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Meticulously Detailed Eye Region Model and Its Application to Analysis of Facial Images

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Abstract

We propose a system that is capable of detailed analysis of eye region images in terms of the position of the iris, degree of eyelid opening, and the shape, complexity, and texture of the eyelids. The system uses a generative eye region model that parameterizes the fine structure and motion of an eye. The structure parameters represent structural individuality of the eye, including the size and color of the iris, the width, boldness, and complexity of the eyelids, the width of the bulge below the eye, and the width of the illumination reflection on the bulge. The motion parameters represent movement of the eye, including the up-down position of the upper and lower eyelids and the 2D position of the iris. The system first registers the eye model to the input in a particular frame and individualizes it by adjusting the structure parameters. The system then tracks motion of the eye by estimating the motion parameters across the entire image sequence. Combined with image stabilization to compensate for appearance changes due to head motion, the system achieves accurate registration and motion recovery of eyes.

Keywords

Computer vision; facial image analysis; facial expression analysis; generative eye region model; motion tracking; texture modeling; gradient descent

1 INTRODUCTION

IN facial image analysis for expression and identity recognition, eyes are particularly important [1], [2], [3], [4]. Gaze tracking plays a significant role in human-computer

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interaction [5], [6] and the eye region provides useful biometric information for face and intention recognition [7], [8]. The Facial Action Coding System (FACS [9]), the de facto standard for coding facial muscle actions in behavioral science [10], defines many action units (AUs) for eyes [11], [12].

Automated analysis of facial images has found eyes still to be a difficult target [13], [14], [15], [16], [17], [18], [19], [20], [21]. The difficulty comes from the diversities in the appearance of eyes due to both structural individuality and motion of eyes, as shown in Fig. 1. Past studies have failed to represent these diversities adequately. For example, Tian et al. [22] used a pair of parabolic curves and a circle as a generic eye model, but parabolic curves have too few parameters to represent the complexity of eyelid shape and motion. Statistical models have been deployed to represent such individual differences for the whole eye region [23], [24], [25], but not for subregions, such as the eyelids, due in part to limited variation in training samples.

In this paper, we propose and evaluate a generative eye region model that can meticulously represent the detailed appearance of the eye region for eye motion tracking. The model parameterizes both the structural individualities and the motions of eyes. Structural individualities include the size and the color of the iris, the width and the boldness of the eyelid, which may have a single or double fold, the width of the bulge below the eye, the furrow below it, and the width of illumination reflection on the bulge. Eye motion includes the up-down positions of upper and lower eyelids and the 2D position of the iris. The input image sequence first is stabilized to compensate for appearance change due to head motion. The system then registers the eye region model to the input eye region and individualizes it by adjusting the structure parameters and accurately tracks the motion of the eye.

2 EYE REGION MODEL

We define a rectangular region around the eye as an eye region for analysis. We exploit a 2D, parameterized, generative model that consists of multiple components corresponding to the anatomy of an eye. These components include the iris, upper and lower eyelids, a white region around the iris *(sclera)*, dark regions near the inner and outer corners of the white region, a bulge below the lower eyelid, a bright region on the bulge, and a furrow below the bulge (the *infraorbital furrow*). The model for each component is rendered in a separate rectangular layer. When overlaid, these layers represent the eye region as illustrated in Fig. 2. Within each layer, pixels that render a component are assigned color intensities or transparency so that the color in a lower layer appears in the final eye region model if all the upper layers above it have transparent pixels at the same locations. For example, the iris layer (the third layer from the bottom) has a circular region to represent the iris. The eyelid layer (the fourth layer, one above the iris layer) has two curves to represent upper and lower eyelids, in which the region between those curves (*palpebral fissure*) is transparent while the region above the upper curve and the region below the lower curve are filled with skin color. When the eyelid layer is superimposed over the iris layer, only the portion of the circular region between the eyelid curves appears in the final eye region image while the rest is occluded by the skin pixels in the eyelid layer. When the upper curve in the eyelid layer is

lowered, corresponding to eyelid closure, a greater portion of the circular region in the iris layer is occluded.

Table 1 shows the eye components represented in the multilayered eye region model along with their control parameters. We call parameters d_u , f, d_b , d_r , r_i , and I_{γ} , the *structure* parameters (denoted by **s**) that define the static and structural detail of an eye region model, while we call parameters v_{height} , v_{skew} , λ_{height} , η_x , and η_y the time-dependent *motion parameters* (denoted by \mathbf{m}_b , *t*: time) that define the dynamic detail of the model. The eye region model defined and constructed by the structure parameters **s** and the motion parameters \mathbf{m}_t is denoted by $T(\mathbf{x}; s, \mathbf{m}_t)$, where **x** denotes pixel positions in the model coordinates. Table 2 and Table 3 show examples of the appearance changes due to the different values of **s** and \mathbf{m}_t in the eye region model $T(\mathbf{x}; \mathbf{s}, \mathbf{m}_t)$.

2.1 Upper Eyelid

The upper eyelid is a skin region that covers the upper area of the *palpebral fissure* (the eye aperture). It has two descriptive features: 1) a boundary between the upper eyelid and the palpebral fissure and 2) a furrow running nearly in parallel to the boundary directly above the upper eyelid.

The model represents these features by two polygonal curves (curve1 and curve2) and the region (region1) surrounded by them. Both curve1 and curve2 consist of N_u vertices denoted by \mathbf{u}_1 and \mathbf{u}_2 , respectively (Table 1).

2.1.1 Structure of Upper Eyelid—To represent the distance between the boundary and the furrow, parameter d_u [0 1] gives the ratio to the predefined maximum distance between curve1 and curve2. When curve1 and curve2 coincide $(d_u = 0)$, the upper eyelid appears to be a uniform region, which we refer to as a single eyelid fold. Single eyelid folds are common in East Asians. "Boldness" parameter $f[0 1]$ controls both the intensity I_{r1} of region1 and the line width w_{c2} of curve2, simultaneously by $I_{r1} = I_{r1}^{brightest} - \beta_1 \cdot f$ and $w_{c2} = \beta_2 \cdot f + w_{c2}^{thickset} (\beta_1, \beta_2)$: constant). The appearance changes controlled by d_u and f are shown in Table 2.

2.1.2 Motion of Upper Eyelid—When an upper eyelid moves up and down in its motion (e.g., blinking), the boundary between the upper eyelid and the *palpebral fissure* moves up and down. The model represents this motion by moving the vertices of curve1 (\mathbf{u}_1) . They move between the predefined curve for a completely open eye (\mathbf{u}_1^{top}) and that for a closed eye (\mathbf{u}_1^{bottom}), as shown in Fig. 3. Parameter v_{height} [0 1] specifies the position of curve1 within this range and, thus, the \hbar h vertex position of curve1 (\mathbf{u}_{1i}) is defined by parameter $ν_{height}$ as,

$$
\mathbf{u}_{1i} = \sin\left(\frac{\pi}{2} \cdot \nu_{height}\right) \cdot \mathbf{u}_{1i}^{top} + \left(1 - \sin\left(\frac{\pi}{2} \cdot \nu_{height}\right)\right) \cdot \mathbf{u}_{1i}^{bottom},\tag{1}
$$

where \mathbf{u}_{1i}^{top} and \mathbf{u}_{1i}^{bottom} are the positions of the *i*th vertices of \mathbf{u}_1^{top} and \mathbf{u}_1^{bottom} , respectively. The sinusoidal term in (1) moves the vertices rapidly when v_{height} is small and slowly when v_{height} is large with respect to the linear change of v_{height} . This corresponds to the possible rapid movement of the upper eyelid when it lowers in motion such as blinking.

The furrow on the upper eyelid also moves together with the boundary. The model represents this motion by moving the vertices of curve2 (\mathbf{u}_2) . The positions of the vertices of curve2 (\mathbf{u}_2) are defined by using parameters v_{height} and d_u such that they move in parallel to curve1 (**u**₁) when v_{height} is larger than a preset threshold v_{height}^T or move slowly keeping the distance between curve1 and curve2 wide otherwise.

If v_{height} is larger than v_{height}^T , then

$$
u_{2i}^x = u_{1i}^x,\tag{2}
$$

$$
u_{2i}^{y} = u_{1i}^{y} - \left(\alpha_1 \cdot \frac{|u_{1i}^{x} - \bar{u}_{1}^{x}|}{|u_{11}^{x} - \bar{u}_{1}^{x}|} + \alpha_2\right) \cdot d_u,
$$
\n(3)

$$
\bar{u}_1^x = \frac{u_{11}^x + u_{1N_u}^x}{2}
$$

else

$$
u_{2i}^{x} = \left(1 - \gamma d_{u, \nu_{height}}\right) \cdot u_{1i}^{x, \nu_{height}} = v_{height}^{T} + \gamma_{d_{u}, \nu_{height}} \cdot u_{1i}^{x, bottom},\tag{4}
$$

$$
u_{2i}^{y} = \left(1 - \gamma d_{u, v_{height}}\right) \cdot \tilde{u}_{1i}^{y, v_{height}} = v_{height}^{T} + \gamma d_{u, v_{height}} \cdot \tilde{u}_{1i}^{y, bottom},\tag{5}
$$

$$
\gamma_{d_{u}}, \nu_{height} = \left(1 - \frac{\nu_{height}}{\nu_{height}}\right) \cdot (1 - d_{u}),
$$

$$
\tilde{u}_{1i}^{y} = u_{1i}^{y} - \left(\alpha_{1} \cdot \frac{|u_{1i}^{x} - \bar{u}_{1}^{x}|}{|u_{11}^{x} - \bar{u}_{1}^{x}|} + \alpha_{2}\right) \cdot d_{u},
$$

end if

where a_1 and a_2 are constant.

The boundary also appears skewed horizontally when the eye is not straight to the camera because it is on a spherical eyeball. The model represents it by horizontally skewing curve1 by using parameter v_{skew} [0 1]. As shown in Fig. 4, the vertices of curve1 (\mathbf{u}_1) defined by (1) are transformed into the skewed positions (\mathbf{u}_1^{skewed}) under orthographic projection, where C denotes the center of the eyeball and θ defines the opening of the eye. The coordinate of C in the $x_{eye} - z_{eye}$ plane is

$$
C_{x_{eye}} = \left(u_{1N_u}^{x_{eye}} + u_{11}^{x_{eye}} \right) / 2,\tag{6}
$$

$$
C_{z_{eye}} = C_{x_{eye}} \cdot \tan\theta \,. \tag{7}
$$

The coordinates of \mathbf{u}_{1i} projected onto the spherical surface, (u_{1i}^{α}) $_{1i}^{x_{eye}}, u_{1i}^{z_{eye}}$, should satisfy (8), with r being the radius of the sphere:

$$
\left(u_{1i}^{x_{eye}} - C_{x_{eye}}\right)^2 + \left(u_{1i}^{z_{eye}} - C_{z_{eye}}\right)^2 = r^2.
$$
\n(8)

The x coordinate of horizontally skewed positions of $\mathbf{u}_{1i}(u_{1i}^{skewed}, x)$ in the x-z plane is obtained as

$$
u_{1i}^{skewed, x} = u_{1i}^{x_{eye}} \cdot \cos(\nu_{skew}) + \left| u_{1i}^{z_{eye}} \right| \cdot \sin(\nu_{skew}). \tag{9}
$$

The first two rows of Table 3 shows examples of the appearance changes due to parameters v_{height} and v_{skew} .

2.2 Lower Eyelid

A lower eyelid is a skin region that covers the lower area of the palpebral fissure. It has four descriptive features:

- **1.** a boundary between the lower eyelid and the palpebral fissure,
- **2.** a bulge below the boundary, which results from the shape of the covered portion of the eye, shortening of the inferior portion of the *orbicularis oculi* muscle (a sphincter muscle around the eye) on its length, and the effects of gravity and aging,
- **3.** an infraorbital furrow parallel to and below the lower eyelid, running from near the inner corner of the eye and following the cheek bone laterally [9], and
- **4.** a brighter region on the bulge, which is mainly caused by the reflection of illumination.

As shown in Table 1, the model represents these features by four polygonal curves (curve3, curve4, curve5, and curve6) and two regions (region2 surrounded by curve3 and curve4 and region3 surrounded by curve3 and curve6). Curve3, curve4, and curve6 consist of N_l vertices

and are denoted by I_1 , I_2 , and I_4 , respectively. Curve5 is the middle portion of curve4, consisting of N_f vertices denoted by I_3 .

2.2.1 Structure of Lower Eyelid—Distance ratio parameter d_b [0 1] controls the distance between curve3 and curve4. The vertices of curve4 (l_2) have the predefined positions for both the thinnest bulge (l_2^{top}) and the thickest bulge (l_2^{bottom}) , as shown in Fig. 5. The positions of the *j*th vertex of \mathbf{l}_2 are defined by using parameter d_b as

$$
\mathbf{l}_{2j} = d_b \cdot \mathbf{l}_{2j}^{bottom} + (1 - d_b) \cdot \mathbf{l}_{2j}^{top},\tag{10}
$$

where I_{2j}^{top} and I_{2j}^{bottom} are the positions of the *j*th vertices of I_{2}^{top} and I_{2}^{bottom} , respectively.

Distance ratio parameter $d_r[0\ 1]$ controls the distance between curve 3 and curve 6. The position of the *j*th vertex of I_4 is defined by using I_1 , I_2 , and parameter d_t as

$$
\mathbf{l}_{4j} = d_r \cdot \mathbf{l}_{2j} + (1 - d_r) \cdot \mathbf{l}_{1j}.
$$
 (11)

2.2.2 Motion of Lower Eyelid—When the lower eyelid moves up or down (e.g., eyelid tightening), the boundary between the lower eyelid and the palpebral fissure moves, correspondingly changing in area. The bulge, the *infraorbital furrow*, and the brighter region on the bulge also move together with the boundary.

Our model represents this motion by moving the vertices of curve3, curve5, and curve6. The vertices of curve 3 have predefined positions for both the highest (l_1^{top}) and the lowest (l_1^{bottom}) . Parameter λ_{height} [0 1] gives the position within this range. The position of the *j*th vertex of I_1 is obtained using parameter λ_{height} as

$$
\mathbf{l}_{1j} = \lambda_{height} \cdot \mathbf{l}_{1j}^{top} + \left(1 - \lambda_{height}\right) \cdot \mathbf{l}_{1j}^{bottom},\tag{12}
$$

where I_{1j}^{top} and I_{1j}^{bottom} are the positions of the *j*th vertices of I_1^{top} and I_1^{bottom} , respectively. Likewise, parameter λ_{height} controls the positions of I_2 , I_2^{top} , and I_2^{bottom} in (10).

$$
\mathbf{l}_{2j}^{top} = \lambda_{height} \cdot \mathbf{l}_{2j}^{top, t} + \left(1 - \lambda_{height}\right) \cdot \mathbf{l}_{2j}^{top, b},\tag{13}
$$

$$
\mathbf{1}_{2j}^{bottom} = \lambda_{height} \cdot \mathbf{1}_{2j}^{bottom, t} + \left(1 - \lambda_{height}\right) \cdot \mathbf{1}_{2j}^{bottom, b},\tag{14}
$$

where $(l_{2j}^{top, t}, l_{2j}^{top, b})$ and $(l_{2j}^{bottom, t}, l_{2j}^{bottom, b})$ are the preset dynamic ranges for l_{2j}^{top} and l_{2j}^{bottom} .

Parameter λ_{height} also controls both the intensity of curve3 and that of curve5 (I_{c3} and I_{c5}) by $I_{c3} = I_{c3}^{brightest} - \beta_3 \cdot \lambda_{height}$ and $I_{c5} = I_{c5}^{brightest} - \beta_4 \cdot \lambda_{height}$ (β_3 , β_4 : constant).

Table 3 shows examples of the appearance changes controlled by parameter λ_{height} .

2.3 Sclera

The sclera is the white portion of the eyeball. We limit it to the region that can be seen in the palpebral fissure, which is surrounded by the upper eyelid and the lower eyelid. Our model represents the sclera by a region (region4) surrounded by curve1 and curve3, which are defined to represent upper and lower eyelids, as shown in Table 1.

When the upper eyelid and/or the lower eyelid move, the sclera changes its shape. Our model controls the change indirectly by parameters v_{height} , v_{skew} , and λ_{height} . These primarily control the appearance changes of the upper eyelid and the lower eyelid due to the motions. Parameter v_{height} also controls the intensity of region4 by $I_{r4} = \beta_5 \cdot v_{height} + I_{r4}^{darkest}$ (β_5 : constant).

2.4 Corners

Corners are regions at the medial (close to the midline) and lateral regions of the sclera. They are usually darker than other parts of the sclera due to shadow and color of the caruncle (a small, red portion of the corner of the eye that contains sebaceous and sweat glands). As shown in Table 1, our model represents the outer corner by a region surrounded by three polygonal curves (curve1, curve3, and curve7) and the inner corner by curve1, curve3, and curve8. Both curve7 and curve8 consist of N_c vertices, denoted by c_1 and c_2 , respectively. Fig. 6 depicts the details of the outer corner model.

When the upper eyelid and/or the lower eyelid move, the shape of the eye corners changes. Our model controls the motion of the upper and the lower boundaries by parameters v_{height} v_{skew} , and λ_{height} as mentioned. The x coordinates of c_{12} and c_{13} are moved from predefined neutral positions based on parameter v_{skew} according to the horizontal proportion $\overline{P_{C_12}/PQ}$ and $\overline{P_{C_13}/PQ}$, respectively, and their y coordinates are so determined as to keep the vertical proportions same.

2.5 Iris

The iris is a circular and colored region on the eyeball. The apparent color of the iris is mainly determined by reflection of environmental illumination and the iris' texture and patterns including the *pupil* (an aperture in the center of the iris). Our model represents the iris by a circular region, region7, as shown in Table 1. Parameter r_i and parameter $I_{\gamma7}$ control the radius and the variable single color of region7, respectively. The color of the iris is represented as the average gray level inside the iris.

The position of the iris center moves when gaze direction moves. Our model represents the motion by moving the vertex of the center coordinate (i_x, i_y) of region7. It has predefined positions for gaze left (i_x^l) , gaze right (i_x^r) , gaze up (i_y^u) , and gaze down (i_y^d) , respectively. Parameters η_X [0 1] and η_V [0 1] give the position within these ranges as

$$
i_x = \eta_x \cdot i_x' + (1 - \eta_x) \cdot i_x^l,\tag{15}
$$

$$
i_y = \eta_y \cdot i_y^u + (1 - \eta_y) \cdot i_y^d. \tag{16}
$$

Table 3 includes examples of the appearance changes due to parameters η_x and η_y .

3 MODEL-BASED EYE IMAGE ANALYSIS

Fig. 7 shows a schematic overview of the whole process of a model-based eye region image analysis system. An input image sequence contains facial behaviors of a subject. Facial behaviors usually accompany spontaneous head motions. The appearance changes of facial images thus comprise both rigid 3D head motions and nonrigid facial actions. Decoupling these two components is realized by recovering the 3D head pose across the image sequence and by accordingly warping the faces to a canonical head pose (frontal and upright), which we refer to as the stabilized images. Stabilized images are intended to include appearance changes due to facial expression only. Eye image analysis proceeds on these stabilized images. For a given stabilized image sequence, the system registers the eye region model to the input in the initial frame and individualizes the model by adjusting the structure parameters **s** (Table 1). Motion of the eye is then tracked by estimating the motion parameters \mathbf{m}_t across the entire image sequence. If the tracking results at any time t are off the right positions, the model is readjusted, otherwise we finally get the estimated motion together with the structure of the eye.

3.1 Head Motion Stabilization

We use a head tracker that is based on a 3D cylindrical head model [26]. Manually given the head region with the pose and feature point locations (e.g., eye corners) in an initial frame, the tracker automatically builds the cylindrical model and recovers 3D head poses and feature point locations across the rest of the sequence. The initial frame is selected such that it has the most frontal and upright face in it. The tracker recovers full 3D rigid motions (three rotations and three translations) of the head. The performance evaluation on both synthetic and real images has demonstrated that it can track as large as 40 degrees and 75 degrees of yaw and pitch, respectively, within 3.86 degrees of average error.

As shown in Fig. 8, the stabilized face images cancel out most of the effect of 3D head pose and contain only the remaining nonrigid facial expression.

3.2 Individualization of Eye Region Model

The system first registers the eye region model to a stabilized face in an initial frame $t = 0$ by scaling and rotating the model so that both ends of curve1 (\mathbf{u}_1) of the upper eyelid coincide with the eye corner points in the image. The initial frame is such a frame that contains a neutral eye (an open eye with the iris at the center), which may be different from the initial frame used in head tracking. In the current implementation, the individualized structure parameters s are obtained manually by using a graphical user interface and fixed across the entire sequence. Example results of individualization with respect to each factor of the appearance diversities in Fig. 1 are shown in Table 4.

3.3 Tracking of Eye Motion

The pixel intensity values of both the input eye region and the eye region model are normalized prior to eye motion tracking so that they have the same average and standard deviation. The motion parameters in the initial frame \mathbf{m}_0 are manually adjusted when the eye region model is individualized.

With the initial motion parameters \mathbf{m}_0 and the structure parameters s, the system tracks the motion of the eye across the rest of the sequence starting from $t = 0$ to obtain \mathbf{m}_t at all t. The system tracks the motion parameters by an extended version of the Lucas-Kanade gradient descent algorithm [27], which allows the template searched (the eye region model here) to deform while tracking. Starting with the values in the previous frame, the motion parameters m_t at the current frame t are estimated by minimizing the following objective function D .

$$
D = \sum [T(\mathbf{x}; \mathbf{m}_t + \delta \mathbf{m}_t) - I(W(\mathbf{x}; \mathbf{p}_t + \delta \mathbf{p}_t))]^2, \tag{17}
$$

where \overline{I} is the input eye region image, W is a warp from the coordinate system of the eye region model to that of the eye region image, and \mathbf{p}_t is a vector of the warp parameters that includes only translation in this implementation. Structure parameters **s** do not show up in ^T because they are fixed while tracking.

 $\delta \mathbf{m}_t$ and $\delta \mathbf{p}_t$ are obtained by solving the simultaneous equations obtained from the first-order Taylor expansion of (17) as explained in detail in the Appendix which can be viewed for free at [http://computer.org/tpami/archives.htm.](http://computer.org/tpami/archives.htm) \mathbf{m}_t and \mathbf{p}_t are updated:

$$
\mathbf{m}_t \leftarrow \mathbf{m}_t + \delta \mathbf{m}_t, \quad \mathbf{p}_t \leftarrow \mathbf{p}_t + \delta \mathbf{p}_t. \tag{18}
$$

The iteration process at a particular frame *t* converges when the absolute values of δm_t and δp_t become less than the preset thresholds or the number of iterations reaches the maximum. The region surrounded by curve1 (\mathbf{u}_1) and curve3 (\mathbf{l}_1) of the eyelids is used for the calculation process so that more weight is placed on the structure inside the eye (the palpebral fissure) and other facial components (such as an eyebrow) that may appear in the eye region will not interfere. When parameter v_{height} is less than a preset threshold, the position of region7 (η_x and η_y) is not updated because the iris is so occluded that its position estimation is unreliable. Also, the warp parameters \mathbf{p}_t are not updated when v_{height} is less than a preset threshold because a closed (or an almost closed) eye appears to have only horizontal structure that gives only the vertical position of the eye region reliably.

4 EXPERIMENTS

We applied the proposed system to 577 image sequences from two independently collected databases: the Cohn-Kanade AU-coded Facial Expression Image Database [28] and the Ekman-Hager Facial Action Exemplars [29]. The subjects in these databases are young adults and include both men and women of varied ethnic background. They wear no glasses or other accessories that could occlude their faces. With few exceptions, head motion ranges from none (Ekman-Hager) to small (Cohn-Kanade) and head pose is frontal. Image sequences were recorded using VHS or S-VHS video and digitized into 640 by 480 gray

scale or 16-bit color pixel arrays. Image sequences begin with a neutral or near-neutral expression and end with a target expression (e.g., lower eyelids tightened). In Cohn-Kanade, image sequences are continuous (30 frames per second). In Ekman-Hager, they are discontinuous and include the initial neutral or near-neutral expression and two each of low, medium, and high-intensity facial action sampled from a longer image sequence.

In the experiments reported here, we empirically chose the following parameter values for the eye model: $N_u = 8$, $N_l = 11$, $N_f = 8$, $a_1 = 30$, $a_2 = 40$, $\beta_1 = 20$, $\beta_2 = 10$, $\beta_3 = 80$, $\beta_4 = 30$, $\beta_5 = 70$, $I_{r1}^{brightest} = 160$, $I_{c3}^{brightest} = 160$, $I_{c5}^{brightest} = 130$, $I_{r4}^{darkest} = 120$, $w_{c2}^{thickest} = 5$, and θ $= \pi/6$. The initialization for tracking was done to the first neutral or near-neutral expression frame in each sequence. The system generates the eye region model as a graphic image with a particular resolution. Because the size and positions of the graphics objects (e.g., lines) are specified in integers, the resolution and sharpness of the graphic images must be high enough for the model to represent the fine structures of an eye region. In our initial implementation, resolution was set at 350 by 250 pixels. The system then registered the model to the input eye region by scaling and rotating it as explained in Section 3.2. We examined the results for diverse static eye structures and for the whole range of appearance changes from the neutral to the utmost intensities in dynamic motion.

4.1 Cohn-Kanade AU-Coded Facial Expression Image Database

This database was collected by the Carnegie Mellon and University of Pittsburgh group. A large part of this database has been publicly released. For this experiment, we used 490 image sequences of facial behaviors from 101 subjects, all but one of which were from the publicly released subset of the database. The subjects are adults that range from 18 to50 years old with both genders (66 females and 35 males) and a variety of ethnicities (86 Caucasians, 12 African Americans, 1 East Asian, and two from other groups). Subjects were instructed by an experimenter to perform single AUs and their combinations in an observation room. Their facial behavior was then manually FACS labeled [9]. Image sequences that we used in this experiment began with a neutral face and had out-of-plane motion as large as 19 degrees.

4.2 Ekman-Hager Facial Action Exemplars

This database was provided by Ekman at the Human Interaction Laboratory, University of California San Francisco, whose images were collected by Hager, Methvin, and Irwin. For this experiment, we used 87 image sequences from 18 Caucasian subjects (11 females and 7 males). Some sequences have large lighting changes between frames. For these, we normalized the intensity so as to keep the average intensity constant throughout the image sequence. Each image sequence in this database consists of six to eight frames that were sampled from a longer sequence. Image sequences begin with neutral expression (or a weak facial action) and end with stronger facial actions.

5 RESULTS AND EVALUATION

We used both qualitative and quantitative approaches to evaluate system performance. Qualitatively, we evaluated the system's ability to represent the upper eyelids, localize and

track the iris, represent the infraorbital furrow, and track widening and closing of the eyelids. Successful performance ensures that the system is robust to ethnic and cosmetic differences in eyelid structure (e.g., single versus double fold) and features that would be necessary for accurate action unit recognition (direction of gaze, infraorbital furrow motion, and eyelid widening and closing). In quantitative evaluation, we investigated system performance with respect to resolution and sharpness of input eye region images, initialization, and complexity of the eye model.

5.1 Examples

Of the total 577 image sequences with 9,530 frames, the eye region model failed to match well in only five image sequences (92 frames total duration) from two subjects. One of the sequences contained relatively large and rapid head motion (approximately 20 degrees within 0.3 seconds) not otherwise present in either database. This motion caused interlacing distortion in the stabilized image that was not parameterized in the model. The other four error cases from a second subject were due to limitations in individualization as discussed below.

5.1.1 Upper Eyelids—A most likely failure would be that a curve of the upper eyelid model matches with the second (upper) curve of a double-fold eyelid in the input when they have similar appearance. As shown in Table 5b, our system was not compromised by such double-fold eyelids. Note that these eye region images shown in the table are after the image stabilization. The face itself moves in the original image sequence. (This is true with the subsequent tables through Table 10.)

When an upper eyelid appears thick due to cosmetics, eyelashes, or shadow, a model with a single thin line could match mistakenly at many locations within the area of thickness. Such errors did not occur; by considering boldness of the upper eyelids as a variable, our system was able to track the correct positions of upper eyelids, as shown in Table 5c.

Some subjects had double-fold eyelids that appeared single-folded when the face was at rest (i.e., neutral expression). In these cases, the second (hidden) curves were revealed when the eyelids began to widen or narrow, which unfolded the double-fold. The boldness parameter absorbed this "revealing effect" and the system was able to track correctly the upper eyelid contour, as shown in Table 5d.

5.1.2 Irises—A most likely failure in tracking irises would be for an iris model to match another dark portion in the eye region, such as shadow around the hollow between the inner corner of the eye and the root of the nose. An especially bright iris could contribute to this type of error. This situation could happen if one were to try to find the location of the iris by finding only a circular region with a fixed dark color (e.g., Tian et al. [22]). Because our method uses a whole eye region as a pattern in matching and includes color and size of the irises as variables, the system was able to track the positions of irises accurately over a wide range of brightness, as shown in Table 6a.

5.1.3 Bulge with Reflection Below the Eye—A most likely failure would be that a curve of the lower eyelid model matches with the lower edge of the bulge or the *infraorbital*

furrow. This could occur when the appearance of a bright bulge and the furrow below it are similar to that of the sclera with a lower eyelid curve below it. By considering the bulge, the illumination reflection on the bulge, and the *infraorbital furrow* in modeling the appearance below the eye, our system tracked lower eyelids accurately, as shown in Table 7.

5.1.4 Motion—Of 44 AUs defined in FACS [9], six single AUs are defined in the eye region. These include AU 5 (upper lid raiser), AU 6 (cheek raiser and lid compressor), AU 7 (lid tightener, which encompasses AU 44 in the 2002 edition of FACS), AU 43 (eye closure), AU 45 (blink), and AU 46 (wink). Gaze directions are also defined as AU 61 (turn left), AU 62 (Turn right), AU 63 (up), and AU 64 (down). Tables 8a, 8b, 8c, 8d, and 8e are correspondent with AU 5, AU 6+62, AU 6, AU 45 and AU 7, and AU 6+7, respectively, which cover the AUs related to the eye region. The frames shown range from neutral to maximum intensity of the AUs. A most likely failure due to appearance changes by the motion of an eye would be that tracking of the upper eyelid and the lower eyelid fails when the distance between them closes, such as in blinking (AU45). Our system tracked blinking well, as shown in Table 8. Tracking eye motion by matching an eye region increased system robustness relative to individually tracking feature points (such as in [3], [22], [30], [31]) or using a generic eye model. Studies [22], [32] that have used parabolic curves to represent eye shape have been less able to represent skewed eyelid shapes. Our model explicitly parameterizes skewing in the upper eyelid model; accordingly, the system was able to track such skewing upper eyelids in their motions as shown in Tables 8b and 8d.

5.1.5 Failure—Iris localization failed in a Caucasian female who had a bright iris with strong specular reflection and a thick and bold outer eye corner. Fig. 9 shows the error. While the eyelids were correctly tracked, the iris model mistakenly located the iris at the dark eye corner. Failure to correctly model the texture inside the iris appeared to be the source of this error. To solve this problem in future work, we anticipate that recurrently incorporating the appearance of the target eye region into the model during tracking would be effective and, more generally, would improve ability to accommodate unexpected appearance variation.

5.2 Quantitative Evaluation

To quantitatively evaluate the system's accuracy, we compared the positions of the model points for the upper and lower eyelids and the iris center $(\mathbf{u}_1, \mathbf{l}_1, \eta_x)$, and η_y in Table 1, respectively) with ground truth. Ground truth was determined by manually labeling the same number of points around the upper and lower eyelids and the iris center using a computer mouse. These points then were connected using polygonal curves. We then computed the Euclidean distance from each of the model points to the closest line segment between manually labeled points. If model points were located horizontally outside of the eye, the line segment from the closest manually labeled endpoint was used. For the iris center, the Euclidean distance to the manually labeled iris center was computed. The Euclidean distances were normalized by dividing them by the width of the eye region. The vector of tracking errors is denoted as vector e .

5.2.1 Sensitivity to Input Image Size and Sharpness—When the size of the input eye region is small relative to the actual size of the eye or the input image is not sufficiently sharp, the fine structure of the eye may not be sufficiently visible. Image sharpness refers to large gain in the high-frequency components of an image. To evaluate system robustness to input image size and sharpness, we compared tracking error with respect to multiple sizes and sharpness of input eye region images. Sharpness of the input images was sampled by applying a high pass filter to the image sequences. We selected for analysis nine sequences based on the response: three sequences that had the strongest response, three the weakest, and three in halfway between these. To vary image size, we resampled the images into make three levels: the original scale, 50 percent scale (0.5 \times 0.5), and quarter scale (0.25 \times 0.25). Eye motion tracking in the smaller scales used the same structure parameters as those used in the original scale. Table 9 shows an example of multiple scales of a particular eye region image. The table also shows the computation time for updating the model parameters (Pentium M, 1.6GHz, 768MB RAM, Windows XP, the average over 10 time trials). Fig. 10 shows the tracking error plotted against the widths of the image sequences. Tracking error up to about 10 percent of eye region width may have resulted from error in manual labeling. The most likely cause of small error in manual labeling was ambiguity of the boundary around the palpebral fissure (Fig. 11). We found that an eye region width of about 15 pixels was the margin under which tracking became impaired for the upper eyelid, lower eyelid, and the iris position. Above this value, performance was relatively robust with respect to both size and sharpness of the input eye region.

5.2.2 Effect of Eye Model Details—The eye region model defines many structural components to represent the diversities of eye structure and motion. To investigate whether all are necessary, we systematically omitted each component and examined the resulting change in tracking error. Table 10 shows the results of this comparison. When the model for double eyelid folds was omitted, tracking of the upper eyelid (Table 10a) was compromised. Omitting components for the appearance below the eye (Table 10b) and only the brightness region on the bulge (Table 10c) had similar effects. To achieve accurate and robust eye motion tracking for diverse eye appearances and motion, all the detailed components of the eye region model proven necessary.

In Table 10a, the tracking error ϵ shows that tracking of the other parts of the eye model was also compromised without the model for double eyelid folds (the error for the upper eyelid curve \mathbf{u}_1 , the lower eyelid curve \mathbf{l}_1 , and the iris center η_x and η_y are shown in parentheses). This indicates that the model components support tracking accuracy as a whole and erroneous individualization of one component affected tracking accuracy of the other parts.

5.2.3 Sensitivity to Model Initialization—The eye region model is manually initialized in the first frame with respect to both the structure parameters **s** and the motion parameters \mathbf{m}_t . We observed that the initialization of the structure parameters (individualization of the model) dominantly affected the tracking results. To evaluate sensitivity of the system to initialization, we individually manipulated each structure parameter in turn while leaving the others fixed. Fig. 12b is the eye region model individualized to an example of input eye region images shown in Figs. 12a and 12c shows

changes in tracking error when parameter d_u was varied from 0.0 to 1.0 while leaving other parameters fixed to $f = 0.7$, $d_b = 0.71$, $d_r = 0.7$, $r_i = 0.5$, and $I_{r7} = 0.7$. Figs. 12d, 12e, 12f, 12g, and 12h were similarly obtained. Each of the individualized structure parameters that provided stable tracking also locally minimized the tracking error. Only the parameter d_r was sensitive to the initialization in this particular example (the tracking error rapidly increased for the slight change of d_p). We also observed that parameters were intercorrelated. Fig. 13 shows a contour plot of tracking error against the changes of an example pair of structure parameters for the same image sequence used in Fig. 12. Nonlinearity is obvious, yet with weak linearity.

6 CONCLUSION

The appearance of the eyes varies markedly due to both individual differences in structure and the motion of the eyelids and iris. Structural individuality includes the size and color of the iris, the width, boldness, and number of eyelid folds, the width of the bulge below the eye, and the width of the illumination reflection on the bulge. Eye motion includes the updown action of the upper and lower eyelids and the 2D movement of the iris. This variation together with self-occlusion and change of reflection and shape of furrows and bulges has made robust and precise analysis of the eye region a challenging problem. To meticulously represent detailed appearance variation in both structural individuality and eye motion, we developed a generative eye-region model and evaluated its effectiveness by using it to analyze a large number of face image sequences from two independent databases. The use of the detailed model led to better results than those previously reported. The system achieved precise tracking of the eyes over a variety of eye appearances and motions. Future work includes initialization of the eye region model by automatic registration.

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Fig. 1.

Diversity in the appearance of eye images. (a) Variance from structural individuality. (b) Variance from motion of a particular eye.

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Fig. 3. The up-down position of curve1.

Fig. 4. The horizontal skew of curve1.

Fig. 5. The model for a lower eyelid.

Fig. 6. The model for the outer corner.

Fig. 8.

Automatic recovery of 3D head motion and image stabilization [26]. (a) Frames 1, 10, and 26 from original image sequence. (b) Face tracking in corresponding frames. (c) Stabilized face images. (d) Localized face regions.

Fig. 9.

A failure case with a bright and specular iris. The dashed circle indicates the correct position manually labeled and the solid circle system's output. The eyelids were correctly tracked, whereas the iris mistakenly located at the dark eye corner.

Sensitivity to image resolution. (a) Tracking error for the upper eyelid. (b) Tracking error for the lower eyelid. (c) Tracking error for the iris center.

ambiguous boundary

Fig. 11. An example of ambiguous boundaries around the palpebral fissure.

Moriyama et al. Page 29

Fig. 12.

An example of individualization of the model and the sensitivity to the parameter changes. (a) Input eye region image. (b) Individualized eye model $s = \{d_u, f, d_v, d_v, r_i, I_{\tau}\} = \{0.5, 0.7,$ 0.71, 0.7, 0.5, 0.7}. (c) Sensitivity to parameter d_u . (d) Sensitivity to parameter f. (e) Sensitivity to parameter d_b . (f) Sensitivity to parameter d_f . (g) Sensitivity to parameter r_i . (h) Sensitivity to parameter I_{r7} .

Moriyama et al. Page 30

Fig. 13.

A contour plot of tracking error against an example pair of the structure parameters: the intensity ratio of the iris model I_{f7} versus the distance ratio between eyelid folds d_u . The other parameters were left fixed. The brighter region indicates larger error. White lines are the values individualized in Fig. 12.

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Detailed Description of the Eye Region Model Detailed Description of the Eye Region Model

Appearance Changes Controlled by Structure Parameters

Appearance Changes Controlled by Motion Parameters

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Moriyama et al. Page 35

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TABLE 5

Example Results for Irises of Different Colors

(a) Bright iris. (b) Dark iris.

Example Results for Differences in Appearance Below the Eye

(a) Bulge. (b) Bulge with reflection.

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TABLE 8

Example Results for Motions

Example Results for Motions

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(a) Upper eyelid raising. (b) Gaze change and cheek raising. (c) Cheek raising. (d) Blinking and eyelid tightening. (e) Cheek raising and eyelid tightening. (a) Upper eyelid raising. (b) Gaze change and cheek raising. (c) Cheek raising. (d) Blinking and eyelid tightening. (e) Cheek raising and eyelid tightening. Author Manuscript Author Manuscript Author Manuscript**Author Manuscript**

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Moriyama et al. Page 43

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Moriyama et al. Page 45

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