

The Origin of GnRH Pulse Generation: An Integrative Mathematical-Experimental Approach

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Fertility critically depends on the gonadotropin-releasing hormone (GnRH) pulse generator, a neural construct comprised of hypothalamic neurons coexpressing kisspeptin, neurokinin-B and dynorphin. Here, using mathematical modeling and *in vivo* optogenetics we reveal for the first time how this neural construct initiates and sustains the appropriate ultradian frequency essential for reproduction. Prompted by mathematical modeling, we show experimentally using female estrous mice that robust pulsatile release of luteinizing hormone, a proxy for GnRH, emerges abruptly as we increase the basal activity of the neuronal network using continuous low-frequency optogenetic stimulation. Further increase in basal activity markedly increases pulse frequency and eventually leads to pulse termination. Additional model predictions that pulsatile dynamics emerge from nonlinear positive and negative feedback interactions mediated through neurokinin-B and dynorphin signaling respectively are confirmed neuropharmacologically. Our results shed light on the long-elusive GnRH pulse generator offering new horizons for reproductive health and wellbeing.

Key words: arcuate nucleus; fertility; gonadotrophin-releasing hormone; kisspeptin neurons; mathematical model

Significance Statement

The gonadotropin-releasing hormone (GnRH) pulse generator controls the pulsatile secretion of the gonadotropic hormones LH and FSH and is critical for fertility. The hypothalamic arcuate kisspeptin neurons are thought to represent the GnRH pulse generator, since their oscillatory activity is coincident with LH pulses in the blood; a proxy for GnRH pulses. However, the mechanisms underlying GnRH pulse generation remain elusive. We developed a mathematical model of the kisspeptin neuronal network and confirmed its predictions experimentally, showing how LH secretion is frequency-modulated as we increase the basal activity of the arcuate kisspeptin neurons *in vivo* using continuous optogenetic stimulation. Our model provides a quantitative framework for understanding the reproductive neuroendocrine system and opens new horizons for fertility regulation.

Introduction

The periodic release of gonadotropin-releasing hormone (GnRH) plays a central role in control of mammalian reproduction and is

driven by hypothalamic neuronal networks (Herbison, 2016). The operation of these networks at a frequency appropriate for the species is critical for the generation of gonadotropin hormone signals (luteinizing hormone, LH; and follicle-stimulating hormone, FSH) by the pituitary gland, which stimulate the gonads and set in motion gametogenesis and ovulation. However, the origin of GnRH pulse generation and mechanisms underlying frequency control remain poorly understood.

Secretion of GnRH by GnRH neurons located in the hypothalamus into the pituitary portal circulation is controlled by upstream hypothalamic signals (Herbison, 2016). The neuropeptide kisspep-

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tin has been identified as a key regulator of GnRH secretion as both humans and rodents with inactivating mutations in kisspeptin or its receptor fail to progress through puberty or show normal pulsatile LH secretion (Seminara et al., 2003; de Roux et al., 2003; Kaiser, 2015). Within the hypothalamus, two major kisspeptin producing neuronal populations are found in the arcuate nucleus (ARC) and in the preoptical area (Hrabovszky, 2014) or the anteroventral periventricular (AVPV)/rostral periventricular (PeN) continuum in rodents (Clarkson et al., 2009). Moreover, the invariable association between neuronal activity in the ARC and LH pulses across a range of species from rodents to primates (Plant and Zeleznik, 2014) has been suggestive that the ARC is the location of the GnRH pulse generator, and therefore the ARC kisspeptin neurons, also known as KNDy for coexpressing neurokinin B (NKB) and dynorphin (Dyn) alongside kisspeptin (Lehman et al., 2010), constitute the core of the GnRH pulse generator.

Although animal studies have shown that KNDy neurons are critical for the regulation of GnRH secretion, there has been relatively little understanding on the regulatory mechanisms involved in generating and sustaining pulsatile dynamics. Pharmacological modulators of kisspeptin, NKB and Dyn signaling have been extensively used to perturb the system and study the effect on the activity of a hypothalamic neuronal population (using ARC multiunit activity (MUA) volleys, an electrophysiological correlate of GnRH pulse generator activity, as a proxy) (Wilson et al., 1984), as well as on downstream GnRH/LH pulse dynamics (Kinsey-Jones et al., 2008, 2012; Navarro et al., 2009; Wakabayashi et al., 2010). For example, it has been shown that kisspeptin (Kp-10) administration does not affect MUA volleys in the ovariectomized rat (Kinsey-Jones et al., 2008), suggesting that kisspeptin is relaying the pulsatile signal to GnRH neurons rather than generating it. On the contrary, administration of NKB or Dyn modulates MUA volley frequency in the ovariectomized goat (Wakabayashi et al., 2010), suggesting a more active role for these neuropeptides in the generation of the pulses. Deciphering, however, the role of NKB has been problematic, and there exist conflicting data showing either an increase or decrease of LH levels in response to administration of a selective NKB receptor (TACR3) agonist (senktide) (Sandoval-Guzmán and Rance, 2004; Navarro et al., 2009; Kinsey-Jones et al., 2012). Recently, a study combining optogenetics, with whole-cell electrophysiology and molecular pharmacology has shed light on the action of the neuropeptides NKB and Dyn in the KNDy network (Qiu et al., 2016), with the key mechanistic finding that NKB functions as an excitatory signal by depolarizing KNDy cells at the postsynaptic site, while coreleased Dyn functions presynaptically to inhibit NKB release.

Taking into account the experimental findings described above, we develop a mathematical model of the ARC KNDy network. The model predicts that this neuronal population behaves as a relaxation oscillator, autonomously generating and sustaining pulsatile activity similar to the hypothalamic MUA volleys observed *in vivo* (Wilson et al., 1984; Kinsey-Jones et al., 2012). Further model analysis reveals that basal activity within the ARC KNDy population is a critical for GnRH/LH pulsatility. We test this predictions *in vivo* using optogenetics and show that LH secretion dynamics are sensitive to *continuous* stimulation of the ARC KNDy network.

Materials and Methods

Animals. Breeding pairs of Kiss-Cre heterozygous transgenic mice (Yeo et al., 2016) were obtained from the Department of Physiology, Development and Neuroscience, University of Cambridge, UK. Litters from

the breeding pairs were genotyped by PCR analysis. Adult female mice (8–14 weeks old; 25–30 g) heterozygous for the Kiss-Cre transgene or wild-type C57BL/6 littermates, with normal pubertal development and estrous cyclicity, were used. Mice were housed under a 12:12 h light/dark cycle (lights on 0700 h) at $22 \pm 2^\circ\text{C}$ and provided with food (standard maintenance diet; Special Dietary Services, Wittam, UK) and water *ad libitum*. All animal procedures performed were approved by the Animal Welfare and Ethical Review Body (AWERB) Committee at King's College London, and in accordance with the UK Home Office Regulations.

Surgical procedures. Surgical procedures for stereotaxic injection of AAV9-EF1-dflox-hChR2-(H134R)-mCherry-WPRE-hGH (4.35×10^{13} GC/ml; Penn Vector Core) to express channelrhodopsin (ChR2) in ARC kisspeptin neurons were performed under aseptic conditions with general anesthesia induced by ketamine (Vetalar, 100 mg/kg, i.p.; Pfizer,) and xylazine (Rompun, 10 mg/kg, i.p.; Bayer). Kiss-Cre female mice ($n = 9$) or wide-type ($n = 3$) were secured in a Kopf Instruments motorized stereotaxic frame and surgical procedures were performed using a Robot Stereotaxy system (Neurostar). A small hole was drilled into the skull at a location above the ARC. The stereotaxic injection coordinates used to target the ARC were obtained from the mouse brain atlas of Paxinos and Franklin (2004) (0.3 mm lateral, 1.2 mm posterior to bregma and at a depth of 6.0 mm). Using a 2 μl Hamilton microsyringe (Esslab) attached to the robot stereotaxy, 1 μl of the AAV-construct was injected unilaterally into the ARC at a rate of 100 nl/min. The needle was left in position for a further 5 min and then removed slowly over 1 min. A fiber-optic cannula (200 μm , 0.39 NA, 1.25 mm ceramic ferrule; Thorlabs) was then inserted at the same coordinates as the injection site, but to a depth of 5.88 mm, so that the fiber optic cannula was situated immediately above the latter. Dental cement or a glue composite was then used to fix the cannula in place, and the skin incision closed with suture. A separate group of mice ($n = 10$) injected with the AAV construct, and fiber optic cannulae as described above, but additionally chronically implanted with an intracerebroventricular fluid cannulae (26 gauge; Plastics One) targeting the lateral ventricle (coordinates: 1.1 mm lateral, 1.0 mm posterior to bregma and at a depth of 3.0 mm), was used for the combined neuropharmacological and optogenetic studies. After surgery, mice were left for 4 weeks to achieve effective opsin expression. After a 1-week recovery period, the mice were handled daily to acclimatize them to the tail-tip blood sampling procedure (Steyn et al., 2013).

Validation of AAV injection site. After completion of experiments, mice were anesthetized with a lethal dose of ketamine and transcardially perfused with heparinized saline for 5 min, followed by 10 min of ice-cold 4% paraformaldehyde (PFA) in phosphate buffer, pH 7.4, for 15 min using a pump (Minipuls; Gilson). Brains were rapidly collected and post-fixed sequentially at 4°C in 15% sucrose in 4% PFA and in 30% sucrose in PBS until they sank. Afterward, brains were snap-frozen on dry ice and stored at -80°C until processing. Brains were coronally sectioned (40 μm) using a cryostat (Bright Instrument) and every third section was collected between -1.34 mm to -2.70 mm from the bregma. Sections were mounted on microscope slides, air-dried and coverslipped with ProLong Antifade mounting medium (Invitrogen). The injection site was verified and evaluated using Axioskop 2 Plus microscope equipped with axiovision 4.7. One of 19 Kiss-Cre mice failed to show mCherry fluorescence in the ARC and was excluded from the analysis.

Experimental design and blood sampling for LH measurement. Before optogenetic stimulation, the very tip of the mouse's tail was excised using a sterile scalpel for subsequent blood sample collection (Czieselsky et al., 2016). The chronically implanted fiber optic cannula was then attached via a ceramic mating sleeve to a multimode fiber-optic rotary joint patch cables (Thorlabs), allowing freedom of movement of the animal, for delivery of blue light (473 nm wavelength) using a Grass SD9B stimulator controlled DPSS laser (Laserglow Technologies). Laser intensity at the tip of the fiber optic patch cable was 5 mW. After 1 h acclimatization, blood samples (5 μl) were collected every 5 min for 2.5 h. After 1 h of controlled blood sampling, continuous optic stimulation (5 ms pulse width) was initiated at 0.5, 1 and 5 Hz for 90 min. Controls received no optic stimulation. Kiss-Cre mice received the stimulation protocols in random order. Wild-type received 5 Hz optic stimulation only.

Table 1. Model parameter values

No.	Parameter	Description	Value	Reference
1	d_D	Dyn degradation rate	0.25 min^{-1} [0.05, 0.3] min^{-1}	Inferred
2	d_N	NKB degradation rate	1 min^{-1} [0.3, 109.3] min^{-1}	Inferred
3	d_v	Firing rate reset rate	10 min^{-1}	(Qiu et al., 2016)
4	k_D	Maximum Dyn secretion rate	4.5 nM min^{-1} [2.76, 38.4] nM min^{-1}	Inferred
5	k_N	Maximum NKB secretion rate	320 nM min^{-1}	(Ruka et al., 2016)
6	$k_{D,0}$	Basal Dyn secretion rate	$0.175 \text{ nM min}^{-1}$ [10^{-3} , 1.88] nM min^{-1}	Inferred
7	$k_{N,0}$	Basal NKB secretion rate	0 nM min^{-1} [10^{-3} , 0.44] nM min^{-1}	Inferred
8	p_v	Effective strength of synaptic input	1 min	Fixed
9	v_0	Maximum rate of neuronal activity increase	$30000 \text{ spikes min}^{-2}$	(Qiu et al., 2016)
10	K_D	Dyn IC_{50}	0.3 nM	(Yasuda et al., 1993)
11	K_N	NKB EC_{50}	32 nM	(Seabrook et al., 1995)
12	$K_{v,1}$	Firing rate for half-maximal Dyn secretion	$1200 \text{ spikes min}^{-1}$	(Dutton and Dyball, 1979)
13	$K_{v,2}$	Firing rate for half-maximal NKB secretion	$1200 \text{ spikes min}^{-1}$	(Dutton and Dyball, 1979)
14	I_0	Basal activity	0.2 (corresponding to 5 spikes sec^{-1})	(de Croft et al., 2012; Ruka et al., 2016)
15	n_1, n_2, n_3, n_4	Hill coefficients	2 (dimensionless)	Fixed

Parameters values were either found in the literature or Inferred from MUA rat data (see Fig. 3A in Kinsey-Jones et al., 2012). Here, we report the 99% equal tail posterior density interval for the marginal distribution of each Inferred parameter. Along these intervals, we report specific parameter values used for the bifurcation analysis and numerical evaluation of the model.

For the neuropharmacological manipulation of Dyn or NKB signaling with or without simultaneous optogenetic stimulation the animals were appropriately prepared as described above, but in addition an i.c.v. injection cannula with extension tubing, preloaded with drug solution (nor-BNI or SB222200 dissolved in artificial CSF), was inserted into the guide cannula immediately after connection of the fiber optic cannula. The tubing was extended outside the cage and connected to a 10 μl Hamilton syringe mounted in an automated pump (Harvard Apparatus) to allow remote microinfusion without disturbing the mice during the experiment. Five minutes before optic stimulation, intracerebroventricular administration of drug treatment commenced as a bolus injection over 5 min, followed by a continuous infusion for the remainder of the experiment. In the absence of optic stimulation the same intracerebroventricular regimen was used. The blood samples were frozen at -80°C until assayed. LH was measured using an in-house ELISA similar to that described by Steyn et al. (Steyn et al., 2013). Mouse LH standard (AFP-5306A; NIDDK-NHPP) and primary antibody (polyclonal antibody, rabbit LH antiserum, AFP240580Rb; NIDDK-NHPP) were from Harbor-UCLA, and secondary antibody (donkey anti-rabbit IgG polyclonal antibody [horseradish peroxidase]; NA934) was from VWR International. The ELISA validation was performed according to the procedure of Steyn et al. (Steyn et al., 2013), which was derived from protocols defined by the International Union of Pure and Applied Chemistry. The linear detection range was determined by assessment of 9 serially diluted mLH standard replicates ranging from 0.00195 to 1 ng/ml. To interpolate the LH concentration in whole blood samples, a nonlinear regression analysis was performed using serially diluted mLH standards of known concentration to create a standard curve with a detection range from 8.0 to 0.015 ng/ml. Extension of the standard curve by inclusion of a top standard of 1.0 ng/ml and extrapolation of unknowns after nonlinear regression analysis allowed a theoretical detection range of whole blood mLH (in a 1:25 dilution) of 0.187 to 25 ng/mL. In our hand, the sensitivity of the ELISA is 7.5 pg/ml. Accuracy and intraassay and interassay variability were determined using mouse blood samples with known amounts of mLH included in each assay. We observed reliable detection of mLH at a final concentration of 0.0039 ng/ml. A linear regression across a standard curve ranging from 0.0075 to 1.0 ng/ml generated an R^2 value of 0.964. The intraassay and interassay variations were 4.6% and 10.2%, respectively.

LH pulses and statistical analysis. Detection of LH pulses was established by use of the Dynpeak algorithm (Vidal et al., 2012). The effect of optogenetic stimulation on parameters of LH secretion was calculated by comparing the mean number of LH pulse per hour, within the 90 min stimulation/drug delivery period with the 60 min prestimulation/drug delivery control period. For the nonstimulated control animals, the same time points were compared. The mean number of LH pulse per hour, within the 90 min stimulation period, or equivalent, was also compared between experimental groups. Statistical significance was tested using

one-way ANOVA followed by Dunnett's test. $p < 0.05$ was considered statistically significant. Data are presented as the mean \pm SEM.

Modeling the effect of NKB and Dyn receptor antagonists. To model the effect of SB22222, a selective NKB receptor (TACR3) antagonist, we modify the expression for the synaptic input, I , to read:

$$I = I_0 + p_v \frac{\bar{N}^{n_4}}{\bar{N}^{n_4} + E^{n_4} + K_N^{n_4}} \bar{v}$$

Similarly to model the effect of nor-BNI, a κ -opioid receptor antagonist, we modify function f_N to read:

$$f_N(\bar{v}, \bar{D}) = k_{N,0} + k_N \frac{\bar{v}^{n_2}}{\bar{v}^{n_2} + K_{v,2}^{n_2}} \frac{K_D^{n_3} + E^{n_3}}{\bar{D}^{n_3} + E^{n_3} + K_D^{n_3}}$$

In the equations above, parameter E represents the antagonist concentration.

Model calibration. We used an approximate Bayesian computation (ABC) method based on sequential Monte Carlo (SMC) (Toni et al., 2009) to infer model parameters d_D , d_N , k_D , $k_{D,0}$, and $k_{N,0}$ from MUA recordings (see Fig. 3A in Kinsey-Jones et al., 2012). In ABC SMC a population of parameter vectors or particles, θ , initially sampled from the prior distribution π_0 , is propagated to the approximate target posterior distribution $\pi_T(\theta | d(x(t)), x^*(t)) < \epsilon_T$, where $d(x(t), x^*(t))$ is a discrepancy function comparing the simulated dataset $x^*(t)$ to the experimental data $x(t)$ and ϵ_T is the error tolerance level. Propagation is accomplished through a sequence of distributions π_i , $i = 1, \dots, T - 1$, associated with a series of decreasing tolerance levels ϵ_i , thus hence making the transition to the target π_T more gradual and avoiding getting stuck in areas of low probability. We used the following discrepancy function to compare simulated ($x^*(t)$) to experimental ($x(t)$) data:

$$d(x(t), x^*(t)) = \max\left(\frac{I(x(t)) - I(x^*(t))}{I(x(t))}, \frac{DC(x(t)) - DC(x^*(t))}{DC(x(t))}\right)$$

where $I(z(t))$ is the average time interval between pulses in trajectory $z(t)$ and $DC(x(t))$ is the average duty cycle in $z(t)$ (defined as the fraction of time the activity exceeds 50% of the max activity). In the data we used $I(x(t)) = 19.26 \pm 0.32 \text{ min}$ and $DC(x(t)) = 0.181 \pm 0.04$. Simulated trajectories were generated by simulating the model to 6000 min and discarding the first 1000 min. To ensure gradual transition between populations we take $T = 4$ and $\epsilon_i = 10^{2-i}$. The size of the particle population is set to 500. The following prior distributions were used: $\log_{10}(d_D) \sim \text{Uniform}(-3, 3)$, $\log_{10}(d_N) \sim \text{Uniform}(-3, 3)$, $\log_{10}(k_D) \sim \text{Uniform}(-3, 3)$, $\log_{10}(k_{D,0}) \sim \text{Uniform}(-3, 3)$, and $\log_{10}(k_{N,0}) \sim \text{Uniform}(-3, 3)$. All remaining parameters were fixed to values found in the literature (Table 1). For each parameter an independent \log_{10} -normal perturbation kernel with variance 0.05 was used.

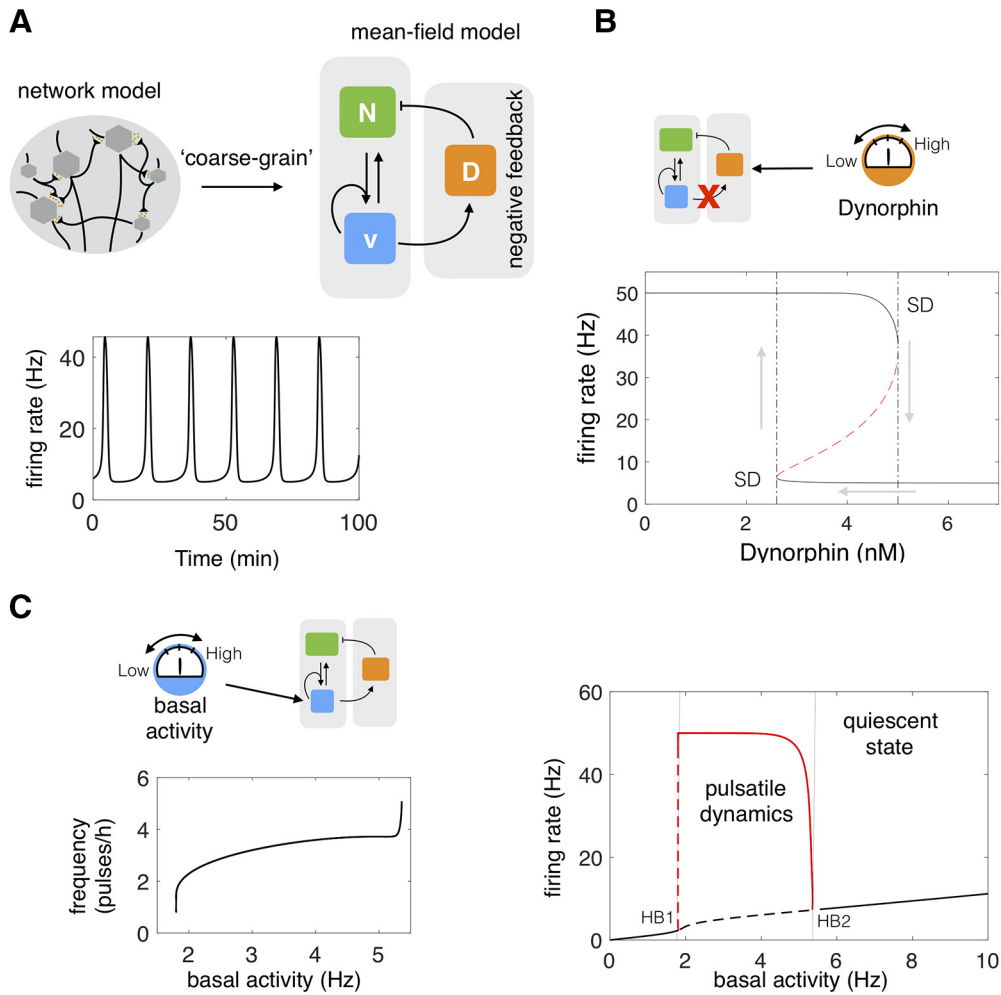


Figure 1. A coarse-grained model gives mechanistic insight into the pulsatile behavior of the ARC KNDy population. **A**, We developed a mean-field model of the neuronal population comprising three dynamical variables: \bar{D} , representing the average concentration of Dyn secreted; \bar{N} , representing the concentration of NKB secreted; and \bar{v} , representing the average firing activity of the neuronal population. The model predicts that the system behaves as a relaxation oscillator owing to NKB induced bistability and Dyn-mediated negative feedback. **B**, Disrupting Dyn negative feedback obliterates the oscillatory behavior of the system. For intermediate levels of externally provided Dyn, the system exhibits two stable equilibria (upper and lower solid lines) and an unstable one (dashed red line). At the edges of the bistable regime equilibria are lost through a saddle-node bifurcation (SD points). The bistability gives rise to hysteresis as the value of Dyn is varied externally (gray arrows). **C**, The model predicts how basal neuronal activity affects the system's dynamics and pulse frequency. As basal activity is increased from zero, high-amplitude, low-frequency pulses emerge after some critical value (HB1 point; Hopf bifurcation). The frequency of pulses continues to increase with basal activity until oscillations disappear (HB2 point; Hopf bifurcation) and the system enters a mono-stable regime (black solid line). The solid red line denotes the amplitude of the pulses. Parameter values used in the bifurcation analysis are given in Table 1.

Bifurcation analysis and numerical experiments. Bifurcation analysis of the model was performed using AUTO-07p (Doedel et al., 2007). The model was simulated in MATLAB using function ode45 (explicit Runge-Kutta (4, 5) solver).

Results

Coarse-grained model of the ARC KNDy population

We propose a mathematical model (Fig. 1A) to study the dynamics of the ARC KNDy population. The model describes the dynamics of the neuronal population using three variables: \bar{D} , representing the average concentration of Dyn secreted by the population; \bar{N} , representing the average concentration of NKB secreted by the population; and \bar{v} , representing the average firing activity of the population, measured in spikes/min. The dynamics of the model variables are governed by the following set of coupled ordinary differential equations (ODEs):

$$\frac{d\bar{D}}{dt} = f_D(\bar{v}) - d_D\bar{D}; \quad (1)$$

$$\frac{d\bar{N}}{dt} = f_N(\bar{v}, \bar{D}) - d_N\bar{N}; \quad (2)$$

$$\frac{d\bar{v}}{dt} = f_v(\bar{v}, \bar{N}) - d_v\bar{v}. \quad (3)$$

Parameters d_D , d_N , and d_v control the characteristic timescale of each variable. In particular, parameters d_D and d_N correspond to the rate at which Dyn and NKB are lost (e.g., due to diffusion or active degradation), while d_v relates to the rate at which neuronal activity resets to its basal level. Functions f_D and f_N describe the secretion rate of Dyn and NKB, respectively, and function f_v encodes how the firing rate changes in response to the current levels of NKB and firing rate.

We employ the following sigmoidal (Hill) functions to describe regulatory relationships between the state variables. In particular, we set the secretion rate of Dyn and NKB to be:

$$f_D(\bar{v}) = k_{D,0} + k_D \frac{\bar{v}^{n_1}}{\bar{v}^{n_1} + K_{v,1}^{n_1}};$$

$$f_N(\bar{v}, \bar{D}) = k_{N,0}$$

$$+ k_N \frac{\bar{v}^{n_2}}{\bar{v}^{n_2} + K_{v,2}^{n_2}} \frac{K_D^{n_3}}{\bar{D}^{n_3} + K_D^{n_3}}.$$

In the equations above, both neuropeptides are constitutively secreted at rates $k_{D,0}$ and $k_{N,0}$, neuronal activity stimulates secretion of the two neuropeptides, and Dyn represses NKB secretion (Qiu et al., 2016). Since the rate of neuropeptide release is inherently limited by availability of cytoplasmic secretory vesicles at the presynaptic terminals (Han et al., 1999), we let secretion rates saturate at k_D and k_N , respectively. The effector levels at which saturation occurs are controlled via parameters $K_{v,1}$, $K_{v,2}$, and K_D . Furthermore, we set:

$$f_v(\bar{v}, \bar{N}) = v_0 \frac{1 - \exp(-I)}{1 + \exp(-I)}$$

$$I = I_0 + p_v \frac{\bar{N}^{n_4}}{\bar{N}^{n_4} + K_N^{n_4}} \bar{v}$$

where v_0 is the maximum rate at which the firing rate increases in response to synaptic inputs I . The stimulatory effect of NKB (which is secreted at the presynaptic terminal) is mediated via G-protein-coupled receptor Tacr3 and is manifested as a short-term depolarization of the postsynaptic neuron (Qiu et al., 2016). In the equation above, we accommodate this effect by letting a synaptic weight that is a sigmoidal function of NKB multiply \bar{v} . Parameter K_N sets the level of NKB at which its effect is half-maximal and parameter p_v controls the strength of the synaptic connections between KNDy neurons. Finally, parameter I_0 controls the basal neuronal activity in the population, which could stem from synaptic noise or external inputs. We find that for biophysically relevant parameter values (Table 1) the model predicts events of synchronized neuronal activity (Fig. 1A), reminiscent of the activity measured from the arcuate nucleus of rodent models (Kinsey-Jones et al., 2012; Clarkson et al., 2017b), and supports the hypothesis that KNDy neurons in the ARC constitute the core of the GnRH pulse generator (Clarkson et al., 2017b).

Analysis of the model reveals the KNDy population functions as a relaxation oscillator

Having shown that the model can reproduce sustained pulses of neuronal activity, we proceed to investigate the mechanisms driving the phenomenon. We first study the role of Dyn-mediated negative feedback using fast–slow analysis (Rinzel, 1985) of the coarse-grained model (Eqs. 1–3). Model calibration suggests that Dyn operates at a slower time-scale than NKB (Table 1). This time-scale separation, also supported by receptor internalization data (Weems et al., 2018), allows us to study the dynamics of the fast subsystem, comprised of \bar{N} and \bar{v} as a function of the slow variable, \bar{D} , which is treated as a constant (bifurcation) parameter. Our analysis shows that for intermediate values of Dyn the

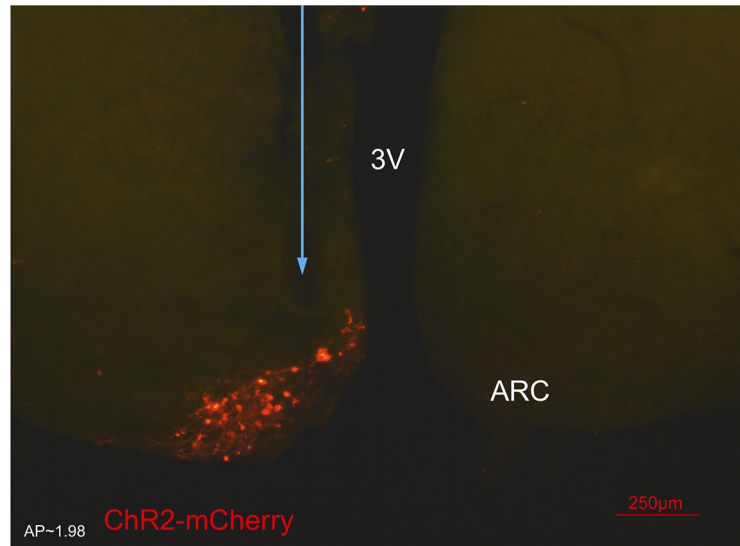


Figure 2. Expression of arcuate nucleus (ARC) kisspeptin neurons with ChR2-mCherry in Kiss-CRE mice. Coronal section showing red mCherry fluorescence positive neurons in the ARC which indicates ChR2 receptor expressing kisspeptin neurons, following unilateral injection of AAV9.EF1.dfloX.hChR2(H134R)-mCherry.WPRE.hGH into the ARC of Kiss-Cre mice. The blue arrow shows the precise location of fiber optic for stimulation. Note the absence of mCherry fluorescence in the other side of ARC. 3V, Third ventricle.

fast subsystem can exist either in a high or a low activity state (Fig. 1B). This bistable behavior, stemming from the nonlinear positive feedback between neuronal activity and NKB secretion, leads to sustained oscillations of neuronal activity when combined with slow, Dyn-mediated, negative feedback. In engineering terms, the system behaves as a relaxation oscillator: where the bistable subsystem is successively excited (moved from low to high state) by external inputs or noise and silenced (moved from high to low state) as a result of negative feedback. We should note that a relatively slow negative feedback is sufficient for sustaining oscillations, however, the combination of negative feedback with bistability is found in many biological oscillators most likely because it confers robustness (Pomeroy et al., 2003).

Next, to demonstrate the role of basal neuronal activity within the KNDy network in the generation and modulation of oscillatory activity, we treat parameter I_0 as a bifurcation parameter. Our analysis shows that oscillatory behavior is supported within a critical range of I_0 values (see Fig. 1C). As I_0 is increased from zero, high-amplitude, low-frequency pulses emerge via a Hopf bifurcation (Fig. 1C; HB1 point). The frequency of pulses further increases with I_0 until oscillations disappear via a Hopf bifurcation (Fig. 1C; HB2 point) and the system reenters a silent (non-oscillatory) regime.

Continuous optogenetic stimulation of KNDy neurons alters the pattern of LH secretion *in vivo*

To test the model prediction that basal excitation within the KNDy population controls LH pulsatility, we continuously stimulated the ARC KNDy population in Kiss-Cre mice (Adekunbi et al., 2018) using optogenetics and measured LH dynamics. ARC kisspeptin-expressing neurons were transduced with a Cre-dependent adeno-associated virus (AAV9-EF1-dfloX-hChR2-(H134R)-mCherry-WPRE-hGH) to express ChR2 (Fig. 2). AAV-injected, Kiss-Cre mice were implanted with a fiber optic cannula in the ARC and the effects on LH pulsatility of continuous stimulation at different frequencies was tested. After 1 h of controlled blood sampling, low-frequency optic stimulation, 5 ms pulses of blue light (473 nm) at 0.5, 1, or 5 Hz, was initiated and continuously deliv-

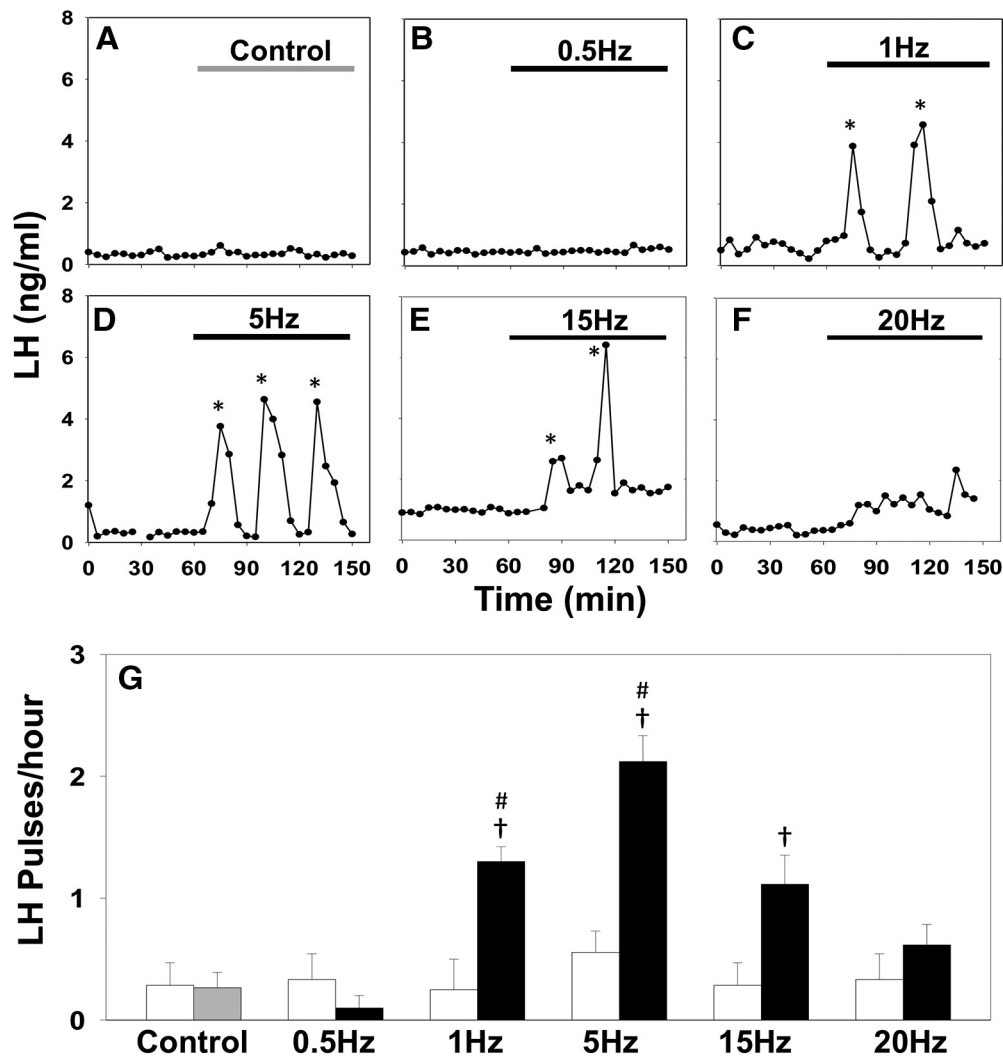


Figure 3. Optic stimulation of ARC kisspeptin neurons triggers LH pulses in estrous Kiss-Cre mice. *A–F*, Representative examples showing LH secretion in response to no stimulation (gray bar) as control (*A*), or continuous blue light (473 nm, 5 ms pulse width, black bar) activation of kisspeptin neurons at 0.5 Hz (*B*), 1 Hz (*C*), 5 Hz (*D*), 15 Hz (*E*), and 20 Hz (*F*). Pulses detected by the DynePeak algorithm are indicated with an asterisk. *G*, Summary showing for each group mean \pm SEM. LH pulse frequency over the 60 min control period (white bars) and over the subsequent stimulation period (black bars). $^{\dagger}p < 0.05$ versus prestimulation; $^{\#}p < 0.05$ versus stimulation at higher frequency. $n = 4–9$ per group.

ered for 90 min. Control mice received no optic stimulation. During the course of the experiment, blood samples (5 μ l) were collected every 5 min (Adekunbi et al., 2018). To maximize the effect of optogenetic stimulation, estrous mice were used which display minimum intrinsic pulse generator activity (Czieselsky et al., 2016). Indeed, the majority of the control nonoptically stimulated Kiss-Cre mice in estrus exhibited no LH pulse or intermittently 1 pulse during the 2.5 h sampling period (Fig. 3*A,G*). Similarly, no LH pulses or occasionally 1 LH pulse was observed in the 60 min control period in the optically stimulated mice (Fig. 3*G*, white bars). Continuous optic stimulation at 0.5 Hz failed to induce LH pulses (Fig. 3*B,G*), while 1 Hz evoked regular LH pulses (Fig. 3*C,G*), in line with our theoretical prediction of sudden qualitative changes in the dynamic behavior of the system (Fig. 1*C*). Stimulation at 5 Hz resulted in a further, statistically significant ($p < 0.05$), increase in LH pulse frequency (Fig. 3*D,G*) further confirming that increasing the basal activity in the ARC KNDy neuronal population via low-frequency continuous stimulation modulates LH pulsatile dynamics. Further increasing the frequency of optic stimulation to 15 Hz led to a reduction in LH pulses (Fig. 3*E,G*), and at 20 Hz the frequency of LH pulses

under optic stimulation was indistinguishable from the control period (Fig. 3*F,G*). Continuous optogenetic stimulation (5 Hz) of AAV-injected wild-type C57BL/6 estrous mice ($n = 3$) failed to induce LH pulses (data not shown).

Levels of Dyn and NKB signaling control the response of the system to optic stimulation

The above theoretical and experimental results indicate a characteristic tipping-point behavior of the system, where a small increase in the basal activation levels is sufficient to trigger robust pulsatile dynamics (Strogatz, 2018). Our model predicts that such behavior emerges as a result of the nonlinear positive and negative feedback interactions that are mediated through NKB and Dyn signaling respectively. Therefore to test the active role of NKB and Dyn signaling on pulse generation, we next combined optogenetic stimulation with neuropharmacological perturbations of the two pathways.

Disrupting Dyn signaling increases the sensitivity of the system to optic stimulation

Our model predicts that disruption of Dyn signaling should enable pulsatile dynamics over a wider range of optic stimulation

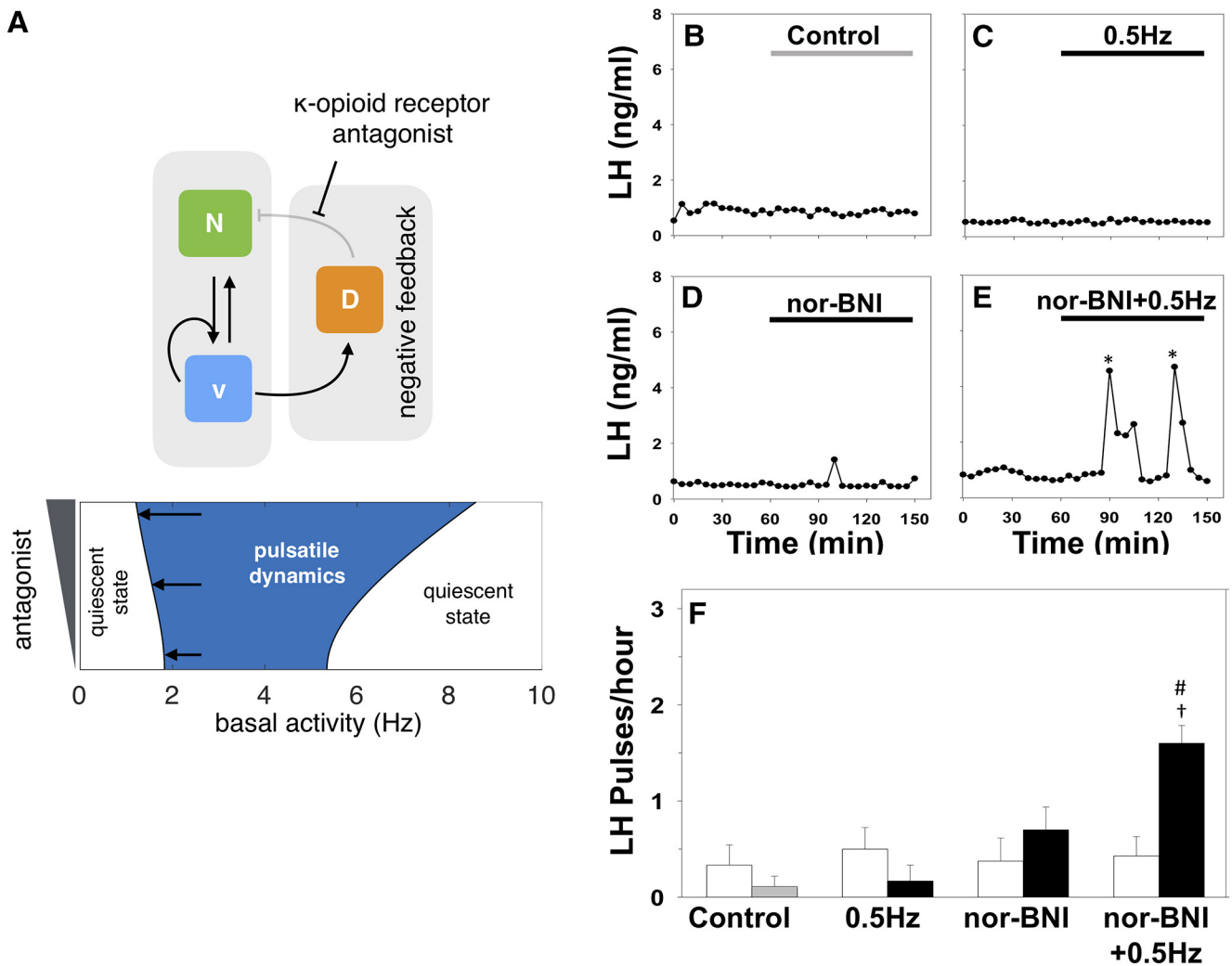


Figure 4. Disrupting Dyn signaling increases the sensitivity of the system to optic stimulation. *A*, The model predicts that reducing the strength of negative feedback by partially blocking Dyn signaling should enable pulsatile dynamics over a wider range of optic stimulation frequencies as shown by the two-parameter bifurcation diagram depicting the region in the parameters (antagonist and basal activity) colored in blue and defined by the loci of HB1 and HB2 (left and right curves respectively) that expands as antagonist is increased). Model parameter values are given in Table 1. *B–E* Nor-BNI, a Dyn receptor (κ -opioid) antagonist, was used to block Dyn signaling *in vivo*. Representative examples showing LH secretion in response to no treatment (gray bar) as control (*B*), continuous blue light (473 nm, 5 ms pulse width, black bar) activation of kisspeptin neurons at 0.5 Hz (*C*), nor-BNI treatment (bolus intracerebroventricular injection of 1.06 nmol in 1.25 μ l over 5 min, followed by a continuous infusion of 1.28 nmol in 1.5 μ l over 90 min (*D*) or combined nor-BNI treatment and optic stimulation at 0.5 Hz (*E*). Pulses detected by the DynePeak algorithm are indicated with an asterisk. *F*, Summary plot showing for each group mean \pm SEM LH pulse frequency over the pretreatment (white bars) and treatment period (black bars). $^{\dagger}p < 0.05$ vs pretreatment; $^{\#}p < 0.05$ vs only optic stimulation treatment. $n = 4–6$ per group.

frequencies (Fig. 4A). Specifically, Figure 4A, bottom, depicts a two-parameter bifurcation diagram showing how the loci of HB1 and HB2 (Fig. 1C) change as we vary two parameters in the model, namely the basal activity (I_0) and antagonist concentration (E) (see Materials and methods). Intuitively, such disruption will reduce the strength of negative feedback in the system and consequently lower optic stimulation frequencies would suffice to excite the bistable neuronal population and set the relaxation oscillator in motion. To test this prediction *in vivo* we repeated the optogenetic stimulation protocol at 0.5 Hz together with nornalorphimine (nor-BNI), a selective κ opioid receptor (KOR) antagonist, to block Dyn signaling. Although 0.5 Hz had previously failed to induce LH pulses (Fig. 4C,F), the addition of nor-BNI (bolus intracerebroventricular injection of 1.06 nmol over 5 min, followed by a continuous infusion of 1.28 nmol over 90 min) evokes a statistically significant increase in LH pulse frequency to ~ 1.6 pulses/h (Fig. 4E,F). Intra-cerebroventricular

injection of nor-BNI alone had no effect on LH pulse frequency (Fig. 4D,F).

Disrupting NKB signaling desensitizes the system to optic stimulation

Our model also predicts that disruption of NKB signaling should desensitize the system to external optic stimulation (Fig. 5A). Specifically, Figure 5A, bottom, depicts a two-parameter bifurcation diagram showing how the loci of HB1 and HB2 (Fig. 1C) change as we vary two parameters in the model, namely the basal activity (I_0) and antagonist (E) (see Materials and Methods). NKB signaling is key for pulsatile behavior as it enables positive feedback interactions within the population and therefore promotes bistability. Hence disrupting NKB signaling ought to decrease the propensity of the system to get excited into the pulsatile regime by external stimulation. To test this prediction *in vivo* we repeated the optogenetic stimulation protocol at the highest frequency (5 Hz), and used SB222200, a selective TACR3 antago-

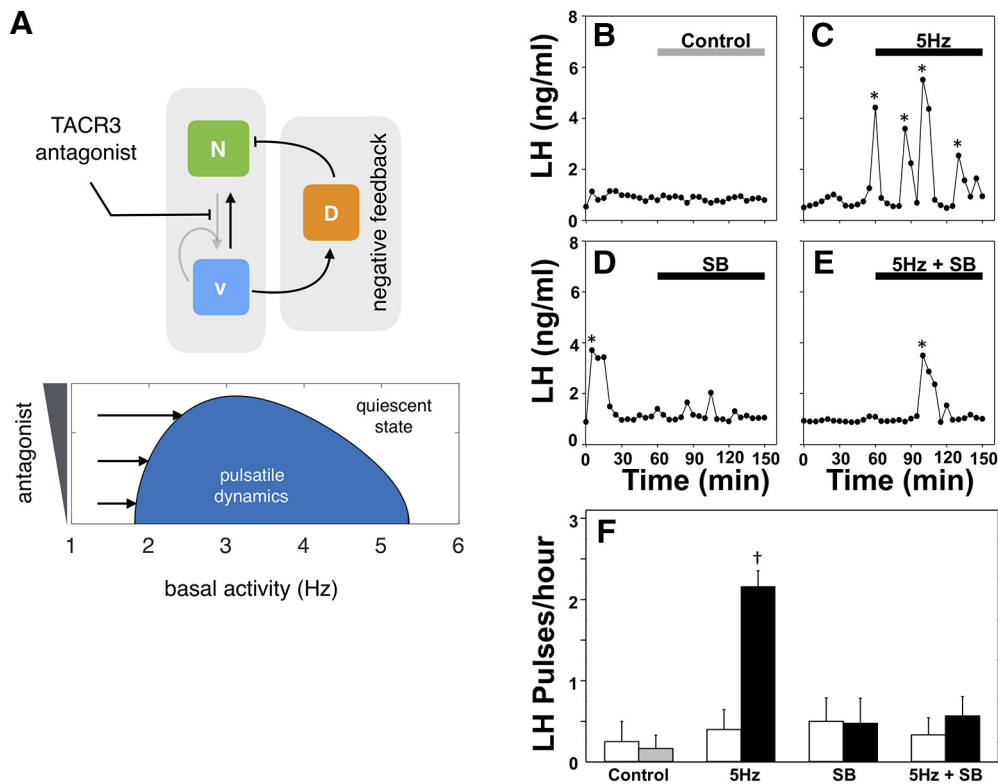


Figure 5. Disrupting NKB signaling desensitize the system to optic stimulation. **A**, The model predicts that weakening bistability by blocking NKB signaling should restrict the range of optic stimulation frequencies that trigger pulsatility as shown by the two-parameter bifurcation diagram depicting the region in the parameters (antagonist and basal activity) colored in blue and defined by the loci of HB1 and HB2 that collide associated with shrinking of the blue region as antagonist is increased. Model parameter values are given in Table 1. **B–E**, SB222200 (SB), an NKB receptor (TACR3) antagonist, was used to block NKB signaling *in vivo*. Representative examples showing LH secretion in response to no treatment (gray bar) as control (**B**), continuous blue light (473 nm, 5 ms pulse width, black bar) activation of kisspeptin neurons at 5 Hz (**C**), SB222200 treatment (bolus intracerebroventricular injection of 6 nmol in 1.25 μ l over 5 min, followed by a continuous infusion of 9 nmol in 1.5 μ l over 90 min) (**D**) or combined SB222200 treatment and optic stimulation at 0.5 Hz (**E**). Pulses detected by the DynePeak algorithm are indicated with an asterisk. **F**, Summary plot showing for each group mean \pm SEM LH pulse frequency over the pretreatment (white bars) and treatment period (black bars). $\dagger p < 0.05$ versus pretreatment. $n = 4–6$ per group.

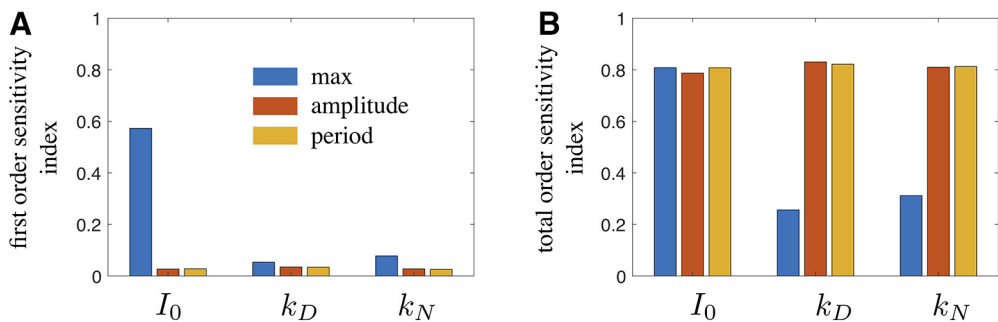


Figure 6. Global sensitivity analysis of the KNDy model. Global sensitivity analysis of the model considering maximum response amplitude, amplitude of oscillations, and period of oscillations. First-order (**A**) and total-order (**B**) sensitivity indices are shown for parameters k_D (maximum rate of Dyn secretion), k_N (maximum rate of NKB secretion), and I_0 (basal synaptic inputs). First order sensitivity indices indicate the proportion of variance of a response feature that is explained by variation in a parameter, keeping other parameters fixed. First order sensitivity indices, therefore, quantify the effect that single parameter perturbations have on the dynamics of the system. Total order sensitivity indices, on the other hand, indicate the proportion of variance in a response feature that is explained by variation in a parameter, while allowing variation in another parameters as well. Therefore, the total order sensitivity index of a parameter is a proxy for the effect this parameters has on the dynamics of the systems in combination with other parameters. Global sensitivity analysis was performed in MATLAB using eFast (Marino et al., 2008). The following parameter distributions were used: $\log_{10}(I_0) \sim \text{Uniform}(-1, 1)$, $\log_{10}(k_D) \sim \text{Uniform}(-1, 3)$, and $\log_{10}(k_N) \sim \text{Uniform}(-1, 3)$. All other model parameters were fixed (Table 1). The model was initialized at state $(D, N, v) = (0, 0, 0)$ and run to 6000 min. Response features (i.e., maximum response amplitude, amplitude of oscillations and the period of oscillation) were calculated from the response trajectory after discarding the first 1000 min.

nist, to block NKB signaling. Although 5 Hz had previously induced a high-frequency LH response (Fig. 4C,F), we observe that antagonist addition (bolus intracerebroventricular injection of 6 nmol over 5 min, followed by a continuous infusion of 9 nmol over 90 min) completely blocked the increased LH pulse frequency (Fig. 5E,F). Intra-cerebroventricular injection of SB222200 alone had no effect on LH pulse frequency (Fig. 5D,F).

Discussion

We developed and studied a mathematical model of the KNDy neural population in the ARC, a population proposed to comprise the core of the GnRH pulse generator (Clarkson et al., 2017a; Fergani and Navarro, 2016). Our model demonstrates that the KNDy population can indeed produce and sustain pulsatile dynamics working as a relaxation oscillator. On the one hand,

auto-stimulation via NKB signaling allows the population to behave as a bistable switch, firing either at a high or low rate. Moreover, basal neuronal activity and negative feedback through Dyn signaling allow the population to switch between the two activity states in a regular manner, giving rise to pulses of neuronal activity. Using global sensitivity analysis, we found that this mechanism of pulse generation is robust to parameter perturbations (Fig. 6). In fact, covariation of parameters governing, for example, the magnitude of basal activity, and the maximum secretion rates of NKB and Dyn is a more effective way of modulating the systems' oscillatory behavior (amplitude and frequency). This multichannel mode of efficient regulation is perhaps not surprising given the system's crucial function, and hints that steroid feedback modulating the dynamics of the pulse generator over the reproductive cycle in female mammals is mediated through multiple, possibly interlinked, pathways.

Our mathematical model presumes that KNDy neurons comprise the core mechanism behind GnRH pulse generation. However, there is ongoing debate over the precise definition of the GnRH pulse generator, and in particular whether pulse generation is intrinsic to the KNDy population or the downstream GnRH neurons. The latter hypothesis is supported by data showing that continuous kisspeptin infusion can increase LH pulse frequency in women with hypothalamic amenorrhoea (Jayasena et al., 2014); healthy men (George et al., 2011); patients with inactivating mutations in the NKB signaling pathway (Young et al., 2013); and in sheep in the presence of NKB antagonism (Clarke et al., 2018). These data do not exclude the KNDy hypothesis nor directly contradict it, as continuous kisspeptin stimulation could be allowing GnRH neurons to respond to residual episodic KNDy activity, however they do highlight the possibility of multiple distinct mechanisms driving LH pulsatility (Lehnert and Khadra, 2019; Lippincott et al., 2019).

Following model predictions, we explored the effect of continuous optogenetic activation of the KNDy population on LH pulse dynamics, a proxy for GnRH pulse dynamics. Analysis of the model highlights that the KNDy population undergoes sudden qualitative changes in its dynamic behavior as the basal activity of the population is modulated. In particular, as the basal activity level is increased the system transitions from a silent into a pulsatile mode, while higher levels of basal activity inhibit pulses and reinstate the quiescent state. Importantly, these sudden transitions are a rudimentary characteristic of the mechanisms underlying pulse generation, and hence should be experimentally verifiable. We tested model predictions *in vivo* using optogenetics (Campos and Herbison, 2014; Han et al., 2015; Clarkson et al., 2017a), and showed that we are able to induce LH pulses in estrous mice by selectively exciting KNDy neurons in a continuous fashion between 1 Hz and 5 Hz. *In vitro* arcuate kisspeptin neurons transfected with ChR2 responded with remarkable fidelity (>97%) to optic stimulation in the range 1–20 Hz (Han et al., 2015), eliciting a single action potential for each pulse of light they receive. This highlights the sudden emergence of pulsatile dynamics as we increase optic stimulation from 0.5 Hz to 1 Hz, in par with the qualitative picture predicted by the model. It is also interesting to note that the optic stimulation frequencies for which we start to see an effect on LH pulsatility match the spontaneous activity measured from KNDy neurones in brain slices from intact (~1 Hz), castrated (~5 Hz) and castrated adult male mice treated with estradiol *in vivo* (~1 Hz) (Ruka et al., 2016). Stimulating at 15 Hz elicited LH pulses but at a decreased frequency compared with 5 Hz stimulation. This apparent slowing down of the pulse generator as the basal activity is increased could reflect fatigue of kisspeptin

and/or GnRH secretion at higher stimulation frequencies or even nonlinear dynamics in the processing of GnRH signals by the pituitary (Pratap et al., 2017) and stresses the need for direct *in vivo* measurements of KNDy activity to probe in greater detail the dynamic mechanisms behind pulse generation and shed light on the multiple pulse generator hypothesis.

It is important to note that the model has informed the design of the experiments by suggesting the use of low-frequency optic stimulation for the first time in investigating LH pulse generation and in contrast to previous studies (Campos and Herbison, 2014; Han et al., 2015; Clarkson et al., 2017a). Our results suggest that inhibitory or excitatory synaptic signaling within the KNDy neural population have a drastic effect on GnRH/LH pulse dynamics. We speculate that this enables KNDy neurons to integrate and transmit information regarding the overall state of the organism that is relevant for reproduction: for example, information on the emotional state and stress level through synaptic connections originating at the level of the amygdala (Lin et al., 2011), a key limbic brain structure; or information regarding the nutritional state of the organism through connections from Agouti-related peptide (AgRP)-expressing neurons in the hypothalamus (Padilla et al., 2017).

Finally, the model predicted that the systems' pulsatile behavior emerges as a result of the nonlinear positive and negative feedback interactions that are mediated through NKB and Dyn signaling respectively. Using experimental protocol suggested by model analysis we showed that the response of the system to external optic stimulation indeed follows our NKB and Dyn signaling predictions. Our results highlight the need for a quantitative understanding of how the sex-steroid milieu affects the NKB and Dyn signaling pathways in the KNDy population. Such an understanding will lead to more accurate interpretation of results from *in vivo* neuropharmacological perturbation experiments in various animal models and will shed light on the mechanisms underlying the regulation of pulsatile LH secretion in various natural settings such as lactational amenorrhoea or pharmaceutical interventions including the hormone contraceptive pill. We envision that as hormonal measurement techniques advance (Liang et al., 2019), enabling accurate, real-time readouts from individuals at low cost, such predictive mathematical models would be a valuable tool for understanding of reproductive pathophysiology.

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