

Practice of Epidemiology

Diagnostics for Pleiotropy in Mendelian Randomization Studies: Global and Individual Tests for Direct Effects

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Diagnosing pleiotropy is critical for assessing the validity of Mendelian randomization (MR) analyses. The popular MR-Egger method evaluates whether there is evidence of bias-generating pleiotropy among a set of candidate genetic instrumental variables. In this article, we propose a statistical method—global and individual tests for direct effects (GLIDE)—for systematically evaluating pleiotropy among the set of genetic variants (e.g., single nucleotide polymorphisms (SNPs)) used for MR. As a global test, simulation experiments suggest that GLIDE is nearly uniformly more powerful than the MR-Egger method. As a sensitivity analysis, GLIDE is capable of detecting outliers in individual variant-level pleiotropy, in order to obtain a refined set of genetic instrumental variables. We used GLIDE to analyze both body mass index and height for associations with colorectal cancer risk in data from the Genetics and Epidemiology of Colorectal Cancer Consortium and the Colon Cancer Family Registry (multiple studies). Among the body mass index–associated SNPs and the height-associated SNPs, several individual variants showed evidence of pleiotropy. Removal of these potentially pleiotropic SNPs resulted in attenuation of respective estimates of the causal effects. In summary, the proposed GLIDE method is useful for sensitivity analyses and improves the validity of MR.

causal inference; direct effect; instrumental variables; sensitivity analysis

Abbreviations: BMI, body mass index; GIANT, Genetic Investigation of Anthropometric Traits; GECCO, Genetics and Epidemiology of Colorectal Cancer; GLIDE, global and individual tests for direct effects; IV, instrumental variable; MR, Mendelian randomization; Q-Q, quantile-quantile; SNP, single nucleotide polymorphism.

Editor's note: An invited commentary on this article appears on page 2681.

Mendelian randomization (MR) $(1-4)$ $(1-4)$ $(1-4)$ $(1-4)$ is an inferential method that uses germ-line genotypes (e.g., single nucleotide polymorphisms (SNPs)) as instrumental variables (IVs) to assess the causal effect of an exposure on a disease outcome, and it is increasingly popular in genetic epidemiology. By exploiting the random assortment of genes from parents to offspring during gamete formation and conception, which has been likened to "Nature's randomized experiment" $(2, 5)$ $(2, 5)$ $(2, 5)$ $(2, 5)$, MR holds promise for removing the potential confounding and reverse causation that loom over observational epidemiology. While this is conceptually appealing, skepticism has persisted on whether the strong assumptions required by MR ([6](#page-7-0)–[9\)](#page-8-0) are plausible. Stated informally, these assumptions require that genetic variants are independent of any confounder of the exposure-disease relationship, that genetic variants are associated with the exposure (preferably strongly), and that there is no direct effect from the genetic variants to the disease outcome other than through the pathway mediated by the exposure—also known as "no pleiotropy."

Pleiotropy, or more specifically, horizontal pleiotropy, refers to the phenomenon wherein a gene or mutation affects multiple phenotypes via independent biological pathways [\(10,](#page-8-0) [11](#page-8-0)). Figure [1](#page-1-0) illustrates the concept of MR and the critical no-pleiotropy assumption. As the founding principle, the independence between genotypes and confounding variables is backed up in theory by the random assortment of genes from parents to offspring, and in practice it is further aided

Figure 1. Causal diagram for Mendelian randomization. The goal is to use genotypes as instrumental variables to infer the causal effect of an exposure on a disease outcome. One critical assumption is that there is no direct effect from the genotype to the disease (no pleiotropy).

through adjustment for population substructures. The strength of the IV's association with the exposure can be improved by increasing the sample size and including additional known risk loci. Perhaps the Achilles' heel of MR is the potential for pleiotropic effects among the genetic risk variants associated with complex diseases, given the biological plausibility of pleiotropy in complex biological pathways and networks. Indeed, recent genome-wide association studies have shown that pleiotropy is pervasive in complex traits, with evidence of numerous genetic variants' affecting multiple traits, some of which represent horizontal pleiotropy ([12](#page-8-0)–[14\)](#page-8-0).

Methods for detecting pleiotropy and, more ambitiously, estimating the causal effect in the presence of pleiotropy, have been under active development. Notably, Egger regression—a tool for detecting small-study bias in meta-analysis—has been adapted to test for the impact of pleiotropy on the casual effect of interest (15) . This test exploits the observation that if there is no pleiotropy, a dosage relationship should be present between the individual genetic associations with the exposure and the corresponding genetic associations with the outcome ([16\)](#page-8-0). A linear regression model is fitted between the 2 sets of genetic associations, and a nonzero intercept suggests that there is evidence of pleiotropy. In the presence of direct effects, and under the "instrument strength independent of direct effect" (InSIDE) assumption, the MR-Egger test yields a valid causal effect estimate, though such an assumption is untestable and may be difficult to justify. Along the same lines, it has been shown that the causal effect can be estimated unbiasedly when fewer than 50% of IVs are invalid, either by the median estimator [\(17\)](#page-8-0) or by the ℓ_1 shrinkage estimation procedure (18) .

When a number of SNPs are used as candidate IVs in MR, it is possible that some variants are valid IVs but others are not. Several informal diagnostic statistics for detecting outliers and investigating pleiotropy have been proposed in MR-Egger and other meta-analytical methods—for example, the heterogeneity in dependent instrument (HEIDI) outlier test [\(19](#page-8-0)–[21](#page-8-0)). There is a pressing need to develop more rigorous significance tests for global and individual-variant pleiotropy. Such analyses will lead to sensitivity analyses that remove variants exhibiting evidence of pleiotropy and estimate causal effects with a more justified set of IVs. This is a challenging task because, without additional constraints, the IV regression approach cannot assess simultaneously the causal effect of primary interest and the individual direct effects.

Binary outcomes pose additional modeling challenges. Most of the existing approaches were formulated for a quantitative trait by linear regression, a feature inherited from the classical 2-stage least-squares regression approaches in the econometrics literature. Strictly speaking, these methods cannot be immediately used for MR analyses with binary disease outcomes. While logistic regression has been the workhorse and the odds ratio is the de facto association estimate for binary outcomes, using an odds ratio as the causal estimand is difficult for causal inference [\(22](#page-8-0)–[24\)](#page-8-0). This is mostly due to the noncollapsibility of the odds ratio (25) , meaning that the stratum-specific odds ratio is not equal to the marginal odds ratio ignoring strata even when the stratification variable is not related to the exposure. The use of 2-stage IV approaches in logistic regression yields approximations of causal odds ratios for rare disease outcomes [\(8](#page-8-0), [26\)](#page-8-0).

In this article, we propose a statistical method—global and individual tests for direct effects (GLIDE)—with which to assess pleiotropy and conduct sensitivity analyses for MR when a number of SNPs were used as candidate IVs, assuming that genetic variants are indeed independent of confounding variables. The novel contribution of GLIDE is a rigorous significance analysis for global and individual-variant pleiotropy, using a quantile-quantile (Q-Q) plot and a permutation procedure. Causal effects are defined in terms of relative risk, a measure that is collapsible and well interpretable for binary disease endpoints [\(27](#page-8-0)). Though individual direct effects are not simultaneously identifiable through the IV regression, we show that "surrogate direct effects"—the direct effects for one individual variant at a time, not conditional on other variants—are estimable and provide valid tests for individual direct effects under plausible conditions. Using the proposed GLIDE method, investigators can determine whether the set of genetic variants being evaluated for IVs show any evidence of global pleiotropy and, if so, which variants exhibit evidence of pleiotropy and therefore should be removed in a sensitivity analysis. We conduct extensive simulation studies to evaluate the performance of the proposed GLIDE method relative to the MR-Egger method. Finally, we use GLIDE to analyze the associations of body mass index (BMI; weight (kg) /height $(m)^2$) and height with colorectal cancer risk in data from the Genetics and Epidemiology of Colorectal Cancer (GECCO) Consortium and the Colon Cancer Family Registry.

METHODS

Consider an MR study with a binary disease outcome Y and a set of *m* independent genetic variants $(m \gg 1)$, denoted by $\mathbf{G} = (G_1, ..., G_m)$, that have been identified as candidate IVs to infer the causal effect of the intermediate exposure X on the outcome Y. Typically, these genetic variants are independent loci derived from prior genome-wide association studies. For an MR analysis, X is not required to be measured in the study, as long as X can be predicted by the set of genotypes \bf{G} and the previously reported association parameters. Suppose the causal effect of X on Y is confounded by a collection of unmeasured variables U. Assume that the independence assumption for G holds, so that **G** ⊥ *U*. For simplicity of notation, additional measured confounding variables are omitted, but the formulation follows immediately when measured confounding variables are added. The interest

herein is to test the third IV assumption of no pleiotropy that there is no direct effect of G on Y other than the hypothesized mediation effect through X . In what follows, the notions of "direct effect" and "pleiotropic effect" will be used interchangeably.

The causal effect of the intermediate exposure X on the outcome Y is defined on the relative risk scale through a log-linear model:

$$
\log \{ \Pr(Y = 1 | X, U, \mathbf{G}) \} = \beta_0 + \beta_1 X + \sum_{j=1}^{m} \beta_{2j} G_j + \beta_3 U,
$$
\n(1)

where β_1 is the causal effect of X on Y and β_{2j} is the direct effect of the *j*th variant G_i . This is a structural equation model in which causal effects are conditional on unmeasured confounding variables U. The global null hypothesis of interest is that there is no direct effect for any genetic variant, expressed as

$$
H_0: \beta_{2j} = 0 \text{ for all } j.
$$

If this global null hypothesis is rejected, the interest is to then assess which individual variants show evidence of a direct effect and therefore should be deleted in the subsequent analysis. However, neither testing the global hypothesis nor diagnosing individual variants can be accomplished by regressing Y on (*X*, **G**) because of the presence of the unmeasured confounding, U.

Suppose a genetic risk score has been developed externally to predict X from G, denoted by $\mathcal{R}(G) = \mathbb{E}(X|G) = \sum_i \alpha_j G_j$, where α_i is the previously derived nonzero weight (coefficient) associated with G_i . The variability of estimating α_i in prior studies when X is a quantitative trait can be negligible in IV estima-tion [\(28\)](#page-8-0). By definition, $X = \mathcal{R}(G) + \varepsilon$, and G is independent of the error term ε . Plugging the expression of X into model 1 (equation 1), we have

$$
\log \{ \Pr(Y = 1 | U, \mathbf{G}, \varepsilon) \}
$$

= $\beta_0 + \beta_1 \mathcal{R}(\mathbf{G}) + \beta_1 \varepsilon + \sum_j \beta_{2j} G_j + \beta_3 U.$

Since **G** is independent of ε and U, integration of ε and U leads to

$$
\log \{ \Pr(Y = 1 | \mathbf{G}) \} = \beta_0^* + \beta_1 \mathcal{R}(\mathbf{G}) + \sum_j \beta_{2j} G_j. \tag{2}
$$

The fundamental problem in estimating direct effects β_{2j} through the IV regression approach is that there are m IVs but now $m + 1$ causal effects to be estimated in model 2 (equation 2). The design matrix for model 2 is rank-deficient, since $\mathcal{R}(G)$ is a linear combination of G_j 's. Therefore β_{2j} 's are not identifiable. Instead, one has to devise tests for nonzero β_{2i} indirectly under some constraints—for example, the MR-Egger test ([15](#page-8-0)). If $β_{2j} = 0$ for all *j*, then the genetic effects on *Y*, expressed as $β₁α_j + β_{2j}$ in our notation, and the genetic effects on *X* (α*j*) should have a dose-response relationship and form a straight line with the intercept 0. This forms the basis for indirect tests of global pleiotropy through testing of the intercept in the MR-Egger method. As informal ways to assess individual pleiotropy, other methods have been developed that involve assessment of heterogeneity in causal effect estimates based on individual genetic variants one at a time ([19](#page-8-0)–[21\)](#page-8-0).

While the direct effects in model 2 (equation 2) are not simultaneously identifiable, we propose GLIDE, an indirect method with which to test the global null hypothesis and at the same time provide diagnostics for pleiotropy for individual variants. The key novelty is the development of an individual-level significance test of pleiotropy for each SNP under suitable conditions. Specifically, a sequence of *m* log-linear models are fitted to $(\mathcal{R}(\mathbf{G}), G_i)$, each assessing the "marginal" direct effect for one genetic variant at a time:

$$
\log \{ \Pr(Y = 1 | \mathcal{R}(\mathbf{G}), G_1) \} = \gamma_{01} + \gamma_{11} \mathcal{R}(\mathbf{G}) + \gamma_{2j} G_1,
$$

\n
$$
\vdots
$$

\n
$$
\log \{ \Pr(Y = 1 | \mathcal{R}(\mathbf{G}), G_m) \} = \gamma_{0m} + \gamma_{1m} \mathcal{R}(\mathbf{G}) + \gamma_{2m} G_m.
$$

\n(3)

We call γ_{2i} the "surrogate direct effect," which is related to the true direct effect β_{2i} and is directly testable. In Web Appendix 1 (available at [https://academic.oup.com/aje\)](https://academic.oup.com/aje), we show that γ_{2j} 's can be expressed explicitly as functions of β_{2j} , α_j , and some distributional parameters for G_j 's. We derive 3 results that form the basis of our proposed test procedure. First, if the global null hypothesis H_0 is true (i.e., if $\beta_{2j} = 0$ for all *j*), then $\gamma_{2j} = 0$ for all *j*. Second, if $\beta_{2i'} = 0$ for all $j' \neq j$, then $\gamma_{2i} = \beta_{2i}$ for the *j*th variant. Third, when the majority of β_{2j} 's are zero or when $\alpha_j \beta_{2j}$ is positive for some *j* and negative for others, γ_{2j} is numerically close to β_{2j} .

These results delineate a test procedure for the unidentifiable parameters β_{2j} through the estimable quantities, the γ_{2j} 's. The core of our GLIDE procedure is to evaluate the P values associated with γ_{2j} , denoted by p_j , with respect to their null distributions derived from Monte Carlo simulations. The benefit of diagnosing pleiotropy by means of P values is that they are agnostic to the sign of direct effects, thereby circumventing the issue in balanced pleiotropy where some direct effects are positive and others are negative. To summarize the evidence for global pleiotropy, we combine the P values by Fisher's method, $-2\sum \log(p_i)$, and compare the observed value with its null distribution to compute the P value for global pleiotropy. A unique feature of GLIDE is that it gives an intuitive Q-Q plot of p_j 's for diagnosing individual variant pleiotropy. To perform a sensitivity analysis with the set of more justified IVs, the procedure can be applied iteratively by deleting potentially pleiotropic variants.

The null distributions of p_j under H_0 require careful derivation. First, because each γ_{2j} is conditional on $\mathcal{R}(\mathbf{G})$, which is shared across *m* models, the *z* scores associated with p_j 's, denoted by z_i 's, are correlated even though the G_i 's are mutually independent. As such, a naive Bonferroni test for *m* variants that ignores the correlation structure may not be optimal. In Web Appendix 2, we derive the asymptotic distribution of $\hat{\gamma}_{2j}$'s from the estimating equation theory. Second, although each γ_{2j} is an estimable quantity, the joint distribution of $\hat{\gamma}_{2j}$'s is degenerate with rank $m - 1$, meaning that if $m - 1 \hat{\gamma}_{2j}$'s are

first obtained, then the one left out is not stochastic and indeed completely determined from previous $m - 1 \hat{\gamma}_{2j}$'s. This is formally proven in Web Appendix 2. This observation is reminiscent of the rank deficiency of β_{2i} in model 2 (equation [2\)](#page-2-0). On the basis of these results, a parametric Monte Carlo simulation program is devised to obtain the null distribution of z_i 's, accounting for both correlation and rank deficiency in the multivariate asymptotic null distribution (Web Appendix 3). The null distributions of the quantiles of *m* observed P values are obtained and compared with the observed quantiles. Testing of the global null hypothesis can then be achieved by comparing the Fisher's combination statistic with its null distribution. The familywise error rate or false discovery rate can be used to perform significance tests for individual pleiotropic effects.

For case-control MR studies, fitting model 3 (equation [3\)](#page-2-0) while accounting for case-control sampling could be accomplished by means of the inverse probability weighting method using estimation procedures for relative risk models as discussed previously, if such weights are known or can be derived from the population incidence of the disease *Y* [\(27\)](#page-8-0). For many cancers, the incidence is low and the odds ratio estimates from standard logistic regression approximate the relative risk estimates, so any software that implements logistic regression can be used to derive surrogate direct effects and associated P values. The crux of computation in the GLIDE procedure is to generate null distributions of surrogate direct effects, particularly when there are a large number of candidate IV SNPs. We have developed an R package (R Foundation for Statistical Computing, Vienna, Austria) for GLIDE, freely available from the Comprehensive R Archive Network [\(https://cran.r-project.org/\)](https://cran.r-project.org/), with which to implement and disseminate the proposed method.

RESULTS

Simulation to assess validity and power

A case-control MR study was simulated to assess the performance of the proposed GLIDE procedure. The data vector for a subject contains a binary outcome *Y*, an exposure *X* that has a normal distribution, 25 SNPs as candidate IVs, and a variable *U* representing unmeasured confounding between *X* and*Y*. The SNPs were generated from a multinomial distribution at (0, 1, 2), with probabilities corresponding to minor allele frequencies randomly selected from a uniform distribution with a range from 0.1 to 0.4. The data-generating models for (Y, X, G, U) are

$$
U = \varepsilon_1 \tag{4}
$$

$$
X = \sum_{j} \alpha_{j} G_{j} + U + \varepsilon_{2} \tag{5}
$$

$$
\mathbb{E}(Y) = \exp\left(\beta_0 + \sum_j \gamma_j G_j + \beta_1 X + U + \varepsilon_3\right),\tag{6}
$$

where β_1 is the causal effect of *X* on *Y* (set to be either 0 or 0.5), α_j 's represent the strength of IVs, γ_j 's are the direct effects to be tested, and $(\varepsilon_1, \varepsilon_2, \varepsilon_3)$ are drawn from independent normal distributions with mean 0 and variance 0.25. We assume that **G** is independent of U in the simulation study shown in the main text, and we left the scenario with **G** being dependent on *U* in Web Appendix 4 as a sensitivity analysis. We generated α_j 's from a uniform distribution with a range from 0.1 to 0.2. The direct effects γ_j 's are zero under the null hypothesis or drawn from a uniform distribution under the alternative hypothesis, which may be correlated with α ^{*'*}s. In all simulation settings, we chose the value of $β_0$ to achieve a disease prevalence 0.01 and generate a population of 50,000 or 250,000 individuals. All cases and an equal number of controls were sampled in the case-control study. The case-control sampling scheme was accounted for in analyses by the inverse probability weighting method.

Control of type I error rate. Table 1 shows the empirical type I error rates in 2,000 simulated data sets when $\gamma_i = 0$ for all *j*, so that there is no direct effect for any of the 25 genetic variants. For GLIDE, we evaluate whether the Fisher's combination statistic for the surrogate direct effects attains the type I error level at 0.05. For the MR-Egger method, we test whether the intercept of the Egger regression is zero, using the weighted least squares procedure ([15](#page-8-0)). As expected, both tests achieve proper control of the type I error rate for the 2 sample sizes considered, whether or not there is a causal effect of *X* on *Y*. The validity of the 2 methods requires the independence between*Gj*'s and*U*, as additional simulations in Web Appendix 4 (Web Table 1) show.

Statistical power for testing for global pleiotropy. In Figure [2](#page-4-0) and Web Figure 1, we show the statistical power achieved for detection of global pleiotropy under a variety of distributions of γ_j 's. The details of the parameter settings in these simulation experiments are described in Web Appendix 5. Figure [2](#page-4-0) shows scenarios where there is a causal effect of *X* on*Y*, namely $\beta_1 = 0.5$ in model 6 (equation 6), among which Figures [2A](#page-4-0)–[2](#page-4-0)C show scenarios where the distributions of the direct effects and the instrumental strengths are uncorrelated and [2](#page-4-0)D shows a scenario where the direct effects and the instrumental strengths are indeed correlated. In Figure [2A](#page-4-0), the direct effects are all positive. In Figure [2](#page-4-0)B, some direct effects are negative and others are positive, representing a scenario close to "balanced pleiotropy" [\(15\)](#page-8-0). In Figure [2C](#page-4-0), only a subset of variants (15 out of the 25 (60%)) have pleiotropic effects. Note that even if the distributions of the direct effects and the instrumental strengths are probabilistically uncorrelated in Figures [2](#page-4-0)A–[2](#page-4-0)C, in each simulated data set the covariance of α_j and γ_j in the sample is not exactly zero; therefore

Table 1. Type I Error Rate for the Proposed GLIDE Test and the MR-Egger^a Test When the Nominal P Value Is 0.05

Sample Size, no.		Causal Effect	Test	
Cases	Controls	(β_1)	GLIDE	MR-Egger
500	500	0	0.0436	0.0489
		0.5	0.0457	0.0505
2.500	2.500	0	0.0482	0.0494
		0.5	0.0484	0.0503

Abbreviations: GLIDE, global and individual tests for direct effects; MR, Mendelian randomization.
^a Egger's test for assessing pleiotropy in MR.

Figure 2. Statistical power, in simulations, of the global and individual tests for direct effects (GLIDE) and Mendelian randomization (MR)-Egger methods to test the global null hypothesis that there is no direct effect for any genetic variant. The sold line represents results of the GLIDE test, and the dotted-dashed line represents results of the MR-Egger test. A) The direct effects are all positive; B) some direct effects are positive and some are negative; C) a proportion of single nucleotide polymorphisms (SNPs) (60%) have pleiotropic effects; D) all SNPs have direct effects that are correlated with the genetic associations with the intermediate exposure. RR, relative risk.

a naive inverse-variance–weighted estimate of the causal effect will be biased in all 4 scenarios (simulation results not shown).

In all 4 scenarios shown in Figure 2, GLIDE outperforms MR-Egger substantially. The power improvement can reach as much as 20% when all direct effects are positive in Figure [1](#page-1-0)A, while a much greater power gain is seen in Figures 2B and 2D. The improvement stems from the MR-Egger test suffering reduced power performance when some direct effects are negative and others are positive, since the intercept in the MR-Egger regression tends to get close to 0 (but not exactly 0), as negative and positive effects may cancel out in the overall impact on the intercept. It is important to note that balanced pleiotropy that does not distort estimation in the MR-Egger method is a numerical coincidence and is rarely exactly satisfied in practice. When the causal effect β_1 was set to be zero while all other parameters remained unchanged (Web Figure 1), the power comparisons showed no difference from Figure 2.

Estimation of individual direct effects. A simulation study was conducted to evaluate the bias of the estimated surrogate direct effect for a particular genetic variant (γ_{1j}) in model 3 (equation [3\)](#page-2-0) as estimates of true individual direct effects (β_{2i}) . The degree of approximation between γ_{1i} and β_{2i} is critical to the use of the Q-Q plot as a means to identify individual variants with potentially pleiotropic effects. The models and results of this simulation study were relegated to Web Appendix 6 (Web Table 2). Under diverse simulation settings, the results in Web Table 2 suggest that the estimated surrogate direct effect captures the corresponding true direct effect and the bias is largely negligible.

GECCO data analyses

We analyzed epidemiologic and genetic data from 10,226 colorectal cancer cases and 10,286 population-based controls of European ancestry from 11 studies (6 cohort studies and 5 case-control studies) included in the GECCO Consortium and the Colon Cancer Family Registry (Web Appendix 7). Full details on these consortia (GECCO and the Colon Cancer Family Registry) have been published elsewhere [\(29](#page-8-0)). We previously reported results for 77 BMI-linked SNPs and 696 height-linked SNPs identified in the Genetic Investigation of Anthropometric Traits (GIANT) Consortium as IVs in MR analyses using GECCO and Colon Cancer Family Registry data [\(30,](#page-8-0) [31](#page-8-0)). These results suggested that genetically determined BMI and height are both associated with the risk of colorectal cancer, indicating evidence of causality ([30](#page-8-0), [31\)](#page-8-0).

We now investigate the validity of these 77 BMI-linked SNPs and 696 height-linked SNPs as IVs, using both GLIDE and the MR-Egger regression approaches. Two genetic risk scores were computed on the basis of association estimates in the GIANT Consortium ([32,](#page-8-0) [33](#page-8-0)). Because colorectal cancer is a rare disease in these populations, surrogate direct effect estimates and their respective P values in model 3 (equation [3\)](#page-2-0) were obtained via a logistic regression model approximating a log-linear model for relative risk estimates. The null distribution of P values was obtained from 50,000 simulated data sets following the degenerate multivariate normal distribution.

Figures 3A and 3C show scatterplots of the reported genetic associations from the GIANT genome-wide association study [\(30](#page-8-0), [31](#page-8-0)) and the associations with risk of colorectal cancer in GECCO, respectively. Figures 3B and 3D show the respective Q-Q plots of P values derived from the GLIDE method. MR-Egger regression suggests that there is no evidence of pleiotropy for either analysis (BMI: intercept = 0.001 , $P = 0.89$; height: intercept = 0.002 , $P = 0.33$). The P values for testing of global pleiotropy from GLIDE are 0.55 (BMI) and 0.02 (height), indicating that there is evidence of global pleiotropy for the height MR analysis. The Q-Q plots are more informative for diagnosing individual variants. Figure 3 shows that there are 2 BMI-linked variants (rs16951275 and rs12286929) with evidence of a direct effect (solid squares; false discovery rate < 0.2) and 3 height-linked SNPs (rs3923086, rs11144688, and rs6085662) with evidence of a direct effect (solid squares; false discovery rate < 0.2). We use a false discovery rate of 0.2 as the significance cutoff because we want to be conservative in selecting

Figure 3. Application of Menedelian randomization (MR)-Egger regression and the proposed global and individual tests for direct effects (GLIDE) test to data from the Genetics and Epidemiology of Colorectal Cancer (GECCO) Consortium in a study of body mass index (BMI; weight (kg)/height (m)²) and height in colorectal cancer (CRC) risk. The solid squares represent single nucleotide polymorphisms (SNPs) with some evidence of pleiotropy detected by GLIDE; the open circles represent SNPs which did not exhibit evidence of pleiotropy. A) MR-Egger regression results showing the intercept and slope for 77 SNPs previously shown to be linked to BMI in the Genetic Investigation of Anthropometric Traits (GIANT) Consortium [\(30](#page-8-0), [31](#page-8-0)). B) Proposed GLIDE test results showing the quantile-quantile (Q-Q) plot for P values derived from assessment of surrogate direct effects for BMI. C) MR-Egger regression results showing the intercept and slope for 696 SNPs previously shown to be linked to height in the GIANT consortium. D) Proposed GLIDE test results showing the Q-Q plot for P values derived from assessment of surrogate direct effects for height. RR, relative risk.

Table 2. Estimates of Surrogate Direct Effects for Single Nucleotide Polymorphisms With Some Evidence of Pleiotropy Detected via the GLIDE Method in Analyses of Body Mass Index and Height Associations With Colorectal Cancer Risk^a

Study and SNPID No.	Gene	Surrogate Direct Effect (RR ^b)	Nominal P Value	FDR
BM ^c				
rs16951275 MAP2K5		1.09	0.0006	0.046
rs12286929	CADM2	0.94	0.0048	0.183
Height				
rs3923086	AXIN2	1.08	2.9×10^{-4} 0.12	
rs11144688	PCSK5	1.14	3.5×10^{-4}	012
rs6085662	BMP2	1.08	5.5×10^{-4}	0.13

Abbreviations: AXIN2, axis inhibition protein 2 gene; BMI, body mass index; BMP2, bone morphogenetic protein 2 gene; CADM2, cell adhesion molecule 2 gene; FDR, false discovery rate; GLIDE, global and individual tests for direct effects; ID, identification; MAP2K5, mitogen-activated protein kinase kinase 5 gene; PCSK5, proprotein convertase subtilisin/kexin type 5 gene; RR, relative risk; rs, reference SNP; SNP, single nucleotide

polymorphism.
^a Data were obtained from 11 studies (6 cohort studies and 5 casecontrol studies) included in the Genetics and Epidemiology of Colorectal Cancer Consortium and the Colon Cancer Family Registry (Web Appendix 7).
^b The RR was calculated per 5-unit increment for BMI and per 10-

cm increment for height.
^c Weight (kg)/height (m)².

valid IVs for MR. As such, these results suggest that these SNPs should be omitted in the subsequent refined MR estimation. For clarity, these SNPs with evidence of pleiotropy are also highlighted in Figures [3A](#page-5-0) and [3C](#page-5-0) as solid squares.

These 5 SNPs and their associated genes are listed in Table 2, each having a small surrogate direct effect estimate in relative risk. Notably, in annotation work in the GIANT studies, Locke et al. (32) (32) (32) and Wood et al. (33) have reported that the genes associated with these SNPs are linked to important cellular functions and multiple pathways: The mitogen-activated protein kinase kinase 5 gene (MAP2K5) is in the MAP kinase signaling pathway involved in growth factor–stimulated cell proliferation and muscle cell differentiation; the cell adhesion molecule 2 gene (CADM2) involves cell-to-cell adhesion and synaptic function in neuronal development and the immune system; the axis inhibition protein 2 gene (*AXIN2*) is a negative regulator of wingless/integrated (Wnt)/β-catenin signaling; the proprotein convertase subtilisin/kexin type 5 gene (PCSK5) is involved in endopeptidase activities, abnormal skeleton development, basal cell carcinoma, and Wnt-protein binding; and the bone morphogenetic protein 2 gene (BMP2) encodes a secreted ligand of the transforming growth factor β family of proteins, which are involved in a number of cellular functions. In either analysis, the MR-Egger test was not able to detect any evidence of pleiotropic effects (Figure [3\)](#page-5-0).

Next, as a sensitivity analysis, we removed the 5 SNPs with some evidence of pleiotropy and recomputed the genetic risk scores and estimated surrogate direct effects for the remaining 75 BMI SNPs and 693 height SNPs, respectively. The Q-Q plots of Table 3. Causal Effect Estimates Obtained With and Without the 2 Single Nucleotide Polymorphisms Showing Evidence of Pleiotropy in Analyses of Body Mass Index and Height Associations With Colorectal Cancer Risk^a

Abbreviations: BMI, body mass index; CI, confidence interval; GECCO, Genetics and Epidemiology of Colorectal Cancer; IV, instrumental variable; RR, relative risk; SNP, single nucleotide polymorphism.
a Data were obtained from 11 studies (6 cohort studies and 5 case-

control studies) included in the GECCO Consortium and the Colon Cancer Family Registry (Web Appendix 7).
^b The RR was calculated per 5-unit increment for BMI and per 10-

cm increment for height. Estimates were adjusted for age, sex, the top 3 principal components in GECCO genome-wide association study data, and the 11 GECCO studies (included as indicator variables in the regression).
^c Weight (kg)/height (m)².

the P values suggested that the refined sets of SNPs exhibit little evidence of pleiotropy in either analysis (Web Figure 2). Table 3 shows the resulting causal estimates obtained when the SNPs with evidence of pleiotropy were excluded in the refined 2-stage IV regression. The estimates were adjusted for age, sex, the top 3 principal components in the GECCO genome-wide association study data, and the 11 GECCO studies (included as indicator variables in the regression). In both the BMI analyses and the height analyses, excluding the violating SNPs results in an attenuated effect size for the causal estimate and an increased P value, because those deleted SNPs are typically the outliers of genetic association. This data example showcases the utility of the proposed method: It enables assessment of individual variants and leads to sensitivity analyses that remove potentially invalid IVs, thereby improving the validity of MR analysis.

DISCUSSION

In this article, we have proposed a diagnostic tool, GLIDE, for assessing global and individual pleiotropy in MR studies. Our method is formulated for estimating causal relative risk in a log-linear model and therefore is tailored specifically for binary disease outcomes. The unique feature of our method with respect to existing methods is that it provides a rigorous assessment of pleiotropy for individual genetic variants, therefore allowing sensitivity analyses with a more justified subset of IVs. Furthermore, for assessment of global pleiotropy, our simulations and data examples show that the power of GLIDE is uniformly better than the MR-Egger regression method.

In analyses evaluating associations of BMI and height with the risk of colorectal cancer, GLIDE detected 2 BMI-linked SNPs and 3 height-linked SNPs that showed evidence of pleiotropy. Removing these SNPs in subsequent MR analyses resulted in attenuated causal effects, since those SNPs often present as outliers in genetic associations. These examples highlight the importance of evaluating and diagnosing IVs before causal testing. As we elaborated in the Introduction, pleiotropic effects can be common for genes and mutations that affect complex traits. Assessment of any direct effects of genotypes on the outcome (i.e., the presence of pleiotropy) can also be tested using mediation analysis, if the information on the intermediate exposure and all confounders is available. However, such an analysis yields inaccurate results when the exposure is measured with error, which is often the case when a single measurement per subject (e.g., blood pressure) is used to represent a long-term average of the exposure (e.g., blood pressure) over time. Thus, the mediation analysis approach is limited in practice, and our method does not have these limitations.

GLIDE works best for MR analyses with many independent variants, where a $Q-Q$ plot of P values can be informative. If there are only a few variants (<10), it becomes difficult to visualize and assess evidence of violations from a Q-Q plot and subsequently remove individual variants that may drive the violation. Paradoxically, more SNPs in the IV would increase the statistical power of testing the causal effect but at the same time lower the power of GLIDE to assess the potential of individual variants' pleiotropic effects due to multiple testing. One possible extension of GLIDE is to group variants by pathways or chromosomes and test pleiotropy by group.

GLIDE assumes that genetic variants are independent of confounding variables. Violation of this independence assumption will lead to false-positive findings in assessing pleiotropy (Web Table 1). GLIDE does not solve the fundamental problem when estimating direct effects through the IV regression approach, as these individual causal direct effects are not identifiable together with the causal effect of interest. The surrogate direct effects estimated through GLIDE are merely approximations of the direct effects when there are many variants, and when there are positive and negative direct effects. Though GLIDE is generally more sensitive than MR-Egger regression for detecting pleiotropy, it does not always detect direct effects. There are scenarios in which surrogate direct effects are zero yet true direct effects are not all zero. This limitation is inevitable, because individual causal direct effects are not identifiable without additional constraints.

Genetic epidemiology is advancing from discovering genome-wide associations to more functionally characterizing genetic associations. In this context, causal inference and mediation analyses are becoming important tools for epidemiologic analysis, providing a stronger, causal interpretation rather than a mere association. However, investigators need to exert caution and carefully examine the underlying assumptions of IVs before engaging in causal estimation. The proposed GLIDE method is useful for assessing variants for evidence of pleiotropy and improving the validity of the MR approach.

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