



HHS Public Access

Author manuscript

Comput Methods Programs Biomed. Author manuscript; available in PMC 2020 September 01.

Published in final edited form as:

Comput Methods Programs Biomed. 2019 September ; 178: 113–122. doi:10.1016/j.cmpb.2019.06.017.

Addressing Challenges of Quantitative Methodologies and Event Interpretation in the Study of Atrial Fibrillation

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Abstract

Atrial fibrillation (AF) is the commonest arrhythmia, yet the mechanisms of its onset and persistence are incompletely known. Although techniques for quantitative assessment have been investigated, there have been few attempts to integrate this information to advance disease treatment protocols. In this review, key quantitative methods for AF analysis are described, and suggestions are provided for the coordination of the available information, and to develop foci and directions for future research efforts. Quantitative biologists may have an interest in this topic in order to develop machine learning and tools for arrhythmia characterization, but they may perhaps have a minimal background in the clinical methodology and in the types of observed events and mechanistic hypotheses that have thus far been developed. We attempt to address these issues via exploration of the published literature. Although no new data is presented in this review, examples are shown of current lines of investigation, and in particular, how electrogram analysis and whole-chamber quantitative modeling of the left atrium may be useful to characterize fibrillatory patterns of activity, so as to propose avenues for more efficacious acquisition and interpretation of AF data.

Keywords

atrial fibrillation; automaton; dominant frequency; electrograms; model

Overview

Atrial fibrillation (AF) is a common heart arrhythmia, yet how it is initiated and maintained is mostly unknown [1]. The risk of AF recurrence and thromboembolism may be mitigated with antiarrhythmic drugs and anticoagulant agents, respectively. However, the success rate with pharmacologic treatment is relatively low, and recurrences are common [2]. Catheter ablation of suspected atrial triggers in arrhythmogenic regions such as the pulmonary veins

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Conflicts of interest

the authors have no conflicts of interest.

can be done in the electrophysiology laboratory. Yet, any arrhythmogenic regions residing outside of the pulmonary veins may be difficult to detect and localize directly, since such triggers are not always evident during electrophysiologic testing. Quantitation of electrograms acquired from the heart surface, and modeling of the myocardial substrate, have been proposed and have shown some promise to visualize suspected drivers, and to describe AF characteristics under certain conditions. To the present time however, the success of such techniques is in rather simple problem-solving, such as to determine the significant differences in the cardiac parameters of patients with paroxysmal versus persistent type of arrhythmia [3]. In ongoing work, major goals include the determination as to whether quantitation can be utilized to estimate and predict the progression of AF and its causal mechanisms, as well as to suggest a more efficacious ablation strategy, perhaps focused on the individual patient, as has been the subject of precision medicine efforts [4]. In this review, issues pertaining to the quantitative interpretation of atrial fibrillation data are described and discussed, and suggestions are made for improvement, such that testable hypotheses and techniques for understanding the mechanisms of AF and best ablation strategies can be developed.

Background

To enhance techniques for obtaining salient information concerning the mechanisms of AF initiation and perpetuation, and to best locate catheter ablation sites at arrhythmogenic zones for treatment, there is a need for improving the methods of data acquisition and interpretation of the acquired data, which includes heart surface recordings (i.e., electrogram signals). To this end, an increase in the spatiotemporal resolution of local heart surface recordings, better analysis of these electrograms, and development of quantitative models more representative of AF phenomena are important. Currently, AF drivers residing outside of the pulmonary vein antrums are difficult to detect in the electrophysiology laboratory [5], and many observed AF events are not well reproduced by quantitative modeling [6]. Furthermore, a major difficulty in targeting sites for ablation is that the sources of arrhythmia at onset are mostly unknown in terms of their dynamic properties and location [7]. Early whole-chamber as well as molecular-level quantitative models have been constructed to simulate the electrophysiologic conditions occurring during AF [8–15]. By tweaking model parameters, it might be possible to develop hypotheses regarding the connection between model-simulated events and corresponding actual AF events. Yet, these models may have limited accuracy in reproducing AF episodes, in part because the important electrophysiologic parameters to incorporate, and the correct values for parameterization, are not entirely known [16]. If it were possible to localize AF drivers from quantitative analysis, such as from heart surface electrogram time series features and spectral analysis [17], to develop higher resolution acquisition and mapping techniques [18], and to better interpret these maps for understanding AF mechanisms, then the timeliness and efficacy of clinical treatment procedures could potentially be improved.

One difficulty in improving quantitative analysis is that the etiology of AF is partially unknown [19]. There are however, two factors likely to be important in its onset and perpetuation [7]. The basic pathophysiological mechanisms of AF are known to be focal ectopic activity and reentry [10]. Electrical impulses typically originating in the pulmonary

veins or in the pulmonary vein antrums, as well as in the left atrial free wall, can overwhelm the normal sinus rhythm activation sequence. These sources may act as premature electrical stimuli so that unexpected, or “rogue”, electrical activation wavefronts, commence in the left atrial myocardium. These stimuli can therefore be considered drivers of AF, but they are focal, in that the electrical impulses originate from point sources, outside the normal sinus rhythm process, to generate irregular and often random electrical activation wavefronts. The coupling interval between any such pulses can sometimes or even frequently be less than the refractory period in certain atrial myocardial regions, resulting in functional conduction block [20]. Even if the periodicity of any rogue wave emanation is longer than the tissue refractory period, if the timing precedes the recovery of excitability after normal sinus rhythm activation, functional block would also occur.

Areas of functional block caused by focal stimuli can lead to rotational electrical activity, as a rogue wave bifurcates around a refractory region, and then may propagate through it in a circular pattern after recovery of excitability [21]. Rotational features so formed also generate rogue waves, and are also likely to be important in the onset and maintenance of AF. Localized focal sources and rotors may be found in patients with any type of AF [22]. Panoramic contact mapping has also provided evidence that sustained AF may be largely due to focal sources and stable electrical rotors in either atrium [23]. Ablation at these sites can terminate or substantially organize the arrhythmia prior to any additional ablation.

The electrophysiologic conditions conducive to the formation of rotational patterns of electrical activity include the presence of areas of slow conduction velocity and/or relatively short refractory period along the prospective reentrant circuit pathway [24]. These factors result in a short wavelength, which is defined as the product of the local refractory period multiplied by the local conduction velocity, i.e.:

$$\lambda = RP * CV$$

At short wavelengths, a finite excitable gap, the time interval during which the local tissue has recovered excitability prior to the next activation cycle, is more likely to be maintained [25]. Thus, the activation wave can be perpetuated in a circuitous path without encountering refractoriness to electrical conduction that would otherwise block its continued propagation.

In patients with ongoing AF, the remodeling of myocardial tissue can occur on both a gross and microscopic scale [26, 27]. Dispersion of action potential duration (APD) is a manifestation of remodeling that is likely important for onset of reentry in AF [28]. Furthermore, microscopic structural changes to electrophysiologic alterations in ion channel function, gap junctional connection, and variability in other cellular structures and parameters may lead to fibrosis [29] and metabolic derangement [30]. An important pathologic alteration observed in persistent AF patients is tissue fibrosis [27]. Fibrosis is a source of anatomical conduction block [31], which can slow the activation wave and cause circuitous pathways of activation, thereby enabling a contribution to the persistence, complexity, and progression of the fibrillatory process.

The two main observed patterns of atrial rotational activity are the presence of vortices, which swirl about a small unexcitable core [22,23,32], and can consist of one, two, or even several reentrant circuit loops in tandem, and freestanding wavelets [33, 34], which are activation wavefronts with distinct ends that travel about larger impediments to conduction, such as regions of fibrosis or an ablation lesion. For both of these rotational type patterns, the leading edge of the activation wave reenters previously excited areas after their recovery of excitability, thus following a circuitous pattern. Tissue remodeling often occurs when rotational features with rapid activation are present in the atrial substrate to drive AF. The remodeling process may include an increased release of calcium ions from the sarcoplasmic reticulum [35], which reduces the APD, and correspondingly shortens the refractory period for electrical conduction. AF is associated with a decrease in adaptation of APD to rate as well as to changes in atrial conduction velocity [36]. These phenomena can contribute to further perpetuation of AF (i.e., 'AF begets AF' [37]) since the wavelength λ is further diminished.

To terminate AF and prevent its recurrence, sources of premature stimuli should be ablated or electrically isolated [38]. However, whether or not anatomical locations which serve as sites of formation for rotational features should also be ablated or electrically isolated, is difficult to determine since they are not readily detectable [39]. Furthermore, AF drivers can be intramurally positioned [40], which would make localization problematic for achieving a successful ablation. AF recurrence could be prevented by removing all ectopic foci and rotational features, both of which are drivers of AF. Yet, targeting triggers outside of pulmonary vein isolation is not currently the standard of care [41]. Since the goal of successful AF treatment in the electrophysiology laboratory is the removal of all drivers, guidance for successful targeting has not yet reached a consensus and requires further study.

The complexity of AF and its mechanism of onset by premature stimulation, and perpetuation by focal and rotational activity, stem from the presence of multiple sites where drivers may appear either sequentially or simultaneously in time. Although multiple reentrant circuits can be present, they may not be fixed in location over long time periods. The presence of any rotational pathways are typically difficult to localize in AF, owing to the lack of long-term repeatability of the temporal activation pattern [42] so that presently, radiofrequency ablation of these regions has unknown efficacy. AF is occasionally a progressive condition [43], so that arrhythmia duration without interruption tends to increase over time.

Acquiring clinical AF data for quantitation

When patients with paroxysmal AF are subject to electrophysiologic study, the pulmonary veins are first electrically isolated, and the ability of the ablation lesions to block propagation is assessed. To eliminate drivers in the atrial free wall region, it would then be necessary to reinduce AF by programmed electrical stimulation, followed by localization of any such suspected drivers. Yet, a particular stimulus location and pulse train may result in AF induction on one instance, but fail to induce AF for a subsequent instance. Furthermore, stimuli applied to one location may result in AF onset, yet from another location the same stimulus train may fail to induce AF. These points are illustrated in Figure 1. The process of

AF induction in the electrophysiology laboratory is tedious and time consuming, because there is no set stimulus pattern which results in AF onset. Thus the induction characteristics for AF are not highly repeatable, and furthermore, differences in the characteristics of the activation pattern during AF may occur on different inductions, making more difficult the drawing of conclusions from quantitative efforts. Moreover, during clinical study, paroxysmal AF can terminate while ablation is ongoing. However, the catheter tip location and the magnitude of energy delivery at termination may be unrelated to the AF process, with further induction and ablation being necessary to prevent arrhythmia recurrence (Figure 2, left side). Thus the characteristics of the acquired heart surface electrogram signal at the termination site is likely to be mostly or entirely irrelevant to the detection of paroxysmal AF drivers, another problem posed for quantitative analysis. After AF termination, programmed electrical stimulation at many sites, and pulsed extrastimuli patterns, may be utilized to establish whether AF can be reinduced, and to test whether or not other atrial arrhythmias such as atrial flutter or tachycardia are inducible [44].

In contrast, for patients with persistent AF, spontaneous termination of arrhythmia during ablation is rare (Figure 2, right side). When termination does occur, the ablation site is likely to be important to arrhythmia maintenance; therefore the time and frequency characteristics of electrograms recorded in the area can potentially be useful markers of persistent AF drivers. After ablation, and after cardioversion when it is needed for termination, the process may be repeated until AF is no longer inducible, and if successful, it can be used as a procedural endpoint. However, in both paroxysmal and persistent patients, AF may recur after many weeks or months due to the reestablishment of conduction pathways across ablation lesions [45], and due to the development of additional microstructural areas where drivers can form. Hence, detecting driver sites through quantitation may involve finding both current locations that are capable of driving arrhythmia, as well as finding locations that are evolving to become drivers. Detection of these latter locations would only be possible if substrate features were to be identified in the data that are predictive of future events, an ongoing research effort.

When surface AF electrograms are acquired with a standard catheter having a single electrode at its tip, there is often a preference for using a bipolar configuration for quantitation, because the far-field signal, motion artifact, and electrical noise are then mostly eliminated by subtraction. Yet, bipolar recordings are difference signals, and their amplitude and shape depend upon activation wavefront direction, so that they must be used with some caution [46].

Furthermore, interelectrode distance also influences bipolar voltage [47]. Noncontact mapping is feasible to estimate heart surface electrogram characteristics with high spatial resolution, and the virtual electrograms obtained can even be used to estimate local frequency characteristics [48]. Moreover, contact catheters having ten bipolar electrodes are becoming more frequently used for AF data acquisition, and even basket catheters with many recording electrodes, as well as higher density mapping catheters, are now utilized in the electrophysiology lab. A difficulty with these multichannel devices is that they can be bulky, and some electrodes may not reside in contact with the endocardial surface [49]. The signals so obtained will then be an average of the activity in the whole atrial chamber, which

will not be reflective of nearby heart surface activation times. Recently introduced multichannel recording devices are beginning to offer greater flexibility, greater spatial resolution, and minimized size and weight, for ease of use and improved surface contact [50], which could prove assistive to improve acquisition quality for future studies. Body surface signals can localize left and right atrial high-frequency rotors in AF [51]. Body surface mapping can also be used to identify reentrant and focal sources important to driving and perpetuating AF [52]. The spectral analysis of such AF body surface recordings enables a noninvasive characterization of the global distribution of the atrial frequency and identification of areas with highest frequency, enabling the possibility of personalized diagnosis and treatment [53].

Dimensionality of the acquired atrial data

Although AF signals are typically acquired in clinical studies from the endocardial heart surface only, which can be considered as a two-dimensional surface, a third dimension, the Z or thickness axis, has significance for understanding disorganized electrical activity [11, 54]. Rotational sources are likely to be in part three-dimensional. Such pathways may have only a small directional component along the Z-axis, particularly at thinner portions of the atrium. Yet thicker wall regions exist in both normal and enlarged atria, thus enabling the establishment of a longer Z-axis pathway through which any reentrant path can proceed. Transmural reentrant features extend from epicardium to endocardium, and breakthrough of electrical impulses traveling along the Z-axis, originating from the epicardium, may occur, which can contribute to activation pattern complexity during AF [55]. Certain electrophysiologic parameters may vary according to wall thickness, and this relationship should be considered in future modeling efforts [56].

The atrial anatomy and thickness may affect electrical wave dynamics in AF [57]. The location of breakthrough sites and lines of functional block during incomplete reentry may be related to preferential propagation according to the underlying subendocardial muscle structure [58]. Based on the contribution of wall thickness, AF substrates are dynamic three-dimensional structures with a range of discordance between epicardial and endocardial tissues [59]. The complex three-dimensional atrial structure can play a major role in activation sequence during AF [58]. Where the atrial wall is relatively thick, small intramural reentrant circuits might possibly contribute to driving AF, and could be responsible for some of the observed heart surface phenomena [40, 60]. Reentry with an intramural axis of rotation (filament) will appear on the endocardial/epicardial surface as breakthrough. A reentrant circuit contained within the atrial wall whose filament stretches between opposite surfaces is transmural in scope. Heterogeneous atrial wall thickness and atrial stretch, in combination with ionic and anatomic remodeling caused by AF, are important to enable atrial scroll waves and maintenance of arrhythmia [61]. In the presence of stretch, meandering three-dimensional scroll waves anchor at regions of large spatial gradient in wall thickness. Greater intramural discontinuity in the form of higher fiber density, or presence of other irregularities in the microstructure, can also serve as formation and anchoring points for any such mid-myocardial circuits [40].

Electrogram quantitative analysis

To detect AF drivers, the amplitude, shape, and repetitiveness of electrogram signals acquired from the endocardial surface of the heart have been proposed as metrics. Typically, electrogram sequences of approximately eight seconds duration are utilized [62]. For spectral estimation, the Fourier transform (FT), an autoregressive model [63], or another estimator is commonly implemented [64]. The statistical stability of the electrogram signal over time is important for frequency analysis [65,66]. Several electrogram frequency parameters have been found useful to distinguish paroxysmal versus persistent AF type. The dominant frequency or DF, which is the largest nonharmonic spectral peak in the range 3–12 Hz, tends to be higher in persistent as compared to paroxysmal AF patients [67] with average values of 6.22Hz for persistent versus 5.67Hz for paroxysmal AF patients [68]. This reflects a tendency for shortened refractory period, due to remodeling, and therefore faster reactivation, in persistent AF. There is also a greater temporal variation in the DF in paroxysmal (1.00Hz) versus persistent AF patients (0.78Hz) [68]. Earliest AF activation is often located close to the highest DF site [69]. Another useful frequency parameter has been shown to be the dominant amplitude (DA), defined as the magnitude of the DF peak, which is measured on normalized signals. The DA tends to be of larger average magnitude in persistent (1.34 normalized millivolts) versus paroxysmal AF patients (1.09 normalized millivolts) [68]. Moreover, the dominant morphology (DM), stated as the shape of sequential electrogram segments with a segment length corresponding to the DF, has a mean temporal correlation of 0.62 for persistent versus 0.50 for paroxysmal AF electrograms [70]. Thus the repetitiveness of electrogram patterns increases and becomes more uniform in persistent as compared with paroxysmal AF [71]. These findings suggest that persistent AF recordings tend to exhibit a more temporally stable and repetitive activation pattern.

To further advance the quantitative methods for interpretation of clinical data, cardiac magnetic resonance has recently been utilized to localize atrial fibrosis, and thereby to determine the relationship between electrogram time series deflections and fibrosis caused by remodeling [72]. Any such relationship might be useful to expound upon the observation that fibrosis is often minimal or nonexistent in paroxysmal AF patients, yet common in persistent AF, from which it may lead to electrogram fractionation [73]. Electrogram fractionation, the appearance of multiple deflections and low amplitude features in the AF electrogram over long intervals, is common at some atrial regions. The electrogram shape may also be related to microarchitectural components [74, 75], though this is yet to be confirmed.

During induced AF, systolic interval shortening following either drift or acceleration of a rotational source has resulted in intermittent fibrillatory conduction and formation of fractionated electrograms at the posterior left atrial wall [69]. Shortening of AF cycle length tends to precede the development of electrogram fractionation [76]. Longer electrogram durations, often observed in fractionated signals, have been recorded more frequently in the left as compared with the right atrium. Activation maps during transitions to fractionation reveal areas of slowed conduction and unidirectional block [69]. Targeting fractionated electrograms has been found to not simply be atrial debulking. Ablating certain fractionated

electrograms increases AF cycle length, suggesting that these areas are important in maintaining AF [77].

The extracellular electrograms recorded during AF can be difficult to interpret due to cycle-to-cycle variability in their amplitude and time duration [78]. To ameliorate, phase mapping has been introduced as a quantitative technique which represents signals in terms of their relative position within a cycle. It has been widely applied to the action potential as well as to unipolar electrogram data [78]. Phase analysis of AF has gained interest due to its ability to localize organized stable rotational drivers to target for therapy [79]. The phase maps highlight areas of high-curvature wavefronts and rotors. Algorithms have been developed for calculating phase from both unipolar and bipolar electrograms recorded during AF [78]. However for some activation patterns, phase mapping generates non-rotational singularity points and false rotors. The number of detected rotors depends in part upon the parameters of the phase detection algorithm and the number of electrodes used for mapping [80]. A double ring comprised of a 2×2 and 4×4 grid of electrodes to acquire phase mapping data has been found useful for robust rotor detection.

Electrogram quantitation implemented thus far has been shown to correspond to some measured clinical parameters. For example, the average electrogram frequency spectrum level is correlated with the duration of uninterrupted persistent AF prior to electrophysiologic study, and to left atrial volume, for both persistent and paroxysmal arrhythmia [81]. Moreover, the DA parameter tends to increase with increasing left atrial volume. Based on a regression analysis, it would therefore be possible to estimate AF duration and atrial volume *a priori*. Furthermore, in early-stage clinical studies, quantitative AF models have been successfully used to identify patients in which pulmonary vein isolation alone is not adequate for treatment of AF, and to suggest novel targets for ablation [6]. Hence, further development of electrogram quantitative methods should be promising to detect and estimate AF events and clinical parameters.

Molecular-level AF simulation—Molecular-level quantitative models can be important for the accurate simulation of AF. Any such models should include a consideration of all observed electrophysiologic phenomena. The elaborate molecular changes in AF are known to be directed primarily at protecting the myocyte from cellular stress [82]. However, this early protection occurs at the expense of electrophysiological changes that promote the long-term maintenance of AF. Occurrence of arrhythmia leads to alterations in potassium and calcium currents that likely cause a decreased APD, and a decreased APD rate adaptation [36]. Increased diastolic sarcoplasmic reticulum Ca^{2+} leak, and the related delayed after-depolarizations/triggered activity, promote cellular arrhythmogenesis in paroxysmal AF patients [83]. Sustained atrial activation and AF-induced electrical remodeling is associated with reductions in transient outward current (I_{to}), ultrarapid delayed rectifier current (I_{Kur}), and L-type calcium current ($I_{Ca,L}$) [8,84,85]. The reduction in $I_{Ca,L}$ alone can account for many morphological features of AF action potentials. Chronic rapid activation of the substrate also alters atrial ion channel gene expression, changing ionic currents so as to promote AF onset. To study AF pathophysiology in order to determine the molecular basis and the contribution of ion currents, animal models have also been used [86].

Whole-chamber AF modeling—Although mathematical models of cardiac electrical excitation at the molecular level are accurate to reproduced observed electrophysiologic phenomena, they have become increasingly complex and computationally expensive [16]. It is difficult to simulate AF for long time periods using state-of-the-art molecular-level models at current computational speeds. Although cellular automata are limited in their ability to reproduce electrophysiologic parameters during AF, they may be useful to show general concepts. In the more sophisticated such models, a sensitivity to the previous rate of activation is imparted to form the restitution parameter of a cell [16]. In one such realistic model, the stochastic initiation of AF arising from bursts of spontaneous activation near the simulated pulmonary veins, and its spontaneous termination with dependence on past AF trajectory has been shown [16]. The design of an automata model of activation wavefront propagation on an anisotropic structure has been developed to mimic the branching network of heart muscle cells [11]. This integration has been utilized to demonstrate how AF emerges spontaneously when the transverse cell-to-cell coupling decreases [11]. It has also been used to elucidate the stochastic nature of progressive transversal uncoupling of muscle strands (e.g., due to fibrosis or gap junctional remodeling), as occurs with age, resulting in variability in AF episode onset time, frequency, duration, burden, and progression between individuals [12]. Using a simple cellular automata model of AF, a method by which re-entrant drivers can be located quickly and accurately using a collection of indirect electrogram measurements has been demonstrated [54]. These simplified representations of atrial electrical activity reduced computational cost.

Although further simplification of whole-chamber atrial electrophysiology is imperfect, it may be useful to show the timing of AF events [13–15]. As an example, after simulated premature stimulation on a 576×576 grid with anisotropy, a refractory gradient, and simulated nonconducting collagen fibers, it has been shown that synthetic fibrillatory activity can commence (Figure 3A). Early-to-late activation is colored from red to violet in the panel. Both rotational features and freestanding wavelets are evident. These features are in part formed and stabilize by the presence of simulated nonconducting fibers. Imparting simulated patch ablation lesions (black squares, Figure 3B), the remaining wavefronts after simulated ablation tend to reside further apart. If simulated linear ablation lesions are imparted to the grid (black lines, Figure 3C), wavefront spatial density also diminishes. The cause of this phenomenon, determined from timing considerations, is diagramized in Figure 4. A gradient of long-to-short refractory period exists from top-to-bottom. When a patch ablation lesion eliminates a rotational feature (Figure 4A), proximate rotational features then drive that region (Figure 4B–C), yet at a slower rate. A diminished activation rate occurs because the top driver spins slowly due to its longer refractory period, while the bottom driver spins more rapidly due to its short refractory period, but this latter event causes 2:1 conduction alternans into the center region where ablation was imparted. Similarly, when linear ablation lesions are applied to the center region, they shield portions of it from activation by its local driver, so that peripheral rotational features activate the center region instead, again at a slower rate. Similarly, during actual EP lab ablation, a number of studies have suggested that activation rate in the atrium decreases during catheter ablation [87,88].

In recent work with this automata, the contribution of simulated APD dispersion, or variation in refractory period, to AF onset and maintenance has been shown and it is similar to what is found in an animal model of AF [28]. In Figure 5, S1-S2 stimuli in a substrate lacking simulated fibrosis but with a refractory period gradient is shown (panel A: refractory period gradient, B-C: propagation of the S1-S2 stimulus wavefronts. However, fibrillatory activity does not occur. Yet, if a random component is added to the refractory period gradient, analogous to APD dispersion (panel D), then after S1-S2 stimulation there is onset of fibrillatory activity (panels E-F). The timing of the spatially heterogeneous refractory period enables progression of wavefronts around areas of functional block, causing synthetic reentrant pathways. Hence, such work may be useful to suggest timing relationships which may be helpful in understanding actual AF events.

Summary and Conclusions

In this review, issues concerning the utility of quantitative methods for the analysis of fibrillatory activity as they pertain to AF were discussed. To date, some electrogram time series and frequency measurements have already been found useful to discern and distinguish AF characteristics by quantitation. Furthermore, some events observed in AF can already be simulated by quantitative models. Yet to the present time, many observed AF events are not adequately synthesized by modeling. For example, atrial fiber direction throughout the myocardium is often not included in quantitative modeling, but might be contributive to improve accuracy [89]. With more accurate modeling, it could then be possible to further develop and test hypotheses concerning AF mechanisms. One overwhelming question as yet to be addressed is how AF can progress from the paroxysmal to persistent state, and then to the permanent type in some patients. Perhaps there is an increasing density of drivers, which could enhance activation pattern complexity and contribute to the persistence of arrhythmia. Yet, testing this hypothesis will require more detailed modeling. Successful simulation of observed events by modelling may lead to more efficacious hypothesis testing in the electrophysiology lab, to improve understanding of AF type, and its ability to be terminated via catheter ablation.

Another major goal pertaining to quantitative modeling, as yet unaddressed, is to develop a simulation that can determine, from electrogram time series, the local characteristics of fibrosis, myofibril disarray [90], and APD, which can be important contributors to arrhythmia. This might involve determining whether spectral properties are correlated to optimal candidate driver locations, as has been suggested [91–93]. The process of quantitative modeling and analysis of AF is promising, and is rapidly proceeding. New algorithms are being developed to map microreentrant circuits sustaining fibrillatory activity [94]. Atrial fibrillation can now be distinguished from sinus rhythm using elegant classification algorithms [95]. Machine learning techniques offer potentially new avenues to gain additional insight into the wealth of highly complex spatiotemporal information that is present during fibrillatory activity [96,97]. Nascent, multiscale atrial models have the ability to incorporate high levels of detail of the atrial anatomy, the tissue ultrastructure, and fibrosis distribution [6]. Simulations using such models have demonstrated how an atrial fibrotic substrate and altered atrial electrophysiology might contribute in some cases to the onset and maintenance of AF [6]. Further advancements in quantitative methodology, such

as by machine learning [97–99], should be beneficial for better understanding AF mechanisms, the transition from paroxysmal to persistent and permanent AF, when it occurs, and how ablation lesion location and shape, among other procedures, can best be employed to prevent recurrence, minimize laboratory procedure time and invasiveness, and reduce procedural costs and patient morbidity.

Acknowledgments

Dr. Peters acknowledges funding from the British Heart Foundation (RG/16/3/32175 and Centre of Research Excellence), Rosetrees Trust, and the National Institute for Health Research (UK) Biomedical Research Centre.

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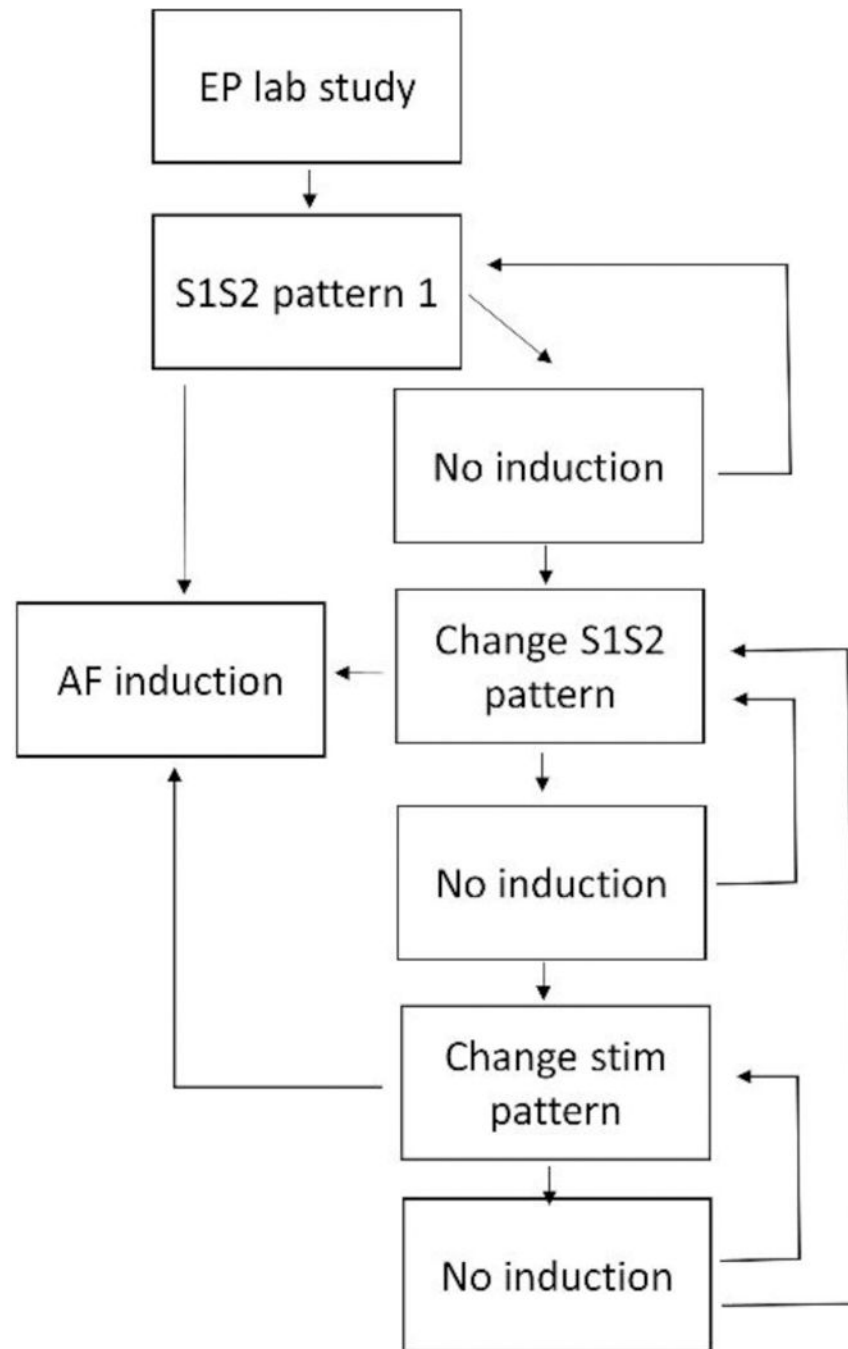
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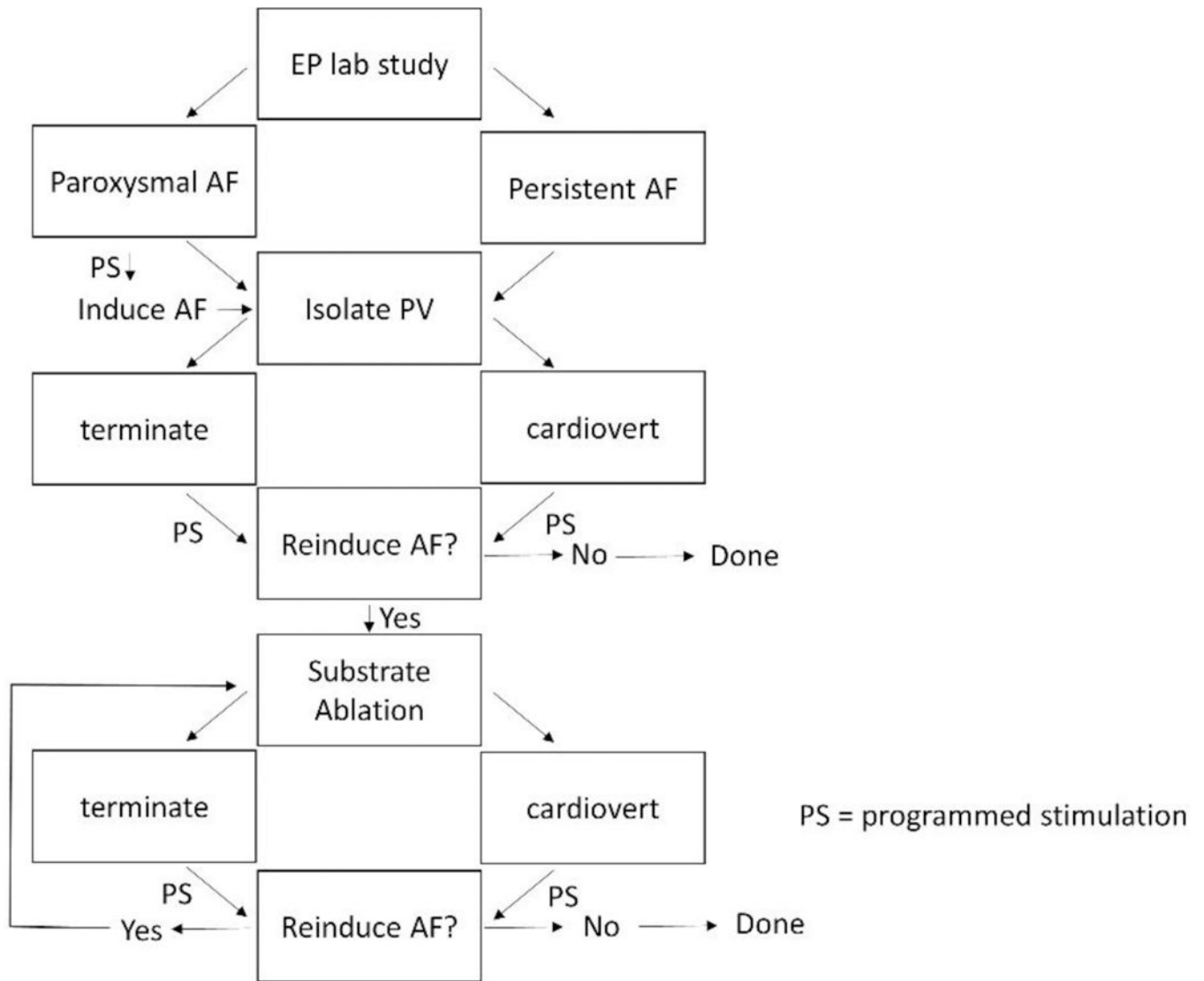
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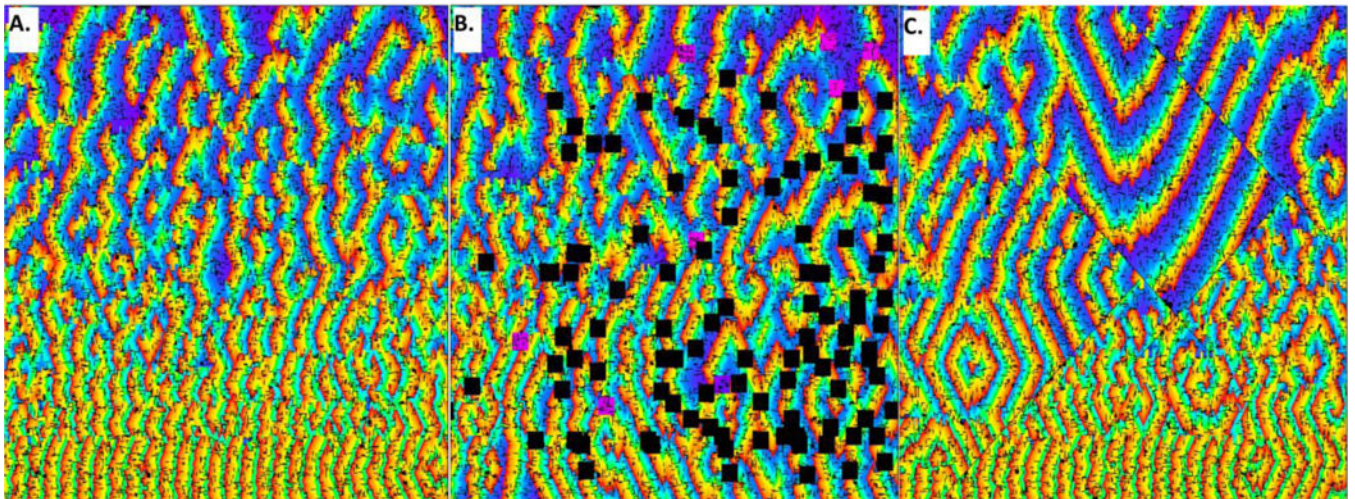
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1. Block diagram of the procedure to induce atrial fibrillation in paroxysmal patients. Various coupling intervals of S1 and S2 pulses are utilized until AF is induced from a particular programmed stimulation site. If these attempts fail, IV isuprel may be administered, and the stimulating electrode is moved to another location and the process repeated. The procedure is repetitive and time-consuming, because little is known regarding the best stimulation sequence to employ, and the events occurring during stimulation are not very repeatable.

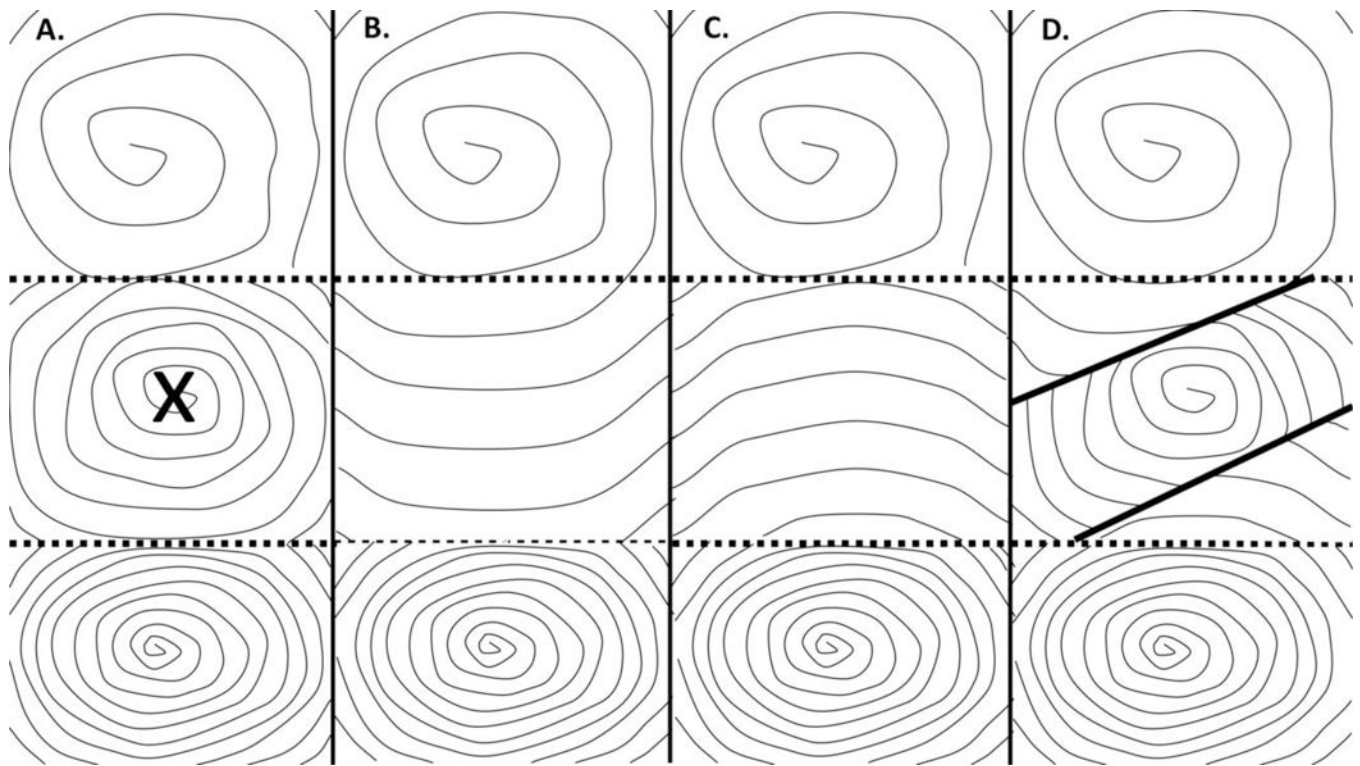


2. Block diagram showing how drivers are eliminated in paroxysmal and persistent AF. Even after ablating suspected driver locations, atrial fibrillation may still need to be terminated in both types of patients. Once atrial fibrillation is terminated, further induction of arrhythmia is attempted, following the paradigm shown in Figure 1. The process is repeated until atrial fibrillation can no longer be induced. The procedure is time-consuming and not always successful, because what to ablate and where to ablate to eliminate drivers is often uncertain.



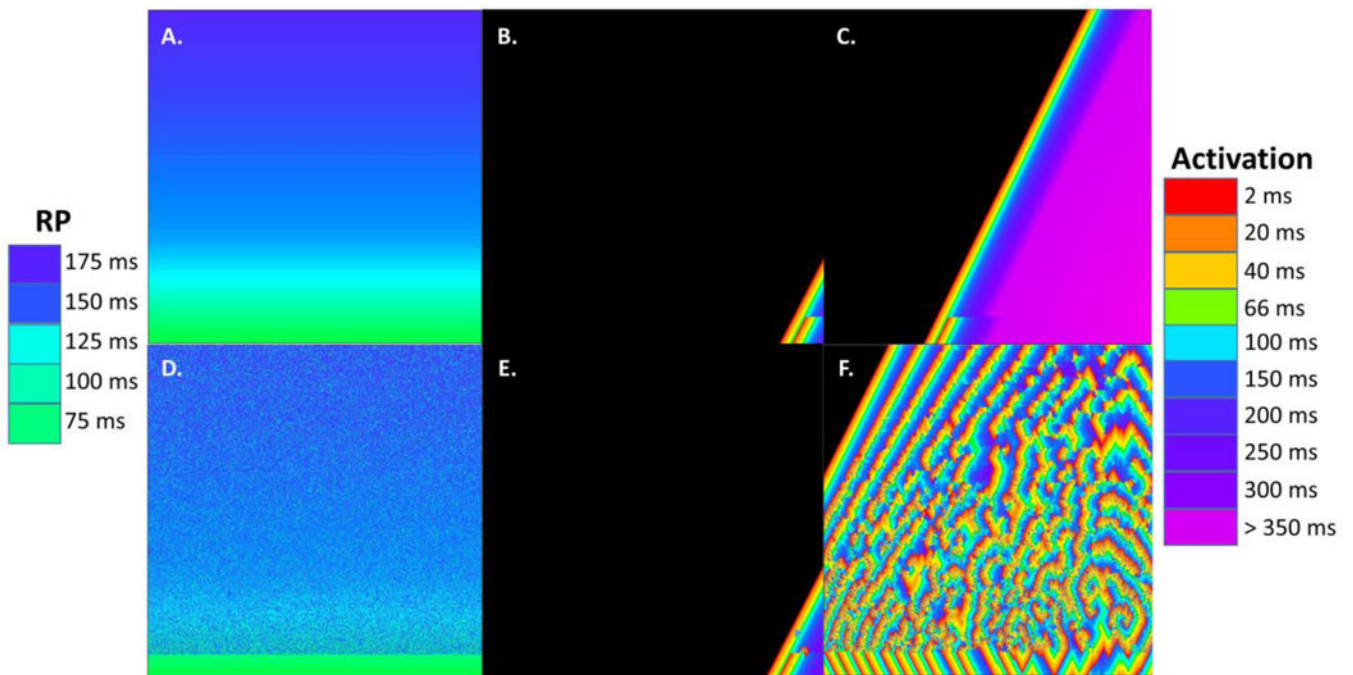
3.

In this simulation, an automata grid is used to simulate fibrillatory activity. A refractory gradient of long to short (175 ms to 75 ms) is present from top to bottom, Panel A. There is 2:1 anisotropic conduction in the vertical versus horizontal directions. Minute fibers are evident as short thin black lines, randomly distributed about the grid to simulate fibrosis. The fibrillatory activity evident in panel A occurs prior to any simulated ablation. In panel B, patch ablation lesions of dimension 20×20 nodes were imparted, illustrated as black squares, at locations where vortices had been evident. There is a loss in the density of activation wavefronts in panel B, and a greater surface area of obstacles to conduction as compared with panel A. This causes prolongation of the mean global cycle length for grid activation, evident as a change in background color, with more blue and violet in panel B. Linear ablation (thin black lines marked by interruption in the activation wave direction and spacing) also impede or eliminate the propagation of local driver wavefronts (panel C). Prolonged activation intervals are evident due to the presence of the linear lesions, which can shield areas from their local drivers, as is particularly evident in the upper portion of panel C.



4.

Diagram showing how ablation lesions affect local cycle length for activation, based on timing considerations as addressed by the cellular automaton. A. rectangular (patch) ablation lesions, marked with an x. This will eliminate the center rotational driver. B. The middle region is now activated at a slower rate by the top driver. C. Alternatively, the middle region is now activated at a slower rate by the lower driver with 2:1 conduction alternans into the center region. D. In this panel, simulated linear ablation (thick lines) are applied in proximity to the center rotational driver. Areas then shielded from the center driver are then driven at a slower rate by the drivers at top and bottom of the panel.



5.

Illustration of the effect of random refractory period changes on simulated fibrillatory activity, cellular automata model. A. The gradient in refractory period ranges from 175 ms (top) to 75 ms (bottom), scale at left. B. An S1-S2 stimuli is applied at the lower right hand corner grid node. The wavefront to the left is S1 and to the right is S2, with the leading edge of each colored red for earliest activation (scale at right). S2 blocks where the refractory period becomes longer than the S1-S2 coupling interval. C. The wavefronts proceed to the opposite side of the grid without occurrence of fibrillatory activity. Since simulated fibrosis was not added, there is nothing to delay the S2 wavefront so that rotational features can form. D. Some grid nodes have been randomly changed in refractory period value as compared with panel A. E. S1-S2 stimuli are imparted to the right hand corner of the grid using the refractory period pattern of panel D. F. Because of the random refractory period imposed in the gradient pattern, functional block occurs at random grid nodes, which in some cases provides sufficient delay so that reentry of the wavefront occurs. The result is a fibrillatory pattern, albeit different from that of Figure 3A.