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Effect of Electrokinetics and Thermodynamic Equilibrium on Low-Salinity Water Flooding for Enhanced Oil Recovery in Sandstone Reservoirs

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ABSTRACT: Wettability alteration (from oil-wet to mixed- or water-wet condition) is the most prominent mechanism in lowsalinity water flooding (LSWF) for enhanced oil recovery (EOR) in sandstone reservoirs. Although several factors influence the wettability alteration, many efforts have been made to find the main controlling factor. In this study, the influence of interface properties of sandstone/brine and thermodynamic equilibrium of sandstone minerals were evaluated to understand the wettability alteration during LSWF. A triple-layer surface complexation model built-in PHREEQC was applied to a quartz/brine interface, and the modeling results were verified with zeta potential experimental



data. This model was combined with that of kaolinite/brine to predict sandstone/brine interface properties. The measured and predicted sandstone zeta potentials were between those obtained for quartz and kaolinite in the diluted seawater. The predicted surface potential of sandstone together with that of crude oil was used in extended Derjaguin–Landau–Verwey–Overbeek theory to estimate the attractive or repulsive force. Consideration of thermodynamic equilibrium between minerals and solution significantly increased the pH and hence resulted in an increase in negative surface potential in the surface complexation. This provided a strong repulsive force between crude oil and sandstone, thus resulting in a more water-wet condition.

■ INTRODUCTION

Low-salinity water flooding (LSWF), which is the injection of brine with low salinity of seawater or formation water into the reservoir, has been considered as the most promising enhanced oil recovery (EOR) technique because of its low cost and it is environmentally friendly.^{1–3} Some studies have confirmed improved oil recovery by LSWF in sandstone and carbonate reservoirs, while others have reported unaffected oil recovery.⁴⁻⁷ More than 15 mechanisms have been proposed in the literature to predict the outcomes of LSWF in EOR.⁶⁻¹³ Among the proposed mechanisms, the wettability alteration toward a more water-wet condition is the primary mechanism with a favorable effect of LSWF in EOR,^{13–15} but other researchers argued that fine migration is a mobility controlled mechanism in EOR during LSWF in sandstone reservoirs.¹² The contact angle measurement and core flooding experiments with low-salinity water have demonstrated the alteration of rock wettability from oil-wet to mixed-wet or water-wet state.^{16–18}

The characteristics of crude oil/brine and rock/brine interfaces and rock dissolution significantly affect the wettability alteration. The zeta potentials of crude oil emulsion and rock suspension in various solutions were used to explain wettability alteration.^{13,19,20} The injection of low-salinity water changes the surface charge of crude oil and rock to the same

polarity and results in repulsive force between the crude oil and rock. Moreover, the low-salinity water causes expansion of the double layer at both crude oil/brine and rock/brine interfaces. These induce a more water-wet state at the rock surface. Extended Derjaguin-Landau-Verwey-Overbeek (DLVO) theory has been used to evaluate the stability of water film on the rock surface for wettability alteration, $^{7,19,21-23}$ where surface charge and the double-layer thickness play a significant role in determining the total disjoining pressure (attractive or repulsive) and consequently water film stability. LSWF shifts the total disjoining pressure from negative (attractive) to positive (repulsive) and results in the release of more oil from the rock surface. Indeed, the type of ions and their composition affect the disjoining pressure, thereby causing wettability alteration. The mineral dissolution changes the pH and solution composition, which could affect the interaction between crude oil and rock and finally have an impact on wettability alteration.

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Numerous experimental and geochemical modeling studies have been reported on the effect of electrokinetics and dissolution of carbonate rocks on wettability alteration, $^{3,7,15,19-25}$ but there are only limited reports for sandstone rock because of the complexity in sandstone mineralogical characteristics. $^{26-29}$ The amount of clay in sandstone would influence the wettability alteration and oil recovery during LSWF thorough clay swelling, fine migration, and dissolution.^{27,28} The proposed geochemical models to describe the interface properties were based on the double-layer model. Moreover, only a few studies have considered the combination of double-laver surface complexation with the thermodynamic equilibrium of minerals.²⁸ The prediction of electrokinetics by the double-layer model or ignoring of minerals equilibrium would result in underestimation of attractive or repulsive forces in the crude oil-brine-rock system. Authors have applied a triple-layer surface complexation model for crude oil/brine, calcite/brine, and kaolinite/brine interfaces to predict the surface potential.³⁰⁻³² Furthermore, the importance of surface potential rather than zeta potential in the calculation of attractive or repulsive force was analyzed.³²

To the best of authors' knowledge, there is no quantitative study on estimating the interface properties of sandstone/brine and combining the properties with phase equilibrium to evaluate the wettability alteration. In the present study, the triple-layer surface complexation model built-in PHREEQC was applied for a quartz/brine interface and integrated with the model of kaolinite/brine to predict the electrokinetic properties of a sandstone/brine interface. The triple-layer surface complexation models were combined with the thermodynamic equilibrium model to evaluate the impact of mineral dissolution on the electrokinetics of the crude oil-brinesandstone system. Furthermore, the attractive or repulsive forces between crude oil and sandstone were estimated by the extended DLVO theory and used to assess the wettability alteration during LSWF.

RESULTS AND DISCUSSION

Surface Complexation Model for the Quartz/Brine Interface. To propose the triple-layer surface complexation model for the quartz/brine interface, the parameters were determined by fitting the experimental zeta potential with modeling results. The surface of quartz consists of >SiOH surface sites, and its site density was assumed to be 4.6 sites/ nm².³³ Inner capacitance of the triple-layer model was calculated from the size of water molecule (for protonation and deprotonation) or the ions directly attached to quartz surface (for calcium or magnesium adsorption), while the outer capacitance was set to 0.2 F/m^2 as adopted for the kaolinite/brine interface.³⁴ Therefore, the calculated inner capacitance values for the interaction of H^+ , Ca^{2+} , and Mg^{2+} were 2.253, 3.098, and 4.302 F/m^2 , respectively. The protonation reactions of the 2-pK model for surface sites of quartz are³³

$$>$$
SiOH + H⁺ \leftrightarrow $>$ SiOH₂⁺ (1)

$$>$$
SiO⁻ + H⁺ \leftrightarrow $>$ SiOH (2)

where >SiOH is the surface site of quartz and >SiO⁻ and >SiOH₂⁺ are the surface species.

Figure 1 shows the fitting and prediction of zeta potential for quartz in varying pH solutions for the ionic strengths of 100 and 20 mM, where an ionic strength of 100 mM was used in



Figure 1. Measured and predicted zeta potential of quartz as a function of pH at ionic strengths of 100 and 20 mM. The ionic strength was adjusted with a NaCl solution.

fitting the model to estimate the equilibrium constants for eqs 1 and 2 while 20 mM was used to validate the estimated equilibrium constants. The measured and predicted zeta potentials were negative for pH > 2.0, and a positive value was not observed. Therefore, the isoelectric point for quartz lies approximately at pH of 2.0, which is consistent with a previous study.³⁴ The zeta potential showed a tendency to increase its absolute value with increasing pH and decreasing ionic strength. The estimated equilibrium constant values for eqs 1 and 2 were -1.75 and 6.75, respectively (Table 1). The equilibrium constant values obtained in this study are consistent with the reported data using the basic Stern model³³ or triple-layer models,^{35,36} which reported -1.57 to -1.87 for eq 1 and 6.37-7.5 for eq 2. The modeling results agree with experimental data at pH < 9, and a notable discrepancy was observed between model prediction and experimental results at pH > 9. In this study, the proposed triple-layer surface complexation model did not consider sodium adsorption, which might affect the zeta potential particularly at high concentrations or high pH values. However, divalent cations have high affinity toward the quartz surface as compared to sodium. Therefore, the surface charge development due to sodium adsorption can be negligible in seawater or its dilution.

The interaction of calcium and magnesium with the quartz surface was investigated by measuring the zeta potential as a function of calcium/magnesium concentration at a constant pH 8. The measured zeta potential at an ionic strength of 100 mM was used for fitting the modeling results to estimate the equilibrium constant, while the data obtained at a 20 mM ionic strength was used for validation of the estimated equilibrium constant. The results are shown in Figure 2 and Figure 3 for calcium and magnesium, respectively. As obtained in kaolinite,³² the adsorption of calcium or magnesium compensated the negative quartz surface, and the measured and predicted zeta potential increased toward a positive value. The estimated equilibrium constant for calcium and magnesium adsorption was -5.70 (Table 1). The estimated equilibrium constants satisfactorily predicted the zeta potential at low ionic strengths.

The determined surface complexation modeling parameters (Table 1) were applied to predict the zeta potential of quartz in SW and its dilution. As SW comprises multi-ions, the large size of calcium ion was considered to determine the inner capacitance. The model prediction was compared with experimental data in Figure 4A. The reduction of salinity increased the absolute value of zeta potential. Model prediction agrees well with experimental data, suggesting the application of the model in sandstone. Figure 4B shows the distribution of predicted concentration of surface species. The concentration

Table 1. Surface Complexation Modeling Parameters for Sandstone

	quartz/brine interface	kaolinite/brine interface ³²
	quartz edge (X = Si)	kaolinite edges (X = Si, Al)
>XOH site density (sites/nm ²)	4.6 ^{<i>a</i>}	5.5
specific surface area of quartz (m^2/g)	0.92	11.47
	<i>log_K</i> at 25 °C	
$>XOH + H^+ \leftrightarrow >XOH_2^+$	-1.75	0.80
$>XO^{-} + H^{+} \leftrightarrow >XOH$	6.75	7.00
$>XOH + Ca^{2+} \leftrightarrow >XOCa^{+} + H^{+}$	-5.70	-6.00
$>$ XOH + Mg ²⁺ \leftrightarrow $>$ XOMg ⁺ + H ⁺	-5.70	-5.55
$C1 (F/m^2)$	2.253 (H ⁺ interaction)	
	3.098 (Ca ²⁺ interaction)	
	4.302 (Mg ²⁺ interaction)	
$C2 (F/m^2)$	0.2	

^aReference 33.



Figure 2. Measured and predicted zeta potential of quartz as a function of $CaCl_2$ concentration at ionic strengths of (A) 100 mM and (B) 20 mM. The ionic strength was adjusted with a NaCl solution.

of $>SiOH_2^+$ was excluded due to its exceptionally low concentration. The concentration of un-ionized surface species (>SiOH) increased with dilution, while the concentration of deprotonated ($>SiO^-$), calcium ($>SiOCa^+$), and magnesium ($>SiOMg^+$) adsorbed surface species decreased with dilution. Higher concentrations of deprotonated surface sites than the summation of calcium and magnesium adsorbed sites contributed to the negative zeta potential in SW or its dilution.

Prediction of Electrokinetic Properties of the Sandstone/Brine Interface. The quartz and clay minerals in sandstone contribute to electrokinetics of sandstone. The zeta potential of sandstone was measured, and the values were compared with quartz and kaolinite in Figure 5 for the suspension in SW and its dilution. The negative sign of zeta potential was associated with a higher fraction of deprotonated surface sites than the concentration of divalent cation adsorbed sites. As observed in quartz and kaolinite,³² sandstone zeta potential decreased with salinity reduction. Furthermore, the sandstone zeta potential in the diluted SW existed in between quartz and kaolinite, suggesting that the surface functional groups of both quartz and kaolinite influence the electrokinetic properties of sandstone. The measured Berea sandstone zeta



Figure 3. Measured and predicted zeta potential of quartz as a function of $MgCl_2$ concentration at ionic strengths of (A) 100 mM and (B) 20 mM. The ionic strength was adjusted with a NaCl solution.

potential in SW or diluted SW was from -2 to -12 mV, which is comparable and consistent with the results reported in the literature.³⁷ The pH of the solution and divalent cation concentration in SW significantly affect the zeta potential of sandstone in addition to the type and amount of clay in sandstone.

The surface complexation modeling parameters of quartz and kaolinite³² were combined to predict the zeta potential of sandstone. It should be noted that the triple-layer model was integrated with the thermodynamic equilibrium in the simulation (see the Supporting Information). The results are shown in Figure 6 for sandstone in SW and its dilution. A good agreement between model prediction and experimental data was obtained, indicating the significance and contribution of quartz and kaolinite electrokinetics on sandstone.

Impact of Surface Electrical Properties and Thermodynamic Equilibrium on the LSWF Effect. The total disjoining pressure between the crude oil and sandstone controls the stability of the water layer between the interfaces and influences the attraction or repulsion between them. A higher disjoining pressure expands the water layer and causes repulsion between the surfaces (water-wet), whereas the low



Figure 4. (A) Comparison between measured and predicted zeta potential of quartz. (B) Surface speciation of the quartz/brine interface in seawater and its dilution.



Figure 5. Measured zeta potential of quartz, kaolinite, and sandstone as a function of dilution in SW (kaolinite data were reprinted from Takeya et al.³²).



Figure 6. Comparison between measured and predicted zeta potential of sandstone as a function of dilution in SW.

disjoining pressure attracts the surfaces (oil-wet). Therefore, total disjoining pressure is a good indicator to evaluate the wettability alteration during LSWF. To understand the contribution of van der Waals, electrical, and structural forces on total disjoining pressure, calculations were performed for crude oil and sandstone in 30 times diluted SW. The triplelayer surface complexation model proposed previously³⁰ for the crude oil/brine interface was used together with the model for sandstone/brine. Therefore, both the crude oil and sandstone (kaolinite and quartz) surfaces compete for the ionization and adsorption of ions in the solution. The calculated disjoining pressure results are shown in Figure 7



Figure 7. Calculated total and individual component of disjoining pressure for the crude oil-30*SW-sandstone system.

where crude oil of AN 1.06 32 was selected with the sandstone, which provides -47.68 mV of surface potential at the crude oil/brine interface. The van der Waals force was attractive, whereas structural and electrical forces were repulsive. The negative surface of both crude oil and sandstone predicted a positive electrical force, which dominated the total disjoining pressure. Therefore, the composition of solution and the surface potential control the attractive/repulsive force between crude oil and sandstone and hence the wettability change.

Since the sandstone consists of several minerals, the thermodynamic equilibrium between the minerals and formation water or injecting low-salinity water would affect the concentration of potential determining ions. As shown in Figure 5, the solution pH causes the negative potential of sandstone minerals. Therefore, pH change in solution significantly influences oil-brine-sandstone interactions in wettability alteration. The effect of thermodynamic equilibrium between minerals and solution on pH change and thus surface potential was evaluated for the oil-brine-sandstone system in SW and its dilution. The thermodynamic equilibrium induced pH increase 2.5-3.6 units during the dilution of SW (Figure 8), and it increased the deprotonation of surface sites, thus notably increasing the surface potential of both crude oil and sandstone. Therefore, the equilibrium of minerals should be considered in the reservoir simulation to correctly predict the wettability alteration and oil recovery.

We assessed the effect of AN of crude oil on the electrokinetics of the crude oil/brine interface³¹ as well as the crude oil-brine-calcite system.³² Furthermore, the calculated total disjoining pressure for the crude oil-brine-kaolinite system showed a positive value (in other words, repulsive) in low-salinity water due to the negative surface of both oil and kaolinite. Herein, we have analyzed the impact of integrating phase equilibrium model with the surface complexation model to understand wettability alteration via total disjoining pressure. The interaction between crude oils (AN 1.06 and 0.07) and sandstone was evaluated as total disjoining pressure, where a constant salinity of 30 times diluted SW was considered in both crude oils to neglect the effect of doublelayer thickness (Figure 9). The negative surface of the crude oil and sandstone resulted in a positive disjoining pressure. More importantly, consideration of mineral equilibrium together



Article





Figure 9. Effect of thermodynamic equilibrium and acid number on total disjoining pressure for the crude oil-30*SW-sandstone system.

with the surface complexation reactions showed a strong repulsive force between crude oil and sandstone, which was significant in a high AN of crude oil.

The pH increase and consequent increase in negative surface potential show a high impact on the interaction between the crude oil and sandstone and resulting in wettability alteration during LSWF. The proposed mechanism for wettability alteration due to electrokinetics between crude oil and sandstone and thermodynamic equilibrium is illustrated in Figure 10. Initially, the high concentration of formation water leads the crude oil to be attached to sandstone via cation bridging and forms a very thin water film between the crude oil and sandstone minerals (oil-wet state). The calculated total disjoining pressure shows a very strong attraction (initial state in Figure 10); the chemical composition of the formation water given in ref 32 and the crude oil of AN 0.07 were used for the calculation of total disjoining pressure. As a result of low-salinity water flooding, the sandstone minerals start to dissolve and increase the pH, which develops a high negative surface charge on both crude oil and sandstone minerals. In here, the electrical force between the crude oil and sandstone



Figure 10. Illustration of electrokinetics and thermodynamic equilibrium effect on wettability alteration. The associated phenomena are shown in total disjoining pressure.

becomes weak, and it reverses to repulsive force (during LSWF in Figure 10); this, in turn, expands the water film (water-wet state) and leads to the release of more oil.

CONCLUSIONS

The electrokinetics of the quartz/brine interface was studied by a zeta potential experiment and triple-layer surface complexation model. The surface complexation modeling parameters were derived by fitting the experimental data and modeling results and validated against different sets of experimental results. The triple-layer model of quartz/brine was integrated with that of kaolinite/brine to predict the electrokinetics of the sandstone/brine interface. The model successfully predicted the zeta potential of sandstone in SW and its dilution. The negative zeta potential of sandstone was lower than that of quartz but higher than that of kaolinite in the diluted solution. The significance of electrokinetics of the sandstone/brine interface in evaluating LSWF for EOR was examined by the extended DLVO theory wherein electrical force dominates the total disjoining pressure for repulsion between the crude oil and sandstone. The pH of the solution controlled the surface potential of sandstone, and the thermodynamic equilibrium between sandstone minerals and solution affected the pH change. The calculated total disjoining pressure proved that consideration of thermodynamic equilibrium together with the surface complexation is necessary to correctly evaluate wettability alteration during LSWF.

EXPERIMENTAL METHODS AND MODELING APPROACH

Experimental Methods. In this study, natural quartz from Toyoura and Berea sandstone were used for experiments. Table 2 shows the chemical composition of quartz and Berea

Table 2. Chemical Composition of Quartz and Berea Sandstone

oxide (%)	quartz	sandstone
SiO ₂	93.21	91.22
Al_2O_3	4.14	5.39
K ₂ O	2.28	1.25
Fe ₂ O ₃	0.09	0.88
CaO	0.02	0.48
MgO	0.02	0.37
TiO ₂	0.07	0.24
Na ₂ O	0.17	0.17

sandstone measured by X-ray fluorescence (XRF) analysis, and the mineralogical composition of sandstone is tabulated in Table 3. The measured BET specific surface areas of quartz and sandstone by N₂ adsorption were 0.92 and 2.34 m²/g,

Table 3. Mineralogy of Sandstone

mineral	wt. (%)
quartz	91.4
kaolinite	1.4
dolomite	1.5
muscovite	0.7
albite	1.2
orthoclase	3.7

respectively. The electrolyte solutions for the experiments were prepared by mixing the chemical reagents of NaOH, HCl, NaCl, CaCl₂, Na₂SO₄, and MgCl₂·6H₂O with deionized water. For the quartz/brine interface model development and validation, 20 and 100 mM ionic strengths of NaCl, CaCl₂, or MgCl₂ solutions were used. The pH was kept at 8 using NaOH for the measurements in calcium or magnesium solution. The ionic composition of prepared seawater (SW) is given in Table 4, and it was diluted to 3, 7, 20, and 30 times for the zeta potential measurement.

Table 4. Composition of Seawater

	Na ⁺	Ca ²⁺	Mg ²	Cl-	SO4 ²⁻	Ionic strength
SW (mg/L)	13,900	600	1560	24300	3420	0.816 [mol/L]

A zeta potential and particle size analyzer ELSZ-1000 manufactured by Otsuka Electronics was used for zeta potential measurement of quartz and sandstone suspension. The suspension was made by adding 0.01 g of quartz or sandstone into 20 mL of electrolyte solution as adopted in our previous study.³² The suspension was kept for 24 h until equilibrium and dispersed with a vortex mixer for 1 min and ultrasonic cleaner for 2 min before zeta potential measurement. The suspension was extracted with a syringe and injected into a standard cell for measurement. The zeta potential measurement was conducted at 25 °C.

Modeling Approach. The geochemical code PHREEQC was employed here for speciation, thermodynamic equilibrium between minerals and solution, and surface complexation calculations.³⁸ The attractive and repulsive forces between crude oil and sandstone were calculated by the extended DLVO theory. The governing equations are described in detail in refs 21-23, 30, 32, and 38and briefly given in Appendix A and Appendix B. For the speciation calculation in PHREEQC, the chemical reaction for mole-balance and mass-action equations, equilibrium constant and its temperature dependence, and activity coefficients are defined in SOLUTION S-PECIES data block, while the solution composition is input using the SOLUTION data block. The sandstone minerals can react with brine to achieve thermodynamic equilibrium, and the reactions are expressed by the mass-action equation. The equilibrium between the aqueous phase and minerals is modeled with PHASES and EQUILIBRIUM PHASES data blocks. The mass action equation, equilibrium constant, and its temperature-dependent constant are defined in the PHASES data block, while the EQUILIBRIUM_PHASES data block is used to input the initial composition of the phase and target saturation indices (which has a value of zero for equilibrium). Table 5 lists the dissolution reactions of minerals and their equilibrium constant under standard conditions used in this study. The PHREEQC default thermodynamic database (Phreeqc.dat)³⁸ was used for the calculations.

The electrokinetic interaction between surface and aqueous species is modeled with surface complexation reactions. The charge distribution-multi-site complexation model (CD-MUSIC) built-in PHREEQC was used as a triple-layer surface complexation model. Authors have developed the surface complexation model for the crude oil/brine (given in Appendix A), calcite/brine, and kaolinite/brine interfaces, and the model is applied herein for the quartz/brine interface.^{30–32} Hydroxyl/ hydrogen, calcium, and magnesium are considered as potential-

Tab	le 5.	Т	hermod	lynamic	Pro	perties	of	Mineral	s U	Jsed	in	the	Simul	lation
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phase	reaction	Log $K_{\rm p}$ at 25 °C
quartz	$SiO_2 + 2H_2O \leftrightarrow H_4SiO_4$	-3.98
kaolinite	$Al_2Si_2O_5(OH)_4 + 6H^+ \leftrightarrow H_2O + 2H_4SiO4 + 2Al^{3+}$	7.44
dolomite	$CaMg(CO_3)_2 \leftrightarrow Ca^{2+} + Mg^{2+} + 2CO_3^{2-}$	-17.09
albite	$NaAlSi_3O_8 + 8H_2O \leftrightarrow Na^+ + Al(OH)_4^- + 3H_4SiO_4$	-18.00
orthoclase	$KAlSi_{3}O_{8} + 8H_{2}O \leftrightarrow K^{+} + Al(OH)_{4}^{-} + 3H_{4}SiO_{4}$	-20.57

determining ions for the quartz surface as they form innersphere complexation reaction with surface functional groups, while sodium and chloride are indifferent ions and exist in the diffuse layer. The specific reaction of aqueous species with the surface species is defined in the SURFACE_SPECIES data block and the site density of each surface and its surface area are input in the SURFACE data block. An example PHREEQC input file for coupling of the triple-layer surface complexation model with the phase-equilibrium model is given in the Supporting Information.

The DLVO theory was used to estimate the forces acting between crude oil and sandstone. The total disjoining pressure in the extended DLVO theory consists of van der Waals, structural, and electrical forces. The van der Waals force, controlled by dielectric constants and refractive indices of the materials, is a long-range force. On the other hand, structural force is a short-range force and acts at a distance of <1 nm. The electrical force can be calculated from the surface potential of crude oil/brine and sandstone/brine interfaces, and it can be attractive or repulsive depending of the surface charge of both oil/brine and sandstone/brine. The surface potential calculated from the triple-layer surface complexation model was used to calculate the electrical forces for the crude oil-brine-sandstone system. Therefore, the electrical force strongly depends on the solution composition and electrokinetics of crude oil/brine and sandstone/brine interfaces. The extended DLVO theory and the associated equations are described in refs 21, 23, and 32 and given in Appendix B.

APPENDIX

A. Triple-Layer Surface Complexation Model

A detailed description of the model is given in ref 30. In the triple-layer (0-, 1-, and 2-plane) model, the surface and zeta potentials are the potential at the 0- and 2-plane. The capacitance of the first (0-to1-plane) and second (1- to 2-plane) Stern layers can be calculated by the following expression:³⁰

$$C = \frac{\varepsilon_0 \varepsilon_r}{d} \tag{A1}$$

Here, ε_0 and ε_r are the absolute (8.85 × 10⁻¹² CV⁻¹ m⁻¹) and relative dielectric constants, respectively, and *d* is the distance between the planes. The diameters of a calcium ion and a water molecule are considered to be distances *d*1 and *d*2, respectively. The dissociation of the surface carboxyl groups and the adsorption of divalent cations on the groups can be represented as

$$-\text{COOH} \leftrightarrow -\text{COO}^{-} + \text{H}^{+} K_{\text{COO}^{-}}$$
$$= \frac{(-\text{COO}^{-}) \times (a_{\text{H}^{+}})}{(-\text{COOH})} \exp\left(-\frac{F\psi_{0}}{RT}\right)$$
(A2)

$$-\text{COOH} + \text{Ca}^{2+} \leftrightarrow -\text{COOCa}^{+} + \text{H}^{+} K_{\text{COOCa}^{+}}$$
$$= \frac{(-\text{COOCa}^{+}) \times (a_{\text{H}^{+}})}{(-\text{COOH}) \times (a_{\text{Ca}^{2+}})} \exp\left(-\frac{F\psi_{1}}{RT}\right)$$
(A3)

$$-\text{COOH} + \text{Mg}^{2+}$$

$$\leftrightarrow -\text{COOMg}^{+} + \text{H}^{+} K_{\text{COOMg}^{+}}$$

$$= \frac{(-\text{COOMg}^{+}) \times (a_{\text{H}^{+}})}{(-\text{COOH}) \times (a_{\text{Mg}^{2+}})} \exp\left(-\frac{F\psi_{1}}{RT}\right)$$
(A4)

where K_{COO^-} , $K_{\text{COOC}a^+}$, and K_{COOMg^+} are the intrinsic equilibrium constants for dissociation, calcium, and magnesium adsorption, respectively, $(-\text{COO}^-)$, (-COOH), $(-\text{COOCa}^+)$, and $(-\text{COOMg}^+)$ are the concentrations (mol/m^2) of the surface species of carboxyl group, a_i is the activity of ionic species i, ψ_0 and ψ_1 are the potentials at the 0and 1-plane, respectively (V), R is the universal gas constant equal to 8.31451 J/(mol·K), and T is the absolute temperature (K).

B. Extended DLVO Theory and Disjoining Pressure Calculation

A detailed description of the calculation is given in ref 32. The attractive and repulsive forces acting between charged surfaces were calculated using the extended DLVO theory. In the reservoir system, these forces can be used to understand the interaction of oil to the rock surface. The total disjoining pressure is composed of van der Waals, electrical, and structural forces^{7,21,22,39}

$$\Pi_{\text{total}}(h) = \Pi_{\text{van}}(h) + \Pi_{\text{ele}}(h) + \Pi_{\text{str}}(h)$$
(B1)

where $\Pi_{\rm total}(h)$ is the total disjoining pressure, $\Pi_{\rm van}(h)$ is the van der Waals force, $\Pi_{\rm ele}(h)$ is the electrical force, and $\Pi_{\rm str}(h)$ is the structural force. A positive disjoining pressure in the oilbrine-rock system indicates the repulsion between the oil/brine and brine/rock interface, and a negative disjoining pressure corresponds to attraction between the surfaces.

The van der Waals force is generated between two approaching surfaces, which is an attractive force controlled by dielectric constants and refractive indices of the materials. The van der Waals force can be calculated as follows:³⁹

$$\Pi_{\rm van}(h) = \frac{-A(15.96h/\lambda + 2)}{12\pi h^3 (1 + 5.32h/\lambda)^2}$$
(B2)

where A is the Hamaker constant of the oil/brine/rock interface, λ is the London wavelength, and h is the distance separating the two surfaces. The London wavelength was assumed to be 100 nm. The Hamaker constant depends on the material properties of dielectric constants and refractive indices.^{40,41} Therefore, it should be calculated from the experiments and agreed with calculation. Based on calculation, it is given as²²

$$A = (\sqrt{A_{\text{rock}}} - \sqrt{A_{\text{water}}})(\sqrt{A_{\text{oil}}} - \sqrt{A_{\text{water}}})$$
(B3)

where subscripts rock, water, and oil indicate Hamaker constant for individual media in vacuum, and the values for $A_{\rm rock}$, $A_{\rm water}$, and $A_{\rm oil}$ are 1.01×10^{-19} , 3.7×10^{-20} , and 6.0×10^{-20} J, respectively. Equation B3 provides the Hamaker constant for the rock-brine-oil system, which is assumed to be 0.66×10^{-20} J.²²

Electrostatic forces develop between charged surfaces due to their surface potentials. The electrostatic forces can be attractive or repulsive depending on the sign of the surface charge and are developed through dissociation and adsorption of ions. The electrostatic force can be calculated from the surface potential as follows:

$$\Pi_{\text{ele}}(h) = nbkT \left(\frac{2\psi_{r1}\psi_{r2}\cosh(\kappa h) - \psi_{r1}^2 - \psi_{r2}^2}{(\sinh(\kappa h))^2} \right)$$
(B4)

where k is the Boltzmann constant (1.38×10^{-23}), T is the temperature in Kelvin, ψ_{r1} and ψ_{r2} are the reduced surface potentials, κ is the reciprocal Debye–Hückel double-layer length, n_b is the ion density in bulk solution, and h is the separating distance. The reduced surface potential and Debye–Hückel thickness were calculated as follows:

$$\psi_{\rm r} = \frac{z e \psi_0}{kT} \tag{BS}$$

$$\kappa = \sqrt{\frac{2e^2 z^2 n_{\rm b}}{\varepsilon_0 \varepsilon_{\rm r} kT}} \tag{B6}$$

where z is the valence of a symmetrical electrolyte solution, e is the electron charge $(1.6 \times 10^{-19} \text{C})$, ψ_0 is the surface potential, ε_0 is the dielectric permittivity of a vacuum (8.854 × 10⁻¹²), and ε_r is the relative permittivity of the electrolyte solution.

Structural forces act at ranges of <1 nm compared to van der Waals and electrostatic forces, which are long-range forces.^{21,22,39} The structural force, similar to the van der Waals force, does not depend on the concentration of the electrolyte solution and can be calculated as follows:

$$\Pi_{\rm str} = A_k \, \exp\!\left(-\frac{h}{h_{\rm s}}\right) \tag{B7}$$

where A_k is the coefficient and h_s is the characteristic decay length of the exponential model. In this study, it was assumed that the coefficient and decay length were 1.5×10^{10} Pa and 0.05 nm, respectively.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsomega.0c05332.

An example PHREEQC input file of the triple-layer surface complexation model coupled with the phaseequilibrium model for sandstone (PDF)

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Notes

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