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An in silico analysis of nanoparticle/cell diffusive transfer:

Application to nano artificial antigen presenting cell:T-cell interaction

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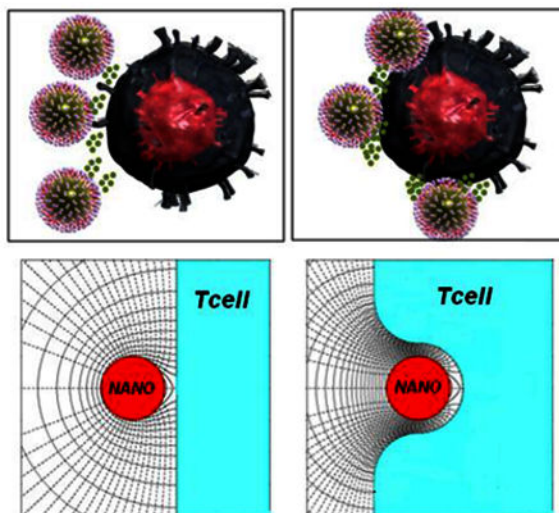
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Abstract

Polymeric nanoparticles (nano-paAPCs) modified with T-cell antigens and encapsulating immunostimulatory or immunoinhibitory factors may act as artificial antigen-presenting cells to circulating immune cells, improving the selective delivery of encapsulated drug or cytokine to antigen-specific T-cells. Paracrine delivery of encapsulated agents from these nanoparticles to adjacent cells facilitate sustained delivery lowering the overall administered dose, thus enhancing the overall drug efficacy while reducing toxicity of pleiotropic factors. Little is known mathematically regarding the local concentration of released agent that accumulates around a nanoparticle that is near or embeds in a cell. These concentration fields are calculated here in an attempt to understand paracrine efficacy of these nano-paAPC systems. The significant factor accumulation that can occur if the particles were to embed in the cell membrane may explain observed experimental data regarding enhanced T-cell activation and nanoparticle-mediated improvement in the drug delivery process to noninternalizing cellular targets.

Graphical Abstract

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Biodegradable nanoparticles (nano-paAPC's) impregnated with Interlukin-2 (IL-2) and surface modified with stimulatory and co-stimulatory T-cell ligands have been found to be efficient artificial antigen-presenting cells for T-cells. The present work is an attempt to better understand the efficacy of these particles by calculating the local IL-2 concentration as a function of the secretion characteristics of the nano-paAPC and particle/cell spacing. The potentially significant IL-2 accumulation found here, especially if the nano-paAPCs embed in the cell membrane, may explain observed experimental data regarding enhanced T-cell activation and nanoparticle-mediated improvement in the drug delivery process to non-internalizing cellular targets.

Keywords

Nanoparticle; artificial antigen presenting cell; immunotherapy; T-cell; diffusion; Interleukin-2; APC; drug delivery; analytical model

INTRODUCTION:

Several features of nanoparticle-mediated drug delivery make it an attractive modality for enhancing the therapeutic efficacy of pharmacologic agents. These particles can encapsulate a high density of bioactive factors and can be directed to specific cells or tissues. They can also be fabricated from materials that release factor in a slow, sustained fashion over variable time scales, from several days to months. Finally, because of the flexibility in controlling their synthesis and formulation, such particles can be extensively modified to enhance their bioactivity and regulate their transport to and metabolism within specific cells and organs.

While substantial progress has already been made in the fabrication of nanoscale drug delivery systems for biological applications¹⁻⁹, and there is a good understanding of the thermodynamic¹⁰ and biophysicochemical interactions at the nano-bio interface^{11, 12}, little is known about the quantitative aspects of nanoparticle-mediated drug delivery at the cell interface. Previous work in modeling of interactions between variously-sized particles, microcapsules, and cells has been quite limited; several articles have focused primarily on

thermodynamic properties of interactions between nanoparticles and cell membranes¹⁰; the role of particle size in receptor interaction, adsorption and Endocytosis¹³; the use of the particles themselves to signal and mediate motion of neighboring particles (in particular, for microfluidic applications that mimic biological cell signaling)¹⁴; hydrodynamic and adhesive interactions between nanocarriers and a cell surface (particularly relevant to the immunological synapse)¹⁵, and the development of microfluidic devices to help isolate and measure cell-cell and particle-cell interactions¹⁶. Thus, most of the literature has focused on the modeling and measurement of interactions between cells and particles themselves rather than on analyzing the paracrine diffusive transfer of encapsulated factors between a particle and a cell; these interactions are of significant interest for targeted drug delivery.

Specifically how does the proximity of a nanoparticle to a target cell influence the concentration and accumulation of factor in the contact region with target cells? This understanding is especially important for nanoparticles engineered to deliver cytokines or immunomodulatory factors to specific immune cell targets implicated in cancer or autoimmune disease. T-cells, for example, are exquisitely sensitive to antigen contact and the magnitude and type of the local cytokine milieu. Thus, the avidity of contact and nature of the local cytokine microenvironment can ultimately result in immune cell differentiation, proliferation or tolerance against a specific antigen^{17, 18}. For this reason, polymeric artificial presenting cells (paAPC)^{19, 20} that release cytokine in the vicinity of the T-cell^{21–23} are promising new tools for directing the magnitude and direction of an immune response inside and outside the body for active and adoptive immunotherapy respectively^{6, 21, 24, 25}

While cell-mediated immunity is well-studied, recent research has focused on applying “immuno-engineering” methodologies - such as nano-sized particle-based drug delivery for immune modulation^{6, 21, 24, 25}. Multiple teams have been developing biomimetic artificial cells capable of modulating cellular immunity: for example, previous work has demonstrated the creation of self-contained “artificial antigen-presenting cells” (aAPCs) using biodegradable polymeric nanoparticles^{6,21, 23, 26–28}. One example are nanoparticles encapsulating the immunomodulatory cytokine Interleukin-2(IL-2), presenting both costimulatory ligands and recognition ligands on the surface^{21,22}. As these systems contact T-cells and begin to degrade, the paracrine delivery of IL-2 amplified the T-cell expansion response already being seen by presentation of surface ligands. The paracrine accumulation of IL-2 in the contact region enabled an effective level of cytotoxic CD8 T-cell mediated therapy.^{21, 23}

The IL-2 receptor (CD25) is sensitive to directional secretion of a cytokine, specifically in synaptic junctions^{18, 29, 30}. The high-affinity IL-2 receptor, composed of alpha, beta, and gamma subunits, does not appear on the surface until approximately 24 hours following antigen encounter²⁹. In the initial phase of cell activation, therefore, these receptors are often few in number and poor in affinity resulting in a very low rate constant characterizing the internalization of the cytokine and the recycling of the receptor. With a scarcity of receptors, the T-cell is basically non-absorbing. Later stages of activation yield higher avidity receptors and the rate of factor absorption increases.

In the case of T-cells in contact with micron-sized artificial antigen presenting cells (micro-aAPCs) presenting T-cell antigens and releasing the stimulatory factor Interleukin-2 (IL-2), we have previously experimentally noted a striking impact on the magnitude of T-cell activation with much lower doses of IL-2²¹⁻²³. Similar observations have been reported through out the literature with different cell types in proximal contact with micro-and nano-sized particles releasing drug³¹⁻³³ inhibitory factors^{34, 35} or stimulatory factors^{7, 24}.

In order to better understand the mechanism by which particles activate cells, it is important to calculate the expected factor concentration near these “cells.” In this regard, our previous analytical work found that in the early stages of cell activation, when there is diffusive transfer of factors between two “cells” of comparable micron size (cell/cell or micro-paAPC/cell: one of which emits and the other receives factor), factor can significantly accumulate in the synaptic contact region leading to a substantial increase in local factor concentration^{21,36,37}. This accumulation was conjectured to effectively induce a T-cell response at much lower overall doses in contrast to free soluble factor. Our attention is turned here to interactions between a cell and nano-sized polymeric antigen presenting cells (nano-paAPC).

Little is known about the magnitude of factor accumulation when a nano-paAPC is in proximity with or embedded in a target cell. The nature of the particle/cell interaction is different than interacting micron sized particles/cells due to the physical size constraint arising from the ligand attachment length, which determines diffusive resistance. As will be shown, significant accumulation can occur but only if the nano-paAPC were to embed into cell membrane. Nanoparticle penetration of the cell membrane has been postulated to occur with a thermodynamic model described by Ginzburg¹⁰ and is independent of targeting if physiochemical factors (particle surface charge, hydrophobicity, size) minimize the free energy of interaction between the particle and the cell membrane¹². Depending on the degree of penetration, the resulting contorted synapse can offer sufficient diffusive resistance to yield “high” amounts of accumulation. The mechanism by which “high” degrees of accumulation can be achieved, therefore, is different for nano- as opposed to micro-particles.

The significant factor accumulation that these calculations predict may explain observed experimental results regarding enhanced T-cell activation with nanoparticles³⁸. Using nanoparticles encapsulating IL-2 attached to carbon nanotubes presenting T cell stimuli a 1000 fold lower cytokine amount achieves the same proliferation and expansion of antigen-specific T cells. Similar observations have been observed with nanoparticles presenting the same stimuli³⁹. This is not a cytokine-dependent phenomenon as it applies to other factors such Leukemia inhibitory factors (LIF) delivered in a paracrine manner to targeted CD4+ T cells⁴⁰ stem cells⁹ and pancreatic islet B cells⁴¹. These experimental observations highlight the need for understanding the level of accumulation at the nanoparticle-cell interface that these calculations provide.

METHODS

Governing equations and assumptions

Since our primary interest remains T-cell activation, this analysis will be limited to the case of non-absorbing (*naïve*) cells but can be extended to absorbing cells in the future. In this case the nano-paAPC exchanges factor only with the ambient medium with none “delivered” to the cell, so we are not looking at paracrine delivery per se, but rather what may be termed *paracrine factor accumulation* near the cell. The particles and cells are assumed to be spherical and in a quiescent, non-reactive, environment and the concentration field is *quasi-steady (QS)*, varying slowly with time. Under these conditions, the diffusion equation reduces to the Laplace equation that may be written in dimensionless form as:

$$\nabla^2 C^* = 0 \quad (1)$$

where C^* , the dimensionless factor concentration, is

$$C^* = (C - C_\infty)/(C_{\text{NANOiso}} - C_\infty) \quad (2)$$

C_{NANOiso} denotes the surface concentration of factor on the nano-paAPC if it was *isolated* (far away) from other cells and C_∞ is the factor concentration in the ambient medium. The terms “high” and “low” concentrations (C^*) used in the following are, therefore, in comparison to the concentration on the surface of an isolated nano-paAPC. A “high” C^* may not be very large in absolute terms. The C^* field near an isolated nano-paAPC is spherically symmetric, has unit value of the surface, and decreases inversely with distance (Figure 1a). Dimensionless quantities are designated with an asterisk (*) when they have a dimensional counterpart. Distances are measured in units of the nano-paAPC particle radius, R_{NANO} . Thus, the dimensionless synaptic gap width (S^*) is S/R_{NANO} . The Laplacian operator in Equation 1 is normalized by R_{NANO}^2 . The use of dimensionless quantities allows one calculation to be applied to many situations. For example, $S^*=0.4$ results can be applied to a 100nm diameter nano-paAPC with a 20nm synaptic gap (S) interacting with the cell; or a 50nm diameter nano-paAPC with a 10nm synaptic gap.

The local normal nano-paAPC surface flux will be assumed to be first order dependent on the local nano-paAPC surface concentration:

$$J_{\text{NANO}} = -D \, dC_{\text{NANO}}/dn = \beta (C_o - C_{\text{NANO}}) \quad (3)$$

Where D is the diffusion coefficient, C_o is the *saturation (equilibrium) concentration* at or above which the surface flux is zero, C_{NANO} is the local factor surface concentration, n indicates differentiation is normal to the surface, and β is the first order rate constant. In dimensionless form:

$$J_{\text{NANO}}^* = - dC_{\text{NANO}}^*/dn^* = \beta^* (C_o^* - C_{\text{NANO}}^*) \quad (4)$$

where

$$C_o^* = (C_o - C_\infty)/(C_{\text{NANOiso}} - C_\infty) \quad (5)$$

$$\beta^* = \beta R_{\text{NANO}}/D \quad (6)$$

It can be shown^{36,37} that when the nano-paAPC is isolated $J_{\text{NANOiso}}^*=1$ and since C_{NANOiso}^* is by definition unity, a simple relationship exists between β^* and C_o^* :

$$C_o^* = 1 + 1/\beta^* \quad (7)$$

Given that factor release from biodegradable polymer nanoparticles such as polyesters can occur in two distinct stages; a burst phase associated with release of factor entrapped at the surface and a slow polymer degradation phase associated with factor entrapment in the interior of the particle and release over prolonged periods, a simple expression such as Equation (3) cannot adequately describe such a complex sequence, but it does capture essential elements of the instantaneous transfer process. Besides, since our primary goal is to examine nano- vs micro- size effects, a fair comparison can only be made by adopting the same rate expression (Equation (3)) as previously used³⁷. If C_o^* is much greater than C_{NANO}^* , then the first order dependence of J_{NANO}^* on C_{NANO}^* can be ignored and J_{NANO}^* will have a constant value of $\beta^*C_o^*$, independent of the surface concentration. Under these conditions, the nano-paAPC act as a *constant flux source*. From Equation 7, *constant flux* behavior would be expected when $\beta^* \ll 1$, although, as will be seen, precisely how small β^* has to be for the flux to remain constant depends on the nano-paAPC environment. Constant flux behavior will occur when intra-particle diffusion is slow in comparison with external diffusion, as may be the case.^{42,43} A *constant flux source* in proximity with a cell is characterized by a non-uniform surface concentration. In the opposite extreme, when $\beta^* \gg 1$, $C_o^* \gg 1$ transfer is limited by diffusion through the medium. In this large β^* case, the nano-paAPC has a uniform surface concentration of unity but a non-uniform local surface flux.

If the T-cell is naïve the normal flux at any point on the cell membrane is zero:

$$J_{\text{CELL}}^* = 0 \quad (8)$$

Equation (1) must be solved subject to the boundary conditions on the surface of nano-paAPC (Equation 4) and on the cell wall (Equation (8)).

Method of solution

The curvature of the cell membrane is small on the nanoscale. If the nano-paAPC does not penetrate then curvature can be ignored and the interaction described as a nano-paAPC near a flat, non-absorbing, wall a distance $1+S^*$ from the nano-paAPC's center. This transfer situation is then equivalent to a nano-paAPC interacting with its image, with a center-to-center of $2(1+S^*)$ (see Figure 1B). When the image is identical (positive) to the nano-paAPC the cell wall midway between the particle and its image is non-absorbing. (Using a negative image would correspond to a perfectly absorbing cell wall.) The boundary condition represented by Equation (8) is automatically satisfied provided Equation(4) is imposed on both the nano-paAPC and its image. The problem can then be solved using the collocation methods described previously^{21,36,37}. These methods use N ring or panel singularities to describe the C^* -field between the nano-paAPC and its image. N equations for the N unknown singularity strengths are generated by satisfying Equation(4) at N surface points. By properly choosing the N points, a reasonable solution for the C^* -field can be obtained. For example, more collocation points should be located where the interactions are the strongest, such as near the synaptic axis points.

RESULTS

Concentration near a non-embedded Nano-paAPC

Figure 2 shows the C^* -field contours surrounding a nearly constant flux ($\beta^*=0.0001$) and a high β^* ($\beta^*=100$) nano-paAPC as a function of distance from a much larger, naive T-cell. Since no special considerations have been made that are specific to size, this and all of the following results, have general applicability to a spherical emitter of any size approaching a non-absorbing flat wall as, for example, a large particle near a vial wall.

When $S^*=10$ (Figures 2top), the C^* field is little affected by the value of β^* . The 0.3 and higher contours decrease inversely with distance and are spherically centered on the nano-paAPC, matching the contours of an isolated nano-paAPC (Figure 1A). The 0.2 contour, however, is no longer spherical but slightly eggshaped. At this spacing, the concentration at the indicated synaptic axis point (SAP) of the cell ($C_{Cell^*}|_{SAP}$) is virtually the same (0.18) for both values of β^* .

As the nano-paAPC moves closer ($S^*=5$) to the wall the 0.3 and lower contours intersect the wall and $C_{Cell^*}|_{SAP}$ is slightly larger than 0.3. The effects of β^* are small but evident. The 0.3 contour strikes the wall at a radius of 2.9 and 1.3 above the SAP when $\beta^*=0.0001$ and 100, respectively.

With further decrease in S^* , higher order contours intersect the cell wall and a corresponding increase in $C_{Cell^*}|_{SAP}$ and the effects of β^* become more evident. $C_{Cell^*}|_{SAP}$ increases from 0.5 to 1.02 with an increase in 0.5 contour strike radius from essentially zero to 3.5 as S^* decreases from 3 to 1 when $\beta^*=0.0001$. For $\beta^*=100$, $C_{Cell^*}|_{SAP}$ increases from 0.44 to 0.78 and the 0.5 strike radius increases only to 2.5 over the same range of S^* . If the actual synaptic gap (S) is 20nm, then $S^*=3, 2,$ and 1 correspond to nano-paAPCs that are 13.33nm, 20nm, and 40nm in diameter, respectively.

Figure 3 shows the fields for smaller S^* values when $\beta^*=0.0001$ (top) and 100 (bottom). The $S^*=0.4, 0.2$ and 0.1 spacings in these figures would correspond to nano-paAPCs of 100nm, 200nm and 400nm in diameter, respectively, if S remained 20nm. Of course, if S is greater or less than 20nm, the corresponding nano-paAPC size would change proportionately. The fields change dramatically due to the more intense interaction with the cell wall for these smaller values S^* , so close-up views of the synaptic region are provided as insets.

For a nearly decreasing S decreasing S ($\beta^*=0.0001$, Figure 3top), contours less than 0.7 are little affected by decreasing S^* . The strike radius of the 0.5 contour, for example, increases only slightly to a value of 3.9 as S^* decrease from 0.4 to 0.1. The effects of S^* are, however, much more dramatic for the high C^* contours near the SAP (see inset). The strike radius of the 1.4 contour increases from 0.6 to 1.05 as S^* decreases from 0.4 to 0.1. $C_{Cell}^*|_{SAP}$ increases from 1.53 to 2.29 coupled with an increase of $C_{Nano}^*|_{SAP}$ from 1.71 to 2.34 over this S^* range. Bear in mind that a C^* of 2.29 means that the concentration is 2.29 times greater than an isolated nano-paAPC. The dashed lines in the insets represent flux-lines. Since the nano-paAPC is nearly a constant source, the spacing between the flux-lines on the nano-paAPC's surface remains constant, but become parallel to the cell wall after leaving the nano-paAPC the closer the particle is to the wall. To maintain a constant flux, a non-uniform surface concentration on the nano-paAPC (and the cell wall) must exist.

Comparing Figure 3(bottom) with Figure 3(top) the C^* -field does not penetrate as far into the medium when $\beta^*=100$ compared with $\beta^*=0.0001$. For $\beta^*=100$, the 0.2 contour is near where the 0.3 contour when $\beta^*=0.0001$. The strike radius for the 0.5 contour is 2.6 compared with 3.9 for $\beta^*=0.0001$. In other words, the area of the cell wall that is bathed in a factor concentration that is greater than 0.5 of the isolated C^* is about 2.25 times larger for a constant source than for a nano-paAPC with $\beta^*=100$. The reason for this is that the $\beta^*=100$ nano-paAPC has a C_o^* of only 1.01, compared with 10001 for $\beta^*=0.0001$. Any factor accumulation, decreases the local rate of emission, as reflected in the increased spacing between the flux-lines in Figure 3bottom compared with Figure 3top. The SAP approaches saturation (1.01) and the local flux from the nano-paAPC in the synaptic region approaches zero. The overall transfer rate, thus, decreases the closer the high- β^* nano-paAPC is to the cell wall.

Figure 4 shows the dimensionless SAP concentration ($C_{Cell}^*|_{SAP}$) as a function of S^* over a range of β^* 's from 0.0001 to 100. Reflecting the qualitative observations in Figures 2 and 3, this graph shows the effect of β^* becomes important when S^* is small. At $S^*=2$, $C_{Cell}^*|_{SAP}$ falls within a narrow band from 0.57 to 0.67 over the 7 decade increase in β^* represented in this figure. The band narrows for larger S^* and eventually approaches zero for large S^* .

As S^* decreases, the $\beta^*=100, 10$, and 5 curves reach their saturation limits of 1.01, 1.1 and 1.2 for $S^*<0.1$. On the other hand, the $\beta^*<1$ curves are far from saturation for these values of S^* . It should be noted that the $\beta^*=0.05$ curve falls just slightly below the $\beta^*=0.0001$ curve. This means that a precise knowledge of β^* is not important in order to estimate $C_{Cell}^*|_{SAP}$. Indeed the utility of this curve lies in the limits it places on possible values of

$C_{\text{Cell}}^*|_{\text{SAP}}$. If $S^*=0.4$, corresponding to a 100nm diameter nano-paAPC with an S of 20nm, $C_{\text{Cell}}^*|_{\text{SAP}}$ would be between $0.96(\beta^*=100)$ and $1.53(\beta^*=0.0001)$.

Concentration near an embedded Nano-paAPC

It was shown in Labowsky and Fahmy³⁷, that cell shape has an important effect on micro-paAPC factor accumulation. If the micron-sized cells were allowed to deform as they interacted, creating a flat synaptic region of radius a^* , the $C_{\text{Cell}}^*|_{\text{SAP}}$ could easily be more than 20–30 times that of an isolated nano-paAPC for small values of β^* . The reason for this large increase in accumulation is the diffusive resistance of the synaptic gap: the higher the resistance, the higher the concentration gradient needed to expel secreted factor from the synapse. An analytical expression was provided in Labowsky and Fahmy (37) for the difference in concentration (Δ_{gap}^*) between the SAP and the edge of the synaptic region (a distance a^* from the axis) for the case of a constant source nano-paAPC interacting with a naïve T-cell:

$$\lim_{\beta^* \rightarrow 0} \Delta_{\text{gap}}^* = a^{*2}/4S^* \quad (9)$$

The narrower the gap or the larger the value of a^* , the greater is the diffusive resistance and, thus, the greater the factor accumulation and the higher the $C_{\text{Cell}}^*|_{\text{SAP}}$. While nano-paAPCs are not expected to deform significantly, if they did, the amount of additional accumulation would be considerably less than that experienced by micro-paAPCs due to the inverse dependence of Δ_{gap}^* on S^* . Deformations, even if they were to occur, therefore, will not appreciably increase factor accumulation for nano-paAPCs as they would for micro-paAPCs.

On the other hand, significant accumulation may occur if the nano-paAPC were to embed in or be partially encapsulated by the cell. The possibility of encapsulation was postulated by Ginzburg¹⁰ and was observed experimentally with confocal microscopy of nanoparticles interacting with cells⁷. To consider the case of embedded particles the numerical procedure in the above analysis, using the image of the nano-paAPC to assure a cell wall, has to be modified. Once the nano-paAPC penetrates the wall collocation points have to be placed not only on the nano-paAPC but also on the cell wall. Further, without prior knowledge concerning how the cell will react in response to penetration by the nano-paAPC, certain liberties must be taken with regard to the shape of the wall. The initial cell indentation (See Figure 1C) is spherical with a radius of $1+S^*$ (centered on the nano-paAPC) up to the “encapsulation angle,” at which point it smoothly blends into an off-axis radius of $1+S^*$. This off-axis radius in turn blends into the nondeformed (flat) portion of the wall. The nano-paAPC and Cell are in “contact” up to the encapsulation angle (Θ). Beyond Θ the distance between the particle and cell exceeds the attachment length (S^*). This is a less precise calculation because the collocation points can stretch only so far up the cell wall and so the wall is not perfectly flat beyond a certain distance (~ 6 nano-paAPC radii) as it was for the non-embedded case.

Figure 5a shows the concentration contours (solid) and flux-lines (dashed) near a nano-paAPC for various degrees of “encapsulation” (Θ) for the case of $S^*=0.4$ when $\beta^*=0.0001$. As may be seen, as Θ increases the concentration contours compress and $C_{Cell}^*|_{SAP}$ increases to 1.58, 2.48, 5.79, 9.67, 12.81 and 20.54 for Θ 's of 10, 45, 90, 110, 120, and 130, respectively. For a Θ of 120 and 130, the concentration contours are so compressed that identification of individual contours is difficult. So, order of magnitude increases in $C_{Cell}^*|_{SAP}$ are possible for large degrees of encapsulation. In addition to the increased $C_{Cell}^*|_{SAP}$, the area of the cell wall that is bathed in an enhanced concentration increases with Θ . Increased accumulation over an extended area should increase the chances of cell activation. It should also be noted that the flux-lines become more focused and directed outward from the encapsulation cavity and may serve as a significant signaling beacon that can draw bystander cells to the penetration site.

Figure 5b shows $C_{Cell}^*|_{SAP}$ as a function of Θ for $S^*=0.4, 0.6, 0.8$ and 1.0 for $\beta^*=0.0001$. All of the curves have similar shapes with relatively small increases in $C_{Cell}^*|_{SAP}$ for $\Theta < 90$. For $\Theta > 90$ and especially for $\Theta > 120$, accumulation rapidly increases with encapsulation. If the synaptic gap is 20nm, then the S^* curves would correspond to nano-paAPCs with diameters of 100nm, 67nm, 50nm and 40nm, respectively. Since the $S^*=0.4$ curve is above the rest, a larger nano-paAPC would seem to be more effective than a smaller one with respect to factor accumulation. On the other hand, it will be more difficult for a larger particle to deeply penetrate the cell. So, while in principle accumulation will be greater the larger the particle, the degree of encapsulation required for this greater accumulation may not be attainable.

Figure 5b also shows that the concept of a “constant source” must be qualified. As $\Theta \rightarrow 180$, $C_{Cell}^*|_{SAP}$ increases until it is no longer negligible in comparison with C_o^* . When Θ is sufficiently large, the transfer rate from the nano-paAPC will eventually begin to decrease and a “constant source” will stop being constant. Indeed, for complete encapsulation ($\Theta=180$), the concentration would reach the equilibrium concentration ($C_o^*=10001$ for $\beta^*=0.0001$); the entire nano-paAPC surface will saturate and all transfer cease until receptors begin to appear on the cell. Designation as a “constant source” is dependent on the ratio the time to emit factor to the diffusion time through the medium. As the cell closes around the nano-paAPC, diffusive resistance dramatically increases, thereby increasing the characteristic diffusion time and the transfer from the nano-paAPC ceases to be constant. With full encapsulation the area of cell wall that is immersed in the equilibrium concentration would be $4\pi(1+S^*)^2$. Transfer will resume only after the cell activates and high quality factor receptors begin to appear on the included surface.

The degree of encapsulation at which C_o^* is approached depends on β^* . For a β^* of 0.0001 this concentration is not approached until the nano-paAPC is nearly fully encapsulated. In contrast, for a high- β^* ($\beta^*=100$, Figure 6) $C_{Cell}^*|_{SAP}$ (0.97) is within computational error of C_o^* (1.01) at $\Theta=10$. The field and flux-lines are much less dramatic than for $\beta^*=0.0001$ in Figure 5a. The cell and nano-paAPC surfaces below and to the right of the 1.0 contour are essentially saturated. As Θ increases, this saturated region spreads further behind the nano-paAPC. Factor flux from the saturated surface shuts down resulting in fewer flux-lines, and a lower bystander signal gradient.

DISCUSSION

Labowsky and Fahmy^{36,37} discuss in detail the assumptions and limitations of using a boundary collocation method to solve problems in diffusive transfer. We note that Equation 3 provides a simplified description of release rate of factor from a nano-paAPC. A more rigorous, but much more complicated, approach to this problem would involve simultaneously solving the internal and external diffusion equations at each instant in time. This requires an empirical estimate of the rate constants and depends on both the polymer material and method of formulation. Equation 3, however, does capture important elements of the more rigorous solution provided it is realized that C_o will decrease with time because a nano-paAPC has only a limited supply of factor. Temporal variations in C_o , however, should be low especially for low β particles. The limited factor supply also sets a limit on the distance from the nano-paAPC over which the concentration field will approach the quasi-steady predictions. Indeed, the quasisteady approximation is reasonably valid near the surface of the nano-paAPC. Fortunately, this is exactly the region of interest here.

It should be emphasized that “high and “low” dimensionless concentrations are in comparison with that at the surface of an isolated nano-paAPC. A “high” C^* may in fact not be very high in absolute terms. In this regard, for small particles emitting a limited number of molecules, the concept of “concentration” must be viewed in a probabilistic sense. At any instant in time, a snapshot in the vicinity of the cells may show few if any molecules. Viewing many snapshots, however, the probability of seeing a molecule at a given location would be directly related to the calculated “concentration.”

Generally, the application of this analysis goes beyond cell activation with nano-paAPCs. The current focus in pharmaceuticals is shifting to a ‘smart drug’ paradigm, in which increased efficacy and decreased toxicity are the motivating factors. It has been envisioned that this could be achieved with targeted nanoparticles, where repertoires of targets and a series of drugs could yield new generations of highly specific therapeutic agents. Interactions of nanoparticles and cells are critical on this front for understanding both the therapeutic effect as well as the design criteria and formulation of the nanosystems needed to achieve this therapeutic effect. In the case of nanoparticles for immunotherapies, the combination of targeting and sustained delivery results in high local concentrations and continuous cytokine signaling. These effects result in modulation of the cytokine milieu surrounding the targeted immune cell, leading to therapeutically relevant changes in immune cell homeostasis. Continuous local delivery also allows for novel techniques to determine the role of such signals in the long-term properties of T-cells. Central to understanding cellular interactions is knowledge of the concentration fields that surround the particle and the cell. If “high” local concentrations are the key to T-cell activation, then it is critical to know when such concentrations will occur. For micro-sized cells, these high concentrations can occur as a result of the high diffusive resistance in the synapse when the cell surfaces deform.³⁷ Due to their small size, nanoparticles are not expected to deform but, as the above analysis shows, “high” concentrations can occur if the particles were to embed in the cell membrane. While the means (encapsulation rather than deformation) is different in both cases local accumulations more than an order of magnitude greater than the isolated surface concentration can occur, depending on the depth of penetration and the secretion

characteristics of the nano-paAPC, and may explain the therapeutic efficacy of these particles. Future experimental work should not only examine nano-paAPC secretion rates and encapsulation but also establish how “high” factor accumulation needs to be in order to stimulate cell activation.

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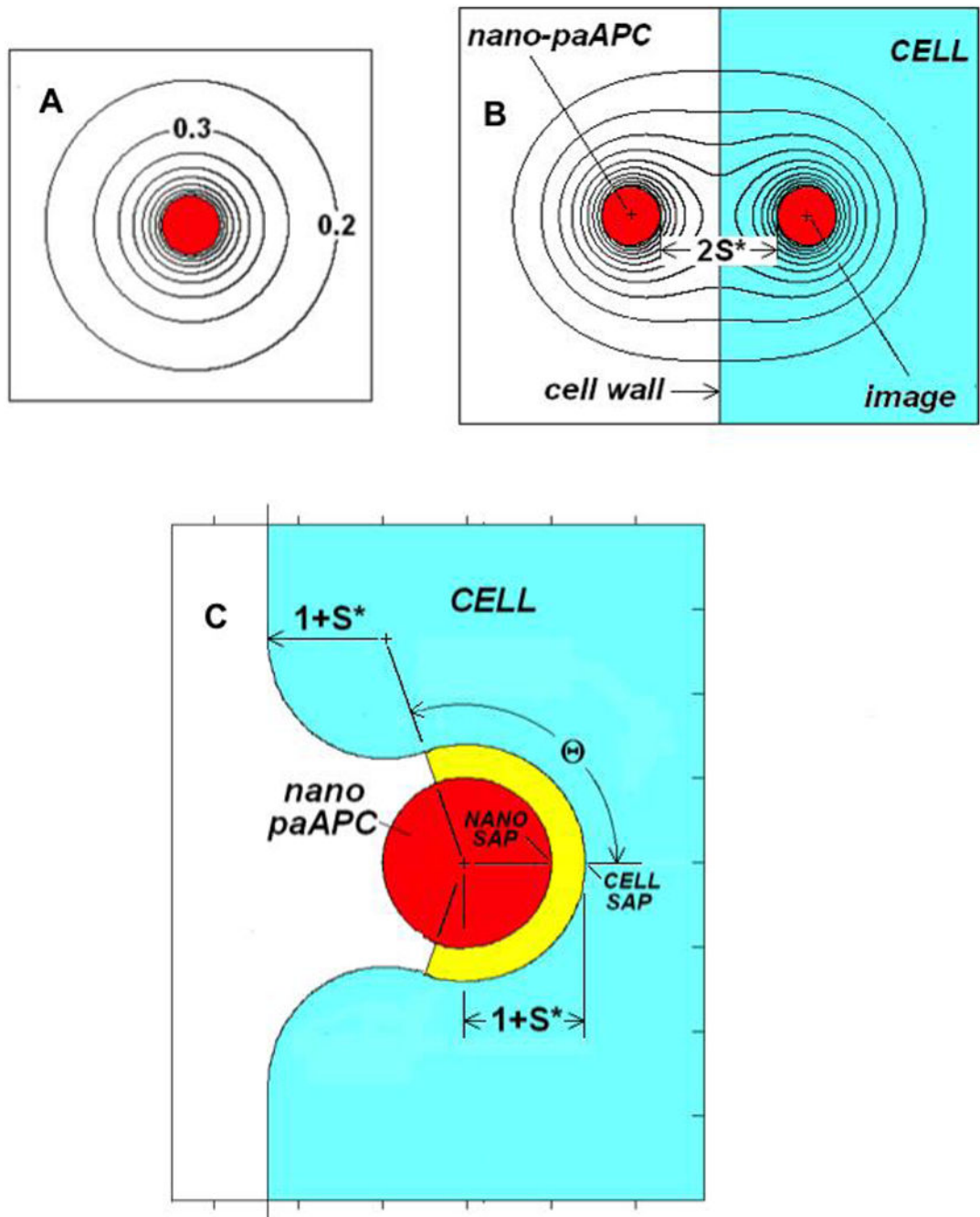


FIGURE 1.

A. C*-field near an isolated nano-paAPC

B. Definition of terms for a nano-paAPC near the surface of a naïve T-cell

C. Definition of terms for an embedded/partially encapsulated nano-paAPC

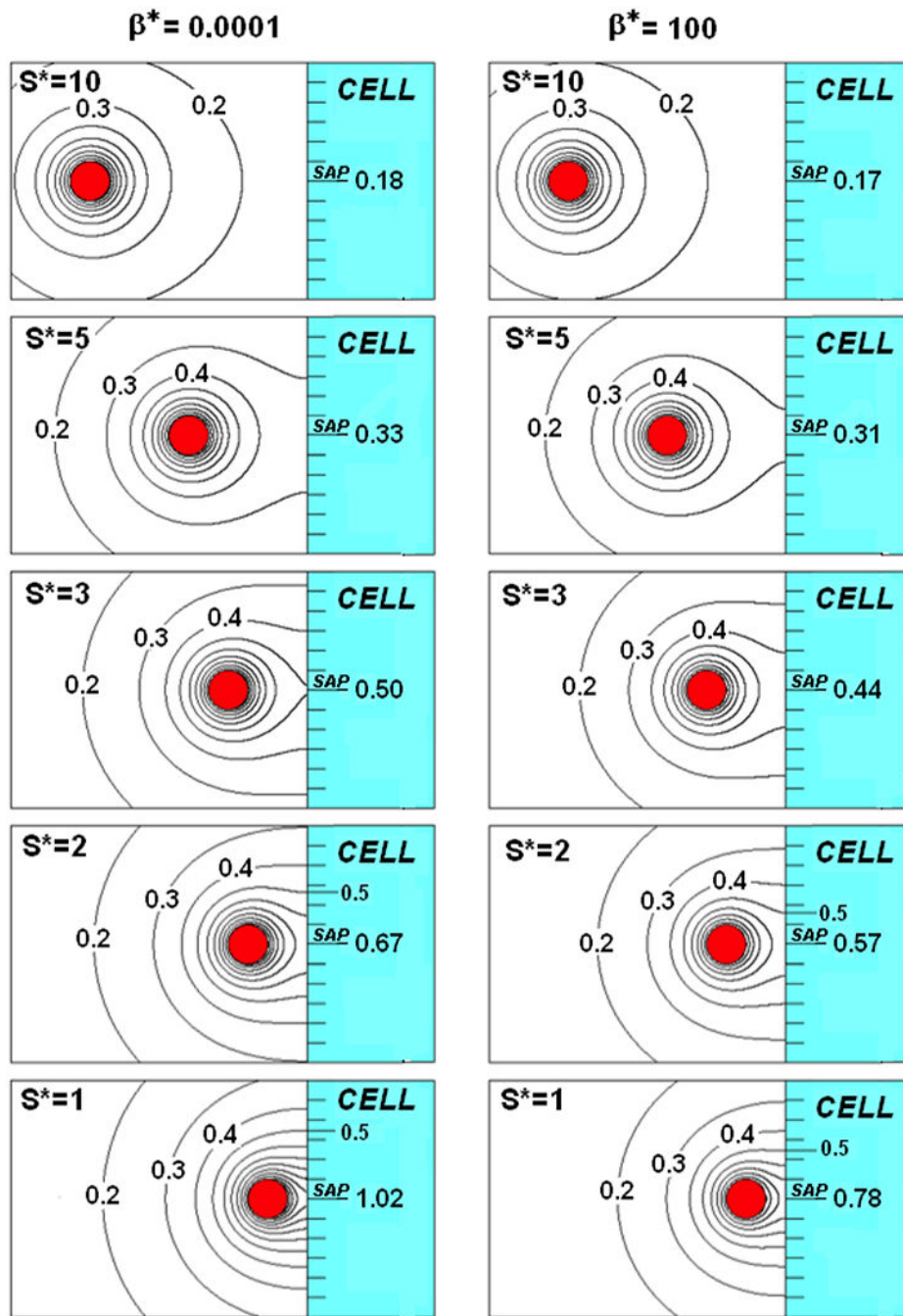


FIGURE 2. A nano-paAPC near the surface of a naïve T-cell for $\beta^* = 0.0001$ (left) and $\beta^* = 100$ (right)

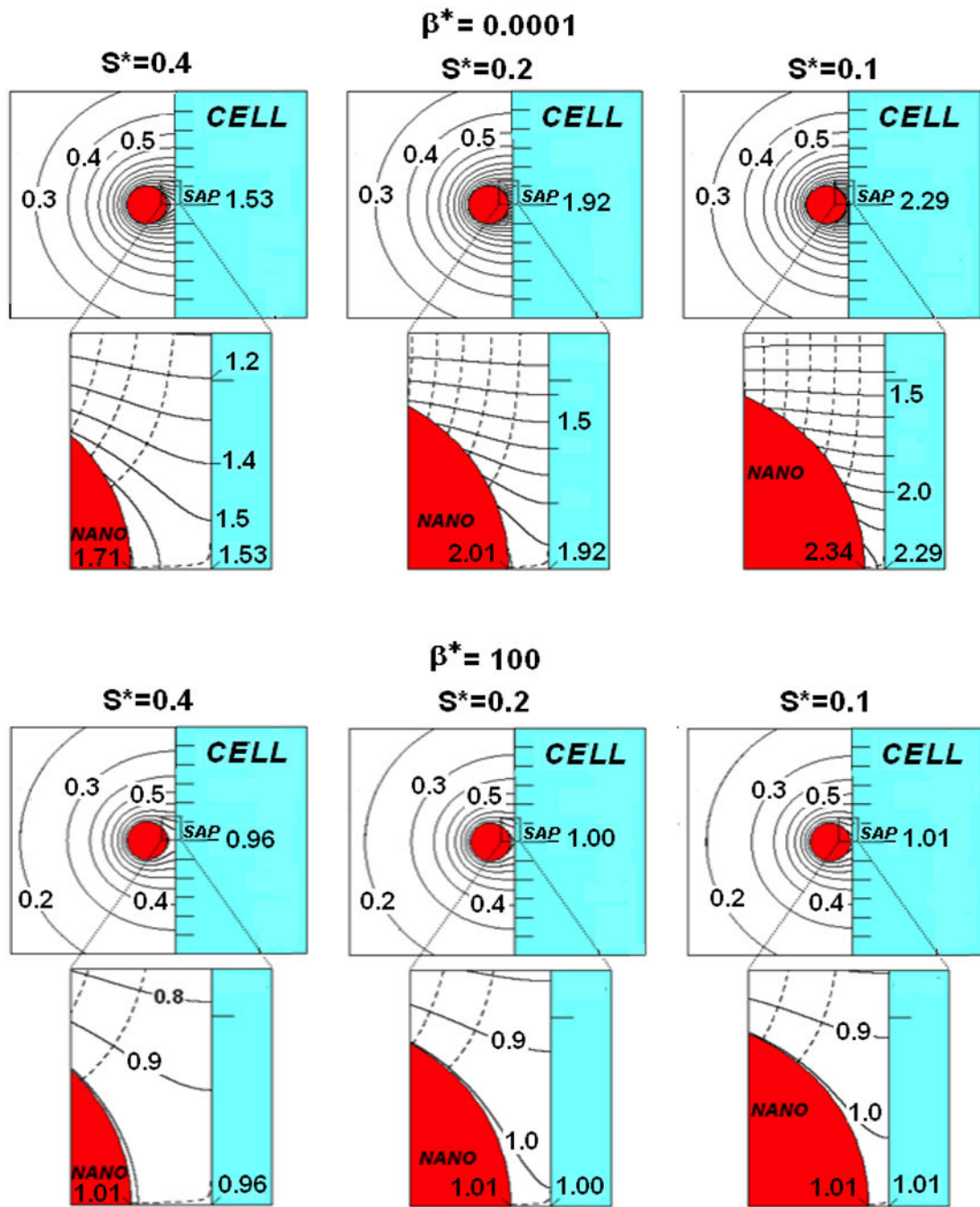


FIGURE 3. A nano-paAPC near the surface of a naïve T-cell for $\beta^*=0.0001$ (top) and $\beta^* =100$ (bottom)

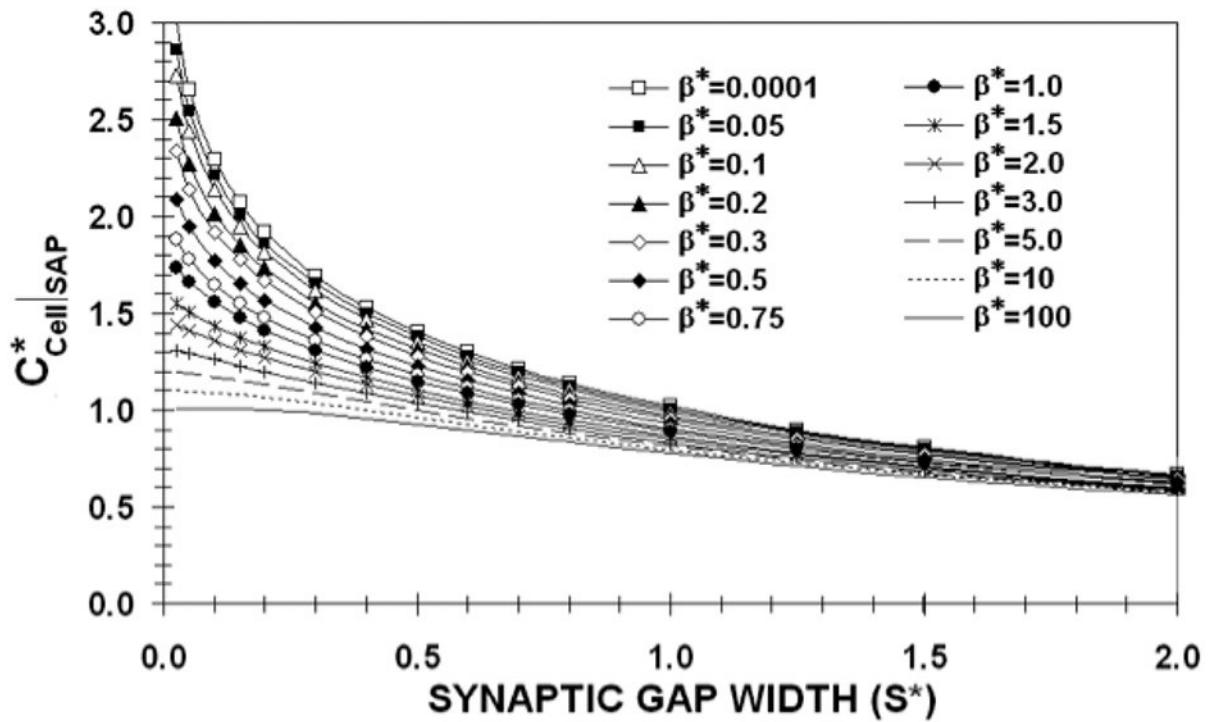


FIGURE 4.

The dimensionless synaptic axis point (SAP) concentration on the T-cell wall as a function of synaptic gap width (S^*) for various values of β^* when a nano-paAPC does not penetrate the cell wall.

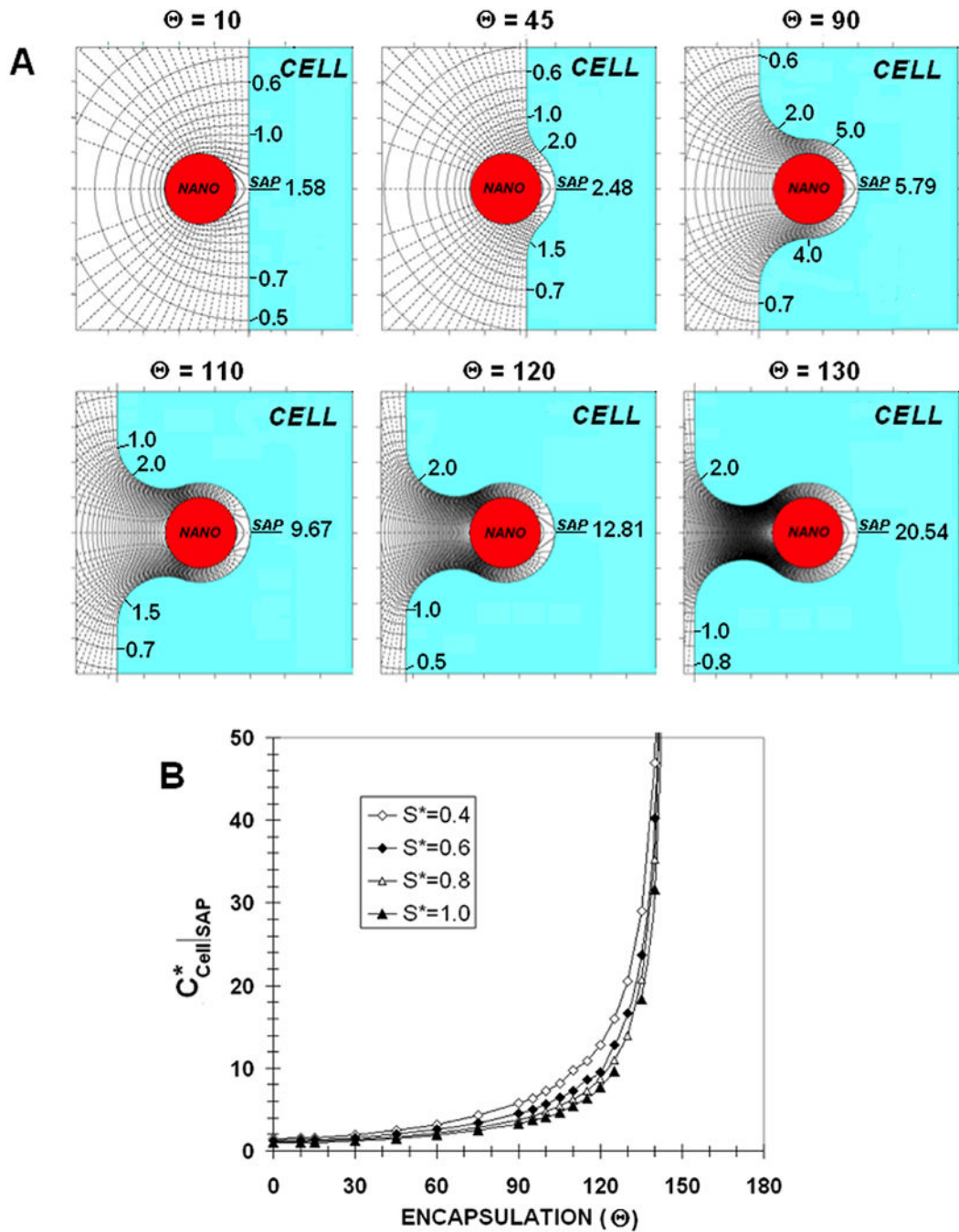


FIGURE 5.

A) Concentration contours (solid) and fluxlines (dashed) near an embedded nano-paAPC for various degrees of encapsulation ($\beta^* = 0.0001$)

B) Dimensionless synaptic axis point (SAP) concentration on the T-cell wall as a function of encapsulation angle (Θ) for various values of synaptic gap width (S^*) when a nano-paAPC embeds in the cell ($\beta^* = 0.0001$)

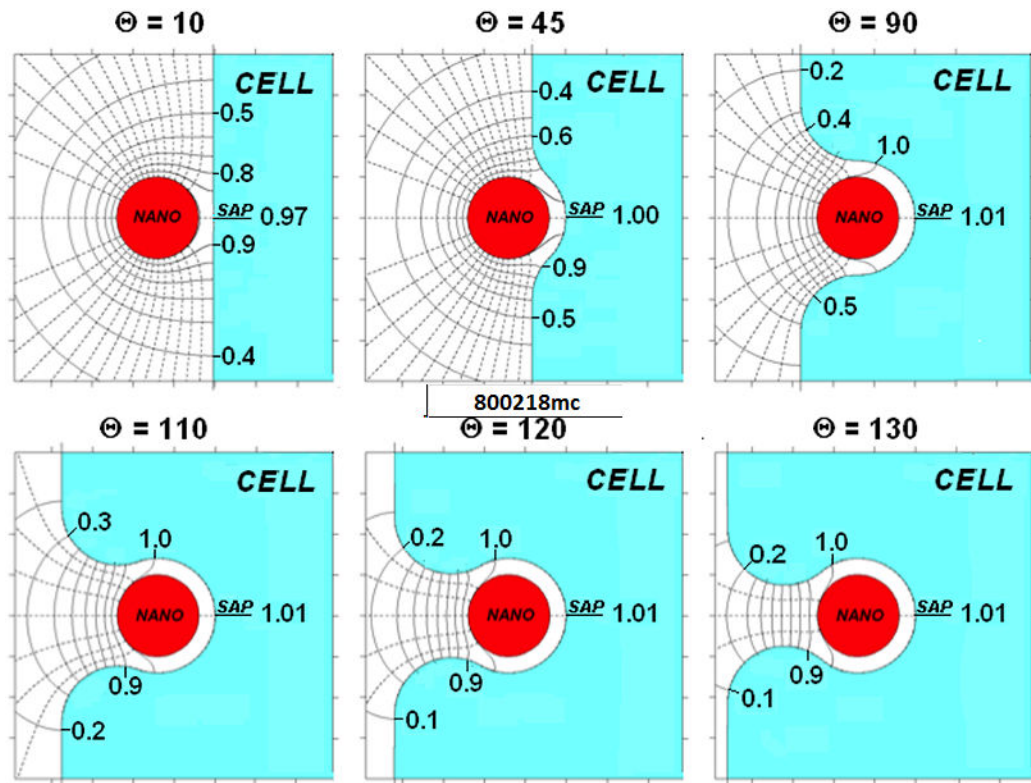


FIGURE 6. Concentration contours (solid) and flux-lines (dashed) near an embedded nano-paAPC for various degrees of encapsulation ($\beta^* = 100$)