

REVIEW



Single-cell RNA-seq clustering: datasets, models, and algorithms

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ABSTRACT

Single-cell RNA sequencing (scRNA-seq) technologies allow numerous opportunities for revealing novel and potentially unexpected biological discoveries. scRNA-seq clustering helps elucidate cell-to-cell heterogeneity and uncover cell subgroups and cell dynamics at the group level. Two important aspects of scRNA-seq data analysis were introduced and discussed in the present review: relevant datasets and analytical tools. In particular, we reviewed popular scRNA-seq datasets and discussed scRNA-seq clustering models including K-means clustering, hierarchical clustering, consensus clustering, and so on. Seven state-of-the-art scRNA clustering methods were compared on five public available datasets. Two primary evaluation metrics, the Adjusted Rand Index (ARI) and the Normalized Mutual Information (NMI), were used to evaluate these methods. Although unsupervised models can effectively cluster scRNA-seq data, these methods also have challenges. Some suggestions were provided for future research directions.

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1. Introduction

Identifying cell lineages within tissues or organisms is one of the most important goals of modern biological sciences. Evaluating these associations will greatly increase our understanding of tissue development and homoeostasis [1,2]. Moreover, a complete understanding of these relationships will allow the identification of developmental disorders and pathologies, in addition to providing targets to mitigate disease states including cancer [3–5]. Lineage families have traditionally been detected by introducing a heritable label into a cell and following its progeny.

Recently, lineage tracing has been conducted by identifying cell types using single-cell transcriptomics [6,7,]. Different cell types comprising the progeny are developmentally associated because their labelled genes all originated from an identical founder cell. Furthermore, the diversity of cell types within the offspring population represents the potential of the founder cell [1,8,]. To precisely infer the potential, lineage tracing requires effective identification of cell-types. Ideally, several markers would be used to conduct accurate cell-type classifications. However, marker numbers are limited, which could possibly mask the variability observed within a group of cells that express the screened marker genes. Consequently, lineage tracing can result in biases [9,10,].

Single-cell RNA sequencing (scRNA-seq) technologies have increasingly allowed the probing of cell types over the past decade. scRNA-seq can help identify complex and rare cell type groups, help identify gene regulatory associations, aid the evaluation of developmental trajectories of different cell lineages, and help reveal cell-to-cell variabilities within various diseases

and therapeutic contexts [1,11–17]. The initial analysis of scRNA-seq data mainly involves clustering and annotation of individual cells into cell types based on their transcriptomes. Such analyses can inform our understanding of the biological characteristics that distinguish different cell groups, tumour cell heterogeneities, and cellular diversities from local tumour microenvironments. More importantly, while bulk tumour transcriptomes can help reveal therapeutic sensitivity, scRNA-seq can improve the inference of treatment efficacy by allowing identification of transcriptomic differences in coexisting tumour groups [18–21].

Many clustering algorithms have recently been developed to identify cell type-like structures from scRNA-seq datasets. These methods are generally developed on the assumption that cells of a particular type have similar transcriptomes that differ from other cell types in tissues [22–27]. In this study, we evaluated the use of scRNA-seq data in the development of analysis tools that are primarily associated with scRNA-seq clustering techniques including K-means clustering, hierarchical clustering, and consensus clustering. Moreover, we evaluated metrics for measuring clustering performances while comparing the clustering models and providing suggestions for future research directions.

2. Materials and methods

2.1. ScRNA-seg datasets

Published studies were gathered, and we summarized 20 scRNA-seq datasets from these including the provider, number of cells, number of genes, and cell resources (Table 1).

Table 1. ScRNA-seq datasets.

	Num. of	Num. of		
Dataset	cells	genes	Cell resource	
Trapnell [28]	182	38,694	Myogenic precursor cells and differentiating myoblast cells	https://www.ebi.ac.uk/biostudies/studies/ S-EPMC4122333?xr=true
Petropoulos [29]	1,529	3,000	Human preimplantation embryonic cells	ArrayExpress (https://www.ebi.ac.uk/arrayex press/)
Biase [72]	49	25,737	2-cell and 4-cell mouse embryos	GEO (https://www.ncbi.xilesou.top/)
Yan's [30]	124	22,687	Human preimplantation embryos and embryonic stem cells	GEO (https://www.ncbi.xilesou.top/)
Goolam [31]	124	41,480	4-cell mouse embryos	GEO (https://www.ncbi.xilesou.top/)
Pollen [70]	301	23,730	Human cerebral cortex	GEO (https://www.ncbi.xilesou.top/)
Kolodziejczyk's [32]	704	38,653	Mouse embryonic stem cell	ArrayExpress (https://www.ebi.ac.uk/arrayex press/)
Treutlein [33]	80	23,271	Distal lung epithelium	GEO (https://www.ncbi.xilesou.top/)
Ting [34]	149	29,018	Pancreatic circulating tumour cells	GEO (https://www.ncbi.xilesou.top/)
Patel [35]	430	5,948	Glioblastoma	PubMed (https://www.ncbi.xilesou.top/)
Usoskin [36]	622	25,334	Sensory neuron	GEO (https://www.ncbi.xilesou.top/)
Klein [37]	2,717	24,175	Embryonic stem cells	GEO (https://www.ncbi.xilesou.top/)
Zeisel [38]	3,005	19,972	Mouse cortex and hippocampus	GEO (https://www.ncbi.xilesou.top/)
Deng [39]	268	22,457	Mammalian cells	Science (https://www.sciencemag.org/)
Peng [81]	14,032	93,951	Peripheral blood mononuclear cells in systemic lupus erythematosus patients	https://github.com/ChengF-Lab/COAC
MacParland [40]	8,444	20,007	Parenchymal and non-parenchymal cells from five human livers	https://github.com/BaderLab/singleLiverCells
Yang [58]	500	32,738	Peripheral blood mononuclear cells	http://support.10xgenomics.com/single-cell/datasets
Shekhar [41]	27,499	13,166	Mouse retinal bipolar cells	GEO (https://www.ncbi.xilesou.top/)
Darmanis [69]	420	22,085	Human brain	GEO (https://www.ncbi.xilesou.top/)
Xu [71]	540	56,650	Idiopathic pulmonary fibrosis	GEO (https://www.ncbi.xilesou.top/)

2.2. Data analysis tools

Several analytical tools have recently been developed to facilitate the visualization of scRNA-seq data and identify subpopulations of cells. Twelve popular scRNA-seq analysis tools are summarized below.

2.2.1. DendroSplit

Zhang et al. [42] developed a clustering framework, DendroSplit [42] (https://github.com/jessemzhang/dendrosplit), for clustering cellular data. The tool emphasizes interpretability and is comparable in speed and accuracy to existing cluster models.

2.2.2. SinCHet

Li et al. [43] developed an analytical framework for continuous data (e.g., mRNA expression data) and binary omics data (e.g., discretized methylation) via a graphical user interface, SinCHet [43] (http://labpages2.moffitt.org/chen/soft ware/). The toolkit can quantify cellular heterogeneity at different clonal resolutions. In particular, it aids in the identification of emerging or disappearing clones and prioritizing biomarkers based on markers or variation between (or within) cellular populations.

2.2.3. Scater

McCarthy et al. [44] developed a bioconductor package, Scater [44] (http://bioconductor.org/packages/scater), to preprocess, normalize, and visualize scRNA-seq data. The package provides a convenient and flexible pipeline to transform raw sequencing reads into a reliable expression dataset that can be applied to downstream analyses.

2.2.4. **SPRING**

Weinreb et al. [45] developed a more reproducible stochastic visualization workflow, SPRING [45] (https://kleintools.hms.har vard.edu/tools/spring.html), that can filter, normalize, and visualize scRNA-seq data. SPRING has been used to uncover detailed biological associations by visualizing gene expression trajectories from upper airway epithelial cells and haematopoietic progenitor cells.

2.2.5. ASAP

Gardeux et al. [46] designed a fully integrated platform, ASAP [46] (https://github.com/DeplanckeLab/ASAP), to analyse scRNA-seq data. ASAP is web-based and combines various supervised learning methods with sophisticated visualization tools. The package can parse, filter, normalize, and visualize scRNA-seq data. In addition, it can help detect cellular subpopulations, differentially expressed genes, and functional gene enrichments. More importantly, it can be broadly applied to any RNA-seq dataset if there is an overlap between bulk RNA-seq and scRNA-seq analysis pipelines.

2.2.6. SIMLR

Wang et al. [47] described an open-source, large-scale genomic analysis tool, SIMLR [47] (https://github.com/BatzoglouLabSU/SIMLR), that learns sample-to-sample similarity from gene expression data of heterogeneous samples. SIMLR can effectively reduce the dimensionality of scRNA-seq data, cluster scRNA-seq data, and visualize heterogeneous populations. In addition, the package provides greater interpretability through useful visualizations.



2.2.7. SCANPY

Wolf et al. [48] designed a scalable tool, SCANPY [48] (https://github.com/theislab/Scanpy), to analyse single-cell gene expression data. SCANPY can preprocess, visualize, and cluster single-cell datasets for over one million cells. In addition, the package can perform tests of differential expression, pseudo-time and trajectory inference, and simulation of gene regulatory networks.

2.2.8. TSCAN

Ji Z. and Ji H. [49] developed the single-cell analysis tool, TSCAN [49] (https://zhiji.shinyapps.io/TSCAN/), to better reconstruct in silico pseudo-temporal paths in scRNA-seq analysis. TSCAN is web-based and can read and preprocess scRNA-seq data, rank cells according to transitions of their transcriptomes, and perform differential gene analysis and single gene visualization.

2.2.9. FastProject

DeTomaso D. and Yosef N. [50] developed the software package, FastProject [50] (https://github.com/YosefLab/ FastProject/wiki), to analyse and interpret scRNA-seq data and explore two-dimensional projections of these data. FastProject can also systematically investigate biological associations between these low-dimensional representations by integrating domain knowledge.

2.2.10. Granatum

Zhu et al. [51] developed an easy-to-use graphical interface, Granatum [51] (http://garmiregroup.org/granatum/app), to analyse scRNA-seq data. Granatum is web-based and contains a comprehensive list of functions including batch-effect removal, outlier-sample removal, gene filtering, gene-expression normalization, imputation, cell clustering, differential gene expression/ enrichment analysis, cellular pseudo-time pathway construction, and visualization of protein interaction networks.

2.2.11. FIt-SNE

Linderman et al. [52] combined t-distributed stochastic neighbour embedding (t-SNE) and designed an advanced version of t-SNE for scRNA-seq data analysis, FIt-SNE [52] (https:// github.com/KlugerLab/FIt-SNE), to visualize rare cell populations. Importantly, they still implemented a heatmap-style visualization (https://github.com/KlugerLab/t-SNE-

Heatmaps) of scRNA-seq data based on one-dimensional t-SNE in order to simultaneously visualize the expression patterns for thousands of genes.

2.2.12. SC3

Kiselev et al. [27] presented a user-friendly tool, SC3 [27] (http://bioconductor.org/packages/SC3), to quantify the characterization of cell types by combining global transcriptome profiles. In particular, SC3 can identify subclones from the transcriptomes of neoplastic cells.

2.3. Clustering methods

Given that gene expression data for p genes on n cells can be organized into a $p \times n$ matrix $x = (x_1, x_2, ..., x_n)$, x_i denotes

the gene expression profile of p genes in cell i and $x_i = (x_{i1}, x_{i2}, ..., x_{ip})'$. Various clustering models can then be used to identify cell subpopulations based on expression data.

2.3.1. K-means clustering

2.3.1.1. RaceID. Grün et al. [53] surmised that detecting rare cell types like cancer stem cells and circulating tumour cells is important for understanding the biological characteristics of normal and diseased tissues. They developed an identification method for rare cell types (RaceID) based on a K-means clustering algorithm. RaceID comprises the following two steps:

Step 1. Preprocessing

RaceID removes cells with low transcript levels, and then normalizes the total transcript counts of each cell, finally filters out genes with very low or high expressed values.

Step 2. Clustering

RaceID computes the similarity between two cells based on Pearson's correlation coefficients. A distance matrix equivalent to 1 minus the coefficient is then used as the distance matrix input for a K-means clustering algorithm in order to identify rare cell types from the gap statistic.

2.3.1.2. K-branches clustering. Chlis et al. [54] developed the K-Branches clustering algorithm. The algorithm introduced a clustering method similar to K-means and locally fitted halflines to represent the branches of differentiation trajectory. It can identify the precise number of 'tip regions' or 'branching regions' in a lineage tree. The K-branches clustering method comprises two steps:

Step 1. Calculate the distance between half-line and data point and assign all data to the nearest half-line.

Step 2. Update centre c and direction v of a cluster until the total cost *j* stops descending and obtain the final clusters.

The K-branches clustering method is similar to the K-means clustering method when computing distance. They are based on the Euclidean distance. However, for the K-means clustering algorithm, the distance computation severely affects the centre of a cluster. More importantly, the selection of the clustering centre is greatly influenced by noisy data that are far away from other samples. Therefore, the K-means clustering algorithm is not suitable to cluster non-spherical data. However, the K-branches clustering method iteratively selects data from a cluster to represent the centre c of the cluster, and then computes the sum of the distances between the remaining data and the centre c to split these data to the nearest half-line. The K-branches clustering algorithm developed a revised GAP statistic method to find whether a data point is at a branch tip, intermediate region or branching region of a lineage tree (Fig. 1).

2.3.2. Hierarchical clustering

2.3.2.1. SINCERA. Guo et al. [55] presented a computational framework for SINgle Cell RNA-seq profiling Analysis (SINCERA) to distinguish and evaluate major cell types, infer gene signatures related to cell types, and determine key factors for cell type identification and activity (driving forces). SINCERA consists of three major analytical procedures: pre-processing of related data, identifying cell types, and analysing gene signatures and driving forces (Fig. 2).

Random initialization:

Random assigning one data point as the center point c; Random assigning K data points as $x_1, x_2, ..., x_K$.



Assigning each data point x_i to its nearest half-line according to $d(x, L_k)$



Iteratively executing the following three optimization procedures until no change in cluster assignments:

- (1) Updating the center point *c*;
- (2) Updating the direction vectors $x_1, x_2, ..., x_K$;
- (3) Assigning each data point to its nearest half-line according to $d(x, L_k)$



Using the revised GAP to identify the region that each data point belongs to

Figure 1. Flowchart of the K-branches clustering method.

2.3.2.2. BISCUIT. Prabhakaran et al. [56] considered that various single-cell gene expression data can be obtained by using emerging technologies. But these expression data are interfered by the error of technologies or cell description. Global normalization is a universal solution; however, it can not fundamentally solve the problem: it failed to resolve missing data and did not consider technical variation, thereby severely depending on latent cell types. Therefore, they developed a Bayesian Inference method for Single-cell ClUstering and ImpuTing (BISCUIT). BISCUIT integrates iterative normalization and a hierarchical Dirichlet process mixture model. It can be iteratively applied to dropout data and clustering. More importantly, it eliminates technical variation caused by different biological signals.

2.3.2.3. CIDR. Lin et al. [24] designed the ultrafast algorithm Clustering through Imputation and Dimensionality Reduction (CIDR) to decrease the impact of dropouts on clustering performance. The CIDR framework comprises five steps:

Step 1. Detect possible dropouts.

CIDR first performs a logarithmic transformation of gene expression data for each cell C_i . It then characterizes the distribution of the transformed expression values through a peak at zero. The sample-

dependent threshold, T_i , is then found that separates the peak from the rest of the expression distribution. The entries in cell C_i with expression values smaller than T_i are possible dropouts, and the entries with expression values of less than T_i are considered as expressed.

Step 2. Estimate the association between the dropout rate and the gene expression level.

Considering the two cells C_i and C_j , CIDR defines their observed expression for a feature F_k as o_{ki} and o_{kj} , respectively. T_i and T_j are respective dropout candidate thresholds. If $o_{ki} < T_i$ and $o_{kj} \ge T_j$, then o_{ki} needs to be imputed and the imputation value, \widehat{o}_{ki} , can be defined as

$$\widehat{o}_{ki} = \widehat{P}(o_{ki})o_{ki} + (1 - \widehat{P}(o_{ki}))o_{ki},$$

where $P(o_{kj})$ is the probability of o_{kj} being a dropout and $\widehat{P}(o_{kj})$ is the estimation of $P(o_{kj})$ on the whole dataset.

Step 3. Calculate the dissimilarities among the expression profiles of the imputed genes for C_i and C_j .

For the cells $C_i = (o_{1i}, o_{2i}, ..., o_{ni})$ and $C_j = (o_{1j}, o_{2j}, ..., o_{nj})$, some entities are set as zeroes when relevant genes may be either not expressed in reality or a dropout value. CIDR computes their dissimilarities based on the Euclidean distance.

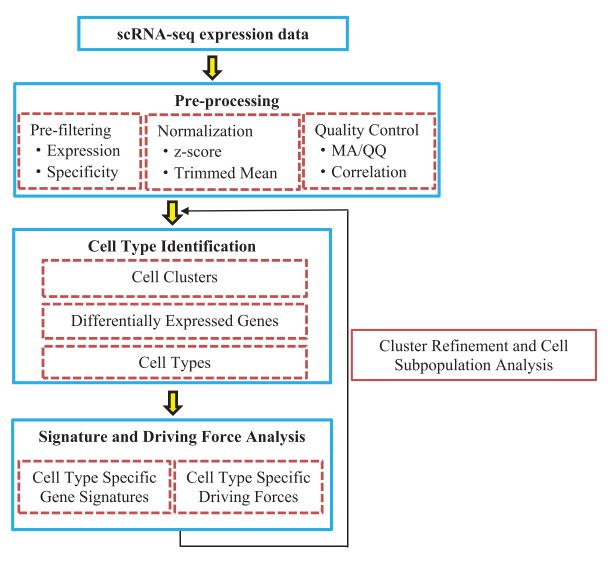


Figure 2. Flowchart of single-cell RNA-seq profiling analysis.

Step 4. Conduct a Principal Coordinates Analysis (PCoA) with the dissimilarity matrix.

CIDR performs a PCoA with the distance matrix obtained from Step 3 to reduce the dimensionality of the data.

Step 5. Cluster with the top principal coordinates.

CIDR performs hierarchical clustering using the top principal coordinates from the PCoA (Fig. 3).

2.3.2.4. Corr. Jiang et al. [25] posited that a key problem in scRNA-seq clustering is quantifying the associations between cells. However, scRNA-seq data are generally sparse, noisy, exhibit high dimensionality, and are heterogeneous. These characteristics seriously impact the effectiveness and reliability of conventional (dis)similarity measure methods when clustering single cells. Therefore, the authors exploited a new single-cell clustering algorithm by integrating cell-cell similarities and hierarchical clustering analysis. The methods comprise four steps (Fig. 4).

Step 1. Define a 'differentiability correlation' (Corr) between two cells based on differential expression patterns of genes in order to measure cell-cell similarities:

$$Corr_{ij} = \frac{\sum_{k=1}^{p} (U_{i_{j}k} - \overline{U}_{i_{j}})(U_{j_{i}k} - \overline{U}_{j_{i}})}{\sqrt{\sum_{k=1}^{p} (U_{i_{j}k} - \overline{U}_{i_{j}})^{2}} \sqrt{\sum_{k=1}^{p} (U_{j_{i}k} - \overline{U}_{j_{i}})^{2}}}$$

where $U_{i,k}$ represents the differential status of the kth gene in cell i:

$$U_{ijk} = \left\{ egin{array}{ll} 1, & k \in V_{i_j}^+ \ -1, & k \in V_{i_j}^- \ 0, & otherwise \end{array}
ight.$$

 $V^+_{i_j}$ (or $V^-_{i_j}$) denotes genes in the ith cell, and the expression level of each gene in $V^+_{i_j}$ (or $V^-_{i_j}$) are all larger (or smaller) than the average value across all other cells except the ith cell.

Step 2. The dissimilarity between two cells is calculated by

$$S_{ij} = 1 - Corr_{ij}$$

Step 3. Determine the optimal number of clusters from the level that cell subpopulations are separated:

Detecting possible dropouts

Step1: Performing a logarithmic transformation

Step2: Characterizing the distribution of the transformed expression values

Step3: Finding possible dropouts based on a sample-dependent threshold



Estimating the association between dropout rate and gene expression level

For two cells C_i and C_j , supposing their dropout candidate thresholds: T_i and T_j and defining imputation value $\hat{O}_{ki} = \hat{P}(O_{kj})O_{kj} + (1 - \hat{P}(O_{kj}))O_{ki}$



Calculating the dissimilarities based on Euclidean distance after implicating imputation



Performing PCoA to implement dimension reduction



Clustering with the top few principal coordinates

Figure 3. Flowchart of imputation and dimensionality reduction framework.

$$r_{j} = \frac{SSB_{j}}{SST_{j}}$$
 where $SSB = \sum_{j=1}^{s} n_{j} (\overline{Y}_{j} - \overline{Y})^{2}$.
$$SST = \sum_{i=1}^{s} \sum_{j=1}^{n_{j}} (Y_{ij} - \overline{Y})^{2}$$

 Y_{ij} represents the random response of the *i*th $(i = 1, 2, ..., n_j)$ observation in the *j*th (j = 1, 2, ..., s) treatment group.

Step 4. Cells are grouped into several subpopulations based on hierarchical clustering.

2.3.2.5. CellBIC. Kim et al. [26] investigated intrinsic multimodality features of heterogeneous scRNA-seq data and presented a single-Cell BImodel Clustering (CellBIC) method to detect cellular subpopulations. CellBIC combines a top-down hierarchical clustering algorithm and a bimodal expression pattern of scRNA-seq data (Fig. 5).

2.3.3. Consensus clustering

2.3.3.1. SC3. Kiselev et al. [27] developed a Single-Cell Consensus Clustering method (SC3). The robust method displayed high accuracy by combining multiple clustering

techniques. SC3 is performed by the following six basic steps (Fig. 6).

Step 1. Gene filtering.

Genes are removed that are either expressed in less than a % of cells or expressed in at least (100-a)% of cells, because these ubiquitous and rare genes, respectively, are not often informative for clustering.

Step 2. Distance calculation.

Distances are calculated between two cells using Euclidean, Pearson, and Spearman metrics.

Step 3. Transformation.

All distance matrices are transformed with PCA or the eigenvectors of the connected graph Laplacian matrix.

Step 4. K-means clustering.

A K-means clustering algorithm is applied on the first *d* eigenvectors of the transformed distance matrices.

Step 5. Consensus clustering

A consensus matrix is calculated with a cluster-based similarity partitioning algorithm [57] via two steps. A binary similarity matrix is first constructed from cell labels for each individual K-means cluster result and all similarity matrices are then averaged for individual clustering results to obtain a consensus matrix. In the former, the SC3 similarity between the two cells is set as 1 if the two cells are clustered into the same subpopulation; otherwise, the similarity is set as 0.

Defining 'differentiability correlation' between two cells

$$Corr_{ij} = \frac{\sum_{k=1}^{p} (U_{i_{j}k} - \overline{U}_{i_{j}})(U_{j_{i}k} - \overline{U}_{j_{i}})}{\sqrt{\sum_{k=1}^{p} (U_{i_{j}k} - \overline{U}_{i_{j}})^{2}} \sqrt{\sum_{k=1}^{p} (U_{j_{i}k} - \overline{U}_{j_{i}})^{2}}}$$

Representing dissimilarity between two cells

$$S_{ij} = 1 - Corr_{ij}$$

Determining optimal number of clusters

$$r_{j} = \frac{SSB_{j}}{SST_{j}} = \frac{\sum_{j=1}^{s} n_{j} (\overline{Y}_{,j} - \overline{Y})^{2}}{\sum_{j=1}^{s} \sum_{i=1}^{n_{j}} (Y_{ij} - \overline{Y})^{2}}$$

Grouping all cells into several subpopulations

Figure 4. Flowchart of differentiability correlation methods.

Calculating Boolean membership using a Gaussian mixture model Capturing a gene group Dissecting cells into two groups Finding a top-down hierarchical cluster

Figure 5. Flowchart of single-cell bimodel clustering (CellBIC) method.

Step 6. Hierarchical clustering.

The resulting consensus matrix is clustered using a hierarchical cluster method with complete agglomeration, followed by inference of the clusters at the *k* level of hierarchy.

2.3.3.2. The SAFE-clustering method. Yang et al. [58] developed the SAFE-clustering method based on aggregated (from ensemble) clustering. The method comprises two components, with the first employing the SAFE-clustering of clustered Clustering the resulting consensus matrix

Figure 6. Flowchart of single-cell consensus clustering method.

scRNA-seq data using four state-of-the-art algorithms (SC3 [27], CIDR [24], Seurat [59] and tSNE+K-means). In the second component, SAFE-clustering performs cluster ensemble aggregation to obtain consensus cluster labels using three hypergraph-based partitioning methods (HGPA, MCLA, and CSPA). The details of the SAFE-clustering method are shown in the algorithm outlined below (Table 2), wherein ANMI represents the Average Normalized Mutual Information (ANMI) in the SAFE-clustering algorithm.

2.3.3.3. GiniClust2. Tsoucas and Yuan [60] developed a new computational model, GiniClust2, to identify rare and common cell types. GiniClust2 effectively combines the advantages of two complementary clustering algorithms including the Gini indexbased technique and the Fano factor-based technique. The model assigns the more reliable subpopulations higher weights based on the following steps (Fig. 7).

Step 1. Filter genes and cells by removing genes expressed in less than three cells, and cells with expression of less than 2,000 genes. GiniClust2 then performs the following four steps.

Step 2. Infer cell subpopulations based on the Gini indexbased features.

In the Gini index-based clustering algorithm, GiniClust2 uses a two-step LOESS regression model and removes the trend with the maximum expression levels to normalize raw Gini index values. Genes with Gini index values significantly larger than zero after normalization are considered as high Gini value genes. The high Gini value genes are then used to calculate the distances between cells with the Jaccard metric. The distances are used to cluster cells with density-based spatial clustering.

Step 3. Infer cellular subpopulations based on Fano factor-based features.

The Fano factor-based clustering algorithm first defines the Fano factor as the variance in mean expression levels for each gene. The 1,000 genes with the highest Fano factor values are then reserved for further analysis. The top 50 principal components from principal components analysis (PCA) are then chosen for clustering analysis from the gene expression matrix. Finally, cellular subpopulations are inferred using the K-means clustering algorithm.

Step 4. Integrate the results from the Gini index-based method in Step 2 and the Fano factor-based method in Step 3 through a cluster-aware and a weighted consensus method to compute the probability that two cells belong to the same cluster.

 P^G and P^F are the partitions obtained from the Gini indexbased and Fano factor-based clustering algorithms, respectively. Each partition consists of cluster sets:

$$C^G = \{C_1^G, C_2^G, ..., C_{k_G}^G\} \text{ and } C^P = \{C_1^F, C_2^F, ..., C_{k_F}^F\}.$$



Table 2. The SAFE-clustering algorithm.

```
1: Run SC3, CIDR, Seurat and t-SNE+K-means to generate a Y_{4\times n} matrix of
2: Transform the output labels of each clustering method into a hypergraph
3: For k=2 to K_{\text{max}}//K_{\text{max}} is either specified by the user or is the maximum
   value across these four individual methods
4:
     If MCLA = TRUE
```

Do MCLA 5: Compute the Jaccard similarity matrix $S_{JAC} = \frac{h_p h_q^T}{h_c^2 + h_a^2 - h_p h_a^T}$ for two 6:

7: k – way partitioning using the *gpmetis* program in the hMETIS

8: Compute the association index (MC_{ci}), c = 1, 2, ..., k, i = 1, 2, ..., n, and assign each single cell to the meta-cluster c with the largest AI metric If there are empty clusters

10: Re-label into k' non-empty meta-clusters

11: End

Fnd 12:

If HGPA = TRUE13:

Do HGPA

k — way partitioning using the *sbmetis* program in the hMETIS 15: package

16: End

If CSPA = TRUE17:

18: Do CSPA

Compute and normalize the similarity matrix S 19:

20: k – way partitioning using the *gpmetis* program in the hMETIS package

21: End

Calculate ANMI across ensemble methods

Return consensus cluster labels L_e and ANMI

25: Return the optimal consensus result \widehat{L}_{e-opt} of \widehat{k}_{e-opt} clusters with the $\text{highest ANMI: } (\widehat{L}_{e-opt}, \widehat{K}_{e-opt}) = \underset{\substack{L_e, K_e, m \in \{HGPA, MCA, and/or CSPA\}}}{\text{arg max}}$

GiniClust2 defines the weighted consensus associated score as,

$$\overline{M}_{ij} = w_{ii}^G M_{ij}(P^G) + w_{ij}^F M_{ij}(P^F)$$

where $M_{ij}(P^G)$ and $M_{ij}(P^F)$ denote the connectivity matrices:

$$M_{ij}(P^G) = egin{cases} 1, (i,j) \in C_k(P^G) \ 0, \ otherwise \end{cases}$$
 and $M_{ij}(P^F) = egin{cases} 1, (i,j) \in C_k(P^F) \ 0, \ otherwise \end{cases}$.

Connectivity between two cells is set as 1 if the two cells are grouped into the same cluster; otherwise, the value is set as 0. and

$$w_{ij}^G = rac{w_{ij}^{G_{ini}}}{w_{ij}^{G_{ini}} + w_{ij}^{F_{ini}}} ext{ and } w_{ij}^{F_{ini}} = rac{w_{ij}^{F_{ini}}}{w_{ij}^{G_{ini}} + w_{ij}^{F_{ini}}},$$

where $w_{ij}^{G_{ini}} = \max(w_i^{G_{ini}}, w_j^{G_{ini}})$, $w_i^{G_{ini}}(x_i)$ denotes the cellspecific Gini index-based weights $w_i^{G_{ini}}(x_i) = 1 - 1/(1 + e^{\frac{x_i - \mu'}{s'}}),$ $w_{ii}^{F_{ini}} = 1 - 1/(1 + e^{\frac{\mu - \mu}{s}})$, x_i is the proportion by which cell i belongs to the Gini index-based cluster, μ' represents the proportion by which the Gini index-based and Fano factorbased clustering algorithms have effectively identical ability to find rare cell types, and s' denotes how quickly the Gini indexbased clustering algorithm loses its ability to find rare cell types above μ' .

Step 5. Determine the final clustering assignment.

GiniClust2 builds the following non-negative matrix factorization model to produce a soft clustering,

$$\min_{U} ||\bar{M} - U||^2$$

where \overline{M} represents the probability that two cells belong to the same cluster. And an orthogonality constraint is used to obtain a hard clustering similar to K-means.

2.3.3.4. ZINB-WaVE. Risso et al. [61] developed the general and flexible model termed the Zero-Inflate Negative Binomial-based Wanted Variation Extraction (ZINB-WaVE) to represent single-cell data in low dimensionality while accounting for dropouts and over-dispersion (Fig. 8).

ZINB-WaVE comprises the following steps.

For any $\pi \in [0,1]$, $\mu \ge 0$ and $\theta > 0$, ZINB-WaVE is first defined as the probability mass function of the ZINB distribution by,

$$f_{ZINB}(y; \mu, \theta, \pi) = \pi \delta_0(y) + (1 - \pi) f_{NB}(y; \mu, \theta)$$

where $\sigma_0(\cdot)$ is the Dirac function, $f_{NB}(y;\mu,\theta) = \frac{(y+\theta)}{(y+1)(\theta)} (\frac{\theta}{\theta+\mu})^{\theta}$ $\left(\frac{\mu}{\mu+\theta}\right)^y$, $\forall y \in \mathbb{N}$.

Given p genes (features) in n cells (samples), Y_{ij} represents the count of features j in sample i. ZINB-WaVE is then modelled as Y_{ij} , representing a random variable following the ZINB distribution where the parameters are satisfied by the following regression models:

$$\ln(\mu_{ij}) = \left(X\beta_{\mu} + \left(V\gamma_{\mu}\right)^{T} + W\alpha_{\mu} + O_{\mu}\right)_{ij}$$
$$\operatorname{logit}(\pi_{ij}) = \left(X\beta_{\pi} + \left(V\gamma_{\pi}\right)^{T} + W\alpha_{\pi} + O_{\pi}\right)_{ij},$$
$$\operatorname{ln}(\theta_{ij}) = \varsigma_{j}$$

where $logit(\pi) = ln(\pi/(1-\pi))$, X is a known $n \times M$ matrix corresponding to M cell-level covariates, V is a known $m \times L$ matrix corresponding to m gene-level covariates, W is an unknown $n \times K$ matrix corresponding to K unknown cell-level covariates, O_{μ} and O_{π} are known nmatrices of offsets, and $\beta = (\beta_u, \beta_\pi)$ is associated with M matrices of X from regression parameters.

2.3.4. Other cluster methods

2.3.4.1. The SNN-clique algorithm. Xu et al. [62] developed the SNN-clique algorithm that combines shared nearest neighbour (SNN) and quasi-clique-based clustering models. The authors first established that the SNN method is relatively robust and can obtain stable performances, and then developed a quasi-clique-based clustering model to capture cell subpopulations with different shapes and densities (Fig. 9).

2.3.4.2. ScImpute. Li W. V. and Li J. J. [63] introduced a statistical model, scImpute, that automatically detects possible dropouts and outlier cells. ScImpute comprises four steps (Fig. 10) as follows.

Step 1. Data processing and normalization.

ScImpute takes a count matrix, X^{C} , providing the expression values of pgenes for n cells as the input and first normalizes X^C with the library size of each cell (sample) to obtain

Filtering of genes and cells

Inference of cellular subpopulations

Inferring cellular subpopulations based on Gini index-based features

Step 1 Normalizing raw Gini index values based on a two-step LOESS regression model

Step 2 Selecting high Gini genes

Step 3 Calculating distances between two cells with the Jaccard metric

Step 4 Using the distance as input to cluster cells with density-based spatial clustering

Inferring cellular subpopulations based on Fano factor-based features

Step1 Defining Fano factor as variance in mean expression level for each gene Step2 Reserving 1,000 genes with the highest Fano factor for further analysis Step 3 Choosing top 50 principal components for clustering analysis with PCA

Step 4 Inferring cell subpopulations by k-means clustering algorithm.

Integration of the results

Computing weighted consensus associated score:

$$\bar{M}_{ij} = w_{ij}^G M_{ij}(P^G) + w_{ij}^F M_{ij}(P^F)$$

Figure 7. Flowchart of method combining gini index and fano factor.

 X^N . ScImpute then computes a matrix, X, to avoid infinite values in parameter estimation using the following model:.

$$X_{ij} = \log_{10}(X_{ii}^{N} + 1.01); i = 1, 2, ..., p, j = 1, 2, ..., n$$

Step 2. Detect cell subpopulations and outliers.

ScImpute performs PCA on X to achieve the ordination results, Z. The distance matrix $D_{n\times n}$ is then calculated from similarities within the Zdataset. For $L=\{l_1,l_2,..,l_n\}$, with l_j representing the distance of cell j to its nearest neighbour, ScImpute denotes its first and third quartiles as Q_1 and Q_3 , respectively. The outlier cells O are then defined as: $O=\{j:l_j>Q_3+1.5(Q_3-Q_1)\}$. Finally, ScImpute clusters the remaining cells $\{1,2,...,n\}\setminus O$ into K subpopulations with spectral clustering.

Step 3. Calculate dropout values.

ScImpute models the expression of gene i in cell cluster k as a random variable, $X_i^{(k)}$, with the density function as.

$$\begin{split} f_{X_i^{(k)}}(x) &= \lambda_i^{(k)} Gamma(x; \alpha_i^{(k)}, \beta_i^{(k)}) \\ &+ (1 - \lambda_i^{(k)} Normal(x; \mu_i^{(k)}, \sigma_i^{(k)}) \end{split}$$

The dropout probability by which gene i in cell j belongs to cluster k can then be estimated as.

$$d_{ij} = \frac{\widehat{\lambda}_{i}^{(k)}Gamma(X_{ij}; \widehat{\alpha}_{i}^{(k)}, \overset{\wedge}{\beta}(k))}{\widehat{\lambda}_{i}^{(k)}Gamma(X_{ij}; \widehat{\alpha}_{i}^{(k)}, \widehat{\beta}_{i}^{(k)}) + (1 - \lambda_{i}^{(k)}Normal(X_{ij}; \widehat{\mu}_{i}^{(k)}, \widehat{\sigma}_{i}^{(k)})}$$

Step 4. Impute dropout values.

Gene set A_j in cell j requires imputation based on the threshold t value of dropout probabilities: $A_j = \{i : d_{ij} \ge t\}$, whereas the gene set $B_j = \{i : d_{ij} \le t\}$ has accurate gene expression data and does not require imputation. Given these assumptions, ScImpute first computes the similarities among cells based on the non-negative least squares from B_i :

$$\widehat{\beta}(j) = \underset{\beta(j)}{\operatorname{arg\,min}} ||X_{B_j,j} - X_{B_j,N_j}\beta(j)||_2$$
subject to $\beta(j) \ge 0$,

where N_j denotes the indices of candidate neighbour

cells of cell j. $\beta(j)$ is then used to impute the expression values of genes in A_j from cell j based on the expression of the same genes in other similar cells from B_j :

$$\widehat{X}_{ij} = \begin{cases} X_{ij}, & i \in B_j \\ X_{i,N_i} \widehat{\beta}^{(j)}, i \in A_j \end{cases}$$

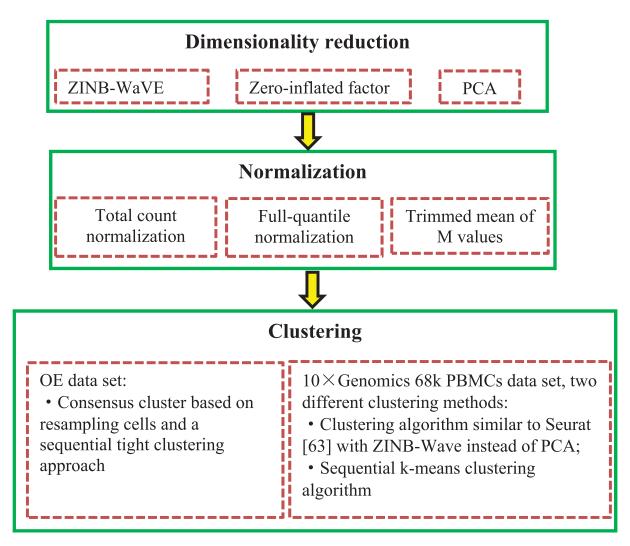


Figure 8. Flowchart of zero-inflate negative binomial-based wanted variation extraction.

2.3.4.3. RAFSIL. Pouyan et al. [64] exploited a random forest-based method, RAFSIL, to identify similarities among cells via clustering of scRNA-seq data using the following three steps

Step 1. Use three types of filtering based on gene abundances: all genes (ALL), frequency filtering (FRQ), and highly expressed genes (HiE).

Step 2. Use FRQ to filter and cluster genes by treating genes as observations and cells as features. The most representative principal components via PCA are then chosen for further analysis.

Step 3. Classification of all cells using a random forest-based similarity learning method (Fig. 11).

2.3.4.4. SparseDC. Barron et al. [65] hypothesized that cell types changed when micro-environments changed and designed the Sparse Differential Clustering (SparseDC) algorithm to evaluate these dynamics. SparseDC defines 'condition A' and 'condition B' as the conditions before and after the change, respectively. The gene expression matrix $X_{p \times n}$ represents the expression of p genes in n cells under condition A. C_k indicates the indices of all cells contained in cluster k

under condition A, $j \in C_k$ indicates that cell j in condition A is grouped into cluster k, j = 1, 2, ..., n, k = 1, 2, ..., K. In addition, N_k is the size of C_k with $\sum_{k=1}^K N_k = n$, μ_{ik} as the cluster centre for gene i and cluster k under condition A. $X', C_k', N_k', \mu_{ik}'$ can similarly be defined for condition B.

SparseDC then exploits the following optimization problem:

$$\begin{split} \min T(C,C',\mu,\mu') &= \sum_{i=1}^{p} \sum_{k=1}^{K} \{ \frac{1}{2} \sum_{j \in C_k} \left(X_{ij} - \mu_{ik} \right)^2 + \frac{1}{2} \sum_{j \in C_k} \left(X'_{ij} - \mu'_{ik} \right)^2 \\ &+ \sqrt{N_k} \lambda_1 \big| \mu_{ik} \big| + \sqrt{N'_k} \lambda_1 \big| \mu'_{ik} \big| \\ &+ \left(\sqrt{N_k} + \sqrt{N'_k} \right) \lambda_2 \big| \mu_{ik} - \mu'_{ik} \big| \}, \end{split}$$

where λ_1 and λ_2 are parameters.

SparseDC initializes C and C' by randomly assigning each cell to clusters and then detecting the final clusters by iteratively updating {C,C'} and { μ , μ' } until the clustering results do not change.

2.3.4.5. ScNN. Lin et al. [66] designed a neural network-based (scNN) method to detect and analyse cellular clusters. Given that the vector $x^{(0)}$ is the input of the scNN algorithm

Constructing an SNN graph with weight of each edge $e(x_i, x_j)$:

$$w(x_i, x_j) = \max\{k - \frac{1}{2}(rank(v, x_i) + rank(v, x_j)) \mid v \in NN(x_i) \cap NN(x_j)\}$$



Extracting maximal quasi-cliques in the SNN graph using a greedy algorithm based on the local degree of e



Finding clusters through merging quasi-cliques based on the overlapping rate:

$$O_{ij} = \frac{|S_i \cap S_j|}{\min(|S_i|, |S_j|)}$$



Assigning nodes to unique clusters based on the proximity between candidate cluster C and the target node V:

$$Score(C, v) = \frac{1}{|C|} \sum_{i=1}^{|C|} w(c_i, v)$$

Identifying clusters in the SNN graph

Figure 9. Flowchart of shared nearest neighbour (SNN) technique and quasi-clique-based clustering models.

and $x^{(i)}$ is the output of *i*th hidden layer, scNN explores the following forward propagation:

$$x^{(i)} = a(W^{(i)}x^{(i-1)} + b^{(i-1)}),$$

where a is the activation function, b is an intercept term, and W is the weight matrix. scNN uses the tangent (tanh) as the activation function due to its optimal performance and subsequently focuses on learning W and b:.

$$tanh(x) = \frac{1 - \exp(-2x)}{1 + \exp(-2x)}$$

For the output layer, scNN uses a softmax activation function to conduct discrete classification:

$$output(x) = soft \max(x) = \left[\frac{\exp(x_1)}{\sum_c \exp(x_c)} \cdots \frac{\exp(x_C)}{\sum_c \exp(x_c)}\right]^T$$

where *C* denotes the indices of all cell types in the training dataset.

The output $f(x^{(0)})_c$ for each node c in the output layer indicates the probability by which the sample $x^{(0)}$ in the input layer belongs to cell type c:

$$f(x^{(0)})_c = p(y = c|x^{(0)}).$$

2.3.4.6. ScVDMC. Zhang et al. [67] exploited a Variance-Driven Multitask-based Clustering (scVDMC) algorithm to solve the cross-cell-population clustering problem. scVDMC utilizes multiple single-cell populations from different datasets and identifies cell clusters by controlling the variance among their subpopulations within each dataset and across all datasets.

scVDMC assumes that the matrix $X^{(d)} \in \mathbb{R}^{p \times n^{(d)}}$ indicates gene expression values of scRNA-seq from domain $d \in \{1,2,...D\}$, where each domain, d, represents a single-cell population for clustering, p is the number of genes (features) and $n^{(d)}$ is the size of single-cell samples from domain d. $U^{(d)} \in \mathbb{R}^{p \times k}$ denotes the centres of clusters (cell types), vector $Y^{i,j} = [U^{(1)}_{i,j}, U^{(2)}_{i,j}, ..., U^{(D)}_{i,j}]^T$ represents the (i,j)-th entry of every $U^{(d)}$, and $V^{(d)} \in \{0,1\}^{n^{(d)} \times k}$ indicates the

Data processing and normalization

$$X_{ij} = \log_{10}(X_{ij}^{N} + 1.01); i = 1, 2, ..., p, j = 1, 2, ..., n$$

Detection of cell subpopulations and outliers

Step 1 Performing PCA on X

Step 2 Calculating distance matrix $D_{n \times n}$

Step 3 Defining outlier cells O as

$$O = \{j: l_i > Q_3 + 1.5(Q_3 - Q_1)\},\$$

Step 4 Clustering the remaining cells $\{1,2,...,n\}\setminus 0$

Computing a random variable
$$X_i^{(k)}$$
 with density function:
$$f_{X_i^{(k)}}(x) = \lambda_i^{(k)} Gamma(x; \alpha_i^{(k)}, \beta_i^{(k)}) + (1 - \lambda_i^{(k)} Normal(x; \mu_i^{(k)}, \sigma_i^{(k)})$$

Computation of dropout values

Computing dropout probability:

$$d_{ij} = \frac{\hat{\lambda}_{i}^{(k)} Gamma(X_{ij}; \hat{\alpha}_{i}^{(k)}, \hat{\beta}_{i}^{(k)})}{\hat{\lambda}_{i}^{(k)} Gamma(X_{ij}; \hat{\alpha}_{i}^{(k)}, \hat{\beta}_{i}^{(k)}) + (1 - \lambda_{i}^{(k)} Normal(X_{ij}; \hat{\mu}_{i}^{(k)}, \hat{\sigma}_{i}^{(k)})}$$

Imputation of the dropout values

Step 1 Computing cells' similarities:

$$\hat{\boldsymbol{\beta}}^{(j)} = \underset{\boldsymbol{\beta}^{(j)}}{\operatorname{arg\,min}} \| X_{\boldsymbol{\beta}_{j}, j} - X_{\boldsymbol{\beta}_{j}, N_{j}} \boldsymbol{\beta}^{(j)} \|_{2}^{2}$$
subject to $\boldsymbol{\beta}^{(j)} \ge 0$

Step 2 Imputing expression values of genes:

$$\hat{X}_{ij} = \begin{cases} X_{ij}, & i \in B_{j} \\ X_{i,N_{j}} \hat{\beta}^{(j)}, & i \in A_{j} \end{cases}$$

Figure 10. Flowchart of a new imputation model for scRNA-seq data.

assignments of each single cell into clusters while k is the number of clusters. $B \in \{0,1\}^p$ represents the indicators of feature selection where B_i is set as 1 if the *i*th gene is selected as a feature, and set as 0 otherwise. D_B is the diagonal matrix on B. scVDMC then defines the following optimization model:

$$\begin{split} & \min_{U^{(d)}, V^{(d)}, B} \frac{1}{2} \sum_{d=1}^{D} ||D_B(X^{(d)} - U^{(d)}V^{(d)^T})||_F^2 - w \sum_{d=1}^{D} B^T Var(U^{(d)}) \\ &+ \alpha \sum_{i,j} B_i Var(Y^{(i,j)}) \end{split}$$

subject to
$$\sum B = \lambda$$
,

Gene filtering by comprising one of the following:

All genes (ALL)

Frequency filtering (FRQ)

Highly expressed genes (HiE)

RAFSIL: feature construction

RAFSIL gene filtering and clustering:

Step 1 Obtaining gene-filtered expression matrix x using FRQ

Step 2 Obtaining the most informative principal components using PCA

Step 3 Deriving gene clusters applying k-means clustering

RAFSIL Spearman feature space construction:

Step 1 Decomposing the column space of x into orthogonal sub-spaces based on gene clustering

Step 2 Calculating $n \times n$ cell-cell similarity matrices $\{C_1, C_2, \dots, C_k\}$ using Spearman rank correlation

Step 3 Obtaining m_i informative principal components by performing PCA for each C_i

Step 4 Yielding k matrices $\{F_i \in \mathbb{R}^{n \times m_i}\}$ based on genes in cluster i

Step 5 Constructing a final feature matrix F by juxtaposing matrices from individual gene clusters: $F = (F_1, F_2, ..., F_k)$

Step 6 Representing each cell j as a feature vector $f_j \in \mathbb{R}^{\tilde{p}} (\tilde{P} = \sum_{i=1}^k m_i)$

RAFSIL: Radom Forest-based Similarity Learning

RAFSIL1:

Step 1 Generating 'synthetic' dataset by shuffling the values of each feature independently;

Step 2 Distinguishing the shuffled data from the unshuffled data with RF classifier;

Step 3 Defining the RF based similarity matrix S^i and dissimilarity matrix D^i ;

Step 4 Repeating the above three steps B times and aggregating individual S^i and D^i into a final matrix S and D.

RAFSIL2 (without the need for synthetically generated datasets):

Step 1 Driving class labels for all cells by selecting a single feature *j* and quantizing its values;

Step 2 Removing the *jth* column from *F* and learning the obtained class labels with the reduced dataset base on RF classifier;

Step 3 Yielding similarity matrix S^i and dissimilarity matrix D^i ;

Step 4 Repeating the above steps for all features and aggregating individual S^i and D^i into a final matrix S and D.

Using similarities as a vector embedding for each cell and performing K-means clustering to identify cell labels

Using learned dissimilarities and running hierarchical clustering with average linkage to identify cell labels

Figure 11. Flowchart of random forest-based single-cell clustering method.

$$\sum_{i} V_{i,j}^{(d)} = 1, \forall i = 1, 2, ..., n^{(d)}, \forall d = 1, 2, ..., D.$$

Zhang *et al.* [67] solved the optimization problem using an alternating updating strategy, thereby addressing the cross-population clustering problem.

2.4. Evaluation metrics

To evaluate clustering methods, several popular metrics can be used including the Adjusted Rand Index (ARI) and the Normalized Mutual Information (NMI) metrics based on known labels of single cells.

2.4.1. ARI

Given that *n* cells are grouped into *k* clusters, $\{u_i\}_{i=1}^n$ represents the inferred cluster labels, and $\{v_i\}_{i=1}^n$ is the pre-annotated labels. Then,

$$ARI = \frac{\sum_{ls} \binom{n_{ls}}{2} - \left(\sum_{l} \binom{n_{l}}{2} \sum_{s} \binom{n_{s}}{2}\right) / \binom{n}{2}}{\left(\sum_{l} \binom{n_{l}}{2} + \sum_{s} \binom{n_{s}}{2}\right) / 2 - \left(\sum_{l} \binom{n_{l}}{2} \sum_{s} \binom{n_{s}}{2}\right) / \binom{n}{2}}$$

where *l* and *s* denote the *k* clusters, $n_l = \sum_{i=1}^{n} I(u_i = l)$, $n_s = \sum_{i=1}^n I(v_i = s)$, and $n_{ls} = \sum_{i,j=1}^n I(u_i = l)I(v_i = s)$ with I(x = l)y) as an indicator function with value of 1 for x = y, but 0 otherwise. The ARI decreases with increasing disagreement between the inferred labels and the known labels, with a value of 1 when the inferred labels perfectly coincide with the known labels.

2.4.2. NMI

Given that $p_l = \frac{n_l}{n}$, $q_s = \frac{n_s}{n}$, and $z_{ls} = \frac{n_l}{n}$, then $\hbar(u) = -\sum_l p_l \log(p_l)$ and $\hbar(v) = -\sum_s q_s \log(q_s)$ are the entropies of the two subpopulations, respectively, and $i(u, v) = \sum_{l,s} z_{ls} \log(z_{ls}/p_l/q_s)$ is their mutual information. The NMI is used to measure the level of perfect overlap between subpopulations, and also decreases with increasing disagreement between the inferred and known labels. The NMI is defined as:

$$NMI = i(u, v) / \sqrt{\hbar(u)\hbar(v)}$$

3. Results

scRNA-seq technologies allow numerous avenues for revealing novel and potentially unexpected biological discoveries. For example, scRNA-seq has been used to capture subclones via transcriptomic comparisons of neoplastic cells. The strategy holds enormous prospects for applied and basic biology, including clinical trials [23]. scRNA-seq clustering aims to elucidate cell-to-cell heterogeneity and uncover cell subgroups and cell dynamics at the group level. More importantly, scRNA-seq clustering analysis can allow the discovery of new subtypes of cells and marker genes for existing cell

Two aspects of scRNA-seq data analysis were discussed in the present review: relevant datasets and analytical tools. In particular, we discussed scRNA-seq clustering models including K-means clustering, hierarchical clustering, consensus clustering, and other similar methods. Two primary evaluation metrics (e.g. ARI and NMI) were used to evaluate these methods.

We performed extensive experiments to evaluate the performances of seven state-of-the-art scRNA clustering methods on five public available datasets. These seven methods are CIDR [24], SC3 [27], tSNE+k-means (tSNE [68] followed by k-means clustering), RaceID [53], scImpute [63], SAFE [58], and GiniClust2 [61], respectively. These five datasets are from human brain [69], cerebral cortex [70], IPF [71], peripheral blood mononuclear cells [58], and mouse 2-cell and 4-cell embryos [72],

respectively. They can be downloaded from the GEO or SRP041736, SRA database (GSE67835, GSE86618, SRP073767 and GSE57249). The experiments were performed on an iMAC with 2.4 GHz Inter Core i5, 8GB 2133 MHz CPDDR3 of RAM and OS Catalina 10.15.2 operating system.

We preprocessed scRNA-seq data based on the preprocessing steps provided by the corresponding papers. The results are shown in Table 3. In the human brain dataset [69], samples with library size more than 10,000 were retained. In the cerebral cortex dataset [70], genes expressed in less than 2 cells were removed. In the peripheral blood mononuclear cells [58] and mouse 2-cell and 4-cell embryos [72] datasets, the raw tag table were normalized by size factor and transformed by $\log_{10}(X+1)$. In the human IPF dataset [71], each expression profile was transformed by z-scores $(z^s_{ij} = \frac{(E^s_{ij} - \mu^s_{ij})}{\sigma^s_i}$, where σ^s_i and μ^s_i represent the standard and mean deviation, respectively). The results of comparison were shown in Table 4-8.

In the human brain scRNA-Seq dataset [69], GiniClust2 obtained an ARI of 0.9121 and can correctly identify most cells for each cell type. SC3 obtained the best NMI of 0.9921 (Table 4). In the human cerebral cortex scRNA-Seq dataset [70], SC3 had the highest score of ARI, and was followed by tSNE+k-means. SC3, tSNE+k-means and scImpute achieved the best results in terms of NMI. But tSNE+k-means (48.10 secs) was faster than SC3 (53.55 secs) (Table 5). In the human IPF scRNA-Seq dataset [71], SC3 achieved the best performances on both ARI and NMI, which were far better than other methods (Table 6). In the peripheral blood mononuclear cells scRNA-Seq dataset [58], these seven methods obtained better performances. tSNE+k-means obtained the best performances on both ARI and NMI (Table 7). In the 2-cell and 4-cell mouse embryos scRNA-Seq dataset [72], tSNE+k-means obtained the best performances (1.0) on both ARI and NMI. More importantly, CIDR was the fastest on these five scRNA-seq datasets (Table 8). The experimental results from these five dataseets shows that CIDR usually has the least runtime, and SC3 and tSNE+k-means usually have better clustering accuracy.

Table 3. The summary statistics of the five scRNA-seq datasets after preprocessing.

Dataset	Cell types	Cells	Genes
human brain	8	420	21,517
human cerebral cortex	11	300	8,686
human IPF	9	540	56,650
peripheral blood mononuclear cells	3	500	32,738
2-cell and 4-cell mouse embryos	3	49	25,737
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Table 4. The performance comparison of seven methods on the human brain dataset.

Method	ARI	NMI	Runtime
CIDR	0.8977	0.9467	6.95 s
SC3	0.7985	0.9921	1.95 min
tSNE+k-means	0.8408	0.8249	30.35 s
RaceID	0.5029	0.8003	1.47 min
scImpute	0.5541	0.7388	2.60 min
SAFE	0.6498	0.7618	2.40 min
GiniClust2	0.9121	0.9492	39.71s

Table 5. The performance comparison of seven methods on the human cerebral cortex dataset.

Method	ARI	NMI	Runtime
CIDR	0.7374	0.4469	2.43 s
SC3	0.8933	1.0	53.55 s
tSNE+k-means	0.8897	1.0	48.10s
RaceID	0.5649	0.2199	1.32 min
sclmpute	0.7548	1.0	1.40 min
SAFE	0.6689	0.5950	59.97s
GiniClust2	0.5819	0.7754	22.14s

Table 6. The performance comparison of seven methods on the human IPF dataset.

Method	ARI	NMI	Runtime
CIDR	0.2183	0.3917	12.01 s
SC3	0.7096	0.9820	3.51 min
tSNE+k-means	0.1736	0.4591	46.33 s
RaceID	0.1009	0.2852	4.99 min
sclmpute	0.2930	0.7702	13.62 min
SAFE	0.2187	0.4375	4.66 min
GiniClust2	0.4871	0.9370	2.06 min

Table 7. The performance comparison of seven methods on the peripheral blood mononuclear cells dataset.

Method	ARI	NMI	Runtime
CIDR	0.9210	0.9752	8.11 s
SC3	0.8546	0.9446	2.71 mins
tSNE+k-means	0.9884	0.9871	20.83 s
RacelD	0.8386	0.0933	57.77 s
scImpute	0.9826	0.9628	1.88 min
SAFE	0.8920	0.9136	3.27 min
GiniClust2	0.9826	0.9814	29.12 min

Table 8. The performance comparison of seven methods on the 2-cell and 4-cell mouse embryos dataset.

Method	ARI	NMI	Runtime
CIDR	0.8606	0.9114	2.03 s
SC3	0.9483	0.9114	21.90 s
tSNE+k-means	1.0	1.0	2.31 s
RaceID	0.1268	0.9114	13.32 s
sclmpute	1.0	0.9114	54.19 s
SAFE	0.7731	0.6877	24.07 s
GiniClust2	0.9483	0.9114	16.45 s

4. Discussion and further research

Current computational models for clustering scRNA-seq data effectively identified cellular subpopulations, however, they have a number of challenges encapsulated within the seven following categories.

4.1. Lacking gold-standard benchmark datasets

scRNA-seq technologies have rapidly developed, and scRNA-seq clustering techniques have efficiently been able to capture cell subpopulations. However, the lack of gold-standard benchmark datasets severely limits systematic comparisons of performance of various clustering algorithms. Thus, integrating existing experimental data and generating single-cell dataset benchmarks may be a major challenge for advancing single-cell data analysis [10,73,74].

4.2. Identifying a cluster number

Almost all clustering algorithms require a parameter for the number of desired clusters. Indeed, the parameter has important effects on clustering outcomes. Although RaceID [53], SNN-cliq [62], and SC3 [27] provide estimations of cluster numbers, K, these methods have other limitations. RaceID [53] performs poorly when no rare cell types are present, while SNN-cliq [62] and SC3 [27] have high complexity and are not scalable. Consequently, selecting an appropriate cluster parameter is a challenging task.

4.3. Reclustering cell subpopulations

Many algorithms (e.g., RaceID [53] and GiniClust2 [60]) exhibit good performances when clusters are roughly equal in size. Unfortunately, decreased performance in identifying rare cell types occurs when more frequent cell types are clustered. To solve this problem, many solutions have used a divide-and-conquer technique to recluster large cell populations after an initial clustering [75,76,]. However, a critical problem arises with regard to how to determine whether a large cell subpopulation should be reclustered [22].

4.4. Dimension reduction

scRNA-seq dataset components contain abundant cells. While it is feasible to cluster these large datasets, visualizing and interpreting these results remains a challenge. Linear dimensional reduction techniques (e.g., PCA) can not accurately uncover potential associations between cells due to dropout and noise. In contrast, nonlinear dimensional reduction strategies (e.g., t-SNE [52,68,77,,] and UMAP [77]) can produce outcomes that are easier to interpret. However, they incorporate parameters requiring manual adjustment, and this severely affects visualization. Thus, using an appropriate method for choosing parameters to perform dimensional reduction in scRNA-seq clustering is an unsolved problem [22].

4.5. Validation and visualization of clustering results

The validation of scRNA-seq clustering results may be one of the most pressing challenges in analysing these data. The currently optimal validation method is to confirm cell types by other methods like screening cells from different cell lines [70] or during the first stages of embryonic development [78], or by evaluating tissues that are well studied (e.g., peripheral blood mononuclear cells) [58]. These cell types or tissues can serve as useful ground-truthing benchmarks but are, however, unlikely to be complex, and there are also limited tissue examples [22]. In addition, there are numerous analysis tools for identifying gene enrichment analysis tools, but tools to analyse cell type enrichment are scarce. Consequently, exploiting visualization tools to identify cell type enrichments may be a promising area of alternative research.



4.6. Ensemble clustering

Experiments have confirmed that no individual scRNA-seq clustering algorithm can capture true clusters and achieve optimal performance in all situations. For example, SC3 [27], SINCERA [55], and pcaReduce [79] performed better than other models in the dataset investigated in Biase et al. [72]. In contrast, tSNE+k-means and SC3 [27] exhibited more robust performances when analysing the dataset provided by Klein et al. [27,80,]. Ensemble clustering produces several clustering results for a given dataset and identifies final solutions based on the associations observed across the ensemble. The solutions from ensemble clustering are more stable and robust than every individual solution within the ensemble. Consequently, it may be an important area of future research to leverage ensemble clustering to integrate gene expression data from all individual cells and diverse clustering methods given that individual clustering algorithms are less likely to achieve as optimal of performances.

4.7. Personalized medicine

More extensive research into individual cellular dynamics can increase our understanding of the developmental processes and pathogenesis mechanisms of various complex diseases. These findings can then be effectively applied in personalized medicine and contribute to the development of the field. For example, scRNA-seq clustering has been used to identify intra-tumoural heterogeneity [73,81-84] subpopulations and cluster tumour cell [85,86,]. Nevertheless, the application of these methods in adult somatic stem cell research is currently restricted due to limited knowledge about individual stem cells [86-89]. Thus, a significant challenge of the field may be to design novel statistical quantification techniques to detect cell subpopulations and design personalized treatment options for individual patients.

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