



Probing transient excited states of the bacterial cell division regulator MinE by relaxation dispersion NMR spectroscopy

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Bacterial MinD and MinE form a standing oscillatory wave which positions the cell division inhibitor MinC, that binds MinD, everywhere on the membrane except at the midpoint of the cell, ensuring midcell positioning of the cytokinetic septum. During this process MinE undergoes fold switching as it interacts with different partners. We explore the exchange dynamics between major and excited states of the MinE dimer in 3 forms using ¹⁵N relaxation dispersion NMR: the full-length protein (6-stranded β -sheet sandwiched between 4 helices) representing the resting state; a 10-residue N-terminal deletion (Δ 10) mimicking the membrane-binding competent state where the N-terminal helix is detached to interact with membrane; and N-terminal deletions of either 30 (Δ 30) or 10 residues with an I24N mutation (Δ 10/I24N), in which the β 1-strands at the dimer interface are extruded and available to bind MinD, leaving behind a 4-stranded β -sheet. Full-length MinE samples 2 “excited” states: The first is similar to a full-length/ Δ 10 heterodimer; the second, also sampled by Δ 10, is either similar to or well along the pathway toward the 4-stranded β -sheet form. Both Δ 30 and Δ 10/I24N sample 2 excited species: The first may involve destabilization of the β 3- and β 3'-strands at the dimer interface; changes in the second are more extensive, involving further disruption of secondary structure, possibly representing an ensemble of states on the pathway toward restoration of the resting state. The quantitative information on MinE conformational dynamics involving these excited states is crucial for understanding the oscillation pattern self-organization by MinD–MinE interaction dynamics on the membrane.

fold switching | excited states | millisecond exchange dynamics | protein conformational dynamics | self-organizing standing wave

Cell division in bacteria is dependent upon the assembly of a cytokinetic septum, morphogenesis of which is controlled by a large protein assembly called the divisome that comprises several dozen proteins (1, 2). Divisome assembly is initiated by guanosine triphosphate-dependent polymerization of the tubulin homolog FtsZ anchored to the inner membrane by FtsA, forming the so-called Z-ring. Thus, the position of FtsZ polymerization determines the position of the cell division septum. The positioning of FtsZ polymerization is controlled by multiple systems, one of which is the MinC/D/E system that limits FtsZ polymerization to near the center of elongating cells (3–5), thereby ensuring proper partitioning of replicated copies of the chromosome and even inheritance of cellular contents to the daughter cells. MinC is an FtsZ polymerization inhibitor whose membrane localization is determined by its binding partner, MinD, an adenosine 5'-triphosphate (ATP)-dependent membrane-binding protein. In the presence of MinE, which controls MinD–membrane interaction dynamics including its ATPase activity, MinD and MinE self-organize in a cell pole-to-cell pole standing wave oscillatory pattern with a node at the midcell where the time-averaged MinD density, and accompanying MinC density, is at a minimum, directing midcell polymerization

of FtsZ (6). MinC is not required for oscillatory pattern formation per se but tracks the distribution of MinD. This ATP-driven dynamic reaction–diffusion system apparently involves positive feedback loops both in the protein–membrane association phase and membrane dissociation phase of the cycle (7). Throughout this process, the MinE dimer is believed to cycle through different conformational states as it switches its binding partner interaction mode (8–11).

The MinE dimer represents a classical example of a fold-switching protein (12) where major conformational transitions are critical to its function. The resting state of MinE (state I) comprises a 6-stranded β -sheet, 3 from each subunit, sandwiched between 4 helices, 2 from each subunit (9). The N-terminal helix α 1 is referred to as the membrane targeting sequence (MTS), because it is thought to anchor onto the anionic cell membrane via its hydrophobic face and associated positively charged residues when the protein is in the active state (13). Thus, to be in a conformation capable of membrane binding, helix α 1 must first

Significance

Self-organization of bacterial MinD and MinE into a standing oscillatory wave controls midcell positioning of the cytokinetic septum, ensuring equal-sized daughter cells for efficient vegetative growth. During this process, the MinE dimer structure switches folds between the resting state (6-stranded β -sheet sandwiched by 2 pairs of helices), a membrane-binding state (N-terminal helix detached and disordered to latch the membrane), and a MinD-binding state (β -strands at dimer interface extruded to interact with MinD, leaving behind a 4-stranded β -sheet). Using relaxation dispersion NMR, we probe millisecond exchange dynamics between ground and excited states of MinE in 3 forms that mimic the major conformations sampled by MinE. These excited states play crucial roles in membrane binding and MinD interaction processes.

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Data deposition: Atomic coordinates, backbone chemical shift assignments, and experimental restraints have been deposited in the Protein Data Bank (<http://www.wwpdb.org/>) and Biological Magnetic Resonance Data Bank (<http://www.bmrb.wisc.edu/>). The PDB/BMRB ID codes are as follows: wt* ngMinE, 6U6P/30661; Δ 10 ngMinE, 6U6Q/30662; Δ 30 ngMinE, 6U6R/30663; and Δ 10/I24N ngMinE, 6U6S/30664. The BMRB code for the backbone chemical shifts of I24N is 50008.

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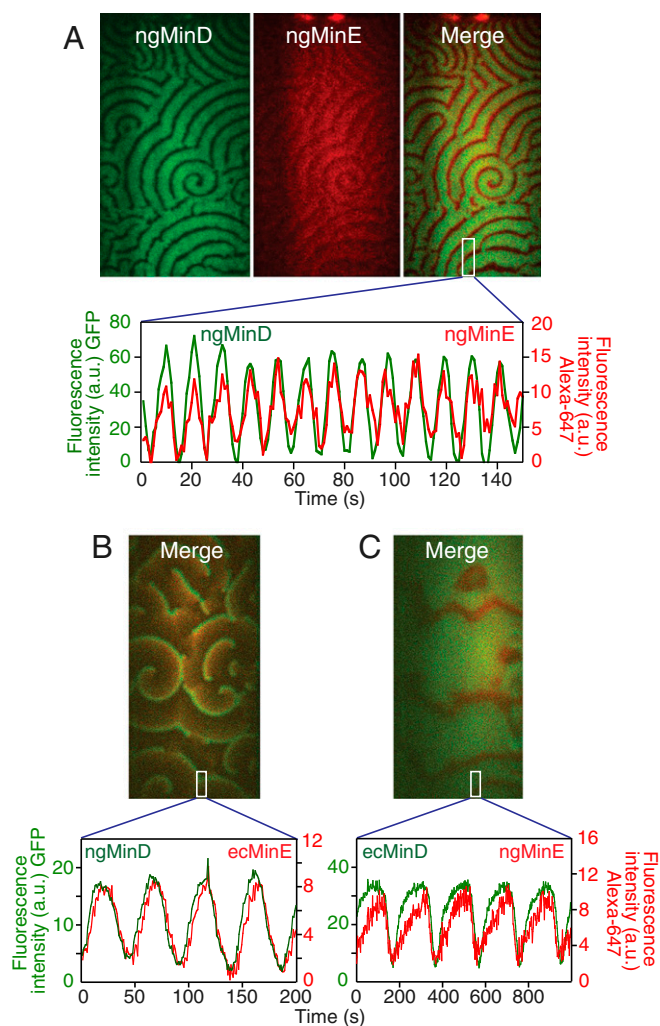


Fig. 1. Oscillatory patterns formed by *N. gonorrhoea* MinD/MinE and combinations of the 2 proteins derived from *N. gonorrhoea* and *E. coli* on supported lipid bilayers monitored by total internal reflection fluorescence microscopy. (A) Spiral wave patterns and temporal oscillation of ngMinD/ngMinE. ngMinE(R10Q/E46A) was labeled with the fluorophore Alexa-647 (red) conjugated to an engineered cysteine (L88C) close to its C terminus. ngMinD was tagged to green fluorescent protein (GFP) at its N terminus. (B) Spiral wave patterns and temporal oscillation of ngMinD/ecMinE. ecMinE was labeled with the fluorophore Alexa-647 (red) conjugated to Cys51. MinD was tagged to GFP at its N terminus. (C) Spiral wave patterns and temporal oscillation of ecMinD/ngMinE(R10Q/E46A). See *SI Appendix* for experimental details.

detach from the 6-stranded sheet (state II). Finally, to bind MinD, the β -strands at the dimer interface must be extruded so that they can interact directly with MinD, leaving behind a 4-stranded β -sheet dimer (state III) (14). When bound to MinD, the extruded β -strand refolds, forming a part of an α -helix that packs against the MinD dimer (10).

Considering the extent of the conformational changes involved, we hypothesized that full-length MinE dimers and truncated or mutant derivatives, that predominantly adopt different structural states, would also likely visit less-populated states resembling those of different conformational states on a short enough time scale to permit their characterization by NMR spectroscopy. To probe and characterize such low occupancy, transient conformational states at the kinetic and structural levels we made use of ^{15}N Carr–Purcell–Meiboom–Gill (CPMG) relaxation dispersion NMR measurements (15–17) on a series of constructs of *Neisseria gonorrhoea* MinE (ngMinE) that are

considered to represent the folded core of the 3 major conformational states (ground states) adopted by MinE at different stages of the pattern self-organization cycle. We show that each construct samples one or more sparsely populated, excited conformational states on the submillisecond to millisecond time scale that provide insights into how fold switching and interconversion between the 3 ground states occurs.

Results and Discussion

N. gonorrhoea MinE and MinD Patterning on Supported Lipid Bilayers.

Wild-type ngMinE has limited solubility that prevents its solution structure determination by NMR and, in our hands, the E46A mutant, employed by Ghasriani et al. (9) to improve solubility, degrades slowly over time due to proteolytic cleavage between Gly9 and Arg10. We therefore mutated Arg10 to Gln, which blocks proteolytic degradation, and the double R10Q/E46A mutant used in the current study is referred to here as wt* ngMinE.

The activity of wt* ngMinE was verified by examining *N. gonorrhoea* MinE/MinD patterning on supported lipid bilayers, as described previously (7, 18) and shown in Fig. 1A. The oscillatory patterning of wt* ngMinE tracks that of ngMinD, organizing propagating waves under standard reaction conditions (*SI Appendix*) adopted from those previously employed to study cell-free *Escherichia coli* MinE/MinD pattern self-organization for this mode of dynamics (7), indicating that wt* ngMinE retains activity in terms of pattern formation. Mutations of positively charged residues within the MTS, such as R10Q, would be predicted to weaken membrane interaction (13) and therefore be expected to exhibit a shortened MinD/MinE oscillation time scale in vitro, shortening the wave length and narrowing the low protein density gaps between the bands of high protein density in the waves (18). The observed oscillation pattern, obtained with

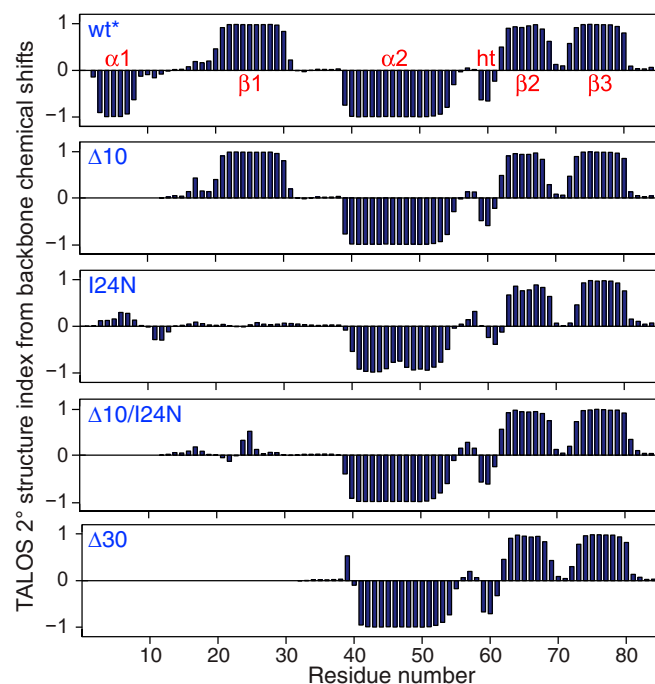


Fig. 2. TALOS secondary structure index derived from backbone ^{15}N , ^{13}C , and ^1H chemical shifts for the various ngMinE constructs (wt*, $\Delta 10$, I24N, $\Delta 10/\text{I24N}$, and $\Delta 30$) used in the current study. Stretches of positive and negative TALOS secondary structures indices are indicative of β -sheet and α -helix, respectively. ht, helical turn.

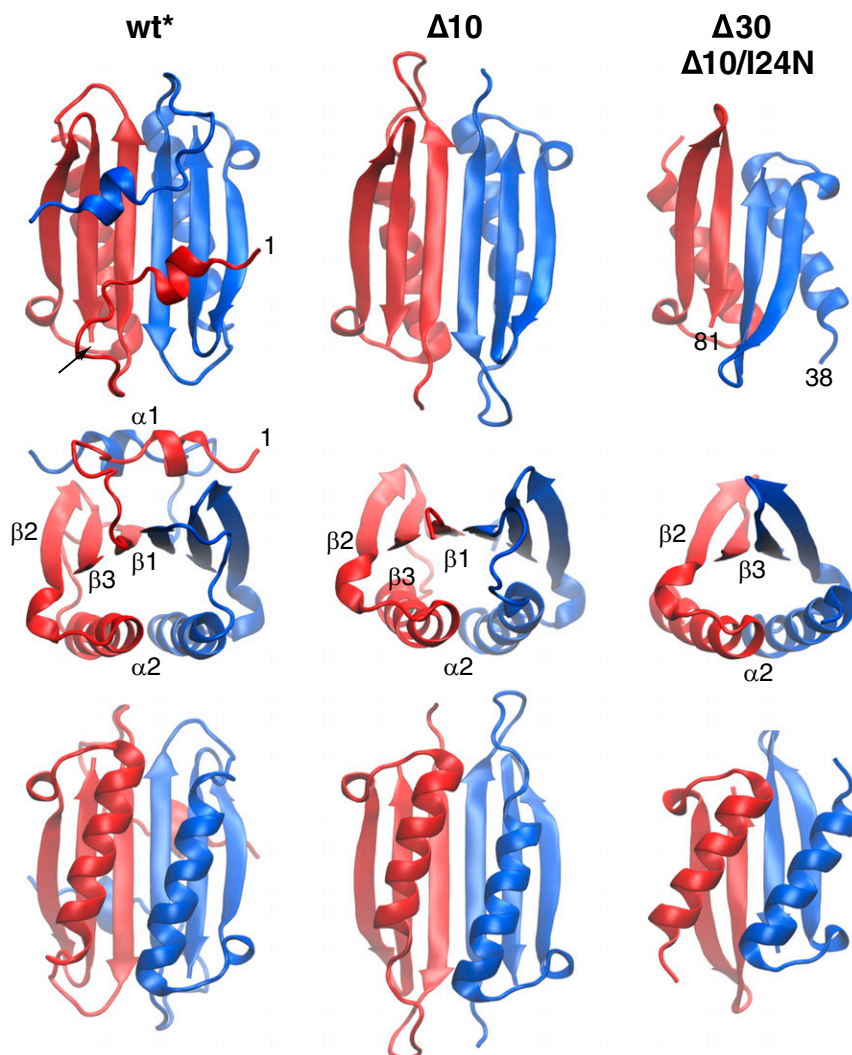


Fig. 3. Ribbon diagrams showing different views of the CS-ROSETTA structures of wt*, $\Delta 10$, and $\Delta 30$ ($\Delta 10/I24N$) ngMinE derived from backbone chemical shifts and $^1D_{NH}$ RDCs. (Note the structures of $\Delta 30$ and $\Delta 10/I24N$ are the same.)

the wt* ngMinE protein studied here, agrees with these expected trends.

To confirm the close functional properties of the ngMin proteins to those of the more extensively studied *E. coli* Min (ecMin) proteins, we tested cell-free pattern self-organization by interspecies mixtures of MinD and MinE under our standard conditions. The combination of ecMinE and ngMinD self-organized into more typical propagating wave patterns resembling those observed with *E. coli* proteins (18–20), indicating that the interaction of ngMinD with ecMinE is functionally close to that between the 2 *E. coli* proteins (Fig. 1B). Propagating wave patterns were also readily observed with the wt* ngMinE and ecMinD combination (Fig. 1C). In this instance, the wave propagation velocity was much slower and the high protein density bands were significantly broader (Fig. 1C). Based on the previous study of the *E. coli* Min system under different reaction conditions and concentrations of MinE (18), the observed wave pattern deviation from the standard patterns with wild-type *E. coli* proteins can be explained by a lower effective concentration of MinE, likely reflecting somewhat compromised interactions between the proteins of the *N. gonorrhoea* and *E. coli* cross-species combination. The observed cross-species complementation among Min proteins in the cell-free system is fully consistent

with in vivo complementation among Min proteins derived from *N. gonorrhoea* in *E. coli* cells reported earlier (21).

Structures of ngMinE Constructs. Five constructs of ngMinE were investigated by NMR spectroscopy: wt* representing the resting state I; a 10-residue N-terminal deletion mutant, $\Delta 10$, representing state II; and I24N, $\Delta 10/I24N$, and $\Delta 30$ ngMinE representing state III. The TALOS-N–predicted secondary structures derived from the backbone (^{15}N , $^{13}C\alpha$, $^{13}C\beta$, $^{13}C'$, and 1H_N) chemical shifts are shown in Fig. 2. The wt* construct comprises 2 α -helices (residues 3 to 8 and 40 to 54) and 3 β -strands (residues 21 to 30, 63 to 69, and 71 to 79). The secondary structure of the $\Delta 10$ construct is identical to that of wt* with the exception that helix $\alpha 1$ is no longer present (Fig. 2). I24N, $\Delta 10/I24N$, and $\Delta 30$ all have the same secondary structure with a single helix and 2 β -strands that correspond to $\alpha 2$, $\beta 2$, and $\beta 3$ of wt* (Fig. 2). The 3-dimensional (3D) folds of the wt*, $\Delta 10$, $\Delta 10/I24N$, and $\Delta 30$ dimers were modeled using the program CS-ROSETTA based on the backbone chemical shifts, supplemented by residual dipolar coupling (RDC) data (22, 23) (see *SI Appendix* for details). CS-ROSETTA makes use of an empirically optimized procedure to select protein fragments from the Protein Data Bank on the basis of sequence and backbone chemical shifts, followed by ROSETTA Monte Carlo assembly, driven in part by the RDC

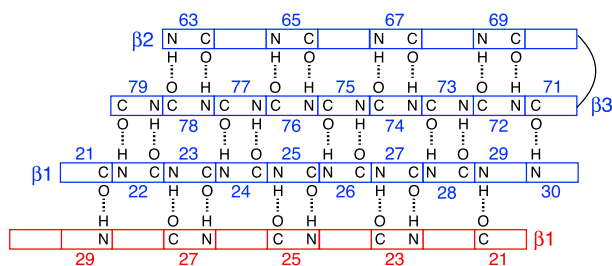
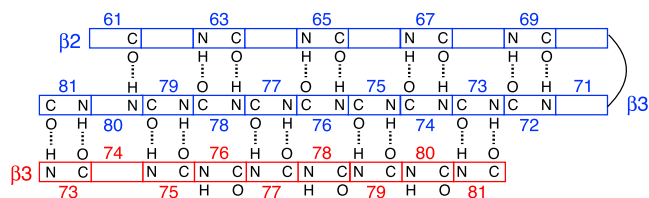
wt* and $\Delta 10$

 $\Delta 10/I24N$ and $\Delta 30$


Fig. 4. β -sheet topology of wt* and $\Delta 10$ (Top), and $\Delta 10/I24N$ and $\Delta 30$ (Bottom) ngMinE constructs derived from the CS-ROSETTA structures. The complete sheet for one subunit is shown in blue, and only the strand of the second subunit located at the dimer interface is shown in red. The registers of the β -sheets, including those at the dimer interface, for both the 6-stranded (wt* and $\Delta 10$) and 4-stranded ($\Delta 10/I24N$ and $\Delta 30$) forms of ngMinE, are fully consistent with the corresponding previously published structures [NMR structure of full-length ngMinE, 2KXO (9); NMR structure of $\Delta 30$ -ecMinE, 1EVO (14); 4.3-Å resolution X-ray structure of I24N ecMinE complexed to MinD, 3R9J (10); these structures were not present in the high-resolution 3D protein coordinate database used in the CS-ROSETTA calculations].

data, to search for compact low-energy folds that are then subject to minimization with an all-atom force field to obtain low-energy models with complementary side-chain packing. The results are shown in Fig. 3. Good structural convergence was obtained with excellent agreement between observed and calculated RDCs (SI Appendix, Fig. S2).

Wt* ngMinE comprises a 6-stranded β -sheet sandwiched between helices $\alpha 1$ and $\alpha 2$ (Fig. 3, Left). This structure, which is in complete agreement with the previously determined solution NMR structure of the E46A mutant of full-length ngMinE (9), is preserved in the $\Delta 10$ construct except that the $\alpha 1$ helix is no longer present (Fig. 3, Middle). The $\beta 1$ strand is located at the dimer interface, and the β -sheet topology, derived from the CS-ROSETTA structures, is shown in Fig. 4, Top. The structure of the $\Delta 10$ construct represents the conformation of the cytoplasmic component of MinE in which helix $\alpha 1$ is no longer packed against the β -sheet but ready to bind to the cell membrane.

The $\Delta 10/I24N$ and $\Delta 30$ constructs share the same structure comprising a 4-stranded β -sheet, with strand $\beta 3$ at the dimer interface (Fig. 4, Bottom), onto which are packed the 2 $\alpha 2$ helices, one from each subunit (Fig. 3, Right). The residues N-terminal to helix $\alpha 2$, which in the case of $\Delta 10/I24N$ include the residues that form strand $\beta 1$ in wt* and $\Delta 10$, are intrinsically disordered as judged by both secondary chemical shifts (Fig. 2) and ^{15}N transverse relaxation rates (SI Appendix, Fig. S1). The structures of $\Delta 10/I24N$ and $\Delta 30$ are in agreement with that of a 30-residue N-terminal truncation of *E. coli* MinE previously determined by NMR (14), except that a small 5-residue N-terminal helix preceding the equivalent of helix $\alpha 2$ is absent in ngMinE. In the complex of ecMinE with ecMinD, the 4-stranded β -sheet form of MinE constitutes the active conformation that binds to MinD via the disordered N-terminal residues that adopt a helical conformation upon complex formation (10).

Conformational Dynamics of ngMinE. Conformational exchange dynamics for wt*, $\Delta 10$, $\Delta 10/24N$, and $\Delta 30$ ngMinE constructs were studied by ^{15}N CPMG relaxation dispersion, which probes exchange between major and sparsely populated species differing in their ^{15}N backbone chemical shifts (15–17). Significant ^{15}N CPMG relaxation dispersions were observed in all 4 cases, indicative of conformational exchange that is intermediate on the chemical shift time scale (Figs. 5 and 6). The ^{15}N CPMG relaxation dispersion curves were concentration-independent over a range of 0.5 to 2 mM for the $\Delta 10$ construct and 1 to 2 mM for the $\Delta 30$ construct (SI Appendix, Fig. S3). Further, analytical ultracentrifugation data on full-length ngMinE (E46A) (9), as well as on the $\Delta 10$ and $\Delta 30$ constructs (SI Appendix, Fig. S4), indicate that the constructs exist as stable dimers with no evidence for the presence of a monomeric species at concentrations as low as 4 to 5 μM . These data further support that the exchange processes observed by ^{15}N CPMG relaxation dispersion do not involve interconversion between a major dimeric form and a minor population of monomer but rather the interconversion between different conformations of the dimer.

Analysis of the ^{15}N CPMG relaxation dispersion data was performed by simultaneously fitting the data for 62, 47, 48, and 39 residues of wt*, $\Delta 10$, $\Delta 10/I24N$, and $\Delta 30$ ngMinE, respectively, to the appropriate McConnell equations (24), optimizing global rate constants for a given kinetic model together with residue-specific chemical shift differences between the states ($\Delta\omega$) and residue specific R_2 transverse relaxation rates (assumed to be the same for major and minor species). Residues were excluded where there was either cross-peak overlap or little to no relaxation dispersion. In addition, the relaxation dispersion data for residues 60, 71, and 74 of the $\Delta 30$ and $\Delta 10/I24N$ constructs were excluded as these residues exhibit unusually large ^{15}N $R_{2,\text{eff}}$ values relative to adjacent residues at a 1-kHz CPMG field (SI Appendix, Fig. S1), suggesting that they are involved in a faster exchange process such that chemical shift exchange line broadening is not fully suppressed (see also SI Appendix, Fig. S5).

While the data for the $\Delta 10$ construct could be well fit to a simple 2-state exchange, the minimal kinetic models required to account for the wt*, $\Delta 10/I24N$, and $\Delta 30$ data comprised linear 3-state exchange systems. (Note that fits to a 3-state branched exchange scheme in which the major species interconverts directly with 2 minor species are significantly worse for the wt* and $\Delta 30$ data both in terms of goodness of fit and the presence of systematic errors in the fits, and slightly worse for the $\Delta 10/I24N$ data, as shown in SI Appendix, Figs. S6–S8, respectively. Further, application of Occam's razor would lead one to expect the same exchange model for the $\Delta 30$ and $\Delta 10/I24N$ constructs.) Examples of ^{15}N CPMG relaxation dispersion data together with the best-fit curves and associated kinetic models, rate constants, and species populations are shown in Fig. 5 (wt* and $\Delta 10$) and Fig. 6 ($\Delta 10/I24N$ and $\Delta 30$).

In the case of the 3-state exchange models, the self-consistency of the residue-specific $\Delta\omega$ values was improved by fitting the data simultaneously to a 2-member, 3-state exchange system where the 2 members share the kinetic rate constants and residue-specific R_2 rates, but in one member the A major state is chosen as the chemical shift reference (i.e., $\omega_A = 0$) while in the second the B minor state is used as the chemical shift reference (i.e., $\omega_B = 0$); the residue-specific $\Delta\omega_{AB}$ values are optimized and shared between the 2 members, the residue-specific $\Delta\omega_{BC}$ values are optimized for the second member only, and the residue-specific $\Delta\omega_{AC}$ values for the first member are given by $\Delta\omega_{AB} + \Delta\omega_{BC}$. This procedure also ensures that the relative sign information of the $\Delta\omega$ values is preserved.

In the case of the $\Delta 30$ and $\Delta 10/I24N$ constructs, the exchange rate ($k_{\text{ex}} = k_{AB} + k_{BA}$) for the A \leftrightarrow B transition is sufficiently slow (180 to 190 s^{-1} ; see Fig. 6) to also be observed by chemical exchange saturation transfer (CEST) spectroscopy (25). Examples

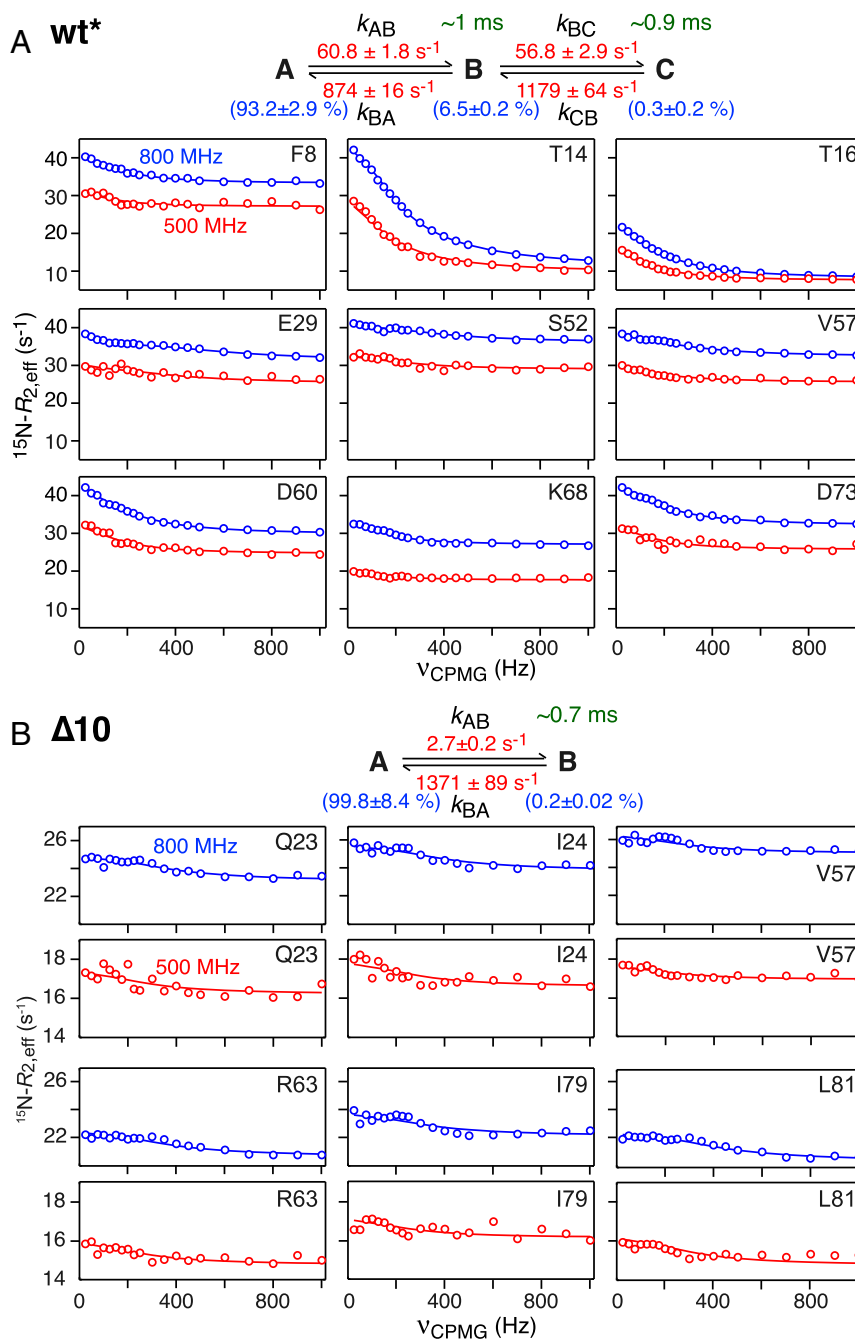


Fig. 5. Nitrogen-15 CPMG relaxation dispersion measurements on wt* and $\Delta 10$ ngMinE constructs. (A) wt* and (B) $\Delta 10$. Representative experimental data (recorded at 25 °C) are shown as circles (blue, 800 MHz; red, 500 MHz) and the best-fit curves to a 3-state linear scheme for wt* and a 2-state scheme for $\Delta 10$ are shown as continuous lines. The rate constants (in red), species populations (in blue), and lifetimes of the excited states (in green) are also indicated.

of CEST profiles for the $\Delta 30$ construct are shown in *SI Appendix, Fig. S9* and are fully consistent with the $\Delta\omega_{AB}$ values obtained from the fits to the CPMG relaxation dispersion data.

Exchange Processes Observed for wt* and $\Delta 10$ ngMinE. The exchange processes involving wt* and $\Delta 10$ are in the millisecond regime with values of ~ 0.7 and ~ 0.5 ms for the $A \leftrightarrow B$ and $B \leftrightarrow C$ transitions in wt* and ~ 0.5 ms for the $A \leftrightarrow B$ transition in the $\Delta 10$ construct (where **A** is the major, spectroscopically observable species). The lifetimes of the **B** and **C** excited states of wt* are ~ 1 and ~ 0.9 ms, respectively, while that of **B** state of the $\Delta 10$ construct is ~ 0.7 ms. The populations of the **C** state of wt* and

the **B** state of $\Delta 10$ are comparable with a value of 0.2 to 0.3%, while that of the intermediate **B** state of wt* is about 20-fold higher ($\sim 6.5\%$).

The differences in ^{15}N chemical shifts between the states provide insight into the nature of the associated conformational transitions. The main determinants of secondary ^{15}N shifts are the ψ_{i-1} and ϕ_i backbone torsion angles of residues $i-1$ and i , respectively; hence, large ^{15}N shifts would be expected in many instances where the conformation of a segment of polypeptide chain shifts from a well-defined ordered structure (such as a helix or sheet) to a random coil (26). Smaller secondary ^{15}N shifts are associated with the rotameric states of residues $i-1$ and i , as well

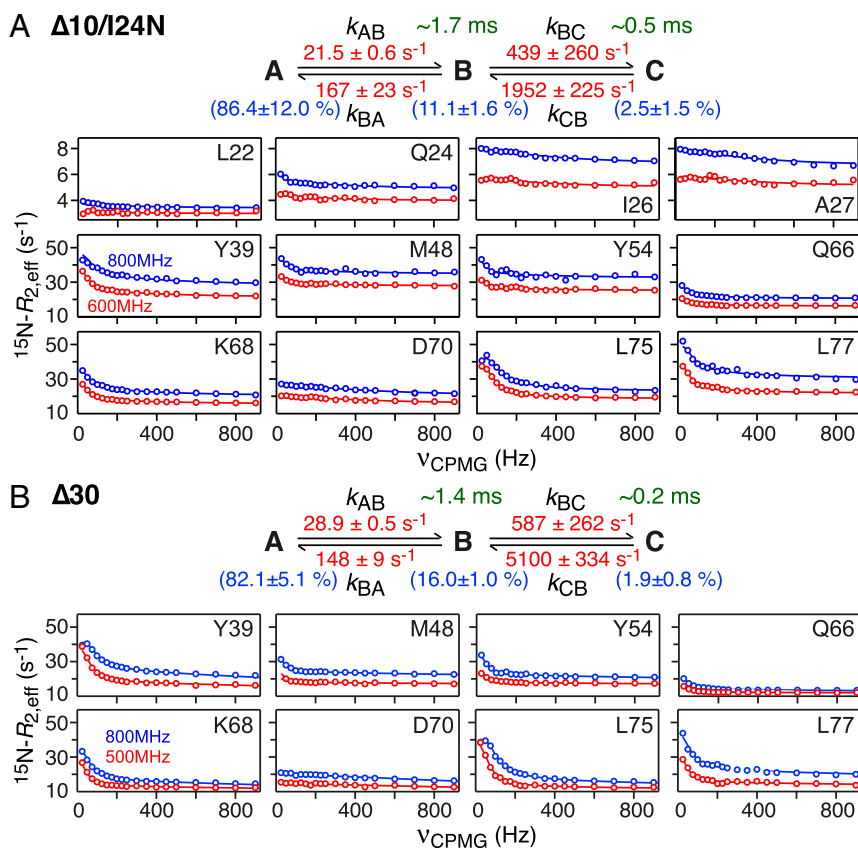


Fig. 6. Nitrogen-15 CPMG relaxation dispersion measurements on $\Delta 10/\Delta 24N$ and $\Delta 30$ MinE constructs. (A) $\Delta 10/\Delta 24N$ and (B) $\Delta 30$. Representative experimental data (recorded at 25 °C) are shown as circles and the best-fit curves to a 3-state linear scheme are shown as continuous lines. The rate constants (in red), species populations (in blue), and lifetimes of the excited states (in green) are also indicated.

as hydrogen bonding of the H_N proton of residue i (26). While $^{13}C\alpha$ secondary shifts provide easily interpretable information on backbone secondary structure (26), unfortunately $^{13}C\alpha$ CPMG measurements on selectively $^{13}C\alpha$ -labeled ngMinE constructs proved not to be feasible owing to large linewidths and poor signal-to-noise ratio.

Plots of the $\Delta\omega_{AB}$ and $\Delta\omega_{BC}$ values for wt* and $\Delta\omega_{AB}$ values for $\Delta 10$ as a function of residue are shown in Fig. 7. It is immediately apparent that the $\Delta\omega_{AB}$ values for wt* (Fig. 7, *Top*) are much smaller than the $\Delta\omega_{BC}$ and $\Delta\omega_{AB}$ values for wt* and $\Delta 10$, respectively, which are clearly correlated with one another (Fig. 7, *Middle* and *Bottom* and Fig. 8C). One can therefore conclude that the conformational changes in the main body of the protein (i.e., excluding helix $\alpha 1$, which is absent in $\Delta 10$) associated with the $B \leftrightarrow C$ and $A \leftrightarrow B$ transitions in wt* and $\Delta 10$, respectively, are similar. It is also worth noting that the good correlation between the wt* $\Delta\omega_{BC}$ values and the $\Delta 10$ $\Delta\omega_{AB}$ values provides further support for the 3-state linear exchange model for wt*.

A comparison of the difference between folded and predicted random coil ^{15}N chemical shifts for the N-terminal 12 residues of wt*, which includes helix $\alpha 1$ (residues 3 to 9), with the corresponding $\Delta\omega_{AB}$ and $\Delta\omega_{BC}$ values for wt* show reasonable correlations but with very different slopes of ~ 6 and ~ 1.1 , respectively (Fig. 8A). This suggests that helix $\alpha 1$ exhibits slightly reduced helicity in state **B** but is effectively disordered in state **C**. Thus, the unstructured N-terminal residues in state **C** can act as a fly-cast (27, 28) to attach wt* ngMinE to the cell membrane.

When heterodimers of wt* and $\Delta 10$ were made by mixing ^{15}N -labeled wt* with a large excess of unlabeled $\Delta 10$, and vice versa,

the difference in ^{15}N chemical shifts between the 2 subunits in the heterodimer for the loop (residues 14 to 19) preceding strand $\beta 1$ is correlated with the corresponding $\Delta\omega_{AB}$ values for wt*; weaker correlations are also observed for residues of strands $\beta 2$ and $\beta 3$, although the differences in ^{15}N chemical shifts are much smaller (Fig. 8B). These data suggest that the **B** state of wt* is similar to the wt*/ $\Delta 10$ heterodimer, and that the reduced helicity of helix $\alpha 1$ in state **B**, noted above, is possibly due to an exchange phenomenon in which only a single $\alpha 1$ helix at a time is detached from the underlying β -sheet within the lifetime of state **B** (~ 1 ms). This interpretation is also supported by the observation that the large dispersions for the loop residues 14 to 16 in the wt* homodimer are significantly reduced in the ^{15}N -labeled wt* chain of the wt*/ $\Delta 10$ heterodimer (*SI Appendix*, Fig. S10). Thus, in state **B**, the probability of 2 $\alpha 1$ helices being detached from the β -sheet surface simultaneously is likely very low, and the slope of ~ 6 for the ^{15}N chemical shift correlation shown in Fig. 8A, *Left* would correspond to a $\sim 30\%$ reduction in the helicity of a single $\alpha 1$ helix. The latter implies that even when a single $\alpha 1$ helix no longer makes contact with the underlying β sheet in state **B**, residues 5 to 9 retain significant helicity and do not locally unfold to a random coil within a ~ 1 -ms time frame.

Further support that state **B** of wt* is similar to the wt*/ $\Delta 10$ heterodimer comes from ^{15}N CPMG relaxation dispersion data recorded on the heterodimer with either wt* or $\Delta 10$ ^{15}N -labeled, and the unlabeled component present at 10-fold excess to ensure the absence of any significant amount of homodimeric ^{15}N -labeled species. Although quantitative analysis of the heterodimer ^{15}N CPMG relaxation data were precluded owing to low signal-to-noise ratio as the ^{15}N -labeled component is only

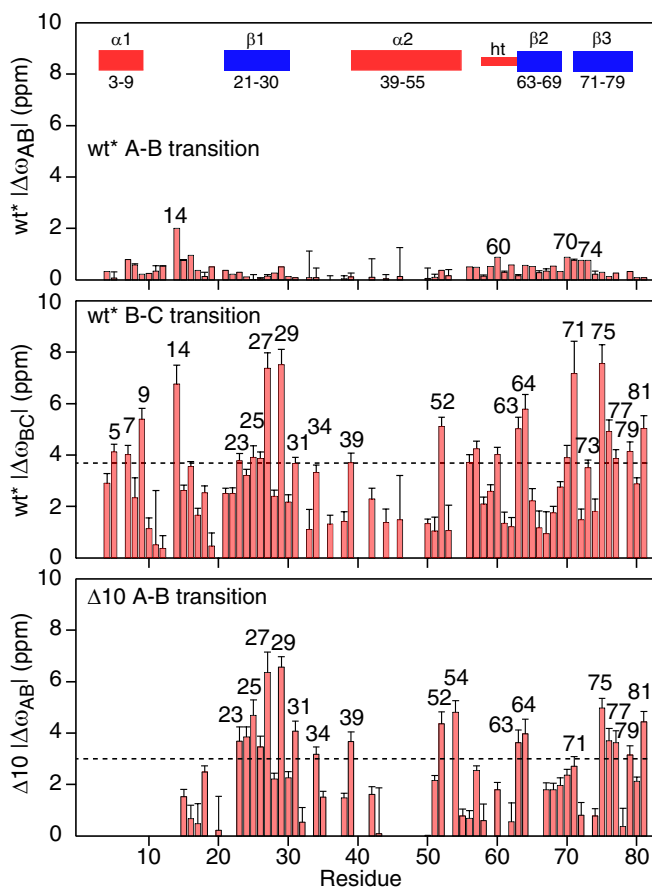


Fig. 7. Profile of ^{15}N chemical shift differences between the exchanging species in wt* and $\Delta 10$ ngMinE constructs derived from the fits to the ^{15}N CPMG relaxation dispersion data.

present at low concentration, the data are sufficient to draw some qualitative inferences. The ^{15}N CPMG dispersion curves for $\Delta 10$ in the context of the homodimer and heterodimer are comparable, suggesting that the $\Delta 10$ chain undergoes a similar 2-state exchange process in both environments. In contrast, residues 14 to 16, located in the loop connecting helix $\alpha 1$ to strand $\beta 1$, show large dispersions in the homodimer that are effectively quenched in the heterodimer (*SI Appendix*, Fig. S10), consistent with only a single $\alpha 1$ helix at a time losing contact with the main body of the protein in state **B** of the wt* homodimer.

The next question is what is the nature of states **C** and **B** of wt* and $\Delta 10$, respectively. The correlation plots of the chemical shift differences between 6-stranded (wt* or $\Delta 10$) and 4-stranded (I24N and $\Delta 10$ /I24N) constructs versus $\Delta\omega_{AC}$ for wt* and $\Delta\omega_{AB}$ for $\Delta 10$ shown in Fig. 9 provide some clues. The top panels depict the correlations for strand $\beta 1$ (residues 21 to 30) and the preceding (residues 15 to 20) and following (residues 31 to 39) loop residues. Two linear correlations are apparent: one with a slope of ~ 0.3 which includes the backbone nitrogens of residues 29 and 27 and those of residues 24, 26, and 30 that participate in intersubunit $\beta 1$ – $\beta 1$ and intrasubunit $\beta 1$ – $\beta 3$ hydrogen bonds, respectively (Fig. 4, *Top*); and the second with a slope of ~ 1.8 which includes the backbone nitrogens of residues 23 and 25 and those of residue 28 that participate in intersubunit $\beta 1$ – $\beta 1$ and intrasubunit $\beta 1$ – $\beta 3$ hydrogen bonds, respectively (Fig. 4, *Top*). These data suggest that state **C** of wt* and state **B** of the $\Delta 10$ construct may represent an intermediate form that is well along the pathway toward the 4-stranded conformation of MinE. This

conclusion is supported by the correlations observed for strands $\beta 2$ and $\beta 3$ shown in Fig. 9, *Bottom*.

Given the ^{15}N chemical shift considerations (Fig. 8C) that indicate that the conformations of the **C** state of wt* and the **B** state of $\Delta 10$ are very similar, it might appear curious that the wt* k_{BC} rate constant is ~ 20 -fold larger than the $\Delta 10$ k_{AB} rate constant. However, the forward and backward rate constants for the overall wt* **A** to **C** interconversion, given by $k_{AB}k_{BC}/(k_{BA} + k_{BC}) \sim 4 \text{ s}^{-1}$ and $k_{CB}k_{BA}/(k_{BA} + k_{BC}) \sim 1,100 \text{ s}^{-1}$, respectively, are comparable to the forward ($k_{AB} \sim 3 \text{ s}^{-1}$) and backward ($k_{BA} \sim 1,400 \text{ s}^{-1}$) rate constants for the $\Delta 10$ **A** \leftrightarrow **B** interconversion.

Exchange Processes Observed for $\Delta 10$ /I24N and $\Delta 30$ ngMinE. Both 4-stranded MinE constructs exhibit similar exchange dynamics (Fig. 6). The intermediate **B** state has an occupancy of 11 to 16% with a lifetime of ~ 1.4 to 1.7 ms. The **C** state has an occupancy of 2 to 2.5%. The lifetime of the **C** state for $\Delta 10$ /I24N (~ 0.5 ms) is about 2.5 times longer than that for $\Delta 30$ (~ 0.2 ms), suggesting the existence of transient interactions between the globular portion of the 2 constructs (comprising helix $\alpha 2$ and strands $\beta 2$ and $\beta 3$) and the intrinsically disordered segment of polypeptide chain preceding helix $\alpha 2$ that are more pronounced in the case of the $\Delta 10$ /I24N construct on account of the longer length of the disordered segment (residues 11 to 38 versus 31 to 38). The $\Delta\omega_{AB}$ values for the 2 constructs, and likewise the $\Delta\omega_{BC}$ values for the 2 constructs, are correlated (Fig. 10A), indicating that the conformations of the **B** and **C** states are probably of a similar nature in the 2 constructs. However, the slopes of the correlations are significantly less than unity, with the $\Delta\omega_{AB}$ and $\Delta\omega_{BC}$ values

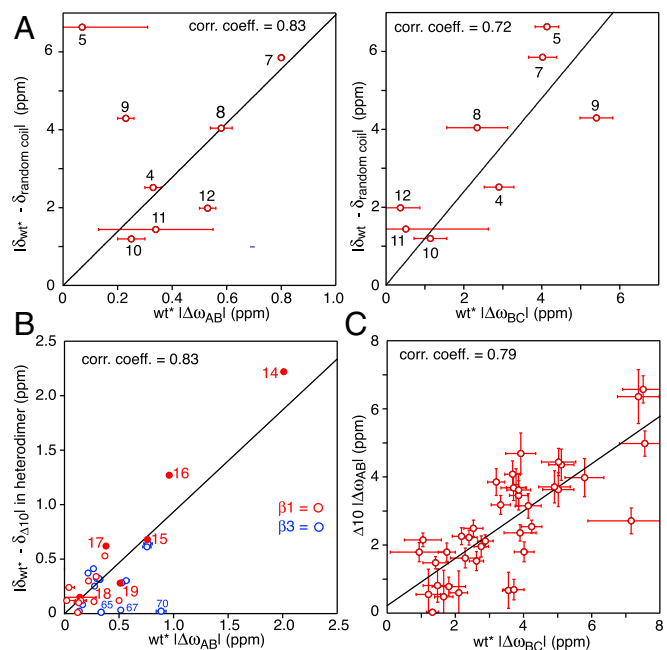


Fig. 8. Nitrogen- ^{15}N chemical shift difference correlations involving wt* and $\Delta 10$ ngMinE constructs. (A) Correlation of the ^{15}N chemical shift differences for residues 5 to 12 (encompassing helix $\alpha 1$ in the wt* construct) between folded and random coil wt* and between the **A** (ground) and **B** (excited) states (*Left*) and between the **B** and **C** excited states (*Right*) of wt*. The random coil shifts for residues 5 to 12 were calculated from the sequence using the algorithm of ref. 40. (B) Correlation of the ^{15}N chemical shift differences for the loop preceding strand $\beta 1$ (residues 14 to 19; solid red circles), strand $\beta 1$ (open red circles), and strand $\beta 3$ (open blue circles) between wt* and $\Delta 10$ in the wt*/ $\Delta 10$ heterodimer and between the **A** (ground) and **B** (excited) states of wt*. (C) Correlation of the ^{15}N chemical shift differences between the **A** ($\Delta\omega_{AB}$) and **B** (excited) states of $\Delta 10$ and the **B** and **C** excited states of wt*.

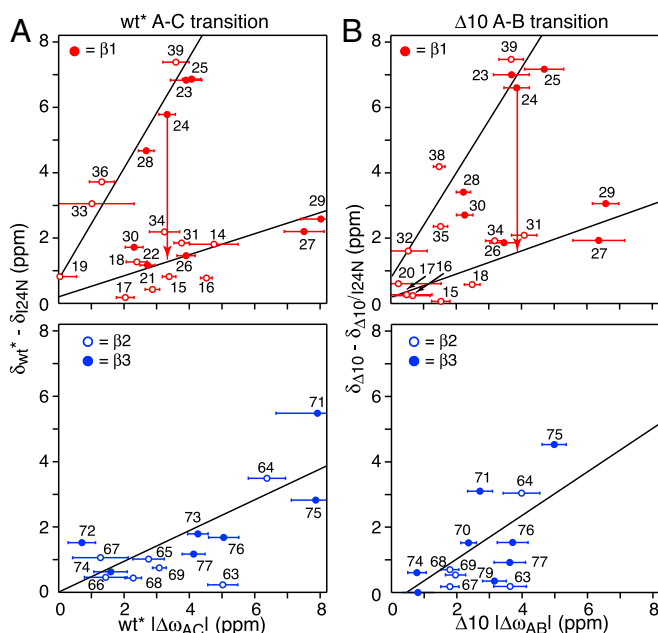


Fig. 9. Correlation of ^{15}N chemical shift changes ($\Delta\omega$) between major (ground) and sparsely populated (excited) states for wt* and $\Delta 10$ determined from ^{15}N CPMG relaxation dispersion and the ^{15}N chemical shift differences between 6-stranded and 4-stranded ground states of ngMinE. (A) Correlation between $\Delta\omega_{\text{AC}}$ values for the wt* A-C transition and the ^{15}N chemical shift differences between wt* (6-stranded) and I24N (4-stranded) constructs. (B) Correlation between $\Delta\omega_{\text{AB}}$ values for the $\Delta 10$ A-B transition and the ^{15}N chemical shift differences between wt* (6-stranded) and $\Delta 10/\text{I}24\text{N}$ (4-stranded) constructs. (Top) The correlations for strand $\beta 1$ (solid circles) as well as residues in loops preceding and following strand $\beta 1$ (open circles); the arrow for residue 24 serves to indicate the chemical shift difference between wt* and predicted random coil values since this residue is mutated from Ile to Asn in the 4-stranded constructs. (Bottom) The correlations for strands $\beta 2$ (open circles) and $\beta 3$ (solid circles). The lines serve purely to guide the eye.

for the $\Delta 30$ construct on average ~ 1.7 - and ~ 2 -fold larger, respectively, than for the $\Delta 10/\text{I}24\text{N}$ construct. This might suggest that the **B** and **C** excited states comprise an ensemble of conformations whose distribution is different in the $\Delta 30$ and $\Delta 10/\text{I}24\text{N}$ constructs as a consequence of transient stabilizing interactions between the long disordered N terminus of the $\Delta 10/\text{I}24\text{N}$ construct and the folded core of the protein. These chemical shift correlation data also indicate that whatever the conformations adopted by the **B** and **C** minor states, they do not represent the 6-stranded conformation of the wt* and $\Delta 10$ ngMinE constructs, since the residues comprising strand $\beta 1$ in wt* and $\Delta 10$ are deleted in the $\Delta 30$ construct.

The **A-B** transition is accompanied by relatively small (1 to 2.5 ppm) ^{15}N shifts (Fig. 10 B, Right) involving the N-terminal residue of helix $\alpha 2$ (residue 39), residue 57 in the loop connecting strand $\beta 2$ to the helical turn, residue 68 in strand $\beta 2$, and residues 75 to 77 and 81 of strand $\beta 3$. It is tempting to suggest that these may reflect partial fraying along the C-terminal half of strand $\beta 3$ and at the N terminus of helix $\alpha 2$ (such that the helix starts at residue 40 in state **B**); residue 57 is in close spatial proximity to strand $\beta 3$, as is residue 68 to the N terminus of helix $\alpha 2$ (Fig. 3, Right).

Larger ^{15}N shifts overall are observed for the **B-C** transition (Fig. 10 B, Right). For the $\Delta 30$ construct (Fig. 10 B, Top Right), $\Delta\omega_{\text{BC}}$ values in the 2- to 5-ppm range are seen within helix $\alpha 2$ (residues 39, 48, 52, 54, and 55), strand $\beta 2$ (residues 63, 64, and 67 to 69), the $\beta 2$ - $\beta 3$ turn (residue 70), and strand $\beta 3$ (residues 72, 73, 75 to 77, and 79 to 81). Residues 69 and 72 are hydrogen-bonded to one another, and residues 73, 75, 77, 79, and 81

participate in hydrogen bonds at the $\beta 3$ - $\beta 3'$ dimer interface (Fig. 4, Bottom). These data are suggestive of significant conformational transitions involving helix $\alpha 2$ and strands $\beta 2$ and $\beta 3$. This is supported by the correlations (albeit relatively weak with a slope significantly less than unity) observed for both the $\Delta 30$ and $\Delta 10/\text{I}24\text{N}$ constructs between the $\Delta\omega_{\text{AC}}$ values of residues in helix $\alpha 2$ and strands $\beta 2$ and $\beta 3$ and the difference in chemical shifts between the major folded **A** species and the predicted random coil shifts (Fig. 11).

Concluding Remarks. Here we have investigated the conformational exchange dynamics exhibited by 3 functionally and structurally distinct ground states of ngMinE: the resting state exemplified by the wt* 6-stranded β -sheet conformation sandwiched by 2 pairs of α -helices; the precursor state for membrane anchoring in which the N-terminal helix no longer lies on the 6-stranded β -sheet but is ready to be anchored to the membrane, mimicked by the $\Delta 10$ truncation mutant in which the N-terminal α -helix is deleted; and the MinD binding competent state in which the internal $\beta 1$ strands at the dimer interface of the resting and membrane-binding precursor configurations are extruded to be ready to interact with MinD, leaving a 4-stranded β -sheet form represented by the $\Delta 10/\text{I}24\text{N}$ and $\Delta 30$ constructs (as well as the I24N construct). Such large conformational transitions imply the presence of extensive conformational dynamics involving minor, “excited” states for each of these forms of the MinE protein. The ^{15}N CPMG relaxation dispersion experiments reveal the presence of conformational exchange on the submillisecond to millisecond time scales: wt*, $\Delta 10/\text{I}24\text{N}$, and $\Delta 30$ constructs exhibit 3-state linear transitions (**A** \leftrightarrow **B** \leftrightarrow **C**) between the major **A** species and 2 minor species **B** and **C**, while the $\Delta 10$ construct displays 2-state transition (**A** \leftrightarrow **B**) between the major **A** and minor **B** species (Figs. 5 and 6).

A comparison of the ^{15}N chemical shift changes accompanying these transitions, obtained from the fits to the ^{15}N CPMG relaxation dispersion data, with differences in the experimental ^{15}N chemical shifts between the various constructs, as well as between the constructs and calculated random coil shifts (Figs. 7–11), are suggestive of the following processes summarized below.

The **A** \leftrightarrow **B** transition in wt* involves the interconversion of the resting state to a state that is similar to that of a wt*/ $\Delta 10$ heterodimer and in which the N-terminal α -helix of one subunit no longer contacts the underlying β sheet and hence exhibits reduced helicity (presumably due to rapid interconversion between helical and intrinsically disordered conformations). The **B** \leftrightarrow **C** wt* transition involves complete disordering of the N-terminal helix of both subunits, in conjunction with a conformational transition involving the β -sheet that is similar to that accompanying the **A** \leftrightarrow **B** transition in the $\Delta 10$ construct. The ^{15}N chemical shift differences between the **A** and **C** states of wt* and between the **A** and **B** states of the $\Delta 10$ construct reveal correlations with the ^{15}N chemical shift differences between the 6-stranded (wt* and $\Delta 10$) and 4-stranded (I24N and $\Delta 10/\text{I}24\text{N}$, respectively) forms of ngMinE, suggesting that both the wt* and $\Delta 10$ constructs perhaps sample a state close to the major ground state of the I24N and $\Delta 10/\text{I}24\text{N}$ constructs with the N-terminal parts of the protein disordered.

The sparsely populated states sampled by the two 4-stranded constructs ($\Delta 10/\text{I}24\text{N}$ and $\Delta 30$) are similar. In each instance the excited species appear to comprise an ensemble of conformations whose distribution is different in the $\Delta 30$ and $\Delta 10/\text{I}24\text{N}$ constructs, presumably as a result of stabilizing, transient interactions involving the long, disordered N-terminal segment of $\Delta 10/\text{I}24\text{N}$. The **A** \leftrightarrow **B** transition may involve partial destabilization of the $\beta 3$ - $\beta 3'$ sheet at the dimer interface. The **B** \leftrightarrow **C** transition is more extensive, suggesting further disruption and/or destabilization of the $\beta 3$ - $\beta 3'$ interface and a portion of the $\beta 2$ - $\beta 3$ sheet formed by the N-terminal end of the latter and the

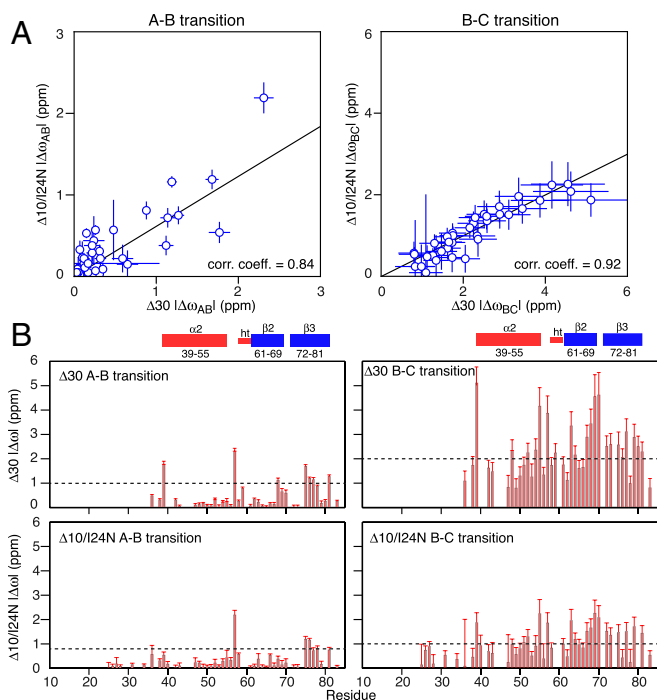


Fig. 10. Nitrogen-15 chemical shift differences between species for $\Delta_{10/I24N}$ and Δ_{30} MinE constructs. (A) Correlation of chemical shift differences observed for the Δ_{30} and $I24N/\Delta_{10}$ constructs between species A (ground state) and the excited state B (Left) and between the excited state species B and C (Right). (B) Profile of ^{15}N chemical shift differences between the exchanging species in Δ_{30} (Top) and $\Delta_{10/I24N}$ (Bottom) derived from the fits to the ^{15}N CPMG relaxation dispersion data. (Left) Difference between the major ground state species A and the minor excited state species B. (Right) Difference between the minor excited state species B and C.

C-terminal end of the former, as well as a transient reduction in helicity of helix α_2 . Thus, the C state of the 4-stranded forms of ngMinE may represent an ensemble of states along the restoration pathway from the 4-stranded to 6-stranded conformations. The wt* and Δ_{10} constructs presumably also visit similar states corresponding to the minor states detected for $\Delta_{10/I24N}$ and Δ_{30} constructs but are not expected to be sufficiently populated to be experimentally detectable as separate states.

The major conformational ground states studied here correspond well to those described in previous crystallographic and NMR structural studies and are expected to play important roles at different steps of MinD/MinE pattern self-organization (9, 10, 14). Here we showed that full-length wt* ngMinE visits transient excited states that are close to the major states of N-terminal deletion constructs, and we successfully measured the equilibrium and transition rate parameters between the different states. We also detected additional excited states that perhaps lie along the reverse path from 4-stranded to 6-stranded core states. The finding that excited states along the fold-switching energy landscape are sampled by the major species is reminiscent of the situation with dihydrofolate reductase where intermediates in the catalytic cycle sample conformations that are close to the ground states of the preceding and following intermediates (29).

The conformational transitions observed for ngMinE take place on time scales that are 5 to 6 orders of magnitude faster (Figs. 5 and 6) than the time scale of ngMinD/ngMinE self-organized oscillation on the lipid bilayer (Fig. 1), indicating that the interconversions between ground and excited states per se are not rate-limiting. Nevertheless, the information obtained here on the occupancies and residence time scales of

these excited states is invaluable for an understanding of MinE–membrane–MinD interaction dynamics during the oscillatory pattern self-organization cycle, considering that these sparsely populated species represent intermediates for these multicomponent interaction processes. Further, the large separation of time scales between the lifetimes of the excited states and the period of the oscillatory waves allows for many cycles of conformational rearrangement and fold switching to occur until optimal configurations are obtained for interaction with the appropriate partner. Thus, the rapid excursion between ground and excited states can be thought of as a bath coupled to binding reactions with interaction partners, in a manner analogous to that found for the multisubstrate enzyme adenylyl kinase where rapid exchange between closed and open states eventually leads to a conformation that permits a chemical reaction (phosphoryl transfer) to occur between 2 substrates (30). Critical questions, however, remain to be addressed concerning the impact of MinE interaction partners, specifically the membrane and MinD, on the conformational dynamics, which are left to be addressed in a future study.

Experiment

Details of protein expression and purification, isotope labeling, NMR experimental details, quantitative analysis of ^{15}N CPMG relaxation dispersion data, structural modeling with CS-ROSETTA, and MinE/MinD spatial patterning experiments on supported lipid bilayers monitored by total internal reflection fluorescence microscopy are provided in *SI Appendix*. The complete set of CPMG relaxation dispersion data is provided in *SI Appendix*, Figs. S11–S14, and the optimized values of the residue-specific parameters ($R_{2,\text{eff}}$ values

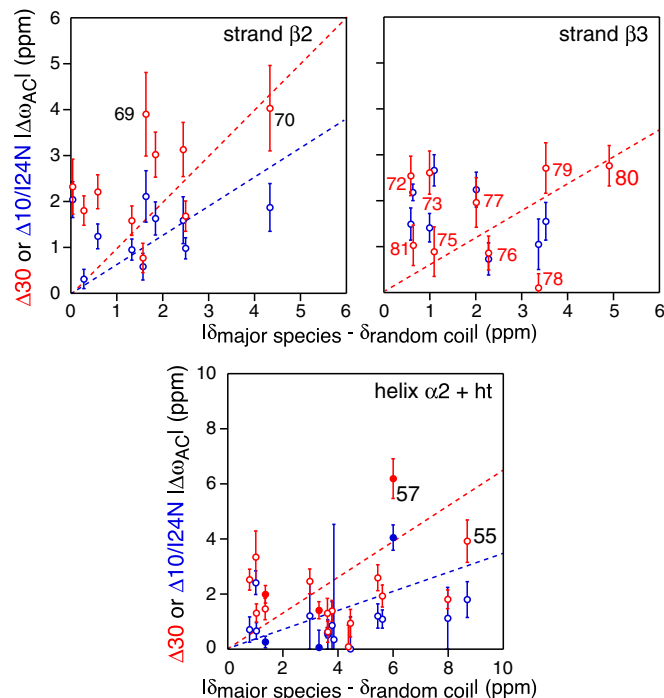


Fig. 11. Correlation of ^{15}N chemical shift differences between the ground state A and the excited state C for the $\Delta_{10/I24N}$ and Δ_{30} constructs determined from ^{15}N CPMG relaxation dispersion, and the differences in chemical shifts between folded and random coil states. The correlations for Δ_{30} and $\Delta_{10/I24N}$ are shown in red and blue, respectively. (Top) β_2 -strand including the first residue (Asp70) of the β_2 – β_3 turn. (Middle) β_3 strand. (Bottom) α_2 -helix, helical turn, and loop connecting them. The correlations for the helical turn (ht) and the short loop connecting the helix to the helical turn are shown as solid circles. The dashed lines serve to guide the eye. The random coil shifts were calculated from the sequence using the algorithm of ref. 40.

at 2 spectrometer frequencies and $\Delta\omega$ values) are listed in *SI Appendix, Tables S1–S4*.

Atomic coordinates, backbone chemical shift assignments and experimental restraints have been deposited in the Protein Data Bank (<http://www wwvwpdb.org/>) and Biological Magnetic Resonance Data Bank (<http://www wwvwmrb.wisc.edu/>). The PDB/BMRB codes are as follows: wt* ngMinE, 6U6P (31)/30661 (32); $\Delta 10$ ngMinE, 6U6Q (33)/30662 (34); $\Delta 30$ ngMinE, 6U6R

(35)/30663 (36); $\Delta 10/124N$ ngMinE, 6U6S (37)/30664 (38). The BMRB code for the backbone chemical shifts of 124N is 50008 (39).

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