



Local initiation conditions for water autoionization

Mahmoud Moqadam^{a,1}, Anders Lervik^{a,1,2}, Enrico Riccardi^a, Vishwesh Venkatraman^a, Bjørn Kåre Alsberg^{a,3}, and Titus S. van Erp^{a,b,2}

^aDepartment of Chemistry, Norwegian University of Science and Technology, N-7491 Trondheim, Norway; and ^bCenter for Molecular Modeling, Ghent University, B9000 Ghent, Belgium

Edited by Phillip L. Geissler, University of California, Berkeley, CA, and accepted by Editorial Board Member R. D. Levine April 5, 2018 (received for review August 9, 2017)

The pH of liquid water is determined by the infrequent process in which water molecules split into short-lived hydroxide and hydronium ions. This reaction is difficult to probe experimentally and challenging to simulate. One of the open questions is whether the local water structure around a slightly stretched OH bond is actually initiating the eventual breakage of this bond or whether this event is driven by a global ordering that involves many water molecules far away from the reaction center. Here, we investigated the self-ionization of water at room temperature by rare-event ab initio molecular dynamics and obtained autoionization rates and activation energies in good agreement with experiments. Based on the analysis of thousands of molecular trajectories, we identified a couple of local order parameters and show that if a bond stretch occurs when all these parameters are around their ideal range, the chance for the first dissociation step (double-proton jump) increases from 10^{-7} to 0.4. Understanding these initiation triggers might ultimately allow the steering of chemical reactions.

autoionization | water | path sampling | machine learning | ab initio molecular dynamics

Among all possible chemical reactions that occur in water, the most fundamental is the water dissociation reaction (1), which is of major importance in many areas of chemistry and biology (2). Water plays an important role as a universal solvent for a wide variety of chemical processes and can act both as an acid and as a base. In aqueous solution, water will self-ionize and form hydroxide (OH^-) and hydronium (H_3O^+) ions which take on Eigen- or Zundel-like structures (2–6). Experiments show that the mean lifetime for an individual molecule before undergoing autoionization is about 11 h (7, 8).

The autoionization event has not been directly probed by experiments and the dissociation rate is obtained using the water dissociation equilibrium constant and the rate for the much faster recombination reaction (7, 8). The experimental challenges make the autoionization event a pertinent target for computer simulations for which previous constrained ab initio simulations have given important information about the mechanism (9–11). However, the use of constraints leads to a loss of the spontaneous dynamics of the system and the selection of a reaction coordinate that accurately measures the progress of the reaction is challenging. These limitations can be avoided by path-sampling methods such as transition path sampling (TPS) (12) or replica exchange transition interface sampling (RETIS) (13, 14) which are specifically designed for sampling rare events without altering the dynamics while less influenced by the choice of the order parameter (15). Geissler et al. (16) applied TPS with ab initio molecular dynamics (MD) to simulate just 10 uncorrelated autoionization events and demonstrated that the mechanism involves transfer of protons along a hydrogen bond wire with concomitant breaking of the wire. In their work, local solvent properties (e.g., ion coordination numbers and the presence of specific hydrogen bonds) were used to interpret the destabilization that leads to ionization. The absence of clear visually observable correlations led to the conclusion that the destabilization is caused by rare electric-field fluctuations which arise primarily from long-range electrostatic interactions and thus that

local order parameters are not suitable to describe the event. Hassanali et al. (17) studied the reverse recombination reaction (i.e., neutralization of ionized water molecules) with standard ab initio MD and reported that this event takes place by a collective compression of the water wire bridging the ions, followed by a triple concerted proton jump. The OH^- ion which is neutralized remains in a hypercoordinated state and Hassanali et al. (17) hypothesized that it could serve, together with the compression of the wire, as a nucleation site for autoionization. This view opposes the statement of Geissler et al. (16) that the dissociation event is primarily triggered by nonlocal structural fluctuations. We note that concerted proton transfers and collective compression of water wires have also been observed for the recombination of a weak base in water (18).

Both of these studies give important information about the autoionization mechanism, although they do not unambiguously reveal the conditions that need to accompany a bond stretch fluctuation to initiate the reaction. In this work, we aim to tackle this ambiguity and quantitatively identify initiation conditions for water autoionization. Simulating the dissociation events may not be sufficient as the apparent initiation conditions observed in trajectories that lead to dissociation may also be present in trajectories with an initial bond stretch but still fail to dissociate. Also nonreactive or “almost reactive” trajectories contain important information as these allow for identification of effective initiation conditions that really matter: those that discriminate

Significance

The dissociation of water is arguably the most fundamental chemical reaction occurring in the aqueous phase. Despite that the splitting of a water molecule very seldom occurs, the reaction is of major importance in many areas of chemistry and biology. Direct experimental probing of the event is still impossible and also simulating the event via accurate computer simulations is challenging. Here, we achieved the latter via specialized rare-event algorithms estimating rates of dissociation in agreement with indirect experimental measurements. Even more interestingly, by a rigorous analysis of our results we identified anomalies in the water structure that act as initiators of the reaction, a finding that suggests paradigms for steering and catalyzing chemical reactions.

Author contributions: A.L. and T.S.v.E. designed research; M.M., A.L., E.R., and T.S.v.E. performed research; M.M., A.L., V.V., and B.K.A. analyzed data; and M.M., A.L., E.R., V.V., and T.S.v.E. wrote the paper.

The authors declare no conflict of interest.

This article is a PNAS Direct Submission. P.L.G. is a guest editor invited by the Editorial Board.

Published under the PNAS license.

¹M.M. and A.L. contributed equally to this work.

²To whom correspondence may be addressed. Email: titus.van.erp@ntnu.no or anders.lervik@ntnu.no.

³Deceased December 27, 2017.

This article contains supporting information online at www.pnas.org/lookup/suppl/doi:10.1073/pnas.1714070115/-DCSupplemental.

Published online April 30, 2018.

between reactive and nonreactive trajectories. To collect this information, we applied the RETIS method and harvested reactive and nonreactive trajectories which we analyzed using the recently developed predictive power method (19) and we built a predictive machine-learning model (20). This allowed us to quantitatively examine the importance of local order parameters and initiation conditions for water autoionization. Based on this analysis we identify important initiation triggers and calculate the full rate of dissociation.

Results and Discussion

The autoionization event was investigated using ab initio RETIS simulations as described in *Materials and Methods*. For the RETIS simulations, we used a relatively simple geometric distance order parameter, λ , as illustrated in Fig. 1: When the system consists of only H_2O species, λ is the largest covalent O–H bond distance, and when the system contains OH^- and H_3O^+ species, λ is taken as the shortest distance between the oxygen in OH^- and the hydrogen atoms in H_3O^+ . In the following, we refer to the oxygen atom used for the order parameter as O^λ . The type of species (OH^- , H_2O , or H_3O^+) was identified by allocating to each hydrogen a single bond connecting

it to the closest oxygen. Note that the definition of the order parameter does not require a threshold for defining a chemical bond nor does it constrain the order parameter to specific water molecules for the duration of the simulation. This means that we compute the rate of dissociation of any water molecule in the system instead of a single targeted O–H bond or water molecule.

From our RETIS simulations, the water dissociation rate constant, k_D , can be obtained as the product of a flux, f_A , and a (conditional) probability, $\mathcal{P}_A(\lambda_N|\lambda_0)$:

$$k_D = f_A \times \mathcal{P}_A(\lambda_N|\lambda_0). \quad [1]$$

Here, λ_0 and λ_N are interfaces defining the initial ($\lambda < \lambda_0$) and final ($\lambda > \lambda_N$) states and $\mathcal{P}_A(\lambda_N|\lambda_0)$ is the probability of reaching the final state before (possibly) reentering the initial state, given that the initial interface λ_0 has been crossed. The flux, f_A , is a measure of the frequency of crossings with λ_0 . Since we consider the dissociation of any water molecule in our system, we have normalized f_A by the number of water molecules present. Typically, for rare events, the crossing probability is very small and in practice, $\mathcal{P}_A(\lambda_N|\lambda_0)$ is calculated by first positioning several more interfaces $\lambda_0 < \lambda_1 < \dots < \lambda_N$ between the initial and the final state. The overall crossing probability is then obtained as a product of several (history-dependent) conditional probabilities (14). The conditional probabilities are calculated in a separate path ensemble simulation where the $[i^+]$ path ensemble defines the collection of paths crossing λ_i . The number and location of the interfaces alter the efficiency of the method, but not the results.

In the present case, we placed the final interface beyond the maximum distance obtainable in our system. All trajectories were thus propagated until the system contained only H_2O species again. Separated ions may still recombine fast (within a few femtoseconds) even if the separation is large (16) and this observation was confirmed in our analysis (*SI Appendix, Fig. S1*). To better identify and distinguish the metastable ionized states, we used path reweighting (21) to project the crossing probability on an alternative order parameter, λ' , which equals the trajectory length (in femtoseconds).

In Fig. 1, we show the calculated crossing probability from our simulations as a function of the order parameter. In principle, there are two potential mechanisms which lead to an increase of the reaction coordinate λ after the first proton jump. The ionic species can separate further by another proton jump, the so-called Grotthuss mechanism, reassigning the H_3O^+ or OH^- ion to another oxygen and causing a sudden discontinuous increase in the reaction coordinate. A second possible mechanism keeps the first ionic species intact and lets them move away from each other by diffusion, yielding a more gradual increase of the reaction coordinate. Based on the completely flat intermediate plateau region between 1.5 Å and 3.2 Å, we can conclude that only the first mechanism is effective. For $\lambda > 3$ Å, we consider λ' as the order parameter and we have used a threshold of $\lambda' \geq 1$ ps as a criterion to identify a stable dissociation event. This choice is rather arbitrary since there is not a clear separation of timescales for the reverse recombination reaction which would result in another flat plateau region of the crossing probability. With a threshold of 1 ps, the crossing probability is $\mathcal{P}_A = 4.0 \times 10^{-15}$. Combined with the initial flux, calculated to be $f_A = 2.9 \times 10^{-3} \text{ fs}^{-1}$ in our simulations, the resulting dissociation constant is $k_D = f_A \times \mathcal{P}_A = 1.1 \times 10^{-2} \text{ s}^{-1}$. An alternative rate constant not requiring any time threshold can be defined by counting the trajectories that undergo a hydrogen swap; i.e., in the last frame some of the water molecules have swapped their protons. The rationale behind this definition is that the proton swap must imply a significant reorganization of the hydrogen bond network so that the reverse reaction can be considered as an

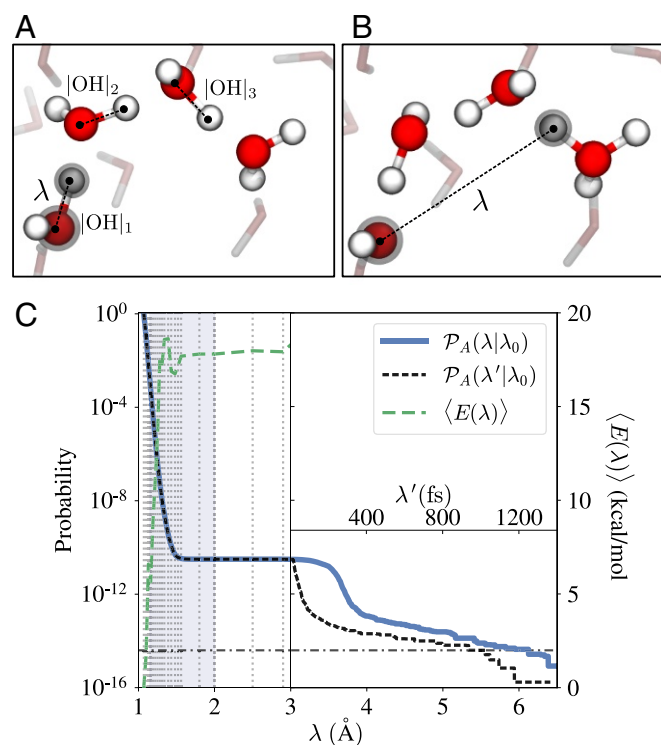


Fig. 1. The order parameter and the probability for water autoionization. (A and B) Definition of the order parameter (λ , dashed line), taken as the largest covalent O–H distance in the system when no ionic species are present (A) or as the shortest distance between the OH^- oxygen atom and the hydrogen atoms in H_3O^+ when ionic species are present (B). A hydrogen bond wire with four members is shown with red (oxygen) and white (hydrogen) spheres and the distances $|\text{OH}|_1$, $|\text{OH}|_2$, $|\text{OH}|_3$ are also indicated. These distances are used to investigate the possible concerted motion of hydrogen atoms along the wire. (C) The crossing probability (\mathcal{P}_A) and average energy of trajectories ($\langle E \rangle$) as a function of the order parameter. The (black) dashed line is calculated using an alternative definition of the order parameter (λ') where the trajectory length (in femtoseconds) defines the order parameter for $\lambda > 3$ Å. The horizontal dotted-dashed line is the crossing probability (4.0×10^{-15}) obtained for long paths ($\lambda' \geq 1$ ps). The activation energy is equal to the plateau value of the average energy which approaches 17.8 kcal/mol. The shaded area ($1.15 < \lambda < 2.0$) is the domain used for the predictive power analysis.

independent recombination reaction. Vice versa, the forward reaction has established a quasi-stable state since it is not followed up by a correlated reverse reaction. This definition yields a rate of $k_D = 0.16 \text{ s}^{-1}$.

Comparing with experimentally determined dissociation constants at 25 °C [$k_D = 2.5 \times 10^{-5} \text{ s}^{-1}$ (7) and $k_D = 2.04 \times 10^{-5} \text{ s}^{-1}$ (8)] we overestimate the rate constant by a factor 500 (although the simulated rate will drop and gets closer to the experimental rate if a larger threshold is chosen). Considering all factors that play a role in the accuracy (statistical error, functional, small system size, purely classical treatment of protons, the time threshold value) the deviation with experiments is satisfactory and comparable to other density functional theory studies. Depending on the functionals considered in the ab initio calculation, energy barriers may be in error by 10–20 kJ/mol (22) which at room temperature would already correspond to a factor 55–3,000 difference between experimental and theoretical rate constants. Still, density functional theory generally manages to reproduce trends and mechanistic information in reasonable agreement with experiments (23).

We also calculated the average energy of the generated trajectories as a function of the order parameter (Fig. 1). The energy is expected to converge to the activation energy as can be derived from the temperature derivative of the rate constant (24, 25). We note that this activation energy gives a more direct comparison with experiments than free energy barriers which depend on the choice of order parameter. The activation energy obtained from the average energy of the accepted paths is approximately 17.8 kcal/mol. For comparison, an Arrhenius plot of the experimental data of Natzle and Moore (8) results in an activation energy of approximately 17.3 kcal/mol while Eigen and Maeyer (7) reported an activation energy between 15.5 kcal/mol and 16.5 kcal/mol. The deviation with our result is lower than the typical error margin mentioned above and the fact that the experimental activation barriers are lower than our simulation result, despite having lower rate constants, is rather remarkable. Since experimental data on this topic are at least three decades old, we hope that our finding will encourage future experimental investigations on the dissociation reaction.

Path sampling methods generate reactive (and nonreactive) trajectories which can be used to discover possible mechanisms and initiation conditions. To characterize these conditions, we considered additional collective variables, which we label $\xi = (\xi_1, \xi_2, \dots)$. In principle, these ξ_i s can be functions of all positions and momenta in the system, and they do not necessarily have simple physical interpretations. Since the ability to form hydrogen bonds is one of the characteristic features of water (26) and since previous computational studies have demonstrated the relevance of the hydrogen bond wire connecting the ionized species (16, 17), we have focused on a set of relatively simple collective variables which quantify the hydrogen bond network and the distortion from tetrahedral geometry.

The first collective variable we consider is the length of the hydrogen bond wire bridging the nascent ion species. Our aim is to predict the outcome of initiated trajectories and in particular the initiation conditions for reactive events. Thus, we cannot define the hydrogen bond wires as connecting the ionic species, since this is one of the outcomes we wish to predict. For a single trajectory, we define the hydrogen bond wire as the shortest wire containing the O^λ species and $i - 1$ other water species at the first point in time when λ is greater than a given threshold value, $\lambda_t = 1.15 \text{ \AA}$. Typically, this threshold is reached within 3–6 fs in our trajectories. This defines a wire containing i water species whose length, w_i , is obtained as the sum of the O–O distances of consecutive members.

In addition, we have considered the following four collective variables which describe the local structure surrounding the O^λ species: (i) The number of hydrogen bonds accepted, n_a , and (ii) donated, n_d , by the water species containing O^λ ; (iii) the tetrahedral order parameter, q , obtained using the angles defined by O^λ and its four nearest oxygen atoms (27, 28) (by the definition $q = 1$ for a perfect tetrahedral structure and $q \neq 1$ otherwise); and (iv) an angle order parameter, q_{\cos} , defined as the smallest of the cosine of the two internal angles in the wire. We refer to *Materials and Methods* for additional information on these collective variables.

After defining the extra ξ s, we analyzed the trajectories using the predictive power method (19). This method begins by classifying the trajectories as reactive or nonreactive based on two thresholds λ^r and λ^c defined such that $\lambda^r > \lambda^c > \lambda_0$. A trajectory is considered reactive if it reaches the specified λ^r ; otherwise it is considered nonreactive. At the first crossing point with λ^c , we record the ξ s and form two distributions using the reactive/nonreactive classification: $r^{\lambda^c, \lambda^r}(\xi)$, the fraction of λ^c -passing trajectories that cross λ^c at a point ξ and reach λ^r , and $u^{\lambda^c, \lambda^r}(\xi)$, the fraction of λ^c -passing trajectories that cross λ^c at a point ξ but fail to reach λ^r . These two distributions give information on the relation between the additional order parameters and the reactivity. For instance, if $u^{\lambda^c, \lambda^r}(\xi) = 0$, it could be that ξ is inaccessible, but if we can cross λ^c at ξ , the trajectory will be reactive. To quantify the importance of the different ξ s, we calculate the predictive ability, $\mathcal{T}_A^{\lambda^c, \lambda^r}$, defined as (19)

$$\mathcal{T}_A^{\lambda^c, \lambda^r} = 1 - \frac{1}{\mathcal{P}_A(\lambda^r|\lambda^c)} \int \frac{r^{\lambda^c, \lambda^r}(\xi) u^{\lambda^c, \lambda^r}(\xi)}{r^{\lambda^c, \lambda^r}(\xi) + u^{\lambda^c, \lambda^r}(\xi)} d\xi, \quad [2]$$

such that $1 \geq \mathcal{T}_A^{\lambda^c, \lambda^r} \geq \mathcal{P}_A(\lambda^r|\lambda^c)$. If the collective variables do not correlate with reactivity, the lower limit is attained but if the ξ s are relevant for the reaction, $\mathcal{T}_A^{\lambda^c, \lambda^r} > \mathcal{P}_A(\lambda^r|\lambda^c)$. We use the ratio $\mathcal{T}_A^{\lambda^c, \lambda^r} / \mathcal{P}_A(\lambda^r|\lambda^c) \geq 1$ to measure how much the predictive ability is increased when considering the extra ξ s, compared with using the crossing probability alone. Note that the definition in Eq. 2 shows that if the overlap of the two distributions is small, then the predictive ability increases.

We first investigated the lengths of hydrogen bond wires containing three, four, and five water molecules. Comparing the predictive abilities for these collective variables (respectively, w_3 , w_4 , w_5) we find that w_4 and w_5 are more correlated with reactivity and that w_4 is more relevant for larger λ^r (SI Appendix, Fig. S2). Thus, in the following we focus on wires containing four water molecules. For the water wires, we observe that when the ionic species are separated by at least two water molecules, the ionic state survives for a longer time compared with cases where they are separated by just one water molecule. This implies that (at least) three proton transfer events have occurred. We monitored the distances of the initially covalent O–H bonds and show these for the first ($|\text{OH}|_1$), the second ($|\text{OH}|_2$), and the third ($|\text{OH}|_3$) transferred proton in Fig. 2. As can be expected from the Grotthuss mechanism (29, 30), the initial autoionization event is followed by several proton transfers in which the ionic species separate along the wire. Fig. 2 shows that this can happen in both a concerted and a stepwise way: The transfer of the first and the second proton occurs almost exclusively in a concerted way, while the transfer of the third proton (if it occurs) can happen stepwise or concertedly. This is also reflected in the waiting time between these events (SI Appendix, Fig. S3): The waiting time distribution between the second and the third proton transfer is broader compared with the first and the second transfer. To investigate the stability of the wires, we also calculated the hydrogen bond

Conclusions

We investigated the autoionization of water at room temperature, using an unconstrained *ab initio* rare-event simulation method. Our simulations sample reactive events that happen on the timescale of minutes and we demonstrated that autoionization can be initiated by the hypercoordination of a stretched OH bond and the compression of a hydrogen bond wire as suggested by Hassalani et al. (17). However, these are not sufficient conditions. Only when the wire is strongly condensed (<7.3 Å) and the stretched OH bond accepts four hydrogen bonds, does the reaction probability become significant (0.15), but only 0.6% of the reactive trajectories start off with such extreme conditions. The vast majority of reactive paths start with milder initial values for these two parameters. In this region of parameter space the reaction probability is largely enhanced compared with an arbitrary case, but still extremely small. Hence, the reaction takes place when additional structural parameters have values inside the right range. We identified additional structural parameters which correspond to the alignment of the hydrogen bond wire and the distortion from a tetrahedral arrangement. Hence, we showed that the local order parameters can be used to predict the self-ionization event, although it requires a combination of several conditions.

Due to the multiple correlated factors that influence the water autoionization, we combined our analysis method with ML techniques which identified additional parameters not considered before, in particular the O–H stretch of the oxygen closest to O^λ . Even though the ML result did not outperform the level of predictiveness by the human effort based on intuition, visual inspection of many molecular movies, and intensive trial-and-error approaches, the ML approach found all previously identified parameters very efficiently and, in addition, revealed some equally important parameters that were overlooked. We therefore believe that ML applied to path sampling has a great potential especially since data limitations will become less of an issue in the future due to the further expected increase of high-performance computing, a better parallelization scheme of sampling unequal trajectory-length path ensembles, and the use of more efficient Monte Carlo (MC) path-generating moves (37). It would therefore be promising to apply the same method to other aqueous-phase chemistry studies which so far have mainly been based on biased dynamics (31, 38).

The fundamental understanding of reaction triggers that can be gathered by this approach could open up avenues of practical applications. For instance, even if not all identified parameters correlating with reactivity will necessarily imply causal correlation, it is plausible that an intelligent manipulation of their equilibrium distribution via external electric fields (39) or inclusion of additives might lead to catalytic ways to steer reactions and in particular water dissociation.

Materials and Methods

Simulation Methods. The MD simulations required by the RETIS algorithm (14) were performed with the Born–Oppenheimer MD capabilities of the CP2K program package (40). We used the Becke–Lee–Yang–Parr (BLYP) functional with a DZVP-MOLOPT (41) basis set and a plane-wave cutoff of 280 Ry. The BLYP functional gives a reasonable description of the structure and dynamics of liquid water (42, 43) and the absence of dispersion corrections (44) is likely of minor importance for ion–water interactions where the dominant interactions are mainly electrostatic. However, we note that the BLYP functional is known to give an overstructured description of liquid water with a low diffusion coefficient (45). Previous studies on the recombination mechanism for water (17, 46) and for weak bases in water (18) have, however, found that the collective compression of the hydrogen bond wire and the motion of the protons are reproduced with different choices of the functional and basis set.

The initial system consisted of 32 water molecules placed in a cubic simulation box of $9.85 \times 9.85 \times 9.85$ Å³. All MD simulations were carried out

under constant energy (microcanonical) dynamics, with a time step of 0.5 fs and periodic boundaries.

The transition region was divided into 20 path ensembles by positioning RETIS interfaces at $\lambda = \{1.07, 1.10, 1.13, 1.16, 1.19, 1.22, 1.25, 1.28, 1.31, 1.34, 1.39, 1.43, 1.48, 1.52, 1.56, 1.80, 2.00, 2.50, 2.90, 3.29\}$ Å. In addition, a final interface was placed at $\lambda = \infty$ such that all trajectories were propagated until they reached the pure water state again. After generating an initial path for each path ensemble (this was done by repeatedly modifying the momenta of the particles and evolving the system forward in time until valid paths were obtained) the RETIS algorithm attempts to either swap paths between different path ensembles or generate new trajectories by the so-called shooting or the time-reversal move. In our simulations the probability of performing a swapping move was set to 50% while the probabilities of the two other moves were both set to 25%. New velocities for the shooting move were drawn from a Maxwell–Boltzmann distribution corresponding to an average temperature of 300 K.

We performed 24,000 MC moves for each path ensemble, using the RETIS algorithm. This generated between 8,000 and 18,000 distinct trajectories in each path ensemble. The length of the trajectories ranged from 13.5 fs to 1,365 fs and we disregarded the first 400 trajectories in our analysis.

Analysis of Trajectories. Crossing probabilities along the reaction coordinate λ were computed by matching the results of the different path ensembles. Projection of the crossing probability along λ' was obtained using the reweighting scheme of Rogal et al. (21) for the path ensembles in the transition interface sampling framework.

For trajectories harvested with the RETIS algorithm we calculated additional collective variables: the hydrogen bond wire length (w), the number of hydrogen bond donors (n_d) and acceptors (n_a), the orientation order parameter (q), and the angle formed by O^λ and its closest oxygen neighbors (q_{\cos}). Using the first configuration in each trajectory, hydrogen atoms were assigned to the closest oxygen atom and this defined the initial H₂O molecules. Then, the hydrogen bond network was obtained for each configuration in the trajectory. Hydrogen bonds were identified using the criteria of Luzar and Chandler (47) and all (shortest) hydrogen bond connections between all pairs of water molecules were determined using the Floyd–Warshall algorithm (48). This allowed us to represent the hydrogen bond structure as a graph. Next, the oxygen atom (O^λ) used in the definition of the order parameter was identified. With no OH[−] present, this is the oxygen atom for which the covalent O–H distance is largest and when we have OH[−] present in the system, this is the OH[−] oxygen atom. After identifying O^λ , we obtained the number of hydrogen bonds accepted (n_a) and donated (n_d) by the water species containing it. The relevant hydrogen bond wire was obtained using the following criteria: (i) The wire should contain the oxygen atom used for the order parameter (identified as explained above) when the order parameter first crossed 1.15 Å, (ii) the wire should contain i water species, and (iii) the wire should be the shortest of the wires where two criteria i and ii are met. The length of the wire was defined as the sum of the O–O distances of consecutive molecules in the wire.

The orientation order parameter measures the distortion from a tetrahedral orientation of four water molecules around a central molecule and is defined by (27, 28)

$$q = 1 - \frac{3}{8} \sum_{j=1}^3 \sum_{k=j+1}^4 \left(\cos \psi_{jk} + \frac{1}{3} \right)^2 \quad [3]$$

Here, ψ_{jk} is the angle formed by the central oxygen and its four nearest oxygen neighbors. The central oxygen is always O^λ or the oxygen with the largest OH bond for pure water or the OH[−] oxygen if it is present. For a perfect tetrahedral orientation $q = 1$ and it is $q \neq 1$ otherwise. The angle order parameter, q_{\cos} , was obtained directly as $q_{\cos} = \min(\cos \alpha, \cos \beta)$, where α and β are the two internal angles in the wire.

After calculating these additional collective variables, we analyzed the trajectories using the methodology of van Erp et al. (19). For the analysis we used 100 subinterfaces for both λ^r and λ^c for the range $0 < \lambda/\text{Å} < 6.4$. The histograms in the collective variable space were constructed using 20 bins for $4.0 \leq w_3/\text{Å} \leq 7.0$, $7.0 \leq w_4/\text{Å} \leq 9.6$, $9.0 \leq w_5/\text{Å} \leq 12$; 20 bins for $0 \leq q \leq 1$; and 25 bins for $-1 \leq q_{\cos} \leq 1$, while the bins (midpoints) were placed at $-0.5, 0.5, 1.5, \dots, 6.5$ for both n_a and n_d .

The classification models were constructed using CARTs (20) available within the R (49) software package. The mean of sensitivity and specificity was used as the classifier performance measure (50).

For the CART models we considered several sets of collective variables and we obtained these variables at the frame in the trajectories where the order parameter first crossed 1.15 Å. The trajectories were classified as reactive if they reached a $\lambda \geq 2$ and as nonreactive otherwise. The first set of collective variables consisted of all 4,560 atom–atom separations in the system, which gave a model in which the oxygen–oxygen distances were most important. This model did not lend itself to an easy interpretation and we next considered several models with a reduced number of collective variables.

In the best-performing model (performance measure for training 0.89 and for testing 0.88) we considered 138 collective variables: all oxygen–hydrogen distances for initially bound water molecules, all oxygen–oxygen distances involving O^λ , the averaged distances between O^λ and its $i = \{2, 3, \dots, 31\}$ oxygen neighbors, the cosine of all angles formed by O^λ

and its 4 closest oxygen neighbors, all of the collective variables considered in the predictive power analysis, and the Steinhardt order parameters of order 3, 4, and 6 (32). When performing the predictive power analysis for the collective variables used by the CART analysis, we used 20 bins in the range [0.7, 2.0] for oxygen–hydrogen distances and 20 bins in the range [1.0, 4.2] for oxygen–oxygen distances, and for angles and the Steinhardt order parameters we used similar bins to those for q_{\cos} and q given above.

ACKNOWLEDGMENTS. The authors thank Øivind Wilhelmsen for fruitful discussions. The authors thank the Research Council of Norway Projects 237423 and 250875 and the Faculty of Natural Sciences and Technology, Norwegian University of Science and Technology (NTNU) for support. This research was supported in part with computational resources at NTNU provided by the Norwegian Metacenter for Computational Science (NOTUR), www.sigma2.no.

1. Stillinger FH (1978) Proton transfer: Reactions and kinetics in water. *Theoretical Chemistry: Advances and Perspectives*, eds Eyring H, Henderson D (Academic, New York), Vol 3, pp 177–234.
2. Agmon N, et al. (2016) Protons and hydroxide ions in aqueous systems. *Chem Rev* 116:7642–7672.
3. Tuckerman M, Laasonen K, Sprik M, Parrinello M (1995) Ab initio molecular dynamics simulation of the solvation and transport of H_3O^+ and OH^- ions in water. *J Phys Chem* 99:5749–5752.
4. Marx D, Tuckerman ME, Hutter J, Parrinello M (1999) The nature of the hydrated excess proton in water. *Nature* 397:601–604.
5. Tuckerman ME, Marx D, Parrinello M (2002) The nature and transport mechanism of hydrated hydroxide ions in aqueous solution. *Nature* 417:925–929.
6. Aziz EF, Ottosson N, Faubel M, Hertel IV, Winter B (2008) Interaction between liquid water and hydroxide revealed by core-hole de-excitation. *Nature* 455:89–91.
7. Eigen M, de Maeyer L (1958) Self-dissociation and protonic charge transport in water and ice. *Proc R Soc A* 247:505–533.
8. Natzle WC, Moore CB (1985) Recombination of H^+ and OH^- in pure liquid water. *J Phys Chem* 89:2605–2612.
9. Trout BL, Parrinello M (1998) The dissociation mechanism of H_2O in water studied by first-principles molecular dynamics. *Chem Phys Lett* 288:343–347.
10. Trout BL, Parrinello M (1999) Analysis of the dissociation of H_2O in water using first-principles molecular dynamics. *J Phys Chem B* 103:7340–7345.
11. Sprik M (2000) Computation of the pK of liquid water using coordination constraints. *Chem Phys* 258:139–150.
12. Dellago C, Bolhuis PG, Chandler D (1998) Efficient transition path sampling: Application to Lennard-Jones cluster rearrangements. *J Chem Phys* 108:9236–9245.
13. van Erp TS, Moroni D, Bolhuis PG (2003) A novel path sampling method for the sampling of rate constants. *J Chem Phys* 118:7762–7774.
14. van Erp TS (2007) Reaction rate calculation by parallel path swapping. *Phys Rev Lett* 98:268301.
15. van Erp TS (2006) Efficiency analysis of reaction rate calculation methods using analytical models I: The two-dimensional sharp barrier. *J Chem Phys* 125:174106.
16. Geissler PL, Dellago C, Chandler D, Hutter J, Parrinello M (2001) Autoionization in liquid water. *Science* 291:2121–2124.
17. Hassanali A, Prakash MK, Eshet H, Parrinello M (2011) On the recombination of hydronium and hydroxide ions in water. *Proc Natl Acad Sci USA* 108:20410–20415.
18. Cuny J, Hassanali AA (2014) Ab initio molecular dynamics study of the mechanism of proton recombination with a weak base. *J Phys Chem B* 118:13903–13912.
19. van Erp TS, Moqadam M, Riccardi E, Lervik A (2016) Analyzing complex reaction mechanisms using path sampling. *J Chem Theory Comput* 12:5398–5410.
20. Breiman L, Friedman J, Olshen R, Stone C (1984) *Classification and Regression Trees* (Chapman & Hall, New York).
21. Rogal J, Lechner W, Juraszek J, Ensing B, Bolhuis PG (2010) The reweighted path ensemble. *J Chem Phys* 133:174109.
22. Piccini G, Alessio M, Sauer J (2016) Ab initio calculation of rate constants for molecule–surface reactions with chemical accuracy. *Angew Chem Int Edit* 55:5235–5237.
23. Van Speybroeck V, et al. (2015) Advances in theory and their application within the field of zeolite chemistry. *Chem Soc Rev* 44:7044–7111.
24. Dellago C, Bolhuis PG (2004) Activation energies from transition path sampling simulations. *Mol Simul* 30:795–799.
25. van Erp TS, Bolhuis PG (2005) Elaborating transition interface sampling methods. *J Comput Phys* 205:157–181.
26. Nilsson A, Pettersson LGM (2015) The structural origin of anomalous properties of liquid water. *Nat Commun* 6:8998.
27. Chau PL, Hardwick AJ (1998) A new order parameter for tetrahedral configurations. *Mol Phys* 93:511–518.
28. Errington JR, Debenedetti PG (2001) Relationship between structural order and the anomalies of liquid water. *Nature* 409:318–321.
29. Agmon N (1995) The Grothuss mechanism. *Chem Phys Lett* 244:456–462.
30. Marx D (2006) Proton transfer 200 years after von Grothuss: Insights from ab initio simulations. *ChemPhysChem* 7:1848–1870.
31. van Erp TS, Meijer EJ (2004) Proton-assisted ethylene hydration in aqueous solution. *Angew Chem Int Ed* 43:1660–1662.
32. Steinhardt PJ, Nelson DR, Ronchetti M (1983) Bond-orientational order in liquids and glasses. *Phys Rev B* 28:784–805.
33. Ma A, Dinner AR (2005) Automatic method for identifying reaction coordinates in complex systems. *J Phys Chem B* 109:6769–6779.
34. Mullen RG, Shea JE, Peters B (2014) Transmission coefficients, committors, and solvent coordinates in ion-pair dissociation. *J Chem Theory Comput* 10:659–667.
35. Friedman JH (2001) Greedy function approximation: A gradient boosting machine. *Ann Stat* 29:1189–1232.
36. Friedman JH (2002) Stochastic gradient boosting. *Comput Stat Data Anal* 38:367–378.
37. Riccardi E, Dahlen O, van Erp TS (2017) Fast decorrelating Monte Carlo moves for efficient path sampling. *J Phys Chem Lett* 8:4456–4460.
38. Galib M, Hanna G (2011) Mechanistic insights into the dissociation and decomposition of carbonic acid in water via the hydroxide route: An ab initio metadynamics study. *J Phys Chem B* 115:15024–15035.
39. Saitta AM, Saija F, Giaquinta PV (2012) Ab initio molecular dynamics study of dissociation of water under an electric field. *Phys Rev Lett* 108:207801.
40. Hutter J, Iannuzzi M, Schiffmann F, VandeVondele J (2014) cp2k: Atomistic simulations of condensed matter systems. *Wiley Interdiscip Rev Comput Mol Sci* 4:15–25.
41. VandeVondele J, Hutter J (2007) Gaussian basis sets for accurate calculations on molecular systems in gas and condensed phases. *J Chem Phys* 127:114105.
42. Sprik M, Hutter J, Parrinello M (1996) Ab initio molecular dynamics simulation of liquid water: Comparison of three gradient-corrected density functionals. *J Chem Phys* 105: 1142–1152.
43. Kumar PP, Kalinichev AG, Kirkpatrick RJ (2009) Hydrogen-bonding structure and dynamics of aqueous carbonate species from car-parrinello molecular dynamics simulations. *J Phys Chem B* 113:794–802.
44. Grimme S, Ehrlich S, Goerigk L (2011) Effect of the damping function in dispersion corrected density functional theory. *J Comput Chem* 32:1456–1465.
45. Gillan MJ, Alfè D, Michaelides A (2016) Perspective: How good is DFT for water? *J Chem Phys* 144:130901.
46. Hassanali A, Giberti F, Cuny J, Kühne TD, Parrinello M (2013) Proton transfer through the water gossamer. *Proc Natl Acad Sci USA* 110:13723–13728.
47. Luzar A, Chandler D (1996) Effect of environment on hydrogen bond dynamics in liquid water. *Phys Rev Lett* 76:928–931.
48. Cormen TH, Leiserson CE, Rivest RL, Stein C (2009) *Introduction to Algorithms* (MIT Press, Cambridge, MA), 3rd Ed.
49. R Core Team (2017) *R: A Language and Environment for Statistical Computing* (R Foundation for Statistical Computing, Vienna).
50. Brodersen KH, Ong CS, Stephan KE, Buhmann JM (2010) The balanced accuracy and its posterior distribution. *Proceedings of the 2010 20th International Conference on Pattern Recognition*, ICPR '10 (IEEE Computer Society, Washington, DC), pp 3121–3124.