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## **Assessing XMT-Measurement Variability of Air-Water Interfacial Areas in Natural Porous Media**

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Author manuscript

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## **Abstract**

This study investigates the accuracy and reproducibility of air-water interfacial areas measured with high-resolution synchrotron x-ray microtomography (XMT). Columns packed with one of two relatively coarse-grained monodisperse granular media, glass beads or a well-sorted quartz sand, were imaged over several years, encompassing changes in acquisition equipment, improved image quality, and enhancements to image acquisition and processing software. For the glass beads, the specific solid surface area (SSSA-XMT) of 31.6  $\pm 1$  cm<sup>-1</sup> determined from direct analysis of the segmented solid-phase image data is statistically identical to the independently calculated geometric specific solid surface area (GSSA,  $32 \pm 1$  cm<sup>-1</sup>) and to the measured SSSA  $(28 \pm 3 \text{ cm}^{-1})$  obtained with the N<sub>2</sub>BET method (NBET). The maximum specific air-water interfacial area (A<sub>max</sub>) is 27.4 (±2) cm<sup>-1</sup>, which compares very well to the SSSA-XMT, GSSA, and SSSA-NBET values. For the sand, the SSSA-XMT (111  $\pm 2$  cm<sup>-1</sup>) and GSSA (113  $\pm 1$  cm<sup>-1</sup>) are similar. The mean A<sub>max</sub> is 96 ±5 cm<sup>-1</sup>, which compares well to both the SSSA and the GSSA values. The XMT-SSSA values deviated from the GSSA values by 7–16% for the first four experiments, but were essentially identical for the later experiments. This indicates that enhancements in image acquisition and processing improved data accuracy. The  $A_{\text{max}}$  values ranged from 74 cm<sup>-1</sup> to 101 cm<sup>-1</sup>, with a coefficient of variation (COV) of 9%. The maximum capillary interfacial area ranged from 12 cm<sup>-1</sup> to 19 cm<sup>-1</sup>, for a COV of 10%. The COVs for both decreased to 5–6% for the latter five experiments. These results demonstrate that XMT imaging provides accurate and reproducible measurements of total and capillary interfacial areas.

#### **Keywords**

X-ray Microtomography; air-water; capillary; image analysis; image processing; interfacial area

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Data availability statement: The data reported in the figures are freely accessible in the University of Arizona permanent repository operated under FAIR guidelines. The data may be used for non-commercial purposes, with complete citation to the original authors. The relevant access link is:<https://repository.arizona.edu/handle/10150/634951>.

## **1. INTRODUCTION**

The importance of fluid-fluid interfaces for fluid-flow processes, contaminant transport and fate, oil and gas recovery,  $CO<sub>2</sub>$  sequestration, and many other applications is now clearly established. Advancements in microtomographic image acquisition and processing methods over the past two decades have provided the means to accurately characterize fluid-fluid interfacial area in three-dimensional porous-media systems. High-resolution industrial x-ray microtomography and in particular synchrotron x-ray microtomography have been used to measure air-water and organic liquid-water interfacial areas for synthetic media (Culligan et al. 2004, 2006; Al Raoush and Wilson 2005; Prodanovic et al., 2006; Lu et al., 2010; Narter and Brusseau, 2010; Porter et al. 2010; Aferka et al. 2011; Landry et al., 2011; Lyu et al., 2017; Patmonoaji et al., 2018; Wang et al., 2019) and natural porous media (Schnaar and Brusseau, 2005, 2006a, 2006b; Brusseau et al., 2006, 2007, 2008, 2009; Costanza-Robinson et al., 2008; Al-Raoush, 2009, 2014; Russo et al., 2009; Willson et al., 2012; Carroll et al., 2015; McDonald et al., 2016; Lyu et al., 2017, Patmonoaji et al., 2018).

Measured XMT data are used to test theoretical and mathematical pore-scale models for multiphase fluid flow. The prior investigations noted above have relied almost exclusively on single sets of image measurements. Accordingly, studies testing theoretical and mathematical models have also relied on single sets of measured data, with no consideration of potential data variability or measurement uncertainty. One question of interest then is the variability and reproducibility of measurements for fluid-fluid interfacial area obtained with imaging methods. Clearly, outcomes from model testing are dependent upon the robustness of the measured data obtained from imaging.

The objective of this work is to investigate the reproducibility of air-water interfacial area measurements obtained with x-ray microtomography (XMT). Columns packed with glass beads or a well-sorted quartz sand were imaged at multiple drainage steps to measure total and capillary air-water interfacial area. Multiple columns were imaged over several years, encompassing changes in acquisition equipment, improved image quality, and enhancements to image acquisition and processing software.

## **2. MATERIALS AND METHODS**

#### **2.1 Experiment Set-Up**

A well-sorted 45–50 mesh quartz sand (Accusand, Unimin Co.) and borosilicate glass beads (Sigma-Aldrich) were used for the experiments. Physical properties of these two media are presented in Table 1. The glass beads were used to help examine the efficacy of the image acquisition and processing methods. Both of these media are water wetting. The wetting phase comprised distilled water containing 12% potassium iodide (KI) (Fisher Scientific) as a contrast agent, to better distinguish between the phases in the system.

Thin-walled polycarbonate columns,  $L = 3.2$  cm, ID = 0.63 cm, or aluminum columns, of similar dimensions (L= 3 cm, ID  $\approx$  0.6 cm), were used for the experiments. The polycarbonate columns, used for the majority of the sand experiments, have minimal dead volume (i.e. water volume that is not part of the porous-medium pack), with less than 0.05

mL compared to a fluid capacity of  $1.14$  mL  $(\leq 4\%)$ . This attribute allows for quantitative comparison between column-wide gravimetric water saturations and image-based values. A hydrophilic capillary membrane (5–15 μm pore diameter) was attached to the bottom of the column and a fine mesh was used at the top of the column to retain the solids.

The aluminum columns were dry-packed with the selected porous medium whereas the polycarbonate columns were packed under slurry conditions. Both methods achieved reasonably uniform bulk densities (Table 2). A programmable electronic syringe pump (KD Scientific) with a 2.5 mL gas-tight syringe was connected to a pressure transducer and to the bottom of the column. The columns were saturated by injecting aqueous solution into the bottom of the column at a low flow rate. Image data collected for each column prior to initiating drainage demonstrated that the columns were fully saturated.

Each experiment comprised a series of image collection and drainage steps. First, each column was imaged prior to drainage. Then a drainage step was induced by removing a small increment of the wetting fluid from the column at a low flow rate of  $\sim 0.05$  ml/min. The column was then left to equilibrate for at least 15 minutes, after which it was imaged again. This procedure was repeated several times per drainage experiment. Final saturation was established when the weight of the column remained unchanged after application of a drainage step, which means no additional water was removed. The mass of the column was measured with an analytical balance for each drainage step after data acquisition. The column was sealed and weighed to calculate the final gravimetric water content for future processing. The data presented in this study reflect a compilation of replicate data sets subject to changes in image collection and processing components beyond our control.

#### **2.2 Image Acquisition**

Synchrotron X-ray microtomography images were collected at the GeoSoilEnviroCARS (GSECARS) BM-13D beamline of the Advanced Photon Source at Argonne National Laboratory, Il. The resolution for all experiments conducted with the sand ranged between 9.7–11 μm/pixel. For the glass beads, the resolution for GB1 was 10 μm/pixel versus 7.5  $\mu$ m/ pixel for GB2. Hence, the resolutions did not change significantly over the course of the study. The field of view for the samples was approximately 7 (h) by 5 (w) mm. The images were collected from the vertical centers of the columns, to minimize the potential influence of end effects. The imaged-domain volumes fulfilled representative elementary volume requirements (Culligan et al., 2004; Brusseau et al., 2006; Razavi et al. 2007; Narter and Brusseau, 2010; Costanza-Robinson et al., 2011).

Sequential images of the columns were collected above and below the iodide absorption edge, at 33.269 and 33.069 keV, respectively. The above-edge image highlights the wetting phase, whereas the below-edge image distinguishes the solid phase. The image set that best represented all three phases was used for simultaneous multiphase segmentation. A particular focus was placed on imaging the solid phase directly. This is in contrast to previous studies (e.g., Wildenschild et al. 2002, 2004, Schnaar and Brusseau 2006a, Costanza-Robinson et al. 2008) wherein image processing focused solely on the segmentation of the fluid phases. In these studies, the solid phase was inferred based on

segmentation of the fluids, thereby avoiding the complexities inherent in the analysis of natural geomedia grains (i.e. Wildenschild et al. 2004; Kaestner et al. 2008).

The images were preprocessed with GSECARS-developed software (Rivers et al., 2010; Rivers, 2012). The program is a set of IDL© (ITT, Visual Information Solutions) routines that were designed to view the raw image data, remove artifacts, correct for dark currents, and to perform a white-field correction. Furthermore, it aligns the rotation axis based on alignment of the sinograms, removes ring artifacts, and filters noise. Finally, the program writes the reconstructed data as a single three-dimensional volume file (16-bit integer files), which can be exported into a series of individual slices or imported into a 3D viewer such as ImageJ (Schneider et al., 2012). The resulting exported image sets are used for analysis. These consist of grayscale values ranging from 0 (black) to 255 (white) for 8-bit resolution, which corresponds to low and high X-ray attenuation, respectively. Further details regarding the facility are available at the GSECARS webpage, [\(http://cars9.uchicago.edu/software/idl/](http://cars9.uchicago.edu/software/idl/tomography.html) [tomography.html](http://cars9.uchicago.edu/software/idl/tomography.html)).

#### **2.3 Image Processing and Analysis**

The multiple steps required to process a reconstructed data volume were combined into a single MatLab Program. Initially, the original grayscale images were cropped with Matlab (The MathWorks Inc.). A circular cropping area was chosen such that it encompasses a large portion of the sample and removes the column wall, while maintaining a reasonable REV. After cropping, the grayscale volumes were normalized for intensity differences with a sequential algorithm developed by Iassonov and Tuller (2010). The relevance of this approach is that it accounts for intra-phase spatial variations of grayscale intensities. The particular mechanics of the algorithms used are beyond the scope of this work. Details regarding the algorithm and respective routines are described in Iassonov et al. (2009), Kulkarni et al. (2012), and Tuller et al. (2013). Prior to segmentation, the data were preprocessed using standard unsharp masking filters and median smoothing steps. A connected component-labeling (CCM) algorithm was also applied after segmentation of all samples to remove small unrealistic voxel clusters, such as voxels enclosed by another phase due to residual noise or the presence of dense metal oxides.

Phase volumes were determined by means of voxel counting, and are used to obtain porosity and volumetric water contents. Surface areas were determined using the method presented by Lindblad (2005). This method is based on the Marching Cube surface reconstruction algorithm, modified to avoid topological ambiguities (Lindblad, 2005).

#### **2.4 Interfacial Area Determination**

The total surface area of air, the non-wetting phase, was used to determine total air-water interfacial area  $(A_{nw})$ . This is based on the fact that the surfaces of the solids are water wetting, and that thin water films are present that cannot be resolved by microtomography. The interfacial areas reported in this work represent the specific interfacial area, unless otherwise noted, wherein the areas are normalized by the volume of the imaged domain (with units of  $\text{cm}^2/\text{cm}^3$  or  $\text{cm}^{-1}$ ).

Specific capillary interfacial area  $(C_{nw})$  was calculated as one half of the difference between the combined sum of the water phase and air phase surface areas and the solid phase surface area (e.g., Montemagno and Ma, 1997; Dalla et al., 2002); where  $a_a$ ,  $a_s$ ,  $a_w$ , indicate the specific total surface areas of air, solid, and water phases, respectively:

$$
C_{nw} = \frac{1}{2}(a_a + a_w - a_s)
$$
 (1)

The capillary interfacial area calculated from equation (1) refers to interfaces associated with the menisci of contacts between air and "bulk" water residing in intergranular pore domains (partially filled capillaries, pendular rings, and wedges). The surface areas were determined individually for each phase, obtained directly from the simultaneous multi-phase segmentation procedure.

#### **2.5 Independent Validation**

The efficacy of the image-acquisition, raw-image processing, and data-segmentation procedures was assessed based on phase-balance complementarity and comparison to independently measured parameters. The porosity from image analysis is determined as the quotient of the volume of void space (i.e., sum of air and water volumes) and the total imaged sample volume  $(n_{XMT} = V_v/V_t)$ . The  $n_{XMT}$  is compared to porosity (*n*) calculated using the gravimetrically measured bulk density  $(\rho_b)$  value obtained during column preparation and the measured particle densities reported in Table 1. The segmented volume of solids in conjunction with the measured particle densities  $(\rho_p)$  can be used to calculate bulk densities for the image domain  $(\rho_b, x_{\text{MT}})$ . These values are also referenced to the gravimetrically measured bulk densities  $(\rho_b)$ . Water saturation  $(S_w)$  can be calculated using either the volume of water,  $V_w/V_v$ , or the volume of air  $(1-(V_a/V_v))$ .

The volume-normalized specific solid surface areas (SSSA) can be calculated directly from the solid surface areas determined from analysis of the segmented solid-phase image data. These values can be compared to independently determined solid surface areas. One such area is the geometric smooth-sphere specific surface area (GSSA,  $=6(1-n)/d_{50}$ ), calculated using the median particle diameter  $(d_{50})$  and the porosity (*n*) obtained from the image data (Table 1). Another relevant solid surface area is a measured value obtained using the  $N<sub>2</sub>$ -Brunauer, Emmet and Teller (NBET) method. This value represents the total external solid surface area available in the system as measured by adsorption of gas molecules onto the solid surface (e.g., Orchiston 1953; Brunauer et al., 1938), and incorporates surface area associated with microscopic surface roughness, if present.

The maximum specific air surface area is defined as the theoretical maximum total air surface area associated with vanishingly small water saturation  $(S_w\rightarrow 0)$ . Similarly, the specific maximum interfacial area  $(A<sub>max</sub>)$  is defined as the theoretical maximum total interfacial area associated with vanishingly small water saturation (Brusseau et al., 2009; 2010; Araujo and Brusseau 2019). Under this condition, a wetting-phase film of a few molecules thick will be present on the solid surfaces. It is expected that under this condition the specific surface area of the non-wetting phase, and the corresponding non-wetting/ wetting interfacial area, will be similar to the specific solid surface area. This provides a

means to compare measured total interfacial areas to independent measurements of specific solid surface areas. The  $A_{\text{max}}$  values are calculated from linear regression of the relationship between  $A_{nw}$  and  $S_{w}$ .

## **3. RESULTS AND DISCUSSION**

#### **3.1 Benchmark Analysis of Glass-bead Data**

The measured SSSA is 28 cm<sup>-1</sup> ( $\pm$ 3, 95% confidence interval) for the glass beads, determined from NBET characterization. The specific solid surface area calculated using the geometric smooth-sphere approach is 32  $(\pm 1)$  cm<sup>-1</sup>, which is similar to the NBET-measured value. This equivalence is consistent with the fact that these glass beads have no measurable surface roughness within the resolution limits of the measurement methods. The absence of measurable surface roughness has been confirmed via scanning electron microscopy (SEM) and phase-contrast microscopy (Araujo and Brusseau, 2019).

Table 1 presents the gravimetric porosity (*n*) and imaged-based porosity ( $n<sub>XMT</sub>$ ) values for both glass-bead experiments. The two sets of values are observed to be statistically identical considering the overlapping 95% confidence intervals. Similarly, the bulk densities obtained using XMT data are consistent with those determined gravimetrically. The SSSA determined from direct analysis of the XMT solid-phase data is 31.6 ( $\pm$ 1) cm<sup>-1</sup>. This value is consistent with both the NBET-measured SSSA and the GSSA values reported above.

Figure 1 shows the total volume-normalized air-water interfacial areas  $(A_{nw})$  as a function of wetting saturation (S<sub>w</sub>) for the glass-bead experiments. The A<sub>max</sub> (27.4 ±2 cm<sup>-1</sup>) is calculated based on the mean of linear regressions of the two individual data sets. The  $A_{\text{max}}$ is very similar to all three specific solid surface areas, the NBET-measured SSSA, the XMTmeasured SSSA, and the GSSA. Similar results were reported by Brusseau et al. (2009) and Narter and Brusseau (2010) for XMT measurements of organic liquid-water interfacial areas for the same glass beads as used herein. The measured  $A_{max}$  values were consistent with the SSSA-XMT, SSSA-NBET, and GSSA specific solid surface areas in both studies. Additionally, Narter and Brusseau independently determined Amax from interfacial partitioning tracer test (IPTT) measurements, and the resultant value  $(28 \text{ cm}^{-1})$  was consistent with the XMT-based Amax as well as the SSSA-NBET and GSSA. Zhong et al. (2016) used a two-phase flow IPTT method to measure organic liquid-water interfacial areas for the same glass beads, and the A<sub>max</sub> (34 cm<sup>-1</sup>) is comparable to the values above. Finally, Lyu et al. (2017) used the gas-absorption/chemical reaction (GACR) method to measure airwater interfacial areas for the same glass beads. The A<sub>max</sub> (29 cm<sup>-1</sup>) they determined is similar to the  $A_{\text{max}}$  and specific solid surface areas discussed above.

The capillary interfacial areas ( $C_{nw}$ ) as a function of water saturation ( $S_{w}$ ) for the glass bead experiments are also presented in Figure 1. Unlike the total  $A<sub>nw</sub>$ , there are no independent measurements to which to reference these results. The profiles exhibited by the  $C_{\text{nw}}$ -S<sub>w</sub> data are consistent with the expected behavior for capillary interfacial area wherein the area first increases during drainage and then decreases at lower saturations. The magnitudes of the values ( $C_{\text{max}}$ ~7.5 cm<sup>-1</sup> for S<sub>w</sub>~0.2) are consistent with prior data reported for glass-bead systems (Culligan et al., 2004, 2006; Porter et al., 2010).

In total, the observed excellent consistency between XMT-measured values and those obtained from independent measurements indicate that the image acquisition and processing methods were robust and produced accurate results. Pore-scale studies of porous media, whether computational or experimental, typically focus on analysis of fluid phases only, indirectly inferring solid-phase properties (e.g., Costanza-Robinson et al., 2008; Baveye et al 2010; Guan et al. 2018). The results presented above illustrate the advantages associated with including solid-phase analyses for pore-scale studies, wherein they are particularly useful for benchmarking analysis and helping to ensure the image acquisition and analysis methods employed are robust.

#### **3.2 Benchmark Analysis of Sand Data**

Table 1 presents the mean gravimetric and imaged-based porosities and bulk densities for the sand. The two sets of values are observed to be statistically identical, just as they were for the glass beads. The specific solid surface area (SSSA) obtained from direct analysis of the solid phase is also presented in Table 1. The mean SSSA for the sand is  $111 \pm 2$  cm<sup>-1</sup> for the latter five experiments (discussed further below), which is statistically identical to the GSSA  $(113 \pm 1 \text{ cm}^{-1})$ . It is noted that the SSSA-NBET for the sand is much greater than the SSSA<sub>XMT</sub> or the GSSA. This disparity reflects the presence of microscopic surface roughness, which is not captured by the latter two measurements.

The total volume-normalized air-water interfacial areas  $(A<sub>nw</sub>)$  as a function of saturation (S<sub>w</sub>) for the sand are presented in Figure 2. The mean A<sub>max</sub> is 96 ( $\pm$ 5) cm<sup>-1</sup>, determined from the latter five experiments. This value is approximately 17% smaller than the SSSA-XMT and GSSA specific solid surface areas. Similar results have been reported in prior studies (Costanza-Robinson et al., 2008; Willson et al., 2012). The observation of  $A_{\text{max}}$ values being somewhat smaller than specific solid surface areas is to be expected given the impact of grain-to-grain contacts and the possible under-prediction of interfacial area due to limited resolution of smaller pore domains.

Figure 2 also shows the volume-normalized capillary interfacial area  $(C_{nw})$  as a function of  $S_w$  for each experiment. The profiles exhibited by the  $C_{nw}S_w$  relationships match the expected behavior for capillary interfacial area, wherein the area first increases during drainage and then decreases at lower saturations as noted above. The calculated maximum  $C_{\text{nw}}$  for the sand is approximately 17 cm<sup>-1</sup> for the sand at S<sub>w</sub>~0.34. As would be expected, this value is larger than the value determined for the glass beads.

#### **3.3 Reproducibility of Measured Interfacial Areas**

Table 2 shows gravimetric porosity (*n*) and imaged-based porosity ( $n<sub>XMT</sub>$ ) values for each replicate sand experiment. The corresponding COV for image-based porosity  $(n<sub>XMT</sub>)$  is 2%, and the COV is 6% for gravimetric porosity. The two values are very similar for most of the experiments, but 10–20% differences between image-based and gravimetric porosities are observed for a few of the experiments. This is to be expected given that local porosities vary spatially to some degree within the column. Similar overall results are observed for bulk densities (Table 2).

The SSSA-XMT values are compared to the GSSA values for all nine experiments in Table 2. It is observed that the two sets of values differ by approximately 7–16% for the first four trips, with the SSSA-XMT values consistently smaller than the GSSA. However, the two sets of values are essentially identical for all later trips, with a mean difference of 2% between the two sets. This suggests that ongoing enhancements in image acquisition and processing improved data accuracy. These improvements included changes in acquisition setup, as well as software changes for optimization of the data collection and reconstruction process (Rivers, 2012, 2016). In addition, a major upgrade occurred in 2010 (after experiment 4) with a switch in the scintillator crystal from Yttrium Aluminum Garnet to Lutetium Aluminum Garnet (Rivers et al., 2010). This reduced blurriness around grains, as quantified by improved greyscale histograms.

The improved image clarity led to improved characterization of the solids, consistent with the observed increase in SSSA-XMT values for experiments 5–9. An increase in  $A<sub>max</sub>$ values is also observed for the data collected after the image enhancements, wherein the mean value is 87 for experiments 1–4 versus 96 for the latter five (as noted below). In addition to improved characterization of solid-phase boundaries, the improved image clarity allows for better characterization of the pore-network configuration (e.g. shape, size, connectivity) and of macro-features on the surfaces of solid grains. Overall, these improvements are expected to affect the determination of SSSA-XMT and A<sub>max</sub>, but would have minimal impact on the GSSA since it is a function only of porosity and median grain size. Interestingly, the SSSA-XMT and GSSA values are essentially identical for the glass beads for both experiment 1 and 2. Noting that experiment 1 was conducted prior to 2011 (and therefore prior to the system improvements), the consistency between the two experiments demonstrates that the pre-2011 limitations influencing characterization of the sand did not affect the glass beads. This is consistent with the fact that the glass beads comprise near-perfect spheres with no measurable surface roughness.

Greater discrepancies between independent and imaged-based values are generally expected to occur when examining the solid phase. Segmentation of the solid phase is particularly sensitive to grayscale variations that occur at the boundary with the wetting phase (e.g., Kaestner 2008). Furthermore, natural media are affected by non-uniform illumination that occurs because of physical and geochemical heterogeneity and beam variability. The consistency in XMT-SSSA and GSSA values observed for the later trips in this study indicate that the improvements reduced the uncertainty associated with imaging analysis of solid phases.

Figure 3 shows the  $A_{nw}$  for each sand experiment as a function of  $S_w$ . The estimated  $A_{max}$ was calculated for each data set, along with the 95% confidence interval for each data set (Table 2). The individual A<sub>max</sub> values range from 74 to 101 cm<sup>-1</sup>, with a mean of 92 ±6 cm  $-1$  and a coefficient of variation (COV) of 9% for all 9 experiments. The mean A<sub>max</sub> is 96 ±5 cm−1 with a COV of 5% for experiments 5–9. Brusseau et al. 2008 reported a COV of 8% for total specific organic liquid-water interfacial areas determined from eight XMT experiments. This variability is similar to that reported herein.

Figure 3 also shows the capillary interfacial area  $(C_{nw})$  as a function of water saturation  $(S_w)$ for all nine experiments. The mean maximum capillary interfacial area is 16  $(\pm 1 \text{ cm}^{-1})$ , with a COV of 10%, for all data sets. The maximum capillary interfacial area for experiments 5–9 is 17  $\pm$ 1 cm<sup>-1</sup>, with a reduction in COV to 6%. The reduced variabilities for both A<sub>nw</sub> and  $C<sub>nw</sub>$  is consistent with the lower variability for specific solid surface areas observed for experiments 5–9.

The small degrees of variability observed for  $A_{max}$  and maximum  $C_{nw}$  may originate from a number of factors. As discussed above, values for SSSA, porosity, and bulk density all vary slightly between experiments. The COVs for the XMT-determined SSSA,  $\rho_b$ , and n are 2%, 1%, and 2%, respectively, for the sand. This variability is a natural consequence of the impacts of variations in properties of the source media from sample to sample and differences in column packs, as well as variability in the imaging.

## **4. SUMMARY**

The accuracy and reproducibility of capillary and total air-water interfacial areas determined from high-resolution synchrotron microtomography data was examined in this study. The accuracy of image-based results was evaluated by benchmarking porosity, bulk density, specific solid surface area, and  $A_{max}$  to independently determined values. Reproducibility was investigated by conducting a total of 11 separate imaging experiments over the course of seven years.

Analysis of data collected for ideal glass beads confirmed that the image acquisition and processing methods produced accurate results. For the sand, porosities and bulk densities obtained from image analysis were statistically identical to independent (gravimetric) parameters. The SSSA-XMT values were consistently smaller than the GSSA values by 7– 16% for the first four trips, but were essentially identical for the later experiments. This indicates that enhancements in image acquisition and processing improved data accuracy primarily through better resolution of the solid phase. The A<sub>max</sub> values ranged from 74 cm<sup>-1</sup> to 101 cm−1, with a coefficient of variation (COV) of 9%. The maximum capillary interfacial area ranged from 12 cm<sup>-1</sup> to 19 cm<sup>-1</sup>, for a COV of 10%. The COVs for both Amax and Cmax decreased to 5–6% for the last five experiments.

These results indicate that the XMT method provided robust measurements of total and capillary interfacial areas for the two tested porous media. The magnitude of measurement variability was relatively small, especially for the later experiments. This provides a degree of confidence in the standard practice of using single measured data sets for experiment and modeling investigations. However, it should be noted that the two media used for this work are relatively coarse-grained, monodisperse granular media. Additional investigation of reproducibility is warranted for media that are finer grained and polydisperse. In addition, the benchmarking employed in the present work helped to demonstrate that the image acquisition and processing methods were robust. It is possible that measurement variability will be greater for conditions in which sub-optimal methods are used. It is important to incorporate measurement variability in experimental and modeling investigations of porescale processes, in recognition that such variability contributes to uncertainty in calculated

and simulated values. Hence, it is recommended that the magnitude of variability be determined in future studies by conducting multiple replicate measurements, at least for a representative subset of samples.

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## **REFERENCES**

- Aferka S, Viva A, Brunazzi E, Marchot P, Crine M, and Toye D (2011), Tomographic measurement of liquid hold up and effective interfacial area distributions in a column packed with high performance structured packings, Chem Eng Sci, 66(14), 3413–3422.
- Al-Kharusi AS, and Blunt MJ (2007), Network extraction from sandstone and carbonate pore space images, Journal of Petroleum Science and Engineering, 56(4), 219–231.
- Al-Raoush RI (2009), Impact of Wettability on Pore-Scale Characteristics of Residual Nonaqueous Phase Liquids, Environ. Sci. Technol, 43(13).
- Al-Raoush R (2014). Experimental investigation of the influence of grain geometry on residual NAPL using synchrotron microtomography. Journal of Contaminant Hydrology,159(04), 1–10. [PubMed: 24534446]
- Al-Raoush RI, and Willson CS (2005), Extraction of physically realistic pore network properties from three-dimensional synchrotron X-ray microtomography images of unconsolidated porous media systems, Journal of Hydrology, 300(1–4), 44–64.
- Araujo JB, and Brusseau ML (2019), Novel fluid-fluid interface domains in geologic media, Environ Sci Process Impacts, 21(1), 145–154. [PubMed: 30542687]
- Araujo JB, Mainhagu J, and Brusseau ML (2015), Measuring air-water interfacial area for soils using the mass balance surfactant-tracer method, Chemosphere, 134, 199–202. [PubMed: 25950136]
- Baveye PC, et al. (2010), Observer-dependent variability of the thresholding step in the quantitative analysis of soil images and X-ray microtomography data, Geoderma, 157(1–2), 51–63.
- Brunauer S, Emmett PH, and Teller E (1938), Adsorption of gases in multimolecular layers, Journal of the American Chemical Society, 60, 309–319.
- Brusseau ML, Peng S, Schnaar G, and Costanza-Robinson MS (2006), Relationships among air-water interfacial area, capillary pressure, and water saturation for a sandy porous medium, Water Resources Research, 42(3).
- Brusseau ML, Peng S, Schnaar G, and Murao A (2007), Measuring air-water interfacial areas with Xray microtomography and interfacial partitioning tracer tests, Environmental Science & Technology, 41(6), 1956–1961. [PubMed: 17410790]
- Brusseau ML, Janousek H, Murao A, and Schnaar G (2008), Synchrotron X-ray microtomography and interfacial partitioning tracer test measurements of NAPL-water interfacial areas, Water Resources Research, 44(1).
- Brusseau ML, Narter M, Schnaar S, and Marble J (2009), Measurement and Estimation of Organic-Liquid/Water Interfacial Areas for Several Natural Porous Media, Environmental Science & Technology, 43(10), 3619–3625. [PubMed: 19544863]
- Brusseau ML, El Ouni A, Araujo JB, and Zhong H (2015), Novel methods for measuring air–water interfacial area in unsaturated porous media, Chemosphere, 127, 208–213. [PubMed: 25732632]

- Costanza-Robinson MS, Harrold KH, and Lieb-Lappen RM (2008), X-ray microtomography determination of air-water interfacial area-water saturation relationships in sandy porous media, Environmental Science & Technology, 42(8), 2949–2956. [PubMed: 18497149]
- Costanza-Robinson MS, Estabrook BD, and Fouhey DF (2011), Representative elementary volume estimation for porosity, moisture saturation, and air-water interfacial areas in unsaturated porous media: Data quality implications, Water Resources Research, 47.
- Culligan KA, Wildenschild D, Christensen BSB, Gray WG, and Rivers ML (2006), Pore-scale characteristics of multiphase flow in porous media: A comparison of air–water and oil–water experiments, Advances in Water Resources, 29(2), 227–238.
- Culligan KA, Wildenschild D, Christensen BSB, Gray WG, Rivers ML, and Tompson AFB (2004), Interfacial area measurements for unsaturated flow through a porous medium, Water Resources Research, 40(12).
- Dalla E, Hilpert M, and Miller CT (2002), Computation of the interfacial area for two-fluid porous medium systems, J Contam Hydrol, 56(1–2), 25–48. [PubMed: 12076022]
- Dobson R, Schroth MH, Oostrom M, and Zeyer J (2006), Determination of NAPL-water interfacial areas in well-characterized porous media, Environmental Science & Technology, 40(3), 815–822. [PubMed: 16509323]
- Guan KM, Nazarova M, Guo B, Tchelepi H, Kovscek AR, and Creux P (2019), Effects of Image Resolution on Sandstone Porosity and Permeability as Obtained from X-Ray Microscopy.(Report), Transport in Porous Media, 127(1), 233.
- Iassonov P, and Tuller M (2010), Application of Segmentation for Correction of Intensity Bias in X-Ray Computed Tomography Images, Vadose Zone Journal, 9(1), 187.
- Iassonov P, Gebrenegus T, and Tuller M (2009), Segmentation of X-ray computed tomography images of porous materials: A crucial step for characterization and quantitative analysis of pore structures, Water Resources Research, 45(9), n/a–n/a.
- Kaestner A, Lehmann E, and Stampanoni M (2008), Imaging and image processing in porous media research, Advances in Water Resources, 31(9), 1174–1187.
- Kulkarni R, Tuller M, Fink W, and Wildenschild D (2012), Three-Dimensional Multiphase Segmentation of X-Ray CT Data of Porous Materials Using a Bayesian Markov Random Field Framework, Vadose Zone Journal, 11(1).
- Landry CJ, Karpyn ZT, and Piri M (2011), Pore-scale analysis of trapped immiscible fluid structures and fluid interfacial areas in oil-wet and water-wet bead packs. Geofluids, 11(2), 209.
- Lindblad J (2005), Surface area estimation of digitized 3D objects using weighted local configurations, Image Vision Comput, 23(2), 111–122.
- Lyu Y, Brusseau ML, El Ouni A, Araujo JB, and Su XS (2017), The Gas-Absorption/Chemical-Reaction Method for Measuring Air-Water Interfacial Area in Natural Porous Media, Water Resources Research, 53(11), 9519–9527. [PubMed: 29662253]
- Lu N, Zeidman BD, Lusk MT, Willson CS, and Wu DT (2010), A Monte Carlo paradigm for capillarity in porous media, Geophysical Research Letters, 37(23), L23402.
- Montemagno CD, and Ma Y (1999), Measurement fo Interfacial Surface Area for Two-Phase Flow in Porous Media from PVI Data, in Characterization and measurement of the hydraulic properties of unsaturated porous media: proceedings of the International Workshop on Characterization and Measurement of the Hydraulic Properties of Unsaturated Porous Media: Riverside, California, October 22–24, 1997, edited by van Genuchten MT, Leij FJ and Wu L, pp. 121–132, U.S. Salinity Laboratory, Agricultural Research Service Dept. of Environmental Sciences, University of California, Riverside, CA.
- Narter M, and Brusseau ML (2010), Comparison of interfacial partitioning tracer test and highresolution microtomography measurements of fluid‐fluid interfacial areas for an ideal porous medium, Water Resources Research, 46(8), W08602.
- Orchiston HD (1953), Adsorption of Water Vapor .1. Soils at 25-Degrees-C, Soil Science, 76(6), 453– 465.
- Patmonoaji A, Tsuji K, Muharrik M, and Suekane T (2018), Micro-tomographic analyses of specific interfacial area inside unconsolidated porous media with differing particle characteristics from

microscopic to macroscopic scale, Journal of Colloid And Interface Science, 532, 614–621. [PubMed: 30114651]

- Peng S, Hu QH, Dultz S, and Zhang M (2012), Using X-ray computed tomography in pore structure characterization for a Berea sandstone: Resolution effect, Journal of Hydrology, 472, 254–261.
- Porter ML, and Wildenschild D (2010), Image analysis algorithms for estimating porous media multiphase flow variables from computed microtomography data: a validation study, Computational Geosciences, 14(1), 15–30.
- Porter ML, Schaap MG, and Wildenschild D (2009), Lattice-Boltzmann simulations of the capillary pressure-saturation-interfacial area relationship for porous media, Advances in Water Resources, 32(11), 1632–1640.
- Porter ML, Wildenschild D, Grant G, and Gerhard JI (2010), Measurement and prediction of the relationship between capillary pressure, saturation, and interfacial area in a NAPL-water-glass bead system, Water Resources Research, 46(8).
- Prodanovic M, Lindquist WB, and Seright RS (2006), Porous structure and fluid partitioning in polyethylene cores from 3D X-ray microtomographic imaging, Journal of Colloid and Interface Science, 298(1), 282–297. [PubMed: 16364351]
- Razavi MR, Muhunthan B, and Al Hattamleh O (2007), Representative elementary volume analysis of sands using X-ray computed tomography, Geotech Test J, 30(3), 212–219.
- Rivers ML (2012), tomoRecon: High-speed tomography reconstruction on workstations using multithreading, Proc Spie, 8506, 85060U–85013.
- Rivers ML, Citron DT, and Wang YB (2010), Recent developments in computed tomography at GSECARS, Developments in X-Ray Tomography Vii, 7804.
- Rivers ML (2016), High-speed tomography using pink beam at GeoSoilEnviroCARS, Developments in X-Ray Tomography X, 9967.
- Russo AE, Narter M, and Brusseau ML (2009), Characterizing pore-scale dissolution of organic immiscible liquid in a poorly-sorted natural porous medium, Environmental Science and Technology, 43(15), 5671–5678. [PubMed: 19731661]
- Schnaar G, and Brusseau ML (2005), Pore-scale characterization of organic immiscible-liquid morphology in natural porous media using synchrotron X-ray microtomography, Environmental Science & Technology, 39(21), 8403–8410. [PubMed: 16294880]
- Schnaar G, and Brusseau ML (2006a), Characterizing pore-scale configuration of organic immiscible liquid in multiphase systems with synchrotron X-ray microtomography, Vadose Zone Journal, 5(2), 641–648.
- Schnaar G, and Brusseau ML (2006b), Characterizing pore-scale dissolution of organic immiscible liquid in natural porous media using synchrotron X-ray microtomography, Environmental Science & Technology, 40(21), 6622–6629. [PubMed: 17144287]
- Schneider CA, Rasband WS, and Eliceiri KW (2012), NIH Image to ImageJ: 25 years of image analysis, Nat Methods, 9(7), 671–675. [PubMed: 22930834]
- Tuller M, Kulkarni R, and Fink W (2013), Segmentation of X-Ray CT Data of Porous Materials: A Review of Global and Locally Adaptive Algorithms, in Soil–Water–Root Processes: Advances in Tomography and Imaging, edited by Anderson SH and Hopmans JW, pp. 157–182, Soil Science Society of America, Madison, WI.
- Wang JP, Lambert P, De Kock T, Cnudde V, and Bertrand F (2019), Investigation of the effect of specific interfacial area on strength of unsaturated granular materials by X-ray tomography, Acta Geotechnica, 14(5), 1545–1559.
- Wildenschild D, Hopmans JW, Vaz CMP, Rivers ML, Rikard D, and Christensen BSB (2002), Using X-ray computed tomography in hydrology: systems, resolutions, and limitations, Journal of Hydrology, 267(3–4), 285–297.
- Wildenschild D, Culligan KA, and Christensen BSB (2004), Application of x-ray microtomography to environmental fluid flow problems, P Soc Photo-Opt Ins, 5535, 432–441.
- Willson CS, Lu N, and Likos WJ (2012), Quantification of grain, pore, and fluid microstructure of unsaturated sand from x-ray computed tomography images, Geotech Test J, 35(6), 911–923.

Zhong H, El Ouni A, Lin D, Wang B, and Brusseau ML (2016), The two-phase flow IPTT method for measurement of nonwetting-wetting liquid interfacial areas at higher nonwetting saturations in natural porous media, Water Resources Research, 52(7), 5506–551 [PubMed: 28959079]

## **Keypoints:**

Air-water interfacial areas measured with XMT have low variability

XMT-measured values are robust based on comparison to independently measured benchmarks



## **Figure 1.**

Total and capillary air-water interfacial area for glass beads. Regression-based maximum Amax is equal to the mean for both experiments (Table 1).



#### **Figure 2.**

Total and capillary air-water interfacial area for 45–50 sand. Regression line calculated using compilation of all data sets (black dash line), and for experiments 5–9 (blue line).

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## **Figure 3:**

Total and capillary air-water interfacial area for each experiment. Regression line calculated for each experiment set and represents,  $A_{max}$  at  $S_w=0.$ 

#### **Table 1.**

Physical Properties of the Porous Media $\vec{\ }$ .



 $\vec{A}$ All values determined using segmented XMT data with the exception of *n* and  $\rho_b$ .

 $a$ Median particle diameter

 $b$ <br>Coefficient of Uniformity, (d<sub>60</sub>/d<sub>10</sub>)

 $\epsilon$  porosity (*n*) from bulk density ( $\rho$ <sub>b</sub>) of sample.

 $\sigma_{\rm pb}^d$  bulk density.

 $e^c$ Maximum *measureable* specific interfacial area, A<sub>max</sub>=A<sub>nw</sub>(1-S<sub>w</sub>), ± indicates upper and lower 95% confidence interval.

 $f$ Specific solid surface area obtained directly from image analysis normalized by imaged volume.

 ${}^g\!N_2$ -Brunauer, Emmet and Teller (NBET) surface area. This value represents the total external solid surface area available in the system and incorporates surface area associated with microscopic surface roughness.

<sup>h</sup>Geometric specific solid surface area based on smooth-sphere assumption,  $(5(1-n)/d50)$ , where d50 is median particle diameter, and *n* is porosity).

#### **Table 2.**

### Column Properties for each experiment<sup> $\vec{t}$ </sup>



 $\dot{N}$ XMT-subscript indicates values calculated solely from segmented imaged data.

 $a$ Maximum *measureable* specific interfacial area, A<sub>max</sub>=A<sub>nw</sub>(1-S<sub>w</sub>)

 $b$ Specific solid surface area obtained directly from image analysis normalized by imaged volume, ±indicates upper and lower 95% confidence interval.

Cometric specific solid surface area based on smooth-sphere assumption,  $(56(1-n)/d50)$ , where d50 is mean particle diameter, and *n* is porosity).

 $d$  porosity (*n*) from bulk density (*ρ*b) of sample.