

Phase-Resolved Surface Plasmon Scattering Probed by Cathodoluminescence Holography

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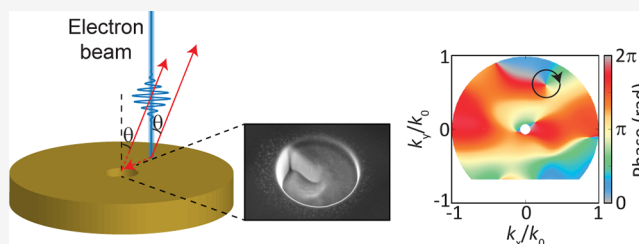
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ABSTRACT: High-energy (1–100 keV) electrons can coherently couple to plasmonic and dielectric nanostructures, creating cathodoluminescence (CL) of which the spectral features reveal details of the material's resonant modes at a deep-subwavelength spatial resolution. While CL provides fundamental insight in optical modes, detecting its phase has remained elusive. Here, we use Fourier-transform CL holography to determine the far-field phase distribution of fields scattered from plasmonic nanoholes, nanocubes, and helical nanoapertures and reconstruct the angle-resolved phase distributions. From the derived fields, we derive the relative strength and phase of induced scattering dipoles. Fourier-transform CL holography opens up a new world of coherent light scattering and surface wave studies with nanoscale spatial resolution.

KEYWORDS: cathodoluminescence, holography, transition radiation, plasmonics, nanoantennas, phase singularity



Cathodoluminescence (CL) spectroscopy is a unique technique to create and probe optical materials excitations at nanoscale spatial resolution.¹ In coherent CL a sample is directly polarized by the time-varying electric fields carried by a high-energy (1–100 keV) electron beam.^{2,3} Each electron creates a single electromagnetic field cycle in the sample with a duration of a few hundred attoseconds with a corresponding frequency spectrum with energies in the 0–30 eV spectral range. The electron thus acts as a broadband source of optical excitation with a spatial resolution limited by the extent of its evanescent field (~ 10 nm).⁴ The electron-induced polarization excitations can then decay by optical radiation (CL) that is collected in the far field.

CL spectroscopy directly probes the radiative local density of optical states, and spatial maps of the CL spectrum probe detailed information on optical modes in photonic nanostructures at deep-subwavelength spatial resolution.^{2,4–6} Several CL modalities have been developed recently: angle-resolved CL spectroscopy provides a direct measure of photonic bandstructures;^{3,4} CL polarimetry provides the full polarization state,⁷ and $g^{(2)}(\tau)$ two-photon correlation spectroscopy provides quantum statistics of emitted CL photons.^{8,9} A key parameter in CL spectroscopy is measurement of the wavefront of the emitted light. Phase information is crucial to reconstruct the nature of the electron-induced polarization densities in CL spectroscopy and, in general, to control the structure of scattered optical wavefronts, which is key to many applications in imaging, integrated optics, optical computing, optical communication, and more.

Previously, we have studied the cathodoluminescence generated by plasmon polaritons scattered from nanoscale

gratings in Ag and found it strongly interferes with transition radiation generated by the same electron.¹⁰ This interference directly represents the phase of the scattered fields, as recently also shown in ref 11. Fourier-transform CL holography can be used to determine from the measured interference pattern the far-field phase distribution of scattered fields with nanoscale spatial excitation resolution.^{12–14} Fourier-transform holography was previously applied in other fields.^{15–19} In our work we analyze the CL signal that originates from electron-beam excited surface plasmon polaritons (SPPs), hybrid light-matter waves that propagate in two dimensions at the interface between a metal and a dielectric. Their strong electric and magnetic fields confined to the interface provide unique ways to control light-matter interactions at the nanoscale. SPPs can carry information in miniature integrated circuits,²⁰ enable efficient sensors,²¹ and couple efficiently to quantum emitters.^{22,23} In all these 2D-confined geometries, precise control over SPP scattering is essential in order to control coupling to the third dimension.

We use 30 keV electrons to excite SPPs that propagate at a Ag/SiO_x interface and subsequently scatter by suitably designed plasmonic scatterers. The scattered light interferes with transition radiation (TR) that is excited by the same

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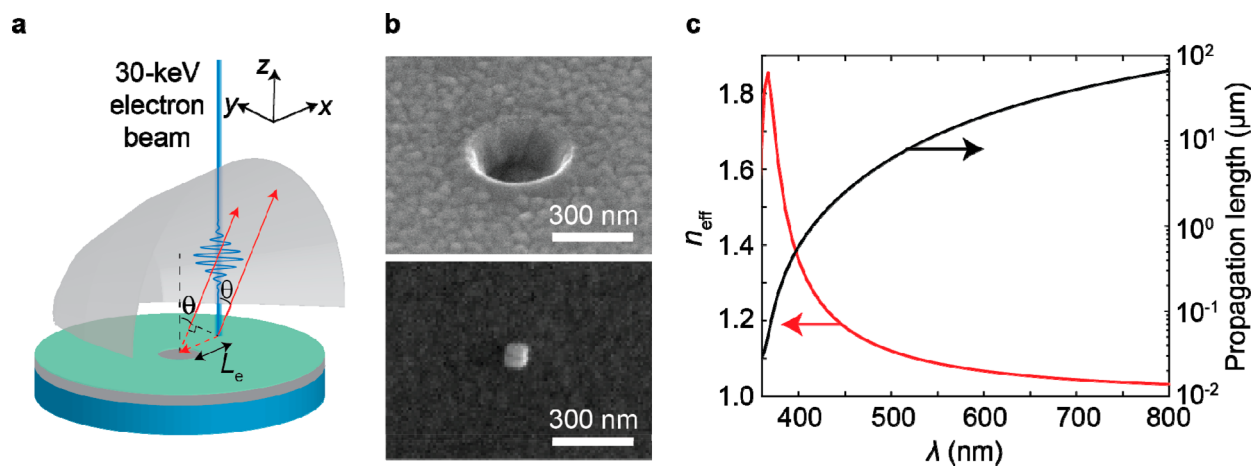


Figure 1. Cathodoluminescence geometry, Ag sample, and surface plasmon polariton dispersion. (a) Schematic of experiment. A 30-keV electron wave packet hits onto a SiO_x (15 nm)/Ag (200 nm)/Si stack and generates broadband transition radiation (TR) and surface plasmon polaritons (SPP). The SPPs scatter from a nanohole, nanocube or nanohelix that is placed at a distance L_e from the excitation point. One example of a TR trajectory toward the parabolic mirror under an angle θ is given as a red solid line. One example of a SPP trajectory is given as a combination of two red lines, where the dashed part is the path difference with respect to TR. Both TR and radiation from scattered SPPs are collimated by a parabolic mirror and projected onto a CCD array. (b) SEM images of 215 nm deep 300 nm diameter nanohole in the layer stack (top) and 75 nm Ag nanocube on the layer stack (bottom). (c) Effective index of SPP mode: $\text{Re}(n_{\text{SPP}})$ and propagation length: $1/[2\text{Im}(k_0 n_{\text{SPP}})]$ of SPP mode derived from the optical constants obtained from spectroscopic ellipsometry of the layer stack.

electron at the point of impact and that serves as a reference field with known phase and polarization.^{3,10,11,24} Applying Fourier-transform CL holography, we reconstruct the angle-resolved amplitude and phase distribution of the p-polarized scattered fields originating from a subwavelength hole in a Ag film. Applying the same technique to a single-crystal Ag nanocube (NC) deposited on the Ag/SiO_x stack, which forms a gap plasmon resonance, we retrieve the π -phase jump for light scattered at frequencies across the resonance. Moreover, Fourier-transform CL holography reveals that helical nanoapertures made in a single-crystal gold surface convert SPPs to free-space waves with pronounced phase singularities. The measurements take advantage of the 10 nm spatial resolution of CL excitation spectroscopy, establishing Fourier-transform CL holography as a powerful deep-subwavelength technique to study scattering phenomena of surface waves and (resonant) nanostructures.

A 200 nm thick Ag film was deposited on a Si(100) substrate using thermal evaporation. Subsequently, a 15 nm thin SiO_x film was deposited to avoid oxidation of the Ag film. Spectroscopic ellipsometry was used to characterize the optical constants and layer thicknesses (see section 1 of the Supporting Information). From these data we derived the SPP dispersion at the Ag/SiO_x interface; the SPP mode effective index and the propagation length are shown in Figure 1c. Focused ion beam milling using 30 keV Ga ions was used to fabricate 300 nm diameter holes in the Ag/SiO_x stack with a depth of 215 nm [see Figure 1b (top)]. On the same multilayer substrate, we drop-casted 75 nm sized single-crystalline Ag nanocubes [NCs; see Figure 1b (bottom)]. The NCs were made using the synthesis procedure as described in ref 25. This procedure leads to a highly monodisperse solution of Ag NCs that are functionalized by polyvinylpyrrolidone (PVP) ligands. Fabrication details on thin-film growth and chemical synthesis of Ag nanocubes are given in the Methods section. Focused ion beam milling using 30 keV Ga ions was used to fabricate helical nanoapertures on the (111) surface of

polished single-crystalline Au. The helical nanoapertures have a diameter of 940 nm and a maximum depth of 570 nm.

CL experiments were performed using a scanning electron microscope (SEM, $V_{\text{acc}} = 30$ kV, $I = 4$ nA) equipped with an aluminum paraboloid mirror to collect CL. We use two measurement geometries: (1) angle-resolved, or Fourier, CL (ARCL) in which a wide zenithal and azimuthal angular emission pattern is collected over a wavelength range determined by a band-pass filter ($\lambda = 600 \pm 20$ nm);²⁶ and (2) hyperspectral angle-resolved cathodoluminescence (HSARCL) in which the angular distribution of CL intensity is collected in the vertical plane along the parabola's center and analyzed with a spectrometer at 0.9 nm spectral resolution.^{27,28} Details of the CL geometry and spectroscopy are described in the Methods section.

Figure 2a shows the ARCL intensity at $\lambda = 600$ nm for the electron beam placed $L_e = 2.29$ μm away from the center of the nanohole. The electron beam is positioned on the right side of the nanohole, along the horizontal x axis crossing the center of the nanohole (see Figure 1a). A clear interference pattern is observed with fringes along the vertical k_y direction.²⁴ Figure 2b shows the ARCL intensity at $\lambda = 600$ nm for the unstructured planar stack. A cylindrically symmetric transition radiation pattern is observed, with the highest intensity observed at larger zenithal angles as expected for a z-polarized dipole slightly above the multilayer stack that represents transition radiation. Subtracting the transition radiation reference from the data of Figure 2a results in a pronounced interference pattern, as shown in Figure 2c. The modulation depth of the fringes is 45% in the forward scattering direction and lower for backward scattering (see section 2 of Supporting Information on how we derived the visibility of the interference fringes). The lower visibility for backward scattering can partially be explained by the partial temporal coherence of light after passing through the bandpass filter. A bandpass filter filters out most frequency components of light, thereby effectively stretching the temporal signal. In the backward scattering direction the time delay between TR and

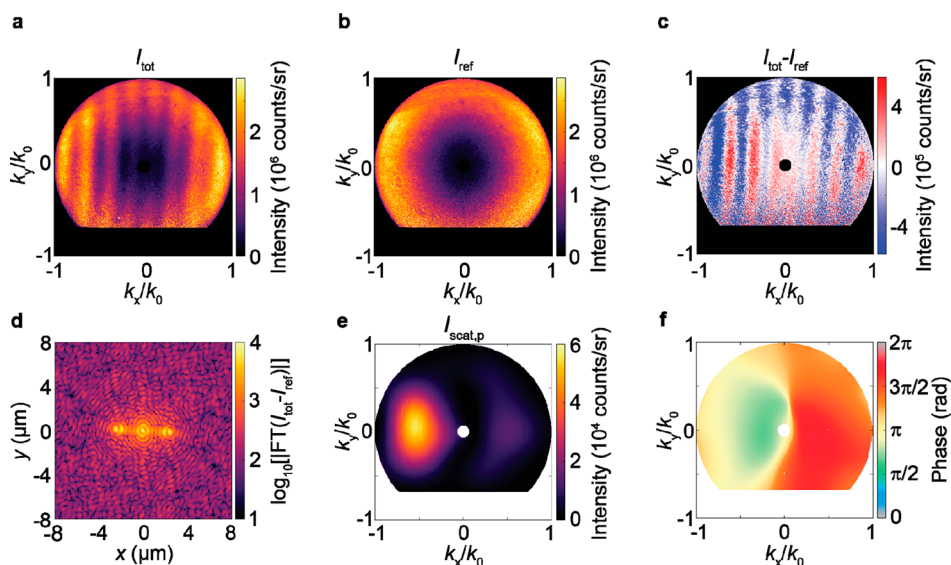


Figure 2. Phase profiles for SPPs scattered from a nanohole in Ag. (a) Angle-resolved cathodoluminescence radiation pattern ($\lambda = 600 \pm 20$ nm) obtained for a 30 keV electron beam placed $2.29 \mu\text{m}$ to the right of a 300 nm diameter nanohole. (b) Transition radiation from the same layer stack in the absence of nanoscatteer. (c) The difference in data presented in (a) and (b). (d) 2D fast Fourier transform of data presented in (c). (e) Numerically derived p-polarized amplitude pattern for the nanohole. (f) Numerically derived phase profile of p-polarized scattered field by the nanohole.

the scattered SPPs is much larger than in the forward scattering direction, which leads to partially washing out interference fringes. The visibility can be enhanced by using a narrower bandpass filter, at the expense of signal intensity. Taking the 2D fast Fourier transform of the data presented in Figure 2c using $k_0 = 2\pi/\lambda$ results in Figure 2d (see section 3 of the Supporting Information for the convention used for the Fourier transform). Aside from a central spot two distinct spots are observed that are displaced $2.29 \mu\text{m}$ from the origin, in agreement with the distance between the electron beam and the center of the hole in the experiment. As shown in section 4 of the Supporting Information, these spots contain the interference terms, while the central spot represents the scattered intensity coming from individual scattering centers. Note that the electron beam can neither be placed too close, nor too far from the scattering object. When the electron beam is placed too close to the nanohole ($<\lambda$), no interference can be seen. When the electron beam is placed too far from the nanohole, the driving field from the SPPs has decreased too much which leads to a reduction of the interference visibility.

After isolating the interference term on the left in Figure 2d (see section 4 of Supporting Information for a detailed explanation and discussion of this numerical technique) and performing a 2D inverse fast Fourier transform, we retrieve the angular amplitude and phase patterns of the p-polarized scattered electric field $E_{\text{scat},p}$. The amplitude profile shown in Figure 2e shows a bright leftward-oriented lobe and a weak rightward lobe along the horizontal k_x axis. Figure 2f shows the phase pattern which shows a π phase flip between left and right propagating fields, all relative to the phase of the spherical transition radiation wavefront which varies only very weakly (see section 5 of Supporting Information). This shows that the induced polarization density in the nanohole breaks cylindrical symmetry and has a strong in-plane component. This analysis now provides the full (p-polarized) electric field amplitude and phase of the field radiated by the SPP-driven nanohole.

As we have shown previously, nanoholes in metal films possess both electric and magnetic dipoles that interfere in the far field resulting in strong angular beaming from the hole.^{29,30} Using the amplitude and phase information from the analysis above, we can directly perform a multipolar decomposition of the scattered fields (for details on this calculation, see section 6 of Supporting Information). Given the small size of the hole we limit the multipolar decomposition to electric and magnetic dipoles and find that SPP excitation of the Ag nanohole induces mainly x - and z -polarized electric (p_x, p_z) and y -polarized magnetic (m_y) dipoles.²⁹ This is in full agreement with the fact that transverse-magnetic (TM)-polarized SPPs propagating along the x axis contain x and z electric field and y magnetic field components that directly couple to these three dipole moments. Figure 3a graphically presents the retrieved complex-valued dipole moments. We find that the phase difference ϕ between m_y and p_x is 0.5π , in full agreement with the Maxwell–Faraday relation that states that the current loop formed by the p_x dipole and its image dipole induces a $\pi/2$ -phase-shifted magnetic field [$\nabla \times \mathbf{E}(\mathbf{r}, \omega) = i\omega\mu_0\mathbf{H}(\mathbf{r}, \omega)$]. The fact that small p_y and m_x contributions are also found, despite the symmetry of the scattering problem, is ascribed to the fact that the parabolic mirror causes the far fields created by p_z, p_y , and m_x to be nonorthogonal (see Table S3). The excitation of p_z then leads to small apparent p_y and m_x components in the measurement. The asymmetric beaming of the scattered radiation (Figure 2e) is a direct consequence of the interference between the induced z -polarized electric dipole and the induced in-plane dipoles.³⁰

Next, we performed HSARCL in which we measure the spectrally resolved angular radiation pattern in the plane defined by the surface normal and the k_y axis in Figure 2a. We rotated the excitation scheme presented in Figure 1a by 90° clockwise, including the Cartesian coordinate system, so that the interference fringes can be measured. This measurement scheme allows probing fine details in the interference phenomena over a wide wavelength range, enabling derivation

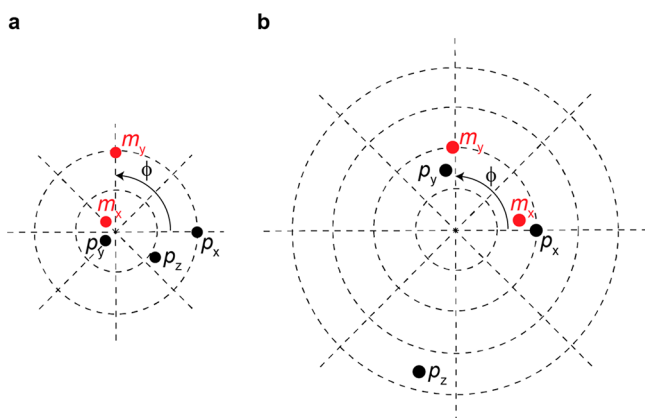


Figure 3. Multipole decomposition of the scattered field from CL holography data. Visualization of numerically retrieved values of electric (black) and magnetic (red) dipole moments. The amplitude of the dipoles is encoded in the radial distance to the center of the circle; the phase in the polar angle ϕ . (a) Electron beam is placed $L_e = 2.29 \mu\text{m}$ to the right of a nanohole. (b) Electron beam is placed $L_e = 2.29 \mu\text{m}$ to the right of the Ag nanocube.

of the SPP dispersion as well as the phase distribution of the scatterer's emission profile, as we will show. Figure 4a shows the CL dispersion diagram in the $\lambda = 375\text{--}820 \text{ nm}$ spectral band for the electron beam placed $L_e = 2.40 \mu\text{m}$ away from the center of the nanohole along the positive x axis. Subtracting

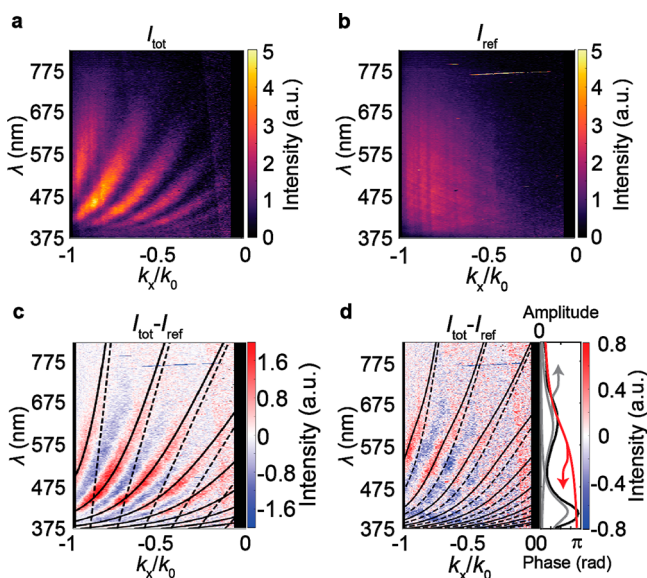


Figure 4. Plasmon dispersion and resonant scattering revealed with hyperspectral angle-resolved cathodoluminescence. (a) CL radiation pattern for electron beam placed $L_e = 2.40 \mu\text{m}$ to the right of the center of a nanohole (I_{tot}). (b) Transition radiation pattern for the stack (I_{ref}). The vertical black sections in (a) and (b) reflect the hole in the parabolic mirror through which the electron beam enters. (c) Difference of data presented in (a) and (b). Solid curve is fit to constructive interference wavelength λ_m given in eq 1. Dashed curve assumes a dispersionless surface wave. (d) Left: $I_{\text{tot}} - I_{\text{ref}}$ for an electron beam placed $L_e = 2.37 \mu\text{m}$ to the right of an Ag nanocube. Solid curve is fit to a constructive interference condition, taking into account a Lorentzian scattering resonance. Dashed curve includes a dispersive surface wave and does not include the resonance. Right: Lorentzian resonance considered for fit (black curve, measured CL spectrum; red curve, fitted phase; gray curve, fitted amplitude).

the transition radiation reference data (Figure 4b), we find clear interference fringes over a broad wavelength range (Figure 4c). We model the dispersion relation of the maxima of the interference fringes by considering the constructive interference conditions in the far field taking into account the optical path lengths ($k_0 n_{\text{SPP}} L_e$, $k_x L_e$), with k_x the in-plane wave vector of scattered light, and a phase term ϕ_{scat} related to scattering:

$$\lambda_m = \frac{L_e}{N - \frac{\phi_{\text{scat}}}{2\pi}} \left(\frac{k_x}{k_0} + n_{\text{SPP}} \right) \quad (1)$$

The solid curves in Figure 4c are fits of this model to the data for different orders N ; they fit the data very well over a broad spectral range, with N ranging from $N = 1\text{--}5$, all for the same scattering phase ($\phi_{\text{scat}} = 0.7\pi$). The curvature of the solid curves clearly reflects the SPP dispersion; the dashed lines show the dispersionless case ($n_{\text{spp}} = 1$) for reference. The largest deviation between the solid and the dashed curves occurs for shorter wavelengths, in agreement with the SPP dispersion shown in Figure 1c. The data in Figure 4a–c show that the scattering of SPPs by the nanohole is a nondispersive process in this wavelength range described by a fixed overall scattering phase of 0.7π .

Next, we investigate the scattering of SPPs by single-crystalline Ag NCs.³¹ It is known that NCs on a metal substrate with a thin dielectric spacer possess gap plasmon resonances in the visible spectral range.³² We collect ARCL data at $\lambda = 600 \text{ nm}$ using the same distance between electron impact position and the center of the NC of $L_e = 2.29 \mu\text{m}$. Subtracting the transition radiation, we find the angular profile in Figure 5a. Clear interference fringes are observed, with a notable left/right asymmetry. To study this in more detail, we plot in Figure 5b the angular data averaged along the vertical angular axis for scattering from the hole and the NC. In both

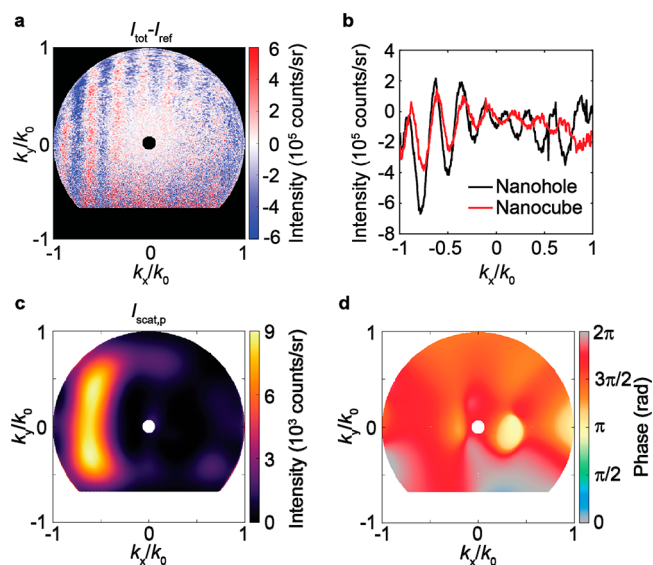


Figure 5. Angular intensity and phase profiles for SPPs scattered from a Ag nanocube. (a) Angle-resolved cathodoluminescence radiation pattern ($\lambda = 600 \pm 20 \text{ nm}$) corrected for transition radiation. (b) Interference fringes obtained by averaging data of Figures 2c and 5c along the k_y/k_0 axis. (c) Numerically derived p-polarized amplitude pattern for the nanocube. (d) Numerically derived phase profile of the p-polarized scattered field by the nanocube.

cases, the fringe amplitude is higher for negative than for positive k_x values, which we relate to the left/right symmetry breaking by the off-center excitation in combination with the use of a bandpass filter (see section S2 of Supporting Information). Moreover, for the Ag NC, the maxima for positive k_x values are phase-shifted compared to values for negative k_x , while this phase shift is not observed for the hole. This reflects a fundamental difference in the SPPs scattering mechanism for NCs and nanoholes, as we will further illustrate below.

Using Fourier analysis, we retrieved both the amplitude (Figure 5c) and phase (Figure 5d) patterns of the p-polarized scattered electric field radiated by the Ag NC. As for the nanohole, we observe beaming of light to the left, which we partially attribute to the asymmetry in the excitation process and the resulting modal excitation. In contrast to the case of the hole, the phase profile is found to be quite homogeneous in angle, that is, the π -phase flip between left and right propagating fields, as was observed for scattering off the hole, is not observed here. Using the intensity and phase patterns, we perform a multipolar decomposition of the scattered fields (see section 6 of Supporting Information) and find that the main scattering contributions come from $p_x, p_y, p_z, m_x,$ and m_y (see Figure 3b for the graphical representation of the retrieved complex-valued dipole moments). We find similar amplitudes for p_x and m_y , and for p_y and m_x , with a phase difference between electric and magnetic dipoles of 0.5π and -0.5π , respectively, again explained by the electric–magnetic dipole coupling argument described above for the nanohole. The nanoparticle shows a dominant z-polarized electric dipole mode, as expected for a plasmonic nanocube above a mirror with a dielectric spacer in between.³³ By symmetry, the angular profile of the phase is expected to be symmetric, as is observed. The contrasting phase symmetries observed for hole and nanocube are clearly reflected in the shifted phase profiles for positive angles in Figure 5b.

Next, we present the HSARCL data for the Ag NC obtained by placing the electron beam at $L_e = 2.37 \mu\text{m}$ in Figure 4d. As for the nanoholes, we observe a clear interference pattern over a broad spectral range, with mode numbers $N = 1$ –5. However, for the case of the NCs, the fringes do not match the dispersive SPP model indicated by the dashed curves. The discrepancy is a direct manifestation of the increasing phase shift between the induced polarization density and the plasmonic driving field as the wavelength is decreased across the scattering resonance. Figure 4d shows the CL spectrum of the Ag NC taken by directly placing the electron beam at a corner of the NC. As can be seen, the plasmon spectrum peaks at 620 nm with a full-width-at-half-maximum line width of 152 nm. Indeed, the largest discrepancy between the data in Figure 4d and the dispersive SPP model occurs for wavelengths below the resonance peak. To quantitatively analyze this trend, we fit the plasmon contribution to the CL spectrum with a single Lorentzian line shape and introduce the corresponding phase shift to the dispersion model (solid curve). Clearly, this resonant scattering model fits the trends in the CL data well for different values of N . This analysis clearly shows the power and sensitivity of CL holography to detect characteristic phase shifts in scattering.

As a final demonstration of the power of CL holography we study SPP scattering from a helical nanoaperture in single-crystalline Au (Figure 6a). Figure 6b shows the ARCL intensity at $\lambda = 600 \text{ nm}$ for the electron beam placed $L_e = 2.29 \mu\text{m}$ away

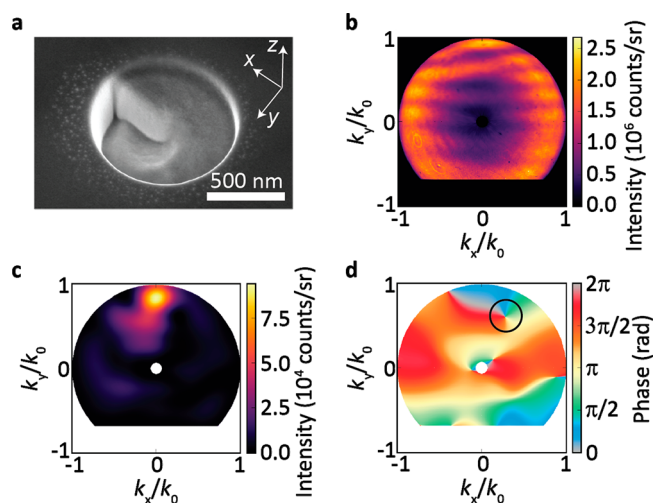


Figure 6. Phase singularity for SPPs scattered from a helical nanoaperture in Au. (a) SEM image of a helical nanoaperture milled in single-crystalline Au. (b) Angle-resolved cathodoluminescence radiation pattern ($\lambda = 600 \pm 20 \text{ nm}$) obtained for a 30 keV electron beam placed $2.29 \mu\text{m}$ from the helical nanoaperture along the negative y -axis. (c) Numerically derived p-polarized intensity pattern for the helical nanoaperture. (d) Numerically derived phase profile of p-polarized scattered field by the helical nanoaperture (indicated by circle) showing phase singularity with topological charge -1 .

from the center of the nanohelix along the negative y -axis. A clear interference pattern is observed with fringes along the k_y direction. Remarkably, we observe a clear fork-like structure around $(k_x/k_0, k_y/k_0) = (0.25; 0.60)$ pointing at the existence of a phase singularity in the far-field phase profile. The retrieved angle-dependent intensity and phase patterns of the scattered field are shown in Figure 6c and d, respectively. Figure 6c shows the radiation profile is strongly beamed in the forward direction. Figure 6d shows for $(k_x/k_0, k_y/k_0) = (0.28; 0.60)$ a phase singularity with topological charge -1 , as the phase evolves once from 0 to 2π when turning clockwise around the phase singularity.

We have used Fourier-transform cathodoluminescence holography to directly retrieve the phase of surface plasmon polaritons scattered from nanoscale holes, nanocubes, and nanohelices. From the data, we retrieve the phase and amplitude of the 3D vectorial electric and magnetic dipole moments that interfere to create the measured scattering pattern. The spectral phase jump across a plasmonic scattering resonance is directly revealed from the data and we directly observe phase singularities in the scattering of plasmonic nanohelices. Fourier-transform cathodoluminescence holography can find many further applications to probe scattering of surface waves and other guided waves from nanoscale objects at high precision.

METHODS

Fabrication of Multilayer Stack. A layer stack of 200 nm Ag and 15 nm SiO_x was made by thermal evaporation. Ag was deposited at a base pressure of 1.6×10^{-6} mbar and a deposition rate of 2 \AA/s . For the SiO_x layer, we used SiO_x as the target, a deposition rate of 0.6 \AA/s , and a base pressure of 9.3×10^{-7} mbar.

Synthesis of Ag Nanocubes. The Ag nanocubes were synthesized by adopting a chemical synthesis procedure reported earlier.³⁴ Well-defined (100)-faceted Ag cubes of

~75 nm were made in solution, filtrated, and dispersed in ethanol, and then dropcast onto the multilayer stack.

Fabrication of Nanohelices. A total of 30 keV Ga focused ion beam milling of nanohelices was performed using serpentine scans at a current of 1.5 pA and a pixel dwell time of 1.5 μ s. The structure was made in 60 passes, each pass taking 667 ms.

CL Measurement Geometries. CL experiments were performed using a Thermo Fisher 650 Quanta SEM equipped with a thermionic Schottky field emission electron source, operated at 30 kV, and a typical beam current on the sample of 4 nA. The CL is collected with an aluminum paraboloid mirror (1.47π sr acceptance angle), of which the focus is aligned with respect to the electron beam and the sample using a motorized micropositioning stage inside the vacuum chamber. The CL signal is analyzed using a Delmic SPARC system equipped with a 2048×512 pixel back-illuminated CCD array mounted on a Czerny-Turner spectrograph. We perform two different types of CL experiments:

1. **Angle-Resolved CL (ARCL).** In this geometry, the spectrometer slit is fully opened (15 mm) and a planar aluminum mirror is selected on the turret in the spectrograph. The reflected light is projected onto the CCD camera. In this way, we acquire a full angular pattern/momentum distribution within the NA of the paraboloid collection optics. Wavelength specificity is attained with a band-pass filter ($\lambda = 600 \pm 20$ nm).

2. **Hyperspectral Angle-Resolved Cathodoluminescence (HSARCL).** The entrance slit is closed to 150 μ m and acts as a filter in angular/momentum space, selecting the radiation in the vertical plane along the paraboloid optical axis. This angular emission pattern is dispersed by the diffraction grating in the spectrometer, leading to a hybrid 2D CCD image with a wavelength on the horizontal axis and an angle on the vertical axis. This map is converted into a wavelength (λ) and momentum (k) map by applying the appropriate coordinate transform.

■ ASSOCIATED CONTENT

SI Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acsp Photonics.0c00209>.

Optical constants of the stack, angle-dependent visibility of interference fringes, definition of Fourier transform, numerical algorithm to retrieve amplitude and phase information on the scattered field, far-field phase profile of transition radiation, multipole expansion, and an additional example of surface plasmon scattering by a hole (PDF)

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Notes

The authors declare the following competing financial interest(s): A.P. is co-founder and co-owner of Delmic BV, a company that produces the cathodoluminescence system that was used in this work.

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