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Exploring the Applicability of Density Functional Tight Binding to Transition Metal Ions. Parameterization for Nickel with the Spin-polarized DFTB3 model

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Abstract

In this work, we explore the applicability and limitations of the current Third Order Density Functional Tight Binding (DFTB3) formalism for treating transition metal ions using nickel as an example. To be consistent with recent parameterization of DFTB3 for copper, the parameterization for nickel is conducted in a spin-polarized formulation and with orbital-resolved Hubbard parameters and their charge derivatives. The performance of the current parameter set is evaluated based on structural and energetic properties of a set of nickel-containing compounds that involve biologically relevant ligands. Qualitatively similar to findings in previous studies of copper complexes, the DFTB3 results are more reliable for nickel complexes with neutral ligands than for charged ligands; nevertheless, encouraging agreement is noted in comparison to the reference method, B3LYP/aug-cc-pVTZ, especially for structural properties, including cases that exhibit Jahn-Teller distortions; the structures also compare favorably to available X-ray data in the Cambridge Crystallographic Database for a number of nickel-containing compounds. As to limitations, we find it is necessary to use different *d* shell Hubbard charge derivatives for Ni(I) and Ni(II), due to the distinct electronic configurations for the nickel ion in the respective complexes, and substantial errors are observed for ligand binding energies, especially for charged ligands, *d* orbital splitting energies and splitting between singlet and triplet spin states for Ni(II) compounds.

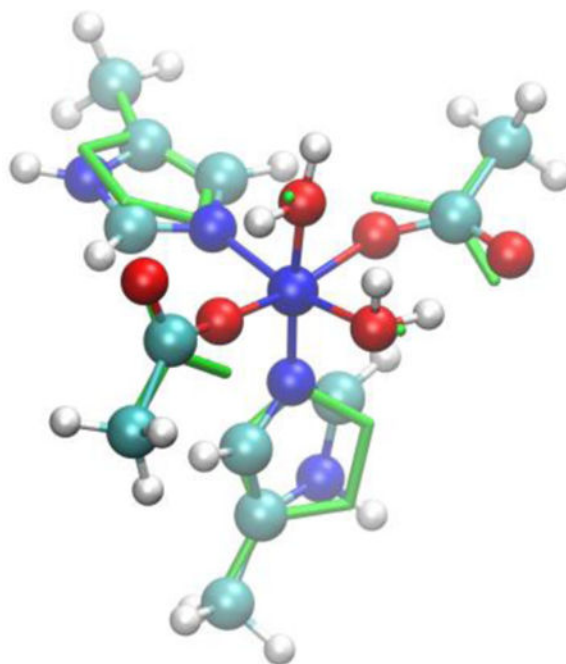
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Supplementary Information

Spin coupling parameters, detailed structural information for the test molecules and additional energetics data (sequential bond dissociation energies, ligand proton affinities; singlet-triple splitting for Ni(II) compounds, in Excel spread sheet format) are available. Also included is a brief discussion of an alternative parameterization that aims to improve Ni...H interactions.

These observations highlight that future improvement in intra-*d* correlation and ligand polarization is required to enable the application of the DFTB3 model to complex transition metal ions.

TOC Graphics



The Density Functional Tight Binding (DFTB) model parameterized for Nickel leads to reliable structural properties for Nickel-containing compounds, including Jahn-Teller distortions, but less accurate ligand binding energies. More sophisticated treatment of the *d-d* interactions is required to improve energetics, including the order of different spin states.

Keywords

DFTB3; DFT; Hubbard parameters; nickel; spin states; Jahn-Teller distortion

1 Introduction

Transition metal ions play various important structural and catalytic roles in biomolecules.¹⁻² To aid experimental analysis regarding how transition metal ions contribute to biomolecular function, effective computational methodologies are needed. For structural properties, molecular mechanical (MM) force fields have been developed for treating metal ions at different levels of sophistication;³ these include simple van der Waals sphere models⁴⁻⁶, non-bonded dummy models,⁷ bonded force field models⁸⁻⁹, valence-bond models¹⁰⁻¹¹ and ligand-field force field models¹²⁻¹⁵. To describe chemical reactions that involve transition metal ions, a quantum mechanical (QM) description is required, which include Density Functional Theory (DFT) and *ab initio* wavefunction approaches.¹⁶⁻¹⁷ The last several decades have seen tremendous progress in both classes of QM methods, and it has become possible to analyze the electronic structure of complex metal co-factors such as

iron-sulfur clusters with modern electronic structure methods¹⁸. Nevertheless, these methods remain computationally expensive, thus even hybrid QM/MM calculations^{19–20} using a modest DFT or *ab initio* region are usually limited to minimum energy path type of calculation or free energy simulations with a minimal amount of sampling²¹. In some applications, the biological system of interest is highly flexible and therefore a meaningful study would require an extensive degree of sampling;²² examples include metalloenzymes that feature a high degree of catalytic promiscuity, metal ion transporters/transcription factors, proteins involved in the assembly of catalytic metal cofactors and peptides/proteins whose (mis)folding and aggregation behaviors are influenced by transition metal binding. For these problems, it is important to develop a QM method that allows adequate sampling while treating the transition metal ions with a reasonable level of accuracy. In this context, the traditional semi-empirical quantum chemical methods (MNDO^{23–25}, AM1²⁶, PMx^{27–31}, OMx³²), although being 2–3 orders of magnitude faster than DFT and *ab initio* QM methods, face difficulties, since they are usually not accurate or transferable enough to deal with the complexity of transition metal ions. This is due in part to the fact that the basis of these semi-empirical methods is Hartree-Fock, in which electron correlation is neglected entirely.

Density Functional Tight Binding (DFTB) emerged^{33–35} in recent years as an alternative semi-empirical approach. It is rigorously rooted in DFT³⁶, and almost all DFTB parameters are computed with DFT for atoms and small (diatomic) molecules; since it is derived from DFT, effects of electron correlation is included explicitly albeit in an approximate fashion. DFTB utilizes minimum valence basis sets and further reduces computational effort by approximations to the matrix elements, leading to 2–3 orders of magnitude faster computations than full DFT³⁷. With careful parameterization, both the second-order (DFTB2³⁶) and third-order (DFTB3³⁸) formulations have proven applicable to many chemical, materials and biological problems, especially when sampling is important.
34–35, 39–45

Specifically for metals, the first set of developed DFTB2 parameters was for zinc, which is a closed-shell d^{10} system⁴⁶. Zheng et al.⁴⁷ developed DFTB2 parameters for several first-row transition metal elements (i.e. Sc, Ti, Fe, Co and Ni); the model was shown to be adequate in predicting geometrical properties of organometallic compounds and small metal clusters⁴⁸, although accuracy in energetics was lacking, especially concerning the order of different spin states. For the third-order model, DFTB3, parameters were developed for closed shell metal ions⁴⁹ (Na, K and Ca), as well as for Mg and Zn⁵⁰, in a framework consistent with the 3OB parameterization for the main group elements (C, H, N and O⁵¹, P and S⁵² and the halogens⁴⁹) for chemical and biological applications. Recently, Gaus et al.⁵³ developed parameters for Cu, which has a d^{10} or d^9 electronic configuration, depending on the oxidation state. Their work considered spin polarization and *spd l*-dependent interactions; including the *l*-dependence in the Hubbard parameters was observed to be crucial to have a balanced treatment of Cu(I) and Cu(II) species.⁵³ Structures and ligand binding energies were found to be generally in good agreement with reference B3LYP calculations with large basis sets (aug-cc-pVTZ), and in some cases the DFTB3 model was observed to outperform the parent DFT model (PBE) with medium sized basis sets, due to the use of higher-level methods for the parameterization. Overall, the performance for charge ligands was less

satisfactory than for neutral ligands, an expected result considering the minimal basis set used in DFTB3; improving the treatment of electronic polarization will likely reduce the errors for charged and polarizable ligands, as found for intermolecular interactions^{42, 54–55}. Finally, we note that Grimme et al.⁵⁶ developed a tight-binding model for the entire periodic table, including transition metal ions; the model was fitted based on 32 transition metal complexes (which included only three Ni-containing compounds) and focused entirely on structural properties and vibrational frequencies without reported energetics.

In this work, we further explore the applicability of the DFTB3 model to transition metal ions by conducting parameterization for nickel, which is involved in enzymes vital in global carbon, nitrogen and oxygen cycles in fungi, algae, eubacteria and higher plants^{57–61}. Seven of eight known nickel enzymes encompass the production or use of important gases (CO, CO₂, CH₄, NH₃ and O₂), e.g., Nickel Superoxide Dismutase⁶², Acireductone Dioxygenase^{63–64}, Urease^{63, 65}, CO Dehydrogenase^{66–67} and NiFe Hydrogenases^{68–69}, highlighting the need of properly understanding nickel bonding and reactivity in biological environments.

We focus in this work on Ni(I) and Ni(II), which feature d^9 and d^8 electronic configurations, respectively. It must be stressed here that this study can only be carried out because these electronic configurations do not require to take into account the strong correlation between the electrons inside the compact d -shell. In particular, the d^9 configuration contains a single hole that is equivalent to that of a non-correlated d^1 configuration⁷⁰ while in the d^8 configuration the two possible ground states with $S=0$ and $S=1$ are usually well separated and many properties can be correctly predicted even when neglecting the intra- d correlation. A reliable treatment of these open-shell configurations would in principle require an explicit treatment of intra- d electron correlation, for example in the framework of LDA+U⁷¹ that would be impossible to avoid when dealing with d^3 to d^7 electron configurations. Prior to including such contributions to the DFTB model, however, it is worthwhile establishing what properties can be adequately described in the current DFTB3 framework, in which the intra- d interactions are treated in an averaged fashion, and what properties clearly require an improved treatment of the d electrons and other effects (e.g., ligand polarization and metal-ligand charge transfer). In particular, transition metal ions show a very strong correlation between their electronic structure, including the magnetic state, and the geometry leading to strong electron-vibration coupling phenomena that can play an important role in reactivity.⁷² Of particular importance is the Jahn-Teller effect where the geometry of the system is distorted towards lower symmetry because of the existence of two or more degenerate electron states whose electron distributions are different; similar distortions may also appear in the absence of degeneracy due to the so-called pseudo Jahn-Teller effect if the vibronic interactions are strong enough. In the case of Nickel we summarize some of these effects in Figures 1 and 2 corresponding with Ni(I) and Ni(II), respectively, and where we show the expected electron configuration, total spin and possible Jahn-Teller distortions for several coordination numbers. Capturing all these effects is a tough test for any approximate computational method and the chief goal of this work is to clearly define the limitations of the current DFTB3 model for the treatment of open-shell transition metal ions and to highlight opportunities for future developments in the DFTB Hamiltonian.

In the following, we first briefly summarize the DFTB3 formalism and then describe the parameterization protocol for nickel, particularly with respect to its $4s^2 3d^8$ atomic configuration and the treatment of Ni(II). This is followed by an extensive evaluation of the resulting DFTB3/3OB model for structures and energetic properties of various complexes that contain nickel and biologically relevant ligands. We conclude by a summary of the results, along with perspectives on necessary improvements of DFTB3 for transition metal ions.

2 A brief review of DFTB3

DFTB represents a class of approximate DFT methods, which are described fully in the literature.^{33, 36, 42, 53, 73–77} The fundamental principle of DFTB is tightly bound electrons with perturbatively treated interactions.

Briefly, DFTB considers the electronic energy of the system as an expansion in terms of the deviation of electron density from a reference density, ρ^0 , which is taken as a superposition of precalculated atomic densities,

$$\rho(\mathbf{r}) = \sum_i n_i \psi_i^*(\mathbf{r}) \psi_i(\mathbf{r}) = \rho^0(\mathbf{r}) + \Delta \rho(\mathbf{r}), \quad (1)$$

in which only valence electrons are described explicitly. Three-center integrals are neglected and the two-center Hamiltonian and overlap matrix elements are precalculated for a mesh^{38, 78} of interatomic distances using Slater-Koster *sin/cos*-rules⁷⁹. This reduces the calculation runtime since no further integration is necessary.

With this treatment of electron density and expanding the electronic energy in a Taylor series of ρ , the DFTB total energy can be written as

$$\begin{aligned} E[\rho^0 + \Delta \rho] &= \sum_i n_i \int \psi_i^*(\mathbf{r}) \left(-\frac{\nabla^2}{2} + V_{ne}(\mathbf{r}) + \int' \frac{\rho^{0'}}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' + V_{xc}[\rho^0] \right) \psi_i(\mathbf{r}) d\mathbf{r} \quad (2) \\ &- \frac{1}{2} \iint' \frac{\rho^{0'} \rho^0}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r} d\mathbf{r}' - \int V_{xc}[\rho^0] \rho^0 d\mathbf{r} + E_{xc}[\rho^0] + E^{mn} \\ &+ \frac{1}{2} \int' \int \left(\frac{1}{|\mathbf{r} - \mathbf{r}'|} + \frac{\delta^2 E_{xc}[\rho]}{\delta \rho \delta \rho'} \bigg|_{\rho^0, \rho^{0'}} \right) \Delta \rho \Delta \rho' d\mathbf{r} d\mathbf{r}' \\ &+ \frac{1}{6} \int'' \int' \int \frac{\delta^3 E_{xc}[\rho]}{\delta \rho \delta \rho' \delta \rho''} \bigg|_{\rho^0, \rho^{0'}, \rho^{0''}} \Delta \rho \Delta \rho' \Delta \rho'' d\mathbf{r} d\mathbf{r}' d\mathbf{r}'' + \dots, \end{aligned}$$

in which E_{xc} , V_{xc} is the exchange-correlation energy and exchange-correlation potential, respectively.

DFTB3 includes up to third order terms^{74–75} in the Taylor expansion, and the DFTB3 total energy reads:

$$E^{DFTB3} = E^{H0} + E^\gamma + E^\Gamma + E^{rep} = \sum_{iab} \sum_{\mu \in a} \sum_{\nu \in b} n_i c_{\mu i} c_{\nu i} H_{\mu\nu}^0 + \frac{1}{2} \sum_{ab} \Delta q_a \Delta q_b \gamma_{ab} + \frac{1}{3} \sum_{ab} \Delta q_a^2 \Delta q_b \Gamma_{ab} + E^{rep}. \quad (3)$$

in which the first three terms represent the first-, second- and third-order electronic contributions, and E^{rep} is the repulsive potential that includes the nuclear-nuclear repulsion and double-counting zero-th order terms. The LCAO coefficients ($C_{\mu i} C_{\nu i}$) are solved self-consistently by applying variational principle to the energy expression, leading to the Kohn-Sham equations that define the corresponding Kohn-Sham orbitals, $\psi_A(\mathbf{r})$.

The second-order kernel, γ_{ab} , reduces to $1/r_{ab}$ for large interatomic distances and describes the Coulomb interaction of q_a and q_b partial charges; in the opposite limit, it describes the on-site self-repulsion and can be expressed as the Hubbard parameter (U_a),

$$\gamma_{aa} = U_a, \quad (4)$$

where U_a is the second derivative of total energy for a neutral atom with respect to the occupation number of the highest occupied orbital. U_a correlates with the size of an atom in an inverse relationship,³⁶ except for the hydrogen atom, for which a modification (referred to as the γ^h function) was made and observed to improve hydrogen bonding interactions.^{37, 77–78}

In DFTB3, the Hubbard parameters are charge dependent (described with Γ_{ab} in Eq. 3)^{78, 80} and therefore γ_{ab} is charge dependent through the Hubbard parameters;^{38, 53} including the charge dependence improves the description of charged and polarizable species within the framework of a minimal basis. Additionally, orbital angular momentum (l) dependence of the Hubbard parameter and its charge derivative can be introduced as in the previous extension of DFTB2 that employs different Hubbard parameters for each element and for each orbital angular momentum⁴⁸. This enhancement of flexibility in the Hamiltonian is especially significant for transition metals, which have notably different $3d$ and $4s$ orbitals⁸¹; including the l -dependence in the Hubbard parameters modifies the effective interaction of electrons in these orbitals through γ_{ab} . Finally, spin-polarization effects have been treated in a collinear fashion as in references^{48, 53, 82–83}.

$$\begin{aligned}
E^{DFTB3} &= E^{H0} + E^\gamma + E^{\Gamma'} + E^{rep} + E^{col-spin} \\
&= \sum_{\sigma=\uparrow,\downarrow} \sum_{iab} \sum_{\mu \in a} \sum_{\nu \in b} n_{i\sigma} c_{\mu i\sigma} c_{\nu i\sigma} H_{\mu\nu}^0 \\
&+ \frac{1}{2} \sum_{ab} \sum_{l_a l_b} \Delta q_{l_a} \Delta q_{l_b} \gamma_{ab, l_a l_b} + \frac{1}{3} \sum_{ab} \sum_{l_a l_b} \Delta q_{l_a} \Delta q_{l_b} \Delta q_a \Gamma_{l_a l_b} + E^{rep} \\
&+ \frac{1}{2} \sum_a \sum_{l \in a} \sum_{l' \in a} p_{l_a} p_{l'_a} W_{l_a l'_a}
\end{aligned} \tag{5}$$

It is important to note that applying this expression is reasonable when there are up to two spin states associated with the d -shell as is the case of Ni(II) (see Figure 2). However, it would be unrealistic to expect the formulation to deal with systems with many intermediate states (as occurring in configurations with 3–7 electrons in the d -shell), since the spin-dependent term does not depend on the magnetic quantum number m_l . Moreover, the charge derivative of the Hubbard parameter has been considered within shell l_a . We adopt the protocol developed by Gaus et al⁵³, in which the Hubbard derivatives are computed using the total atomic charges instead of populations associated with each shell. As described below, we find it is necessary to use different Hubbard derivative parameters for Ni(I) and Ni(II) for more reliable properties within the current DFTB3 formulation. This is ultimately related to the fact that electrons in the d -shell are strongly correlated and cannot be treated on the same footing as those corresponding with the valence shell of main elements.

3 Parametrization procedure

The DFTB3 parametrization protocol involves two steps: the parametrization of electronic parameters and of repulsive potentials. The parametrization is performed in a manner consistent with the 3-ob parameter set^{49–52}, which is available on the www.dftb.org website under the name 3ob-3-1. The global parameter $\zeta=4.00$ is employed for the scaled γ_{XH} along with the specified Hubbard derivatives for each atom in the 3ob set. The choice of reference method for the parametrization of repulsive potentials for transition metal elements has previously been carefully discussed;^{50, 53} to comply with previous studies, the B3LYP/aug-cc-pVTZ level of theory is again employed, although we are aware of the limitations of the B3LYP functional for Ni complexes¹⁷ (for example, for a quantitative description of Jahn-Teller distortions⁸⁴). Atomic one-center electronic calculations are performed with the PBE⁸⁵ functional as developed by Perdew and Zunger⁸⁶, which has become standard for this parametrization step of DFTB models^{50–51, 53}. The atom-centered wave functions ϕ_μ are formulated as Slater-type orbitals and as such employ wavefunction (r_l^{wf}) and density (r^{dens}) compression radii. Since collinear spin-polarization calculations are employed, atomic spin-polarization constants derived with the PBE functional are utilized^{53, 87} (see Table S1).

3.1 Electronic Parameters

The ground state electronic configuration for nickel is $4s^2 3d^8$ and it is used to determine the two-center integrals of the charge independent Hamiltonian and overlap integrals. The other possible choice is the $4s^1 3d^9$ configuration; for a proper description of Ni(II) compounds, however, the atomic $4s^2 3d^8$ configuration is more appropriate. As a consequence of this choice, slightly better geometries for Ni(II) species in comparison to Ni(I) is observed (*vide infra* and in the Supplementary Information). For calculating ϵ_s , ϵ_p , ϵ_d , E^{spin} , Hubbard parameters as well as the Hamiltonian and overlap matrix elements, two in-house programs *slateratom* and *sktwocnt* are employed. Although the $4p$ orbitals of Ni are unoccupied, they are included in the basis set as polarization functions. The addition of polarization functions is consistent with previous parametrization of several elements within the DFTB3/3OB framework^{50, 53} and, as previously, it is noted that addition of polarization functions helps improve the bonding of Ni to other elements.

Several values obtained via atomic one-center PBE calculations are adjusted (ϵ_p , ϵ_d , U_s , U_p , U_d , U_d^d) in order to accommodate the complexity of the nickel electronic configuration, while the others are kept as computed (see Table 1). It is noted that the sign of ϵ_p greatly influences convergence of tetra-coordinated nickel complexes and the positive value of 0.046000 a.u. is ultimately chosen. With the ϵ_p value shifted, setting the value of U_p to 0.251943 a.u. instead of the computed value of 0.158730 a.u. improves the results. It is also found advantageous to change U_s from the computed value of 0.251943 a.u. to 0.158730 a.u. to ensure the smooth curvature of the repulsive potentials. The Hubbard parameter and its charge derivative for the $3d$ orbitals are adjusted so that the oxidation potential of $Ni^+ \rightarrow Ni^{2+}$ calculated at the B3LYP/aug-cc-pVTZ level of theory is reproduced. This choice improves bond dissociation energies (BDEs) and other properties. Furthermore, with the Hubbard parameter value and its charge derivative adjusted, a slight change of ϵ_d from the computed value of -0.338730 a.u. to -0.398730 a.u. is needed to ensure the smooth curvature of the repulsive potentials.

While the adjusted Hubbard parameters lead to satisfactory results for Ni(I) compounds, we find the same parameters do not describe Ni(II) compounds with the same level of accuracy; this is the first clear indication that the average treatment of intra- d interactions in the current DFTB3 model is inadequate for the two unpaired electrons in the d^8 configuration of Ni(II). To improve the performance with minimal variation in the model, we modify the Hubbard charge derivative for Ni(II), while the Hubbard parameters and their charge derivatives for s and p shells remain the same for both Ni(I) and Ni(II); the charge derivative U_d^d is shifted to a lower value of -0.210000 for Ni(II) from -0.139760 for Ni(I).

Previously, it was reported that the Hubbard derivatives do not significantly alter most properties and can be fitted in the last step of parametrization⁵⁰; for open-shell systems that feature multiple unpaired d electrons, this statement may not be accurate and a proper choice of the Hubbard derivatives proved paramount to the current nickel parametrization (see below).

The values of r_{sp}^{wf} and r_d^{wf} are chosen so that the geometrical properties are well reproduced, specifically angles of tetra- and hexa-coordinated complexes. It is observed that r^{dens} greatly influences nickel-ligand bond lengths, and good agreement with the reference (B3LYP/aug-cc-pVTZ) is achieved when r^{dens} is increased beyond a critical value. Thus r^{dens} is set to a fairly large value, as in the previous parametrization of Ni by Zheng et al.⁴⁷, and in the Mg parametrization⁵⁰ where the value was set to 14.0 bohr.

3.2 Repulsive Parameters

The repulsive energy is written as the sum of pair-wise repulsive potentials V_{ab}^{rep} :

$$E^{rep} = \frac{1}{2} \sum_{ab} V_{ab}^{rep}[\rho_a^0, \rho_b^0, r_{ab}]. \quad (6)$$

For two atoms a and b , the repulsive potential is calculated by subtracting the DFTB electronic energy E^{el} from the total energy of reference systems calculated with B3LYP/aug-cc-pVTZ at different interatomic distances,³⁷

$$V_{ab}^{rep}(r_{ab}) = \{E^{ref}(r_{ab}) - E^{el}(r_{ab})\}_{reference\ system}. \quad (7)$$

The repulsive potentials are fitted against reference geometries and energies employing the *erepfit* program (an in-house developed program). The parameters defining the repulsive potentials are given in Table S2.

The Ni-Ni repulsive potential is fitted against a Ni(I)-Ni(I) geometry with $r(\text{Ni-Ni})$ set to 2.22 Å, which is the average $r(\text{Ni-Ni})$ from Ni(I)-Ni(I) and Ni(I)-Ni(II) geometries, both obtained with the B3LYP/aug-cc-pVTZ level of theory. All reference geometries and potential energy differences are based on Ni(I) compounds, except for $[\text{Ni}(\text{H}_2\text{O})_6]^{2+}$ and $[\text{Ni}(\text{NH}_3)_6]^{2+}$ which are introduced in order to adjust the treatment of highly coordinated nickel complexes. The division points are chosen in a way that best reproduces energetic properties, as even a small change of division points could lead to substantial differences in sequential BDEs. Graph of the nickel-oxygen repulsive potential as a function of distance, as well as its first and second derivative is given in Figure 3, while all other Ni-X repulsive potentials are included in the Supplementary information (Figure S1).

4 Results and discussion

The parameterized DFTB3/3OB model for nickel is evaluated using structures from the Cambridge Structural Database (CSD). Additionally, the model is tested on a range of Ni(I) and Ni(II) complexes for a series of structural and energetic properties; comparison is made to both B3LYP/aug-cc-pVTZ and DFT (B3LYP or PBE)/6-31+G(d) levels of theory. Two different test sets are used and discussed below: the standard test set – comprising mostly of simple ligands, some of which are used for the parameterization; the diverse test set, which comprises of more complex ligands of biological relevance. Since nitrogen hybridization

remains a problem for the current monopole-based DFTB3/3OB model, for all calculations involving nitrogen atoms, the “NHmod” repulsive potential is used; this impacts mostly on ligand proton affinities⁵¹. Since all tested molecules are small the dispersion correction has not been included in either DFTB or DFT calculations. For Ni(I) compounds, there is no ambiguity in the spin state; for Ni(II) compounds, the triplet state is mainly studied in both DFTB3/3OB and DFT calculations, except for the square-planar structures, for which singlet is expected to be more stable. The splitting between singlet and triplet spin states is briefly discussed below; detailed energetics are summarized in the excel spreadsheet in the Supplementary Information. For comparison, the xTB model of Grimme and co-workers⁵⁶ has also been tested for selected systems.

4.1 Benchmark calculations

4.1.1 Comparison to CSD structures—Several structures from the CSD database (Figure 4) are used to compare DFTB3 and B3LYP/6–31+G(d) optimized geometries. These compounds are chosen based on the previous work of Hocking et al.,¹² who examined the applicability of DFT methods to coordination compounds. Root mean square deviations (RMSD) are calculated with the VMD program⁸⁸ and include all atoms (Table 2); errors in bond lengths of the first coordination sphere are also summarized in Table 2, with the original data listed in Table S3.

It is evident from Tables 2 and S3 that DFTB3 geometries are generally in good agreement with the X-ray structures. In fact, for most compounds considered here, DFTB3 outperforms B3LYP/6–31+G(d), albeit the difference is small; the MAD for Ni-O/Ni-N distances is 0.06/0.08 Å for DFTB3 and 0.11/0.14 Å for B3LYP. In the case of AMENIP and ENIACH, rather large structural distortions are observed in the B3LYP calculations, while no such large deviation is observed in the DFTB3 calculations. As shown in Table 2, the xTB model⁵⁶ gives very similar results as DFTB3/3OB, with only slightly larger MAD values for Ni-O and Ni-N distances.

4.1.2 Geometries of the Standard and Diverse Test sets—The bond lengths and angles of all structures in the Standard and Diverse test sets are summarized in Tables S4 and S5, respectively; the errors for bond lengths and angles are summarized in Table 3, which also compares the performance of DFTB3/3OB and PBE/6–31+G(d) calculations. Since DFTB3 is parameterized using PBE, including the PBE comparison below helps identify whether certain errors observed for DFTB3 are due to the use of that exchange-correlation functional or to other approximations specific to DFTB3.

Once r^{dens} is properly adjusted, DFTB3 generally gives a decent description of the geometries in comparison to the reference (B3LYP/aug-cc-pVTZ) structures. For both the standard and diverse tests sets, the MAD value for Ni-ligand distance is about 0.04–0.06 Å, regardless of Ni(I) and Ni(II), which is comparable to the quality of PBE/6–31+G(d); for ligand-Ni-ligand bond angles, the MAD is in the range of 5–7 degrees for DFTB3, slightly larger than the value of 4–5 degrees at the PBE /6-31+G(d) level. As shown in Figure 5, DFTB3/3OB successfully captures the difference in structure between Ni(I) and Ni(II) compounds, including the expected Jahn-Teller distortions. For example, as indicated in

Figures 1–2, with three ligands, Ni(I) is expected to deviate from the symmetric triangular structure, while no such distortion is expected for Ni(II); as shown in Figure 5a, this is well captured at both DFTB3/3OB and B3LYP/aug-cc-pVTZ levels for water ligand. Similarly, with four ligands, tetrahedral structures are expected to undergo distortion for both Ni(I) and Ni(II); this is observed consistently for both DFTB3/3OB and B3LYP/aug-cc-pVTZ for ammonia and hydrogen sulfide ligands (see Figure 5b-c), although the magnitude of distortion is slightly underestimated for $[\text{Ni}(\text{H}_2\text{S})_4]^{2+}$ at the DFTB3/3OB level. The xTB⁵⁶ results are generally similar to DFTB3/3OB, with the Ni-N distances in better agreement with B3LYP references; the xTB model also qualitatively captures Jahn-Teller distortions, although the magnitude is overestimated in the case of $[\text{Ni}(\text{NH}_3)_4]^{2+}$ (Figure 5b).

We do observe, however, cases that exhibit substantially larger differences between DFTB3 and B3LYP, as reflected by the maximum deviations in ligand-Ni-ligand angles summarized in Table 3. Some of the examples are illustrated in Figures 6 and 7, for the standard and diverse test sets, respectively. For example, the Ni...H interaction appears to be overestimated in the current parameterization (see additional discussion in Supplementary Information). As a result, for a number of structures, especially those feature small anionic ligands such as OH^- , the orientation of the ligand is distorted due to artificially strong Ni...H interactions (Figure 6a); the largest impact on the structure is observed for $[\text{Ni}(\text{H}_2\text{S})_5]^{2+}$, for which B3LYP predicts a square pyramidal structure while DFTB3/3OB predicts a trigonal bipyramidal structure with two equatorial H_2S molecules significantly distorted due to artificially strong Ni...H interactions (Figure 6c). As another example, $[\text{Ni}(\text{CO})_3]^{2+}$ deviates from a symmetrical triangular structure at the B3LYP level, while no distortion is observed at the DFTB3 level (Figure 6b); as shown in Table S4, PBE/6–31+G(d) also predicts a non-symmetrical structure, thus the error in DFTB3, in this case, is not due to the exchange-correlation functional used in the model.

It should be noted, however, that B3LYP is not optimal in all cases either. For example, $[\text{Ni}(\text{CO})_3]^{2+}$ is expected to remain symmetrical (Figure 2), as found in DFTB3 calculations, yet B3LYP gives a distorted structure (Figure 6b). By contrast, $[\text{Ni}(\text{CO})_3]^+$ is expected to deviate from the symmetrical triangular structure due to Jahn-Teller distortion (Figure 1), B3LYP/aug-cc-pVTZ predicts a highly symmetrical structure; the distortion, however, is captured at both DFTB3/3OB and PBE/6–31+G(d,p) levels (Table S4). Therefore, the functional dependence of DFT results for transition metal ions¹⁷ should always be kept in mind.

In the diverse set, the largest differences between DFTB3/3OB and B3LYP are observed for the structures illustrated in Figure 7. For $[\text{Ni}(\text{NC})_4]^{3-}$ the deviation from tetrahedron is modest at the B3LYP level, while the structure is almost planar with DFTB3/3OB; for $[\text{Ni}(\text{NC})_4]^{2-}$ the deviation from tetrahedron is also exaggerated at the DFTB3 level (Figure 7a). For the complex with ethylenediamine, while DFTB3/3OB and B3LYP are consistent for the Ni(I) compound, the two ethylenediamines are out-of-plane at the DFTB3/3OB level for the Ni(II) compound (Figure 7b). For the compound with two formaldehydes, DFTB3/3OB predicts a more bent coordination for both Ni(I) and Ni(II) cases (Figure 7c). In all these examples, the errors for PBE/6–31+G(d) are substantially smaller (see Table S5), thus the exchange-correlation functional used for DFTB3/3OB is not to blame here.

As discussed below, these larger structural deviations lead to larger errors in single point ligand binding energy calculations at the B3LYP//DFTB3 level, as compared to our observations for copper compounds.⁵³ As also shown in Figures 6–7, xTB also tends to have notable errors for most of these cases, and the magnitude of error can be either larger or smaller than that for DFTB3/3OB. Therefore, these problematic cases likely reflect the intrinsic limitations of the tight binding Hamiltonian employed in both models.

4.1.3 Sequential Bond Dissociation Energies—The sequential bond dissociation energies (sBDE) computed with DFTB3/3OB and various DFT methods for complexes in the standard and diverse test sets are presented in Tables S6 to S8; as a further evaluation of the DFTB3 structures, single point B3LYP/aug-cc-pVTZ calculations are also conducted and summarized in the tables. The errors are summarized in Table 4.

For Ni(I) complexes in the standard test set (Table S6) with neutral ligands, the MAD for the sBDE is 6.3 kcal/mol, which is slightly lower than the value of 8.8 kcal/mol for PBE/6–31+G(d); the errors are substantially larger for charged ligands, with a MAD value of 22.4 kcal/mol for DFTB3/3OB and 11.8 kcal/mol for PBE/6–31+G(d). As discussed in the previous study⁵³ of copper compounds, the larger errors for the charged ligands reflect the minimal basis nature of DFTB3; indeed, the error (MAD) decreases drastically to 3.7 kcal/mol for single point B3LYP/aug-cc-pVTZ calculations at DFTB3/3OB structures for the charged ligands. Nevertheless, it is worth noting that the errors for the single point calculations remain substantially larger for the Ni(I) compounds (MAD in the range of 4 kcal/mol for neutral and charged ligands) than for the copper compounds, for which the single point MAD is about 1 kcal/mol, even for Cu(II) compounds.⁵³ This difference reflects the significant errors in several nickel structures as discussed in the last subsection. For example, large errors are observed for water and hydroxide ligands, even with single point energy calculations; this is because the overestimated Ni...H interaction distorts the orientation of these ligands (e.g., see Figure 6a). The large error associated with $[\text{Ni}(\text{CO})_4]^+$ is due in part to the fact that, as discussed above, B3LYP and DFTB3 predict different structures for $[\text{Ni}(\text{CO})_3]^+$.

For Ni(II) compounds (Table S7), the MAD is slightly larger than Ni(I), although this is only after adjusting the charge derivative of *d* shell Hubbard parameter U_d to a lower value, highlighting the challenging nature of nickel relative to copper for the current DFTB3 model. Indeed, even with the adjusted Hubbard charge derivative, the MAD for Ni(II) with charged ligands (26.8 kcal/mol) is substantially higher than that for Cu(II) with charged ligands (with a MAD of 14.0 kcal/mol⁵³). Again, single point B3LYP/aug-cc-pVTZ calculations at DFTB3/3OB structures generally reduces the errors, especially for charged ligands, the MAD remains significant due to the structural distortions discussed above, especially for hydroxide ligands and $[\text{Ni}(\text{H}_2\text{S})_5]^{2+}$ shown in Figure 7. For $[\text{Ni}(\text{NH}_3)_6]^{2+}$, the single point error is rather large (–22.2 kcal/mol), not because the relevant structures are distorted but because the Ni...N distances are consistently underestimated by about 0.1 Å (see Figure 5b for example).

For the diverse test set (see Table S8), the basic trends follow those for the standard test set; the errors at the DFTB3/3OB and PBE/6–31+G(d) levels are comparable, and the errors are

slightly larger for Ni(II) than for Ni(I). Single point energy calculations at DFTB3 structures reduce the errors significantly, leading to MADs in the range of 3–4 kcal/mol. Nevertheless, large errors are observed in several cases for which DFTB3 and B3LYP structures are substantially different (see Figure 7).

4.1.4 Ligand Proton Affinities—The ligand proton affinities for various compounds in the standard test set are calculated using DFTB3/3OB and compared to DFT calculations (Table S9). Within the DFTB3 formalism the proton affinities (E^{PA}) are calculated as follows

$$E^{PA} = E^{A^-} + E^{H^+} + E^{AH} \quad (8)$$

in which E^{H^+} is the energy of proton, and E^{AH} and E^{A^-} are the energies of the protonated and deprotonated species, respectively. Note that due to the density expansion nature of DFTB, the energy of a proton is not zero.⁹⁹

The DFTB3 results are in fair agreement with the B3LYP reference values, and the MAD values are considerably smaller than PBE/6–31+G(d); it is well-established that proton affinity is sensitive to the inclusion of polarization functions on the hydrogen atoms. A closer inspection of the results in Tables S9 reveals that the large MAD value for Ni (I) complexes is due mainly to phosphorus containing complexes, and for Ni(II) the same holds for nitrogen compounds. Overall, the performance is comparable to the previous results for copper ligands (the RMSDs for Cu(I) and Cu(II) are 6.0 and 5.7 kcal/mol, respectively).⁵³ Again, one difference is that the errors do not reduce with single point energy calculations for nickel compounds, while the errors reduce to a MAD around 1 kcal/mol for copper compounds.⁵³ This is largely because of the overestimated Ni...H interaction noted above, which are particularly severe for structures with deprotonated ligands (e.g., OH⁻ vs. H₂O as ligand). Thus systematically improving Ni...H interaction is essential for reducing errors in proton affinities (see discussions in Supplementary Information).

4.1.5 Electronic Structure—It is well established in coordination chemistry that depending on the ligand environment, *d* orbitals split in specific ways upon descent in symmetry. For octahedral (O_h) Ni(II) complexes, the electronic configuration is (t_{2g})⁶(e_g)². This splitting is well reproduced by our orbital angular momentum resolved DFTB3 model, although the ligand field splitting is overestimated (Figure 8), and this is noted for all structures under investigation to different extent.

More importantly, for complexes with coordination number 4, two distinct geometries can be observed: square planar and tetrahedral. In the former case, electronic configuration reads as: (e_g)⁴(a_{1g})²(b_{2g})²(b_{1g})⁰, giving ¹A_{1g} as the ground state in the D_{4h} symmetry. Tetrahedral nickel(II) complexes have an electronic configuration of (e)⁴(t₂)⁴, giving ³T₁ state as the ground state, which is subject to the Jahn-Teller distortion; this is the T ⊗ e Jahn-Teller effect, which although weak, can be noticed by angular distortion leading to the D_{2d} geometry. Other examples are summarized in Figures 1–2. Encouragingly, the DFTB3 calculations properly capture Jahn-Teller distortions in all tetrahedral complexes as reflected by the L-Ni-L angles (e.g., see Figure 5), although the magnitude of distortion can be

different from B3LYP results (e.g., see Figure 7). For the case of three ligands, DFTB3 follows the expectation for most cases, even when B3LYP does not, as discussed above for $[\text{Ni}(\text{CO})_3]^+$ and $[\text{Ni}(\text{CO})_3]^{2+}$.

The fact that Jahn-Teller distortion is captured in DFTB3 (also noted in previous studies of copper¹¹) is consistent with the observation that qualitative splitting of d orbitals is described by the model, suggesting that metal-ligand matrix elements computed for the parameterization are reliable. We note, however, that with the current spin-polarization model (Eq. 5), it is difficult to reliably describe the order of spin states, even for Ni(II), which has a d^8 configuration. This is because the spin-polarization term employed here does not depend on the magnetic quantum number and involves only the spin population of the entire d shell (p_l in Eq. 5). Indeed, with the computed spin coupling $\left(W_{l' a'}\right)$ values, the singlet-triplet splittings are very different from the B3LYP and PBE values (see the excel spreadsheet in Supplementary Information). Simple adjustments in the spin coupling parameters (e.g., by matching singlet-triplet splitting in Ni^{2+} at the B3LYP/aug-cc-pVTZ level) leads to considerable improvements but not a transferable model. Since we focus entirely on the triplet states (except for square planar structure) for Ni(II) compounds in this study, we have not pursued an extensive effort in refining the spin coupling parameters. Instead, we leave the improvement of spin states as important future work, which necessarily involves an explicit treatment of metal d orbitals with m_l dependent d - d interactions.

4.1.6. Active site models for nickel enzymes—Finally, we test the DFTB3/3OB model using several active site models for nickel enzymes, selected based on a recent review that discussed the structure and mechanism of nickel-dependent enzymes.⁶¹ Due to the size of the models, the reference is taken to be B3LYP with a modest basis set, which includes LanL2dz effective core potential and the associated basis set for Ni,¹⁰¹ and 6-31+G(d,p) for the other elements. As shown in Figure 9, the DFTB3/3OB structures are largely consistent with the B3LYP structures, with a RMSD value ranging from 0.11 to about 0.5 Å. The deviations are due mainly to the overestimated Ni...H interactions, which distort the orientation of small molecule ligands such as H_2O (e.g., in Figure 9c-d). It is encouraging that the current DFTB3 model appears to work well, at least for structures, for even a Ni(III) case (Figure 9b for Ni-containing superoxide dismutase) and a bi-metallic case (Figure 9d for urease), although more stringent tests would involve molecular dynamics simulations in a QM/MM framework, as was done for copper proteins;¹¹ this is left for future work.

5 Concluding Remarks

DFTB3 has shown promise in treating simple metal ions such as Mg^{2+} and Zn^{2+} with more favorable computational efficiency than DFT,^{50, 53} making it attractive for the study of condensed phase systems. Since DFTB innately bears the principles of DFT, it is potentially better suited for the treatment of transition metals than other semi-empirical techniques, such as the traditional NDDO methods. Indeed, l -resolved DFTB3 was found to provide encouraging results for copper,^{11, 53} which has d^{10}/d^9 configuration depending on the oxidation state. Here we explore the applicability and limitation of the current DFTB3

model for treating more complex transition metal ions by conducting parametrization for nickel (I) and nickel (II).

Overall, the results for nickel are largely in line with previous findings for copper.⁵³ Geometries are in general in favorable agreement with available X-ray structures and B3LYP/aug-cc-pVTZ calculations, although we are aware that this level of theory may not be the best choice for structures of transition metals; it was chosen as the reference here so that the DFTB3 nickel model is consistent with the 3OB parameterization for other elements reported so far. It is encouraging that Jahn-Teller distortion expected for three- and four-ligand cases is captured in most Ni(I) and Ni(II) compounds, although the magnitude of distortion is not always perfectly reproduced; this is consistent with the finding that *d* orbital splitting is qualitatively reproduced, although the result is often not quantitative. For the selected cases studied here, the xTB model of Grimme et al.⁵⁶ also gives reliable structures, although the degree of Jahn-Teller distortion is also not always quantitatively reproduced. Considering that only three Ni-containing compounds were included in the parameterization, the performance of xTB model is satisfying, further suggesting that the DFTB framework is adequate to describe many key structural features.

It is observed that ligand binding energies and geometries are better reproduced for more covalent type complexes, such as those with carbon or sulfur in the first coordination sphere. DFTB3 treatment of charged ligands, especially for ligand binding energies, has considerable errors with MAD in the range of 20 kcal/mol; this is consistent with previous findings for copper and reflects the current limitations imposed by the use of a minimal basis set for treating transition metals and their interaction with highly polarizable ligands⁵³.

There are several distinct differences in the nickel parameterization compared to previous work on copper. First, we find that it is necessary to use different charge derivatives for the Hubbard parameter for the *d* shell of Ni(I) and Ni(II) cases, while a single charge derivative of the *d*-shell Hubbard parameter was found adequate for both oxidation states of copper.⁵³ Moreover, although single point B3LYP calculations at DFTB3 structures often reduce the error in ligand binding energies, especially for charged ligands, the error remains substantial (MAD of 3–4 and up to ~7 kcal/mol in contrast to the MAD of 1–2 kcal/mol observed for copper⁵³) for many cases, reflecting that notable deficiencies exist in the structure. Some of the structural errors are due to overestimated Ni...H interactions most visible for small ligands such as water and hydroxide, while other types of structural distortions are also observed; in some cases, similar deviations are also observed with PBE/6–31+G(d) calculations, although many structural errors are unique to DFTB3, suggesting that the use of PBE as the exchange-correlation functional is not the main origin. Finally, with the computed spin coupling parameters based on atomic calculations, the current DFTB3 model has large errors in the singlet/triplet splitting of Ni(II) compounds, similar to previous parameterization of DFTB2 for transition metals.⁴⁷ These challenges clearly highlight the higher level of complexity in the electronic structure of nickel as compared to copper, which has either a full *d* shell or a single hole (*d*⁹). An explicit treatment of the interactions among the electrons in different *d* orbitals, thus going beyond the averaged interaction over each *t*-shell in the current DFTB3 model, is required to overcome these fundamental limitations and make the DFTB approach applicable to treat first row transition metal ions with open *d*-

shells. Nevertheless, the observation that many key properties of nickel compounds, such as Jahn-Teller distortions, have been captured already with the current DFTB3 model indicates that further efforts are clearly worthwhile.

Finally, we note that, similar to previous developments of 3OB parameters for DFTB3, we have limited ourselves to molecular species. An important topic of study is to understand the transferability of the DFTB3 model to solid state systems, in terms of both physical and chemical properties. While DFTB3/3OB has been applied to examine lattice energies of organic molecules,^{102–103} electronic properties such as band structures have not been studied systematically.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

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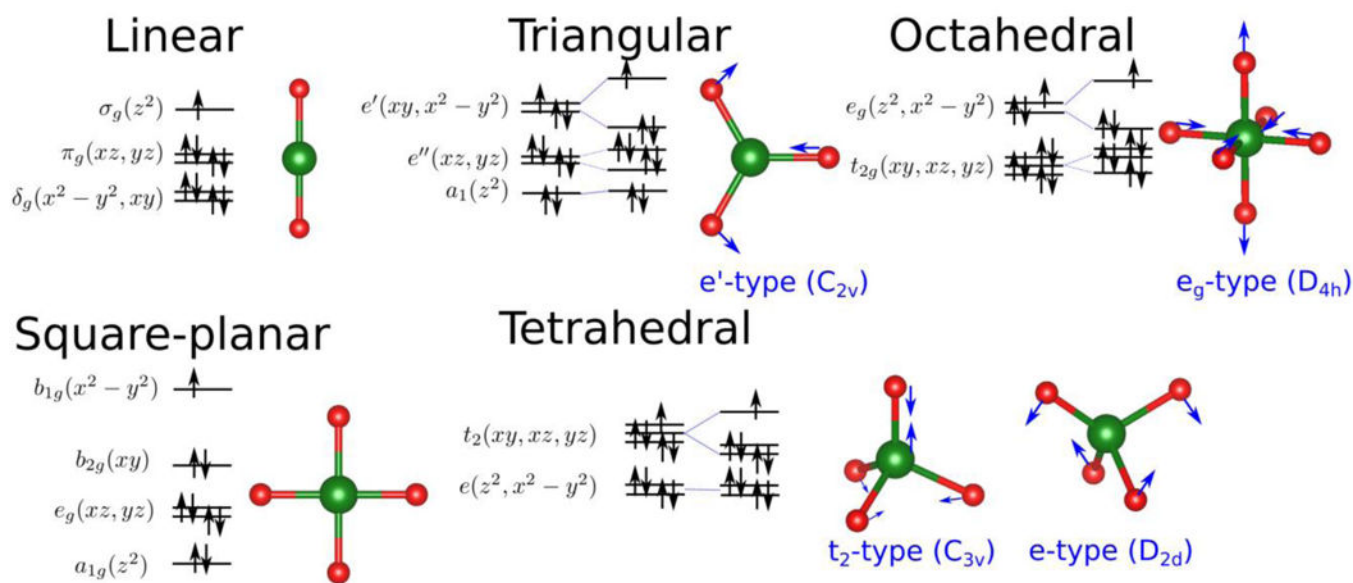


Figure 1. Expected electronic configuration and Jahn-Teller distortions for Ni(I) ions displaying a d^9 configuration under different coordinations.

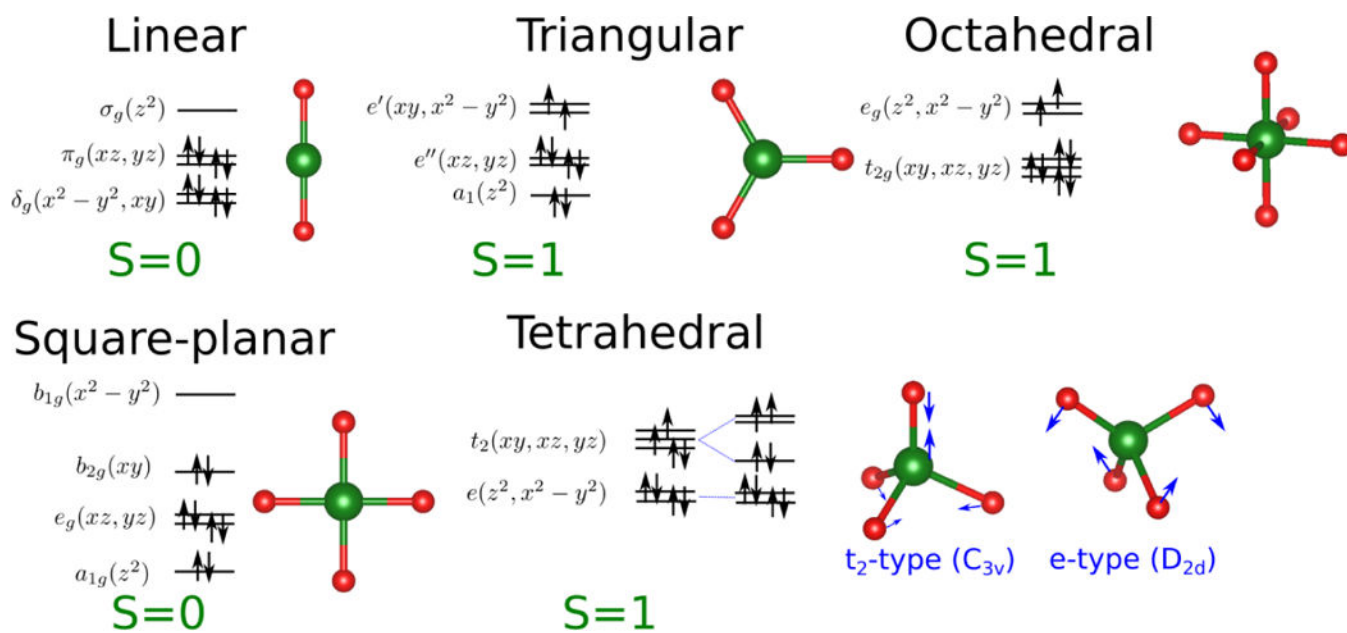


Figure 2. Expected electronic configuration, total spin and Jahn-Teller distortions for Ni(II) ions displaying a d^8 configuration under different coordinations.

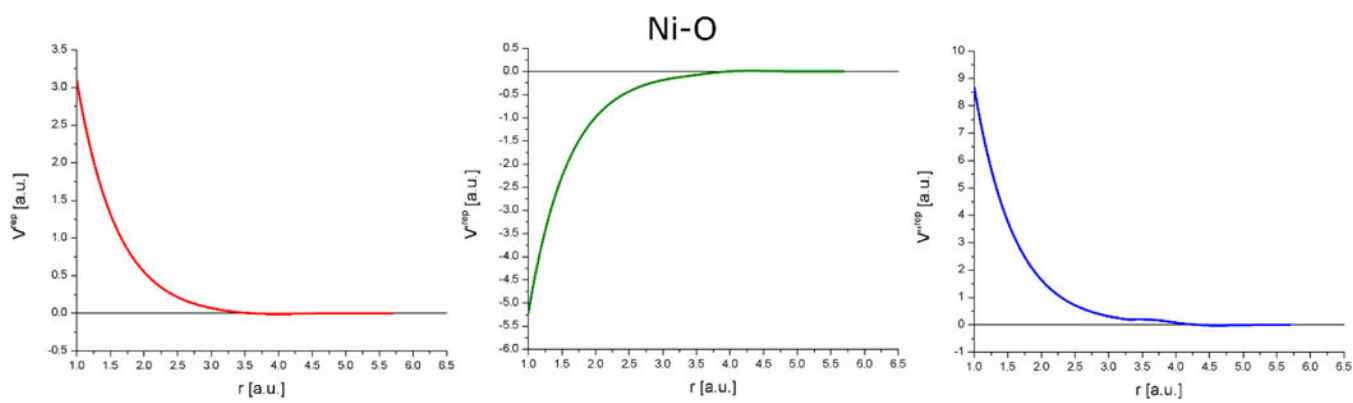


Figure 3. Illustration of Repulsive potential for Ni-O, as well as its first and second derivative as a function of distance.

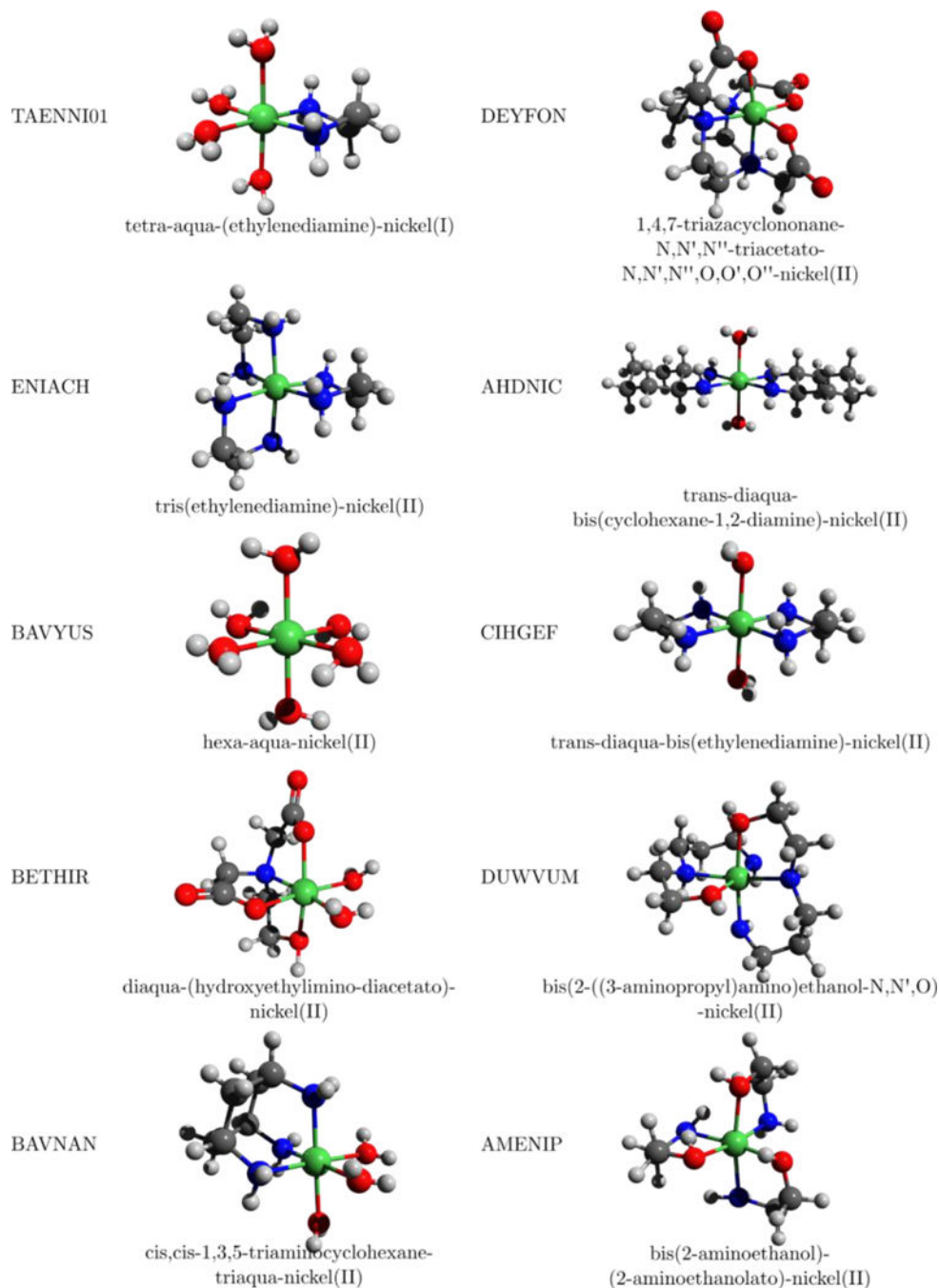
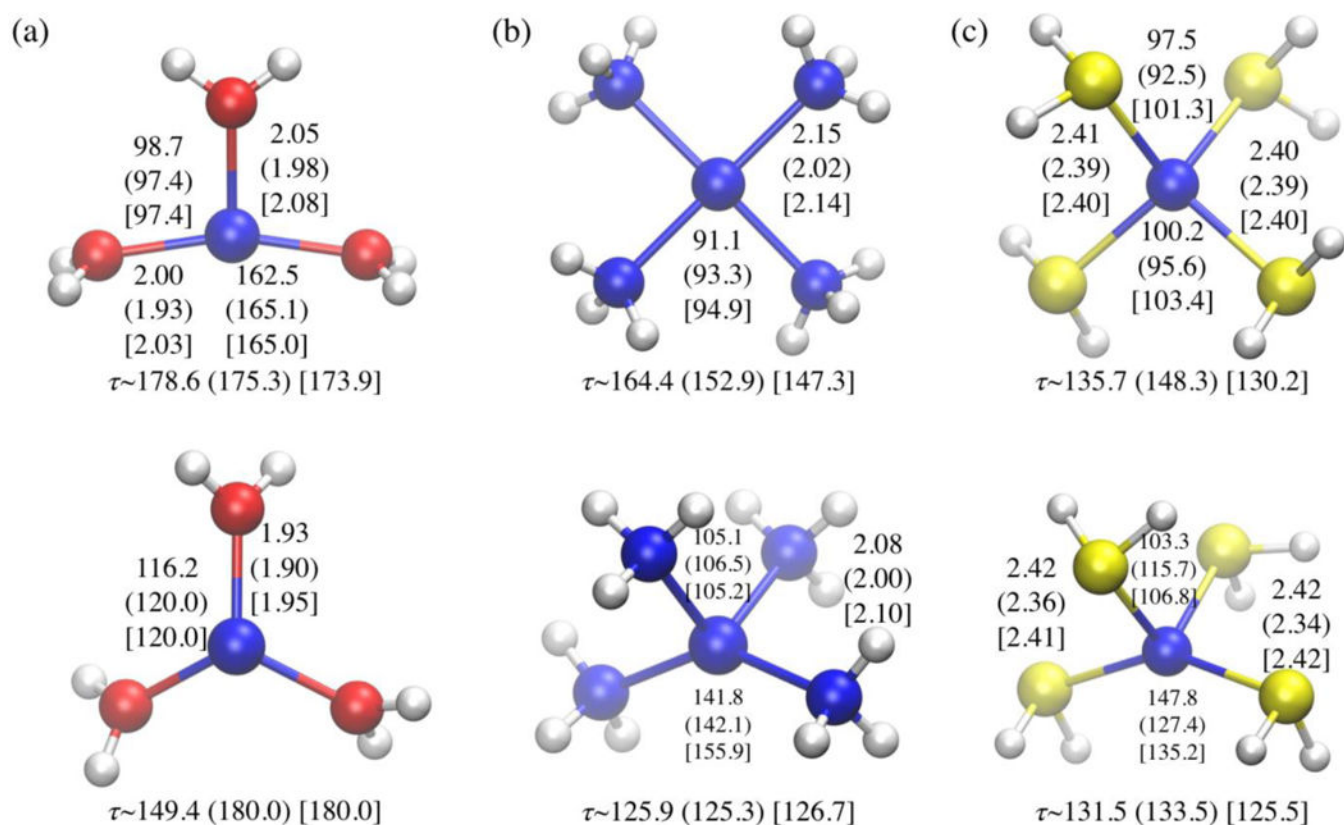
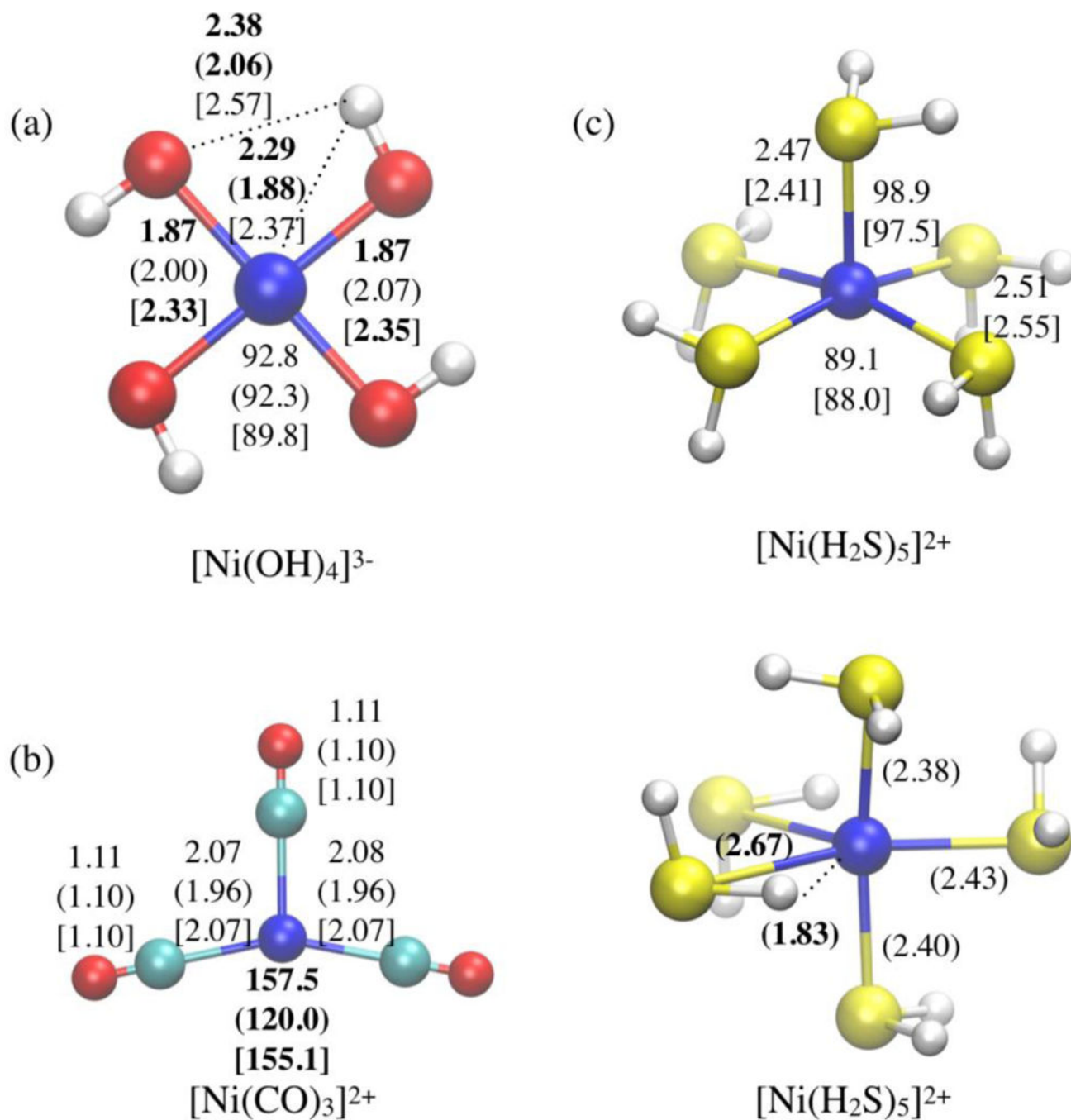


Figure 4. Graphical representation of X ray structures found in within CSD. Color scheme: nickel-green, nitrogen-blue, oxygen-red, carbon-black.

**Figure 5.**

Examples for structures in the standard test set (with water, ammonia and hydrogen sulfide as the ligands); for each panel, the top structure is for Ni(I), and the bottom for Ni(II). Numbers (distances in Å and angles in degrees) without parentheses are the reference value at the B3LYP/aug-cc-pVTZ level; those with parentheses are DFTB3/3OB values; those with brackets are xTB⁵⁶ values. The τ is the L-L-Ni-L dihedral angle that characterizes how close is the structure to be planar ($\tau=180^\circ$) or tetradedral ($\tau=120^\circ$).

**Figure 6.**

Examples for structures in the standard test set that exhibit significant deviation between DFTB3/3OB and the reference (B3LYP/aug-cc-pVTZ) geometries. Geometrical parameters (distances in Å and angles in degrees) with significant deviations are highlighted in bold; numbers without and with parentheses are the B3LYP/aug-cc-pVTZ and DFTB3/3OB values, respectively; those with brackets are xTB⁵⁶ values.

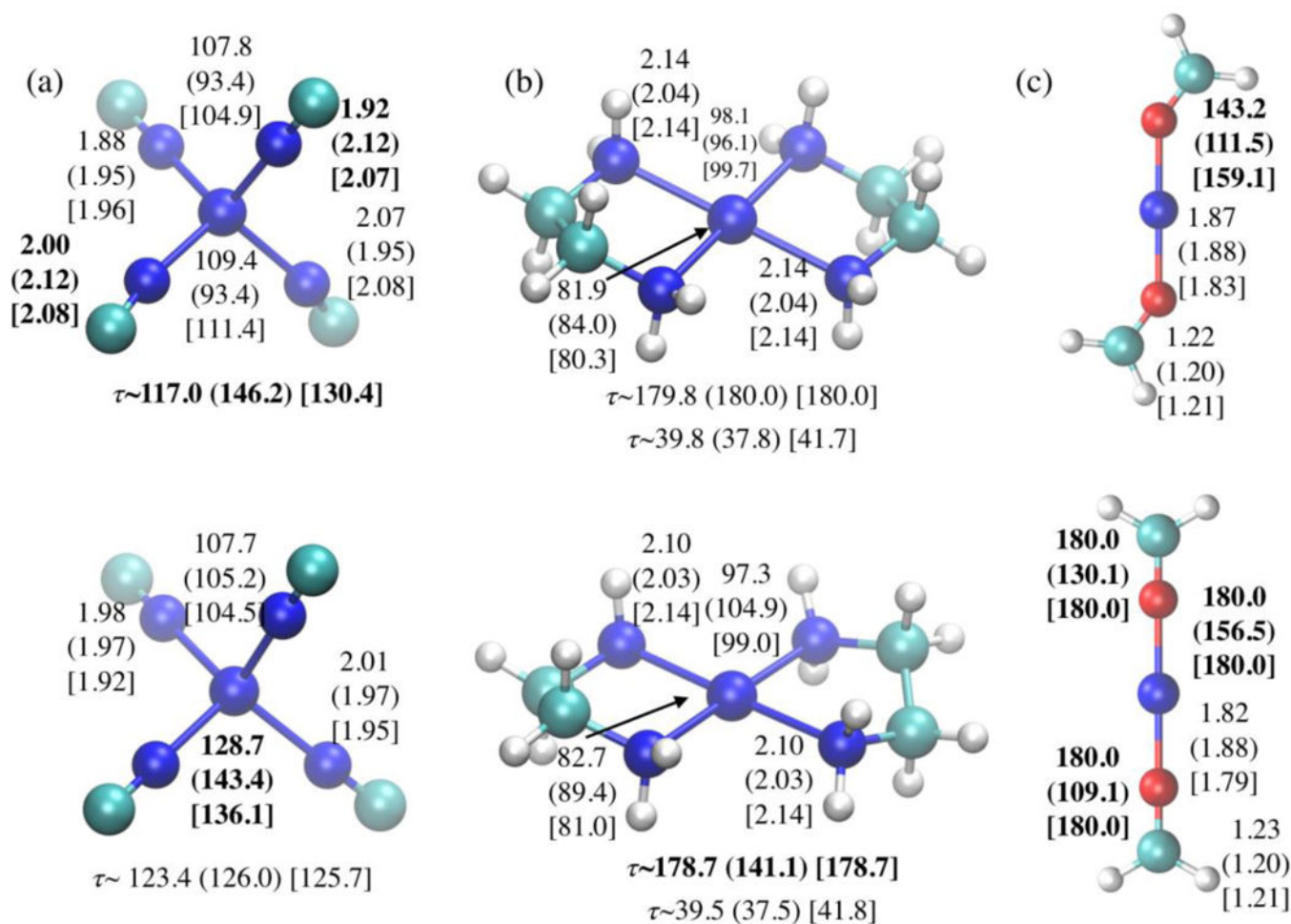


Figure 7. Examples for structures in the diverse test set that exhibit significant deviation between DFTB3/3OB and the reference (B3LYP/aug-cc-pVTZ) geometries. The ligands are CN^- , ethylenediamine (en)₂, and formaldehyde; for each panel, the top row is for Ni(I) and the bottom for Ni(II). Geometrical parameters (distances in Å and angles in degrees) with significant deviations are highlighted in bold; numbers without and with parentheses are the B3LYP/aug-cc-pVTZ and DFTB3/3OB values, respectively; those with brackets are xTB⁵⁶ values.

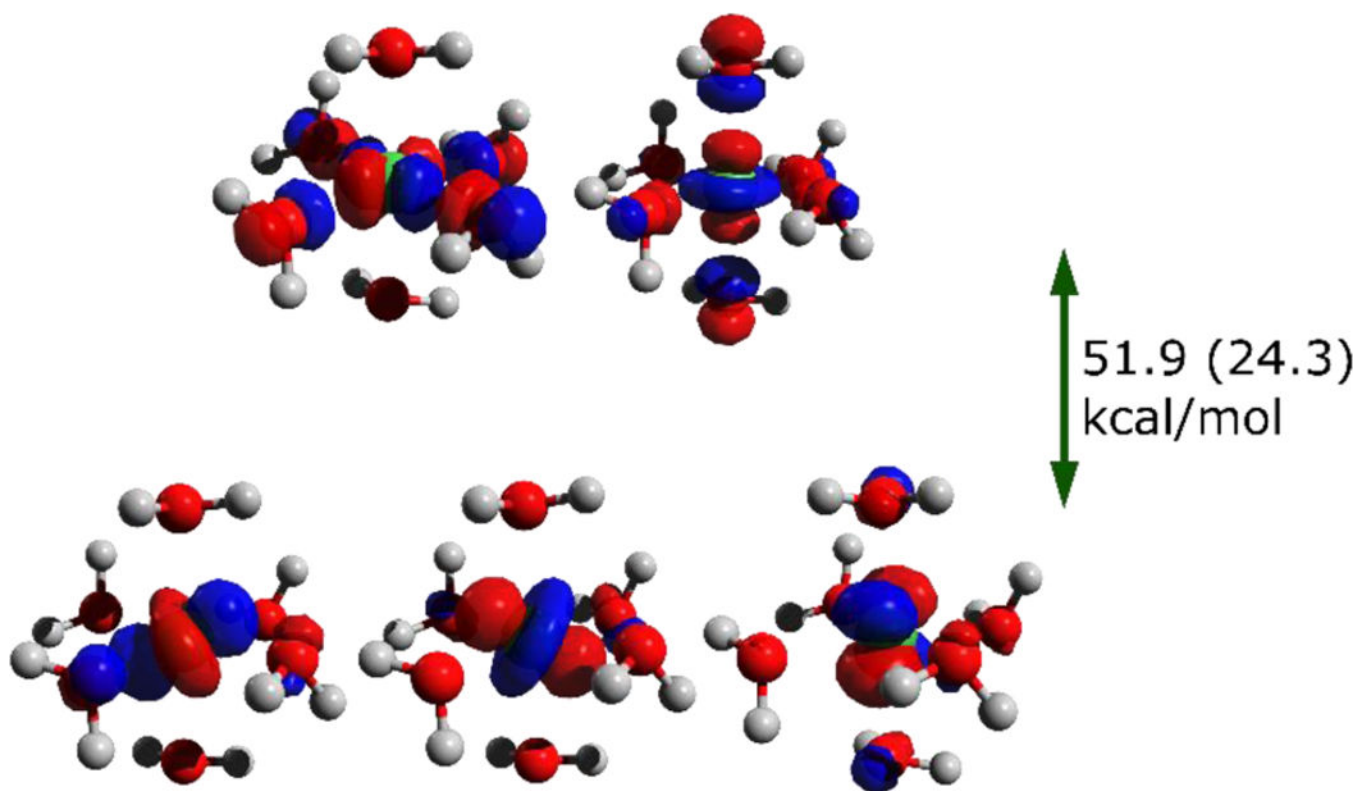


Figure 8.

An illustration of *d* orbital splitting in Ni ion with [Ni(H₂O)₆]²⁺ as an example. Contours of *d* orbitals (isovalue 0.06 a.u.) and the splitting between the *t*_{2g} and *e* sets computed with DFTB3/3OB are shown; the experimental value¹⁰⁰ is enclosed in parentheses.

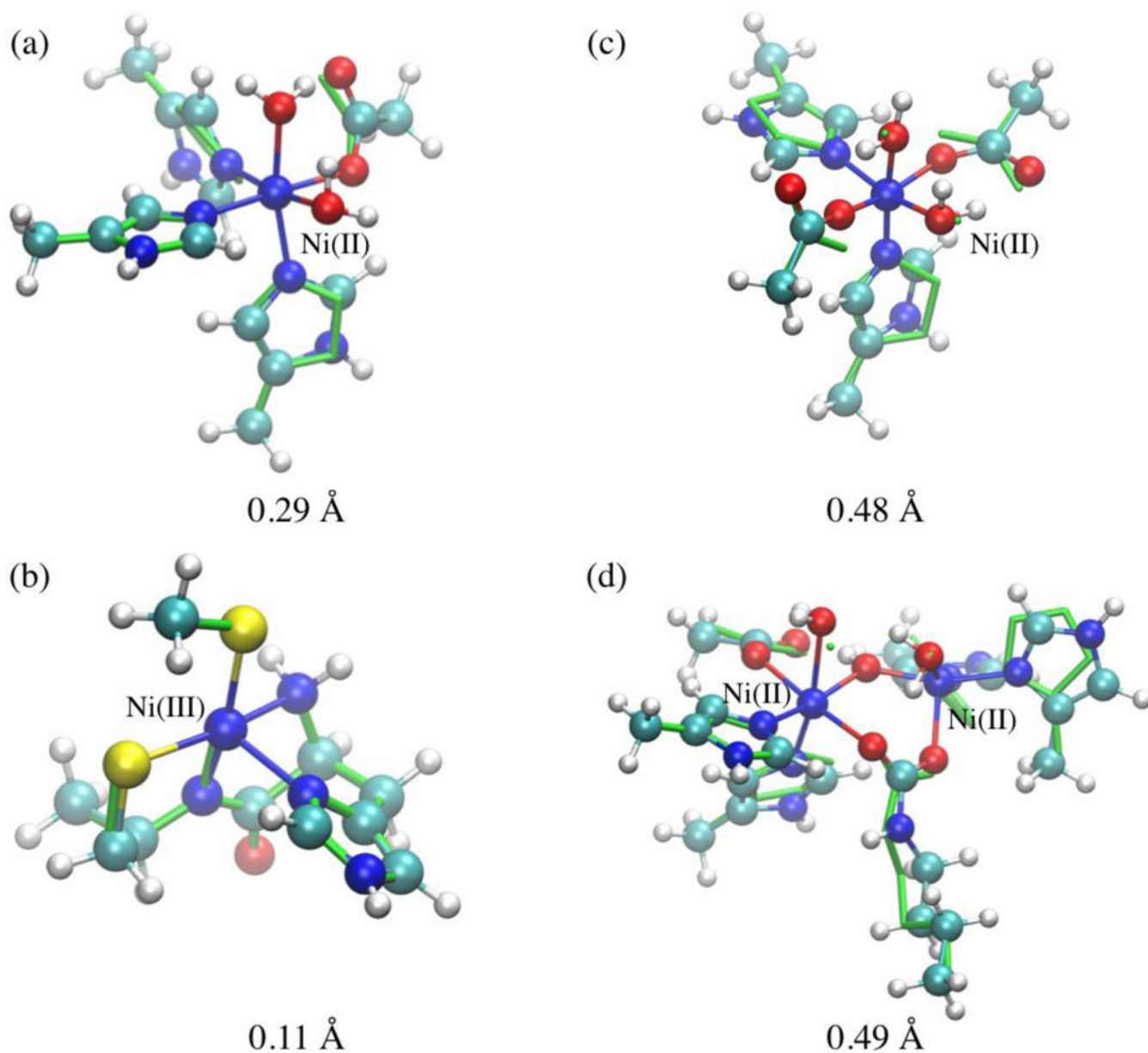


Figure 9. Superposition of optimized active site models for several nickel enzymes at the B3LYP and DFTB3/3OB levels. The B3LYP optimized structures are shown as CPK with atoms colored based on element type, and DFTB3 structures are shown in the line form in green. The RMSD value between the optimized structures (not including hydrogen atoms) is shown for each model. The formal oxidation state for Ni is Ni(II) for all cases, except for panel (b), which represents a model for Ni-containing superoxide dismutase (PDB code 1Q0D).

Table 1.

Overview of the Nickel electronic parameters (in atomic units if not dimensionless), with $\zeta=4.00$.^a

Parameter	Value
l_{max}	2
a_0	0.50
a_1	1.37
a_2	3.74
a_3	10.24
a_4	28.00
r_{sp}^{wf}	2.50
r_d^{wf}	5.20
r^{dens}	16.00
ϵ_s	-0.202977
ϵ_p^*	0.046000
ϵ_d^*	-0.398730
E^{pin}	-0.036536
U_s^*	0.158730
U_p^*	0.251943
U_d^*	0.370410
U_{sp}^d	-0.060288
Ni(I) U_d^{d*}	-0.139760
Ni(II) U_d^{d*}	-0.210000

^aValues with asterisk * are adjusted, the rest are calculated using the PBE functional.

Table 2.

Root Mean Square Deviations of geometry (in Å) and errors in Ni-ligand distances (in Å) at DFTB3 and B3LYP levels for 10 Ni-containing compounds in comparison to experimental X-ray geometries in the Cambridge Structural Database (see Figure 4).

CSD entry	DFTB3/3OB	B3LYP/6-31+G(d)	xTB ⁵⁶
TAENNI01 ⁸⁹	0.36	0.47	0.36
ENIACH ⁹⁰	0.33	0.59	0.22
BAVYUS ⁹¹	0.57	0.61	0.44
BETHIR ⁹²	0.47	0.39	0.53
BAVNAN ⁹³	0.29	0.35	0.24
DEYFON ⁹⁴	0.23	0.20	0.27
AHDNIC ⁹⁵	0.26	0.28	0.23
CIHGEF ⁹⁶	0.24	0.28	0.22
DUWVUM ⁹⁷	0.38	0.24	0.40
AMENIP ⁹⁸	0.47	0.80	0.50
Error in Ni-O/N distances (Å)			
MAD (Ni-O) ^a	0.06	0.11	0.10
MAX (Ni-O) ^a	0.25	1.00	0.24
MAD (Ni-N) ^a	0.08	0.14	0.10
MAX (Ni-N) ^a	0.27	0.81	0.24

^aFor here and rest of the text, MAD: Mean Absolute Deviation; MAX: Maximum Absolute Deviation. Only ligands directly coordinated to the nickel ion are considered.

Table 3.

Summary of errors in Ni-ligand distance and ligand-Ni-ligand angle at DFTB3 and PBE/6-31+G(d) levels in comparison to the reference data (B3LYP/aug-cc-pVTZ).^a

Dataset	Error	Ni-ligand distance (Å)			Ligand-Ni-ligand angle (degree)		
		N	PBE 6-31+G(d)	DFTB3/3OB	N	PBE 6-31+G(d)	DFTB3/3OB
Standard	MAD	103 (140)	0.06 (0.04)	0.06 (0.06)	96 (176)	5.1 (3.3)	5.5 (6.4)
	MAX		0.20 (0.14)	0.40 (0.23)		37.9 (71.1)	38.6 (42.3)
Diverse	MAD	51 (51)	0.06 (0.03)	0.04 (0.05)	44 (44)	3.9 (3.7)	7.4 (14.0)
	MAX		0.11 (0.05)	0.04 (0.20)		27.8 (27.9)	40.7 (75.1)

^a“N” is the number of bond distances and bond angles included for the error analysis; the numbers without parentheses are for Ni(I), and those with parentheses are for Ni(II). The reference structures are optimized at the B3LYP/aug-cc-pVTZ level.

Table 4.

Summary of errors in the sequential bond dissociation energies (sBDEs) and ligand proton affinities (PAs) of different benchmark datasets for Ni-containing compounds.^a

Dataset	Error	PBE/6-31+G(d)	DFTB3/3OB	B3LYP//DFTB3
<i>Standard set sBDE</i>				
Ni(I): neutral ligands	MAD	8.8	6.3	4.2
	MAX	16.2	14.1	13.6
Ni(I): charged ligands	MAD	11.8	22.4	3.7
	MAX	25.3	39.9	18.5
Ni(II): neutral ligands	MAD	8.4	6.5	8.7/6.2 ^b
	MAX	16.6	18.5	45.5/22.2 ^b
Ni(II): charged ligands	MAD	14.4	26.8	4.6
	MAX	27.4	52.5	16.4
<i>Diverse set sBDE</i>				
Ni(I) compounds	MAD	11.8	10.0	2.8
	MAX	22.3	32.3	11.3
Ni(II) compounds	MAD	13.9	13.1	4.4
	MAX	30.7	26.3	28.7
<i>Standard set PA</i>				
Ni(I) compounds	MAD	12.7	5.4	3.5
	MAX	17.9	21.4	8.9
Ni(II) compounds	MAD	13.4	8.2	7.0
	MAX	23.8	17.4	19.9

^aThe reference is B3LYP/aug-cc-PVTZ. All calculations are done for 0K without including zero point energy correction.

^bThe values after the slash exclude the extreme case of $[\text{Ni}(\text{H}_2\text{S})_5]^{2+}$, for which DFTB3/3OB predicts a very different structure (see Figure 6c).