REVIEW PAPER

Characterizing the brain's dynamical response from scalp-level neural electrical signals: a review of methodology development

Guang Ouyang¹ \bullet · Changsong Zhou²

Received: 20 July 2020 / Revised: 9 August 2020 / Accepted: 27 August 2020 / Published online: 4 September 2020 - Springer Nature B.V. 2020

Abstract

The brain displays dynamical system behaviors at various levels that are functionally and cognitively relevant. Ample researches have examined how the dynamical properties of brain activity reflect the neural cognitive working mechanisms. A prevalent approach in this field is to extract the trial-averaged brain electrophysiological signals as a representation of the dynamical response of the complex neural system to external stimuli. However, the responses are intrinsically variable in latency from trial to trial. The variability compromises the accuracy of the detected dynamical response pattern based on trial-averaged approach, which may mislead subsequent modelling works. More accurate characterization of the brain's dynamical response incorporating single trial variability information is of profound significance in deepening our understanding of neural cognitive dynamics and brain's working principles. Various methods have been attempted to address the trial-to-trial asynchrony issue in order to achieve an improved representation of the dynamical response. We review the latest development of methodology in this area and the contribution of latency variability-based decomposition and reconstruction of dynamical response to neural cognitive researches.

Keywords Event-related potential · Dynamical brain response · Brain response variability · ERP latency jitter · ERP decomposition

Characterization of the brain's dynamical response and its variability from instance to instance

Characterization of dynamical brain response to stimuli in cognitive tasks forms a cornerstone in neurocognitive research. To examine how this complex dynamical system behaves and how it is associated with function and cognition, neuroscientists usually give the brain a 'kick' (e.g., sensory input) and observe its neural response, like physicists examining the dynamics nature of a pendulum

Department of Physics, Centre for Nonlinear Studies, Institute of Computational and Theoretical Studies, Hong Kong Baptist University, Kowloon Tong, Hong Kong

(Fig. [1b](#page-1-0)). The response is not merely an increase or decrease of activity strength in some kind, but displays a rich structure of dynamical system response pattern at the time scale of millisecond, which can be used to infer the underlying architecture and configuration of dynamical neural system at various levels (Deco et al. [2008;](#page-9-0) Graben et al. [2008](#page-9-0); Kiebel et al. [2006,](#page-9-0) [2008\)](#page-9-0). Electroencephalography (EEG) technology provides a non-invasive means to measure such dynamical neural responses with sufficiently high temporal resolution. Since EEG signal contains a large amount of spontaneous background activity, the pattern of the response activity to the 'kick', also known as eventrelated potential (ERP), becomes visible only after averaging multiple trials, which cancels out the strong spontaneous activity (Fig. [1c](#page-1-0)). ERP waveform (Fig. [1c](#page-1-0)), typically showing a delicate response pattern of dynamic oscillators, has engendered a large amount of research on brain-behavior relationships (dating back to the 1930s (Davis [1939\)](#page-9-0)). At scalp level, the average ERP approach has hitherto remained the main approach to obtaining the dynamical response pattern with sufficient temporal

 \boxtimes Guang Ouyang ouyangg@hku.hk

 \boxtimes Changsong Zhou cszhou@hkbu.edu.hk

¹ Faculty of Education, The University of Hong Kong, Pokfulam, Hong Kong Island, Hong Kong

Fig. 1 EEG as a tool to characterize the brain's dynamical response. a A typical EEG experiment paradigm in which discrete events are presented to the subject to elicit brain response while EEG signal is being recorded continuously. b Eliciting brain response by stimulus can be analogized to hitting a pendulum and observing its dynamic response. c The average ERP method assumes that a specific response activity is evoked by stimulus and is added to the spontaneous activity. By averaging a number of trials aligned to stimulus onsets the spontaneous activity will be cancelled out and the evoked

resolution, and it has been demonstrated to be a powerful tool for investigating the neural dynamics-cognition relationships. Manipulations of cognitive processes (e.g., to perform fast or to perform accurate) or stimulus properties (e.g., luminance) can specifically alter an ERP peak or trough in a temporally fine-grained manner, showing a fascinating psychophysical phenomenon (Tobimatsu and Celesia [2006](#page-11-0)). Such a trial-averaged ERP approach has given birth to fruitful research outcomes with respect to the neural mechanisms of perception, emotion, memory, language, and various other cognitive processes.

Trial-averaging appears to be a powerful approach to characterizing the dynamical responses to external stimuli. However, the averaged waveform is not an accurate representation of the dynamical responses due to brain response variability (Fig. 1c). Unlike a pendulum, the brain

response will remain. However, due to the trial-to-trial variability of brain response (represented by shifting blue peaks), the average ERP may end up showing a blurred version of the response pattern (bottom). d Real EEG data showing that there are different subcomponents in the single trial ERPs with differential latency variabilities. The data are single trials ERP sorted by P3 latencies from electrode CPz of a single subject from a face recognition task (Rellecke et al. [2012](#page-10-0)) This figure is taken from Ouyang [\(2020](#page-10-0)). Permission has been obtained

is an active dynamical system that responds variably to the same 'kick'. This variability may stem from neural functional mechanisms (e.g., adaptation and learning (Brooks et al. [2015](#page-9-0); Collins and Frank [2018;](#page-9-0) Dhawale et al. [2017](#page-9-0)), from dynamical nature of multilevel neural working (Mendonca et al. [2016](#page-10-0)), or simply from noise (Faisal et al. [2008](#page-9-0)). This renders the trial-averaged ERP inaccurate in describing brain response due to the blurring effect, as explained in Fig. 1c. In the worst case, the inaccuracy could lead to misleading conclusion in neurocognitive research (Ouyang et al. [2016;](#page-10-0) Stokes and Spaak [2016](#page-11-0)). From the dynamical system point of view, the distorted representation of system response will also render all the inferences of system architecture and configurations questionable (Kashyap et al. [2019](#page-9-0)).

Strictly speaking, the brain's dynamical response pattern only genuinely unfolds in a single trial. It is thus important to characterize the response pattern at single trial level. However, this endeavor is greatly hindered by a fundamental challenge—how can a genuine response activity be differentiated from the overlapping, spontaneous, selfsustaining activity in a single trial? In fact, the spontaneous activity—the activity that reflects the sustained neural dynamics in functional operation—occupies the major power in a single trial brain EEG (Cole and Voytek [2017\)](#page-9-0), even after the artifactual signals are removed. This overwhelmmingly dominant ongoing activity makes it difficult to identify the exact pattern of an externally elicited response. These inherent neural data features create a "single trial vs. average" dilemma in the characterization of dynamical brain responses using EEG technology in cognitive neuroscience research: In a single trial, the dynamical response pattern is genuinely preserved but is mixed with strong spontaneous activity; In the average ERP, the spontaneous activity are effectively canceled out but the dynamical response pattern are distorted by the trial-to-trial variability. Advanced signal processing technology and a theoretical framework for addressing this dilemma are therefore needed in view of the importance of knowing what the dynamical response really looks like in a single trial for a deeper understanding of various neural cognitive mechanisms.

No two brain responses are the same. The brain's fundamental ability of adapting to the environment and thriving lies in its flexibility and malleability of its internal system and behaviors. Therefore, being variable is one of the defining features of the brain dynamical systems. It has been proposed by many dynamical system researchers that the brain system lies in a critical state that balances reliability and variability in which various functions are best achieved and maintained (Cocchi et al. [2017](#page-9-0); Wang et al. [2016,](#page-11-0) [2019](#page-11-0)). As such, the variability information of brain dynamical response provides another key channel to investigating the core mechanisms, aside from the pattern of the dynamical response per se. Various neurophysiological factors can contribute to response variability. The key question is, to what extent is cognitive behavior variability reflected in single trials ERP?

A clear answer to this question is the first step that stimulates and illuminates further development of single trial ERP-based characterization of brain dynamical responses. Reliably obtaining the variability information of the brain dynamical response remained a challenging topic for a long time, again, due to the strong spontaneous EEG activity that hampers its reliable estimation. Nevertheless, statistically, the relationship between trial-to-trial variability of brain response (e.g., amplitude, latency, oscillatory power) and various external covariates (e.g., response speed, correctness, reward signal) has been extensively confirmed (Bridwell et al. [2018](#page-9-0)). In fact, numerous recent findings have revealed a strikingly close relationship between single trial ERP variability and complex real time cognitive processes ranging from memory/evidence-based decision making (Loughnane et al. [2016](#page-10-0); Ratcliff et al. [2016](#page-10-0)) to real time dynamics of expectation, feedback processing, and cognitive control in the dynamic reinforcement learning process (Collins and Frank [2018;](#page-9-0) Frank et al. [2015](#page-9-0)). These concrete findings have firmly pointed out that the high temporal resolution, non-invasive technology of EEG is able to reveal rich information associated with complex cognitive variability from trial to trial. However, confirming the functional relevance of the trialto-trial variability is still substantially different from precisely characterizing the variability pattern. The latter is more important for informing and validating dynamical modelling studies. For example, knowing the significant correlation between single trial neural response strength and reaction times does not mean knowing the distribution pattern of the neural response strength across trials (which can be Gaussian, ex-Gaussian, or Poisson) because the samples may be too few or amount of noise may be too strong to reliably infer the distribution patterns. Such distribution patterns are crucially important as they reflect the properties of the underlying model that generates the responses.

Characterizing the trial-to-trial variability of brain response as revealed by ERP has been an increasingly trendy research in recent years. The two major aspects of variability information are amplitude and latencies, which have both been shown to be highly variable (Ouyang et al. [2015](#page-10-0)), also see Fig. [1](#page-1-0)d). The variability of the morphology of the entire response pattern of spatiotemporal features across trials has been less attended, which we also believe to be an important aspect to look into. Regarding the more detailed feature of the variability pattern, it has been shown that the early ERP components, such as P1, N1, P2, that reflect the early stages of low level perception, appear to be less variable, whereas the late components, such as P3, N400, P600, that reflect high-level cognitive processes, appear to be highly variable (Ouyang et al. [2015](#page-10-0); Wang et al. [2015](#page-11-0)). The variability is ubiquitous in all task paradigms (Ouyang et al. [2017](#page-10-0)). Ample evidence of cognitive relevance of the variability in single-trial ERPs has been reported in the ERP literature (Arazi et al. [2017](#page-9-0); Loughnane et al. [2016](#page-10-0); Pisauro et al. [2017;](#page-10-0) Stefanics et al. [2018](#page-10-0)). This further suggests a need to shift from the conventional trial-averaging approach to more advanced approaches of characterizing dynamical responses after explicitly addressing the latency asynchrony issue. The major reasons for this shift are: (1) an average pattern mis-represents the dynamical responses in single trials (Fig. [1\)](#page-1-0). And such misrepresentation of neural response patterns could mislead researchers' understanding of neural working mechanisms (Stokes and Spaak [2016](#page-11-0)) and behavioral effects on neural system (Ouyang et al. [2016](#page-10-0)), and many other aspects such as precise timing, subtle effects, and intricate dynamics. (2) Rich information about the dynamics of neurocognitive and functional processes is only accessible in single trials.

Significance of addressing the issue of trialto-trial variability in brain response

According to the issues related to trial-to-trial brain response variability that we elaborated above, we argue that addressing them will have profound benefits in many domains in neural cognitive research. (1) Obtaining a more accurate pattern of dynamical response by compensating the variability effect will provide important information for inferring the dynamical and functional mechanisms of neural systems. (2) Obtaining a more accurate response pattern is beneficial to better characterization of trial-totrial variability, as the rectified pattern can serve as a better template. The trial-to-trial variability is also an important feature dimension of the dynamical system response. (3) The improved dynamical response pattern and trial-to-trial variability information provide new channels for studying the brain-cognition relationships, cross-sectional differences, and individual differences from the dynamical system's perspective. Below we provide an overview of the development of methods that are oriented to study more precise representation of brain's dynamical response pattern and its variability measured by the tool of ERP.

Current state of methodology

The pursuing of a more accurate characterization of brain's dynamical response beyond simple averaging has a long history and is still advancing. Since a time marker-locked average ERP is a blurred version of the dynamical response, de-blurring is a major approach to restore the response pattern. The earliest relevant attempt in this line dates back to half a century ago (Woody [1967\)](#page-11-0). Woody pioneered the method of identifying the single trial latencies of ERP components and re-synchronizing single trials according to the estimated latencies with the aim of obtaining a 'rectified' ERP, thus better representing the dynamical response pattern. Since then, various methods and approaches have been attempted. In the following, we summarized the developments in this area including the latest ones.

Averaging after resynchronization

Resynchronization is the core procedure for dealing with the asynchrony problem. A coarse approach is to identify the single trial latencies of ERP and re-synchronize single trials to the identified latencies instead of to stimulus onsets and obtain a new ERP (Patterson et al. [2000](#page-10-0); Pomalazaraez and Mcgillem [1986;](#page-10-0) Woody [1967\)](#page-11-0). This approach can adjust large ERP components such as P3 (Kutas et al. [1977](#page-10-0); Patterson et al. [2000;](#page-10-0) Pomalazaraez and Mcgillem [1986](#page-10-0); Spencer et al. [2000](#page-10-0)). However, resynchronizing single trials to the latencies of a late ERP component is as problematic as stimulus-locked averaging, because an ERP is not simply a homogeneous ensemble temporally locked to a single time event (Fig. [1](#page-1-0)c). For instance, a reaction time (RT)-locked average ERP will simply blur stimulus-locked portions (Berchicci et al. [2016\)](#page-9-0). The multi-compositional nature of ERP makes simple resynchronization of single trials to one component's latency an ineffective approach to improving the detection of dynamical response pattern. To address this issue, methods that decompose ERP into multiple components with differential trial-to-trial variability had been developed.

Time marker-based ERP decomposition

Neural cognitive processes are functionally modular—they can be divided into, for example, perception, central cognition, and response/execution (Hurley [2001\)](#page-9-0). Neural activations associated with different sub-processes have different degrees of trial-to-trial variability. They may be locked to stimulus onset, response, or neither-nor ((Ribeiro et al. [2016;](#page-10-0) Schiff et al. [2014;](#page-10-0) Verleger et al. [2014](#page-11-0)), or refer to illustration in Fig. [2](#page-4-0)), meaning that resynchronization could be and should be done separately on different subcomponents. One straightforward idea is to decompose these several component clusters with different latency variabilities and resynchronize them separately (Fig. [2](#page-4-0)). The earliest attempt at such decomposition was simply to separate an ERP into a stimulus-locked component cluster and a response-locked component cluster based on markers of stimulus onsets and reaction times, which can be done with mathematical derivation (Bardy et al. [2014;](#page-9-0) Dandekar et al. [2012](#page-9-0); Hansen [1983;](#page-9-0) Smith and Kutas [2015a](#page-10-0), [b](#page-10-0); Takeda et al. [2008;](#page-11-0) Yin et al. [2009;](#page-11-0) J. Zhang [1998\)](#page-11-0). In essence, these time marker-based decomposition methods all share the same mathematical core: a general linear model (GLM) in which the time markers serve as the regressors (independent variables), the raw EEG data serve as the dependent variables, and the waveform associated with each regressor is the coefficient vector to be solved in

Fig. 2 Illustration of ERP decomposition and reconstruction. It is assumed that there are three component clusters in single trials ERPs: stimulus-locked cluster (blue), central cluster (red), and response time-locked cluster (green). To obtain a better representation of the

the GLM framework. The mathematical derivation for the component decomposition can be summarized below.

Assuming two activation components co-existing in every single trial, temporally locked to different events, the EEG trace can be described as:

$$
EEG(t) = \sum_{\tau=1}^{T_1} C_1(\tau)X_1(t-\tau) + \sum_{\tau=1}^{T_2} C_2(\tau)X_2(t-\tau) + \varepsilon.
$$
\n(1)

where C is the component waveform function and X is timing functions coding the time markers of the components with value one (e.g., stimulus onsets or response times) and others zero. T_1 and T_2 indicate the duration of components and ε is the noise term. In reality, more than two components locked to different time events can be modeled and (1) can be simply extended to such cases. Equation (1) can be written in a matrix form:

$$
EEG = X \cdot C + \varepsilon. \tag{2}
$$

With the information of the time markers X, the least square error-based solution of the components can be expressed as Eq. (3) below (Dandekar et al. [2012](#page-9-0)), which serves as the solution for the decomposed components:

$$
C = (XtX)-1 \cdot Xt \cdot EEG.
$$
 (3)

One obvious limitation of this approach is that it requires RT to be included in the experiment, a requirement which many experiments with covert responses (e.g., internal counting) cannot fulfill. Even in the ERP data with both stimulus onsets and RT markers (or other markers), an issue may arise as to whether RT precisely represents the latency of the late latency-variable ERP components. The

brain response pattern at a single trial, the three clusters need to be decomposed (middle panel) and separately re-synchronized (right panel). (Color figure online). Figure was adapted from Ouyang et al. ([2016\)](#page-10-0). Permission has been obtained

second limitation, which is much subtler and less widely known, is a noise amplification issue (Ouyang et al. [2015](#page-10-0)). Specifically, when two sets of markers (e.g., stimulus and RT) have very small inter-marker jitter across trials, the mathematical solution of the two marker-locked components are two complementary waveforms (with large amplitude) that are clearly not biologically plausible. This is due to the close-to-singularity of the covariance matrix of the two regressors (Ouyang et al. [2015](#page-10-0)). Similar issues exist in dipole source localization when different dipole sources have a high spatial correlation, in which case the source temporal activity will have complementary patterns resembling amplification of noise (Wolters et al. [1999\)](#page-11-0). A solution to this issue that is both practically and theoretically sound has yet to be found. From practical perspective, a common solution is introducing regularization, the configuration of which is however usually dependent on specific circumstances.

ERP decomposition without time marker

Motivated by the potential issue that the external time markers may not precisely represent an underlying component's latency, and are often not available, researchers have proposed several methods to decompose ERP without fully relying on time markers (Ouyang et al. [2015;](#page-10-0) Takeda et al. [2010;](#page-11-0) Truccolo et al. [2003;](#page-11-0) Wu et al. [2014](#page-11-0)). The basic approach is to estimate the latencies of the components whose single trial latencies are not or inaccurately represented by external time markers, thus creating 'time markers' that are to be fed into the time marker-based ERP decomposition methods. For instance, recognition of a word during sentence comprehension elicits functionally

differentiable processes such as low-level visual, semantic and syntactic processes, which are presumably variable in latency that is difficult to measure externally. N400 and P600 are two neural activations associated with subprocesses of language processing. Wang et al. ([2015\)](#page-11-0) attempted to estimate single trial latencies of these two components and separate them (F. Wang et al. [2015](#page-11-0)) based on the assumption that the two components have differential trial-to-trial latency variability. The decomposition using the estimated latencies was similar to the markerbased decomposition whereby each type of marker is coupled with a specific component, but is based on a more robust iterative scheme (Wang et al. 2015). The work thus demonstrated that the precision of single trial latency estimation sufficed for the decomposition. However, these non-time marker-based methods still inherit the limitation of marker-based methods as described above (e.g., noise amplification), with an additional limitation resulting from the inaccuracy in the single trial latency estimation.

General issues and challenges

Although the distortion issue in using trial-averaged ERP to represent the dynamical response is widely known (Jung et al. [2001;](#page-9-0) Kutas et al. [1977;](#page-10-0) Makeig and Onton [2011](#page-10-0); Ouyang [2020](#page-10-0); Ouyang et al. [2017](#page-10-0); Sassenhagen and Bornkessel-Schlesewsky [2015](#page-10-0); Saville et al. [2015;](#page-10-0) Walhovd et al. [2008\)](#page-11-0), there is still not a commonly accepted solution that has come into play in the community. Researchers are still mainly using trial-averaged ERP as a representation of the brain dynamical response. A sound framework for improving the representation of the dynamical response is strongly needed. Nevertheless, recent development has seen some promising methods emerged. In the following, we continue to summarize some recent methodological developments that have attempted to address these issues.

Reconstruction of a more accurate representation of the dynamical response

With the advancement of signal processing techniques and theoretical modelling, a substitute for trial-averaged ERPs should be sought to more accurately characterize the dynamical neural response at the single trial level. Obtaining this substitute certainly needs to (1) incorporate trial-to-trial variability information and (2) differentially treat the sub-components with different variability features. A new framework was recently proposed by Ouyang et al. [\(2016](#page-10-0), 2020) that was designed to obtain such a substitute. The procedure, called ERP reconstruction, comprises the following steps: (1) decomposing an ERP into different

subcomponents with different variability; (2) obtaining the latencies of each subcomponent at single trial level; (3) separately re-synchronizing each subcomponent according to their own single trial latencies (either estimated or prescribed) in the temporal axis with respect to stimulus onset (Fig. [2\)](#page-4-0). The moving of each single trials is referred to the median latency of all trials, i.e., trials with latencies smaller than the median should move rightward, vice visa; and (4) summing up the re-synchronized subcomponents and obtaining an ERP that has been adjusted for the blurring effect. The procedure is illustrated in Fig. [2.](#page-4-0) In principle, the reconstructed ERP is a more precise reorientation of the dynamical response pattern occurs at single trial level. Comparatively, the stimulus-locked averaged version misrepresents the pattern, as the blurred portion (Figs. [1](#page-1-0) and [2\)](#page-4-0) does not actually occur in a single trial. The reconstruction effect in a real EEG dataset is shown in Fig. 3.

Recovering the internal dynamics of neural cognitive sub-processes

Although ERP reconstruction can, in principle, provide a more accurate representation of the dynamical response, it still possesses an inherent limitation that the reconstructed ERP still represents a mixture of different neural cognitive sub-processes, each one of which may have unique dynamical features and functional signatures. An illustration of this issue has been shown in several previous studies (Ouyang et al. [2013;](#page-10-0) Sturmer et al. [2013](#page-11-0); Verleger et al. [2014\)](#page-11-0). The brain response to an external input is functionally modular—it can be divided into different stages such as sensation, central evaluation and response action. Different stages possess a uniquely rich structure of

Fig. 3 Comparison of a standard averaged ERP (left) and a reconstructed ERP (right) Figure was adapted from Ouyang et al. [\(2015](#page-10-0)). Permission has been obtained

dynamical activation pattern of their own (Ouyang et al. [2015\)](#page-10-0). Moreover, different stages have different degree of variability, which accumulatively contribute to behavioral variability (Ouyang et al. [2015\)](#page-10-0). Both standard ERP and reconstructed ERP are a summed representation of different subprocesses. Beside the fact that they cannot provide detailed dynamics pattern of sub-processes, the summed ERP may also provide ambiguous neural effects (Ouyang et al. [2013](#page-10-0)). How these different sub-processes are mapped to the ERP sub-components, how their dynamics and variability are reflected and to what extent they can be extracted from single trial data are important questions in cognitive neurodynamics research. This query requires further decomposition of ERP sub-components at a finergrained level of cognitive sub-processes that generate neural activations overlapping with each other, which further requires tackling of several theoretical and methodological complexity in investigating separate components, such as (1) What should be the number of subcomponents supported by a sound theoretical basis? (2) How to validate the decomposition? (3) What could be the additional complexity issue brought by the decomposition methods?

Oriented to addressing these frontier issues, the recent development of trial-to-trial variability-based ERP analysis methodology has demonstrated that the brain dynamical response pattern and its variability at the level of differential sub-processes can be reliably accessed with a sophisticated signal processing method. Figure [4](#page-7-0) presents the results derived by a recent methodological framework Residue Iteration Decomposition (RIDE, (Ouyang et al. [2015\)](#page-10-0)). RIDE assumes ERPs to be composed of different internal sub-components with differential latency variability. A unique aspect of this framework is that the decomposition and extraction of the sub-components are based on the information of single trial latency variability (Ouyang et al. [2015\)](#page-10-0). Figure [4](#page-7-0) shows that the RIDE framework decomposes the ERP into stimulus-locked component cluster S, central component cluster C and RTlocked component cluster R. The novel scenario provided by this framework is that each component cluster displays a distinct dynamical activation pattern and clearly differential single trial variability that are otherwise hidden and mixed in the conventional average ERP and reconstructed ERP. In order to deal with theoretical issues such as noise amplification, the RIDE methodology incorporated sophisticated signal processing procedures including L1 norm minimization-based iteration and strict time-window specifications, which bears a high degree of complexity in this framework (Ouyang et al. [2015\)](#page-10-0). Nevertheless, the analysis scenario of dissociating overlapping ERP subcomponents points to an appealing direction of characterizing brain dynamical responses at a finer-grained level of

cognitive sub-processes. Since this decomposition framework is relatively new, much more systematic evaluation and validations need to be conducted to further establish its utility in neural cognitive research. One major aspect of evaluation is its sensitivity to parameters in EEG pre-processing and in the method itself. For example, choice of referencing method (Dong et al. [2017;](#page-9-0) Yao [2001\)](#page-11-0), filtering method, and artifact rejection procedures can substantially affect the obtained ERP, which will in turn affect the decomposed or reconstructed ERP. Optimizing the parameters for the new methodologies to best investigate the internal dynamics and variability of neural sub-processes would be an important direction to develop.

Contribution of latency variability-based ERP decomposition and reconstruction to neural cognitive research

Studying the ERP sub-components provides access to the structures of neural cognitive dynamics associated with different sensory and cognitive stages that are otherwise inter-mixed, distorted, or hidden in the average waveform. Therefore, tackling the sub-components in the average ERP waveform is crucial for the future development in neural cognitive researches, especially regarding the neural dynamical system. Recent applications of ERP decomposition and reconstruction methods have demonstrated the benefits in this regard. A brief summary is provided below.

The benefits of applying the above-mentioned methods for improving the brain dynamical response pattern and for extracting the internal dynamics and trial-to-trial variabilities of sub-processes can be categorized into the following three areas: (1) Restoring the true neural effects associated with external factors that are otherwise attenuated and covered in the standard ERP due to the latency variabilityinduced distortion; (2) Pin-pointing the neural effects in a specific sub-process from the entire cognitive process of perceiving, evaluating, and responding to a stimulus; (3) examining the functional signature of trial-to-trial variability of neural cognitive sub-processes.

A detailed demonstration of the application in the first area has been provided in Ouyang et al. [2016](#page-10-0). Applications in this area, specifically, restoring true neural effects blurred by latency jitter, have covered many different cognitive constructs and topics including episodic memory effect (Murray et al. [2019](#page-10-0)), novelty processing effect (Warren et al. [2020\)](#page-11-0), cognitive flexibility (Kopp et al. [2020](#page-10-0)), language processing (Fjaellingsdal et al. [2020\)](#page-9-0), and reliability of ERP components (Martin-Loeches et al. [2017](#page-10-0)). These applications indirectly reflect the ubiquity of the latency variability across a broad range of cognitive paradigms. For the second application area, ample

Fig. 4 Dynamical pattern and trial-to-trial variability of overlapping ERP sub-components. The RIDE method decomposes ERP data into different temporally overlapping sub-component clusters with different features of single trial variability. The framework reveals that some sub-components are stimulus-locked, some are RT-locked and some are in-between, and they can be separated. The separation reveals richer neural dynamical activity pattern that are otherwise

mixed and hidden in the stimulus-locked average ERP. The consistency of the separation scenario has been demonstrated elsewhere (Ouyang et al. [2015](#page-10-0)). Data are from a single subject performing a face recognition task. The time zero indicates the presentation time of the facial stimulus. Vertical black line: stimulus onset. Black curve: RT. The single trials data were normalized in amplitude and filtered under 40 Hz

applications of RIDE decomposition algorithms in recent years have shown that the decomposition of ERP into different sub-components revealed richer internal

structures and mechanisms regarding the modular cognitive stages. Selected examples include differentiating neural activities associated with early, direct perceptual

response and with late, indirect, top-down controlled response in executive function tasks (Sturmer et al. [2013](#page-11-0)), investigating the cognitive transitioning and binding processes (Opitz et al. [2020](#page-10-0); Takacs et al. [2020\)](#page-11-0), pinpointing the specific neural cognitive processes that are affected by external manipulations (Peng et al. [2020;](#page-10-0) Steinemann et al. [2018\)](#page-11-0), or by various brain disorders, aging, or different drugs (Bluschke et al. [2020](#page-9-0); Giller and Beste [2019](#page-9-0); Kleimaker et al. [2020;](#page-9-0) Muckschel et al. [2020;](#page-10-0) Wolff et al. [2019\)](#page-11-0), differentiating neural activates of different cognitive stages in various other tasks (Valt et al. [2020\)](#page-11-0). In addition to the research area, the benefits of improved brain response characterization by overcoming the latency variability issue are, in principle, applicable in clinical area, which has been explored as well (De Venuto et al. [2018](#page-9-0)). As for the third application area, the functional signature of trial-to-trial variability, one study has shown that the crosstrial variability of brain response in individuals estimated by RIDE was modulated by COMT genotype (Rostami et al. [2017\)](#page-10-0). Furthermore, individual difference regarding the correlation between neural variables of and cognitive abilities has also been shown to be better revealed in specific sub-components of brain response extracted by RIDE (Meyer et al. [2019](#page-10-0)), which showed that the extracted neural characteristics are further associated with intersubject variability. While a considerable number of applications in recent years have demonstrated the contribution of the new methodologies in neural cognitive research, many questions still remain open. In Fig. 5 we summarized the contributions as elaborated above and some outstanding remaining questions in this field.

Concluding remarks

In this review article, we have provided an overview of the long-standing latency asynchrony issue in brain research that has been based on trial-averaged ERPs as a tool for depicting the brain's dynamical responses, and the latest developments in methodology in addressing the limitations of trial-averaging approach. It is worth to note that the latency asynchrony issue is by no means a negligible technical limitation compromising data fidelity. Instead, it distorts neural representations in terms of (but not confined to) timing (Miller et al. [2009](#page-10-0)), behavioral effect (Zhang et al. [2015](#page-11-0)), functional role (Bodmer et al. [2018\)](#page-9-0), and anatomical feature (Yang et al. [2017\)](#page-11-0). With the advancement in signal processing techniques and theoretical modelling, the limitations that latency asynchrony imposes on brain response characterization are being progressively

addressed. A more detailed characterization of dynamical response concerning single trial variability and the dynamics of sub-components that are mixed in the compound of average ERPs has started to show advantages in neural cognitive research. We have presented the latest methodological development that can be used for either remedying the standard ERP with comparable simplicity or accessing the richer structure of ERP sub-components and single trial variabilities. These latest developments point to a future trend of exploring the rich patterns of complex neural dynamics associated with cognition.

Acknowledgements This work was partially supported by the Hong Kong Research Grant Council (ECS 27603818) and the Seed Fund for Basic Research from the University of Hong Kong (Nos. 201804159003, 201811159032) to G.O., and by the Hong Kong Baptist University Research Committee Interdisciplinary Research Matching Scheme (IRMS/16-17/04) to C.S.Z.

References

- Arazi A, Gonen-Yaacovi G, Dinstein I (2017) The magnitude of trialby-trial neural variability is reproducible over time and across tasks in humans. Eneuro. [https://doi.org/10.1523/eneuro.0292-](https://doi.org/10.1523/eneuro.0292-17.2017) [17.2017](https://doi.org/10.1523/eneuro.0292-17.2017)
- Bardy F, Van Dun B, Dillon H, Cowan R (2014) Least-squares (LS) deconvolution of a series of overlapping cortical auditory evoked potentials: a simulation and experimental study. J Neural Eng. <https://doi.org/10.1088/1741-2560/11/4/046016>
- Berchicci M, Spinelli D, Di Russo F (2016) New insights into old waves. Matching stimulus- and response-locked ERPs on the same time-window. Biol Psychol 117:202–215. [https://doi.org/](https://doi.org/10.1016/j.biopsycho.2016.04.007) [10.1016/j.biopsycho.2016.04.007](https://doi.org/10.1016/j.biopsycho.2016.04.007)
- Bluschke A, Muckschel M, Roessner V, Beste C (2020) Intact stimulus-response conflict processing in ADHD-multilevel evidence and theoretical implications. J Clin Med. [https://doi.org/](https://doi.org/10.3390/jcm9010234) [10.3390/jcm9010234](https://doi.org/10.3390/jcm9010234)
- Bodmer B, Muckschel M, Roessner V, Beste C (2018) Neurophysiological variability masks differences in functional neuroanatomical networks and their effectiveness to modulate response inhibition between children and adults. Brain Struct Funct 223(4):1797–1810. [https://doi.org/10.1007/s00429-017-](https://doi.org/10.1007/s00429-017-1589-6) [1589-6](https://doi.org/10.1007/s00429-017-1589-6)
- Bridwell DA, Cavanagh JF, Collins AGE, Nunez MD, Srinivasan R, Stober S, Calhoun VD (2018) Moving beyond ERP components: a selective review of approaches to integrate EEG and behavior. Front Hum Neurosci. <https://doi.org/10.3389/fnhum.2018.00106>
- Brooks JX, Carriot J, Cullen KE (2015) Learning to expect the unexpected: rapid updating in primate cerebellum during voluntary self-motion. Nat Neurosci 18(9):1310. [https://doi.org/10.](https://doi.org/10.1038/nn.4077) [1038/nn.4077](https://doi.org/10.1038/nn.4077)
- Cocchi L, Gollo LL, Zalesky A, Breakspear M (2017) Criticality in the brain: a synthesis of neurobiology, models and cognition. Prog Neurobiol 158:132–152. [https://doi.org/10.1016/j.pneuro](https://doi.org/10.1016/j.pneurobio.2017.07.002) [bio.2017.07.002](https://doi.org/10.1016/j.pneurobio.2017.07.002)
- Cole SR, Voytek B (2017) Brain oscillations and the importance of waveform shape. Trends Cognit Sci 21(2):137-149. [https://doi.](https://doi.org/10.1016/j.tics.2016.12.008) [org/10.1016/j.tics.2016.12.008](https://doi.org/10.1016/j.tics.2016.12.008)
- Collins AGE, Frank MJ (2018) Within- and across-trial dynamics of human EEG reveal cooperative interplay between reinforcement

learning and working memory. Proc Natl Acad Sci USA 115(10):2502–2507. <https://doi.org/10.1073/pnas.1720963115>

- Dandekar S, Privitera C, Carney T, Klein SA (2012) Neural saccadic response estimation during natural viewing. J Neurophysiol 107(6):1776–1790. <https://doi.org/10.1152/jn.00237.2011>
- Davis PA (1939) Effects of acoustic stimuli on the waking human brain. J Neurophysiol 2(6):494–499
- De Venuto D, Annese VF, Mezzina G, Scioscia F, Ruta M, Di Sciascio E, Vincentelli AS (2018) A mobile health system for neurocognitive impairment evaluation based on P300 detection. ACM Trans Cyber Phys Syst. <https://doi.org/10.1145/3140236>
- Deco G, Jirsa VK, Robinson PA, Breakspear M, Friston KJ (2008) The dynamic brain: from spiking neurons to neural masses and cortical fields. PLoS Comput Biol. [https://doi.org/10.1371/](https://doi.org/10.1371/journal.pcbi.1000092) [journal.pcbi.1000092](https://doi.org/10.1371/journal.pcbi.1000092)
- Dhawale AK, Smith MA, Olveczky BP (2017) The role of variability in motor learning. Annu Rev Neurosci 40:479–498. [https://doi.](https://doi.org/10.1146/annurev-neuro-072116-031548) [org/10.1146/annurev-neuro-072116-031548](https://doi.org/10.1146/annurev-neuro-072116-031548)
- Dong L, Li FL, Liu Q, Wen X, Lai YX, Xu P, Yao DZ (2017) MATLAB toolboxes for reference electrode standardization technique (REST) of scalp EEG. Front Neurosci. [https://doi.org/](https://doi.org/10.3389/fnins.2017.00601) [10.3389/fnins.2017.00601](https://doi.org/10.3389/fnins.2017.00601)
- Faisal AA, Selen LPJ, Wolpert DM (2008) Noise in the nervous system. Nat Rev Neurosci 9(4):292–303. [https://doi.org/10.1038/](https://doi.org/10.1038/nrn2258) [nrn2258](https://doi.org/10.1038/nrn2258)
- Fjaellingsdal TG, Schwenke D, Ruigendijk E, Scherbaum S, Bleichner MG (2020) Studying brain activity during word-by-word interactions using wireless EEG. PLoS ONE 15(3):e0230280. <https://doi.org/10.1371/journal.pone.0230280>
- Frank MJ, Gagne C, Nyhus E, Masters S, Wiecki TV, Cavanagh JF, Badre D (2015) fMRI and EEG predictors of dynamic decision parameters during human reinforcement learning. J Neurosci 35(2):485–494. <https://doi.org/10.1523/jneurosci.2036-14.2015>
- Giller F, Beste C (2019) Effects of aging on sequential cognitive flexibility are associated with fronto-parietal processing deficits. Brain Struct Funct 224(7):2343–2355. [https://doi.org/10.1007/](https://doi.org/10.1007/s00429-019-01910-z) [s00429-019-01910-z](https://doi.org/10.1007/s00429-019-01910-z)
- Graben PB, Gerth S, Vasishth S (2008) Towards dynamical system models of language-related brain potentials. Cogn Neurodyn 2(3):229–255. <https://doi.org/10.1007/s11571-008-9041-5>
- Hansen JC (1983) Separation of overlapping waveforms having known temporal distributions. J Neurosci Methods 9(2):127–139. [https://doi.org/10.1016/0165-0270\(83\)90126-7](https://doi.org/10.1016/0165-0270(83)90126-7)
- Hurley S (2001) Perception and action: alternative views. Synthese 129(1):3–40. <https://doi.org/10.1023/a:1012643006930>
- Jung TP, Makeig S, Westerfield M, Townsend J, Courchesne E, Sejnowski TJ (2001) Analysis and visualization of single-trial event-related potentials. Hum Brain Mapp 14(3):166–185. <https://doi.org/10.1002/hbm.1050>
- Kashyap R, Bhattacharjee S, Sommer W, Zhou CS (2019) Repetition priming effects for famous faces through dynamic causal modelling of latency-corrected event-related brain potentials. Eur J Neurosci 49(10):1330–1347. [https://doi.org/10.1111/ejn.](https://doi.org/10.1111/ejn.14303) [14303](https://doi.org/10.1111/ejn.14303)
- Kiebel SJ, David O, Friston KJ (2006) Dynamic causal modelling of evoked responses in EEG/MEG with lead field parameterization. Neuroimage 30(4):1273–1284. [https://doi.org/10.1016/j.neuro](https://doi.org/10.1016/j.neuroimage.2005.12.055) [image.2005.12.055](https://doi.org/10.1016/j.neuroimage.2005.12.055)
- Kiebel SJ, Garrido MI, Moran RJ, Friston KJ (2008) Dynamic causal modelling for EEG and MEG. Cogn Neurodyn 2(2):121–136. <https://doi.org/10.1007/s11571-008-9038-0>
- Kleimaker M, Takacs A, Conte G, Onken R, Verrel J, Baumer T et al (2020) Increased perception-action binding in Tourette syndrome. Brain 143:1934–1945. [https://doi.org/10.1093/brain/](https://doi.org/10.1093/brain/awaa111) [awaa111](https://doi.org/10.1093/brain/awaa111)
- Kopp B, Steinke A, Visalli A (2020) Cognitive flexibility and N2/P3 event-related brain potentials. Sci Rep 10(1):9859. [https://doi.](https://doi.org/10.1038/s41598-020-66781-5) [org/10.1038/s41598-020-66781-5](https://doi.org/10.1038/s41598-020-66781-5)
- Kutas M, Mccarthy G, Donchin E (1977) Augmenting mental chronometry: P300 as a measure of stimulus evaluation time. Science 197(4305):792–795. [https://doi.org/10.1126/science.](https://doi.org/10.1126/science.887923) [887923](https://doi.org/10.1126/science.887923)
- Loughnane GM, Newman DP, Bellgrove MA, Lalor EC, Kelly SP, O'Connell RG (2016) Target selection signals influence perceptual decisions by modulating the onset and rate of evidence accumulation. Curr Biol 26(4):496–502. [https://doi.org/10.1016/](https://doi.org/10.1016/j.cub.2015.12.049) [j.cub.2015.12.049](https://doi.org/10.1016/j.cub.2015.12.049)
- Makeig S, Onton J (2011) ERP features and EEG dynamics: an ICA perspective. In: Luck SJ, Kappenman ES (eds) Oxford handbook of event-related potential components. Oxford University Press, Oxford
- Martin-Loeches M, Ouyang G, Rausch P, Sturmer B, Palazova M, Schacht A, Sommer W (2017) Test-retest reliability of the N400 component in a sentence-reading paradigm. Lang Cognit Neurosci 32(10):1261–1272. [https://doi.org/10.1080/23273798.2017.](https://doi.org/10.1080/23273798.2017.1330485) [1330485](https://doi.org/10.1080/23273798.2017.1330485)
- Mendonca PRF, Vargas-Caballero M, Erdelyi F, Szabo G, Paulsen O, Robinson HPC (2016) Stochastic and deterministic dynamics of intrinsically irregular firing in cortical inhibitory interneurons. Elife. <https://doi.org/10.7554/elife.16475>
- Meyer K, Rostami HN, Ouyang G, Debener S, Sommer W, Hildebrandt A (2019) Mechanisms of face specificity-differentiating speed and accuracy in face cognition by event-related potentials of central processing
- Miller J, Ulrich R, Schwarz W (2009) Why jackknifing yields good latency estimates. Psychophysiology 46(2):300–312. [https://doi.](https://doi.org/10.1111/j.1469-8986.2008.00761.x) [org/10.1111/j.1469-8986.2008.00761.x](https://doi.org/10.1111/j.1469-8986.2008.00761.x)
- Muckschel M, Roessner V, Beste C (2020) Task experience eliminates catecholaminergic effects on inhibitory control: A randomized, double-blind cross-over neurophysiological study. Eur Neuropsychopharmacol 35:89–99. [https://doi.org/10.1016/j.](https://doi.org/10.1016/j.euroneuro.2020.03.013) [euroneuro.2020.03.013](https://doi.org/10.1016/j.euroneuro.2020.03.013)
- Murray JG, Ouyang G, Donaldson DI (2019) Compensation of trialto-trial latency jitter reveals the parietal retrieval success effect to be both variable and thresholded in older adults. Front Aging Neurosci. <https://doi.org/10.3389/fnagi.2019.00179>
- Opitz A, Beste C, Stock AK (2020) Using temporal EEG signal decomposition to identify specific neurophysiological correlates of distractor-response bindings proposed by the theory of event coding. Neuroimage. [https://doi.org/10.1016/j.neuroimage.2020.](https://doi.org/10.1016/j.neuroimage.2020.116524) [116524](https://doi.org/10.1016/j.neuroimage.2020.116524)
- Ouyang G (2020) ReSync: correcting the trial-to-trial asynchrony of event-related brain potentials to improve neural response representation. J Neurosci Methods 339:108722. [https://doi.org/10.](https://doi.org/10.1016/j.jneumeth.2020.108722) [1016/j.jneumeth.2020.108722](https://doi.org/10.1016/j.jneumeth.2020.108722)
- Ouyang G, Schacht A, Zhou CS, Sommer W (2013) Overcoming limitations of the ERP method with residue iteration decomposition (RIDE): a demonstration in go/no-go experiments. Psychophysiology 50(3):253–265. [https://doi.org/10.1111/psyp.](https://doi.org/10.1111/psyp.12004) [12004](https://doi.org/10.1111/psyp.12004)
- Ouyang G, Sommer W, Zhou CS (2015) Updating and validating a new framework for restoring and analyzing latency-variable ERP components from single trials with residue iteration decomposition (RIDE). Psychophysiology 52(6):839–856. [https://doi.org/](https://doi.org/10.1111/psyp.12411) [10.1111/psyp.12411](https://doi.org/10.1111/psyp.12411)
- Ouyang G, Sommer W, Zhou CS (2016) Reconstructing ERP amplitude effects after compensating for trial-to-trial latency jitter: a solution based on a novel application of residue iteration decomposition. Int J Psychophysiol 109:9–20. [https://doi.org/10.](https://doi.org/10.1016/j.ijpsycho.2016.09.015) [1016/j.ijpsycho.2016.09.015](https://doi.org/10.1016/j.ijpsycho.2016.09.015)
- Ouyang G, Hildebrandt A, Sommer W, Zhou CS (2017) Exploiting the intra-subject latency variability from single-trial eventrelated potentials in the P3 time range: a review and comparative evaluation of methods. Neurosci Biobehav Rev 75:1–21. [https://](https://doi.org/10.1016/j.neubiorev.2017.01.023) doi.org/10.1016/j.neubiorev.2017.01.023
- Patterson JV, Jin Y, Gierczak M, Hetrick WP, Potkin S, Bunney WE, Sandman CA (2000) Effects of temporal variability on P50 and the gating ratio in schizophrenia: a frequency domain adaptive filter single-trial analysis. Arch Gen Psychiatry 57(1):57–64. <https://doi.org/10.1001/archpsyc.57.1.57>
- Peng SH, Xuan B, Li P (2020) Fearful faces modulate cognitive control under varying levels of uncertainty: an event-related potential study. Brain Cogn. [https://doi.org/10.1016/j.bandc.](https://doi.org/10.1016/j.bandc.2020.105550) [2020.105550](https://doi.org/10.1016/j.bandc.2020.105550)
- Pisauro MA, Fouragnan E, Retzler C, Philiastides MG (2017) Neural correlates of evidence accumulation during value-based decisions revealed via simultaneous EEG-fMRI. Nat Commun. <https://doi.org/10.1038/ncomms15808>
- Pomalazaraez CA, Mcgillem CD (1986) Enhancement of event related potentials by iterative restoration algorithms. IEEE Trans Biomed Eng 33(12):1107–1113. [https://doi.org/10.1109/tbme.](https://doi.org/10.1109/tbme.1986.325687) [1986.325687](https://doi.org/10.1109/tbme.1986.325687)
- Ratcliff R, Sederberg PB, Smith TA, Childers R (2016) A single trial analysis of EEG in recognition memory: tracking the neural correlates of memory strength. Neuropsychologia 93:128–141. <https://doi.org/10.1016/j.neuropsychologia.2016.09.026>
- Rellecke J, Sommer W, Schacht A (2012) Does processing of emotional facial expressions depend on intention? Time-resolved evidence from event-related brain potentials. Biol Psychol 90(1):23–32. <https://doi.org/10.1016/j.biopsycho.2012.02.002>
- Ribeiro MJ, Paiva JS, Castelo-Branco M (2016) Spontaneous fluctuations in sensory processing predict within-subject reaction time variability. Front Hum Neurosci. [https://doi.org/10.3389/](https://doi.org/10.3389/fnhum.2016.00200) [fnhum.2016.00200](https://doi.org/10.3389/fnhum.2016.00200)
- Rostami HN, Saville CWN, Klein C, Ouyang G, Sommer W, Zhou CS, Hildebrandt A (2017) COMT genotype is differentially associated with single trial variability of ERPs as a function of memory type. Biol Psychol 127:209–219. [https://doi.org/10.](https://doi.org/10.1016/j.biopsycho.2017.06.002) [1016/j.biopsycho.2017.06.002](https://doi.org/10.1016/j.biopsycho.2017.06.002)
- Sassenhagen J, Bornkessel-Schlesewsky I (2015) The P600 as a correlate of ventral attention network reorientation. Cortex 66:A3–A20. <https://doi.org/10.1016/j.cortex.2014.12.019>
- Saville CWN, Feige B, Kluckert C, Bender S, Biscaldi M, Berger A et al (2015) Increased reaction time variability in attentiondeficit hyperactivity disorder as a response-related phenomenon: evidence from single-trial event-related potentials. J Child Psychol Psychiatry 56(7):801–813. [https://doi.org/10.1111/jcpp.](https://doi.org/10.1111/jcpp.12348) [12348](https://doi.org/10.1111/jcpp.12348)
- Schiff S, D'Avanzo C, Cona G, Goljahani A, Montagnese S, Volpato C et al (2014) Insight into the relationship between brain/ behavioral speed and variability in patients with minimal hepatic encephalopathy. Clin Neurophysiol 125(2):287-297. [https://doi.](https://doi.org/10.1016/j.clinph.2013.08.004) [org/10.1016/j.clinph.2013.08.004](https://doi.org/10.1016/j.clinph.2013.08.004)
- Smith NJ, Kutas M (2015a) Regression-based estimation of ERP waveforms: I. The rERP framework. Psychophysiology 52(2):157–168. <https://doi.org/10.1111/psyp.12317>
- Smith NJ, Kutas M (2015b) Regression-based estimation of ERP waveforms: II. Nonlinear effects, overlap correction, and practical considerations. Psychophysiology 52(2):169–181. [https://](https://doi.org/10.1111/psyp.12320) doi.org/10.1111/psyp.12320
- Spencer KM, Abad EV, Donchin E (2000) On the search for the neurophysiological manifestation of recollective experience. Psychophysiology 37(4):494–506. [https://doi.org/10.1111/1469-](https://doi.org/10.1111/1469-8986.3740494) [8986.3740494](https://doi.org/10.1111/1469-8986.3740494)
- Stefanics G, Heinzle J, Horvath AA, Stephan KE (2018) Visual mismatch and predictive coding: a computational single-trial

ERP study. J Neurosci 38(16):4020–4030. [https://doi.org/10.](https://doi.org/10.1523/jneurosci.3365-17.2018) [1523/jneurosci.3365-17.2018](https://doi.org/10.1523/jneurosci.3365-17.2018)

- Steinemann NA, O'Connell RG, Kelly SP (2018) Decisions are expedited through multiple neural adjustments spanning the sensorimotor hierarchy. Nat Commun. [https://doi.org/10.1038/](https://doi.org/10.1038/s41467-018-06117-0) [s41467-018-06117-0](https://doi.org/10.1038/s41467-018-06117-0)
- Stokes M, Spaak E (2016) The importance of single-trial analyses in cognitive neuroscience. Trends Cognit Sci 20(7):483–486. <https://doi.org/10.1016/j.tics.2016.05.008>
- Sturmer B, Ouyang G, Zhou CS, Boldt A, Sommer W (2013) Separating stimulus-driven and response-related LRP components with residue iteration decomposition (RIDE). Psychophysiology 50(1):70–73. [https://doi.org/10.1111/j.1469-8986.2012.](https://doi.org/10.1111/j.1469-8986.2012.01479.x) [01479.x](https://doi.org/10.1111/j.1469-8986.2012.01479.x)
- Takacs A, Mückschel M, Roessner V, Beste C (2020) Decoding stimulus-response representations and their stability using EEGbased multivariate pattern analysis. Cereb Cortex Commun $1:1-12$
- Takeda Y, Yamanaka K, Yamamoto Y (2008) Temporal decomposition of EEG during a simple reaction time task into stimulusand response-locked components. Neuroimage 39(2):742–754. <https://doi.org/10.1016/j.neuroimage.2007.09.003>
- Takeda Y, Sato M, Yamanaka K, Nozaki D, Yamamoto Y (2010) A generalized method to estimate waveforms common across trials from EEGs. Neuroimage 51(2):629–641. [https://doi.org/10.1016/](https://doi.org/10.1016/j.neuroimage.2010.02.002) [j.neuroimage.2010.02.002](https://doi.org/10.1016/j.neuroimage.2010.02.002)
- Tobimatsu S, Celesia GG (2006) Studies of human visual pathophysiology with visual evoked potentials. Clin Neurophysiol 117(7):1414–1433. <https://doi.org/10.1016/j.clinph.2006.01.004>
- Truccolo W, Knuth KH, Shah A, Bressler SL, Schroeder CE, Ding MZ (2003) Estimation of single-trial multicomponent ERPs: differentially variable component analysis (dVCA). Biol Cybern 89(6):426–438. <https://doi.org/10.1007/s00422-003-0433-7>
- Valt C, Sprengeler MK, Sturmer B (2020) Feedback processing in the context of social comparison. Psychophysiology. [https://doi.org/](https://doi.org/10.1111/psyp.13489) [10.1111/psyp.13489](https://doi.org/10.1111/psyp.13489)
- Verleger R, Metzner MF, Ouyang G, Smigasiewicz K, Zhou CS (2014) Testing the stimulus-to-response bridging function of the oddball-P3 by delayed response signals and residue iteration decomposition (RIDE). Neuroimage 100:271–289. [https://doi.](https://doi.org/10.1016/j.neuroimage.2014.06.036) [org/10.1016/j.neuroimage.2014.06.036](https://doi.org/10.1016/j.neuroimage.2014.06.036)
- Walhovd KB, Rosquist H, Fjell AM (2008) P300 amplitude age reductions are not caused by latency jitter. Psychophysiology 45(4):545–553
- Wang F, Ouyang G, Zhou CS, Wang SP (2015) Re-examination of chinese semantic processing and syntactic processing: evidence from conventional ERPs and reconstructed ERPs by residue iteration decomposition (RIDE). PLoS ONE. [https://doi.org/10.](https://doi.org/10.1371/journal.pone.0117324) [1371/journal.pone.0117324](https://doi.org/10.1371/journal.pone.0117324)
- Wang SJ, Ouyang G, Guang J, Zhang MS, Wong KYM, Zhou CS (2016) Stochastic oscillation in self-organized critical states of small systems: sensitive resting state in neural systems. Phys Rev Lett. <https://doi.org/10.1103/physrevlett.116.018101>
- Wang R, Lin P, Liu MX, Wu Y, Zhou T, Zhou CS (2019) Hierarchical connectome modes and critical state jointly maximize human brain functional diversity. Phys Rev Lett. [https://](https://doi.org/10.1103/physrevlett.123.038301) doi.org/10.1103/physrevlett.123.038301
- Warren CV, Maraver MJ, de Luca A, Kopp B (2020) The effect of Transcutaneous auricular vagal nerve stimulation (taVNS) on P3 event-related potentials during a bayesian oddball task. Brain Sci 10(6):404
- Wolff N, Chmielewski W, Buse J, Roessner V, Beste C (2019) Paradoxical response inhibition advantages in adolescent obsessive compulsive disorder result from the interplay of automatic and controlled processes. Neuroimage Clin. [https://doi.org/10.](https://doi.org/10.1016/j.nicl.2019.101893) [1016/j.nicl.2019.101893](https://doi.org/10.1016/j.nicl.2019.101893)
- Wolters CH, Beckmann RF, Rienacker A, Buchner H (1999) Comparing regularized and non-regularized nonlinear dipole fit methods: a study in a simulated sulcus structure. Brain Topogr 12(1):3–18. <https://doi.org/10.1023/a:1022281005608>
- Woody CD (1967) Characterization of an adaptive filter for the analysis of variable latency neuroelectric signals. Med Biol Eng 5(6):539–554
- Wu W, Wu CH, Gao SK, Liu BL, Li YQ, Gao XR (2014) Bayesian estimation of ERP components from multicondition and multichannel EEG. Neuroimage 88:319–339. [https://doi.org/10.1016/](https://doi.org/10.1016/j.neuroimage.2013.11.028) [j.neuroimage.2013.11.028](https://doi.org/10.1016/j.neuroimage.2013.11.028)
- Yang H, Zhao J, Gaspar CM, Chen W, Tan YF, Weng XC (2017) Selectivity of N170 for visual words in the right hemisphere: evidence from single-trial analysis. Psychophysiology 54(8):1128–1137. <https://doi.org/10.1111/psyp.12867>
- Yao DZ (2001) A method to standardize a reference of scalp EEG recordings to a point at infinity. Physiol Meas 22(4):693–711. <https://doi.org/10.1088/0967-3334/22/4/305>
- Yin G, Zhang J, Tian Y, Yao DZ (2009) A multi-component decomposition algorithm for event-related potentials. J Neurosci Methods 178(1):219–227. [https://doi.org/10.1016/j.jneumeth.](https://doi.org/10.1016/j.jneumeth.2008.11.022) [2008.11.022](https://doi.org/10.1016/j.jneumeth.2008.11.022)
- Zhang J (1998) Decomposing stimulus and response component waveforms in ERP. J Neurosci Methods 80(1):49–63. [https://doi.](https://doi.org/10.1016/s0165-0270(97)00194-5) [org/10.1016/s0165-0270\(97\)00194-5](https://doi.org/10.1016/s0165-0270(97)00194-5)
- Zhang DD, Ding HY, Wang XC, Qi CZ, Luo YJ (2015) Enhanced response inhibition in experienced fencers. Sci Rep. [https://doi.](https://doi.org/10.1038/srep16282) [org/10.1038/srep16282](https://doi.org/10.1038/srep16282)

Publisher's Note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.