126/science.1133755](http://dx.doi.org/10.1126/science.1133755))
- 20. Smith CA, Wilson WG. 2007 Evolutionary stable dispersal with pattern formation in a mutualist – antagonist system. Evol. Ecol. Res. 9, 987– 1004.
- 21. Allison SD. 2005 Cheaters, diffusion and nutrients constrain decomposition by microbial enzymes in spatially structured environments. Ecol. Lett. 8, 626– 635. [\(doi:10.1111/j.1461-0248.2005.00756.x\)](http://dx.doi.org/10.1111/j.1461-0248.2005.00756.x)
- 22. Nadell CD, Foster KR, Xavier JB. 2010 Emergence of spatial structure in cell groups and the evolution of cooperation. PLoS Comput. Biol. 6, 9. [\(doi:10.1371/](http://dx.doi.org/10.1371/journal.pcbi.1000716) [journal.pcbi.1000716](http://dx.doi.org/10.1371/journal.pcbi.1000716))
- 23. Momeni B, Waite AJ, Shou W. 2013 Spatial selforganization favors heterotypic cooperation over cheating. Elife 2, e00960. ([doi:10.7554/eLife.](http://dx.doi.org/10.7554/eLife.00960) [00960](http://dx.doi.org/10.7554/eLife.00960))
- 24. Wilson DS, Sober E. 1994 Reintroducing group selection to the human behavioral sciences. Behav. Brain Sci. 17, 585 – 608. ([doi:10.1017/S0140525X](http://dx.doi.org/10.1017/S0140525X00036104) [00036104](http://dx.doi.org/10.1017/S0140525X00036104))
- 25. Mee MT, Wang HH. 2012 Engineering ecosystems and synthetic ecologies. Mol. Biosyst. 8, 2470 – 2483. [\(doi:10.1039/c2mb25133g](http://dx.doi.org/10.1039/c2mb25133g))
- 26. Brenner K, You LC, Arnold FH. 2008 Engineering microbial consortia: a new frontier in synthetic biology. Trends Biotechnol. 26, 483– 489. [\(doi:10.](http://dx.doi.org/10.1016/j.tibtech.2008.05.004) [1016/j.tibtech.2008.05.004\)](http://dx.doi.org/10.1016/j.tibtech.2008.05.004)
- 27. Mee MT, Collins JJ, Church GM, Wang HH. 2014 Syntrophic exchange in synthetic microbial communities. Proc. Natl Acad. Sci. USA 111, E2149 – E2156. ([doi:10.1073/pnas.](http://dx.doi.org/10.1073/pnas.1405641111) [1405641111](http://dx.doi.org/10.1073/pnas.1405641111))
- 28. Wintermute EH, Silver PA. 2010 Dynamics in the mixed microbial concourse. Genes Dev. 24, 2603 – 2614. [\(doi:10.1101/gad.1985210](http://dx.doi.org/10.1101/gad.1985210))
- 29. Shou W, Ram S, Vilar JMG. 2007 Synthetic cooperation in engineered yeast populations. Proc. Natl Acad. Sci. USA 104, 1877– 1882. ([doi:10.1073/](http://dx.doi.org/10.1073/pnas.0610575104) [pnas.0610575104](http://dx.doi.org/10.1073/pnas.0610575104))
- 30. Kim HJ, Boedicker JQ, Choi JW, Ismagilov RF. 2008 Defined spatial structure stabilizes a synthetic multispecies bacterial community. Proc. Natl Acad. Sci. USA 105, 18 188 - 18 193. [\(doi:10.1073/pnas.](http://dx.doi.org/10.1073/pnas.0807935105) [0807935105\)](http://dx.doi.org/10.1073/pnas.0807935105)
- 31. Travisano M, Velicer GJ. 2004 Strategies of microbial cheater control. Trends Microbiol. **12**, 72-78. [\(doi:10.1016/j.tim.2003.12.009\)](http://dx.doi.org/10.1016/j.tim.2003.12.009)
- 32. Brenner K, Karig DK, Weiss R, Arnold FH. 2007 Engineered bidirectional communication mediates a consensus in a microbial biofilm consortium. Proc. Natl Acad. Sci. USA 104, 17 300– 17 304. ([doi:10.](http://dx.doi.org/10.1073/pnas.0704256104) [1073/pnas.0704256104](http://dx.doi.org/10.1073/pnas.0704256104))
- 33. Durrett R, Levin SA. 1994 Stochastic spatial models: a user's guide to ecological applications. Phil. Trans. R. Soc. Lond. B 343, 329 – 350. [\(doi:10.1098/](http://dx.doi.org/10.1098/rstb.1994.0028) [rstb.1994.0028\)](http://dx.doi.org/10.1098/rstb.1994.0028)
- 34. Von Liebig J. 1840 Die organische chemie in ihre anwendung auf agricultur und physiologie. Braunschweig, Germany: F. Vieweg und Sohn.
- 35. Harpole WS et al. 2011 Nutrient co-limitation of primary producer communities. Ecol. Lett. 14, 852 – 862. [\(doi:10.1111/j.1461-0248.2011.01651.x](http://dx.doi.org/10.1111/j.1461-0248.2011.01651.x))
- 36. Armstrong RA. 1987 A patch model of mutualism. J. Theor. Biol. 125, 243– 246. ([doi:10.1016/S0022-](http://dx.doi.org/10.1016/S0022-5193(87)80045-0) [5193\(87\)80045-0](http://dx.doi.org/10.1016/S0022-5193(87)80045-0))
- 37. Nisbet RM, Gurney WSC. 1982 Modelling fluctuating populations. Caldwell, NJ: The Blackburn Press.
- 38. Turing AM. 1952 The chemical basis of morphogenesis. Phil. Trans. R. Soc. Lond. B 237. 37 – 72. ([doi:10.1098/rstb.1952.0012\)](http://dx.doi.org/10.1098/rstb.1952.0012)
- 39. Durrett R, Levin S. 1994 The importance of being discrete (and spatial). Theor. Popul. Biol. 46, 363 – 394. [\(doi:10.1006/tpbi.1994.1032](http://dx.doi.org/10.1006/tpbi.1994.1032))
- 40. Driscoll WW, Pepper JW. 2010 Theory for the evolution of diffusible external goods. Evolution

64, 2682–2687. [\(doi:10.1111/j.1558-5646.2010.](http://dx.doi.org/10.1111/j.1558-5646.2010.01002.x) [01002.x\)](http://dx.doi.org/10.1111/j.1558-5646.2010.01002.x)

- 41. Dobay A, Bagheri HC, Messina A, Kümmerli R, Rankin DJ. 2014 Interaction effects of cell diffusion, cell density and public goods properties on the evolution of cooperation in digital microbes. J. Evol. Biol. 27, 1869– 1877. ([doi:10.1111/jeb.12437](http://dx.doi.org/10.1111/jeb.12437))
- 42. Nadell CD, Drescher K, Foster KR. 2016 Spatial structure, cooperation and competition in biofilms. Nat. Rev. Microbiol. 14, 589– 600. ([doi:10.1038/](http://dx.doi.org/10.1038/nrmicro.2016.84) [nrmicro.2016.84](http://dx.doi.org/10.1038/nrmicro.2016.84))
- 43. Archetti M, Scheuring I, Hoffman M, Frederickson ME, Pierce NE, Yu DW. 2011 Economic game theory for mutualism and cooperation. Ecol. Lett. 14, 1300– 1312. ([doi:10.1111/j.1461-0248.2011.01697.x](http://dx.doi.org/10.1111/j.1461-0248.2011.01697.x))
- 44. Goers L, Freemont P, Polizzi KM. 2014 Co-culture systems and technologies: taking synthetic biology to the next level. J. R. Soc. Interface 11, 20140065. ([doi:10.1098/rsif.2014.0065](http://dx.doi.org/10.1098/rsif.2014.0065))
- 45. Park J, Kerner A, Burns MA, Lin XN. 2011 Microdroplet-enabled highly parallel co-cultivation of microbial communities. PLoS ONE 6, 317019. ([doi:10.1371/journal.pone.0017019](http://dx.doi.org/10.1371/journal.pone.0017019))
- 46. Stump SM, Johnson EC, Klausmeier CA. 2018 Data from: Local interactions and self-organized spatial patterns stabilize microbial cross-feeding against cheaters. Dryad Digital Repository. ([http://dx.doi.](http://dx.doi.org/10.5061/dryad.s1v3801) [org/10.5061/dryad.s1v3801](http://dx.doi.org/10.5061/dryad.s1v3801))
- 47. Stump SM, Chesson P. 2015 Distance-responsive predation is not necessary for the Janzen – Connell hypothesis. Theor. Popul. Biol. 106 , $60 - 70$. [\(doi:10.](http://dx.doi.org/10.1016/j.tpb.2015.10.006) [1016/j.tpb.2015.10.006\)](http://dx.doi.org/10.1016/j.tpb.2015.10.006)