



Erratum

# Erratum to: Marginal measures and causal effects using the relative survival framework

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The originally published version of this article contained some errors in the setting of some equations (see below). These have now been corrected. OUP apologises for this error.

Published version (wrong version)	How it should be (RIGHT version)
<i>Corrections in section: Marginal relative survival</i>	
<i>Page 3</i>	
$R(t Z_2)$	$R(t Z_2)$
<i>Equation 2</i>	
$\theta(t) = E[R(t Z_2)]$	$\theta(t) = E[R(t Z_2)]$
<i>Page 4</i>	
$\hat{\theta}(t) = \frac{1}{N} \sum_{i=1}^N \hat{R}(t Z_2 = z_{2i})$	$\hat{\theta}(t) = \frac{1}{N} \sum_{i=1}^N \hat{R}(t Z_2 = z_{2i})$
<i>Page 4</i>	
$\hat{\theta}(t) = \frac{1}{N} \sum_{i=1}^N w_i \hat{R}(t, Z_2 = z_{2i})$	$\hat{\theta}(t) = \frac{1}{N} \sum_{i=1}^N w_i \hat{R}(t Z_2 = z_{2i})$
<i>Corrections in section: Marginal all-cause survival</i>	
<i>Equation 3</i>	
$\theta(t) = E[S(t Z)] = E[S^*(t Z_1)R(t Z_2)]$	$\theta(t) = E[S(t Z)] = E[S^*(t Z_1)R(t Z_2)]$
<i>Page 4</i>	
$\hat{\theta}(t) = \frac{1}{N} \sum_{i=1}^N S^*(t Z_1 = z_{1i}) \hat{R}(t Z_2 = z_{2i})$	$\hat{\theta}(t) = \frac{1}{N} \sum_{i=1}^N S^*(t Z_1 = z_{1i}) \hat{R}(t Z_2 = z_{2i})$
<i>Corrections in section: Marginal crude probabilities of death</i>	
<i>Page 4</i>	
$F_c(t Z)$	$F_c(t Z)$
<i>Page 4</i>	
$F_o(t Z)$	$F_o(t Z)$
<i>Page 4</i>	
$\theta_c(t) = E[F_c(t Z)] = E\left[\int_0^t S^*(u Z_1)R(u Z_2)\lambda(u Z_2)du\right]$	$\theta_c(t) = E[F_c(t Z)] = E\left[\int_0^t S^*(u Z_1)R(u Z_2)\lambda(u Z_2)du\right]$

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Published version (wrong version)

How it should be (RIGHT version)

Page 4

$$\hat{\theta}_c(t) = \frac{1}{N} \sum_{i=1}^N \hat{F}_c(t|Z = z_i)$$

$$= \frac{1}{N} \sum_{i=1}^N \int_0^t S^*(u|Z_1 = z_{1i}) \hat{R}(u|Z_2 = z_{2i}) \hat{\lambda}(u|Z_2 = z_{2i}) du$$

$$\hat{\theta}_c(t) = \frac{1}{N} \sum_{i=1}^N \hat{F}_c(t|Z = z_i)$$

$$= \frac{1}{N} \sum_{i=1}^N \int_0^t S^*(u|Z_1 = z_{1i}) \hat{R}(u|Z_2 = z_{2i}) \hat{\lambda}(u|Z_2 = z_{2i}) du$$

Page 4

$$\hat{\theta}_o(t) = \frac{1}{N} \sum_{i=1}^N \hat{F}_o(t|z_i)$$

$$= \frac{1}{N} \sum_{i=1}^N \int_0^t S^*(u|Z_1 = z_{1i}) \hat{R}(u|Z_2 = z_{2i}) h^*(u|Z_1 = z_{1i}) du$$

$$\hat{\theta}_o(t) = \frac{1}{N} \sum_{i=1}^N \hat{F}_o(t|Z = z_i)$$

$$= \frac{1}{N} \sum_{i=1}^N \int_0^t S^*(u|Z_1 = z_{1i}) \hat{R}(u|Z_2 = z_{2i}) h^*(u|Z_1 = z_{1i}) du$$

Corrections in section: Relative survival differences

Page 5

$$\frac{1}{N} \sum_{i=1}^N \hat{R}(t|X = 1, Z_2 = z_{2i}) - \frac{1}{N} \sum_{i=1}^N \hat{R}(t|X = 0, Z_2 = z_{2i})$$

$$\frac{1}{N} \sum_{i=1}^N \hat{R}(t|X = 1, Z_2 = z_{2i}) - \frac{1}{N} \sum_{i=1}^N \hat{R}(t|X = 0, Z_2 = z_{2i})$$

Corrections in section: All-cause survival differences

Equation 5

$$E[S^*(t|X = 1, Z_1)R(t|X = 1, Z_2)]$$

$$- E[S^*(t|X = 0, Z_1)R(t|X = 0, Z_2)]$$

$$E[S^*(t|X = 1, Z_1)R(t|X = 1, Z_2)]$$

$$- E[S^*(t|X = 0, Z_1)R(t|X = 0, Z_2)]$$

Page 5

$$\frac{1}{N} \sum_{i=1}^N S^*(t|X = 1, Z_1 = z_{1i}) \hat{R}(t|X = 1, Z_2 = z_{2i})$$

$$- \frac{1}{N} \sum_{i=1}^N S^*(t|X = 0, Z_1 = z_{1i}) \hat{R}(t|X = 0, Z_2 = z_{2i})$$

$$\frac{1}{N} \sum_{i=1}^N S^*(t|X = 1, Z_1 = z_{1i}) \hat{R}(t|X = 1, Z_2 = z_{2i})$$

$$- \frac{1}{N} \sum_{i=1}^N S^*(t|X = 0, Z_1 = z_{1i}) \hat{R}(t|X = 0, Z_2 = z_{2i})$$

Corrections in section: Forming contrasts within subsets of the population

Equation 6

$$E[S^*(t|X = 1, Z_1^{X=1})R(t|X = 1, Z_2^{X=1})]$$

$$- E[S^*(t|X = 0, Z_1^{X=1})R(t|X = 0, Z_2^{X=1})]$$

$$E[S^*(t|X = 1, Z_1^{X=1})R(t|X = 1, Z_2^{X=1})]$$

$$- E[S^*(t|X = 0, Z_1^{X=1})R(t|X = 0, Z_2^{X=1})]$$

Page 6

$$\frac{1}{N^{X=1}} \sum_{i=1}^{N^{X=1}} S^*(t|X = 1, Z_1^{X=1} = z_{1i}) \hat{R}(t|X = 1, Z_2^{X=1} = z_{2i})$$

$$- \frac{1}{N^{X=1}} \sum_{i=1}^{N^{X=1}} S^*(t|X = 0, Z_1^{X=1} = z_{1i}) \hat{R}(t|X = 0, Z_2^{X=1} = z_{2i})$$

$$\frac{1}{N^{X=1}} \sum_{i=1}^{N^{X=1}} S^*(t|X = 1, Z_1^{X=1} = z_{1i}) \hat{R}(t|X = 1, Z_2^{X=1} = z_{2i})$$

$$- \frac{1}{N^{X=1}} \sum_{i=1}^{N^{X=1}} S^*(t|X = 0, Z_1^{X=1} = z_{1i}) \hat{R}(t|X = 0, Z_2^{X=1} = z_{2i})$$

Corrections in section: Eliminating cancer-related differences

Equation 7

$$E[S^*(t|X = 1, Z_1^{X=1})R(t|X = 1, Z_2^{X=1})]$$

$$- E[S^*(t|X = 1, Z_1^{X=1})R(t|X = 0, Z_2^{X=1})]$$

$$E[S^*(t|X = 1, Z_1^{X=1})R(t|X = 1, Z_2^{X=1})]$$

$$- E[S^*(t|X = 1, Z_1^{X=1})R(t|X = 0, Z_2^{X=1})]$$

Page 6

$$\frac{1}{N^{X=1}} \sum_{i=1}^{N^{X=1}} S^*(t|X = 1, Z_1^{X=1} = z_{1i}) \hat{R}(t|X = 1, Z_2^{X=1} = z_{2i})$$

$$- \frac{1}{N^{X=1}} \sum_{i=1}^{N^{X=1}} S^*(t|X = 1, Z_1^{X=1} = z_{1i}) \hat{R}(t|X = 0, Z_2^{X=1} = z_{2i})$$

$$\frac{1}{N^{X=1}} \sum_{i=1}^{N^{X=1}} S^*(t|X = 1, Z_1^{X=1} = z_{1i}) \hat{R}(t|X = 1, Z_2^{X=1} = z_{2i})$$

$$- \frac{1}{N^{X=1}} \sum_{i=1}^{N^{X=1}} S^*(t|X = 1, Z_1^{X=1} = z_{1i}) \hat{R}(t|X = 0, Z_2^{X=1} = z_{2i})$$

Corrections in section: Avoidable deaths

Page 7

$$D_1(t|X = 1) = N^* [1 - E[S^*(t|X = 1, Z_1^{X=1})R(t|X = 1, Z_2^{X=1})]]$$

$$D_1(t|X = 1) = N^* [1 - E[S^*(t|X = 1, Z_1^{X=1})R(t|X = 1, Z_2^{X=1})]]$$

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How it should be (RIGHT version)

Page 7

$$D_{R_0}(t|X=1) = N^* [1 - E[S^*(t|X=1, Z_1^{X=1})R(t|X=0, Z_2^{X=1})]]$$

$$D_{R_0}(t|X=1) = N^* [1 - E[S^*(t|X=1, Z_1^{X=1})R(t|X=0, Z_2^{X=1})]]$$

Equation 8

$$AD_{R_0} = D_1(t|X=1) - D_{R_0}(t|X=1)$$

$$AD_{R_0} = D_1(t|X=1) - D_{R_0}(t|X=1)$$

Equation 9

$$N^* \left[ 1 - \frac{1}{N^{X=1}} \sum_{i=1}^{N^{X=1}} S^*(t|X=1, Z_1^{X=1} = z_{1i}) \hat{R}(t|X=x, Z_2^{X=1} = z_{2i}) \right]$$

$$N^* \left[ 1 - \frac{1}{N^{X=1}} \sum_{i=1}^{N^{X=1}} S^*(t|X=1, Z_1^{X=1} = z_{1i}) \hat{R}(t|X=x, Z_2^{X=1} = z_{2i}) \right]$$