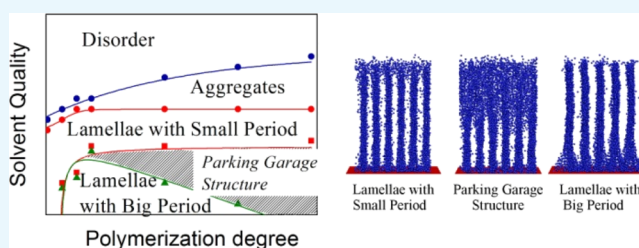


Lamellae—Parking Garage Structure—Lamellae Transition in Densely Grafted Layers of Amphiphilic Homopolymers: Impact of Polymerization Degree

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ABSTRACT: By means of computer modeling, the self-organization of densely grafted macromolecules with amphiphilic monomer units as a function of macromolecular polymerization degree and solvent quality was studied and a diagram of state was constructed. The diagram contains fields of disordered distribution of monomer units and of prolonged aggregates, regions of lamellae with small and big domain spacing, and transition region. Within the transition region, the lamellae with different spacing coexist: the lamellae with big domain spacing are on the top of the grafting layer and the lamellae with small domain spacing are close to the grafting surface. The lamellae are connected with each other and form bicontinuous parking garage structure joining all side groups into a single cluster. The domain spacing of lamellae does not depend on the macromolecular length, but the width of the transition region decreases with the decrease of polymerization degree until total vanishing at relatively short macromolecules. The sharp switch between lamellae and bicontinuous structure opens the perspective for practical applications of densely grafted layers with amphiphilic monomer units.



INTRODUCTION

The brush surfaces, decorated by responsive macromolecules, could change their properties on demand of external stimuli, and thereby they are able to control adhesion and wetting, to operate as sensors, to form a coating with changeable pattern, and so forth.^{1–3} Responsive brush surfaces occur in nature.^{3–5}

The self-assembly of grafted macromolecules is a complex process sensitive to many factors, among which are grafting density and solvent quality, architecture and chemical composition of macromolecules, availability of groups with different affinity to solvent and their relative content, interaction with substrate, and so forth.^{6–8}

In a good solvent with the increase of grafting density, the macromolecules undergo a smooth transition from coil to almost a fully stretched state.^{9,10} The macromolecules start to stretch perpendicular to the grafting surface when the distance d between grafting points becomes comparable with macromolecular radius of gyration, R_g . It is accepted that the grafting layer is in the so-called mushroom regime when the parameter of reduced grafting density $\Sigma = \pi \left(\frac{R_g}{d} \right)^2$ is less than unity: $\Sigma < 1$; in brush regime at $\Sigma > 5$; and in the intermediate regime when $1 < \Sigma < 5$.¹¹ The macromolecular size R_g and grafting density for mushroom–brush transition depend on the solvent quality. Also, in a poor solvent, the increase of grafting density causes a sequence of transformations: single globule—compacted micelles of few polymer chains—fused micelles or stripes—reverse micelles—homogeneous layer.^{12–16} The homogeneous layers are literally uniform. However, different macromolecules are unequally stretched perpendicular to the

substrate, and their free ends can be distributed over the whole layer.¹⁷ Such a distribution significantly increases the cumulative conformational entropy of grafted macromolecules and thus decreases the total elastic force acting on all grafted polymer chains.^{17–19}

Diblock copolymers could repeat the above-described sequencing of morphological transformation with the growth of grafting density in case of strongly incompatible blocks and solvent being selectively poor for internal, grafted to the substrate, blocks.^{20–28} In other cases (relative compatibility of blocks, strong hydrophilicity or explicit hydrophobicity of external blocks, and so forth), much more complex structures are observed. There could be micelles with one or few hydrophobic cores covered by hydrophilic monomers, structured stripes, and domains oriented perpendicular to the substrate.^{20–28} The latter structures are formed in nonselective solvents by external blocks bent inward. Depending on their relative lengths, the external blocks can join into semispherical, cylindrical, or layered domains. These domains are deepened to the matrix of internal blocks and have no contacts with the substrate. To stress this fact, ref 28 proposes to call them “golf holes”, “stalactites”, and “ridges and gullies”, correspondingly.

Grafted layers of amphiphilic homopolymers consisting the identical and amphiphilic monomers including both hydrophobic and hydrophilic groups were addressed in refs.^{29–31} The presence of groups having an affinity to different solvents

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implies surface activity of such monomer units^{32,33} accounted for by the dumbbell model of monomer units.³⁴ This model represents an amphiphilic monomer unit as two A and B beads linked with each other by covalent bonds. Some beads, for example, A, form a backbone and other beads, B, are pendants.³⁴ It was shown that such a model allows to describe the unique conformations adopted by macromolecules with amphiphilic monomer units in dilute and concentrated solutions,^{34–39} to reconstruct their specific ordering in the bulk^{40,41} and near interface.^{42–44} In selective solvent, amphiphilic homopolymers sparsely grafted onto a flat substrate can form an ultrathin coating having the width of about two monomer units.²⁹ Domains oriented perpendicularly to the substrate are observed in densely grafted amphiphilic homopolymers.^{30,31} Depending on the solvent selectivity, they can be strands of few macromolecules,^{30,31} lamellae with different periods, and parking garage structures,³¹ joining lamellae with different periods by screw ramps.

This article addresses the influence of macromolecular length on the structure formed in densely grafted layers of macromolecules with amphiphilic monomer units.

SIMULATION MODEL

The studied polymer brush is depicted in Figure 1. It comprises n identical macromolecules, each consisting of N

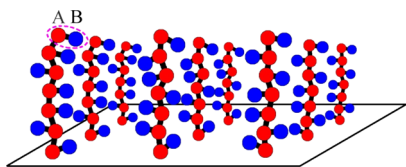


Figure 1. Schematic presentation of studied amphiphilic homopolymer brush.

amphiphilic monomer units. The amphiphilic monomer is represented as an *A-graft-B* dumbbell of two A and B beads linked together by a covalent bond. A beads form the polymer backbone, and B beads are side pendants. The macromolecules are tethered to the solid substrate through the fixation of A beads of the first monomer of each macromolecule in sites of square lattice with side d . The polymer brush is placed into the selective solvent being athermal for backbone A groups and poor for side B groups.

The calculations are performed at a coarse-grained level using the molecular dynamic technique with the LAMMPS software package⁴⁵ and resources of the Supercomputing Center of Lomonosov Moscow State University.⁴⁶

The excluded volume of beads is accounted for by the shifted and truncated repulsive branch of the 12–6 Lennard-Jones (Weeks–Chandler–Andersen) potential, E_v

$$E_v(r) = \begin{cases} 4\epsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 + \frac{1}{4} \right], & r \leq r_c = \sqrt{2}\sigma \\ 0, & r > r_c = \sqrt{2}\sigma \end{cases} \quad (1)$$

where r is the distance between two particles; σ refers to the bead diameter; and ϵ defines the strength of the interaction in units of temperature $k_B T$ (k_B is the Boltzmann's constant). We take the diameter $\sigma \equiv 1$ as the unit of length, the energy $\epsilon \equiv 1$ as the unit of energy, and subsequent results are presented in terms of these natural units.

The bonded beads interact via finitely extensible nonlinear elastic (FENE) potential, E_{FENE} , acting between the beads adjacent along the backbone and between two beads forming *A-graft-B* monomer unit

$$E_{\text{FENE}}(r) = \begin{cases} -\frac{1}{2} K b_{\text{max}}^2 \ln \left[1 - \left(\frac{r}{b_{\text{max}}} \right)^2 \right], & r < b_{\text{max}} \\ 0, & r \geq b_{\text{max}} \end{cases} \quad (2)$$

where $K = 30$ is the spring constant, and $b_{\text{max}} = 1.5$ is the maximum bond length. An equilibrium bond length b determined by the interplay of elastic (2) and excluded volume (1) interactions with the selected K and b_{max} values is a little less than unity: $b = 0.97$.

The nonbonded monomer units interact via Yukawa-type potential, $E_{\text{IJ}}(r)$, accounting implicitly the solvent quality

$$E_{\text{IJ}}(r) = \begin{cases} \epsilon_{\text{IJ}} \left(\frac{\exp(-kr)}{r} - \frac{\exp(-kr_{\text{cb}})}{r_{\text{cb}}} \right), & r < r_{\text{cb}} = 4 \\ 0, & r \geq r_{\text{cb}} = 4 \end{cases} \quad (3)$$

where $k = 1.2$ is the inverse screening length, and characteristic energies ϵ_{IJ} are different for different groups (I, J = A, B).

In a simulation presented here, $\epsilon_{\text{AA}} = 0$, $\epsilon_{\text{AB}} > 0$, and $\epsilon_{\text{BB}} \leq 0$. There are no any, except excluded volume, interactions between backbone A groups, and the solvent is selectively good for them. The positive parameter ϵ_{AB} promotes segregation of A and B groups and ensures the surface activity of amphiphilic *A-graft-B* monomer units. The negative parameter ϵ_{BB} provides attractive interaction between side B groups and reproduces poor solvent conditions for monomer pendants: $-10 < \epsilon_{\text{BB}} < 0$.

The substrate is modeled as a flat wall located at $z = 0$ and interacting with each bead via truncated repulsive branch of the 9–3 Lennard-Jones potential, E_s ⁴⁷

$$E_s(z) = \begin{cases} 2\epsilon \left[\frac{2}{15} \left(\frac{\sigma}{z} \right)^9 - \left(\frac{\sigma}{z} \right)^3 + \sqrt{\frac{10}{9}} \right], & z \leq r_s = \sqrt[3]{2/5} \\ 0, & z > r_s = \sqrt[3]{2/5} \end{cases} \quad (4)$$

where z is a distance normal to the surface.

As usual, temperature T was maintained by a Langevin thermostat with a friction term and a Langevin uncorrelated noise term R_i related to the viscosity of the solvent through the fluctuation–dissipation theorem⁴⁸

$$R_{\alpha i}(0)R_{\alpha i}(t) = 2\Gamma k_B T \delta(t) \quad (5)$$

where δ is the Dirac delta function; $\alpha = x, y, z$ are the coordinates, $i = 1, \dots, nN$; and parameter $\Gamma = 0.01$ in all calculations.

In each computer experiment, the polymer brush contains $n = 169$ macromolecules and the distance between grafting points $d = 2$. The degree of polymerization N changes from $N = 10$ to $N = 100$ monomer units. Thus, the reduced grafting density $\Sigma = \pi \left(\frac{R_{\text{G0}}}{d} \right)^2$ varies from $\Sigma \approx 8.2$ to $\Sigma \approx 82$, where R_{G0} is the gyration radius of macromolecule in the melt. Our

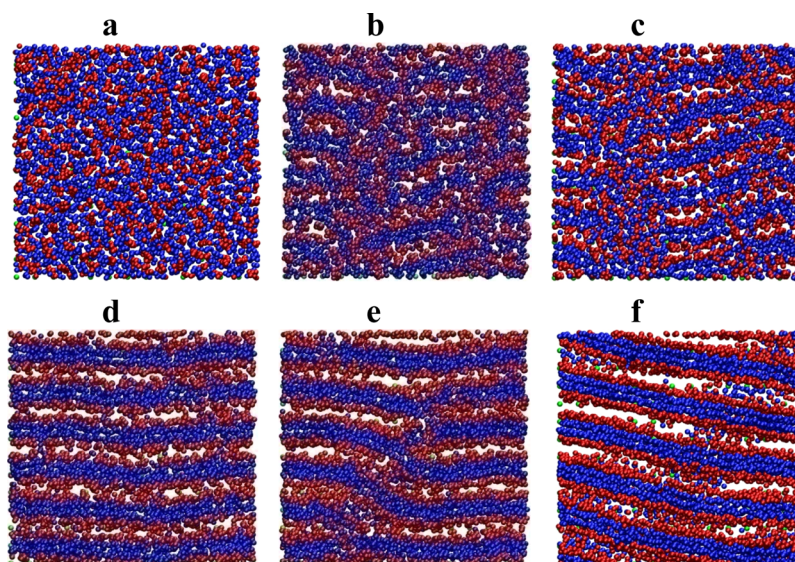


Figure 2. Snapshots of typical structures. Top view of brush slice at height $z = 15$ from the surface, polymerization degree $N = 50$, energy $\varepsilon_{BB} = 0$ (a); -3.0 (b); -3.5 (c); -5.5 (d); -7 (e); and -9.5 (f).

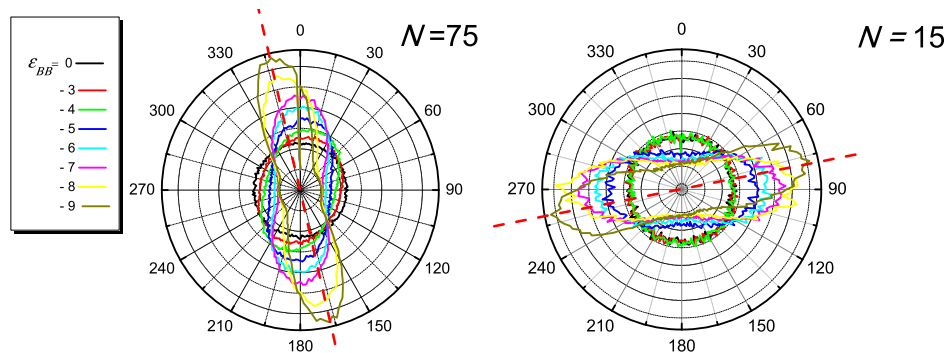


Figure 3. Distribution $\mathcal{R}(\Omega)$ of bond vectors \vec{r}_{AB} over angle Ω for different energies ε_{BB} , $N = 75$ (left) and $N = 15$ (right). Dashed red lines indicate main directions of bond vectors at high values of $|\varepsilon_{BB}|$.

calculations show that although the backbone A–A bonds experience excessive tension, even at the highest grafting density, the average bond length was not more than 1% longer than its equilibrium value: $b = 0.97$.

In the initial configuration, the polymer chains were extended in the direction of the z -axis; then, the polymer brush was equilibrated for a long time with $\varepsilon_{AA} = 0$, $\varepsilon_{AB} = 0$, and $\varepsilon_{BB} = 0$. After that, the energy ε_{BB} was gradually increased to $\varepsilon_{BB} = -10$ in steps of $\Delta\varepsilon_{BB} = -0.25$. For each value of ε_{BB} , simulations were performed during prolonged time with the integration step of 0.01τ ($\tau = \sigma\sqrt{m/\varepsilon}$ is the unit of time) to ensure system equilibration. After that, the production stage was committed. The relaxation and production times were fitted to ensure a complete system equilibration and a rational result justification, which were checked by standard procedures.³¹ The full calculation time varied from $10\,000\tau$ to $60\,000\tau$ steps depending on the macromolecular length and interaction energy ε_{BB} .

The results of the calculations are discussed in the next section.

RESULTS

Typical structures distinguished in computer experiments are shown in Figure 2. There are totally mixed state with a

homogeneous distribution of A and B groups (A), prolonged aggregates (B and C), and lamellae with different domain spacing (D–F).

As it was shown recently,³¹ the segregation of A and B groups is accompanied by limitation of possible directions of bond vectors \vec{r}_{AB} connecting A and B groups of the monomer unit. Numerically, this effect could be accounted for by calculations of circular distribution \mathcal{R} of bond vectors $\vec{r}_{AB}(i)$ over orientation angle Ω_i , which was determined, for definiteness, as an angle between the bond projection $\text{Pr}_{xy}[\vec{r}_{AB}(i)]$ on the grafting plane XY and the axis OX : $\Omega_i = \arctan(y_{AB}(i)/x_{AB}(i))$, where $i = 1, \dots, nN$. The distribution $\mathcal{R}(\Omega)$ averaged over time for different energies ε_{BB} , and polymerization degrees N are shown in Figure 3. The distributions are presented in polar coordinates (\mathcal{R} , Ω) with angle Ω changing in the interval $0 \leq \Omega \leq 360^\circ$ and radius \mathcal{R} showing the fraction of A–B bond vectors with given angle Ω : $\sum_{\Omega=0}^{2\pi} \mathcal{R}(\Omega) = 1$.

It is seen that at low values of $|\varepsilon_{BB}|$, the distribution $\mathcal{R}(\Omega)$ is an almost perfect circle with the center at the origin point and negligible fluctuations in radius \mathcal{R} . Growth of B–B attractive interaction $|\varepsilon_{BB}|$ leads to visible deformation of $\mathcal{R}(\Omega)$: fraction \mathcal{R} increases for some angles Ω and simultaneously decreases for others. In case of $N = 75$, at $\varepsilon_{BB} > -4$, the distribution

$\mathcal{R}(\Omega)$ looks similar to a flattened oval. Within interval $-8 < \varepsilon_{\text{BB}} < -4$, the long axis of this oval is placed parallel to oX axis. $\mathcal{R}(\Omega)$ has a maxima at $\Omega \approx 0^\circ$ and 180° and minima at $\Omega \approx 90^\circ$ and 270° . The $\mathcal{R}(\Omega)$ oval becomes thinner with the increase of $|\varepsilon_{\text{BB}}|$, and also at $\varepsilon_{\text{BB}} = -8$, it changes orientation: the long axis rotates by about 14° . $\mathcal{R}(\Omega)$ rotation indicates the rotation of lamellae and also implies the changes of periodic structures. Lamellae of shorter macromolecules ($N = 15$) are arranged first parallel to oX : the bond vectors are mostly perpendicular to oX . Then, they turn by about 14° as well. We would like to mention that the size of the cell was chosen as a commensurate size of lamellae with a small domain spacing. It contains an integer number of domain spacings of such lamellae and ensures their spontaneous arrangement parallel to cell sides.⁴⁹

The circular distribution $\mathcal{R}(\Omega)$ is characterized by dispersion σ_Ω calculated as⁵⁰

$$\sigma_\Omega = \frac{1}{\pi} \left(-\log \left[\left(\frac{1}{nN} \sum_{i=1}^{nN} \cos \Omega_i \right)^2 + \left(\frac{1}{nN} \sum_{i=1}^{nN} \sin \Omega_i \right)^2 \right] \right)^{1/2} \quad (6)$$

The dispersion σ_Ω allows estimating quantitatively the range of available bond vectors \vec{r}_{AB} orientations. In case of a totally free orientation of A–B bonds, the dispersion σ_Ω is maximal and equals unity: $\sigma_\Omega = 1$. Any limitation on the position of A–B bonds leads to σ_Ω decrease.

The dependences $\sigma_\Omega(\varepsilon_{\text{BB}})$ for different N are shown in Figure 4.

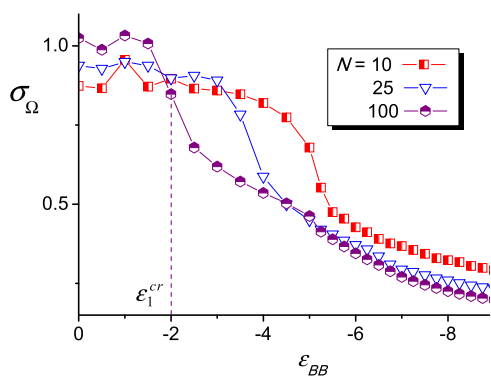


Figure 4. Dispersion σ_Ω as a function of ε_{BB} for different polymerization degree N . Dashed vertical lines indicate critical points of transition from ordered to disordered state for $N = 100$.

In the absence of energetic interactions between B groups ($\varepsilon_{\text{BB}} \approx 0$) and at a relatively weak B–B attraction, the dispersion σ_Ω is close to unity. It reflects that in this field, the bond vector \vec{r}_{AB} could accept any directions. The dispersion σ_Ω decreases with the increase of $|\varepsilon_{\text{BB}}|$. First, it drops sharply; after that, it smoothly goes to plateau. The amplitude of the drop as well as its position depend on the macromolecular length N . For macromolecules with $N = 100$, the sharp drop of dispersion σ_Ω from $\sigma_\Omega \approx \pi$ to $\sigma_\Omega \approx 0.69\pi$ proceeds within the interval $\Delta\varepsilon_{\text{BB}} \approx -1.5 \div -2.5$. For macromolecules with $N = 25$, the interval of sharp drop shifts toward larger $|\varepsilon_{\text{BB}}|$: $\Delta\varepsilon_{\text{BB}} \approx -3.0 \div -4.0$; within this interval, the dispersion σ_Ω changes from $\sigma_\Omega \approx 1$ to $\sigma_\Omega \approx 0.6$. Inflection points of $\sigma_\Omega(\varepsilon_{\text{BB}})$ dependence can be referred to as critical values $\varepsilon_1^{\text{cr}}$ of transition

from disordered to ordered state with prolonged aggregates. It is seen that the longer is macromolecular length N , the smaller is $|\varepsilon_1^{\text{cr}}|$.

Figure 5 shows the structure factor $S(\vec{q})$ calculated according to the procedure of ref 49

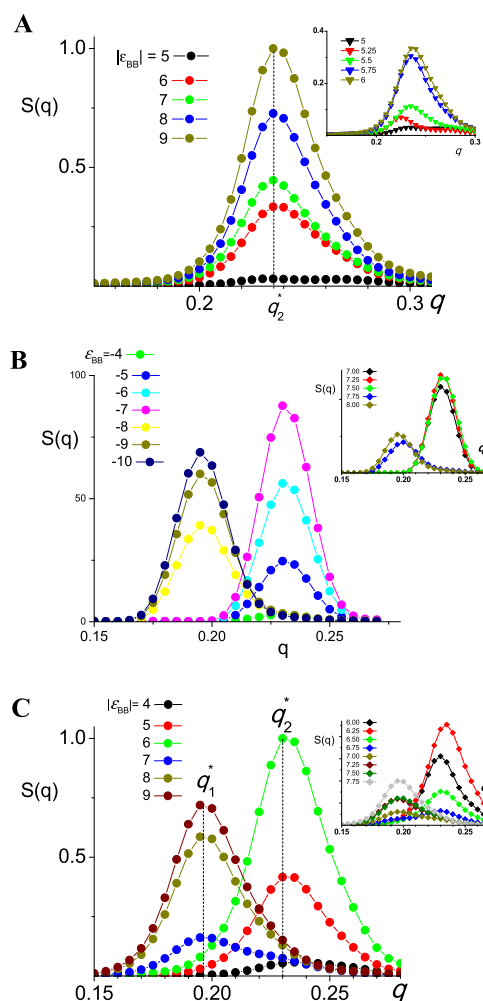


Figure 5. Structure factor $S(q)$ as a function of wave vector q for different energy ε_{BB} at $N = 10$ (A); 20 (B); and 50 (C).

$$S(\vec{q}) = \frac{1}{V} \sum_{i,j} (e_i e_j - e_i^2) \exp\left(\frac{i\vec{q} \cdot \vec{r}_{ij}}{2\pi}\right)$$

where \vec{r}_{ij} is the vector between groups ($i, j = 1, \dots, 2nN$); e_i is -1 for A groups and $+1$ for B groups.

Defined in that way, the structure factor $S(\vec{q})$ allows detecting the lamellar ordering and determining their domain spacing as: $\lambda = 1/q^*$, where q^* is the wave vector of the maximum of the structure factor.

It is seen in Figure 5 that the structure factor $S(\vec{q})$ can have pronounced maximum at two different values $q_1^* \approx 0.195$ and $q_2^* \approx 0.23$ indicating the existence of two types of lamellar structures with big $\lambda_1 \approx 5$ and small $\lambda_2 \approx 4.35$ domain spacing. The lamellae with small domain spacing are observed at the weaker ε_{BB} attraction. The availability and height of the maxima depend on the energy ε_{BB} and polymerization degree N .

In case of macromolecules with $N = 10$, the structure factor $S(q)$ has the only maximum at $q \approx 0.235$. This maximum appears at $|\epsilon_{BB}| \approx 5.5$ and demonstrates steady growth with the increase of $|\epsilon_{BB}|$. For $N = 20$, one can distinguish three characteristic regions. At $|\epsilon_{BB}| \leq 4$, the structure factor $S(q)$ has no extreme point; within interval $4 < |\epsilon_{BB}| \leq 7.5$, the structure factor $S(q)$ has a well-pronounced maximum at $q_2^* \approx 0.23$. At $|\epsilon_{BB}| \geq 7.75$, the structure factor $S(q)$ also has the only maximum located at a lower wave vector: $q_1^* \approx 0.195$ (see Figure 5B and insert). Thus, within interval $7.5 < |\epsilon_{BB}| < 7.75$, the period of lamellae structure increases from $\lambda_2 \approx 4.35$ to $\lambda_1 \approx 5$. In case of longer macromolecules ($N = 50$), the transformation of lamellae proceeds within a much wider interval from $|\epsilon_{BB}| = 6.5$ to $|\epsilon_{BB}| = 7.75$. Within this interval, the structure factor has a broad maximum covering both q_1^* and q_2^* area and indicating the coexistence of lamellae with different domain spacing. Also, here the maximum value of the structure factor is much lower. Thus, the analysis of structure factors allows us to distinguish the field of lamellae with small spacing (the only distinct maximum at q_2^*), the field of lamellae with big period (the only distinct maximum at q_1^*) and the transition region. For a given degree of polymerization N , the field of lamellae with a small period is limited by an energy interval $\epsilon_{s-b}^{cr} < \epsilon_{BB} < \epsilon_s^{cr}$, where plot $S(q)$ demonstrates the only maximum at the big wave vector. The boundary ϵ_b^{cr} of lamellae with a big domain spacing field is determined as the maximum value of energy ϵ_{BB} having a structure factor with the only maximum at the small wave vector. The interval from ϵ_{s-b}^{cr} to ϵ_b^{cr} is the transition region which includes both lamellae structures joined with each other to single structure referred as the parking garage structure.³¹

The results are summarized as a diagram of states in Figure 6. There, regions without segregation of A and B groups and

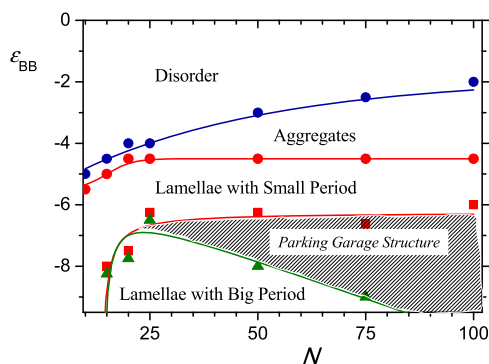


Figure 6. State diagram. ϵ_1^{cr} (-●-); ϵ_s^{cr} (-●-); ϵ_{s-b}^{cr} (-■-); and ϵ_b^{cr} (-▲-).

with aggregates from few macromolecules, fields of lamellae with small and big domain spacing, and parking garage region are shown. The boundaries between different regions are calculated according to the procedures described above.

One can see that longer macromolecules undergo disorder-aggregates transition at the lower attraction between side groups. Curve, indicating the boundary between aggregates and region of lamellae with small domain spacing, is increasing function of N only at small polymerization degree ($N < 20$); then, it goes to plateau and remain constant. Another curve, limiting the region of lamellae with small domain spacing at high values of $|\epsilon_{BB}|$ also is parallel to N axis at $N > 25$. At smaller N ($N < 25$), it drops sharply. Our calculations show

that macromolecules with $N < 15$ keep small domain spacing even at extremely high attraction ϵ_{BB} . Longer macromolecules join to lamellae with a small domain spacing at relatively small B–B attractive interaction (Figure 7, $\epsilon_{BB} = -6.25$) and form

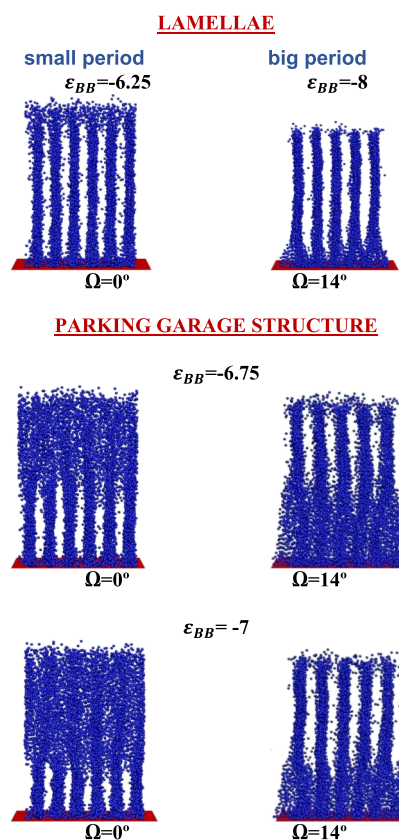


Figure 7. Instant snapshots taken from different angles Ω at different energies ϵ_{BB} . $N = 50$. Only side B groups are shown.

lamellae with a big period at high attraction (Figure 7, $\epsilon_{BB} = -8$). Boundary of the region of lamellae with a big domain spacing is shown by green. The shaded spacing between red and green curves is the transition region. It is extremely narrow for short macromolecules and broadens with the increase of polymerization degree N . In this transition region, the lamellae with different periods are piled one over the other (Figure 7, $\epsilon_{BB} = -6.75$ and -7): lamellae with big domain spacing are in the top of the brush and lamellae with small domain spacing are close to the grafting surface. In fact, they form a system of parallel layers mutually connected by bridges which are similar to the ramps in the multistorey parking garage³¹ (first, the term “parking garage structure” was employed to name a similar ordering in the endoplasmic reticulum with stacked membrane sheets and twisted membrane connection⁵¹).

The formation of a parking garage structure embarks as the appearance of a thin layer of the lamellae with big domain spacing on the top of the brush (Figure 7). This layer is turned with respect to the bottom lamellae on an angle of 14° . To make it clear, we present instant snapshots in the front projection ($\Omega = 0$) and in projection rotated by $\Omega = 14^\circ$. One can see that the bottom layer contains six lamellae which are parallel to the oX . Upper layer includes five lamellae. With the increase of $|\epsilon_{BB}|$, this layer becomes thicker, it shifts closer to the grafting surface, and finally spreads to the whole grafting layer.

Short macromolecules ($N < 25$) pass through the parking garage structure within an extremely narrow interval of ϵ_{BB} . Long macromolecules with $N = 100$ persist parking garage structure even at a rather strong attractive interactions: $\epsilon_{BB} < -10$.

To reveal bicontinuous properties of the parking garage structure, the fraction $\langle M \rangle$ of B groups belonging to the largest aggregate was calculated. Aggregate is defined as a set of B groups, each within the distance $r_{ag} = 1.3$ from one or more other groups in the cluster. By definition, $\langle M \rangle$ changes within the interval $0 < \langle M \rangle \leq 1$ and reaches its maximum value when all B groups are joined into a single cluster. It is seen (Figure 8) that $\langle M \rangle$ is a complex function of ϵ_{BB} . First, it

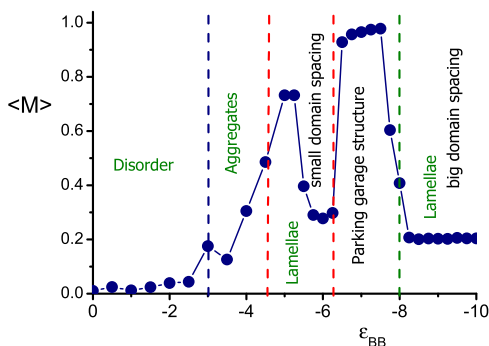


Figure 8. Fraction $\langle M \rangle$ of B groups at the biggest aggregate as a function of ϵ_{BB} . $N = 50$.

monotonously increases up to $\langle M \rangle \approx 0.7$, then drops to $\langle M \rangle \approx 0.3$, abruptly goes to $\langle M \rangle \approx 1$, and finally undergoes a sharp transition to $\langle M \rangle \approx 0.2$. It is seen that sharp changes in $\langle M \rangle$ are the consequence of structure reconstruction. The boundaries of structure are shown by a dashed line colored in accordance with the state diagram in Figure 6. Aggregation number $\langle M \rangle$ reaches its largest possible value in the region of the parking garage structure where $\langle M \rangle = 1$. In that way, we numerically confirm the bicontinuous character of parking garage structure with all B groups joined in the single cluster.

The significant stretching of macromolecules caused by their dense grafting leads to substantial backbone tension Y_{AA} .^{52,53} Backbone tension $Y_{AA}(l)$ of the l bond ($l = 1, \dots, N - 1$) is a total force acting between l and $l + 1$ monomer units and determined by excluded volume (1) and FENE (2) potentials. The backbone tension $Y_{AA}(l)$, averaged over chains and time, is shown in Figure 9 for different ϵ_{BB} .

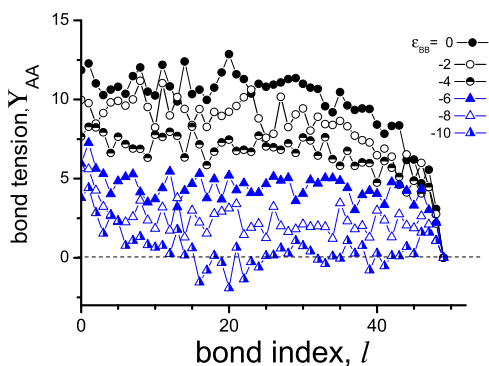


Figure 9. Backbone tension Y_{AA} as a function of bond index l for $N = 50$ and different energies ϵ_{BB} .

It is seen that one could distinguish two characteristic scenarios of $Y_{AA}(l)$ dependencies. In the absence of attractive interaction and for relatively weak attraction ($-4 \leq \epsilon_{BB} \leq 0$), the backbone tension $Y_{AA}(l)$ is high. It is almost constant for the initial, closest to the grafting surface, part of macromolecules, and sharply declines with the increase of l for the ending part of the chain. It is seen here that the tension of starting part of macromolecules decreases with the increase of B–B attraction (the increase of absolute value $|\epsilon_{BB}|$), and that even bonds in the external part ($l = 47$ and 48) are exposed to significant tension. In contrast, at stronger attractive interaction $\epsilon_{BB} \leq -6$, the backbone tension $Y_{AA}(l)$ sharply decreases at the initial part of the chain, and then it stays as a constant. Here also, the backbone tension $Y_{AA}(l)$ decreases with $|\epsilon_{BB}|$ growth. At $\epsilon_{BB} \approx -10$, the backbone tension Y_{AA} takes zero and negative values.

It means that in this case, the A–A bonds could be stretched ($Y_{AA} > 0$), shrunken ($Y_{AA} < 0$), or have precisely an equilibrium length ($Y_{AA} = 0$). It is seen that in fact only the initial part ($l < 15$) is stretched ($Y_{AA} > 0$), and the tension in the ending part ($l > 15$) fluctuates around zero. Our calculations reveal that even at the highest overall tension ($\epsilon_{BB} = 0$), the average bond length expands by less than 1% from its equilibrium value: $b = 0.97$. In case $\epsilon_{BB} \approx -10$, fluctuations in the length of bond with index $l > 15$ are about 0.05%, and one can conclude that at $\epsilon_{BB} = -10$, the bonds of ending part of macromolecules are close to their basic states with $b = 0.97$. Thus, the self-organization in densely grafted layers relieves the bond tension and diminishes the corresponding energy.

CONCLUSIONS

By means of computer modeling, we study the self-organization of macromolecules densely grafted to plane (polymer brushes) with surface-active monomers and different polymerization degree. The surface activity of monomers was accounted for by representing them as an A-graft-B “dumbbells” of two beads. A and B beads repel each other and selectively interact with the solvent. The solvent being athermal for backbone A groups and poor for pendant B, graduate worsening of the solvent quality, modeled by the increase of attractive B–B energy ϵ_{BB} , leads to aggregation of B groups and transformation of polymer brushes from the state with homogeneous A and B distribution to prolonged aggregates and lamellae structures. The plane of the lamellae is perpendicular to the grafting surface. The lamellae could have two different domain spacing: smaller in a less poor solvent and bigger in a more poor solvent. The domain spacings of both lamellae structures, if they arise, do not depend on the polymerization degree. In the transition region, these lamellae coexist but reside at different heights. Lamellae with small domain spacing are closer to the grafting surface and lamellae with large domain spacing are on the top. They are turned with respect to each other and are connected by twisted bridges to form the parking garage structure. The results are presented as a state diagram with five different regions: disorder, aggregates, lamellae with small domains spacing, transition region, and lamellae with big domain spacing. The boundaries were determined qualitatively through the calculations of the structure factor function, the circular distribution of A–B bond vectors, and its dispersion.

The boundary between disorder region and aggregates is monotonically an increasing function of polymerization

degree: the longer are the macromolecules, the poorer is the solvent quality of aggregate formation. The position of the border between the region of aggregates and the region of lamellae with a small period does not depend on the polymerization degree for a sufficiently long chain ($N > 25$) and shifts toward poor solvent quality with the decrease of chain length N for shorter chains ($N < 25$). The width of the transition region between lamellae with different spacing depends on the polymerization degree: it is the widest for long macromolecules, narrows down with the decrease of macromolecular length, and totally disappears for relatively short macromolecules ($N < 15$). The reduced density of macromolecules was quite high (from 8.2 to 82), and macromolecules are stretched perpendicular to the grafting surface. This stretching is a result of excluded volume interaction with neighbor chains and induces sufficient backbone tension which is distributed over chains and depends on solvent quality. In the absence or at the relatively weak B–B attraction (disordered or aggregates regions in state diagram), the dependence of bond tension on bond index looks similar to a step function: the bond tension is constant which does not depend on the bond index for the whole chain except short outer piece, where tension drops sharply. At strong B–B attraction (lamellae and parking garage structure), the repulsive excluded volume interactions are screened and bond tension as a whole is smaller, and maximum tension is imposed on the bond next to grafting surface. It can be explained by larger scale of emerging structures that leads to stretching of the beginning pieces of chains, the so-called legs. The stretching is balanced by energetic gains because of stronger aggregation of B groups and formation of sufficient room for A–B segregation. In short macromolecules, legs could comprise a significant part of the chain, and the shorter the chain, the larger interaction energy ϵ_{BB} is needed to counterbalance the stretching of legs. In extremely short macromolecules, such balance is unreachable at least for an investigated range of interaction energy ϵ_{BB} ; thus, lamellae with a larger domain spacing do not appear at all.

The formation of different structures is accompanied by the change of B–B aggregation number which exhibits sharp jump in the region of “aggregates-lamellae” and “lamellae-parking structure-lamellae” transitions. For the parking garage structure, the aggregation number, measured as a fraction of monomer units entering the biggest clusters, is close to unity. It is the maximum possible value indicating the merge of all B groups to the only cluster and the formation of the bicontinuous structure. The ability to pass rapidly from bicontinuous to lamellae structure could be interesting for practical applications which require a quick change of connectivity, such as molecular switches, elements of electrical circuits, the system for controllable catalysis, and so forth.⁵⁴ We believe that such types of reconstruction (lamellae—parking garage—lamellae) could be observed in other polymer systems, where self-organization is accompanied by the conformation changes of their constituent parts.

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Notes

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