

# Dynamic Regional Phase Synchrony (DRePS): An Instantaneous Measure of Local fMRI Connectivity Within Spatially Clustered Brain Areas

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**Abstract:** Dynamic functional brain connectivity analysis is a fast expanding field in computational neuroscience research with the promise of elucidating brain network interactions. Sliding temporal window based approaches are commonly used in order to explore dynamic behavior of brain networks in task-free functional magnetic resonance imaging (fMRI) data. However, the low effective temporal resolution of sliding window methods fail to capture the full dynamics of brain activity at each time point. These also require subjective decisions regarding window size and window overlap. In this study, we introduce dynamic regional phase synchrony (DRePS), a novel analysis approach that measures mean local instantaneous phase coherence within adjacent fMRI voxels. We evaluate the DRePS framework on simulated data showing that the proposed measure is able to estimate synchrony at higher temporal resolution than sliding windows of local connectivity. We applied DRePS analysis to task-free fMRI data of 20 control subjects, revealing ultra-slow dynamics of local connectivity in different brain areas. Spatial clustering based on the DRePS feature time series reveals biologically congruent local phase synchrony networks (LPSNs). Taken together, our results demonstrate three main findings. Firstly, DRePS has increased temporal sensitivity compared to sliding window correlation analysis in capturing locally synchronous events. Secondly, DRePS of task-free fMRI reveals ultra-slow fluctuations of  $\sim 0.002$ – $0.02$  Hz. Lastly, LPSNs provide plausible spatial information about time-varying brain local phase synchrony. With the DRePS method, we introduce a framework for interrogating brain local connectivity, which can potentially provide biomarkers of human brain function in health and disease. *Hum Brain Mapp* 37:1970–1985, 2016. © 2016 Wiley Periodicals, Inc.

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## INTRODUCTION

The human brain can be modeled as a collection of complex functional networks containing interconnected “nodes” that are dynamically interacting with each other on local and global scales [Bullmore and Sporns, 2009; Rubinov and Sporns, 2010; Sporns, 2011]. Non-invasive neuroimaging methods including functional magnetic resonance imaging (fMRI) have been used to understand such brain network interactions. In this context, task-free fMRI is a functional brain imaging technique with high spatial resolution, measuring blood oxygenation level dependent (BOLD) changes in response to spontaneous neural activity [Biswal et al., 1995]. The temporal resolution of fMRI data is determined by its repetition time ( $T_R$ ) parameter associated with the time interval between successive excitation pulse sequences applied to the same brain slice. This is the optimal time accuracy which one can reach to investigate the dynamics of brain functionality through BOLD changes.

Improving our knowledge of local network behaviour at a macroscopic level is important for conceptualizing the human brain as a complex dynamic system. The organization of brain networks are both modular and hierarchical [Park and Friston, 2013]. This hierarchical/modular configuration constitutes a potential ground for integrating local neuronal functions at the global level. From this perspective, brain functionality may be viewed as “global integration of local integrators” where short-range connections are the fundament of specialized functional processing, whilst long-range connections are generally responsible for higher level cognition [Park and Friston, 2013; Sepulcre et al.,

2010]. Brain interactions are also known to be of dynamic nature [Bullmore and Sporns, 2009; Rubinov and Sporns, 2010; Sporns, 2011]. Therefore, it is fair to speculate time-varying spatial distributions of local functional units for brain networks. Similarity assessment of adjacent brain regions during transient spontaneous brain activity at the spatial resolution of fMRI data may aid our understanding of these functional dynamics [Jiang and Zuo, 2015].

Local network properties of task-free fMRI can be examined through different methodologies. Integrated local correlation [Deshpande et al., 2009] is a voxel-wise measure of local coherence in fMRI time series which is applied over the entire length of data. Local functional connectivity density mapping [Tomasi et al., 2014] is another time-constant voxel-wise methodology which searches for the Pearson correlation-based functional connections of a given fMRI voxel until the connectivity edges become lower than a certain threshold. The cross-correlation coefficients of spontaneous low frequency fluctuations index [Li et al., 2002] is a local measure of fMRI connectivity which computes the average cross-correlation between spontaneous low-frequency components of fMRI time series within a region of interest over the scanning time period. Regional homogeneity (ReHo) is based on the Kendall’s coefficient of concordance (KCC-ReHo) [Zang et al., 2004], and evaluates the mean correlation between the fMRI time series at a given voxel and its neighboring voxels. The coherence-based version of KCC-ReHo (cohe-ReHo) [Liu et al., 2010] has also been developed which considers the coherence values of the time series in the frequency domain instead of their temporal correlation (see [Zuo et al., 2013] for more details).

Among the aforementioned methods, KCC-ReHo has found wide acceptance in brain functional connectivity research, as it is a non-parametric data-driven measure with no requirement for Gaussianity of fMRI data, it is computationally fast with minimal parameter settings and is robust to noise [Zuo et al., 2013]. The main limitation of ReHo is the assumption that the dynamics within the brain’s functional networks remains stationary over time. However, there is increasing evidence that dynamics of brain functional connectivity during a task-free situation is nonstationary [Damaraju et al., 2014; Handwerker et al., 2012; Liu and Duyn, 2013; Tailby et al., 2015; Waites et al., 2005; Yu et al., 2015; Zalesky et al., 2014]. In order to mitigate this limitation for KCC-ReHo, a sliding window version (SW-ReHo) has been utilized, requiring the assumption of stationarity in the BOLD signal over only short time periods [Hudetz et al., 2015]. In this approach, the KCC-ReHo measure is successively computed on the

### Abbreviations

AAL	Automated anatomical labeling
BIC	Bayes Information Criterion
BOLD	Blood oxygenation level dependent
Cohe-Reho	Coherence-based regional homogeneity
DRePS	Dynamic regional phase synchrony
fMRI	functional magnetic resonance imaging
GMM	Gaussian mixture modeling
KCC-ReHo	Kendal’s coefficient of concordance
LPSN	Local phase synchrony network
PCA	Principal component analysis
PSD	Power spectral density
ReHo	Regional homogeneity
RMS	Root mean squared
ROI	Regions of interest
RSN	Resting state network
SW-ReHo	Sliding window regional homogeneity

segmented BOLD signal, or on the segmented time courses of spatial independent components. This methodology, however, is subject to the *Uncertainty Principle*, where high temporal resolution can be achieved only at the cost of poor spectral resolution and vice versa [Boashash, 2016].

In this article, we introduce a time-varying measure of local fMRI connectivity, which alleviates some inherent limitations of using short-time sliding segments. The proposed method requires minimal parameter tuning with the benefit of not having to define a window length. Dynamic Regional Phase Synchrony (DRePS) maps are obtained as the (spatial) mean of the instantaneous phase coherence within a local neighborhood of fMRI voxels (e.g., within a spatial extent akin to that used in the ReHo method). We show, through simulation, that DRePS achieves higher temporal resolution than the SW-ReHo approach and investigate its properties within different frequency bands. We also apply DRePS to task-free fMRI data from 20 healthy controls, and test the hypothesis that dynamic local functional connectivity is associated with local phase synchrony networks (LPSNs), within spatially distributed brain areas.

## MATERIALS AND METHODS

We begin with a description of the existing SW-ReHo method, as the approach we subsequently describe shares some features, and we will be comparing results of our framework to those of SW-ReHo.

### Exploring Dynamic Local Connectivity in Task-Free fMRI Data Using SW-ReHo

Regional characteristics of task-free fMRI data have been successfully investigated using the ReHo measure [Liu et al., 2008; Tang et al., 2014; Wang et al., 2012; Zang et al., 2004; Zuo et al., 2013]. ReHo computes average Kendall's coefficient of concordance between the fMRI time series at each voxel and its adjacent voxels within a surrounding 3D cube [Zang et al., 2004]. It returns values from 0 to 1 with higher values implying stronger local connectivity. ReHo can be extended to a nonstationary version using a sliding window approach, SW-ReHo. Sliding window analysis is a widely used way of characterizing variations of spatio-temporal connectivity in BOLD data, as it is easy to implement and interpret [Hutchison et al., 2013]. SW-ReHo is based on shifting a set number of data points in time with a pre-defined overlap while extracting ReHo from each segment. This leads to a series of time-varying features over time. Accuracy of SW-ReHo strongly depends on the choices of window size, window shape and overlapping length. Short-length rectangular windows (i.e., low number of time points) may increase temporal resolution of the feature time series, but it can negatively affect the reliability of ReHo, and reduce the spectral reso-

lution within that window [Zuo et al., 2013]. Overlapping between successive windows can multiply the number of feature points, but the overlapping length nevertheless introduces temporal smoothing to the feature time series. Therefore, development of a time-varying local connectivity measure for task-free fMRI data at  $T_R$ -resolution can improve the temporal precision of brain functionality studies. In the following section, we outline an alternative framework to SW-ReHo based on the concept of instantaneous phase, which evaluates nonstationary local connectivity of BOLD signal changes at  $T_R$ -level with no need for window parameter settings.

### Instantaneous Phase of fMRI Time Series

We propose that instantaneous mean phase coherence between time series of neighboring fMRI voxels can be used as a time-varying measure of brain local connectivity. To this end, we employed the concept of analytic associates based on the Hilbert transform [Sun and Small, 2009] to extract the phase information of fMRI time series. Despite the important role of band-pass filtering in phase synchrony analysis of task-free fMRI data, its theoretical aspects have not yet been systematically investigated in the fMRI literature. The frequency band of 0.03–0.07 Hz has been used in two previous studies of task-free fMRI instantaneous phase synchrony analysis, but its justification has been mainly based on practical considerations of minimizing artifact and noise in the data [Glerean et al., 2012; Ponce-Alvarez et al., 2015]. We take this concept further and discuss the requirements needed for extracting meaningful phase information from nonstationary signals.

A real-valued signal  $x[n]$  can be defined without ambiguity based on its instantaneous amplitude and instantaneous phase as follows [Picinbono, 1997]:

$$x[n] = a_x[n] \cos(\varphi_x[n]), \quad (1)$$

where  $a_x[n]$  and  $\varphi_x[n]$  denote the instantaneous amplitude and phase of  $x[n]$ , respectively. In order to obtain the phase information  $\varphi_x[n]$ , we have to convert the real-valued presentation of Eq. (1) into a complex form. This can be done by estimating  $z_x[n]$ , i.e., the complex analytic associate of  $x[n]$  using the Hilbert transform [Picinbono, 1997; Sun and Small, 2009]:

$$z_x[n] = x[n] + j\tilde{x}[n] \quad (2a)$$

$$= a_x[n] \cos(\varphi_x[n]) + j\mathcal{H}\{a_x[n] \cos(\varphi_x[n])\}, \quad (2b)$$

where  $j = \sqrt{-1}$  and  $\mathcal{H}\{\cdot\}$  means the Hilbert transform. The complex nature of  $z_x[n]$  in the time domain arises from its asymmetric power spectral density (PSD) function having no negative frequency components [Picinbono, 1997]. Extraction of the instantaneous phase signal  $\varphi_x[n]$  from  $z_x$

$[n]$  is straightforward by re-writing Eq. (2a) into the following *quadrature* form:

$$z_x[n] = a_x[n]e^{j\varphi_x[n]}. \quad (3a)$$

$$= a_x[n]\cos(\varphi_x[n]) + ja_x[n]\sin(\varphi_x[n]), \quad (3b)$$

This is, however, only possible if the following relationship is satisfied:

$$\mathcal{H}\{a_x[n]\cos(\varphi_x[n])\} = a_x[n]\sin(\varphi_x[n]). \quad (4)$$

This condition can be examined by using the Bedrosian theorem [Bedrosian, 1963], which deals with the Hilbert transform of the product of two real-valued signals in the time domain. The Bedrosian's requirement states that if two functions  $F_{LP}[n]$  and  $F_{HP}[n]$  have non-overlapping frequency spectra, and the support of the spectrum of  $F_{LP}[n]$  is lower than that of  $F_{HP}[n]$ , then:

$$\mathcal{H}\{F_{LP}[n]F_{HP}[n]\} = F_{LP}[n]\mathcal{H}\{F_{HP}[n]\}. \quad (5)$$

In other words, the low-frequency envelope of the product  $F_{LP}[n]F_{HP}[n]$  can be extracted from its Hilbert transform, but only if  $F_{LP}[n]$  and  $F_{HP}[n]$  meet the Bedrosian's requirement. Eq. (5) is also known as Bedrosian identity [Venouziou and Zhang, 2008].

As a direct application of the Bedrosian theorem, the left side of Eq. (4) can be split into a pair of slow and fast terms, if the amplitude envelope  $a_x[n]$  is low-pass, the phase signal  $\cos(\varphi_x[n])$  is high-pass, and their frequency spectra are distinct [Picinbono, 1997]:

$$\mathcal{H}\{a_x[n]\cos(\varphi_x[n])\} = a_x[n]\mathcal{H}\{\cos(\varphi_x[n])\}. \quad (6)$$

On the other hand, we know from the Hilbert transform properties that  $\mathcal{H}\{\cos[n]\}$  is equal to  $\sin[n]$  over an infinite time interval [Picinbono, 1997]. However, Eq. (6) is not necessarily equivalent with the following equation [Picinbono, 1997] for real-world signals due to their finite-length:

$$\mathcal{H}\{\cos(\varphi_x[n])\} = \sin(\varphi_x[n]). \quad (7)$$

Consequently, we still cannot infer the quadrature form of Eq. (3a) from Eq. (2a) for practical signals, even if they satisfy the Bedrosian's requirement. This implies that for a rigorous evaluation of the credibility of the extracted phase information, one must check both Bedrosian theorem as well as Eq. (7) for the underlying signal. To this end, we computed an error signal  $\epsilon[n]$  based on Eq. (7) as an accuracy indicator of instantaneous phase [Picinbono, 1997]:

$$\epsilon[n] = \cos^2(\varphi_x[n]) + (\mathcal{H}\{\cos(\varphi_x[n])\})^2. \quad (8)$$

In an ideal case of perfect analytic associates, the error signal  $\epsilon[n]$  will be equal to 1.

## Dynamic Regional Phase Synchrony (DRePS) of Task-Free fMRI

Let  $\varphi_x[n]$  and  $\varphi_y[n]$  be the instantaneous phases of signals  $x[n]$  and  $y[n]$ , respectively. The two signals are phase-locked of order 1:1 if [Mormann et al., 2000]:

$$|\varphi_x[n] - \varphi_y[n]| \approx 0. \quad (9)$$

Phase synchronization between  $x[n]$  and  $y[n]$  can then be quantified using the mean phase coherence  $R_{x,y}$  given by [Lachaux et al., 1999; Mormann et al., 2000]:

$$R_{x,y} = \sqrt{\langle \cos(\varphi_x - \varphi_y) \rangle^2 + \langle \sin(\varphi_x - \varphi_y) \rangle^2}. \quad (10)$$

where  $\langle \cdot \rangle$  represents the mean operator.  $R_{x,y}$  is restricted to the interval  $[0,1]$  where  $R_{x,y}=1$  reflects no random phase difference between  $x$  and  $y$ , whilst  $R_{x,y}$  approaches zero when the instantaneous phase difference between the two signals increases.

Now, assume  $\varphi_x[n]$  and  $\varphi_{y_i}[n]$  are the instantaneous phase functions of a band-pass filtered fMRI time series with Bedrosian identity consisting of  $T$  time-points ( $n=1, \dots, T$ ) at a given voxel  $x$  and its neighboring voxels  $y_i$  ( $i=1, \dots, M-1$ ) where  $M$  is the entire number of non-zero voxels within a 3D cube centered at  $x$ . The DRePS measure associated with the voxel  $x$  is then computed as:

$$\psi_x[n] = \frac{1}{M-1} \sqrt{\left\{ \sum_{i=1}^{M-1} \cos(\varphi_x[n] - \varphi_{y_i}[n]) \right\}^2 + \left\{ \sum_{i=1}^{M-1} \sin(\varphi_x[n] - \varphi_{y_i}[n]) \right\}^2}. \quad (11)$$

The function  $\psi_x[n]$  quantifies the instantaneous mean phase coherence between  $x$  and all of its adjacent neighbors within its associated 3D space. In this study, we considered two sizes of 6 and 26 immediate neighboring voxels with respect to the central voxel, in analogy to the ReHo method [Zang et al., 2004]. This calculation was repeated for every gray-matter voxel after exclusion of all zero-value voxels from the neighboring cube. Figure 1 illustrates the schematic procedure of DRePS extraction from a typical 3D cube of size 27.

The DRePS function extracted from a 4D task-free fMRI data will be another 4D map with the same single- $T_R$  temporal resolution. The DRePS time series at each voxel represents its simultaneous relationship with the nearest neighbors. With a gray matter mask containing 51603 voxels and a fMRI data including 200 volumes, our MATLAB implementation of DRePS takes approximately 40 seconds using a GNU/Linux-based PC of 2.66 GHz Intel Quad Core i7 CPU and 8 GB of RAM.

## Analysis of DRePS: Two Scenarios

We developed two separate scenarios for inspecting the DRePS maps:

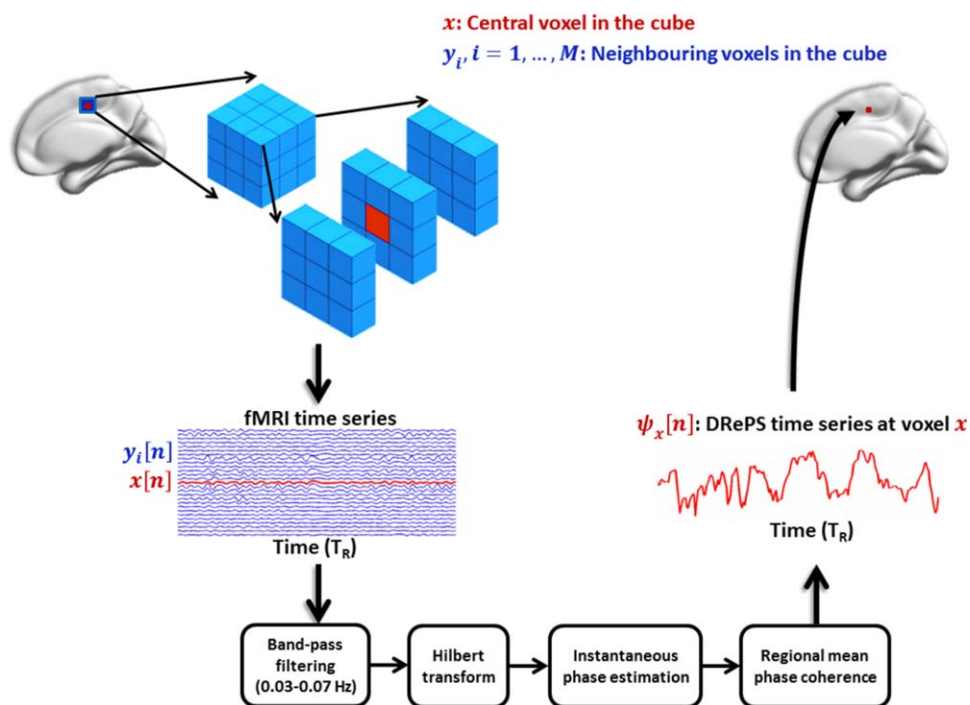


Figure 1.

A schematic example of extracting the DRePS measure  $\psi_x[n]$  from a typical moving  $3 \times 3 \times 3$  cube of fMRI voxels including a central voxel  $x$  (red voxel) and its neighboring voxels  $y_i$ ,  $i = 1, \dots, 26$  (blue voxels). The DRePS time series  $\psi_x[n]$  is obtained by taking

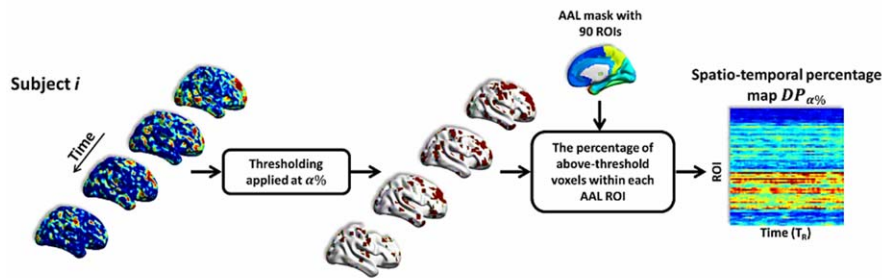
the mean of instantaneous phase coherence between the central voxel  $x$  and its adjacent non-zero neighbors at different time points. [Color figure can be viewed in the online issue, which is available at [wileyonlinelibrary.com](http://wileyonlinelibrary.com).]

**Scenario A:** In the first scenario (Fig. 2A), we aimed to assess how particular brain regions, segmented *a priori*, were locally “engaged” (highly synchronous) or “disengaged” (weakly synchronous) over time. The DRePS time series were directly analyzed using a time-dependent thresholding approach. For each time point, the associated 3D DRePS map was thresholded at the  $\alpha^{\text{th}}$  percentile (here,  $\alpha=95$ ) of its histogram over all voxels (very high regional synchrony). This provided a binary 3D map of voxels surviving the high local connectivity threshold. The 3D binary map was parcellated using an automated anatomical labeling (AAL) atlas [Tzourio-Mazoyer et al., 2002] with 90 regions of interest (ROIs) excluding cerebellum. The percentage of suprathreshold voxels within each ROI (i.e., ratio of ones over the ROI size) was then calculated. A spatio-temporal DRePS percentage plot  $DP_{\alpha\%}$  was obtained for each subject, where the  $x$ -axis was associated with the fMRI volume timing (in  $T_R$ ) and the  $y$ -axis represented the ROI indices (Fig. 2A). Each row in  $DP_{\alpha\%}$  reflects the time-varying quota of a given ROI with high DRePS values.

The significance testing for the  $DP_{\alpha\%}$  maps was done through the surrogate data method by generating 1000 random realizations of the null hypothesis based on the

original DRePS time series. To this end, all time series inside the gray matter mask of each subject-specific 4D DRePS map were re-arranged into a 2D matrix, so that each row was associated with a DRePS time series at a certain voxel. The voxels were then parcellated using the AAL atlas. Each ROI was spatially concatenated over subjects. The concatenated ROIs underwent a permutation testing procedure. At each run, voxels of each concatenated ROI were shuffled and the first set of random voxels with the same size of the underlying ROI was taken. It led to a permuted DRePS map in which the voxels of each ROI and their associated DRePS time series were randomly selected from the group of subjects. This was done to preserve the inherent characteristics of the brain by keeping the same anatomical mask at each permutation, while randomizing the dynamic local network properties over the entire group. The shuffled 4D DRePS maps were subjected to the process of obtaining the  $DP_{\alpha\%}$  maps where each element in the time-space domain was associated with a null distribution of 1000 values. A 2D spatio-temporal map with the same size of  $DP_{\alpha\%}$  was obtained via significance thresholding at the 95<sup>th</sup> percentile of these distributions. The resulting surrogate map was finally used to threshold the subject-specific percentage maps.

Method for scenario A: Percentage of voxels above DRePS threshold within each ROI



Method for scenario B: Decomposing DRePS into Local Phase Synchrony Networks (LPSNs)

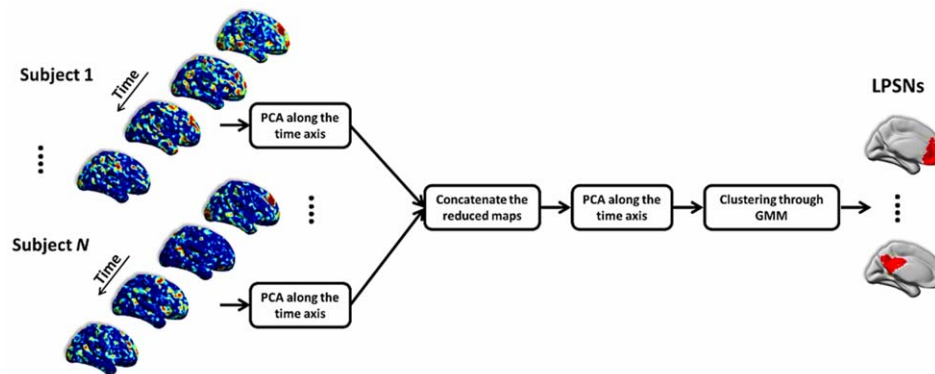


Figure 2.

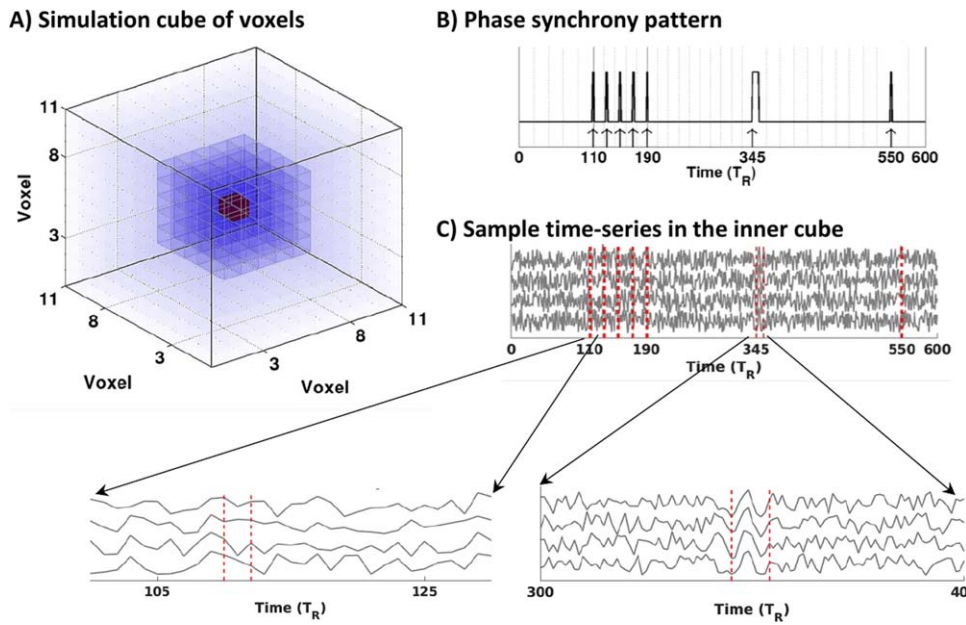
Two scenarios for analysis of DRePS maps: (A) voxels with the most significant DRePS values within each 3D ROI were counted leading to a spatio-temporal DRePS percentage map, (B) reduced DRePS feature vectors were spatially clustered using Gaussian Mixture Modeling (GMM) resulting in communities of local oscillators in fMRI data called local phase synchrony networks (LPSNs). [Color figure can be viewed in the online issue, which is available at [wileyonlinelibrary.com](http://wileyonlinelibrary.com).]

**Scenario B:** In the second scenario (Fig. 2B), we hypothesized that communities of locally synchronous oscillators within the brain are linked to functional brain activity. Therefore, dimensions of maximal variance in the DRePS data may convey meaningful information about local dynamics of task-free fMRI data, and one could use this information to segment the brain *a posteriori* into functionally related regions. From this perspective, each DRePS time series (one per voxel) was treated as a feature vector. A two-step dimension reduction using principal component analysis (PCA) was conducted. The first step was done at the subject level where the DRePS temporal dimension was reduced from 200 (number of volumes for each subject) to 30. After dimensionality reduction of each individual's 4D DRePS map, they were temporally concatenated over the group of subjects and fed into another PCA with a further reduction to 30 dimensions. The number of principal components was chosen by checking the cumulative sum of eigenvalues. In order to determine the intrinsic grouping in the reduced 'DRePS feature vectors', a clustering procedure was applied to the data using Gaussian mixture modeling (GMM) [McLachlan and Peel, 2000].

With GMM, we assume that the data points are generated from a mixture of multi-dimensional Gaussian distributions whose unknown parameters could be estimated using the iterative Expectation-Maximization algorithm [McLachlan and Peel, 2000]. GMM was performed over a range of model orders (i.e., number of Gaussians) for which the goodness-of-fit was evaluated using Bayes Information Criterion (BIC). The optimum order was then selected as the model order with minimal BIC. The GMM procedure resulted in spatial clusters of voxels with similar DRePS characteristics called local phase synchrony networks (LPSNs).

In order to evaluate spatial overlap between LPSNs and commonly reported resting state networks (RSNs) in fMRI data of healthy subjects, we compared the LPSNs (25, as determined by BIC) obtained from within the frequency band of 0.03–0.07 Hz and cube size of 27 with 21 RSNs provided by another independent study in the same space (i.e., MNI<sup>1</sup>) [Smith et al., 2012]. Since selecting the RSNs

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**Figure 3.**

Simulated data: **(A)** 3D arrangement of voxels in the simulated data. The inner compartment of time series with phase synchrony pattern has been highlighted with greater opacity. The central voxel has been shown in red, **(B)** phase synchrony pattern  $M[n]$ , **(C)** four representative time-series extracted from the inner cube. [Color figure can be viewed in the online issue, which is available at [wileyonlinelibrary.com](http://wileyonlinelibrary.com).]

through independent component analysis of our own cohort would be a fairly subjective procedure, we chose to use a set of publicly available and reliable RSNs in our study for the sake of objective and reproducible comparison. The RSNs were acquired from 42 10-minute fMRI datasets of 5 subjects in 7 sessions<sup>2</sup>. Each RSN was binarized by thresholding values above two standard deviations of its voxel values. Pair-wise Jaccard indices were then computed between the LPSNs and binarized RSNs to quantify the similarity and diversity of spatial patterns among them.

### Simulation

We created a 3D simulated data representing random phase relationships between synthetic voxels as well as random patterns of phase synchrony with time-varying attributes in order to:

1. Evaluate the capability of DRePS for tracking local phase synchrony changes at sample-rate resolution,

<sup>2</sup>Publicly available at: [http://www.fmrib.ox.ac.uk/analysis/TFMs/sICA22\\_RSN21.nii.gz](http://www.fmrib.ox.ac.uk/analysis/TFMs/sICA22_RSN21.nii.gz). Data were made available by the WU-Minn Human Connectome Project (1U54MH091657), funded by the 16 NIH Institutes and Centers that Support the NIH Blueprint for Neuroscience Research.

2. Compare the temporal resolution of instantaneous features generated by DRePS, and window-based dynamic features obtained by SW-ReHo for representation of sudden changes in local phase synchrony,
3. Investigate the effects of the number of adjacent voxels and band pass filtering used in the DRePS calculation.

To this end, we generated a 4D array of size  $11 \times 11 \times 11 \times 600$  including an inner compartment of size  $5 \times 5 \times 5 \times 600$  where the first three dimensions represent a spatial volume (Fig. 3A) and the fourth dimension is time (in  $T_R$ , here 3 s). The time series at each voxel  $i$  outside of the inner cube was made of pure background activity  $b_i[n]$ . Each voxel  $j$  in the inner cube was associated with a time series  $x_j[n]$  consisting of two components: background activity  $b_j[n]$  and synchronous activity  $s_j[n]$  masked by  $M[n]$  (Fig. 3B) and elevated by the factor of 2 to resemble amplitude changes. The signals  $b_i[n]$ ,  $s_i[n]$  and  $x_i[n]$  are defined as follows:

$$\begin{cases} b_i[n] = \sin(2\pi f_i^b n + \phi_i^b[n]) + \eta[n], f_i^b \in [0 \ 0.16] \text{ Hz}, \\ -\pi < \phi_i^b[n] < \pi \\ s_i[n] = 2 \times \sin(2\pi f_c n) + \eta[n], f_c = 0.05 \text{ Hz} \\ x_i[n] = b_i[n] + s_i[n] \times M[n], n = 1, \dots, 600 \text{ (in } T_R) \end{cases} \quad (12)$$

where  $\eta[n]$  is additive uniform noise between 0 and 1,  $f_i^b$  is a normally distributed random frequency within the range

of 0 to  $1/(2T_R) \approx 0.16$  Hz,  $\phi_i^b[n]$  is time-varying random phase with maximum variation over the unit circle and  $f_c$  is a voxel-independent central frequency locked to 0.05 Hz. Intuitively, voxels inside the inner cube follow a synchronous pattern governed by  $M[n]$ , while the phase entrainment between voxels outside of the inner cube is purely random. Figure 3C illustrates an example of four representative time series extracted from the inner cube. In the figure, the phase synchrony mask  $M[n]$  represents a block of five equidistance single- $T_R$  events distributing over  $t = 330$  s to  $t = 570$  s, an individual event starting at  $t = 1035$  s and a single- $T_R$  event at  $t = 1650$  s.

The simulated data was examined by DRePS and SW-ReHo methods within a wide frequency band of 0.01–0.09 Hz and a narrow frequency band of 0.03–0.07 Hz as well as two moving cubes of 6 and 26 neighboring voxels. The generated data may not necessarily represent the same natural signatures of real fMRI data, but it intends to show the basic idea behind the DRePS analysis procedure.

### Subjects and fMRI Scanning Procedure

fMRI data of 20 healthy controls (mean age:  $32.4 \pm 10$  y, 6 female) were used in this study. All subjects were scanned with Siemens (Erlangen, Germany) 3T Trio/Skyra scanners while not performing any specific mental task with eyes closed, and were asked to remain awake. Functional data were acquired using an EPI sequence with 44 interleaved 3 mm slices,  $T_R = 3$  s,  $T_E = 30$  ms, flip angle =  $85^\circ$ , voxel size of  $3 \times 3 \times 3$  mm<sup>3</sup> and an acquisition matrix of  $72 \times 72$ .  $T_1$  weighted images were also acquired following the functional scans. A total of 200 volumes of task-free fMRI data were used for all subjects. The study was approved by the Austin Health Human Research Ethics Committee and all subjects gave written informed consent to participate in the study.

### fMRI Data Preprocessing

In the preprocessing pipeline we used SPM8 (<http://www.fil.ion.ucl.ac.uk/spm/software/spm8/>) and DPARSF [Chao-Gan and Yu-Feng, 2010] in MATLAB R2013b (MathWorks Inc., Natick, Massachusetts, United States). Steps included slice timing correction, re-alignment, coregistration to subject's own  $T_1$  weighted images followed by spatial normalization to the standard MNI space (152-brain average template). The linear trend was removed and white matter and cerebrospinal fluid signals were regressed out from the data. To compensate for head movement inside the MRI scanner, 24 motion re-alignment parameters were linearly regressed out of the data [Friston et al., 1996]. All volumes with head movement above 0.5 mm were omitted and replaced by time points derived using cubic spline temporal interpolation in order to ensure continuous temporal data for all subjects.

Task-free BOLD data of each subject were band-pass filtered within four ranges of 0.01–0.09 Hz, 0.03–0.07 Hz, 0.05–0.09 Hz and 0.03–0.11 Hz. All bands were used for analysis of instantaneous phase (see “Assessing Phase Synchrony Analysis Requirements”) and spectral analysis of DRePS (see “Scenario A: Direct Analysis of DRePS Applied to Real-World fMRI Data”). However, the frequency interval of 0.03–0.07 Hz was chosen for extracting LPSNs when evaluating DRePS as a nonstationary feature of the brain's dynamic local connectivity (see “Scenario B: DRePS as a Nonstationary Feature of the Brain's Dynamic Local Connectivity”). These frequency bands were chosen to cover different bandwidths (0.04 Hz and 0.08 Hz) and central frequencies (0.05 Hz and 0.07 Hz) relevant to the task-free fMRI spectral content.

## RESULTS

### Assessing Phase Synchrony Analysis Requirements

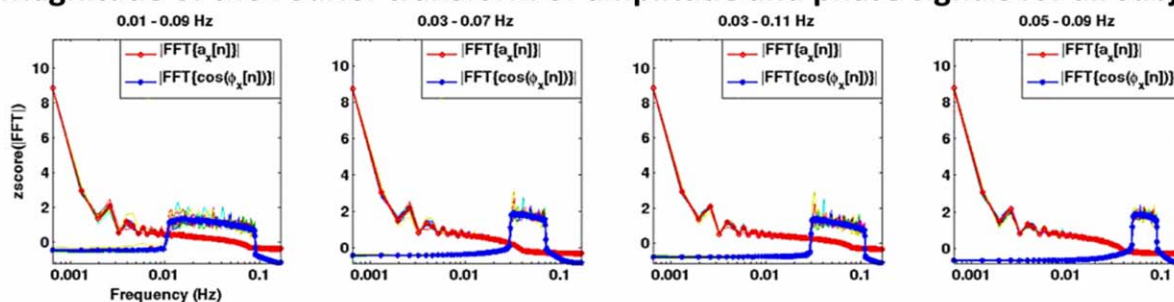
Prior to the DRePS analysis, we examined the Bedrosian's requirement and error signal  $\epsilon[n]$  for the filtered fMRI time series by assessing the low-band and high-band components of their analytic associates (i.e.,  $|\mathcal{F}\{a_x[n]\}|$  and  $|\mathcal{F}\{\cos(\phi_x[n])\}|$  in Eq. (1), respectively where  $\mathcal{F}\{\cdot\}$  means the Fourier transform and  $|\cdot|$  is the magnitude operator). Also, we computed voxel-wise temporal average of the root mean squared (RMS) of the deviations of  $\epsilon[n]$  around 1 and its distribution over all voxels for each band-pass filtered fMRI dataset as a quality indicator of the instantaneous phase signals. Figure 4A illustrates the bandwidths of the z-scored low-pass and high-pass components of analytic associates averaged over voxels for each subject. The grand mean spectra are also overlaid on the subject-specific curves. Although the narrower bands (i.e., 0.03–0.07 Hz and 0.05–0.09 Hz) represent larger separation of the low-pass/high-pass components, a fairly clear distinction can also be observed for wider bands of 0.01–0.09 Hz and 0.03–0.11 Hz. In other words, the Bedrosian's requirement is still relatively retained after applying a wider filtering to the task-free fMRI data in the DRePS framework. This observation is again verified by estimating the error signals of four band-pass filters illustrated in Fig. 4B, where  $\epsilon[n]$  is roughly fluctuating around 1 for the bands 0.01–0.09 Hz and 0.03–0.11 Hz with RMS error percentages below 20%. The relevance of these frequency bands for DRePS analysis of task-free fMRI data, considering the majority of BOLD information within 0.01–0.1 Hz [Biswal et al., 1995], is also shown in “Scenario A: Direct Analysis of DRePS Applied to Real-World fMRI Data”.

### Simulation Results

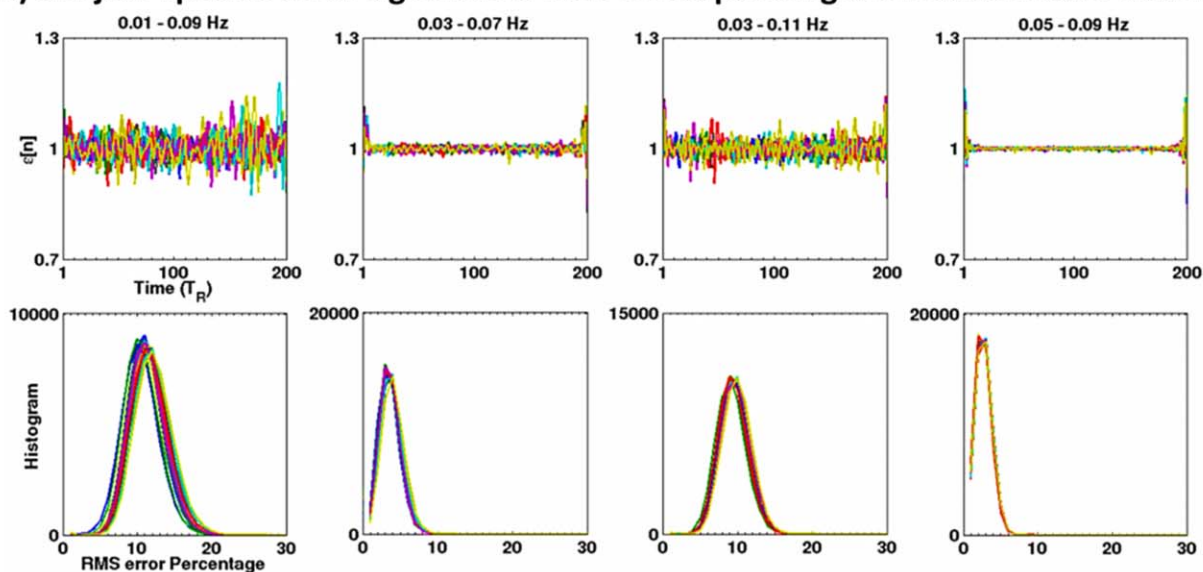
Figure 5 illustrates the spatio-temporal local connectivity maps of time series of the inner cube within the simulated



**A) Magnitude of the Fourier transform of amplitude and phase signals for all subjects**



**B) Subject-specific error signals and their corresponding distributions over voxels**



**Figure 4.**

(A) Bandwidths of the low-pass and high-pass components of analytic associates [see Eq. (1)] averaged over voxels of each subject. Each subject-specific curve is illustrated with a single color and the grand mean spectra are shown in bold. The y-label  $zscore(|FFT|)$  means the magnitude of the Fourier transform converted into the z-score over frequency bins (zero mean and unit variance). Whilst the wider bands exhibit a smaller separation between the low-pass and high-pass components compared to

the narrower bands, Bedrosian's requirement still remains satisfied. (B) Subject-specific averages of the error signal  $\epsilon[n]$  over all voxels for the analytic associates of fMRI data within four frequency bands (top row) and their corresponding distributions of the RMS of their deviation from one (bottom row). In all panels, each subject-specific curve is illustrated with a unique color. [Color figure can be viewed in the online issue, which is available at [wileyonlinelibrary.com](http://wileyonlinelibrary.com).]

data obtained by DRePS (Fig. 5A) and SW-ReHo approach using a rectangular sliding window of length  $20T_R$ 's (Fig. 5B). For both methods, a moving cube of 26 neighboring voxels (i.e., 27 voxels in total) and band-pass filtering of 0.03–0.07 Hz were used. In both maps, the y-axis has been sorted based on the Euclidian distance between non-central voxels within the inner cube and the central voxel (red voxel in Fig. 3A) where 0 represents the central voxel and symmetric positive/negative values are associated with equidistant voxels to the center. The rectangular patterns in the SW-ReHo time series of Fig. 5B reflect the impact of windowing on the short-time local connectivity

estimates: all events shorter than a window length are treated as if they have the same temporal attribute (e.g., last two single events in the map). Also, adjacent events cannot be differentiated temporally if they are close to each other, as seen for the block of events in Fig. 5B. Furthermore, the sliding window approach fails to provide dynamic connectivity information for half the window width each at the beginning and end of the entire time span due to the window length. In contrast, the spatio-temporal DRePS map of Fig. 5A demonstrates  $T_R$ -resolution accuracy in tracking phase synchrony changes among voxels. The salt-and-pepper noise over the connectivity

### Phase synchrony pattern

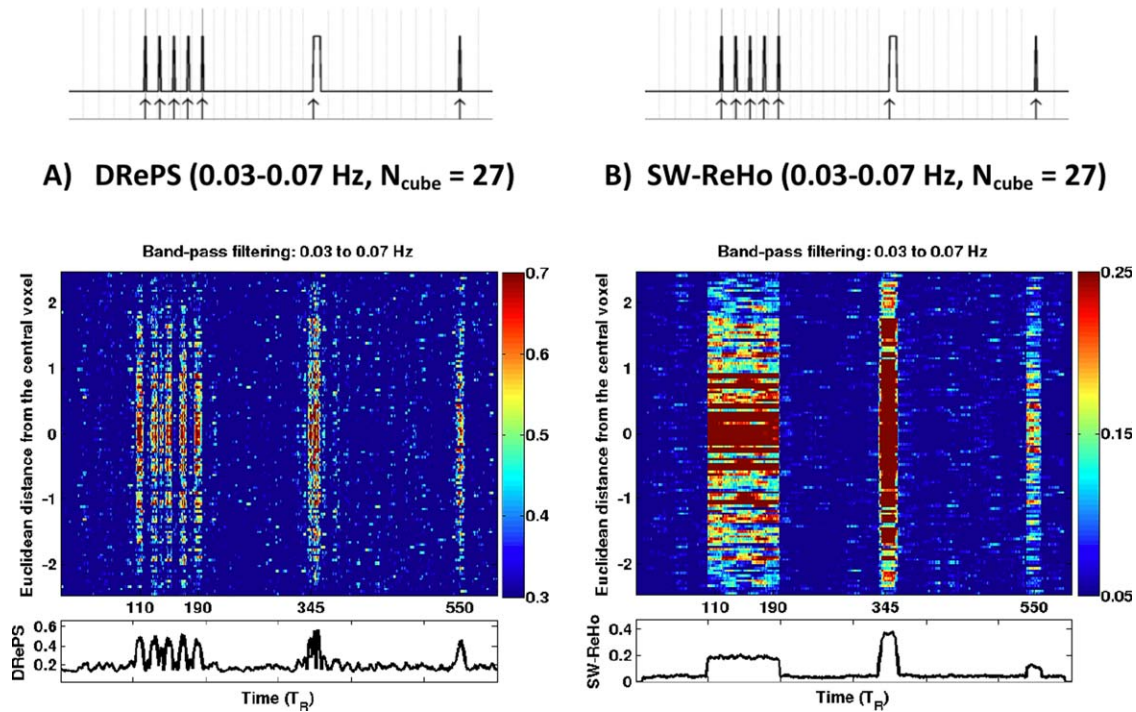


Figure 5.

Simulation results: spatio-temporal local connectivity maps associated with the voxels inside the inner cube of simulated data (Fig. 3A) obtained from the DRePS method (A) and the SW-ReHo method (B) using the band-pass filtering of 0.03–0.07 Hz and neighboring size of 26. For each map, the horizontal profile (i.e., averaging over voxels) is presented at the bottom. DRePS

map obtained by the SW-ReHo approach is more noticeable than DRePS due to its inherent temporal averaging. For both SW-ReHo and DRePS, a fading pattern is observed in the vertical profile (along the y-axis projection) from the central voxel towards the inner cube boundaries. This is expected because of the decrease in the number of synchronous time series within the moving cube of  $3 \times 3 \times 3$  adjacent voxels in both methods when shifting towards the boundaries, resulting in a reduction in the local connectivity estimates.

The effect of band-pass filtering and internal smoothing (governed by the number of neighboring voxels in the moving cube) on DRePS/SW-ReHo was also investigated through simulations. As Supporting Information Fig. S1 demonstrates, the neighboring size of 6 introduces widespread noise over the whole time-space domain in both DRePS and SW-ReHo maps. Also, switching between narrowband filtering of 0.03–0.07 Hz and wideband filtering of 0.01–0.09 Hz does not impose a significant change on the spatio-temporal maps of the simulated data. Due to the mitigating effect of internal smoothing on the noise

provides far superior temporal resolution than SW-ReHo. The phase synchrony mask  $M[n]$  (see Fig. 3) is given on top of each map for comparison purposes. See also Supporting Information Fig. S1 for simulation results with other choices of band-pass filtering and neighboring size. [Color figure can be viewed in the online issue, which is available at [wileyonlinelibrary.com](http://wileyonlinelibrary.com).]

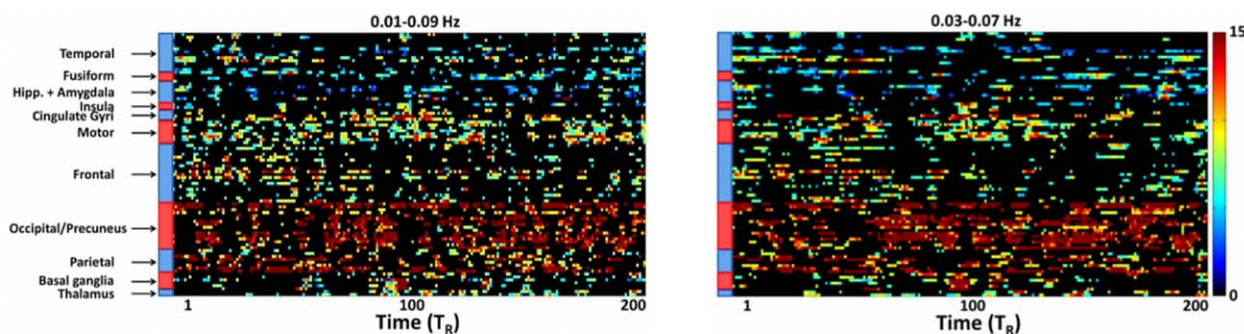
level of DRePS spatio-temporal maps, we chose the neighboring size of 26 for task-free fMRI analysis in the following sections.

#### Scenario A: Direct Analysis of DRePS Applied to Real-World fMRI Data

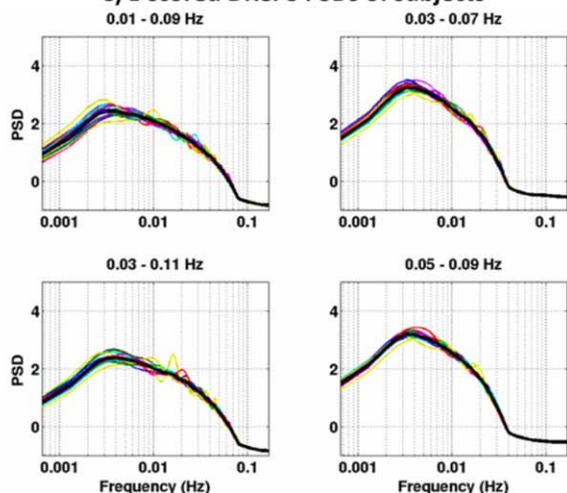
We evaluated the first analysis pipeline delineated in Fig. 2A by applying it to the DRePS 4D maps of 20 healthy control subjects. Figure 6A,B illustrate the  $DP_{95\%}$  plots of a typical subject within two frequency bands of 0.03–0.07 Hz and 0.01–0.09 Hz after statistical testing, where the insignificant data-points have been blacked out. All subjects' thresholded percentage plots can be found in the Supporting Information as a .mat file. The spatio-temporal maps suggest that the highest values in the  $DP_{95\%}$  map are associated with precuneus, occipital and parietal areas (see the horizontal ribbon of high values in Fig. 6A,B).

Figure 6D demonstrates the grand mean spatio-spectral distribution of DRePS time series obtained by averaging subject-specific PSDs over the entire frequency interval

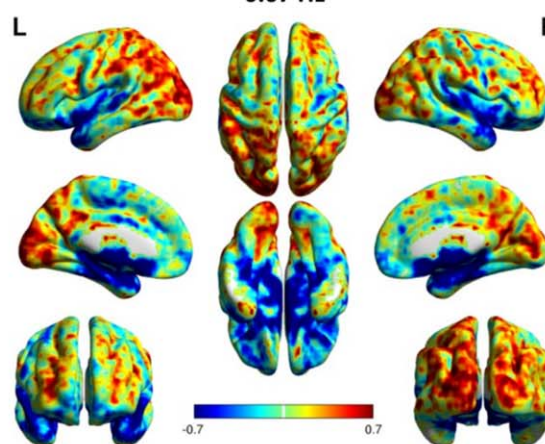
**A, B) Percentage of voxels above DRePS threshold within each ROI (frequency band 0.3-0.7, subject 19)**



**C) z-scored DRePS PSDs of subjects**



**D) PSD distribution of grand mean DRePS within 0.03-0.07 Hz**



**Figure 6.**

(A,B) Analysis of DRePS time series over the control group: Spatio-temporal DRePS percentage plot associated with the voxels above the 95<sup>th</sup> percentile ( $DP_{95\%}$ ) obtained from band-pass filtering of **A)** 0.03–0.07 Hz and **(B)** 0.01–0.09 Hz, after permutation testing, shown for a typical subject. The insignificant values have been blacked out. **(C)** Mean PSD of DRePS time series across all voxels for each subject (colored traces), and grand mean over all subjects (black bold line). The PSD values were normalized to

z-scores at the individual level for easier comparison between subjects, **(D)** Mean power of DRePS time series (band-pass filtering of 0.03–0.07 Hz, neighboring size of 26) across the entire frequency, up to the Nyquist rate of 0.16 Hz for each voxel, then z-scored and averaged across all subjects. See also Supporting Information Fig. S2 for the grand mean PSD spatial maps with other choices of band-pass filtering. [Color figure can be viewed in the online issue, which is available at [wileyonlinelibrary.com](http://wileyonlinelibrary.com).]

$[0 F_s/2]$  Hz where  $F_s=1/3$  Hz. The individual PSDs (thin curves in Fig. 6C) were normalized to z-scores over the frequency bins for easier comparison between subjects. In Fig. 6C, thin curves represent whole-brain mean spatial frequency for each subject. Spatial patterns consistent with the  $DP_{95\%}$  maps (Fig. 6A,B) are also observed in the spatio-spectral distribution of DRePS with higher frequency fluctuations in the visual and parietal areas and lower frequency fluctuations in sub-cortical brain regions (Fig. 6D). There is a consistent peak of ultra-slow DRePS activity within 0.002–0.02 Hz for all subjects as shown in Fig. 6C which is clearly distinct from the frequency band of the filtered BOLD data (i.e., 0.03–0.07 Hz). This ultra-slow signature can be observed for all of the four pass-bands, though

its power decreases by widening the band-pass filter in the DRePS framework (the left column of Fig. 6C vs. the right column). The closely similar spectral properties of DRePS time series within different frequency bands (Fig. 6C) can also be verified by checking the grand mean PSD spatial map of 0.03–0.07 Hz in Fig. 6C and the other corresponding maps in Supporting Information Fig. S2.

**Scenario B: DRePS as a Nonstationary Feature of the Brain’s Dynamic Local Connectivity**

The results of the GMM clustering analysis for DRePS maps obtained through the band-pass filtering of 0.03–0.07

Hz and cube size of 27 are summarized in Fig. 7. Components associated with the minimum of normalized BIC curves suggested a range of  $7.1 \pm 3.4$  clusters at the individual level (Fig. 7A), while this number varied within the range of 20–30 for the group level (Fig. 7B). In order to improve the statistical power of the spatial DRePS clusters, GMM was only applied to the group data. According to the BIC curve of Fig. 7B, after roughly 25 Gaussian components for the group GMM clustering, BIC changes became relatively stable as denoted by a plateau. Therefore, 25 spatial clusters of brain voxels with normally distributed DRePS characteristics were extracted. In Fig. 7C, eight exemplary clusters out of 25 are shown, all with biologically meaningful brain regions. The clusters can be considered as spatial networks of adjacent/remote brain locations with similar local phase synchrony properties. We call these synchronous networks as LPSNs. The selected components also overlap with commonly reported “long-range” RSNs [Hoff et al., 2013]. These include a wide range of networks important in task-free states (precuneus), task-positive states, salient task-switching, visual areas and cortical motor behavior. It may establish a link between networks in which amplitude modulation is typically associated with an active task, and locally synchronous fluctuations of the task-free fMRI data. The full set of 25 LPSNs can be found in Supporting Information as a 4D NIFTI-1 data format file.

Figure 7E demonstrates the pair-wise Jaccard indices between the LPSNs and binarized RSNs [Smith et al., 2012] to quantify the similarity and diversity of spatial patterns in two brain network families. As the similarity matrix suggests, RSNs and LPSNs may overlap across different areas. However, the highest overlap is associated with the primary visual area (RSN1 vs. LPSN11), posterior cingulate cortex (RSN3 vs. LPSN14) and motor areas (RSN5 vs. LPSN20) illustrated in Fig. 7D.

## DISCUSSION

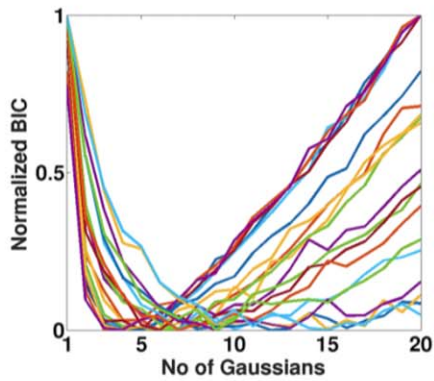
Brain functional connectivity is intrinsically nonstationary [Chang and Glover, 2010; Damaraju et al., 2014; Handwerker et al., 2012; Liu and Duyn, 2013; Yu et al., 2015; Zalesky et al., 2014], and this property is revealed locally at high temporal resolution by DRePS. This important aspect of brain dynamics may be partly ignored if stationary signal processing tools are employed in fMRI connectivity studies. A common way of addressing nonstationarity in fMRI connectivity analysis is to temporally segment it using a fixed-length sliding window. A window has to be short enough to satisfy the assumption of stationarity, but narrow segments fail to provide acceptable localization in the frequency domain. In addition, the window shape can have a non-trivial influence on the spectral signature of functional connectivity results. For example, a rectangular window can introduce a spectral leak to the frequency content of the

segmented BOLD changes and indirectly affect fMRI connectivity metrics. These issues, along with the issue of overlapping length between successive windows, have led to a semi-arbitrary parameter selection paradigm for the sliding window approach in the literature (e.g., see [Allen et al., 2012; Li et al., 2014; Shirer et al., 2011; Yu et al., 2015; Zalesky et al., 2014]). Furthermore, the sliding window approach fails to provide dynamic connectivity information for half the window width each at the beginning and end of the entire time span due to the window length. In contrast to the sliding window approach, the proposed DRePS analysis framework in this article characterizes instantaneous dynamic properties of time-varying local fMRI connectivity at each time point. Based on the simulation results in Fig. 5, temporal resolution of DRePS time series in capturing the number of synchronous events and their time intervals is higher than time-varying ReHo estimates obtained by the sliding window approach. It is noteworthy that brain dynamic connectivity may also be examined by other approaches such as adaptive window length methods or wavelet analysis at wide frequency and temporal scales. These techniques may bring different insight into brain function in contrast to the narrow spectral view of DRePS within short frequency bands. Comparison between the DRePS approach and wide-band dynamic local connectivity methods on the same task-free fMRI data may be an informative avenue of future research. Also, incorporating a non-uniform sampling approach such as point process analysis [Tagliazucchi et al., 2012] to the DRePS framework may act as a data reduction step to further facilitate analysis of time-varying changes of local connectivity in fMRI data.

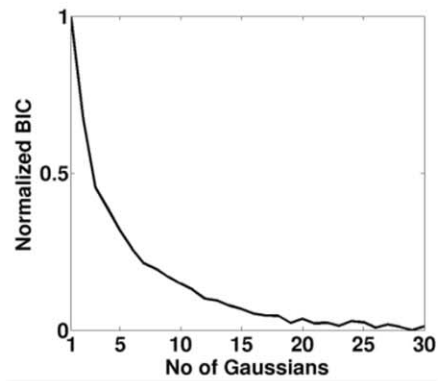
There is evidence that local neuronal activity and long-range functional connectivity in the human brain are related to each other [Park and Friston, 2013; Riedl et al., 2014]. This finding suggests that brain function may be supported by dynamically organizing “local neighborhoods” that transiently share synchronized BOLD activity, and are also synchronized with other distant communities to form large-scale networks [Zang et al., 2004]. This view on local brain connectivity was a motivation for developing DRePS, which quantifies instantaneous regional phase synchronization of BOLD data in a data-driven and model-free way. We hypothesize that dynamic information extracted from DRePS time series may reflect spatial clusters of local oscillators in the brain (Fig. 7C). It remains for further research to examine biological relationships between local neighborhoods and large communities in BOLD changes observed in DRePS maps.

Local cortical connectivity of DRePS was most prominent in primary visual cortex and default mode network areas. This observation may be explained due to the high metabolic demands of these brain regions in the healthy brain [Spetsieris et al., 2015]. Low values of dynamic local functional connectivity were mainly observed within deep sub-cortical brain regions, including the hippocampus and

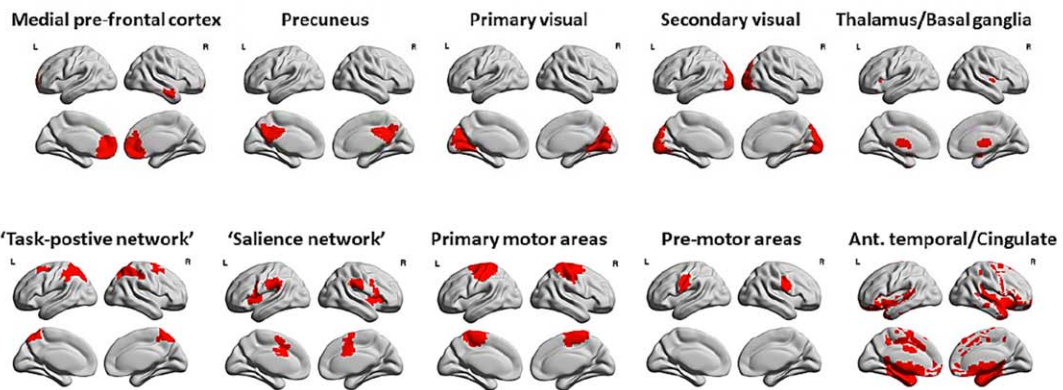
### A) Normalized BIC curves of subjects



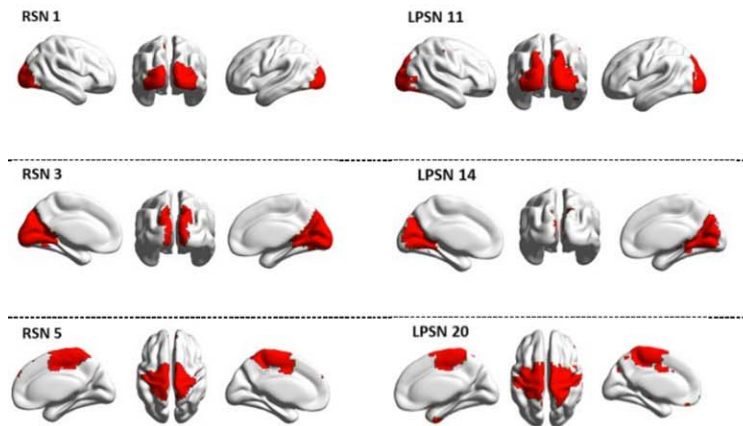
### B) Normalized BIC curve of the group



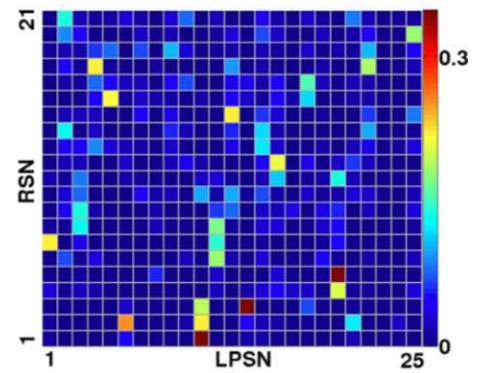
### C) Example LPSNs



### D) LPSNs with highest congruence to RSNs



### E) Jaccard matrix



**Figure 7.**

Analysis results of DRePS maps treated as dynamic feature vectors of the brain's local functional connectivity, (A) BIC curves at the individual level obtained after running GMM for different number of Gaussian clusters, (B) the BIC curve at the group level after running GMM for a range of Gaussian clusters, (C) eight exemplary LPSNs obtained from this study, (D) the most

similar spatial patterns between RSNs and LPSNs based on the Jaccard similarity matrix, (E) The Jaccard similarity matrix between the RSNs provided by [Smith et al., 2012] and the LPSNs obtained as the outcome of GMM at the group level. [Color figure can be viewed in the online issue, which is available at [wileyonlinelibrary.com](http://wileyonlinelibrary.com).]

amygdala (Fig. 6A). Indeed, this suggests that neuronal activity in these regions may not fluctuate synchronously within the frequency band to which DRePS analysis was performed. Song et al. (2014) hypothesized that complex and diverse neural activity occurs even within small volumes, particularly in subcortical areas, and this cannot be captured by local connectivity methods such as ReHo (and possibly, the DRePS method presented here). This is in stark contrast to cortical local connectivity of primary visual cortex and “default-mode” brain nodes. Whether these differences in local connectivity across cortical and subcortical brain regions are an effect of frequencies studied for functional connectivity analysis, or a “neurobiological trait,” requires further attention. This may also originate from a limitation of the DRePS method where the cortical curvatures are ignored by averaging phase difference values over a moving cube of  $\sim 1 \text{ cm}^3$ . However the DRePS approach is not inherently restricted to cube-shaped volumes. For example, following additional validation, it might potentially be applied to regions with anatomical constraints derived from structural imaging measures. Further task-free fMRI connectivity studies are needed for explaining the precise biological underpinnings of temporal local synchrony features.

We believe that LPSNs and RSNs (see Fig. 7D) represent distinct neural processes, in part due to their propensity to detect ‘local’ and ‘global’ connectivity, respectively. Whilst RSNs are associated with large-scale functional brain networks, we interpret each LPSN as a population of local oscillators in task-free fMRI data. This may be explained based on the difference between GMM clustering used for generating LPSNs and independent component analysis used for extracting RSNs [Smith et al., 2012]. In contrast to group independent component analysis as a method of extracting “temporally independent sources” of functional connectivity in fMRI data, GMM-based clustering of DRePS resembles a functional parcellation of the brain using voxel-wise DRePS feature vectors. It estimates the similarity (i.e., dependence to the same Gaussian distribution) between reduced DRePS feature vectors, and then all voxels with similar distribution form a cluster.

Ultra-slow fluctuations are an important property of dynamic local connectivity in the normal brain. A recent study has shown nonstationary evolution of global synchronization patterns between the BOLD activities of different brain areas oscillating on an ultra-slow ( $< 0.01 \text{ Hz}$ ) time scale [Ponce-Alvarez et al., 2015]. Our study, in contrast, considers spatial distributions of local phase synchrony with statistically similar dynamics. Nevertheless, the dominant frequency content of the DRePS time series over all subjects remains proximate to that which has been reported previously using global functional connectivity ( $0.002\text{--}0.02 \text{ Hz}$ , see Fig. 6C). Emergence and dissolution of high DRePS values (for example, across parts of the default mode network, visual and parietal areas as

shown in Fig. 6A) at very slow time scale may be linked to the concept of ultra-slow connectivity states as discussed in the previous brain connectivity studies [Allen et al., 2012; Cribben et al., 2012; Shirer et al., 2011; Yu et al., 2015]. It means that the DRePS variations are hardly random, but represent structured clusters of connectivity over time.

An important assessment step prior to any Hilbert transform based instantaneous phase analysis study (including DRePS) would be to evaluate Bedrosian identity and error signal  $\epsilon[n]$  (see “Instantaneous Phase of fMRI Time Series”) for the underlying data. Another factor to consider here would be possible dependence between phase information and amplitude changes in finite-length signals such as fMRI time series. This is reflected in similar patterns of phase synchrony obtained by DRePS and SW-ReHo (as a solely dependent method to signal amplitude) in Fig. 5 and Supporting Information Fig. S1. However, the main advantage of DRePS over amplitude-based methods such as SW-ReHo stems from its higher temporal resolution, as shown in the simulation results. Note that the impact of amplitude changes on phase information is not only relevant to DRePS, but also applies to all other phase synchrony analysis techniques dealing with finite-length signals. The amplitude variations in task-free fMRI data may originate from genuine “local phase synchrony” and/or confounding factors such as physiological artifacts, movement etc. In this study, we tried to alleviate these problematic confounds through multiple preprocessing steps as much as possible. Also, internal spatial smoothing of the DRePS framework, inherited from ReHo [Zuo et al., 2013], may enhance signal-to-noise ratio, as reflected in the difference between the simulation results of 27 (strong smoothing) and 7 (weaker smoothing) cube sizes in Supporting Information Fig. S1. However, there is still a chance that different physiological variations such as pseudo-cyclic respiratory and cardiac changes are aliased into the narrow low frequency band of  $0.03\text{--}0.07 \text{ Hz}$  given the  $T_R$  of 3 seconds in our study. This aliasing may result in an overlap between non-neural fluctuations and real dynamic functional connectivity within the applied frequency band. Thus effective minimization of physiological confounds in data acquisition and preprocessing is important in DRePS just as it is important in other fMRI connectivity approaches.

We have shown in Fig. 6 and Supporting Information Fig. S2 that wide-band filtering may have negligible impact on the analysis outcome of the proposed DRePS methodology. However, excessive expansion of the band-pass filter can potentially cause considerable standard deviations in the error signal fluctuations. For example, one can see in Fig. 4 that the subject-specific error signal averages and their corresponding RMS distributions within  $0.03\text{--}0.07 \text{ Hz}$  and  $0.05\text{--}0.09 \text{ Hz}$  are larger than  $0.01\text{--}0.09 \text{ Hz}$  and  $0.03\text{--}0.11 \text{ Hz}$ . This limitation may hamper extension to wider band filtering that may be of interest given recent evidence of BOLD contribution above  $0.1 \text{ Hz}$  [Chen and

Glover, 2015]. A possible solution may be to decompose the BOLD dynamics into frequency bands of interest in order to make the band-pass filter as restricted as possible [Bajaj et al., 2013; Xue et al., 2014; Zuo et al., 2010].

Non-stationarity characteristics of task-free functional connectivity may not be efficiently captured using low temporal resolution fMRI datasets. Indeed, recent fast EPI imaging techniques with sub-second whole-brain scanning time hold promise for deeper investigation of non-linear and nonstationary patterns of brain dynamics [Paton et al., 2013]. From this perspective, the maximal capacity of the DRePS analysis framework is most likely to be exploited when studying brain functional connectivity in fast EPI images.

## CONCLUSION

The current study introduces the instantaneous measure of Dynamic Regional Phase Synchrony (DRePS), based on time-varying mean phase coherence among neighboring voxels in fMRI data. In contrast to sliding window approaches, DRePS provides single- $T_R$  resolution with no loss of time points and no temporal smoothing. We observed that time-varying DRePS changes are associated with spatially clustered brain areas, called local phase synchrony networks (LPSNs). Although evaluation of phase synchrony is not the only approach available to interrogate dynamic behavior of brain interactions, we propose that in the emerging field of dynamic functional connectivity, DRePS has the ability to provide new insights into normal and abnormal brain function.

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