

A data-entrained computational model for testing the regulatory logic of the vertebrate unfolded protein response

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ABSTRACT The vertebrate unfolded protein response (UPR) is characterized by multiple interacting nodes among its three pathways, yet the logic underlying this regulatory complexity is unclear. To begin to address this issue, we created a computational model of the vertebrate UPR that was entrained upon and then validated against experimental data. As part of this validation, the model successfully predicted the phenotypes of cells with lesions in UPR signaling, including a surprising and previously unreported differential role for the eIF2 α phosphatase GADD34 in exacerbating severe stress but ameliorating mild stress. We then used the model to test the functional importance of a feedforward circuit within the PERK/CHOP axis and of cross-regulatory control of BiP and CHOP expression. We found that the wiring structure of the UPR appears to balance the ability of the response to remain sensitive to endoplasmic reticulum stress and to be deactivated rapidly by improved protein-folding conditions. This model should serve as a valuable resource for further exploring the regulatory logic of the UPR.

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INTRODUCTION

The vertebrate unfolded protein response (UPR) is a complex signal-transduction pathway with multiple points of overlap and feedback (both positive and negative) and feedforward loops. At least three

pathways constitute the UPR, initiated by IRE1 (the ubiquitous α and tissue-specific β paralogues), PERK, and the partially redundant ATF6 α and β pathways (Parmar and Schröder, 2012). Although IRE1 mediates degradation of endoplasmic reticulum (ER)-associated mRNAs (known as regulated IRE1-dependent decay, or RIDD) (Hollien and Weissman, 2006; Hollien *et al.*, 2009) and PERK effects translational arrest (Harding *et al.*, 1999), each UPR pathway also culminates in transcriptional control. IRE1 does so through splicing of *Xbp1* mRNA, PERK through eIF2 α -dependent translation of the transcription factor ATF4, and ATF6 through S1P/S2P-dependent cleavage, which liberates an active transcription factor (Walter and Ron, 2011). The genes up-regulated by the UPR include most notably the gene encoding BiP (heavy-chain binding protein), which is one of the most abundant ER proteins and plays a central role in ER protein translocation and folding and ER-associated degradation (Gething, 1999; Nishikawa *et al.*, 2005). While in principle each pathway might regulate a distinct set of downstream genes, in reality there is considerable overlap among the targets regulated by each; the PERK pathway, in particular, appears to regulate a broad swath of target genes, including those also regulated by ATF6 and IRE1 (Harding *et al.*, 2003; Teske *et al.*, 2011).

One essential function of the vertebrate UPR is the need to balance the ability of cells to adapt to ER stress with the imperative to commit to apoptosis if the stress is too severe (Tabas and Ron, 2011;

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Abbreviations used: ATF, activating transcription factor; CHOP, C/EBP homologous protein; eIF, eukaryotic initiation factor; ER, endoplasmic reticulum; GADD, growth arrest and DNA damage inducible; IRE, inositol-requiring enzyme; MEF, mouse embryonic fibroblast; ODE, ordinary differential equation; qRT-PCR, quantitative reverse transcription PCR; RIDD, regulated IRE1-dependent decay; S1/2P, site 1/2 protease; TG, thapsigargin; UPR, unfolded protein response; XBP, X-box binding protein.

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Hetz, 2012). Adaptive and apoptotic signaling could in principle be under the control of different pathways. Yet none of the vertebrate UPR pathways is intrinsically apoptotic: each initiates both survival and cell death programs, and selective activation of only a subset of UPR pathways is not strictly required for cells to escape death and adapt to persistent stress (Rutkowski *et al.*, 2006). One example of this paradox is expression of the transcription factor C/EBP homologous protein (CHOP). CHOP is strongly associated with ER stress-induced cell death. Several mechanisms have been proposed to account for CHOP-induced cell death (Marciniak *et al.*, 2004; Puthalakath *et al.*, 2007; Li *et al.*, 2009), and so its exact role in the process is still uncertain. However, CHOP is of clear functional importance in that cells or animals lacking CHOP are protected from a wide variety of genetic, pharmacological, or biological insults that elicit ER stress (Zinszner *et al.*, 1998; Oyadomari *et al.*, 2002; Pennuto *et al.*, 2008; Song *et al.*, 2008; Namba *et al.*, 2009; Thorp *et al.*, 2009; Gao *et al.*, 2011). Yet CHOP expression alone is insufficient to commit cells to death, as even stresses that cells can survive without appreciable cell death elicit transient up-regulation of CHOP (Rutkowski *et al.*, 2006). In fact, one indicator that cells will not survive ER stress is *persistent*, rather than transient, expression of CHOP (Rutkowski *et al.*, 2006). Thus, a key requirement for understanding how cells live or die during ER stress is to determine how their expression of death-promoting factors such as CHOP is controlled directly by transcriptional regulation, and also indirectly by the expression of proteins such as BiP that alleviate ER stress and deactivate the UPR.

While important in adaptation and apoptosis, respectively, BiP and CHOP are also exemplars of the regulatory complexity of the vertebrate UPR. BiP mRNA expression is directly regulated by ATF6 (Yoshida *et al.*, 2000; Wu *et al.*, 2007; Yamamoto *et al.*, 2007), and yet its induction during stress depends partly on PERK activity as well (Luo *et al.*, 2003; Wu *et al.*, 2007; Teske *et al.*, 2011; Han *et al.*, 2013). Conversely, CHOP transcription is strongly regulated by PERK activation (Harding *et al.*, 2000a, 2003), but ATF6 also directly contributes to its expression (Ma *et al.*, 2002; Wu *et al.*, 2007). The purpose of this overlap is unclear, as are its consequences for cell survival versus cell death. However, this and many other related questions about why the UPR is structured the way it is are challenging to test experimentally.

We reasoned that a computational model that allowed disruptive alterations to be tested *in silico* could overcome this problem and illuminate the regulatory logic of the vertebrate UPR. The key elements in the UPR survival-versus-death axes appear to strongly depend on timing—it is persistent stress that sustains expression of CHOP and that elicits cell death. For this purpose, then, an ordinary differential equation (ODE) model holds the most promise, as it is appropriate when the components of a pathway are known but the temporal relationships among them must be investigated (Kim *et al.*, 2009). There have been several attempts to build ODE models of the UPR either in part or in full, each with its own strengths and limitations. The first rudimentary attempt modeled production and degradation of BiP and CHOP in order to test whether the discrepant degradation kinetics of these two components was sufficient to account for the phenotype seen in stress-adapted cells, where only stable BiP expression is observed (Rutkowski *et al.*, 2006). This approach left entirely open the question of how the upstream stress-sensing molecules (IRE1, PERK, and ATF6) influence response output. Later, a model examining the interplay between chaperone synthesis and translational attenuation in alleviating stress illustrated how translational attenuation protects better against distinct types of stresses (Trusina *et al.*, 2008; Trusina and Tang, 2010). We then

described a more complete ODE model of the UPR, accounting for both its activation and output (Curtu and Diedrichs, 2010). This model provided a framework of the UPR signaling network but was not parameterized. A more recent fully parameterized complete ODE model of the UPR described cell death versus adaptation as an emergent property of the response, but this model was not entrained on experimental data and was sparingly validated (Erguler *et al.*, 2013).

Our ultimate goal is to develop a computational model of the UPR that is biologically trustworthy, predicative, and explanatory. Toward that end, and starting from our existing framework (Curtu and Diedrichs, 2010), we strove to parameterize a UPR model that not only was entrained on experimental data, but also could be validated against genetically modified mouse embryonic fibroblasts (MEFs)—and that could then be used to query the regulatory logic of the response.

RESULTS

Describing the contributions of each UPR pathway to its output

To entrain, parameterize, and refine our initial ODE model of the UPR, we examined the behavior of MEFs treated with the ER calcium-depleting agent thapsigargin (TG). TG was chosen because it is robust, activates all three UPR pathways even at low doses (Rutkowski *et al.*, 2006), and does not depend on protein synthesis to elicit ER stress as does the other oft-used ER stressor tunicamycin. MEFs are a useful model cell type because they can be isolated even from knockouts that lead to prenatal lethality.

We first examined the response of MEFs lacking each of the three UPR stress sensors—PERK (Harding *et al.*, 2000b), ATF6 α (Wu *et al.*, 2007), and IRE1 α (Zhang *et al.*, 2011)—to varying doses of TG from 2.5 to 100 nM for 8 h in order to confirm the regulatory interactions among these sensors and the UPR targets BiP and CHOP. In this cell type, 2.5 nM TG is the lowest dose still capable of eliciting ER stress but allowing cells to adapt, 10 nM is the lowest dose that precludes net cell survival, and doses over 10 nM are superphysiological (Rutkowski *et al.*, 2006). As expected, CHOP protein up-regulation was essentially completely lost in *Perk* $^{-/-}$ MEFs, due to the effects of both ATF4 on *Chop* transcription and eIF2 α phosphorylation on CHOP translation (Palam *et al.*, 2011; Figure 1, A and B). In addition, while there appeared to be little effect of *Perk* deletion on up-regulation of BiP protein, at least at this time point (Figure 1A), it had a modest but significant effect on up-regulation of *Bip* mRNA, as shown previously (Wu *et al.*, 2007; Figure 1B). Also consistent with previous findings (Wu *et al.*, 2007; Yamamoto *et al.*, 2007), deletion of *Atf6 α* diminished (but did not eliminate) up-regulation of both BiP and CHOP (Figure 1, C and D). In contrast, the response of cells lacking IRE1 α was more complex. BiP up-regulation at the protein level was, if anything, enhanced in *Ire1 α* $^{-/-}$ cells, and *Bip* mRNA expression was not significantly different (Figure 1, E and F). CHOP up-regulation was compromised at low doses of stress but not at high doses (Figure 1, E and F). These results are consistent with the idea that IRE1 signaling contributes only indirectly to the up-regulation of either of these genes (Lee *et al.*, 2003) and with the absence of XBP1 binding sites (unfolded protein response elements, or UPRs) in both gene promoters.

Modification of the UPR wiring diagram

One feature of the experimental system used here that is apparent from these results is that UPR signaling can vary somewhat in

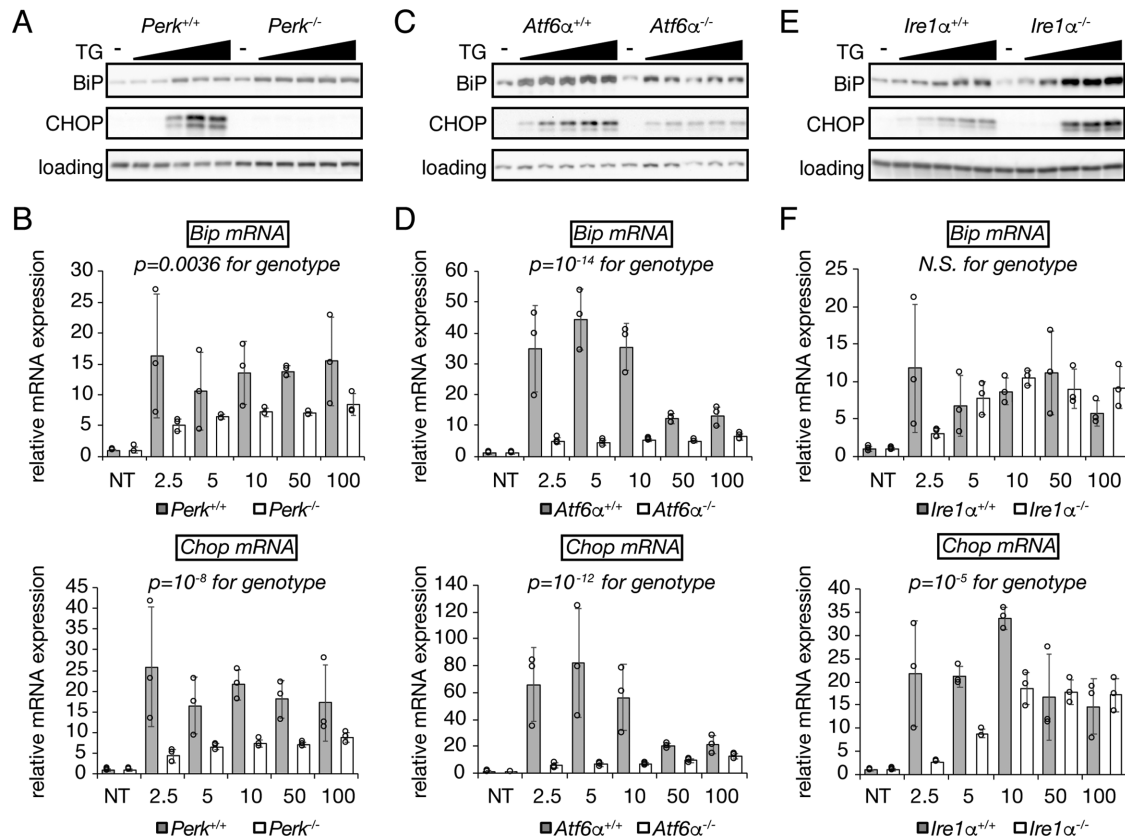


FIGURE 1: Contributions of PERK, ATF6 α , and IRE1 α to UPR output in MEFs. MEFs of the indicated genotype were treated with increasing concentrations of TG ranging from 2.5 to 100 nM, or with vehicle as a control. Cells were harvested for analysis by either immunoblot (A, C, E) or qRT-PCR (B, D, F). Statistical significance was calculated by two-way analysis of variance (ANOVA) for concentration and genotype; the *p*-value for genotype is shown (ANOVA for concentration was highly significant in all cases). Individual data points (three biological replicates) for qRT-PCR are shown as open circles, along with means \pm SDM from those replicates. The loading control for immunoblots was calnexin, the expression of which is not regulated by ER stress in MEFs. Note that the apparent enhanced up-regulation of *Bip* and *Chop* mRNA at low TG concentrations in *Atf6 α /+* cells is a somewhat atypical result relative to other wild-type MEF lines.

magnitude and duration from experiment to experiment, even under carefully standardized conditions. This is apparent even from the data in Figure 1, where different wild-type cells from highly backcrossed (>10 generations) animals—effectively isogenic cell lines—up-regulate *Bip* and *Chop* mRNA to different extents. The intensity of the response is subject to a number of influences, including cell passage number, degree of confluence, nutrient level, batch of stressor, cellular epigenetic status, and the individual conditions under which each line was isolated from its corresponding embryo, which are controllable to greater or lesser degrees. Thus, a useful computational model must be entrained on experimental data yet not overfit; rather than recapitulating the precise magnitude of any event, it must capture the trends that are consistent from one experiment to another.

We set about building an ODE model of the UPR based on the framework of our existing base model, which incorporated all three limbs of the UPR (Curtu and Diedrichs, 2010). A schematic diagram showing the components of this model and their interactions with each other is shown in Figure 2A, with the corresponding wiring diagram in Figure 2B. To avoid overspecification, we chose to model only relationships within the core framework of UPR signaling. These are as follows:

1. Unfolded proteins are generated by an input stress, which causes those proteins to associate with BiP.

2. Unfolded protein accumulation leads to activation of PERK and IRE1 by phosphorylation and activation of ATF6 by cleavage (Harding *et al.*, 1999; Haze *et al.*, 1999).
3. Activated IRE1 induces production of XBP1, the product of the spliced form of *Xbp1* mRNA (*Xbp1s*) (Shen *et al.*, 2001; Yoshida *et al.*, 2001; Calfon *et al.*, 2002; Lee *et al.*, 2002). Even though XBP1 does not directly up-regulate *Bip* mRNA, we modeled that relationship as a proxy for its general effect in improving protein folding through its action on other UPR target genes that are not part of the model. Activated IRE1 also activates a RIDD function (Hollien and Weissman, 2006; Hollien *et al.*, 2009). We modeled this effect as a diminution in the rate constants for unfolded proteins being synthesized and associating with BiP. We also modeled activated IRE1 as contributing to degradation of *Bip* mRNA via its RIDD function, as has been suggested by us (Gomez and Rutkowski, 2016) and others (Han *et al.*, 2009). Notably, because IRE1 has only modest effects in this system (Figure 1), the contribution of each of these pathways to overall model output is small.
4. Activated PERK phosphorylates eIF2 α (Harding *et al.*, 1999), which inhibits global protein synthesis (Wong *et al.*, 1993) to alleviate ER stress (Harding *et al.*, 2000b) and stimulates translation of *Atf4* mRNA (Harding *et al.*, 2000a).
5. ATF4 transcriptionally regulates CHOP (Harding *et al.*, 2000a), which, along with ATF4, transcriptionally regulates GADD34 (Novoa *et al.*, 2001; Ma and Hendershot, 2003).

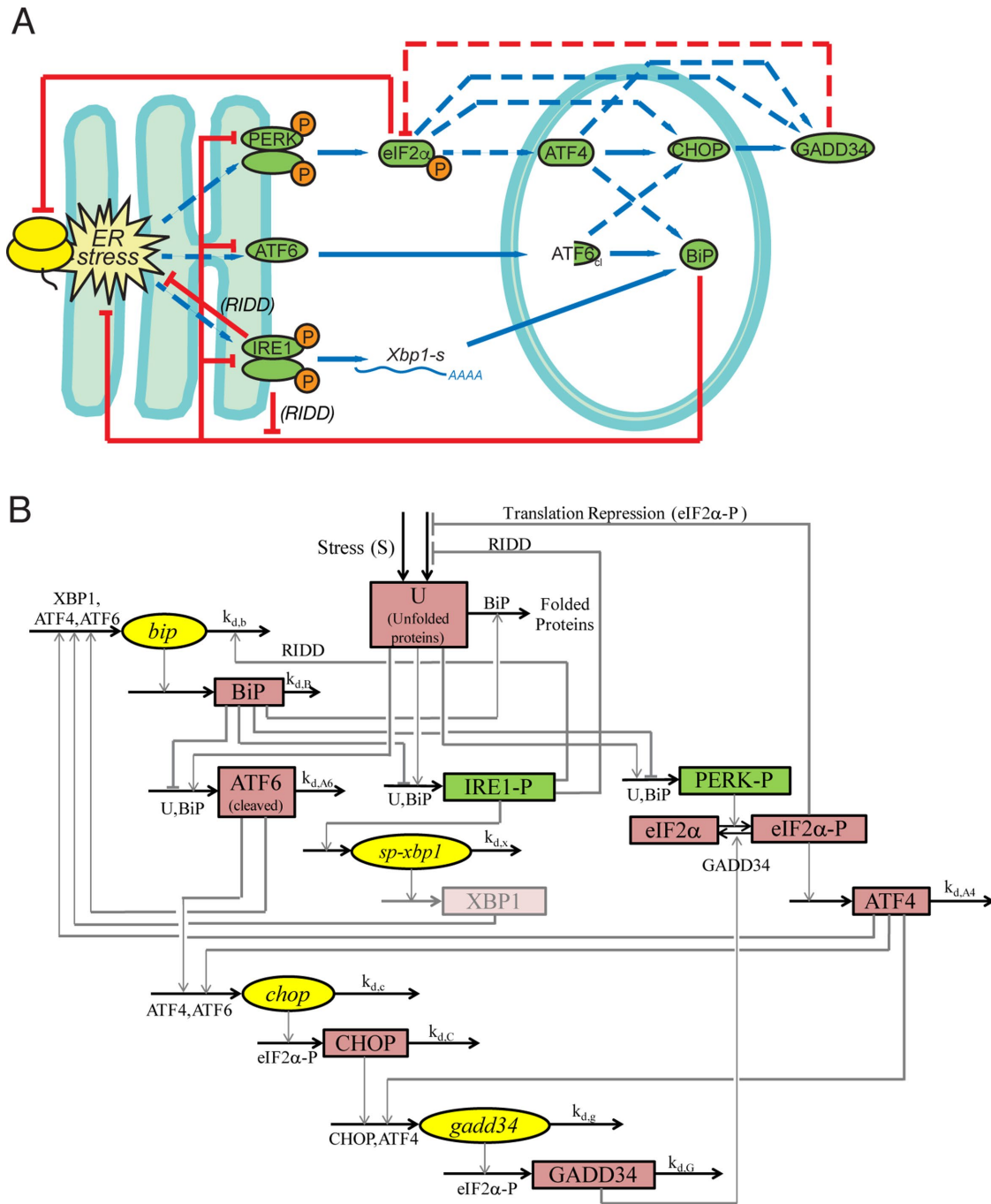


FIGURE 2: Modeled relationships among UPR components. (A) Schematic showing the relationships among UPR components accounted for by the model, with blue lines indicating stimulatory interactions and red lines inhibitory ones. Dashed lines denote relationships examined by *in silico* manipulation. (B) Wiring diagram depicting the same relationships shown in A, along with the relevant rate constants. The model simulates the concentration level for four specific mRNA (ellipse; yellow) and seven specific protein (rectangle; red) species (see Table 1, Eqs. 4–14). It also shows unfolded proteins. It defines PERK and IRE1 phosphorylation (rectangle; green) and free BiP (not shown in the wiring diagram) as functions of the unfolded proteins and total BiP (Table 1, Eqs. 1–3). For simplification purposes, *Bip* mRNA is here responsive to *Xbp1* mRNA, used as a proxy for XBP1 protein, which is not explicitly modeled.

6. Phosphorylated eIF2 α also translationally regulates both CHOP and GADD34 (Lee *et al.*, 2009; Palam *et al.*, 2011).
7. Cleaved ATF6 transcriptionally regulates both *Bip* and *Chop* (Haze *et al.*, 1999; Ma *et al.*, 2002).
8. ATF4 transcriptionally regulates BiP (Luo *et al.*, 2003; Han *et al.*, 2013).

9. BiP alleviates ER stress (by improving protein folding; Kassenbrock *et al.*, 1988; Morris *et al.*, 1997) and also directly suppresses activation of PERK and ATF6 (Bertolotti *et al.*, 2000; Shen *et al.*, 2002).

The list of equations is given in Table 1, and the definitions of each component and interaction are in Table 2. The model as constructed rests on the following simplifying assumptions:

$$B = \frac{B_{\text{tot}}}{1 + \frac{U}{K_{BU}}} \quad (1)$$

$$P_p = (1/f) \frac{U}{K_{UP} + \frac{K_{UP}}{K_{BP}} B + U} \quad (2)$$

$$I_p = (1/f_i) \frac{U}{K_{UI} + \frac{K_{UI}}{K_{BI}} B + U} \quad (3)$$

$$\frac{dU}{dt} = \frac{k_{s,U}}{1 + K_{UI}(I_p - I_p^*)} + S(t) - \delta \frac{U}{1 + K_{II}(I_p - I_p^*)} B \quad (4)$$

$$\frac{dE_p}{dt} = \frac{k_{ph} P_p (E_{\text{tot}} - E_p)}{K_{ph} + (E_{\text{tot}} - E_p)} - \frac{(k_{deph1} + k_{deph2}(G - G^*)) E_p}{K_{deph} + E_p} \quad (5)$$

$$\frac{dx}{dt} = \frac{k_{sp} I_p (x_{\text{tot}} - x)}{K_X + (x_{\text{tot}} - x)} - k_{d,x} x \quad (6)$$

$$\frac{dA6}{dt} = k_{c1}(U - U^*) \frac{A6_{\text{tot}} - A6}{1 + \frac{B}{K_{BA6}}} - k_{d,A6}(A6 - A6^*) \quad (7)$$

$$\frac{dA4}{dt} = \gamma(U - U^*) E_p - k_{d,A4}(A4 - A4^*) \quad (8)$$

$$\begin{aligned} \frac{db}{dt} = & \alpha_{A6}(1 + K_{b6} A4) \frac{(A6 - A6^*)^2}{(A6 - A6^*)^2 + K_{A6}^2 (1 + K_{th6} A4^n)} \\ & + \alpha_{A4}(1 + K_{b4} A6) \frac{(A4 - A4^*)^2}{(A4 - A4^*)^2 + [K_{A4}(1 + K_{th4} A6)]^2} \\ & + \alpha_X \frac{x - x^*}{K_{Xb} + (x - x^*)} - k_{d,b} \frac{1 + \alpha_I(I_p - I_p^*)}{1 + \beta_I(I_p - I_p^*)} (b - b^*) \end{aligned} \quad (9)$$

$$\frac{dB_{\text{tot}}}{dt} = k_{t,B} b - k_{d,B} B_{\text{tot}} \quad (10)$$

$$\begin{aligned} \frac{dc}{dt} = & \mu_{A4}(1 + K_{c4} A6) \frac{(A4 - A4^*)^2}{(A4 - A4^*)^2 + [K_{A4c}(1 + K_{th4c} A6)]^2} \\ & - k_{d,c}(c - c^*) \end{aligned} \quad (11)$$

$$\frac{dC}{dt} = [k_{t0,C} + k_{t,C}(E_p - E_p^*)] c - k_{d,C} C \quad (12)$$

$$\begin{aligned} \frac{dg}{dt} = & \eta_C \frac{(A4 - A4^*) + K_{A4g}(A4 - A4^*)(C - C^*)}{(A4 - A4^*) + K_{th4g}(A4 - A4^*)(C - C^*) + K_C} \\ & - k_{d,g}(g - g^*) \end{aligned} \quad (13)$$

$$\frac{dG}{dt} = [k_{t0,G} + k_{t,G}(E_p - E_p^*)] g - k_{d,G} G \quad (14)$$

TABLE 1: Model equations.

1. Separate differential equations are provided for both mRNA and protein species of BiP, CHOP, and GADD34. As the regulation of ATF4 is predominantly (though not exclusively) translational (Scheuner *et al.*, 2001; Lu *et al.*, 2004; Dey *et al.*, 2010), its transcription is not considered. UPR activation alters mRNA expression of several species in this model (*Atf4*, *Atf6*, and *Perk*) on the order of twofold (unpublished data), and these effects were not

considered here because of their relatively small magnitude, although further model refinement should include them.

- The total amounts of PERK (phosphorylated and unphosphorylated), IRE1 (phosphorylated and unphosphorylated), eIF2 α (phosphorylated and unphosphorylated), and ATF6 (cleaved and uncleaved) are held constant.
- XBP1 protein is presumed to be directly proportional to its spliced mRNA (*Xbp1s*), and thus the protein is not explicitly modeled. There is evidence that XBP1 protein produced from unspliced *Xbp1* mRNA can interfere with XBP1 protein produced from spliced *Xbp1* mRNA (Yoshida *et al.*, 2006), but given the relatively minor contribution of the entire IRE1/XBP1 pathway to this particular system, this species is not included.
- BiP is known to bind to PERK, IRE1, and ATF6, but BiP is much more abundant than these sensors (Ron and Walter, 2007); thus the total BiP concentration is approximated as the sum of free BiP and BiP in complex with unfolded proteins ($[BiP_{\text{tot}}] \cong [BiP] + [BU]$).
- BiP is taken as a proxy for transcriptionally up-regulated proteins that augment the ER protein folding capacity. In reality, there are dozens of such proteins, many of which, like BiP, are transcriptionally regulated by both the ATF6 and PERK axes (Wu *et al.*, 2007; Teske *et al.*, 2011), but there is little doubt that, as the most abundant chaperone in the ER lumen and the one with the widest substrate binding specificity, up-regulation of BiP is central to adaptation to stress.
- The folding process can be modeled by the following reactions: $BiP + U \rightarrow BU \rightarrow BiP + F$.

A free chaperone BiP associates with an unfolded protein U, converting it to a folded protein F, which releases the chaperone. Because these two reactions happen fast (within a few minutes) compared with the time scale of the other reactions of interest in the UPR (several hours), we made a quasi-steady-state assumption for BU. Using a mass-action law to model the kinetics of these reactions and setting

$$\frac{d[BU]}{dt} = 0$$

we determined that

$$[BU] = \frac{[BiP] \cdot [U]}{K_{BU}}$$

where K_{BU} is a positive constant. Equation 1 of the model (Table 1) is then obtained by incorporating this result into the equation for total BiP (see above).

- Under unstressed conditions, PERK exists in a complex with BiP (here called "BP"). An increase in unfolded proteins (induced by stress) causes the BiP–PERK complexes to dissociate. PERK is then free to come into contact with the unfolded proteins and multimerize (Gardner *et al.*, 2013), promoting its autophosphorylation and activating its downstream signaling function. Therefore, we assume that PERK is phosphorylated when it is associated with luminal unfolded proteins ($[PERK-P] \cong [UP]$, where "UP" represents these PERK-unfolded protein complexes). The dissociation of PERK from BiP and its subsequent association with unfolded proteins are fast reactions (a few minutes) compared with the time scales of interest in the UPR (several hours). Therefore, we made a quasi-steady-state assumption for the following reactions:



Appears in equation for variable	Parameter	Value	Units	Appears in equation for variable	Parameter	Value	Units
B , free BiP protein	K_{BU}	0.8	—	b , Bip mRNA	$k_{d,b}$	0.001284	min^{-1}
					α_{A6}	0.012	min^{-1}
Pp , Phosphorylated PERK	f	0.02	—	K_{b6}	0.56	—	
	K_{BP}	0.01	—	K_{A6}	3	—	
	$K_{UP} = \frac{(1/f-1)U^*}{1 + \frac{B_{tot}^*}{K_{BP}} \frac{1}{1+U^*/K_{BU}}}$	1.07824	—	K_{th6}	0.00001	—	
Ip , Phosphorylated IRE1 α	f_i	0.01	—	n	7	—	
	K_{BI}	0.01	—	α_{A4}	0.007	min^{-1}	
	$K_{UI} = \frac{(1/f_i-1)U^*}{1 + \frac{B_{tot}^*}{K_{BI}} \frac{1}{1+U^*/K_{BU}}}$	2.17848	—	K_{b4}	0.5	—	
U , Unfolded proteins	$k_{s,U}$	0.89	min^{-1}	K_{A4}	3	—	
	K_{UI}	0.01	—	K_{th4}	0.167	—	
	K_E	3	—	α_X	0.002	min^{-1}	
	K_{UU}	6	—	K_{Xb}	8	—	
	δ	1.5	min^{-1}	α_I	0.2	—	
	K_{II}	0.01	—	β_I	0.1	—	
Ep , Phosphorylated eIF2 α	k_{ph}	0.00651	min^{-1}	B_{tot} , total BiP protein	$k_{d,B}$	0.0002514	min^{-1}
	K_{ph}	14	—		$k_{t,B} = (k_{d,B}B_{tot}^*)/b^*$	0.0002514	min^{-1}
	E_{tot}	20	—	c , $Chop$ mRNA	μ_{A4}	0.1	min^{-1}
	k_{deph1}	0.03	min^{-1}		$k_{d,c}$	0.00393	min^{-1}
	k_{deph2}	0.08	min^{-1}		K_{c4}	0.56	—
	K_{deph}	7	—		K_{A4c}	2	—
x , Spliced $Xbp1$ mRNA	$k_{d,x}$	0.006546	min^{-1}	K_{th4c}	0.25	—	
	x_{tot}	16	—	C , CHOP protein	$k_{d,C}$	0.005478	min^{-1}
	k_{sp}	0.00785	min^{-1}		$k_{t,C}$	0.0001	min^{-1}
	K_X	3	—	$k_{t0,C} = (k_{d,C}C^*)/c^*$	0.005478	min^{-1}	
$A6$, Cleaved ATF6 α	k_{cl}	4	min^{-1}	g , $Gadd34$ mRNA	η_C	0.012	min^{-1}
	K_{BA6}	0.000016	—		K_{A4g}	0.75	—
	A_{6tot}	15	—	K_{th4g}	0.1	—	
$A4$, ATF4 protein	γ	0.001	min^{-1}	K_C	5	—	
	$k_{d,A4}$	0.00384	min^{-1}	$k_{d,g}$	0.003468	min^{-1}	
				G , GADD34 protein	$k_{d,G}$	0.003852	min^{-1}
					$k_{t,G}$	0.0015	min^{-1}
				$k_{t0,G} = (k_{d,G}G^*)/g^*$	0.003852	min^{-1}	

All steady state values are normalized under unstressed conditions: $P_p^* = I_p^* = x^* = U^* = E_p^* = A6^* = A4^* = b^* = B_{tot}^* = c^* = C^* = g^* = G^* = 1$.

TABLE 2: Definitions of variables and parameter values.

We modeled these reactions using a mass-action law in their steady state, setting the reaction speed in their differential equations to zero

$$\frac{d[BP]}{dt} = \frac{d[UP]}{dt} = 0$$

and solving the equations for [BP] and [UP], respectively, effectively converting these variables to dependent variables:

$$[BP] = \frac{[BiP] \cdot [PERK]}{K_{BP}}, \quad [UP] = \frac{[U] \cdot [PERK]}{K_{UP}},$$

where K_{BP} and K_{UP} are positive constants.

Because the total quantity of PERK is constant, we then obtained the amount of phosphorylated PERK from

$$\begin{aligned} [\text{PERK} - \text{tot}] &= [\text{PERK}] + [\text{BP}] + [\text{UP}] \\ &= [\text{PERK}] + \frac{[\text{BiP}] \cdot [\text{PERK}]}{K_{BP}} + \frac{[U] \cdot [\text{PERK}]}{K_{UP}} \\ &= [\text{PERK}] \left(1 + \frac{[\text{BiP}]}{K_{BP}} + \frac{[U]}{K_{UP}} \right) \\ &\equiv [\text{PERK} - P] \frac{K_{UP}}{[U]} \left(1 + \frac{[\text{BiP}]}{K_{BP}} + \frac{[U]}{K_{UP}} \right). \end{aligned}$$

With a notation for the percentage of total PERK that is phosphorylated under unstressed conditions ($f = \frac{[\text{PERK}-P]}{[\text{PERK}-\text{tot}]}$), this becomes

$$[\text{PERK}-P] = \frac{[\text{PERK}-P]}{K_{UP} + \frac{K_{UP}}{K_{BP}}[\text{BiP}] + [U]} [U]$$

which gives rise to Eq. 2 in the model. The same assumptions were made in modeling IRE1 (Eq. 3).

Model specification and fit

The model was entrained upon a representative data set quantifying mRNA expression of *Bip*, *Chop*, and *Gadd34* taken from wild-type MEFs. We chose RNA concentrations as the basis for entrainment because RNA species can be more easily and precisely quantified than can protein species by virtue of quantitative reverse transcription PCR (qRT-PCR). In addition, the use of only these three measures should in principle guide the model toward biological relevance without unnecessarily constraining it. A sense of the intrinsic biological variability of the response can be gained from Supplemental Figure S1, which compares the entrainment data set with an independent data set collected from a separate line of wild-type cells.

Of the 61 parameters (Table 2), nine degradation rates were previously experimentally determined: those of BiP mRNA and protein, CHOP mRNA and protein, GADD34 mRNA and protein, *Xbp1* mRNA, ATF4 protein, and cleaved ATF6 protein (Rutkowski *et al.*, 2006). In addition, we set $k_{t,B} = k_{d,B}$, $k_{t,C} = k_{d,C}$, and $k_{t,G} = k_{d,G}$ to ensure that the variables B_{tot} , C , and G (quantities of BiP, CHOP, and GADD34 proteins) remain at steady state levels under unstressed conditions. We also constrained the parameters K_{UP} and K_{UI} to ensure that P_p and I_p (phosphorylated PERK and IRE1, respectively) have their steady states normalized to 1. The remaining 47 parameters were unknown and had to be determined by fitting the solutions of the model to the experimental data using COPASI software.

There are, in principle, an infinite number of possible wiring diagrams and structures that could have been used to specify the model. Therefore, qualitative judgments about the likely relationships among components and how best to represent them mathematically drove the model creation. Furthermore, determining the numerical value of the parameters was an underdetermined problem, as the model had a large number of degrees of freedom, given by the number of unknown parameters, and a relatively sparse data set to constrain its solution.

The system was solved hundreds of times, each with a different set of parameters θ , and COPASI's numerical optimization algorithms guided the parameter search toward a set that best replicated the experimental data by finding a local minimum for the weighted residual sum of squares (RSS(θ)) between experimental data and simulation for all variables at all time points:

$$\text{RSS}(\theta) = \sum_{ij} w_j (x_{ij} - y_{ij}(\theta))^2$$

where x_{ij} is the experimental measurement of variable j at time step i and $y_{ij}(\theta)$ is the corresponding value given by the model using parameter set θ . COPASI's default method multiplies each squared residual by a weight factor $w_j = 1/(x_j^2)$, where $\langle x_j^2 \rangle$ is the mean value of the points x_j^2 in the trajectory for variable j . The purpose of this weight factor is to give the trajectories of each variable similar importance in the fit, regardless of their magnitude in relation to the other variables. The weight factors were scaled so that the maximal occurring weight for each stress level was 1, and all other weights

scaled accordingly. Thus, the RSS tests the goodness of fit of a parameter set against all other parameter sets, given the input equations. To further constrain the parameter search, we constrained each parameter to vary by a mean of no more than two orders of magnitude.

Our parameter search methodology combined this quantitative approach to the fit of the model to the variables for which we had experimental data with qualitative judgements as to reasonable simulation results in the other variables, in order to define an optimum parameter set θ^* with a low RSS and qualitatively correct solutions for all variables. Thus, although the optimal parameter set is not the one with the absolute lowest local minimum RSS determined by the search algorithm, it is not far from it. A random sampling of 200 parameter sets in our parameter space generated RSS values ranging from 43 to 4996. Only 3% of these parameter sets give RSS values below the RSS for our optimum parameter set (224). Supplemental Figure S2 shows a bee-swarm representation of the distribution of RSS values obtained from this simulation, which was repeated multiple times with similar results. This figure also shows an example of unsatisfactory model output arising from a lower-RSS parameter set, illustrating that the optimum model is one that combines a low RSS value with qualitatively faithful outputs.

The solutions to the ODE system with these parameters, modeled at stress levels of 2.5 or 10 nM TG based solely on varying the stress input function $S(t)$, are shown in Figure 3, compared with the entrainment data set for the mRNA expression of *Bip*, *Chop*, and *Gadd34* (also Supplemental Figure S1). The simulation shows both activation and deactivation/recovery phases of the UPR. The most important feature that we strove to recapitulate in parameter selection was the relative kinetics of both phases of the response. As is evident in Supplemental Figure S1, the model solution was faithful to real UPR kinetics within the context of inter- and intraexperiment variability. It is important to note that model fitting inevitably entails compromises; for example, attempts to make the resolution of *Gadd34* expression under the 2.5 nM condition more closely match the experimental data (by, for instance, peaking at 8 h rather than 12 h; Supplemental Figure S1C) resulted in a poorer fit under the 10 nM condition. The model represented the best-fit solution given these constraints.

The other qualitative feature that we wished the model to reproduce was the complete loss of CHOP and GADD34 up-regulation under conditions where cells can survive (i.e., 2.5 nM TG) but their persistence under conditions where cells cannot survive (i.e., 10 nM; Rutkowski *et al.*, 2006). The presented solution was able to successfully recreate this response (Figure 3, H and J), and was accompanied by a nearly complete resolution of unfolded proteins—i.e., a return to basal levels—under the 2.5 nM condition but not the 10 nM condition (Figure 3A). Finally, up-regulation of BiP protein had to persist long past the resolution phase of the response under both conditions (Rutkowski *et al.*, 2006); this behavior is seen in Figure 3M.

Validation of the model against knockouts

To test the biological trustworthiness of the model, we next tested the effects of *in silico* deletion of integral UPR components against the phenotypes of cells lacking those same components, both as reported in the literature and in our own experimental testing. The first of these deletions was PERK (Supplemental Figure S3); the most salient features that we expected the model to reproduce were nearly complete dependence of the downstream proteins ATF4, CHOP and GADD34 on PERK, and also a partial dependence of BiP up-regulation (Harding *et al.*, 2000a). Indeed, we observed these relationships (Supplemental Figure S3, F, H, J, and M), which

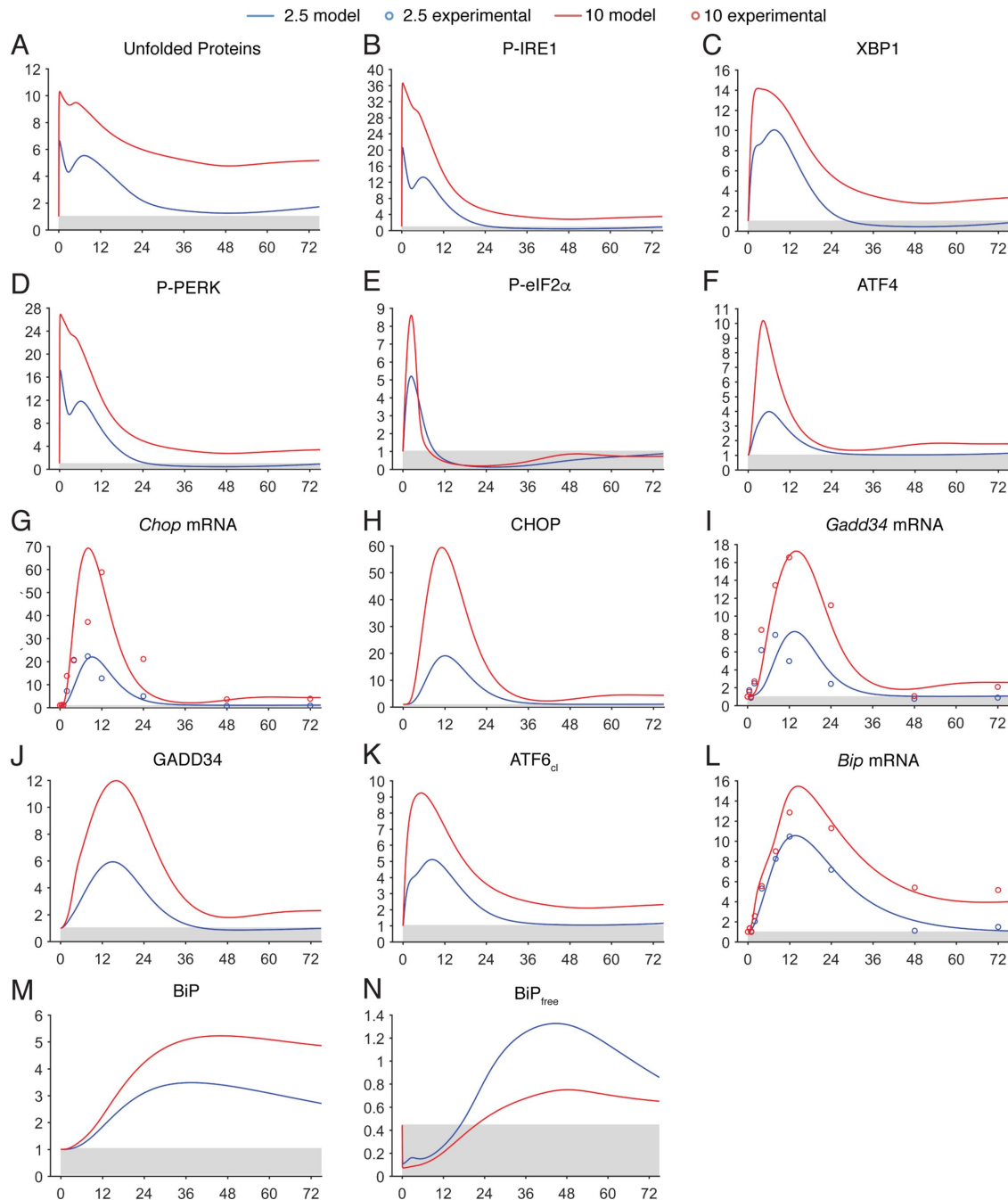


FIGURE 3: Comparison of model prediction against experimental data. The various outputs of the model under simulations of 2.5- or 10-nM TG treatment are shown (solid lines), with fold induction as the y-axis value. Superimposed (open circles) are experimental data for the same conditions, with only mean values shown for simplicity; means were collected from experiments conducted in biological triplicate. In this and subsequent figures, the gray shaded areas define the basal value for each component, and the x-axis denotes time in hours. See also Supplemental Figure S1.

followed naturally from ablation of eIF2 α phosphorylation (Supplemental Figure S3E). The attenuation of *Bip* up-regulation was seen despite elevated ATF6 cleavage (Supplemental Figure S3K), which followed presumably from an increased burden of unfolded proteins (Supplemental Figure S3A). We also modeled in silico deletion of IRE1; these results are shown in Supplemental Figure S4. As described above, the parameter set was chosen so that the contribution of the IRE1/XBP1 pathway would be modest, although its inclusion in the model means that its contribution can be more heavily weighted when other systems are being considered.

More stringent tests of the model would include ablation of components whose contribution to downstream targets was partial rather than complete, as these are likely to affect UPR output in more complex ways. Thus, we compared the result of in silico ATF6 deletion against cells lacking ATF6 (Figure 4; Supplemental Figure S5), since ATF6 contributes to but is not absolutely essential for the regulation of both BiP and CHOP (Wu *et al.*, 2007). Under both 2.5- and 10-nM stress conditions, in silico loss of ATF6 perpetuated ER stress (Figure 4A) and consequently, PERK activation (Figure 4B). Up-regulation of CHOP was blunted in the early phase of the

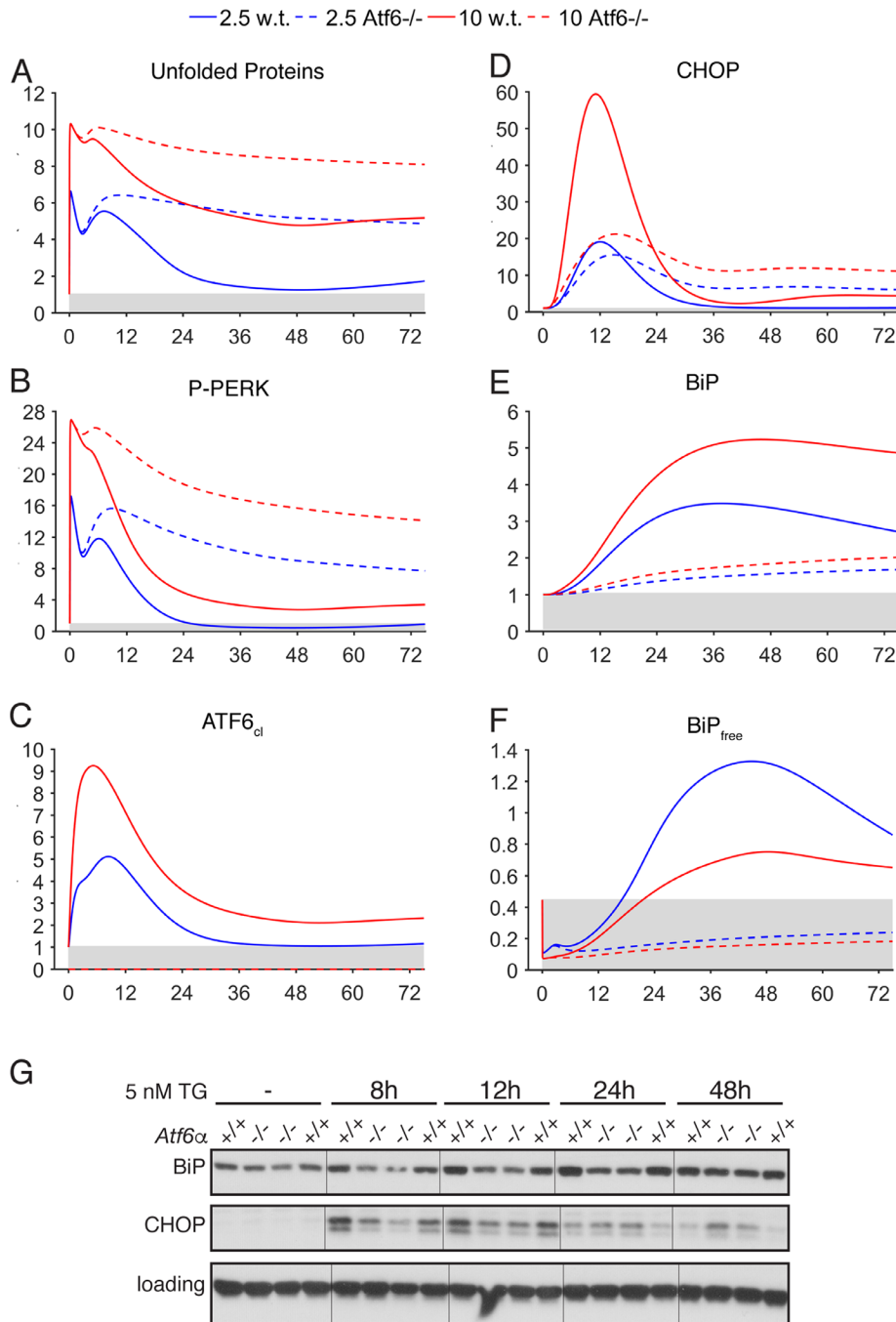


FIGURE 4: Comparison of model and experimental outputs for deletion of *ATF6 α* . (A–F) Selected model outputs are shown after *ATF6 α* was deleted in silico (dashed lines), compared against outputs in wild-type simulations (solid lines). (G) Wild-type or *Atf6*^{−/−} MEFs (two independent lines of each; genotype indicated above each panel) were treated with 5 nM TG for the indicated times, and expression of BiP and CHOP was assessed by immunoblot. See also Supplemental Figure S5. Loading control was α -actin. Hairlines are for visual clarity only.

response, but persisted long after being resolved or attenuated in the wild-type simulations (Figure 4D). BiP up-regulation was also compromised throughout the time course of the simulation (Figure 4E). The likely consequence of this attenuated BiP up-regulation was failure to restore levels of free (i.e., not bound by unfolded proteins) BiP (Figure 4F). While the true concentrations of unfolded proteins or free BiP are not readily measurable and are thus inferred, the expression of BiP and CHOP in cells was similar to the model's

predictions. In response to 5 nM TG (i.e., between 2.5 and 10 nM), CHOP up-regulation was reduced at early times but augmented at later times in *Atf6 α* ^{−/−} cells, as predicted by the model (Supplemental Figure S5O), while BiP up-regulation lagged throughout (Figure 4G).

We next conducted similar experiments comparing in silico deletion of ATF4 to *Atf4*^{−/−} cells (Figure 5; Supplemental Figure S6). Beyond dramatically compromising up-regulation of CHOP, as expected (Supplemental Figure S6, G and H), the model also predicted persistent phosphorylation of eIF2 α , likely due to failure to up-regulate the eIF2 α phosphatase GADD34 (Figure 5A). In fact, eIF2 α phosphorylation asymptotically approached an elevated steady-state level (Figure 5B) that persisted even when the simulation was continued for 250 h (unpublished data). Mirroring this prediction, eIF2 α phosphorylation diminished markedly from its initial 8-h peak in wild-type cells but not in *Atf4*^{−/−} cells (Figure 5C). ATF4 also directly binds to the *Bip* promoter (Luo et al., 2003; Han et al., 2013), and so the model predicted suppressed *Bip* up-regulation in the early phase of the response (Figure 5D). A suppression of *Bip* mRNA in *Atf4*^{−/−} MEFs was also seen experimentally (Figure 5E).

Our final validation test of the model was to delete GADD34 (Figure 6; Supplemental Figure S7), which modulates the regulatory step of eIF2 α dephosphorylation rather than an initiating step as with PERK, IRE1, ATF6, and ATF4. One of the most surprising previously unaccounted-for features of *Gadd34* deletion reported in cells is the failure of those cells to fully transcriptionally up-regulate BiP (Novoa et al., 2003). When we deleted GADD34 in silico, we found a dramatic diminution of unfolded proteins at intermediate times (4–24 h), consistent with the idea that GADD34 exacerbates ER stress by promoting ongoing protein synthesis in the stressed ER (Figure 6B; Marciniak et al., 2004). This diminished unfolded protein accumulation was also presumably responsible for blunted activation of ATF6 (Figure 6C), which in turn compromised up-regulation of *Bip* mRNA (Figure 6D) and protein (Figure 6E). Thus, our model to some extent mirrors and accounts for the phenotype of *Gadd34*^{−/−} cells.

Our model also makes a surprising prediction about the phenotype of *Gadd34*^{−/−} cells: at long time points under the 2.5-nM condition, *Gadd34*^{−/−} cells should have a greater unfolded protein burden (Figure 6B) than wild-type cells, while, paradoxically, the situation is reversed under the 10-nM condition. In other words, loss of GADD34 should sensitize cells to low concentrations of TG, but should protect cells from higher concentrations. Based on the model, the highest sensitivity to stress should be seen in wild-type

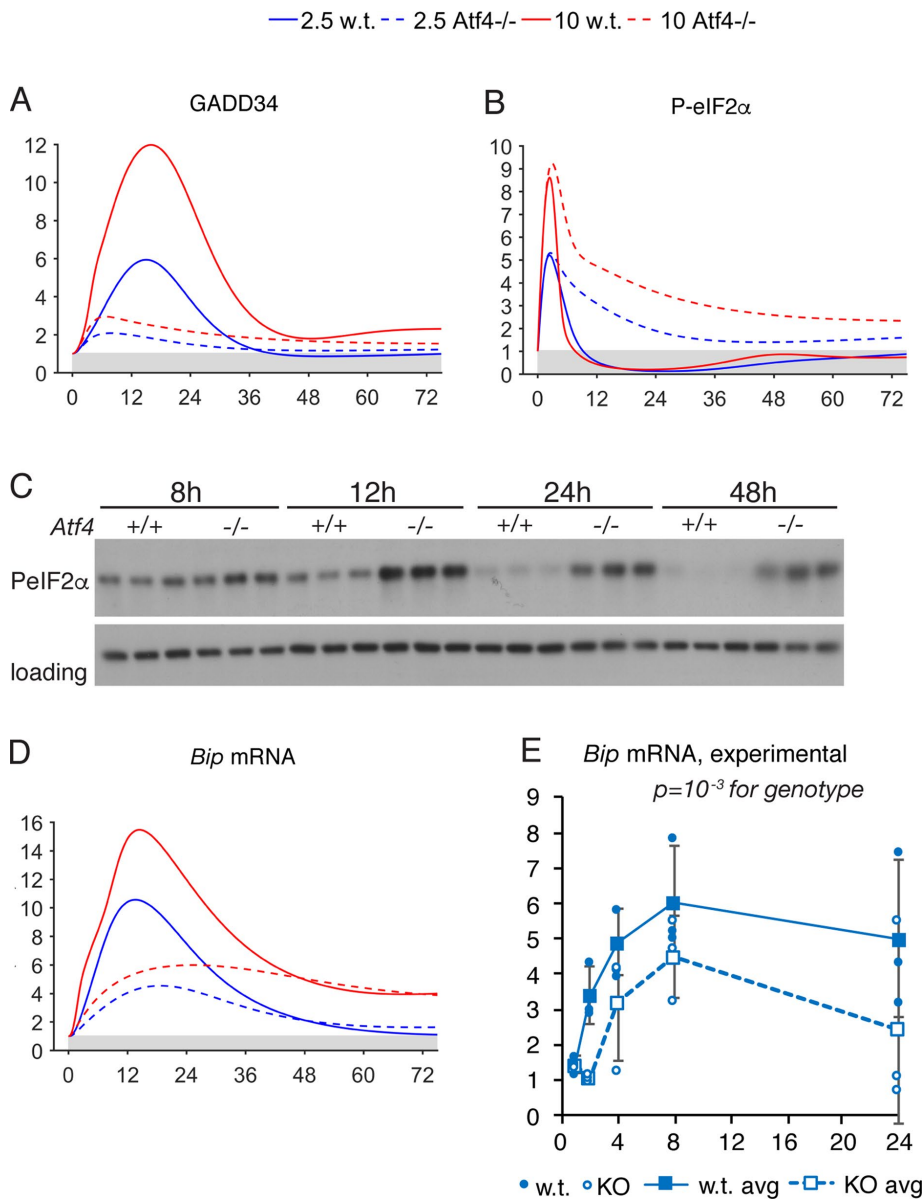


FIGURE 5: Comparison of model and experimental outputs for deletion of ATF4. (A, B, D) Selected model outputs are shown after ATF4 was deleted in silico (dashed lines), compared against outputs in wild-type simulations (solid lines). (C) Immunoblot showing the phosphorylated form of eIF2 α upon treatment of wild-type or *Atf4*^{-/-} MEFs with 2.5 nM TG for the indicated times. Loading control was calnexin. (E) qRT-PCR quantifying *Bip* mRNA expression in wild-type or *Atf4*^{-/-} MEFs upon treatment with 2.5 nM TG for the indicated times. Data were normalized against expression in cells of the same genotype treated with vehicle. Significance was calculated by two-way ANOVA for time and genotype.

cells treated with 10 nM TG, followed by *Gadd34*^{-/-} cells treated with 10 nM TG, then *Gadd34*^{-/-} cells treated with 2.5 nM TG, and last wild-type cells treated with 2.5 nM TG as the most resistant (from Figure 6B). To test this prediction, we treated cells with the GADD34 inhibitor salubrinal (Boyce *et al.*, 2005) and found that, indeed, inhibition of GADD34 activity paradoxically sensitizes cells to 2.5 nM TG but protects them from 10 nM (and 100 nM) TG (Figure 6, G and H).

Like any drug, salubrinal is an imperfect vehicle for probing GADD34 ablation; the more recently discovered GADD34 inhibitor Sephin1 was, in our hands, extremely toxic to MEFs on its own

(unpublished data). In addition, here we are taking viability as an indicator of sensitivity to stress. The true unfolded protein burden is difficult to quantify, and linking the unfolded protein burden to viability rests on the assumption that cell death follows from the ER stress level. Despite these caveats, the computational and experimental data are consistent at least to the extent that GADD34 has opposing effects on the cellular response to 2.5 versus 10 nM TG. These data also suggest that GADD34 seems not so much to accelerate cell dysfunction and death as to potentiate a steep threshold between adaptation and death.

Using the model to explore the regulatory logic of the UPR

Taken together, the above data show that the model makes predictions about UPR output that can be successfully tested experimentally. The validation experiments above lend confidence to the idea that the model captures the important temporal trends of the response and the relationships among its constituents. We thus used the model as a tool to explore the functional consequences of the regulatory pathways embedded within the UPR in in silico experiments that would be cumbersome to carry out in living cells. While many different questions might be asked with this model, we were particularly interested in examining how the output of a UPR stripped of its various feedbacks, feedforwards, and overlaps would differ from its actual output, and what implications these differences might have for UPR responsiveness and cell fate. We chose two such manipulations for these purposes.

We first tested the significance of translational stimulation of CHOP and GADD34 by eIF2 α phosphorylation (Figure 7; Supplemental Figure S8; Lee *et al.*, 2009; Palam *et al.*, 2011), which is consistent with the presence of short open reading frames in the 5' untranslated region of each mRNA akin to those found in *Atf4* mRNA. A priori, one might assume that the role of such a feedforward circuit would be to enhance the expression of both components. However, we found that this was not the case; instead, *ablation* of the contribution of eIF2 α to CHOP and GADD34 *enhanced* maximal up-regulation of both proteins (Figure 7, C and D). Rather, we observed that deletion of this feedforward loop changed the temporal sensitivity of the response: in wild-type cells, GADD34 was significantly up-regulated at earlier times than in feedforward-ablated cells and was likewise down-regulated more rapidly in the recovery phase (Figure 7, D and E; note that the dashed lines designating *Gadd34*^{-/-} cells begin their ascent later than the solid lines denoting wild-type cells). Thus, despite ultimately yielding a greater peak of GADD34 expression, feedforward-ablated cells

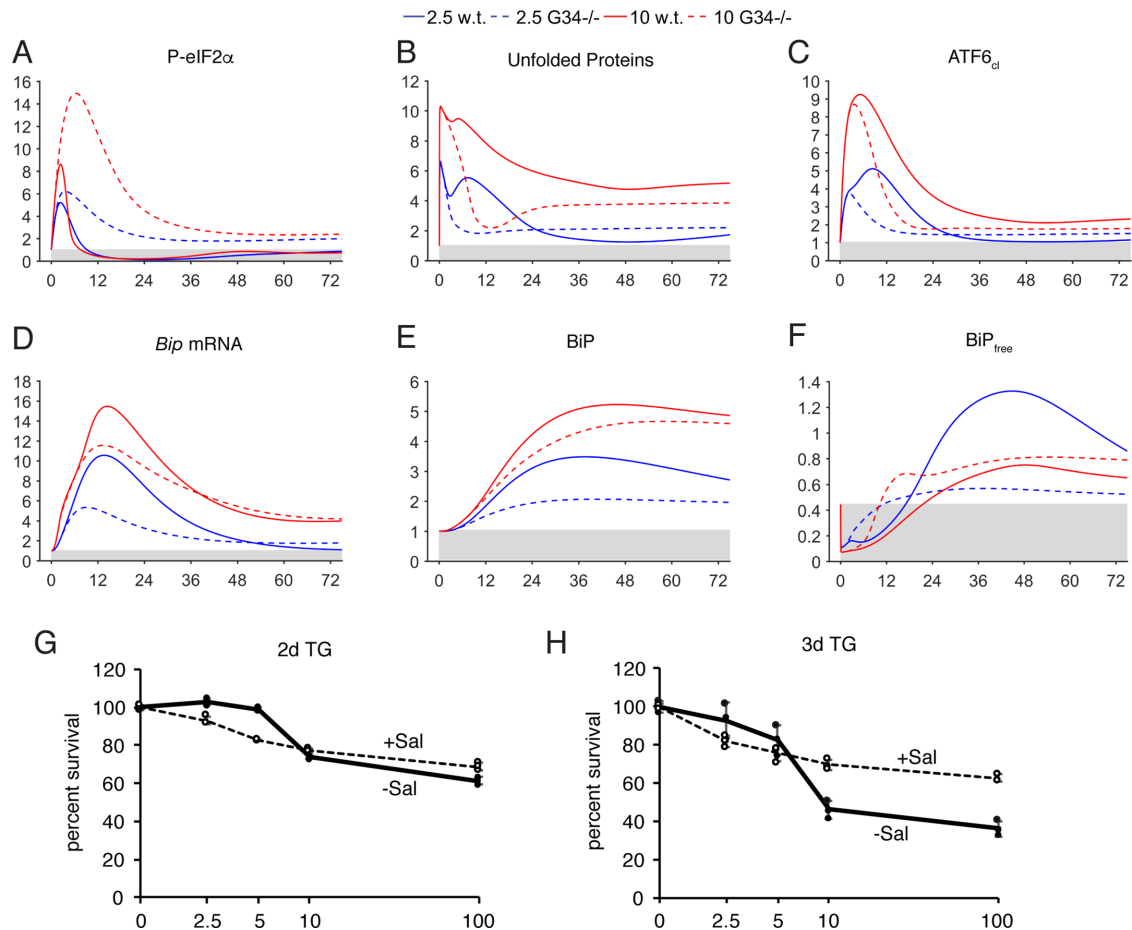


FIGURE 6: Model-predicted output for deletion of GADD34. (A–F) GADD34 was deleted in silico and various model outputs are shown. (G, H) Wild-type MEFs were treated for 2 or 3 d with the indicated concentration of TG in the presence or absence of 50 μ M salubrinal (Sal). An MTT assay was used to assess cell number relative to cells without TG. Error bars represent means \pm SDM. Individual data points from three samples of each condition are shown as open (+Sal) or filled (-Sal) circles.

showed elevated and more persistent phosphorylation of eIF2 α (Figure 7, F and G).

Next, we used the model to explore the regulatory logic underlying crosstalk between the PERK and ATF6 pathways. Namely, why does ATF6 contribute to CHOP expression when ATF6 largely regulates ER chaperones and other adaptive factors (Wu *et al.*, 2007; Adachi *et al.*, 2008)? Likewise, why does the PERK pathway (presumably through ATF4) regulate BiP expression when activation of the ATF6 pathway would seem adequate for that purpose? Thus, we either deleted the contribution of ATF6 to *Chop*, the contribution of ATF4 to *Bip*, or both (termed “linear,” since the crosstalk between pathways is removed; Figure 8; Supplemental Figures S9 and S10). As expected, deleting the ATF4 contribution to *Bip* caused unfolded proteins to persist (Figure 8B), presumably due to attenuated BiP up-regulation (Figure 8C). In contrast, deleting the ATF6 contribution to *Chop* had no effect on unfolded proteins; even though this deletion had a small effect on GADD34 production, this effect was not sufficient to alter eIF2 α dephosphorylation (Supplemental Figures S9 and S10). However, both deletions affected CHOP expression, but in distinct ways (Figure 8D). Deletion of the ATF6 contribution to CHOP caused CHOP expression to reach a lower peak, but to return to basal levels in the same time as in the wild type. Deletion of the ATF4 contribution to BiP caused CHOP to reach a greater peak. Its clearance occurred with similar kinetics as in the

wild type, but because of its greater maximum, its expression persisted longer. The linear simulation (i.e., the combination of both deletions) combined the features of both single deletions, so that CHOP expression was blunted, yet slower to resolve. This result was evident for both the 2.5- and 10-nM conditions (Supplemental Figures S9 and S10).

We reasoned that the tendency of BiP and CHOP to act at cross purposes in promoting adaptation or death, respectively, might make comparing the relative amounts of these two proteins an enlightening metric. From this ratio, it can be seen that crosstalk between the two pathways creates a condition under which the anti-adaptive pathway is relatively favored at earlier time points (notably, those that occur prior to the commitment to cell death, which occurs in the range of 12–16 h; Harding *et al.*, 2003), but then is rapidly disfavored at later time points (Figure 8, E and F). Absent the contribution of ATF4 to BiP, CHOP was both more favored and more persistent, while absent the contribution of ATF6 to CHOP, initial CHOP induction was blunted.

DISCUSSION

This paper establishes the first mathematical model for the dynamics of vertebrate UPR signaling entrained on experimental data. We constructed a wiring diagram based on qualitative knowledge about previously studied core UPR components and their hypothetical

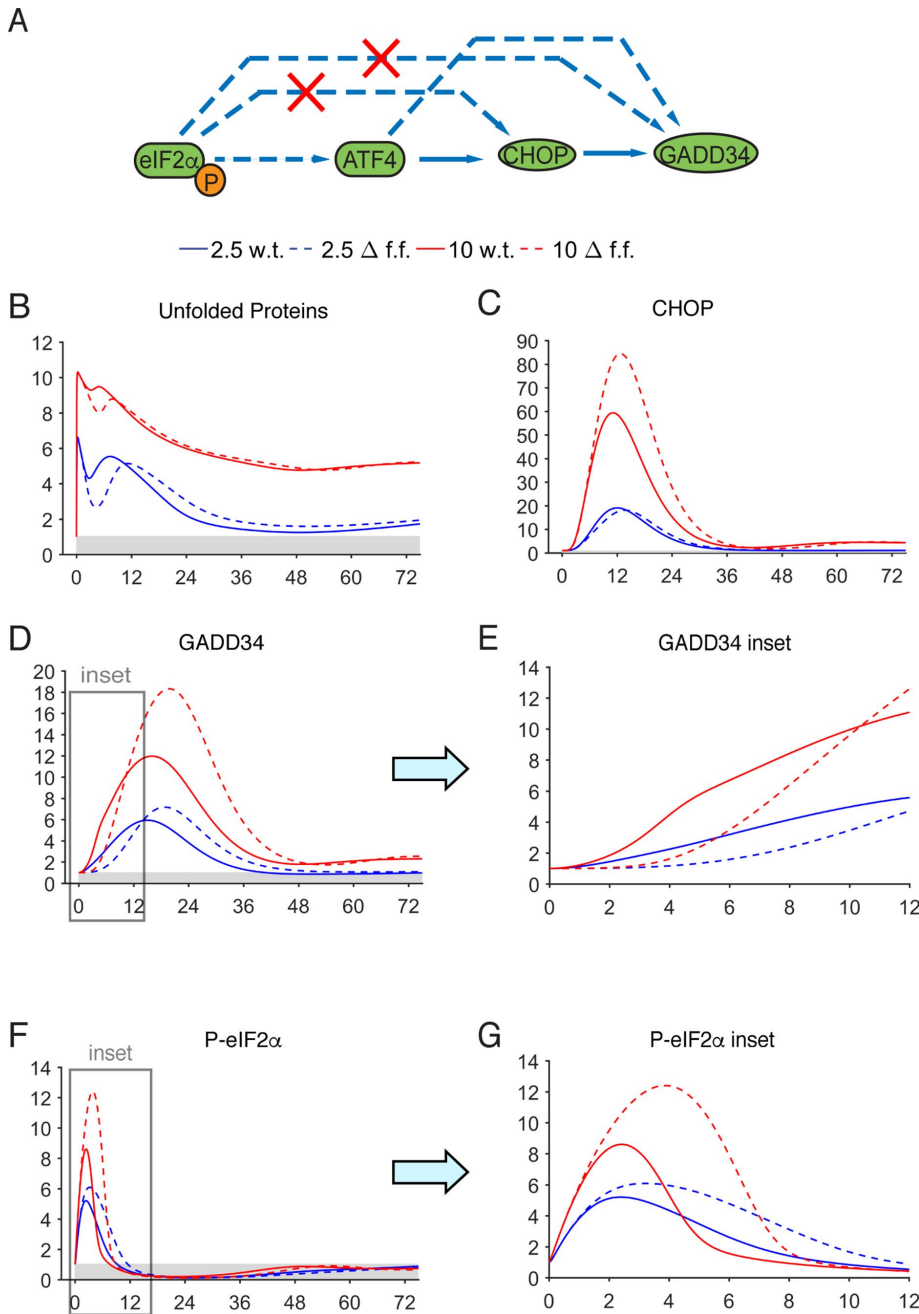


FIGURE 7: In silico deletion of feedforward control of CHOP and GADD34. (A) Schematic showing the steps targeted by in silico deletion (red “X”). (B–G) Model simulations were run after translational control of CHOP and GADD34 was removed by eIF2 α (Δ f.f.; dashed lines), compared against wild-type output (solid lines). Panels E and G are insets representing times 0–12 h for GADD34 and P-eIF2 α , respectively.

interactions, including the ATF6 and PERK signaling pathways and crosstalk leading to the expression of BiP, CHOP, and GADD34. Then we devised a framework to approach the construction of the ODEs associated with this wiring diagram, based on assumed biochemical reactions involving each node in the UPR’s network. Unknown kinetic parameters were determined by fitting the model’s solutions to experimental time-course data for relative increases of *Bip*, *Chop*, and *Gadd34* mRNA collected from wild-type MEFs under stress induced by thapsigargin in two different doses: low (2.5 nM TG) and high (10 nM TG). The model was validated by both

its fit to experimental data in wild-type cells and its ability to successfully predict the phenotypes of genetically or pharmacologically manipulated cells.

While the bulk of this manuscript is devoted to the building and validation of our model, the model’s ultimate intent was to understand why the UPR is structured the way it is. Toward that end, we conducted two in silico experiments testing manipulations that were not easily tested experimentally: eliminating eIF2 α -mediated translational stimulation of CHOP and GADD34 and ablating direct crosstalk between the PERK and ATF6 pathways. Both manipulations provided insight into the ways in which the structure of the UPR governs its responsiveness. The first suggested that the effect of feedforward translational stimulation of CHOP and GADD34 is not to augment their up-regulation, but rather to ultimately potentiate more rapid eIF2 α dephosphorylation—i.e., that eIF2 α initiates an autoregulatory negative feedback loop. The second manipulation suggested that a functional consequence of pathway crosstalk might be to make the CHOP-dependent apoptotic limb of the UPR maximally responsive to stress—allowing robust induction of CHOP while simultaneously permitting rapid CHOP loss when stress is alleviated. Experimentally testing these sorts of model predictions would require homologous-directed genome editing to make precise changes in the *Bip* or *Chop* promoters, or the *Chop* and *Gadd34* 5’ untranslated regions, plus identifying, selecting, and propagating targeted clones (or generating mutations in stem cells and then differentiating them into fibroblasts). Thus, experimental validation would be laborious, which highlights one of the major utilities of a computational model: by providing testable predictions, it can help identify experiments that are likely to be worth their time, effort, and cost.

How trustworthy are the predictions made by our model? The fact that the model recapitulates essential features of the response—and, more importantly, captures at least in general terms the behavior of the response when individual components are ablated—suggests that its predictions are likely

to be relevant. Of course, there are ways in which the model as currently configured can be refined. One of these is expansion of IRE1/XBP1 signaling. There is little doubt that IRE1 mediates essential UPR responses, particularly in professional secretory cells such as plasma lymphocytes, hepatocytes, and pancreatic acinar cells (van Anken and Braakman, 2005). The apparent lack of a direct contribution of IRE1 signaling to BiP and CHOP expression in MEFs (Figure 1, E and F) led us to minimize its contribution here, but its contribution to response output can be differently weighted when the model is applied to other systems. A more complete IRE1/XBP1 module would

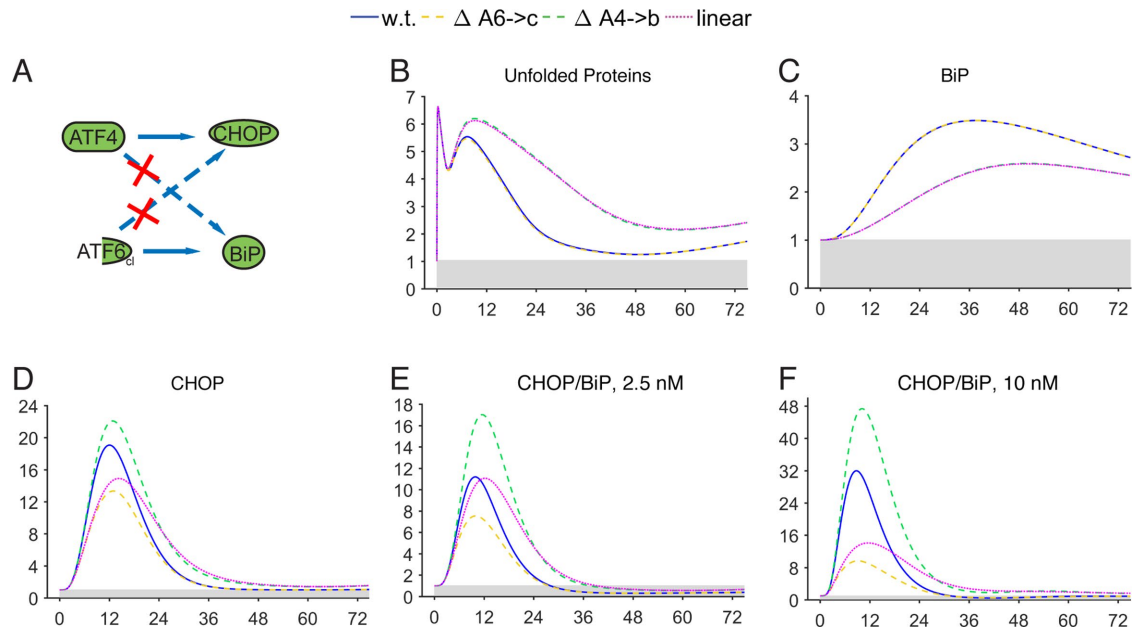


FIGURE 8: In silico removal of direct crosstalk between ATF6 and PERK pathways. (A) Schematic showing the steps targeted by in silico deletion (red "X"). (B–F) Model simulations were run after removal of the contribution of ATF6 to transcription of Chop ($\Delta A6 \rightarrow c$; yellow dashed line), the contribution of ATF4 to BiP transcription ($\Delta A4 \rightarrow b$; green dashed line), or both (linear; magenta dotted line). Selected model outputs for the 2.5-nM condition are shown (B–D). Panels E and F graph the ratio of CHOP to BiP during the simulation for 2.5- and 10-nM conditions, respectively.

explicitly include synthesis of active XBP1 protein from *Xbp1s* mRNA, as well as inhibition of that protein by XBP1 translated from unspliced *Xbp1* mRNA (Yoshida *et al.*, 2006).

The model's consideration of unfolded proteins will also ultimately need to account for different types of stimuli. The model is currently entrained upon only TG stress and could thus be expected to model other stresses that activate all three limbs of the UPR and that do not require protein synthesis to exert their effects, simply by changing the strength and dynamics of the input stress $S(t)$. Different stressors, such as inhibition of N-linked glycosylation, ER protein overload, or loading with saturated fatty acids, are likely to result in distinctly different activation profiles of the UPR. In fact, there is increasing evidence that the cell senses pharmacological ER stress differently from overexpression of a misfolded protein (Bakunts *et al.*, 2017; Bergmann *et al.*, 2018). Protein synthesis is not explicitly modeled in our system; including it would allow greater flexibility in modeling different stresses. Related to this point, the activity of the RIDD pathway in degrading ER-associated RNAs (and thereby reducing ER protein import) could then be modeled directly, rather than indirectly, as in our system.

Finally, there are many modulatory components that act upon UPR signaling pathways and that are themselves targets of UPR activation; certainly the response biologically cannot be distilled to just BiP, CHOP, and GADD34. Some of them, such as the putative negative regulator of ATF6 signaling WFS1 (Fonseca *et al.*, 2010), have already been included in attempts to model the UPR (Erguler *et al.*, 2013). While we have excluded such components in the interest of avoiding overspecification, a complete model must ultimately include them. It will be interesting to see where the predictions made by our model, as it is expanded by us or others, agree or diverge with those of Erguler *et al.* (2013). Although the inclusion of new components would necessitate reparameterization, our existing model provides a jumping-off point for such attempts.

This model opens many directions of future investigation for the vertebrate UPR research community. The model can be used to run a large variety of simulations to study the UPR under various types of external and internal conditions. The stress function $S(t)$ can be customized to model a variety of different external stress stimuli, including stresses that gradually build in intensity, periodic stress corresponding to repeated drug treatments, cyclical stress of varying intensity following the cell's reproductive cycle or the circadian rhythm, a short spike of ER stress lasting a few minutes to model a sudden insult, or a low-intensity stress of long duration to model a chronic disease. The stress function may also include more complex forms of stress that would be challenging to replicate in vitro.

In addition, the model can be used to predict how different cell types, which differ in their basal expression of UPR components, might respond to a given type of stress. For example, while the expression of the ER-resident stress sensors IRE1, PERK, and ATF6 is low in MEFs, these components are abundantly expressed in highly secretory cell types such as pancreas and liver. Does this elevated expression make the system more or less readily activated? And what would be the consequence of having one or two sensors highly expressed but not all three? A related question is which of the parameters modeled here are critical determinants of response output and which are minor modulators—a question that can be addressed by sensitivity analysis, which systematically varies parameters to identify those with the greatest contribution to response output (Turányi, 1990; Helton *et al.*, 2006).

Other areas for exploration can include adding stochasticity, defining parameters to be random variables (i.e., to test which might be subject to biological regulation), and performing a dynamic Monte Carlo simulation. Identifying potential alternative steady states for certain variables through bifurcation analysis is another direction, in particular to test whether UPR signaling migrates toward competing bistable states that reflect adaptive versus

apoptotic programs. Our hope is that this model might be used by the field as a starting point for refinement.

MATERIALS AND METHODS

Cell culture experiments

MEFs were harvested, cultured, and treated as described (Wu *et al.*, 2007) from wild-type animals or from *Perk*^{-/-} (Harding *et al.*, 2000b), *Atf6*^{α-/-} (Wu *et al.*, 2007), or *Atf4*^{-/-} (Hettmann *et al.*, 2000) animals or littermate controls. *Ire1*^{-/-} MEFs were prepared by in vitro deletion of immortalized MEFs isolated from *Ire1*^{fl/fl} animals (Zhang *et al.*, 2011) and were a gift from R. J. Kaufman (Sanford Burnham Institute). All animals were highly backcrossed (>10 generations) into the C57BL/6J line; thus wild-type MEFs isolated from any of these strains, or from pure C57BL/6J embryos, are considered effectively isogenic, and any differences in response are most likely due to non-genetic variables. Entrainment data displayed in Supplemental Figure S1 were taken from two independent experiments using two separate wild-type lines. Cells were always used prior to passage number five. Twenty-four hours prior to treatment, cells were plated at 2×10^5 cells per well in six-well dishes. TG and salubrinal were purchased from EMD Millipore (Darmstadt, Germany), dissolved in dimethylsulfoxide (DMSO), and aliquoted and stored at -20°C. TG treatments were carried out by preparing 1000x dilutions from stock in DMSO, adding to media in a tube, and then replacing existing media on cells with stressor-containing media. Quantitative RT-PCR and immunoblot experiments were carried out as described (Rutkowski *et al.*, 2006). Statistical analyses were performed as described in the figure legends. Antibodies were from BD (BiP; cat 610978), Santa Cruz (CHOP; sc-793), or Invitrogen (Pelf2α; 44728G). For MTT assays, cells were plated on 96-well dishes using a multi-channel pipette. After resting overnight, media were replaced with fresh media containing stressor. After the desired time in culture with media refreshed daily, MTT reduction was measured using the CellTiter 96 Aqueous One kit (Promega) according to the manufacturer's instructions.

Model construction and validation

Degradation rate constants were taken from Rutkowski *et al.* (2006), which in turn were generated from experimental measurements (RNA degradation rate constants from experiments in the presence of the transcription inhibitor actinomycin D, and protein degradation rate constants from experiments in the presence of the translation inhibitor cycloheximide). In addition, we set the protein synthesis rate constants at time $t = 0$ equal to the degradation rate constants for BiP, CHOP, and GADD34 to ensure that the amounts of BiP, CHOP, and GADD34 remained at a steady state value of "1" under unstressed conditions. We also constrained the value of parameters K_{UP} , K_{UI} in Eqs. 2–3 to ensure that in the absence of stress, phosphorylated PERK and IRE1 were also at steady state "1." The remaining parameters were derived by fitting the model solutions to experimental data.

All variables in the ODE system (Tables 1 and 2) were unitless and normalized to their steady state values under unstressed conditions. Table 3 shows the definition of each variable as well as baseline values for these quantities under unstressed conditions in terms of actual protein and mRNA quantities. The latter were chosen to capture the appropriate relative proportions of each species (Ron and Walter, 2007).

We used COPASI (Hoops *et al.*, 2006) to solve the model numerically using its ODE solver LSODAR (Petzold, 1983) and normalized the initial condition of all variables to 1 to reflect in silico the fact that up-regulatory and down-regulatory events are expressed in

Normalized variable	Quantification
$B = [BIP] / [\overline{BIP\text{-tot}}]$	—
$P_p = [PERK\text{-P}] / [\overline{PERK\text{-P}}]$	$[\overline{PERK\text{-P}}] = 30$
$I_p = [IRE1\text{-P}] / [\overline{IRE1\text{-P}}]$	$[\overline{IRE1\text{-P}}] = 30$
$U = [U] / [\overline{U}]$	$[\overline{U}] = 100$
$E_p = [eIF2\alpha\text{-P}] / [\overline{eIF2\alpha\text{-P}}]$	$[\overline{eIF2\alpha\text{-P}}] = 500$
$x = [x_{bp1\text{-sp}}] / [\overline{x_{bp1\text{-sp}}}]$	$[\overline{x_{bp1\text{-sp}}}] = 10$
$A6 = [ATF6\text{-cl}] / [\overline{ATF6\text{-cl}}]$	$[\overline{ATF6\text{-cl}}] = 100$
$A4 = [ATF4] / [\overline{ATF4}]$	$[\overline{ATF4}] = 100$
$b = [BiP] / [\overline{BiP}]$	$[\overline{BiP}] = 1600$
$B_{tot} = [BIP\text{-tot}] / [\overline{BIP\text{-tot}}]$	$[\overline{BIP\text{-tot}}] = 200,000$
$c = [Chop] / [\overline{Chop}]$	$[\overline{Chop}] = 100$
$C = [CHOP] / [\overline{CHOP}]$	$[\overline{CHOP}] = 100$
$g = [Gadd34] / [\overline{Gadd34}]$	$[\overline{Gadd34}] = 100$
$G = [GADD34] / [\overline{GADD34}]$	$[\overline{GADD34}] = 100$
	$[PERK\text{-tot}] = (1/f)[\overline{PERK\text{-P}}] = 1500$
	$[IRE1\text{-tot}] = (1/f_i)[\overline{IRE1\text{-P}}] = 3000$
	$[x_{bp1\text{-tot}}] = x_{tot}[\overline{x_{bp1\text{-sp}}}] = 160$
	$[eIF2\alpha\text{-tot}] = E_{tot}[\overline{eIF2\alpha\text{-P}}] = 10,000$
	$[ATF6\text{-tot}] = A6_{tot}[\overline{ATF6\text{-cl}}] = 1500$

TABLE 3: Model variables in terms of actual protein and mRNA steady state quantifications under unstressed conditions.

experimental data as fold changes. The units of the simulated time were minutes. The input stress was described as a rate function $S(t)$ measured in $[\text{min}^{-1}]$ and assumed here to be constant, with the difference between the unstressed condition and the 2.5 and 10 nM TG conditions being $S(t) = 0, S(t) = 2$, and $S(t) = 8 [\text{min}^{-1}]$, respectively. We then used $S(t) = 4 [\text{min}^{-1}]$ to simulate stress at 5 nM TG (Supplemental Figure S5O).

In silico deletions were created as follows: for PERK deletion, variable P_p was set to $P_p = 0$; for IRE1 deletion, $I_p = I_p^* = 0$; for ATF6 deletion, $A6_{tot} = 0$ and $A6^* = 0$; for ATF4 deletion, $A4^* = 0$ and $\gamma = 0$. For GADD34 deletion, $g^* = G^* = 0$ and $dg/dt = 0$, $dG/dt = 0$ in Eqs. 13 and 14; for deletion of the feedforward loop connecting eIF2α phosphorylation to CHOP and GADD34 translation, $k_{t,C}$ and $k_{t,G} = 0$; for $\Delta A6 \rightarrow c$ simulations, K_{c4} and $K_{th4c} = 0$; for $\Delta A4 \rightarrow b$, α_{A4} , K_{th6} , and $K_{b6} = 0$. The linear model incorporated both sets of changes. The COPASI file, allowing the model to be run and manipulated by others, is included in the Supplemental Materials and is also deposited in the BioModels Database under model ID# MODEL1803300000 (www.ebi.ac.uk/biomodels/).

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