

1 **Can Hyperperfusion of Non-aerated Lung Explain COVID-19 Hypoxia?**

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13 **Abstract**

14 Early stages of the novel coronavirus disease (COVID-19) have been associated with ‘silent
15 hypoxia’ and poor oxygenation despite relatively small fractions of afflicted lung. Although it
16 has been speculated that such paradoxical findings may be explained by impairment of hypoxic
17 pulmonary vasoconstriction in infected lungs regions, no studies have confirmed this hypothesis
18 nor determined whether such extreme degrees of perfusion redistribution are physiologically
19 plausible. Here, we present a mathematical model which provides evidence that the extreme
20 amount of pulmonary shunt observed in patients with early COVID-19 is not plausible without
21 hyperperfusion of the relatively small fraction of injured lung, with three-fold increases in
22 regional perfusion to afflicted regions. Although underlying perfusion heterogeneity (e.g., due to
23 gravity or pulmonary emboli) exacerbated existing shunt in the model, the reported severity of
24 hypoxia in early COVID-19 patients could not be replicated without considerable reduction of
25 vascular resistance in nonoxygenated regions.

26 **Introduction**

27 Gattinoni et al. described disease due to the novel coronavirus (COVID-19) as following
28 two stages, or phenotypes ¹. Patients initially present with a “Type L” phenotype characterized
29 by “Low” lung stiffness (normal compliance averaging 50 mL cmH₂O⁻¹) despite poor
30 oxygenation. Type L may transition into a frequently fatal “Type H” phenotype characterized by
31 “High” lung stiffness (reduced compliance) accompanied by features reminiscent of
32 conventional acute respiratory distress syndrome (ARDS) ¹. Although a strict dichotomy of
33 phenotypes based on respiratory compliance is controversial ², there are nonetheless frequent
34 reports of severe hypoxia in patients with only a small fraction of nonaerated lung ³⁻⁵, including
35 so-called ‘silent hypoxia’. Thus the early stages of COVID-19 appear to be unique and poorly
36 understood, manifesting in the lung as peripheral lesions characterized by ground-glass
37 opacification on computed tomography (CT) ^{6,7}. Curiously, the fraction of lung affected in this
38 way is often surprisingly low given the severity of the associated hypoxia and estimated shunt
39 fractions (average 50%) ⁸. If one assumes that ground-glass opacification represents lung that is
40 nonventilated, these CT studies imply abnormally high ratios of shunt fraction to nonaerated lung
41 fraction of 3.0 for COVID-19 compared to 1.3 for ARDS ⁸.

42 A possible interpretation of the Type L phenotype is that a disproportionately large
43 fraction of the pulmonary circulation is being directed through nonaerated lung ^{1,5,8}. Accordingly,
44 Gattinoni et al. hypothesized that their seemingly paradoxical observations of hypoxia and high
45 compliance were related to an underlying impairment of hypoxic pulmonary vasoconstriction
46 (HPV) ⁸. Normally, HPV is a feedback mechanism whereby pulmonary arterioles constrict in
47 lung regions with poor oxygenation ⁹. This response results in increased regional vascular
48 resistance, reduced regional perfusion, and thereby reduced overall shunt fraction. It seems

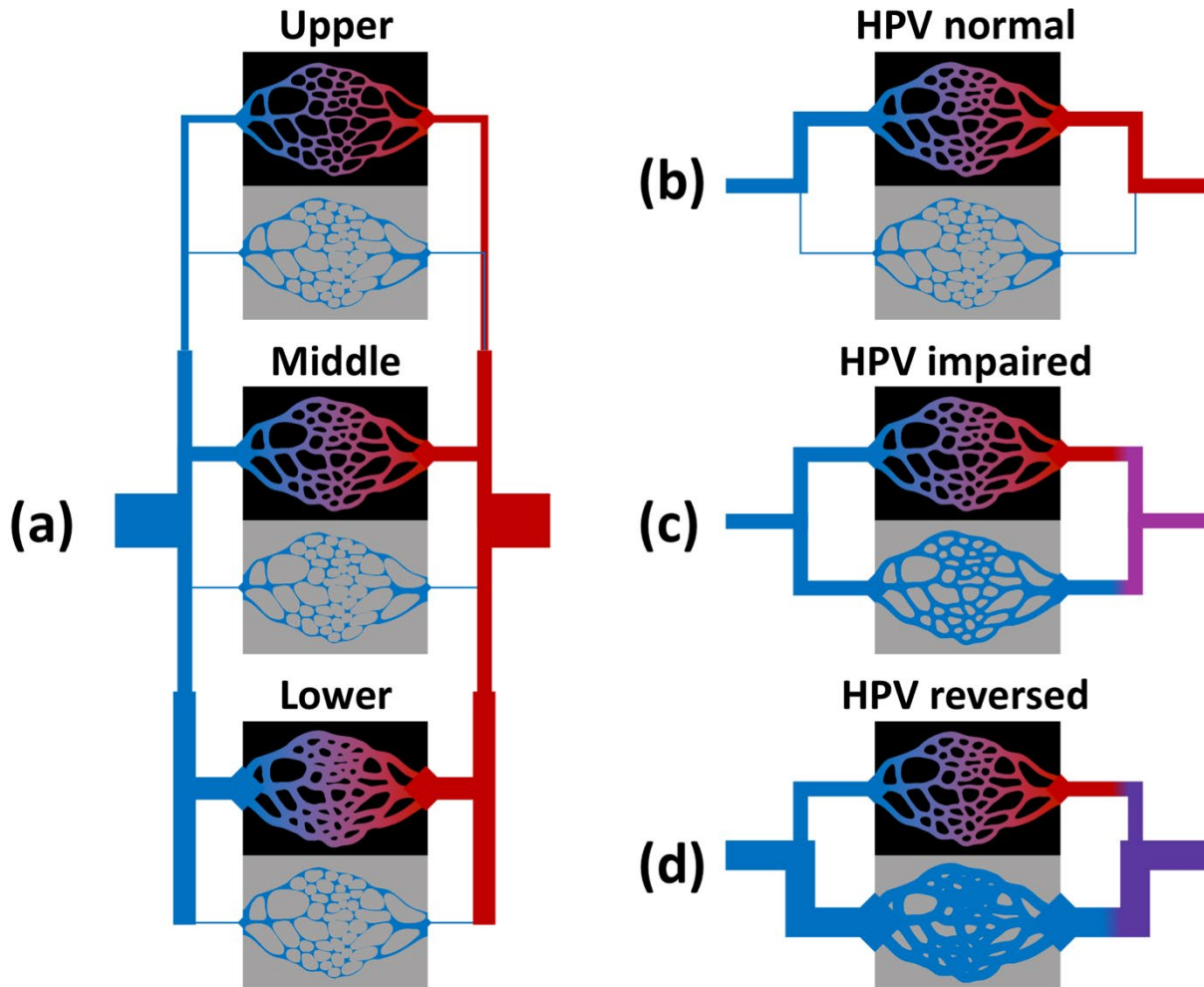
49 reasonable, therefore, that an impairment in HPV might upset the balance between ventilation
50 and perfusion enough to explain the intriguing clinical findings that have been reported in
51 COVID-19 patients.

52 Whether the above explanation is actually plausible, however, requires a quantitative
53 analysis of the factors responsible for determining shunt fraction, ventilation maldistribution, and
54 their relationship to each other. For example, given a certain fraction of injured lung (F_{inj}) with
55 impaired oxygen transport, what increase in regional blood flow and hence vasodilation would
56 be necessary to manifest a ratio of shunt fraction (F_{shu}) to F_{inj} above 3? What are the limitations
57 on oxygen diffusion in injured lung that would be compatible with clinical findings? What role
58 might gravitational gradients play? In the present study we used a mathematical model of
59 perfusion and oxygen transport to address these questions with the goal of determining if the
60 altered HPV hypothesis can potentially explain the Type L phenotype of COVID-19, or whether
61 we need to look for an alternative explanation.

62 **Results**

63 The lung model was partitioned into 6 compartments (Figure 1), representing 1 injured
64 and 1 normal compartment at each of 3 height levels. Each compartment was perfused, receiving
65 deoxygenated mixed venous blood and returning end-capillary blood with oxygen content
66 determined by injury severity. Perfusion distribution in the model reflected the relative vascular
67 resistance in each compartment. Baseline resistances were determined by a specified baseline
68 perfusion gradient, defined as half the range of perfusion across all height levels divided by the
69 average. Vascular resistance was then adjusted in injured regions to reflect possible
70 abnormalities arising in COVID-19. Three types of modification were examined: 1) normal HPV
71 function increased resistance exponentially in regions with low P_cO_2 ; 2) impaired HPV function

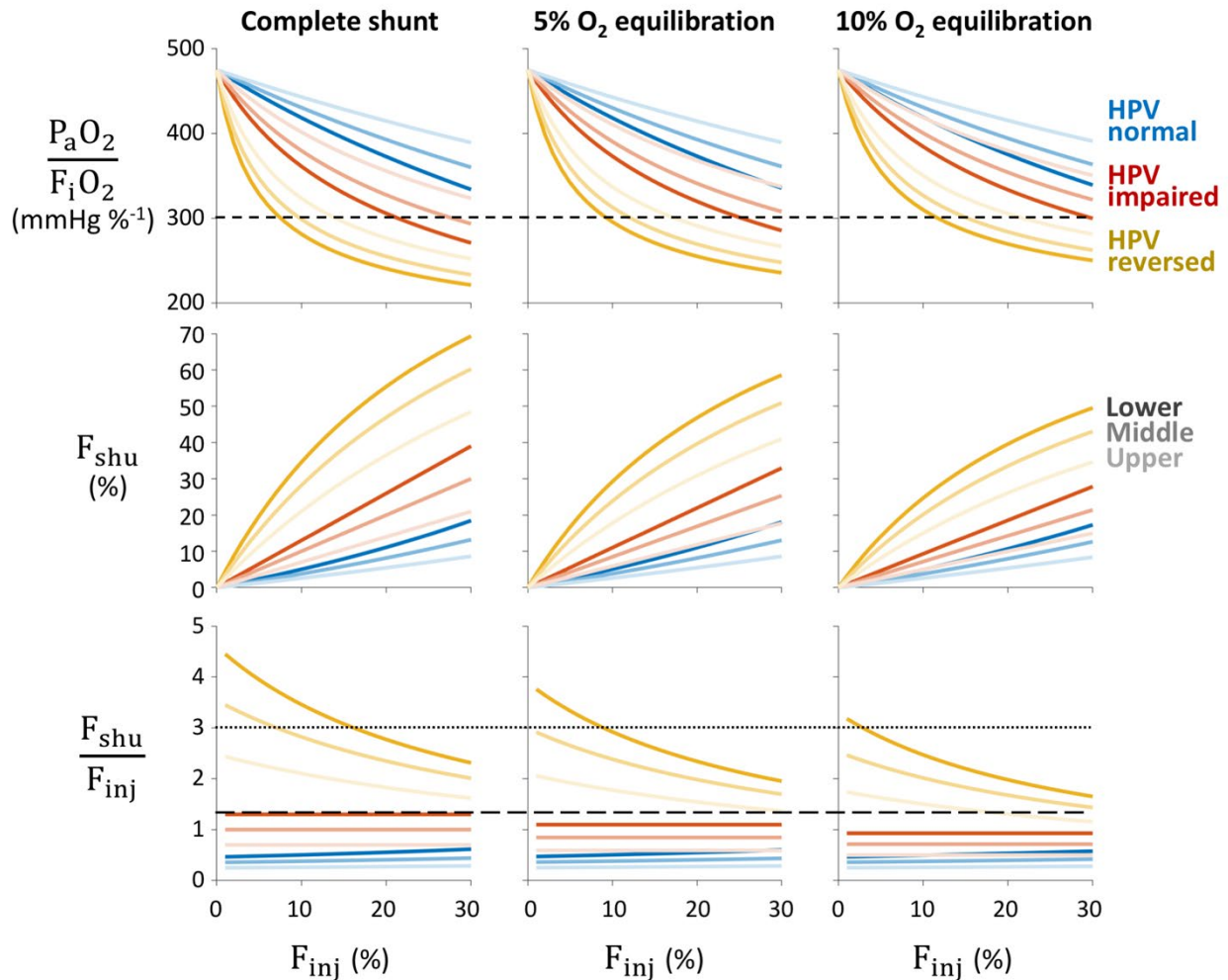
72 produced no change in resistance; and 3) “reversed” HPV reduced resistance regardless of
73 oxygenation. Measured outcomes included F_{shu} , ratio $F_{shu}:F_{inj}$, and ratio $P_aO_2:F_iO_2$.



74
75 **Figure 1.** Model overview. (a) Schematic of the 6-compartment model used to simulate
76 distributed perfusion in aerated and injured compartments at different height levels.
77 Deoxygenated mixed venous blood (blue) passes through aerated (black) or injured (grey)
78 compartments, and returns to the oxygenated mixed arterial blood (red). Vascular resistance in
79 each compartment was determined by height level as well as the degree of oxygenation or injury.
80 Hypoxic pulmonary vasoconstriction (HPV) could be either (b) “normal” with reduced perfusion
81 to regions of low end-capillary oxygen content, (c) “impaired” with no response, or (d)
82 “reversed” with increased perfusion to injured regions.
83

84 The variability in $F_{shu}:F_{inj}$ with respect to injury location and HPV alterations is shown in
85 Figure 2. For simplicity, the extent of injury in each simulation was restricted to only 1 height
86 zone: lower, middle, or upper. Normal HPV function results in the lowest pulmonary shunt

87 fractions and lowest degree of hypoxia, preventing $P_aO_2:F_iO_2 < 300 \text{ mmHg } \%^{-1}$ until $F_{inj} > 30\%$.
 88 Given a relatively small fraction of injured lung, with F_{inj} ranging from 0 to 30%, both a
 89 complete shunt (i.e., zero oxygen uptake) and “reversal” of HPV (i.e., vasodilation in injured

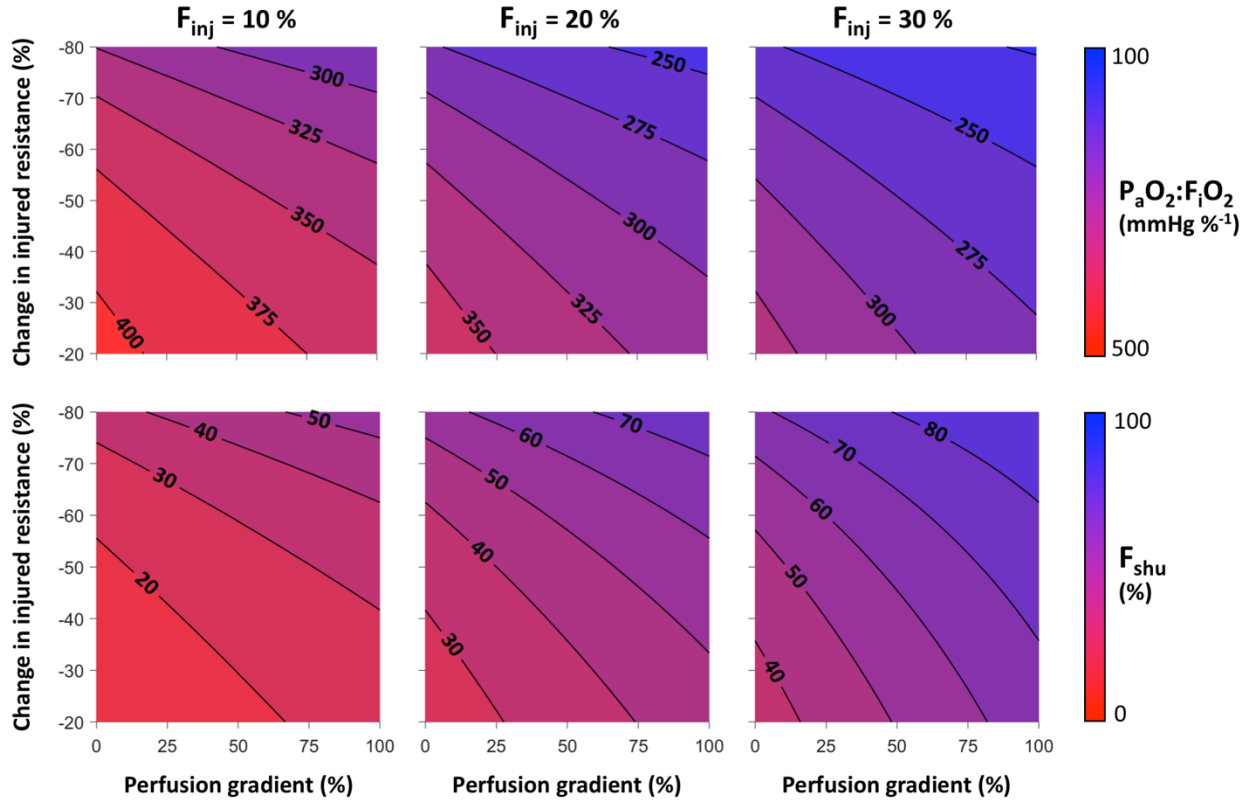


90
 91 **Figure 2.** Effects of alterations to hypoxic pulmonary vasoconstriction (HPV). Severity of
 92 pulmonary shunt with respect to fractional injury extent (F_{inj}), type of HPV modification (color),
 93 injury location within one height level (light to dark). Rows correspond to the ratio of arterial
 94 oxygen tension to inspired oxygen fraction ($P_aO_2:F_iO_2$), shunt fraction (F_{shu}), and ratio of shunt
 95 fraction to injured fraction ($F_{shu}:F_{inj}$). Columns correspond to varying degrees of impaired
 96 oxygen equilibration between capillary blood and alveolar gas in the injured region. Baseline
 97 perfusion gradient was 30%, and reversed HPV was modeled with 72% reduction of vascular
 98 resistance in injured regions. Short-dashed line in the top row indicates $P_aO_2:F_iO_2 = 300 \text{ mmHg } \%^{-1}$, a threshold for ARDS. Dotted and long-dashed lines in the bottom row indicate $F_{shu}:F_{inj}$
 99 ratios of 3.0 and 1.3, respectively, the values reported by Gattinoni et al. for COVID-19 and
 100 ARDS patients, respectively ⁸.
 101

102 regions) are necessary conditions for $F_{shu}:F_{inj} > 2$ and $P_{aO_2}:F_{iO_2} < 300 \text{ mmHg } \%^{-1}$. By contrast,
103 impairment of HPV alone is not sufficient to produce the same level of severe hypoxia at low
104 values of F_{inj} as found by Gattinoni et al. ⁸. With HPV impairment, F_{shu} more closely follows F_{inj}
105 such that the ratio of F_{shu} to F_{inj} lies between 0.7 and 1.3. For all considered alterations to HPV,
106 focusing the injury in the lower zone (i.e., those with higher baseline perfusion) results in higher
107 F_{shu} and worse hypoxia. Interestingly, as F_{inj} decreases in the reversed HPV model, the $F_{shu}:F_{inj}$
108 ratio increases, indicating that F_{shu} decreases more slowly than F_{inj} . Note that the impaired HPV
109 model represents unaltered vascular resistances from baseline values, and therefore corresponds
110 to a model with relatively uniform perfusion distribution.

111 The interplay between baseline perfusion gradients and vasodilation in the HPV reversal
112 model is shown in Figure 3. Baseline perfusion gradient varied between 0 and 100% representing
113 a range of perfusion heterogeneity from uniform with $\frac{1}{3}-\frac{1}{3}-\frac{1}{3}$ distribution at 0% gradient to $0-\frac{1}{3}-$
114 $\frac{2}{3}$ distribution at 100% gradient. Pulmonary shunt and hypoxia both become more severe with
115 increases in either the vasodilation of injured regions or the baseline perfusion gradient. Both of
116 these factors determine the overall degree of perfusion heterogeneity in the injured lung, and in
117 the specific case of injury focused in the lower lung, both contribute to enhanced perfusion to the
118 injured region. Hypoxia and shunt are more sensitive to the degree of vasodilation compared to
119 the baseline gradient. The ratio of $F_{shu}:F_{inj} = 3$ is represented in each panel by contours of F_{shu} at
120 30, 60, and 90% for F_{inj} at 10, 20, and 30%, respectively. Note that baseline perfusion gradient
121 does not explicitly require the definition of upright vs. supine vs. prone positioning, but instead
122 simply reflects discrepant perfusion in 3 arbitrary lung compartments.

123



124
 125 **Figure 3.** Hypoxia severity maps with respect to perfusion gradient and percent change in
 126 vascular resistance within the injured compartment of the lower lung zone. Top row shows
 127 contours of the ratio of arterial oxygen tension to inspired oxygen fraction ($P_aO_2:F_iO_2$). Bottom
 128 row shows contours of the shunt fraction (F_{shu}). Columns represent different levels of the fraction
 129 of lung injured (F_{inj}).

130 Discussion

131 Our analysis based on a simple mathematical model of perfusion in normal and shunted
 132 compartments suggests that the extreme amount of pulmonary shunt observed in patients with
 133 early stage severe COVID-19 is not plausible without hyperperfusion of the relatively small
 134 fraction of injured lung, with up to 3-fold increases in regional perfusion to the afflicted regions.
 135 Furthermore, the obstruction to oxygen diffusion in the injured regions must be nearly complete
 136 such that there is less than 5% equilibration between alveolar gas and end-capillary blood.

137 The Type L early stage of COVID-19 described by Gattinoni et al. ^{1,8}, characterized by
 138 severe hypoxia but relatively normal lung compliance, cannot be recapitulated in this model

139 without dramatic reductions to vascular resistance in the injured regions. To replicate the
140 reported values for F_{shu} of 50% and $F_{shu}:F_{inj}$ of 3 (implying F_{inj} of 17%), the model requires
141 reductions in injured resistance of 60 to 70%, depending on the baseline perfusion gradient
142 (Figure 3). Approximating vascular resistance using the Hagen-Poiseuille equation, this change
143 in resistance corresponds to an increase in vascular diameter of 26 to 35%. Whether this degree
144 of vasodilation is physiologically plausible is uncertain. Vasodilation using inhaled nitric oxide
145 has been reported to decrease total pulmonary vascular resistance by up to 50%^{10,11}. If the
146 model-predicted 60 to 70% reduction of resistance is possible, it likely represents maximal
147 vasodilation and recruitment of pulmonary capillaries. Although speculative, it may be possible
148 that COVID-19 interferes with the HPV feedback mechanism in such a way that pulmonary
149 arterioles do not constrict, and potentially dilate, in injured lung regions in which there is little or
150 no oxygen transport into the blood. The virus is known to enter cells via the ACE2 receptor, and
151 may potentially interfere with the renin-angiotensin system in ways that alter pulmonary vascular
152 tone¹². Although it is reported that later stages of the disease are characterized by
153 downregulation of ACE2 and vasoconstriction (promoting ARDS)¹²⁻¹⁴, it is possible that earlier
154 stages instead promote local vasodilation or impairment of HPV^{5,15}. Other evidence of
155 vasodilation due to COVID-19 includes recent discovery of cardiovascular complications
156 reminiscent of vasodilatory shock and Kawasaki disease¹⁶, which is associated with weakened
157 walls of the coronary artery.

158 Impairment of HPV alone cannot reproduce the same extreme values of $F_{shu}:F_{inj} > 2$ in
159 our model. Instead, the $F_{shu}:F_{inj}$ ratio in the impaired HPV model is limited by the magnitude of
160 the baseline perfusion gradient. With zero baseline perfusion gradient and impaired HPV,
161 vascular resistance is uniform across all compartments, and thus the fraction of shunted blood

162 flow is equal to the fraction of lung with impaired oxygen transport ($F_{shu}:F_{inj} = 1$). Heterogeneous
163 perfusion may increase the risk for larger F_{shu} , especially when the injured region also receives
164 more baseline perfusion (see Figure 2). The value of $F_{shu}:F_{inj} = 1.3$ for typical ARDS reported by
165 Gattinoni et al. ⁸ is well-matched in our model with a moderate baseline perfusion gradient of
166 30%, impairment of HPV, and injury focused in the lower compartment (see Figure 2). This
167 suggests that HPV impairment (e.g., due to sedatives or anesthetic agents with vasodilating
168 effects) and prevalence of derecruitment in the gravitationally dependent lung (typically dorsal
169 regions in a supine patient) are plausible factors contributing to the observed $F_{shu}:F_{inj}$ ratio of 1.3.

170 In COVID-19, the lower left and lower right lobes are most commonly afflicted
171 according to radiographic abnormalities ^{7,17}, and these are typically the gravitationally dependent
172 regions of the lung in either upright or supine positioning. However even with an extreme
173 baseline perfusion gradient of 100% (corresponding to 0- $\frac{1}{3}$ - $\frac{2}{3}$ distribution), $F_{shu}:F_{inj}$ in the model
174 is still limited to 2 at most. For example, in Figure 3, $F_{shu}:F_{inj}$ does not exceed 3 even at 100%
175 baseline perfusion gradient until the resistance reduction is 40% for $F_{inj} = 10\%$, or 55% for $F_{inj} =$
176 20%. Therefore it appears unlikely that the degree of pulmonary shunt reported in COVID-19
177 patients ($F_{shu} = 50\%$ and $F_{shu}:F_{inj} = 3$) could occur without a substantial degree of vasodilation
178 and hyperperfusion in the small fraction of injured lung, even when considering the possibility
179 that one-third of the lung is physiologic dead space.

180 It should be noted that the model assumptions do not require gravity to explain the
181 presence of a baseline perfusion gradient. Given arbitrarily defined compartments, differences in
182 regional perfusion could also represent conditions manifesting abnormal perfusion defects such
183 as pulmonary emboli. Coagulation and thrombosis have been identified as symptoms of COVID-
184 19, and in many cases are associated with mortality due to stroke, myocardial infarction, or

185 pulmonary embolism^{13,18,19}. Pulmonary embolism may reduce or eliminate perfusion to well-
186 aerated or ventilated lung regions, resulting in physiologic dead space and redistribution of
187 perfusion to other lung regions. This alone does not necessarily produce hypoxia, but can
188 exacerbate hypoxia if perfusion is redistributed to regions of pulmonary shunt. In our simple
189 model, a baseline perfusion gradient of 100% corresponds to zero perfusion in one-third of the
190 lung, which may be interpreted similarly to the result of severe thrombotic pulmonary emboli.
191 Even in this case, $F_{shu}:F_{inj}$ is still limited to at most 2 with only impaired HPV, and vasodilation
192 in injured regions remains necessary to explain $F_{shu}:F_{inj} \geq 3$. A case report using dual-energy CT
193 demonstrated no indications of pulmonary emboli in the well-aerated lung, but rather
194 vasodilation of pulmonary arteries and hyperperfusion adjacent to infected regions⁵.

195 Compounding the effects of large perfusion defects with “reversed” HPV, a given ratio of
196 $F_{shu}:F_{inj}$ may be obtained at a lower level of vasodilation in the injured region (see Figure 3). A
197 recent study of COVID-19 patients requiring mechanical ventilation reported physiologic dead
198 space fractions as high as 45% at the time of intubation, as well as moderate reductions in
199 compliance²⁰. Although this cohort may represent a later stage of COVID-19, these findings
200 support the notion that disease progression is accompanied by perfusion redistribution away from
201 aerated regions. If thrombotic pulmonary emboli occur during the early stages of COVID-19 as
202 well, this could amplify the apparent F_{shu} and hypoxia. In cases of increased physiologic dead
203 space, ratios of $F_{shu}:F_{inj} = 3$ may occur with lower, more plausible reductions of resistance in
204 injured regions (30 to 50%), compared to the 60 to 70% reduction required without considering
205 any physiologic dead space. Another factor that may contribute to systemic hypoxia is increased
206 oxygen uptake by lung tissues, which may account for up to 20% of total oxygen metabolism in
207 patients with lung injury compared to only 5% at baseline²¹.

208 Reports of “silent hypoxia” in early stages of COVID-19³ may reflect the Type L
209 phenotype. It is intriguing that hypoxia in these patients is not associated with hypercapnia. One
210 might assume that severe pulmonary shunt would produce deficiencies in both oxygen and
211 carbon dioxide exchange. Hypercapnia is less likely to be “silent”, considering that even small
212 increases in arterial carbon dioxide tension elicit feedback response from pH-sensitive central
213 chemoreceptors to increase respiratory drive. Although our model suggests that oxygen
214 equilibration must be less than 5% to produce high ratios of $F_{shu}:F_{inj}$, it is possible that
215 elimination of carbon dioxide is less impaired given that diffusion of carbon dioxide across the
216 alveolar-capillary membrane is roughly 20-fold faster than that of oxygen³.

217 Pulmonary vasodilators such as inhaled nitric oxide, sildenafil, and angiotensin-(1,7) are
218 currently involved in clinical trials for treatment of COVID-19 (e.g., ClinicalTrials.gov
219 identifiers NCT04290871, NCT04304313, NCT04332666). Notwithstanding other systemic
220 effects of pharmacological interventions, our model suggests that vasodilation throughout the
221 noninjured lung may counterbalance disease-induced vasodilation in the injured regions,
222 restoring a more uniform baseline perfusion distribution similar to the impaired HPV model.
223 Vasodilation may also reduce the severity of thrombotic pulmonary emboli, thereby reducing
224 physiologic dead space and perfusion heterogeneity. Prone positioning is another intervention
225 which may reduce baseline perfusion gradients compared to supine positioning²², and is also
226 reportedly beneficial for COVID-19 patients^{23,24}. Therefore, our model may explain a
227 mechanism by which pulmonary vasodilators and prone positioning may improve ventilation-to-
228 perfusion matching and reduce hypoxia, perhaps providing palliative care for COVID-19
229 patients.

230 It should be noted that no consensus has yet been established for these interventions,
231 current evidence is largely anecdotal, and the theories proposed herein based on our simple
232 model are speculative. The direct implications of this study are furthermore limited to palliative
233 care, and cannot be applied to identify or verify underlying viral mechanisms that initiate or
234 progress the disease, or to explain why asymptomatic patients exhibit radiographic indicators of
235 viral pneumonia ⁷. It should also be noted that our model was designed to represent only early
236 stages of severe COVID-19 (i.e., before it develops into full-blown ARDS) where there is only a
237 small fraction of injured lung and before the initiation of mechanical ventilation or other
238 respiratory support. The purpose of the model was to quantitatively assess the plausibility of the
239 hypothesis that severe hypoxia in early COVID-19 is the result of hyperperfusion within a small
240 amount of injured lung. The model demonstrates that vasodilation of injured, unoxygenated
241 regions appears to be a necessary feature of early COVID-19 to explain the reported severity of
242 hypoxia, with or without shunt amplification by thrombotic pulmonary emboli.

243 **Methods**

244 The lung model was partitioned into 6 compartments (Figure 1), representing 1 injured
245 and 1 normal compartment at each of 3 height levels with different gravitational potentials
246 corresponding to West zones ²⁵. Each compartment was perfused, receiving deoxygenated mixed
247 venous blood and returning end-capillary blood with oxygen content determined by injury
248 severity. The model described time-averaged gas exchange, i.e., neglecting within-breath and
249 within-beat fluctuations. Normal lung compartments had normal oxygen diffusion such that end-
250 capillary oxygen tension (P_{cO_2}) equilibrated with alveolar oxygen tension (P_{AO_2}). Injured lung
251 compartments had limited or zero oxygen diffusion such that P_{cO_2} was either equal to mixed
252 venous oxygen tension (P_{vO_2}) or a weighted average of P_{vO_2} and P_{AO_2} :

253
$$P_cO_2 = P_vO_2 + B \cdot (P_AO_2 - P_vO_2)$$

254 Note that in the normal lung compartments, B was assumed to have a value of 1. A value of 0 for
255 B corresponds to a complete shunt with no oxygen diffusion. Oxygen tensions were assumed to
256 be $P_vO_2 = 40$ mmHg and $P_AO_2 = 100$ mmHg, representing patients upon admission without
257 supplemental oxygen. These values result from the alveolar gas equation, with 21% inspired
258 oxygen, 47 mmHg water vapor pressure at 37 C, 40 mmHg arterial carbon dioxide tension, and
259 0.8 respiratory quotient:

260
$$P_AO_2 = 0.21 \cdot (760 \text{ mmHg} - 47 \text{ mmHg}) - \frac{40 \text{ mmHg}}{0.8}$$

261 Perfusion distribution in the model reflected the relative vascular resistance in each
262 compartment. First, baseline resistances (R_{bas}) were determined to establish a baseline perfusion
263 gradient in 3 equal-sized normal compartments (i.e., in the absence of any injury). Baseline
264 perfusion gradient was defined as half the range of perfusion across all height levels divided by
265 the average. Baseline vascular resistance (R_{bas}) at each height level (h), relative to baseline total
266 pulmonary vascular resistance (PVR_{bas}), was determined as follows:

267
$$R_{bas}(h) = \frac{1}{3} PVR_{bas} \frac{Q_{tot}}{Q_{bas}(h)}$$

268 where Q_{tot} is total pulmonary perfusion (i.e., cardiac output), and Q_{bas} is baseline perfusion at
269 each height level. Vascular resistance was then adjusted in injured regions to reflect possible
270 abnormalities arising in COVID-19. Three types of modification were examined: 1) normal HPV
271 function increased resistance exponentially in regions with low P_cO_2 ; 2) impaired HPV function
272 produced no change in resistance; and 3) “reversed” HPV reduced resistance by a factor $0 < K <$
273 1 regardless of oxygenation. The following equations were used:

$$\frac{R_{inj}(h)}{R_{bas}(h)} = \begin{cases} 1 + 100e^{-P_cO_2/10} & \text{HPV normal} \\ 1 & \text{HPV impaired} \\ K & \text{HPV reversed} \end{cases}$$

where R_{inj} is resistance of the injured compartment. Note that resistances were defined in a volumetric manner, such that the effective compartmental resistance was inversely proportional to the fraction of lung it represented. Following these HPV modifications and now accounting for an injured compartment at each height level with altered vascular resistance, total pulmonary vascular resistance (PVR) was computed by the parallel combination of compartmental resistances.

$$\frac{1}{PVR} = \frac{1}{3} \sum_h \left[\left(\frac{F_{inj}(h)}{R_{inj}(h)} \right) + \left(\frac{1 - F_{inj}(h)}{R_{bas}(h)} \right) \right]$$

Perfusion to each n 'th compartment was then allocated in inverse proportion to compartmental resistance.

$$Q_n = PVR \left(\frac{F_n}{R_n} \right)$$

where R_n is the resistance of the n 'th compartment and F_n is the fraction of the total lung represented by that compartment. End-capillary oxygen content (C_cO_2) was computed based on P_cO_2 for each compartment:

$$C_cO_2 = 1.34 \cdot [Hb] \cdot S_cO_2 + 0.0031 \cdot P_cO_2$$

where S_cO_2 is oxygen saturation of hemoglobin determined by the Severinghaus equation fit to the oxygen-hemoglobin dissociation curve²⁶:

$$S_cO_2 = \left(1 + \frac{23400}{P_cO_2^3 + 150 \cdot P_cO_2} \right)^{-1}$$

292 Mixed venous oxygen content (C_vO_2) was calculated in the same manner. Mixed arterial oxygen
293 content (C_aO_2) was then determined as a perfusion-weighted average of compartmental end-
294 capillary oxygen contents.

$$295 \quad C_aO_2 = \sum_n (C_cO_2)_n \cdot \frac{Q_n}{Q_{tot}}$$

296 Shunt fraction (F_{shu}) was defined as the ratio of unoxygenated to total blood flow:

$$297 \quad F_{shu} = \frac{C_{c*}O_2 - C_aO_2}{C_{c*}O_2 - C_vO_2}$$

298 where $C_{c*}O_2$ represents a normal(noninjured) compartment.

299 Measured outcomes included F_{shu} , ratio $F_{shu}:F_{inj}$, and ratio $P_aO_2:F_iO_2$. Simulations were
300 conducted over a range of F_{inj} from 0 to 30%. For example, 15% of the lower lung zone injured
301 reflects an overall F_{inj} of 5%, because the lower zone represents 1/3 of the total lung. For
302 simplicity, the extent of injury in each simulation was restricted to only 1 height zone: lower,
303 middle, or upper. Baseline perfusion gradient varied between 0 and 100% representing a range of
304 perfusion heterogeneity from uniform with $\frac{1}{3}$ - $\frac{1}{3}$ - $\frac{1}{3}$ distribution at 0% gradient to 0- $\frac{1}{3}$ - $\frac{2}{3}$
305 distribution at 100% gradient. The degree of limited oxygen diffusion in the injured compartment
306 varied between 0 and 20%, where 0% represents complete shunt and 100% represents complete
307 equilibration with alveolar gas.

308 **Code Availability**

309 A Matlab script for evaluating the mathematical model described herein is available as
310 supplementary material.

311

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389 **Competing Interests Statement:**

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