Video Article Experimental Methods for Spin- and Angle-Resolved Photoemission Spectroscopy Combined with Polarization-Variable Laser

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Abstract

The goal of this protocol is to present how to perform spin- and angle-resolved photoemission spectroscopy combined with polarization-variable 7-eV laser (laser-SARPES), and demonstrate a power of this technique for studying solid state physics. Laser-SARPES achieves two great capabilities. Firstly, by examining orbital selection rule of linearly polarized lasers, orbital selective excitation can be carried out in SAPRES experiment. Secondly, the technique can show full information of a variation of the spin quantum axis as a function of the light polarization. To demonstrate the power of the collaboration of these capabilities in laser-SARPES, we apply this technique for the investigations of spin-orbit coupled surface states of Bi₂Se₃. This technique affords to decompose spin and orbital components from the spin-orbit coupled wavefunctions. Moreover, as a representative advantage of using the direct spin detection collaborated with the polarization-variable laser, the technique unambiguously visualizes the light polarization dependence of the spin quantum axis in three-dimension. Laser-SARPES dramatically increases a capability of photoemission technique.

Video Link

The video component of this article can be found at <https://www.jove.com/video/57090/>

Introduction

Angle-resolved photoemission spectroscopy (ARPES) technique has developed into one of the most powerful tool to investigate quasiparticle band structures in solid states¹. The most of attractive feature of ARPES is the capability for band mapping to characterize electronic states in energy and momentum space. Spin-resolved ARPES (SARPES), which is here equipped with spin-detectors, e.g. Mott detector^{2,3} , further enables us to resolve the spin character of the observed band structures⁴. Since the Mott detector can measure the spin with two axes (*x* and *z*, or *y* and *z*), the combination of the two Mott detectors further allows one to obtain the spin orientation in three dimension^{4,5}. For several decades, however, the SARPES experiments were suffered from their low efficiency (typically 1/10000 compared to that for spin-integrated ARPES
measurement)^{3,4,5,6,7}, which had limited the energy and angular-resolutions. Recently, a high-efficient spin detector based on exchange scattering, the so-called very-low-energy electron-diffraction (VLEED) detector^{7,8,9,10}. With this detector, the data quality has been significantly improved and the data acquisition time has been shortened. Recently, SARPES has succeeded greatly to address spin-polarized electronic states and particularly spin-orbit coupling effect resulting in the spin texture of the surface bands⁷.

Here, we employ SARPES measurements with a polarization-variable vacuum ultraviolet laser light (laser-SARPES) and demonstrate the great advantages of this combined technique. Through the investigation on the spin-orbit coupled surface states in Bi₂Se₃, we present two capabilities of laser-SARPES. Firstly, due to the orbital selection rule of linearly polarized lasers in dipole transition regime, *p*- and *s*-polarized lights selectively excite a part of eigen-wavefunctions with different orbital symmetry. Such an orbital selective excitation is thereby available in SARPES, namely, orbital-selective SARPES. Secondly, three-dimensional (3D) spin-detection in SARPES shows the direction of the spin quantum axis and directly displays full information of the light-polarization dependence. In this protocol, we briefly describe a methodology to perform this state-of-the-art laser-SARPES technique to study the strong spin-orbit coupling effects.

Our laser-SARPES system is located at The Institute for Solid State Physics, The University of Tokyo¹¹. The schematic drawing of our laser-SAPRES machine is shown in Figure 1. The polarization-variable 7-eV laser light¹² illuminates the sample surface and the photoelectrons are emitted from the sample. The polarization of laser is automatically controlled by MgF₂-based λ/2- and λ/4-waveplates to selectively use linear and circular polarizations. A hemispherical electron analyzer corrects the photoelectrons, and analyzes their kinetic energy (*E*kin) and emission angle (θ_x and θ_y). The photoelectron intensities are mapped on the *E*_{kin}-θ_x screen monitored by a CCD camera. This image is directly transformed into the energy band structure in reciprocal space.

For SARPES measurement, the photoelectrons with a specific emission angle and kinetic energy analyzed by the electron analyzer are guided to two VLEED-type spin detectors with a 90-degree photoelectron deflector and the photoelectron beams are focused onto two different targets of Fe(001)-*p*(1×1) films terminated by oxygen. The photoelectrons reflected by the targets are detected in single channel detection by using

a channeltron placed in each spin detector. The VLEED targets can be magnetized with Helmholtz-type electric coils which are arranged with orthogonal geometry with respect to each other. The magnetization direction is controlled by the bipolar condenser bank. The double VLEED spin detectors thereby enable us to analyze the spin-polarization vector of the photoelectron in three dimensions.

Protocol

1. Sample Mount and Installation

- 1. Cut single-crystal samples of Bi₂Se₃¹³ in an approximate size of 1 × 1 × 0.5 mm³ and use sliver-based epoxy to glue the sample to the sample holder.
- 2. Paste the scotch tape on the sample surface.
- NOTE: The scotch tape is used to cleave the sample in ultrahigh vacuum (UHV) chamber to obtain an atomically clean surface.
- 3. Install the sample into the sample magazine in the load lock, and start the pump until the pressure of the load lock is lower than 1×10^{-5} Pa.

2. Sample Cleaving

- 1. Open the UHV valve between the load lock and the UHV preparation chamber.
- 2. Move the sample magazine from the load rock to the preparation chamber by using the linear/rotary feedthrough which is attached to the load lock chamber.
- 3. Pick up the sample from the sample magazine by the transfer rod attached to the preparation chamber.
- 4. Put back the sample magazine into the load lock and close the UHV valve.
- 5. Wait until the pressure of the preparation chamber is below 5×10^{-7} Pa.
- 6. Peel the scotch tape by using wobble stick in the preparation chamber and cleave the sample under the UHV condition.

3. Sample Transfer to The Measurement Position

- 1. Transfer the sample to the UHV measurement chamber, and fix the sample to the main gonio-stage by the screw driver equipped with the measurement chamber.
- 2. Move the gonio-stage to the measurement position and use the micrometer stage to precisely move the sample position onto the focus of the spectrometer.

4. 7eV-laser Setup

1. Turn on the Nd:YVO4 laser.

NOTE: The laser generates 355 nm laser light with a high repetition rate of 120 MHz.

- 2. Open the laser beam shutter, and make sure that the laser passes through the KBBF crystal and a second-harmonic wave of 177 nm (6.994 eV) is generated.
- 3. Optimize the power of the 7eV-laser by changing the power of the 355-nm laser with the variable attenuator.

5. ARPES Data Acquisition

- 1. Open the analyzer control software on the desktop computer.
- NOTE: We use "SES software" which is a general program for controlling ScientaOmicron analyzer with an electron deflector.
- 2. Select **Setup**… below **Sequence** on the menu bar (**Figure 2**, step i.2-1).
- 3. Choose **ARPES configuration** (**Figure 3**, step i.3-1) and **ARPES Mapping** in the list (**Figure 3**, step i.3-2) to perform Fermi surface mapping with the photoelectron deflector.
- 4. Click **Edit** (**Figure 3**, step i.3-3) and configure Fermi surface mapping ranging from -12° to 12° of an emission angle *θ^y* with step size of 0.5° (**Figure 3**, step i.3-4).

NOTE: The hemispherical analyzer with an electron deflector enables us to map the Fermi surface without the sample rotations.

5. Click **Run** (**Figure 2**, step i.2-3).

6. SARPES Data Acquisition

- 1. Manually change the machine set-up for SARPES measurement including the analyzer entrance slit and the aperture size (**Figure 1**).
- 2. Select **Setup**… below **Sequence** on the menu bar (**Figure 2**, step i.2-2).
- 3. Choose **Spin configuration** (**Figure 4**, step i.4-1) and **Normal** in the list (**Figure 4**, step i.4-2), and click **OK** (**Figure 4**, step i.4-3).
- 4. Select **DA30** (**Figure 5**, step i.5-1) on the menu bar and **Control Theta**… (**Figure 5**, step i.5-2) to open the setting panel for the DA30 angle (*θ^x , θ^y*) configuration.
- 5. Choose the emission angle (*θ^x , θ^y*) = (-6°, 0°) to take SARPES spectra (**Figure 5**, step i.5-3).
- 6. Apply magnetic field by controlling the bipolar condenser bank to magnetize the VLEED target in positive direction along the particular axis (α: *x*, *y*, or *z*).

NOTE: In our system, this process can be done through command prompt [**Figure 6 (a)**].

- 7. Click **Run** to take intensity spectrum (**Figure 2**, step i.2-3).
- 8. Apply magnetic field to magnetize the VLEED target in negative direction along α and start scan to take intensity spectrum.

9. Calculate the spin-polarization and the spin-resolved spectra.

7. Scanning the light polarization dependence

- 1. Change the angle of the λ/2-waveplate precisely controlled by the stepping motor to tune the light polarization of the 7 eV-laser.
- NOTE: In our system, this process can be done through command prompt [**Figure 6 (b)**].
- 2. Take the spin-resolved spectra for *x, y* and *z* axes.
- 3. Scan the spin-resolved spectra as a function of the light polarization with varying the half waveplate angle from 0° to 102° with step size of 3°.

Representative Results

Before starting SARPES experiments, *k* positions need to be accurately determined for taking spin-resolved spectrum by using high statistic spin-integrated ARPES results with high energy- and angular-resolutions (protocol 5.1-5.5). This is demonstrated in **Figure 7** where the ARPES results for a Bi₂Se₃ single crystal are presented. This material is known as a prototypical topological insulator with a spin-polarized surface states^{14,15}. The ARPES band map clearly resolves the very steep Dirac-cone-like energy dispersion of the two-dimensional surface state¹⁶. The ARPES results confirm high quality of the cleaved surface and the sample orientation. From the energy and momentum information of the band map and the Fermi surface mapping, one can now choose the specific emission angle for SARPES experiment.

Figure 8(a) represents the energy distribution curves (EDCs) for different magnetization direction (+*M^y* and -*M^y*) taken at (*θ^x , θ^y*)=(-6°, 0°) across -*k*F of the surface band, corresponding to the cut along the dashed line shown in **Figure 7**. From the data, the spin-resolved EDCs can be obtained in the following. At first, the spin polarization (*P^y*) is estimated by using this relation:

$$
P_{\alpha} = \frac{1}{S_{eff}} \frac{I_{+M\alpha} - I_{-M\alpha}}{I_{total}^{\alpha}}, \qquad I_{total}^{\alpha} = I_{+M\alpha} + I_{-M\alpha}
$$

where α is the resolved axis (x, y and z), and I_{+Ma} (I_{-Ma}) is the photoelectron intensity for +M_a (-M_a), and S_{eff} is the Sherman function which is typically 0.3¹¹. The obtained P_y curve is shown in **Figure 8 (b)**. The spin-resolved spectra for spin-up (I_1^α) and spin-down (I_1^α) are then obtained by:

$$
I_{\uparrow}^{\alpha} = \frac{1}{2} (1 + P_{\alpha}) I_{total}^{\alpha}, \qquad I_{\downarrow}^{\alpha} = \frac{1}{2} (1 - P_{\alpha}) I_{total}^{\alpha}.
$$

The resulting spin-resolved spectra are shown in **Figure 8(c)**.

The double VLEED spin detectors allow us to obtain 3D spin-resolution along *x*, *y* and *z* axes. This is demonstrated in **Figure 9(a)** where the spin-resolved spectra by using *p*-polarization set-up and the corresponding spin-polarization (*P^x* , *P^y* and *P^z*) are shown. The clear peak near the Fermi energy is assigned to the surface state of Bi₂Se₃. The data represents that P_γ is fully spin-polarized ~100 % while the other components, *Px* and *P^z* , are negligibly small. The 3D spin-resolved spectra thus illustrate the spin quantum axis of the surface state fixed along *y*, which is consistent with band calculations¹ .

Then, we focus on the orbital selective excitation of *p*- and s-polarized laser. In general, under strong spin-orbit coupling, different orbital
symmetry is mixed with opposite spinor in a single eigenfunction^{17,18}. In *px* and *p^z* (*p^y*) orbital components in the spin-orbit coupled wavefunction (inset in **Figure 9**). Thereby, through the spin-orbital coupling, orbitalselective laser-SARPES should detect opposite spin-polarization for *p*- and *s*-polarization. Indeed, this is demonstrated in **Figure 9(a)** and **9(b)**. We clearly observe significant light polarization dependence of P_y directly displaying spin-orbit coupling effect in the surface state^{17,18} .

In addition, laser-SARPES affords to further investigate the linear-polarization evolution of P_x , P_y and P_z even with tilted light polarization
between *p*- and s-polarizations¹⁹. As shown in **Figure 10(a)**, laserbinding energy as a function of the linear-polarizations. Here, the result contains 102 data points, which was acquired within 6 h. The polarization dependence of *P^y* is easily explained by a fact that the positive and negative *P*^y of the photoelectrons excited by *p*- and *s*-components of the applied laser cancel out. However, this cannot explain the evolution of P_x and P_z . To completely describe this result, it is necessary to consider coherent spin process in photoemission as summarized in **Figure 10(b)**. If the linear polarization simultaneously excites spin-up and spin-down states, these two quantum-spin bases are coherently superposed in a photoelectron state, resulting in the spin rotation. In fact, the displayed polarization dependence is well reproduced by the model calculation with a consideration of coherent interference between spin-up and spindown excited by *p*- and *s*-polarizations¹⁹. The similar spin effect has been alternatively observed by 3D SARPES with synchrotron radiation^{20,21}.

Figure 1: Schematic drawing of the detection systems of laser-SARPES. Two VLEED spin-detectors arranged with orthogonal geometry are connected to the hemispherical photoelectron analyzer. This figure has been modified from Yaji, K. et al.¹¹. [Please click here to view a larger](https://cloudflare.jove.com/files/ftp_upload/57090/57090fig1large.jpg) [version of this figure.](https://cloudflare.jove.com/files/ftp_upload/57090/57090fig1large.jpg)

Figure 2: Screenshots of the analyzer control software. Steps i.2-1 to i.2-3 show how to start for selecting detection mode (ARPES or SARPES) and taking data. [Please click here to view a larger version of this figure.](https://cloudflare.jove.com/files/ftp_upload/57090/57090fig2large.jpg)

Figure 3: Screenshots of the control panel for choosing detection-mode. Steps i.3-1 to i.3-4 show how to start Fermi surface mapping. If the button **Edit** is pressed (step i.3-3), the new panel will pop up to define the properties of the mapping (step i.3-4).

Figure 4: Screenshots of the control panel for choosing detection-mode. Steps i.4-1 to i.4-3 show how to start SARPES mode. If the region of **spin** is selected (step i.4-1) and the bottom **OK** is pressed (step i.4-3), the panel will close and the whole analyzer setup will turn to be the SARPES mode.

Figure 5: Screenshots of the electron deflector control-panel. Steps i.5-1 to i.5-3 show how to control the photoelectron deflector. If the region control **theta…** is pressed (step i.5-2), the new panel will pop up to define the properties of the photoelectron deflector (step i.5-3). [Please](https://cloudflare.jove.com/files/ftp_upload/57090/57090fig5large.jpg) [click here to view a larger version of this figure.](https://cloudflare.jove.com/files/ftp_upload/57090/57090fig5large.jpg)

Figure 6: Screenshots of the panels for magnetic field of spin targets and light polarization. These properties are controlled by command lines in our system. (a) the command to control the magnetic field for spin targets: "spin_coil.exe + X" corresponds to "the name of the application file", "the direction of the field, + or -" and "the axis, *x*, *y* or *z*". (B) the command to control the light polarization: "wave_plate.exe 180" corresponds to "the name of the application file" and "the angle of the *λ*/2-waveplate".

Figure 7: Fermi surface mapping and *E-k* **band mapping of Bi2Se3 surface state by using ARPES.** The dash line indicates *k* position for taking spin-resolved spectra shown in **Figure 8** and **Figure 9**. [Please click here to view a larger version of this figure.](https://cloudflare.jove.com/files/ftp_upload/57090/57090fig7large.jpg)

Figure 8: Spin- and angle-resolved surface band spectra of Bi2Se3. (a) Energy distribution curves (EDCs) measured for different magnetization directions +*M^y* and -*My* at a fixed emission angle corresponding to the dashed line cut in **Figure 7**. (b) Spin polarizations as a function of binding energy obtained from the spin-resolved analysis. (c) The resulting EDCs for spin-up (red triangles) and spin-down (blue triangles) channels. [Please click here to view a larger version of this figure.](https://cloudflare.jove.com/files/ftp_upload/57090/57090fig8large.jpg)

Figure 9: *p***- and** *s***-polarization dependence of photoelectron spin from the surface state of Bi2Se3.** (a) and (b) 3D spin-resolved spectra for_x, y and z axes, and the corresponding spin polarizations (*P_x, P_y* and *P_z*) as a function of binding energy obtained by *p*- and *s*-polarizations at a fixed emission angle corresponding to the dashed line cut in **Figure 7**. In the inset, experimental configurations for *p*- and *s*-polarizations are shown. This figure has been modified from Kuroda K. *et al.*¹⁹. The *p*- (s-) polarization selectively excites p_x and p_z (p_y) like orbital wavefunction. The *p_x* and *p_z* (*p_y*) states are coupled to +*y* spin (−*y* spin) in the spin-orbital coupled surface state^{16,17}. [Please click here to view a larger version](https://cloudflare.jove.com/files/ftp_upload/57090/57090fig9large.jpg) [of this figure.](https://cloudflare.jove.com/files/ftp_upload/57090/57090fig9large.jpg)

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Figure 10: Three-dimensional spin polarization effect induced by linearly polarized light. (a)The plots of $P_{x\cdot y\cdot z}$ **of the Bi₂Se₃ surface state** with respect to the applied linearly polarized laser. In the inset, the applied electric field of the laser projected onto the *x-z* plane is shown. The overall data points were taken within 6 h. This figure has been modified from Kuroda, K. *et al*. 19 . (b) Visualized 3D spin rotation due to the interference of spin-up and spin-down spin. [Please click here to view a larger version of this figure.](https://cloudflare.jove.com/files/ftp_upload/57090/57090fig10large.jpg)

Discussion

ARPES and SARPES techniques have been commonly used for studying electronic band structures through the band mapping and spindetection^{1,2}. In addition to these general advantages shown above, laser-SARPES based on orbital selection rule in optical dipole excitation can be employed as a novel technique for visualizing the spin-orbital coupling effect in the wavefunction and quantum spin interference. As demonstrated in **Figure 9 and 10**, the polarization of laser can be easily manipulated just by waveplates to tilted linear polarizations between p- and *s*-polarizations¹⁹. In principle, circular and even elliptical polarized lights can be obtained and used in laser-SAPRES. This variety of tunable polarization is hardly obtained in conventional light source such as noble-gas-discharge lamp and synchrotron radiation. Therefore, a combination of polarization-variable laser and SARPES with 3D spin-resolution dramatically increases a capability of photoemission technique.

To perform laser-SARPES under the best condition, one must be always careful about space-charge effect¹², which generally broadens the energy of the photoelectrons due to Coulomb repulsion in a dense electron packet emitted by the high intensity laser. If this issue appears, one needs optimize the power of the 7-eV laser (step 4.3). Second, if the photoelectron intensity from samples is poor, the analyzer entrance slit, and the aperture should be open (step 6.1), however, the energy resolution is sacrificed in this case. Therefore, one needs carefully select the experimental set-up to fit laser-SARPES experiments.

The main disadvantage of laser-SARPES compared to standard photoemission technique with synchrotron radiation is that in laser-SAPRES the photon energy of laser is generally not tunable. In photoemission technique, the tunable photon is necessary to probe *k^z* dispersion, and identifies 3D bulk band structures and two-dimensional surface states¹. Moreover, the photon energy of 7 eV used in this paper can scan small *k* area compared to that with higher photon energy. Therefore, laser-SARPES is likely restricted into the investigations of two-dimensional surface states around Brillouin zone center.

However, it should be noted that the power of laser-SARPES technique can be widely applied for spin-orbit coupled states. Recently, by using the protocol described within this paper, we have further revealed strong spin-orbit coupling effect and its significant *k*-dependence in Bi thin
film²² and BiAg₂/Ag(111) surface alloy²³. Also, it is worth noting th becomes a standard experimental technique. The protocol is intended to help researchers use SARPES and understand the produced data.

Disclosures

The authors declare that they have no competing financial interests.

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