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Isothermal Titration Calorimetry of Be²⁺ with Phosphatidylserine Models Guides All-Atom Force Field Development for Lipid-Ion Interactions

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Abstract

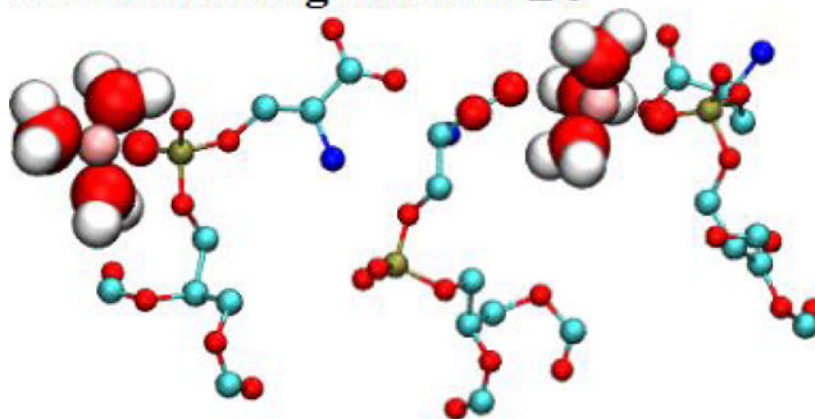
Beryllium has multiple industrial applications, but exposure to its dust during manufacturing is associated with developing chronic inflammation in lungs known as berylliosis. Besides binding to specific alleles of MHC-II, Be²⁺ was recently found to compete with Ca²⁺ for binding sites on phosphatidylserine-containing membranes and inhibit recognition of this lipid by phagocytes. Computational studies of possible molecular targets for this small toxic dication are impeded by the absence of a reliable force field. This study introduces parameters for Be²⁺ for the CHARMM36 (C36) additive force field that represent interactions with water, including free energy of hydration and ion-monohydrate interaction energy and separation distance; and interaction parameters describing Be²⁺ affinity for divalent ion binding sites on lipids, namely phosphoryl and carboxylate oxygens. Results from isothermal titration calorimetry (ITC) experiments for the binding affinities of Be²⁺ to dimethyl phosphate and acetate ions reveal that Be²⁺ strongly binds to phosphoryl groups. Revised interaction parameters for Be²⁺ with these types of oxygens reproduce experimental affinities in solution simulations. Surface tensions calculated from simulations of DOPS monolayers with varied concentrations of Be²⁺ are compared with prior results from Langmuir monolayer experiments, verifying the compacting effect that produces greater surface tensions (lower pressures) for Be²⁺-bound monolayers at the same surface area in comparison with K⁺. The new parameters will enable simulations that should reveal the mechanism of Be²⁺ interference with molecular recognition and signaling processes.

Graphical Abstract

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Supporting Information. Single document containing additional plots of equilibrated systems (Fig. S1 – S3 & S7), ITC results (Fig. S4 & S5), solution snapshots (Fig. S6), and analysis (Fig. S8 & S9); table of interaction parameters r_{ij}^{\min} tested to select appropriate NBFIX values (Table S1); and description of soluble lipid acetate model (Appendix S1).

DOPS binding sites for Be^{2+}



1. Introduction

Polyvalent ions coordinated by biological macromolecules play multiple functional roles. While permanently associated ions are typically involved in catalysis,¹ weaker and more transient associations of divalent ions (primarily Ca^{2+}) with proteins and lipids play critical roles in reversible cell adhesion,² blood clotting, normal and pathological calcification³ as well as intra- and extracellular recognition and signaling reactions.⁴ Toxicity of some polyvalent ions has been linked to their ability to interfere with calcium-dependent processes. Cadmium ions (Cd^{2+}), for instance, are known to interfere with mechanisms involving Ca^{2+} -calmodulin,⁵ whereas accumulating Cu^{2+} can promote undesirable misfolding and aggregation of proteins.^{6,7} Toxic pro-inflammatory effects of Be^{2+} are proposed to be mediated not only by abnormal binding to specific MHC-II alleles,^{8,9} but also by its ability to outcompete Ca^{2+} on the surface of phosphatidylserine domains and thus negatively affect recognition of this signaling lipid by macrophages removing apoptotic cells in a non-inflammatory way.¹⁰ The use of molecular dynamics simulations for studies of these events is often ineffective due to either imprecision or absence of force field parameters that would predict realistic affinities, ionic competition, and ion coordination by specific chemical groups.

Interactions of divalent ions with polar electronegative groups present a challenge in molecular dynamics simulations because in pairwise additive non-polarizable force fields, electrostatic interactions are effectively magnified at close range by the inability of atomic electron densities to adjust to the ambient electric field. Salt solutions therefore can be simulated in two regimes: near infinite dilution, in which ionic interactions are shielded, and high concentrations in which close-range interactions are common and can result in unnatural clustering.¹¹⁻¹³ Special adjustments are required to correct for overbinding artifacts.

The parameters of the Lennard-Jones (LJ) potential for individual ions in additive force fields are developed to reproduce experimental data in dilute solutions. Interaction potentials describing cation-anion pair interactions and ionic interactions with polar species can be

adjusted for atoms of species i and j by changing of the position of the LJ well minimum, described by the parameter r_{ij}^{\min} . For example, it has been shown that in sodium acetate solutions of more than 1 M concentration, Na^+ and acetate over-bind unless r_{ij}^{\min} is increased.¹² Because ions are more concentrated near a charged surface, they are prone to over-bind to charged lipid headgroups in bilayer and monolayer simulations. The artifacts are more severe when the simulated systems contain ions with strong interaction potentials, such as divalent ions especially with small atomic radii.

While not present in large quantities in biological systems, Be^{2+} has received recent attention for its ability to displace Ca^{2+} from binding sites in phosphatidylserine (PS).¹⁰ While both divalent ions (Ca^{2+} and Be^{2+}) interact strongly with PS, the smaller atomic radius of Be^{2+} allows it to outcompete Ca^{2+} and bind with greater affinity to DOPS liposomes (with equilibrium binding constants $K_{\text{eq}} \sim 3 \cdot 10^4 \text{ M}^{-1}$ for Ca^{2+} and $\sim 3 \cdot 10^5 \text{ M}^{-1}$ for Be^{2+}).¹⁰ The smaller size of the Be^{2+} ion also stipulates a small coordination number ($n=4$)¹⁴ which prevents this ion from adequately substituting Ca^{2+} in physiological reactions between proteins and lipids.¹ Adsorption of Be^{2+} to PS-containing domains on the surface of apoptotic cells may prevent normal phagocytosis, causing necrotic inflammation and possibly contributing to berylliosis, a chronic inflammation of the lungs associated with exposure to Be^{2+} dust.^{10, 15}

With the goal of investigating Be^{2+} binding to PS and its cognate receptors using all-atom molecular dynamics, in this iterative study we first find LJ parameters to describe the interaction of Be^{2+} with water. *Ab initio* data for ion-mono-hydrate interactions is considered, as well as solution properties including free energy of hydration ΔG_{hyd} , coordination number, and radial distribution function $g(r)$ peak position. Isothermal titration calorimetry (ITC) experiments are then used to characterize the association of Be^{2+} with model substances emulating ion-binding groups in PS. Solutions of sodium acetate or dimethyl phosphate (DMP) are titrated into $\text{Be}(\text{SO}_4)_2$ solutions. Resulting binding parameters are used to fit LJ interaction parameters r_{ij}^{\min} between Be^{2+} and the free carboxylate and phosphate oxygens, yielding improved agreement with experimental free energy of binding.

The r_{ij}^{\min} interaction parameters between Be^{2+} and phosphoryl and carboxylate oxygens are then used in DOPS monolayer simulations. Surface pressures of DOPS monolayers, found from Langmuir experiments, are dependent on salt species and concentration. Relative to Ca^{2+} , which has a larger atomic radius, Be^{2+} has a stronger compacting effect on DOPS monolayers in these experiments.¹⁰ Revised interaction parameters for Be^{2+} with phosphoryl and carboxylate oxygens reproduce experimental surface tensions for DOPS monolayers, verifying the trend of compaction of the monolayer in the presence of Be^{2+} relative to K^+ . This study validates ITC as means to perform consistent parametrization of ion-lipid interactions in molecular dynamics force fields.

2. Methods

2.1. ITC experiments.

Solutions of BeSO_4 , dimethyl phosphate ($\text{C}_2\text{H}_7\text{O}_4\text{P}$, DMP), or sodium acetate (NaCH_3COO , NaAc) were prepared in 10 mM KCl buffered with 2 mM Tris-HCl (pH 7.3) as a background electrolyte. Titrations were carried out on a MicroCal VP-ITC microcalorimeter at 30°C using injections of 10–15 μl separated by 200–300 s time intervals. To avoid subtracting large enthalpies associated with dilution of a divalent ion, solutions containing the small molecule were the titrants and the solutions containing Be^{2+} were in the chamber initially in all experiments. 4 mM DMP or 20 mM NaAc were titrated into a 2 or 5 mM BeSO_4 solution for DMP or NaAc experiments, respectively. Fitting of the integrated thermograms was done with MicroCal Origin software's one-site fitting routine¹⁶ to extract a single binding constant for each reaction. For each experimental setup, a control was performed in which the titrant was injected into pure buffer and the resulting energy subtracted before fitting was performed. Each experiment was repeated three times, and error estimates were calculated from the standard error among trials.

2.2. Molecular dynamics simulations and free energy calculations.

Standard C36 parameters were used for DOPS and DMP.¹⁷ These can be found in the C36 lipid FF¹⁷ files. Two sets of parameters were tested for acetate. The first is the standard model for soluble acetate found in the CHARMM CGEN force field files,¹⁸ referred to hereafter as “acetate, CGEN FF.” Because partial charge assignments for this model differ from those in the DOPS model, a new model for soluble acetate was developed that uses lipid atom types and partial charges similar to those of DOPS, hereafter referred to as “acetate, lipid FF.” Only interaction parameters developed for the lipid FF were tested in DOPS monolayer simulations. See supplemental information appendix S1 for partial charges of both models and additional parameters.

The TIP3P water model¹⁹ as modified²⁰ for CHARMM was used as the solvent. For solution simulations requiring counterions, revised Na^+ ion LJ interaction parameters for oxygen atoms occurring in carboxylate, carboxylate ester, and phosphate ester groups were employed.¹²

Simulations of Be^{2+} in solution with the desired small molecule were used to observe and count common configurations. Be^{2+} -small molecule pairs simulated include: Be^{2+} with DMP and Be^{2+} with acetate. Each system contained 60 small molecules, 20 divalent ions, 20 Na^+ ions to keep the system electroneutral and between 12,500 and 13,500 water molecules. Simulations of Be^{2+} with acetate were run for 40 ns, and of Be^{2+} with DMP for 330 ns, at 303.15 K in the constant number, pressure, and temperature (NPT) ensemble for comparison with ITC data. Equilibration of the systems, determined by stability of the divalent ion/oxygen pair correlation functions, occurred by 30 and 5 ns for the Be^{2+} -acetate systems with default and adjusted parameters, respectively; and by 40 and 165 ns for the Be^{2+} -phosphate systems with default and adjusted parameters, respectively. Only equilibrated segments of trajectories were used to compute configuration probabilities. See supplemental information

Figs. S1, S2, and S3 for plots demonstrating stability of the pair correlation functions for systems with revised interaction parameters.

Simulations of aqueous BeCl_2 to obtain the radial distribution functions $g(r)$ and evaluate coordination numbers and $g(r)$ peak positions were run at 298.15 K and contained between 570 and 580 TIP3P waters, 55 Be^{2+} , and 110 Cl^- distributed using random replacement. Resulting 5.3-molal solutions matched the concentration of a comparison X-ray scattering experiment used to generate the total $g(r)$.²¹ In the present study, two 30-ns simulations from different starting configurations were run at standard temperature and pressure, with the last 10 ns evaluated and error computed from the standard error in measurements from the two simulations.

Simulations of pure DOPS monolayers contained 40 lipids/leaflet, 40 divalent ions or 80 K^+ ions, and 50 waters/lipid. Initial configurations were assembled using the CHARMM-GUI *Membrane Builder*,^{22–25} which splits a single bilayer into two oppositely-oriented leaflets separated by water. Two replicates each of DOPS monolayers with Be^{2+} or K^+ at 65.3 and 71.6 $\text{\AA}^2/\text{lipid}$ were run for 150 ns in NAMD²⁶ using the constant number, volume, and temperature (NVT) ensemble to simulate the Langmuir trough experiment, with $T = 295.15$ K for comparison with experimental results.¹⁰ After 30-ns equilibration, monolayer surface tensions (γ_m), and residence times and pair correlation functions $g(r)$ of Be^{2+} with phosphate, carboxylate, and water oxygens were computed from 30 – 150 ns. To compute γ_m , pressure output was saved every 1,000 steps.

All solution ion-small molecule simulations and monolayer simulations were run in NAMD²⁶ with a 2-fs timestep using the C36 force field¹⁷ with modifications to Lennard-Jones (LJ) parameters for Be^{2+} and LJ interaction parameters between Be^{2+} and the deprotonated oxygen of each PS component molecule. A LJ force-switching function was used (10 to 12 \AA) to modulate the LJ potential at the cutoff. Long-range electrostatic interactions were evaluated with the Particle mesh Ewald (PME) method.²⁷ Temperature was held constant by Langevin dynamics with a weak coupling constant of 1 ps^{-1} in NAMD. Pressure was maintained in constant number, pressure, and temperature (NPT) simulations by a NoséHoover-Langevin piston^{28, 29} at 1 bar.

All pair correlation functions $g(r)$ were computed from trajectories using the program Visual Molecular Dynamics (VMD).³⁰ Plots of $g(r)$ were normalized in VMD unless indicated otherwise. If not normalized, the raw histogram data was plotted for comparison of relative $g(r)$ peak heights of different species pairs.

2.3. Free energy calculations.

Free energy perturbation (FEP) simulations were used to calculate the free energy of hydration (ΔG_{hyd}) of Be^{2+} , and the free energy of binding between Be^{2+} and small molecules in a given configuration (ΔG_c), according to the protocol developed by Deng and Roux.^{31, 32} The repulsive term, due to its sharp dependence on separation distance, cannot be accurately treated with a linear perturbation. Instead, a soft-core potential is used. It is found in multiple stages with a staging parameter s . The staging parameter s is set to 0.0,

0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, and 1.0. For the electrostatic term, the coupling parameter λ was increased from [0,1] in increments of 0.05, with a 0.1 window size, such that half of each window overlaps the previous window. The free energies from simulations using these different staging or coupling parameters are summed.

To calculate ΔG_{hyd} , a Be^{2+} ion in a vacuum was simulated for the initial stage of the FEP thermodynamic cycle, and in the aqueous phase for the final stage. When calculating free energies of hydration of highly charged species, the potential arising from crossing the liquid-vacuum interface, called the Galvani potential, is expected to contribute significantly:
32–34

$$\Delta G_{\text{hyd}} = \Delta G_{\text{intrinsic}} + zF\Phi. \quad [1]$$

Here, $\Delta G_{\text{intrinsic}}$ is the thermodynamic work required to move an ion from the vacuum state into the interior of pure water, and $zF\Phi$ is the work needed to cross the liquid-vacuum interface; z is the ion's charge, F is Faraday's constant, and Φ is the Galvani potential of the liquid, which has been calculated to be -0.51 V for TIP3P at standard temperature and pressure.³³ Thus, values reported for ΔG_{hyd} of Be^{2+} include $\Delta G_{\text{intrinsic}}$ (calculated from FEP simulations) and a correction of -11.76 kcal/mol to account for the Galvani potential.

To calculate ΔG_{c} for a given configuration, Be^{2+} in the aqueous phase was simulated for the initial stage, and in an appropriate binding configuration for the final stage. Standard errors between free energies calculated from at least three separate thermodynamic cycles are reported. Initial coordinates of the bound configurations for calculating ΔG_{c} were taken from the equilibrated solution simulations used to count probabilities. Water boxes were pre-equilibrated and contained between 350 and 380 waters. Production simulations of 2 ns for each staging or attenuation parameter were run using the CHARMM program³⁵ in the NPT ensemble with a timestep of 2 fs. Temperature was held constant with the Hoover thermostat³⁶ and the pressure maintained by the Nosé-Hoover piston.^{37, 38}

2.4. Fitting Lennard-Jones parameters for Be^{2+} in water.

This study introduces CHARMM LJ parameters for Be^{2+} based on the structure and energetics of the ion's interactions with water. Target experimental data for the interaction of Be^{2+} with bulk water included the free energy of hydration,³⁹ coordination number,¹⁴ and peak position of the radial distribution function, $g(r)$.²¹ Additionally, *ab initio* data of ion-monohydrate binding energy and a derivative molecular mechanics model predicting the ion-monohydrate separation distance⁴⁰ were used as target data for ion-monohydrate interaction.

Following the FEP protocol of Deng and Roux,³¹ LJ parameters for Be^{2+} were varied and the free energy of hydration (ΔG_{hyd}) in TIP3P water was calculated. The ion-monohydrate interaction energy and separation distance were also calculated using CHARMM directives. ³⁵ CHARMM LJ parameters ϵ and r^{min} were varied along a grid, with ΔG_{hyd} and monohydrate interactions calculated for values of ϵ varied from $[-0.0115, -0.0006]$ in

increments of 5×10^{-5} and r^{\min} varied from [0.2, 1.3] in increments of 0.1. The parameter set that minimized error in all three measurements was chosen.

The chosen ϵ , r^{\min} pair was then used to find the peak position of $g(r)$ and coordination number of a 5.3-molal aqueous solution of BeCl_2 . The coordination number can be found by integrating over the first peak of the radial distribution function of Be^{2+} :

$$n_{\text{coord}} = 4\pi\rho \int_0^{r_1} g(r)r^2 dr. \quad [2]$$

The integral is computed from a separation distance $r = 0$ to $r = r_1$, where r_1 is the minimum after the first peak of $g(r)$. Results for n_{coord} and $g(r)$ peak position were in satisfactory agreement with experiment.

2.5. Adjusting LJ interaction parameters to fit experimental ΔG_r .

FEP was used to obtain the association energy of each observed configuration from bulk solution simulations of divalent ions with PS components described previously. The total free energy of the reaction, ΔG_r , was calculated from the probability (p_c) and free energy (ΔG_c) of each binding configuration:

$$\Delta G_r = \sum_i \Delta G_c^i p_c^i. \quad [3]$$

ΔG_r is related to the equilibrium binding constant of the reaction from ITC (K_r^{eq}) by:

$$\Delta G_r = -kT \ln K_r^{\text{eq}}, \quad [4]$$

where k is Boltzmann's constant and T is the temperature. In this way, we compared ΔG_r calculated from simulation with the K_r^{eq} found from ITC, and adjusted simulation parameters iteratively until ΔG_r from simulation was in satisfactory agreement with the experimental value.

In the CHARMM force field, interaction energy between nonbonded pairs is the sum of the Columbic and Lennard-Jones (LJ) contributions:

$$U_{\text{non-bonded}} = U_{\text{LJ}} + U_{\text{elec}} = \sum_{\text{nonb. pairs}} \epsilon_{ij} \left[\left(\frac{r_{ij}^{\min}}{r_{ij}} \right)^{12} - 2 \left(\frac{r_{ij}^{\min}}{r_{ij}} \right)^6 \right] + \sum_{\text{nonb. pairs}} \frac{q_i q_j}{\epsilon r_{ij}}. \quad [5]$$

The first sum on the right-hand side of Eq. [5] accounts for LJ interactions, and the second for Coulombic interactions. r_{ij} is the distance between atoms i and j , ϵ is the dielectric constant of the media, and q_i is the partial atomic charge of the i^{th} atom. Energies depend on the LJ interaction parameters ϵ_{ij} and r_{ij}^{min} , given by:

$$\epsilon_{ij} = \sqrt{\epsilon_i \epsilon_j}; \quad [6]$$

$$r_{ij}^{\text{min}} = \frac{r_i^{\text{min}} + r_j^{\text{min}}}{2}. \quad [7]$$

Use of these combining rules implies lack of empirical, interaction-specific parameterization for a given pair of atom types. In the case of highly charged species, the parameters r_{ij}^{min} are doubly significant because they affect pair separation and therefore the strength of Coulomb interactions. Additionally, lack of atomic polarizability tends to augment ionic interactions at close range. Historically, pair-specific interactions have been adjusted by increasing r_{ij}^{min} .⁴¹ The value of r_{ij}^{min} can be supplied for a specific atom pair using the “NBFIX” directive in CHARMM or NAMD.

Values of r_{ij}^{min} were varied for each Be^{2+} /small molecule pair until ΔG_r from simulation reached satisfactory agreement with the value found from ITC binding experiments. Interacting atom pairs and values of r_{ij}^{min} tested for each pair can be found in supplemental information Table S1.

Because DMP and acetate each present Be^{2+} with a single binding site at biological pH,⁴² solution configurations of these molecules were defined as the number of associated small molecules per Be^{2+} ion (N_{SM}). Probabilities of configurations with 0, 1, 2, 3, or 4 associated small molecules ($N_{\text{SM}} = 0, 1, 2, 3, \text{ or } 4$) were counted using the integral of the pair correlation function from Be^{2+} /small molecule simulations. For example, it was observed that before adjusting LJ interaction parameters, Be^{2+} could take two possible configurations in association with DMP: It could associate with 2 or 3 molecules of DMP. The $g(r)$ of Be^{2+} with the deprotonated oxygen of DMP (O_{dp}) was used to count probabilities of bound configurations.

The number of binding events per Be^{2+} ion, $N_{\text{Be}^{2+} - \text{O}_{\text{dp}}}$, is associated with the integral of the pair correlation function:

$$N_{\text{Be}^{2+} - \text{O}_{\text{dp}}} = 4\pi\rho \int_0^{r_1} g(r)_{\text{Be}^{2+} - \text{O}_{\text{dp}}} r^2 dr. \quad [8]$$

Here, $g(r)_{\text{Be}^{2+} - \text{O}_{\text{dp}}}$ is the pair correlation function of the separation distance between Be^{2+} and O_{dp} . $N_{\text{Be}^{2+} - \text{O}_{\text{dp}}}$ is the average number of O_{dp} associating with a single Be^{2+} ion. The average binding distance is the position of the first peak of $g(r)_{\text{Be}^{2+} - \text{O}_{\text{dp}}}$, and the integral is computed over the first peak.

From $N_{\text{Be}^{2+} - \text{O}_{\text{dp}}}$, the probability of each divalent ion associating with 0, 1, 2, 3, or 4 PS component molecules can be calculated by solving a system of linear equations. The system of equations chosen depends on the possible values of N_{SM} . The sum of all configuration probabilities equals 1:

$$p_0 + p_1 + p_2 + p_3 + p_4 = 1. \quad [9]$$

Here, p_i is the probability of a divalent ion associating with i small molecules. To avoid double-counting of free divalent ions, p_0 was included with p_1 when calculating $\Delta G_r(p_{1/0} = p_1 + p_0)$, because dissociation was observed in FEP simulations where $N_{\text{SM}} = 1$ and $p_0 > 1$. Configurations with probabilities less than 0.02 were neglected. Systems of equations used to find configuration probabilities before and after adjustment of r_{ij}^{min} can be found in Table 1.

2.6. Analyzing DOPS monolayer trajectories.

Interfacial tensions (γ_m) are calculated from simulation using the diagonal elements of the pressure tensor.⁴³

$$\gamma_m = 0.5 \left(L_z \left[P_{zz} - 0.5(P_{xx} + P_{yy}) \right] \right). \quad [10]$$

Here, L_z is the size of the simulation box normal to the interface, P_{zz} is the normal component of the pressure tensor, and P_{xx} and P_{yy} are the tangential components. The prefactor of 0.5 is needed to account for the presence of two water-lipid interfaces in the simulation box. For comparison, γ_m can be calculated from experimental surface pressures (π) by subtracting π from the surface tension of pure water (γ_0): $\gamma_m = \gamma_0 - \pi$.⁴⁴ At $T = 295.15$ K, $\gamma_0 = 72.5$ dyn/cm.⁴⁵ Error in γ_m from simulation was estimated from the standard deviation of samples computed over 1-ns blocks.

Residence times of divalent ions at DOPS monolayer binding sites were computed from 30 – 120 ns using the CHARMM program³⁵ and standard errors were computed. From the residence times, expected occupancies were also computed using CHARMM, here defined as the expected number of associations with interacting DOPS oxygen a given time (can be greater than 1). Be^{2+} and O_{DP} are considered to associate if they are found within association distance r_{cut} , which is 2.1 and 2.5 Å for phosphate and acetate oxygens, respectively, for Be^{2+} ; and within 3.4 Å for both species with K^+ . Water bridging

associations were analyzed using the CHARMM directive “ncoor hbond” with “cuthb” set to 2.5 Å between associating species and TIP3P water residues.

3. Results

3.1. ITC results.

Two possible coordinating atoms for Be²⁺ in the surface-exposed headgroup of PS are the phosphoryl oxygen (above the glycerol-ester linkage) and the carboxylate oxygen (headgroup terminal). Acetate and DMP, shown in Fig. 1, were chosen as model compounds as they carry the same types of cation-coordinating oxygen atoms. DOPS, used in monolayer simulations, is also shown in Fig. 1.

Be²⁺ is known to interact strongly with phosphate oxygen,⁴⁶ which is here assumed to prevent Be²⁺ from penetrating to the carbonyl oxygens located deeper along the bilayer normal. Monolayer simulations (discussed in Sec. 3.4) corroborate this assumption; Be²⁺ was not seen to interact with ester carbonyls due to strong coordination by phosphate oxygens.

Results in Table 2 indicate that Be²⁺ binds to DMP with moderate affinity ($K_d \sim 2$ uM), and with much weaker affinity to acetate ($K_d \sim 3$ mM). ΔG is negative and H positive, indicating entropically-driven reactions, likely due to liberation of water when ions are dehydrated. The control titrations shown in Fig. 2A and C indicate a large heat of dilution for aqueous DMP, but not for acetate. Subtracting the heat of dilution of DMP reverses the sign of H for DMP + Be²⁺ from negative to positive at the experimental pH, temperature, and concentration levels (Fig. 2B). Strong association with phosphate comports with a known property of Be²⁺; above pH 3, Be²⁺ precipitates in phosphate buffer, even in the presence of chelating ligands such as DHBA.⁴⁶

See supplemental information Figs. S4 and S5 for plots of the raw ITC data from all experiments, including three replicates each of Be²⁺ interacting with DMP and acetate.

Fig. 2D and E show the fit to the integrated heat of a single trial each of DMP and acetate titration. It is likely that full saturation was not reached in these experiments due to limitations inherent in the systems. This may cause systematic errors in estimates of H or n not reflected in the standard errors in these measurements. The slopes of each fit are clearly defined indicating accurate measure of the rate of change of heat with respect to relative concentration. To assure accurate calculation of K_r^{eq} , neither H nor n were fixed during fitting. From these reliably converging fits the K_r^{eq} parameter is extracted.¹⁶

3.2. CHARMM LJ parameters for Be²⁺ interactions with water.

Following the iterative procedure described in Sec. 2.4, in which Be²⁺ with various values of the LJ parameters r_i^{\min} and ϵ_i was evaluated for energetic and structural interactions with water, LJ parameters were chosen which yielded satisfactory agreement with all observables. Final LJ parameters for Be²⁺ are $\frac{1}{2}r_i^{\min} = 0.8085$ Å; $\epsilon_i = -0.000825$ kcal/mol. The binding

radius is lower in magnitude than other ions⁴⁷ in the CHARMM FF, reflecting the great binding capacity of this small divalent ion. The next-smallest binding radius of 1.18 belongs to Mg^{2+} . The energy well is shallower than that of Li^+ , which has $\epsilon_j = -0.0023$ kcal/mol,^{32, 48} and considerably shallower than that of the larger Ca^{2+} ($\epsilon_j = -0.12$ kcal/mol).⁴⁹ The shallower LJ energy well contributes to beryllium's low coordination number ($n=4$).

Be^{2+} solution and monohydrate results are listed in Table 3. Final Be^{2+} LJ parameters yield improved agreement with experimental properties of 5.3-molal BeCl_2 solutions, with a $g(r)$ peak position of 1.55 Å and a coordination of 3.94, both within 10 % of experimental values (1.66 Å and 4, respectively^{14, 21}). ΔG_{hyd} underestimates experiment by 9 % at 298.15 K (in magnitude). This is because energetic and structural properties were found to be at odds. For example, use of a lower r_{min} parameter for Be^{2+} would bring ΔG_{hyd} in closer agreement with experiment, but also decrease the $g(r)$ peak position.

Fig. 3 plots $g(r)$ for Be^{2+} in a 5.3-molal solution of BeCl_2 . The pair correlation function between Be^{2+} and water differs from the total $g(r)$ (between Be^{2+} and water/ Cl^-) in that it has a distinct secondary peak attributable to Be^{2+} - Cl^- interactions. In the experimental study by Yamaguchi et al.,²¹ $g(r)$ between Be^{2+} and Cl^- is not deduced from experiment, but the authors note a decrease in Cl^- coordination by water oxygen in the presence of Be^{2+} , indicating association of the two ionic species at this concentration.

QM results for ion-monohydrate interaction energy and separation distance, listed in Table 3, are borrowed from a study by Yang et al.⁴⁰ The ion-monohydrate separation distance was computed with the atom bond electronegativity equalization method fused with molecular mechanics (ABEEM/MM). ABEEM and van der Waals parameters were fit to the interaction energies. As with solution properties, simulation results from the present study are within 10 % deviation from expected values. Final LJ parameters represent a compromise between accurate interaction energy and separation distance.

3.3. Divalent ion/small molecule interactions and simulation parameters.

With the LJ parameters fit to water interactions, Be^{2+} showed significant overbinding to both DMP and acetate. This is an expected result from a nonpolarizable FF, in which close-range ionic interactions are not modulated by adjustment of effective atomic dipole moments.

Increasing the r_{ij}^{min} interaction parameter between Be^{2+} and interacting oxygens was sufficient to decrease binding probability and bring ΔG_r within 10 % deviation from ITC results. Table 4 lists the adjusted interaction parameters. For all atom type pairs, the default value was 2.51 ($\epsilon = -0.12$ kcal/mol and $\frac{1}{2}r_i^{\text{min}} = 1.7$ Å for all three oxygen types). The lipid FF required a lesser increase in r_{ij}^{min} than the CGEN FF, likely due to the reduced magnitude of charge assigned to OCL relative to OG2D2 (-0.67 and 0.76, respectively). Full charge distributions for both models can be found in supplemental information Appendix S1.

Table 5 compares configuration states and probabilities before and after adjustment of r_{ij}^{\min} . It also gives the integration of the pair correlation function $N_{\text{Be}^{2+} - \text{O}_{\text{dp}}}$, from which the numbers of associated molecules, N_{SM} , are computed. Because configurations are counted by the number of DMP or acetate ions bound to a single Be^{2+} atom, clustering is not reflected. Solution simulations with the original LJ parameters did exhibit clustering, but simulations with the adjusted parameters did not.

Table 6 compares resulting ΔG_{r} with experiment and shows the extent of overbinding when parameters fit to water interactions are used. Interestingly, Be^{2+} binds more tightly to carboxylate than phosphate with the original r_{ij}^{\min} values (ΔG_{r} is more negative), but both interactions are grossly overestimated. This is significant because, in DOPS bilayers and monolayers, carboxylate sits at the water-lipid interface and encounters solvated Be^{2+} before phosphate. Overbinding to carboxylates could prevent Be^{2+} from penetrating deep enough into the headgroup region to bind with phosphate. Final r_{ij}^{\min} parameters yield ΔG_{r} that agrees with experiment for Be^{2+} and acetate and slightly overestimates binding affinity with the phosphate oxygen.

Fig. 4 compares $g(r)_{\text{Be}^{2+} - \text{O}_{\text{dp}}}$ before and after adjustment of lipid FF parameters. Note the adjustment of the LJ interaction parameters increased the separation distance between bound Be^{2+} and O_{dp} , and decreased the height of the first peak of $g(r)_{\text{Be}^{2+} - \text{O}_{\text{dp}}}$, both indicating weaker binding after adjustment of the LJ interaction parameters. Additionally, $g(r)_{\text{Be}^{2+} - \text{O}_{\text{dp}}}$ are very similar before parameter adjustment; the curves overlap but DMP peak is slightly higher. Coordination number, determined by integration of the first peak of $g(r)$, is greater for DMP than acetate after adjustment, and coordination is tighter, as can be seen from the closer $g(r)$ peak position.

Fig. 5 shows sample configurations of Be^{2+} in solution with DMP (lipid FF), and similar shots with acetate (lipid FF) can be found in supplemental information Fig. S6. In both figures, water and Na^+ ions are present but not shown. Default parameters show extensive clustering with DMP, but the resulting ΔG_{r} is too favorable, indicating these configurations are not realistic. Less clustering is seen with default acetate interaction parameters. In both DMP and acetate systems, adjustment of r_{ij}^{\min} reduces clustering.

3.4. DOPS monolayer surface tensions and Be^{2+} coordination.

Surface tensions of DOPS monolayers (γ_{m}) calculated from simulation agree with experiment for both Be^{2+} with adjusted interaction parameters and K^+ . A sample time series of γ_{m} for a DOPS monolayer with bound Be^{2+} and $A_{\text{l}} = 65.3 \text{ \AA}^2/\text{lipid}$ can be found in supplemental information Fig. S7. $A_{\text{l}} = 65.3 \text{ \AA}^2/\text{lipid}$ is of interest because it is the experimental A_{l} for DOPS membranes at 303.15 K.⁵⁰ γ_{m} for the sample trajectory fluctuates between 40 and 70 dyn/cm, with a mean of 52.8 dyn/cm calculated from 30 to 150 ns.

As has been demonstrated experimentally,¹⁰ γ_m and A_f are directly related along a pressure-area isotherm; γ_m is higher at greater A_f . Fig. 6 plots the experimental data (provided by Ermakov et al.¹⁰) for DOPS monolayers in solutions of 1 mM Be^{2+} or K^+ . In the Langmuir experiments, the subphase solution contained 10 mM KCl as a background electrolyte and buffered with 2 mM Tris-HCl (pH 7.3). DOPS monolayers with Be^{2+} exhibit a greater γ_m than with K^+ . At equal γ_m , DOPS monolayers in the presence of Be^{2+} have a lesser A_f , indicating that Be^{2+} has a compacting effect on the monolayer. This can be attributed to both strong ionic interactions with the divalent ion and the smaller radius of Be^{2+} relative to K^+ . While not as strong as direct ion-oxygen associations, our findings also indicate that Be^{2+} is able to associate with phosphoryl and carboxylate oxygens through water bridging (see below).

Table 7 compares simulation results for γ_m , calculated using Eq. [10], with experimental results.¹⁰ Because experimental concentrations were too low to match with the simulation box size used, enough ions were added to equilibrate the system (40 Be^{2+} and 80 K^+). In Be^{2+} -DOPS systems, Be^{2+} saturated the monolayer and, due to long residence times, dissociated infrequently. The bulk concentration of Be^{2+} in these simulations therefore accurately represents the experimental concentration, in which Be^{2+} freely saturated the DOPS monolayers and existed in solution in concentrations too low to simulate. Experimental values for γ_m at 65.3 and 71.6 $\text{\AA}^2/\text{lipid}$ are reproduced in simulation using the adjusted interaction parameters. A snapshot for the distribution of Be^{2+} in an equilibrated monolayer simulation can be seen in Fig. 7.

Fig. 8 compares pair correlation functions $g(r)$ for Be^{2+} with various oxygens in DOPS monolayer simulations at 65.3 $\text{\AA}^2/\text{lipid}$. The carboxylate peak below 2 \AA is too small to be visible in $g(r)$ for all oxygens (black line), but the phosphate peak is clearly visible. From $g(r)$ for all oxygens, it is evident that more associations occur with water oxygens than with phosphate oxygens (the integral of this peak is greater). Supplemental information Fig. S8 compares $g(r)$ between K^+ and oxygen species.

Preferential association with phosphate relative to acetate is not seen in K^+ simulations, although K^+ has not been specifically parameterized for these interactions. Solubility data of acetate and phosphate salts indicate that phosphate associates more strongly with ions in general, and with potassium in particular: Potassium acetate is about 17 times as soluble as potassium dihydrogen phosphate at standard temperature and pressure.⁵¹ Additionally, the bond dissociation energy of potassium from trimethyl phosphate as determined by threshold collision-induced dissociation (CID) is similar to that of potassium with acetone and greater than with methanol (135, 140, and 92 kcal/mol, respectively).⁵² Dissociation energies reveal that sodium binds more favorably to trimethyl phosphate than both acetone and methanol (171, 145, and 111 kcal/mol, respectively). Therefore, even fully methylated phosphate associates strongly with ions in solution, with equal or greater affinity than acetate binding sites. However, specific binding affinities of potassium with acetate and dimethyl phosphate are not known.

While $g(r)$ for Be^{2+} with lipid and water oxygens is similar at 71.6 and 65.3 $\text{\AA}^2/\text{lipid}$, there is one notable difference: The more condensed monolayer shows close association with

carboxylates, as can be seen from the pair correlation function of Be^{2+} with carboxylate oxygens in Fig. 9. The $g(r)$ for the condensed monolayer has a sharp first peak at 1.85 Å, which is lacking in the monolayer with 71.6 Å²/lipid. Both monolayers have secondary peak around 3.5 Å due to the proximity of the carboxylate oxygens to phosphate oxygens, which sit an average of 3.5 Å apart in these simulations.

Tables 8 and 9 quantify the associations between Be^{2+} or K^+ and various oxygens in DOPS monolayer simulations. Ion-oxygen associations in Table 8, computed from pair correlation functions, confirm that Be^{2+} only associates with carboxylate oxygen in the more condensed monolayer (65.3 Å²/lipid). As would be expected, Be^{2+} associated with more lipid oxygens overall at 65.3 than at 71.6 Å²/lipid; 1.84 and 1.64 associations, respectively. Each K^+ ion associates with about 1 lipid oxygen, and some K^+ is solvated. Table 9 lists the average oxygen-ion residence times and occupancies computed from time series of bond distances. For example, the 0.42 expected occupancy for phosphoryl oxygen and Be^{2+} signifies that a given phosphoryl oxygen will coordinate an average of 0.42 Be^{2+} ions at a given time. While the residence time for Be^{2+} associations with phosphoryl oxygens in DOPS monolayers is significant (about 1/4 of the trajectory length used in the calculation), dissociations do occur. The residence time for associations with carboxylate oxygens, which only occur at higher A_l , is much shorter. This is expected given the greater magnitude of ΔG_r between Be^{2+} and phosphoryl oxygen found from ITC experiments. Residence times for K^+ associations are three orders of magnitude smaller than those for Be^{2+} -phosphate interactions and are similar for phosphoryl and carboxylate oxygens. K^+ expected occupancies are higher with carboxylate than phosphoryl oxygen, but parameterization of the relevant interaction parameters for potassium is needed to infer physical significance of this difference.

Supplemental information Fig. S9 is a histogram of residence times for Be^{2+} -phosphate associations with $A_l = 65.3$ Å, disregarding association times < 20 ps. Binding events can be separated into three regimes by duration of association. Twenty-one associations endured for the length of trajectory analyzed (90 ns), and another large group dissociated in less than 20 ns. A third regime of 15 associations were stable, but not as long, lasting between 20 and 60 ns. The total number of associations is 67, 1.67 times the number of Be^{2+} ions in the simulation. Adding associations in the middle regime and the group that did not dissociate yields 21 + 15 = 36, nearly the number of Be^{2+} ions in the simulation. Thus, each Be^{2+} ion is coordinating an average of one or two lipids, and while some of these associations are weak, most Be^{2+} ions tightly coordinate a single phosphoryl oxygen. Fig. 10 shows sample Be^{2+} -ion coordination by DOPS headgroups and snapshot bond distances.

Where Be^{2+} associates with water, it can form water bridges with both phosphoryl and carboxylate oxygens. Table 9 reports bridging residence times and expected occupancies (“+ water” columns). Decreased association times (ps rather than ns scale) for bridging events indicate the expected weakness of bridged hydrogen bonding relative to direct associations. Bridging between Be^{2+} and carboxylate oxygens was more common than with phosphoryl oxygens. This is because direct association between Be^{2+} and phosphoryl oxygen positions carboxylate oxygen at an appropriate distance for a bridging event. Fig. 10D. shows an

example configuration of Be^{2+} directly coordinating phosphoryl oxygen and coordinating carboxylate oxygen through a water bridge. Bridging events were not significantly influenced by A_j .

4. Discussion and Conclusions

Previous attempts to parametrize cation interactions with coordinating groups for MD simulations were focusing primarily on ion solvation by water.^{47, 53} More recently, a study by Lou and Roux⁴¹ used osmotic pressure results for sodium and potassium chloride solutions at concentrations from 1 to 5 M to obtain the relevant r_{ij}^{min} parameters. This range of concentrations is a factor of 10 greater than physiologically relevant concentrations and the question how well these parameters represent diluted solutions remains.

In this study, we first adjusted LJ parameters for Be^{2+} interactions with water to reflect the known free energy of ion solvation.^{21, 39, 54} We then performed ITC titrations of Be^{2+} with small molecules representing components of PS to determine the free energies of ion interaction with phosphoryl and carboxylate oxygens separately. The results indicate strong association with phosphate oxygen in solution, and considerably weaker association with carboxylates. While previous work^{12, 13, 41, 55} has relied on osmotic pressure data to find appropriate values for interaction parameters r_{ij}^{min} between ion-oxygen pairs, the goal of this study is to observe effects of ion binding (close interactions), of which ITC data is a more direct measure. Osmotic pressure experiments always characterize ionic interactions in fairly concentrated solutions and for this reason may overlook dominant modes for binding which occur in a lower concentration range.

Results reported by Venable et al.¹² indicate that r_{ij}^{min} interaction parameters for Na^+ and K^+ ions based on osmotic pressure data are reasonably transferable to simulations of anionic lipid bilayers with these ions. They found that use of osmotic pressure data to correct sodium and potassium overbinding to carboxylates in palmitoyloleoyl phosphatidylserine (POPS) membranes did reduce deuterium order parameters of the palmitate chains, bringing results in closer agreement NMR results. However, they consider interactions of lower affinity. In our case, experimental affinities of Be^{2+} for anionic phospholipids are in the micromolar range, which is most suitable for ITC⁵⁶, which is also capable of detecting more than one type of binding sites characterized with different affinities.

LJ parameters for Be^{2+} improve agreement with solution and monohydrate properties obtained from experiment and QM, including free energy of hydration, coordination number, and ion-monohydrate separation distance and interaction energy. While agreement in all measurements is within 10%, structural and energetic results are at odds, indicating the need for a more complex force field to describe solubility of this strongly-interacting ion. A study by Yang and Li⁴⁰ used QM calculations of ionic interactions with 1 – 7 water molecules to develop LJ parameters for Be^{2+} , Mg^{2+} , and Ca^{2+} to accompany their seven-site flexible water model with fluctuating charges. While results for Be^{2+} interaction energies and separation distances agreed well with QM results, the hydration shell for Be^{2+} was larger than expected in solution (5.8 water molecules), causing the authors to echo the conclusion

that Be^{2+} requires a more complex treatment of nonbonded potential. Azam et al.⁵⁷ obtain accurate first hydration shell bond averages and coordination numbers using QM charge field molecular dynamics (QMCF/MD) to model a single hydrated Be^{2+} ion. QMCF/MD utilizes a partitioning scheme in which the system is divided into two parts. The chemically most relevant region, in this case the ion and first and second hydration shells, are treated by *ab initio* quantum mechanics. The remaining part of the system evolves under an empirical potential. This is computationally expensive relative to all-atom MD and restricts the focus of the simulation to the immediate vicinity of a particular reaction. The authors do not report solution energetics.

Use of the new Be^{2+} LJ parameters (given in Sec. 3.2) in solution simulations with components of PS result in overbinding to both acetate and dimethyl phosphate, causing clustering. The CGEN FF model for soluble acetate¹⁸ exhibits the most overbinding to Be^{2+} before parameter adjustment, binding even more tightly than to DMP. The carboxylate model based on the lipid FF, which carries a lesser partial charge on the free oxygen (-0.67 rather than -0.76), still exhibits overbinding. Adjustment of the LJ interaction parameter r_{ij}^{\min} sufficiently reduces binding to all small molecules in solution.

This aspect was not taken into account in a recent study of Be^{2+} -PS interactions. To study Be^{2+} -PS interactions with the C36 FF, Ermakov et al.¹⁰ approximated LJ parameters for Be^{2+} by borrowing from $\epsilon_j\text{Ca}^{2+}$ ($\epsilon_j = -0.12$, more negative than the present results derived empirically) and setting $r_{ij}^{\min} = 0.35 \text{ \AA}$ based on experimental Be-O bond distances. The resulting “small calcium” (smallCa^{2+}) yielded the expected coordination number (4), but interaction energies with PS coordinating groups were not considered individually. smallCa^{2+} was seen to coordinate both carboxylate and phosphate oxygens when Be^{2+} was added to simulations of DOPS bilayers in the presence of sodium chloride. As with the present study, dissociations were infrequent, and smallCa^{2+} was rarely found free in solution at this concentration. The present study shows that coordination of PS binding sites is heavily dependent on interaction parameters. Adjustment of r_{ij}^{\min} to reflect stronger binding to phosphate oxygens results in pronounced preference for binding to phosphoryl over carboxylate oxygens.

Pair correlation functions directly reflect association probabilities and together with free energy calculations provide a statistical accounting for the free energy of binding in solution. The free energies of Be^{2+} interaction with water and dimethyl phosphate in solution are similar; free energy of hydration is -572 kcal/mol ,³⁹ and binding to dimethyl phosphate is -6.49 kcal/mol more favorable. Parameterization of Be^{2+} -oxygen interactions is therefore a fine-tuning of two reactions with similar affinities, hydration and binding in solution. We found that even in a saturated solution, a single Be^{2+} ion associates with only one or two dimethyl phosphate molecules and maintains associations with water. Associations with acetate in solution are considerably weaker. A Be^{2+} ion may associate with a single acetate molecule, and dissociations are frequent. Final LJ interaction parameters describing Be^{2+} -phosphate and -acetate binding agree well with the equilibrium constants for these reactions found from ITC experiments.

Analysis of K^+ associations with DOPS oxygens indicate it binds preferentially to carboxylate over phosphoryl oxygens. However, K^+ has not been specifically parameterized for associations with acetate and dimethyl phosphate. Solubility data⁵¹ and dissociation energies⁵² indicate K^+ may bind with greater affinity to phosphoryl oxygens in solution. This would corroborate the present results for Be^{2+} , which associates much more strongly with dimethyl phosphate than acetate. Fine tuning the force field for K^+ with lipids may be needed but is not the focus of this work.

Surface tensions of DOPS monolayers, recorded in Langmuir experiments, are dependent on salt species and concentration in the subphase. Relative to Ca^{2+} , which has a larger atomic radius, and to monovalent K^+ , Be^{2+} has a compacting effect on DOPS monolayers in these experiments.¹⁰ Revised interaction parameters for Be^{2+} with phosphate and carboxylate oxygens reproduce experimental surface tensions for DOPS monolayers and show compaction relative to monolayers equilibrated with K^+ . In these simulations, Be^{2+} preferentially associates with phosphate oxygens and maintains associations with water, which penetrates the monolayer. While some associations between Be^{2+} and carboxylates are present in simulations with $65.3 \text{ \AA}^2/\text{lipid}$ (equivalent to experimental A_1 at 303.15 K)⁵⁰, less condensed monolayers ($71.6 \text{ \AA}^2/\text{lipid}$) show no associations with carboxylates.

The new parameters for Be^{2+} developed in this study open possibilities of realistic visualization of multiple biochemical processes where we expect interference of this small dication underlying its toxicity. This includes competition between Ca^{2+} and Be^{2+} at the surface of phosphatidylserine-containing membranes and domains, Be^{2+} interference with phosphatidylserine recognition by its receptors on macrophages, components of coagulation cascade, and Ca^{2+} -dependent membrane fusion machinery. A few more steps will be required for full parametrization of this cation for simulations with proteins.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

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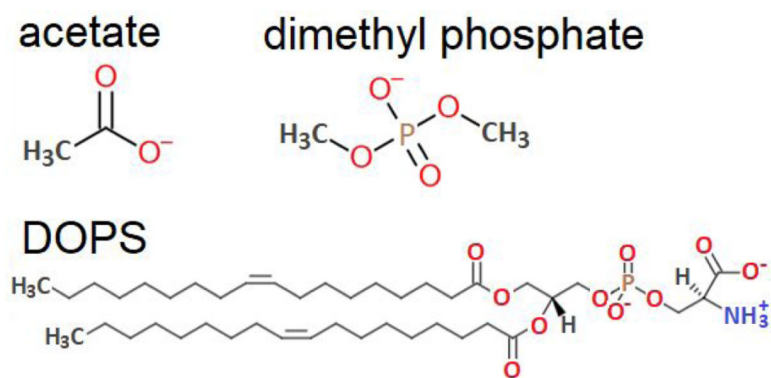


Figure 1. Structures of acetate, dimethyl phosphate, and DOPS.

DOPS with denoted positions of electronegative ion-binding atoms; and structures of small molecules, acetate and dimethyl phosphate, carrying similar types of oxygens and representing separate ion-binding components of PS.

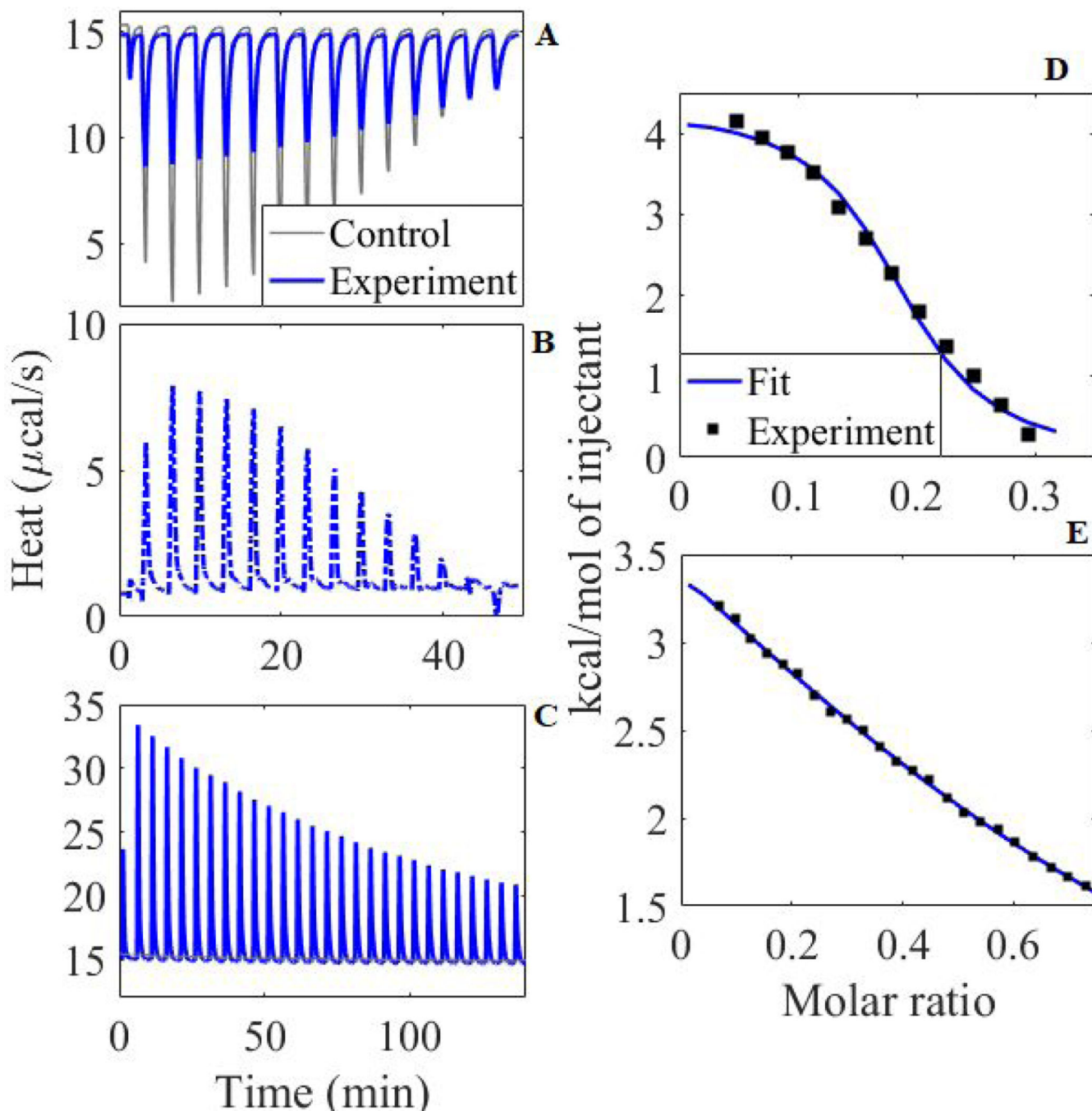


Figure 2. Titration Results.

Raw titration data for Be^{2+} into DMP solution (A), with control subtracted (B), and into acetate solution (C); integrated heat for Be^{2+} into DMP solution (D) and acetate solution (E). In integrated heat plots, molar ratio is shown for small molecule/ Be^{2+} in cell, and control was subtracted from integrated heat. Control in (C) is present but not visible at around 15 kcal/mol.

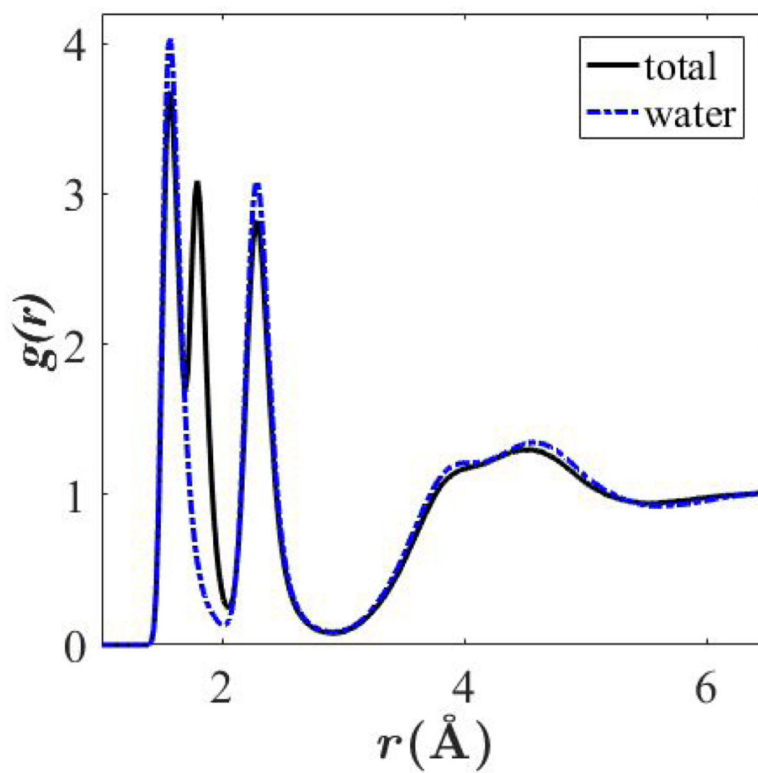


Figure 3. Radial distribution functions for 5.3-molal BeCl solution.

Total radial distribution function for Be^{2+} (black; Be^{2+} with water and Cl^-) and pair correlation function for Be^{2+} with water (blue).

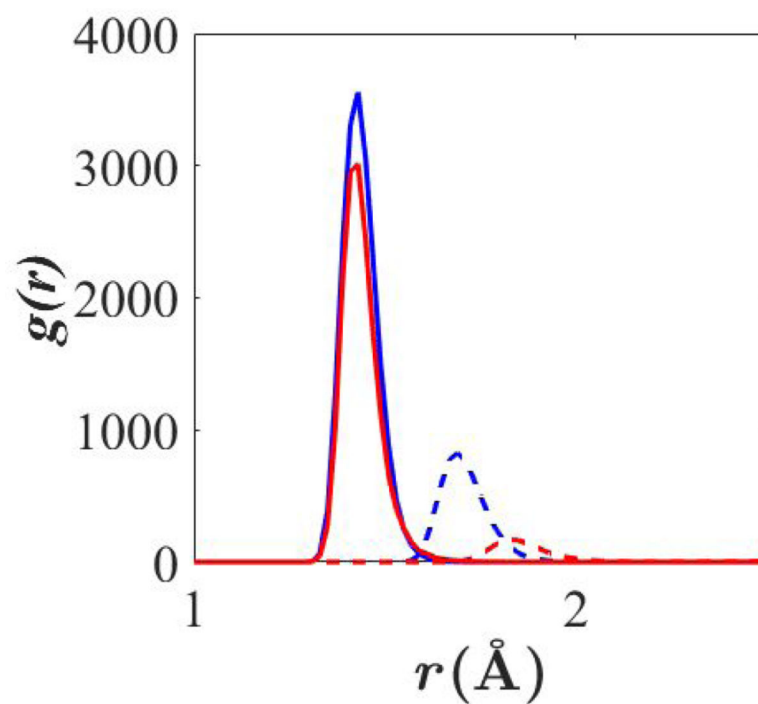


Figure 4. $g(r)_{\text{Be}^{2+} - \text{O}_{\text{dp}}}$ between Be^{2+} and free deprotonated oxygens.

Blue: DMP. Red: acetate. Solid: initial r_{ij}^{min} . Dashed: final r_{ij}^{min} . Lipid FF parameters used.

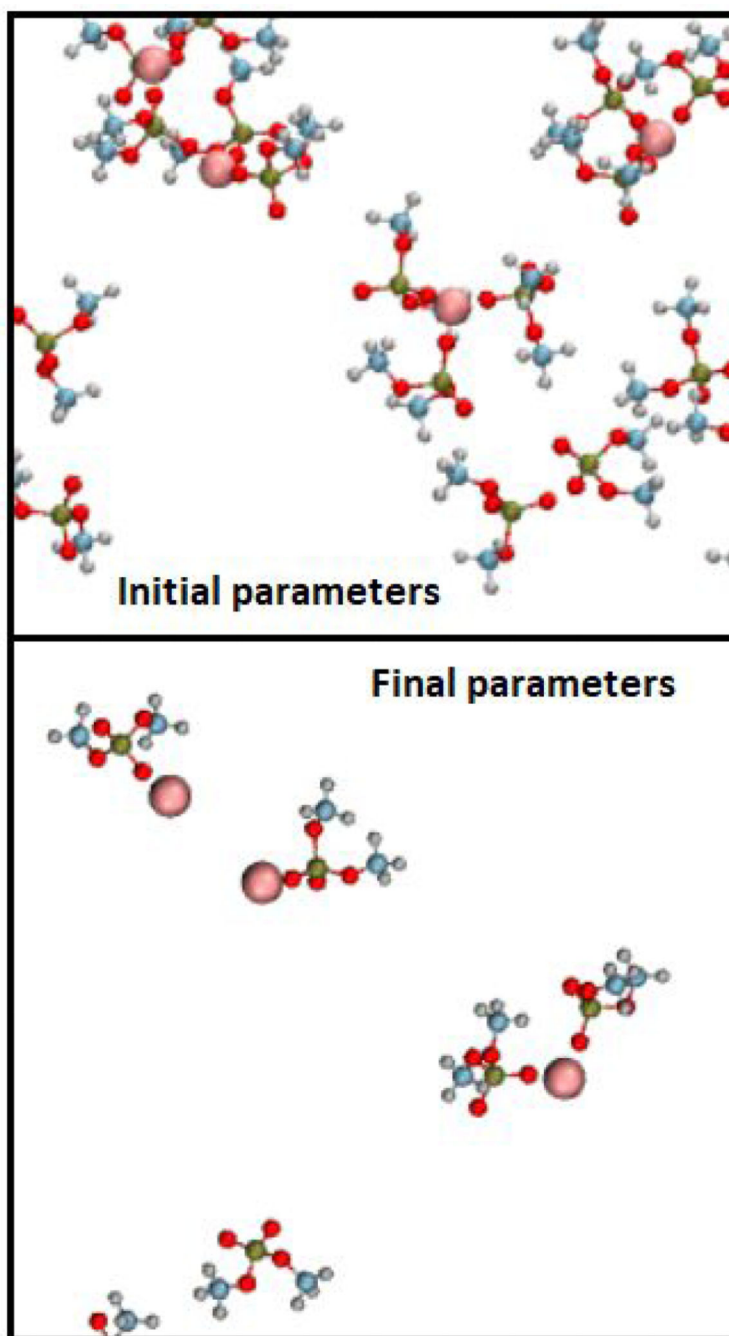


Figure 5. Be^{2+} in solution with DMP.

Default (top) and adjusted (bottom) LJ interaction parameters. Colors: Be^{2+} , pink; O, red; C, blue; H, gray; P, gold. Water and Na^+ ions not shown.

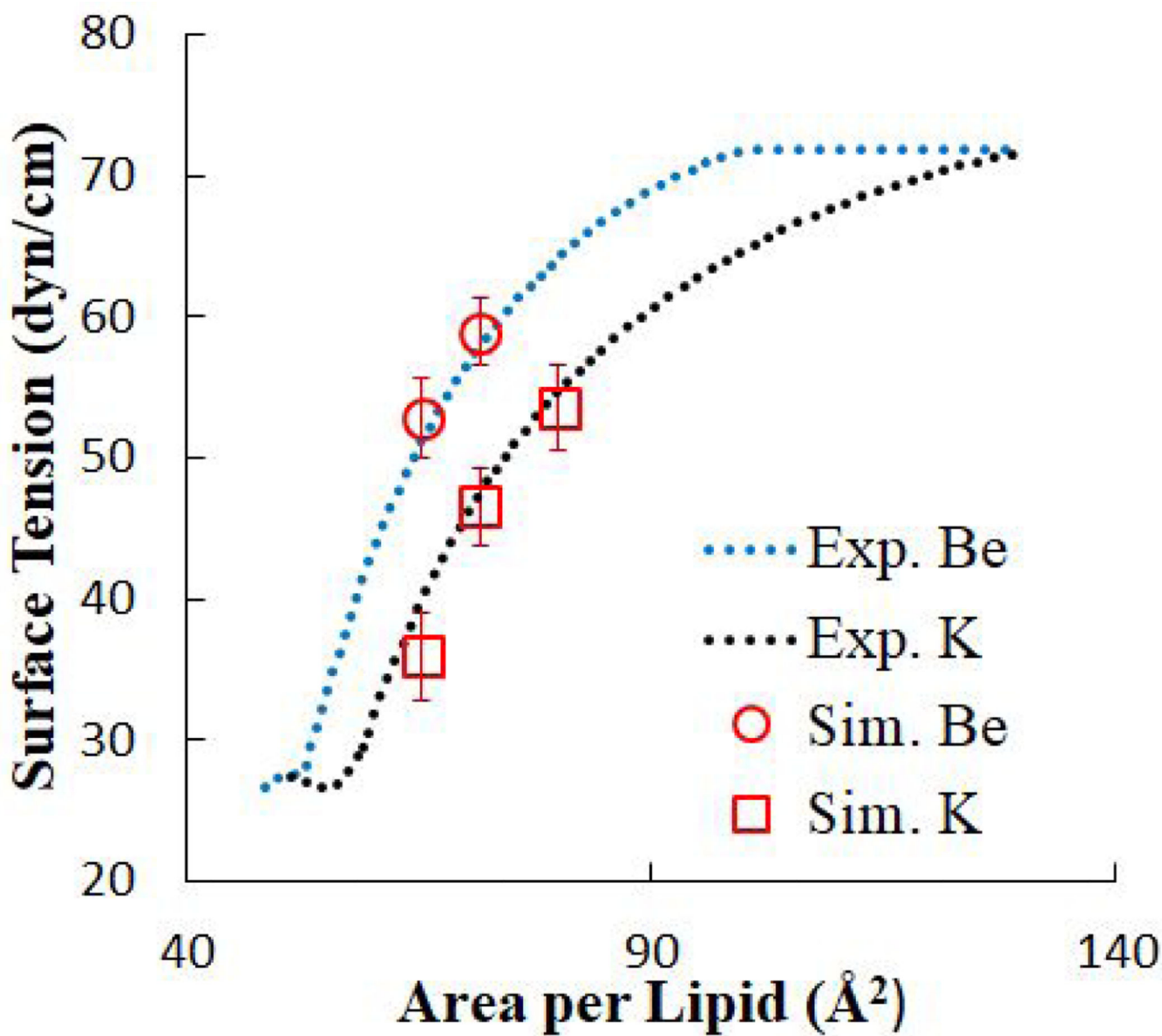


Figure 6. DOPS surface tension isotherms from Langmuir monolayer experiments and simulation.

Bulk ion concentration in experiment: 1mM.¹⁰

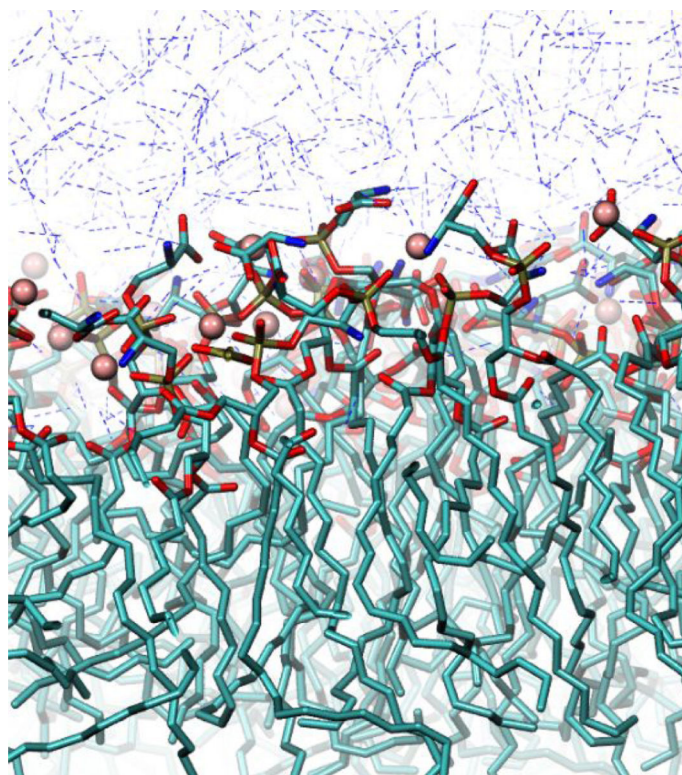


Figure 7. DOPS monolayer with bound Be²⁺.
 $A_l = 65.3 \text{ \AA}^2$. Be²⁺: pink sphere, C: teal licorice, O, red licorice, P: gold licorice, N: blue licorice, water: blue dashed.

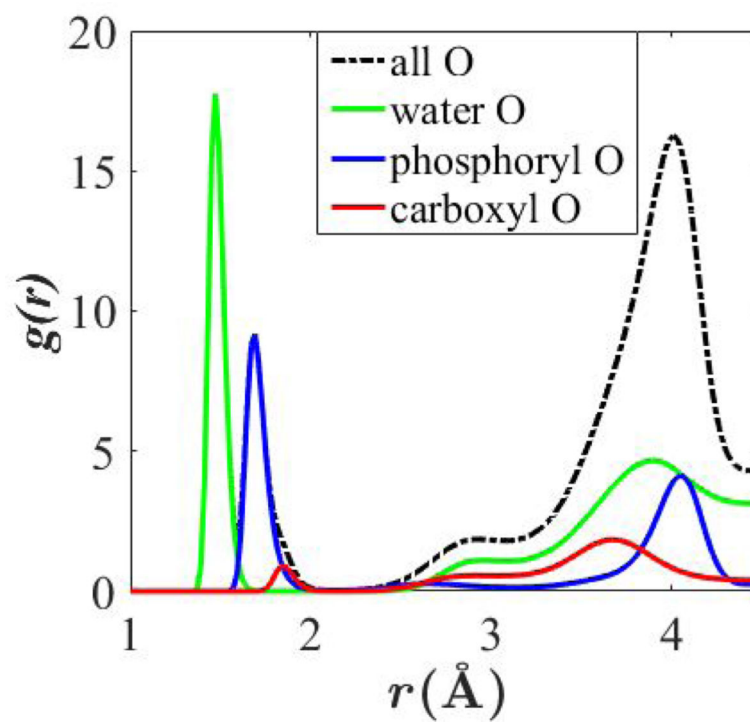


Figure 8. Pair correlation functions of Be^{2+} with various oxygens. $A_l = 65.3 \text{ \AA}^2/\text{lipid}$. For comparison, $g(r)$ are not normalized.

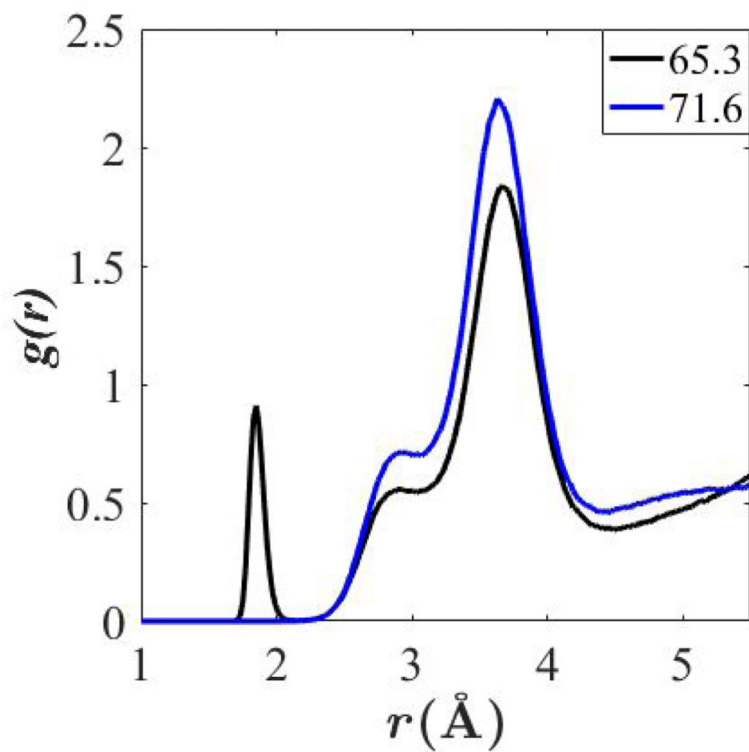


Figure 9. Pair correlation functions of Be^{2+} with DOPS carboxylate oxygens. Averaged over last 60 ns of trajectory for DOPS monolayer simulations with 65.3 and 71.6 $\text{\AA}^2/\text{lipid}$. $A_l = 65.3 \text{ \AA}^2/\text{lipid}$. For consistency with Fig. 8, $g(r)$ are not normalized.

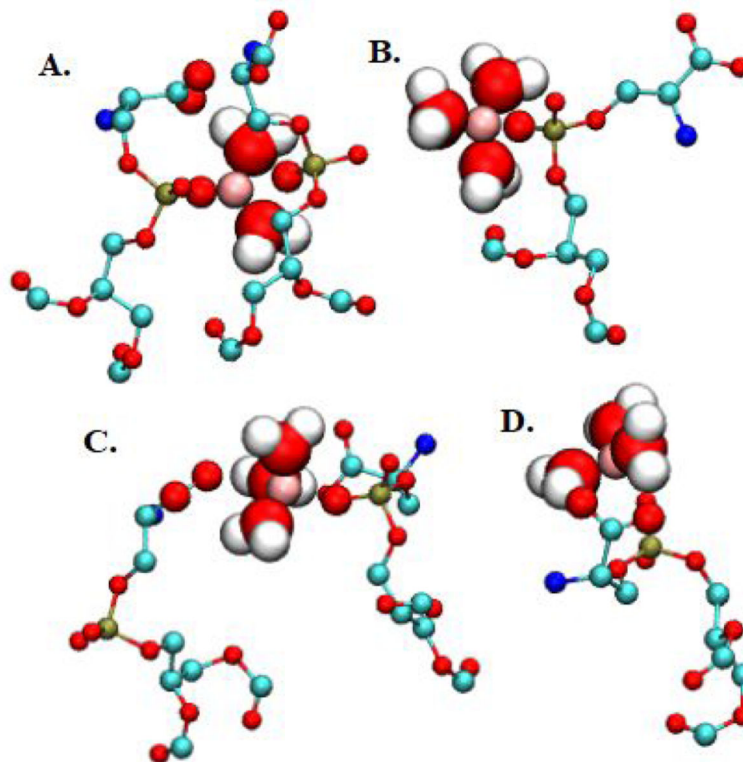


Figure 10. Common Be^{2+} binding configurations in DOPS monolayers. DOPS headgroups and Be^{2+} shown. Snapshot bond lengths (\AA) in parentheses. A. Be^{2+} (pink sphere) coordinating 2 phosphate oxygens (1.68 and 2.7) and 2 water oxygens (avg. 1.48). B. Coordinating 1 phosphate oxygen (1.75) and 3 waters (avg. 1.51). C. Coordinating 1 acetate oxygen (2.5), 1 phosphate oxygen (1.77), and 3 waters (avg. 1.78). D. Water bridge with acetate (3.4 between Be^{2+} and acetate O; 2.0 between acetate O and water H; 1.5 between Be^{2+} and water O). Colors: C: teal licorice, O: red licorice, P: gold licorice, N: blue licorice, water: red dashed interior. $A_J = 65.3 \text{ \AA}^2$.

Table 1.

Systems of linear equations used to evaluate configuration probabilities for Be^{2+} ion interactions with small ligands.*

Small Molecule		N_{SM}	System of Equations
DMP	Lipid FF	3, 2	$3p_3 + 2p_2 = N_{\text{Be}^{2+} - \text{O}_{\text{dp}}} ;$ $p_2 + p_3 = 1$
	Adjusted	2, 1	$2p_2 + 1p_1 = N_{\text{Be}^{2+} - \text{O}_{\text{dp}}} ;$ $p_1 + p_2 = 1$
Acetate	CGEN FF	4, 3	$4p_4 + 3p_3 = N_{\text{Be}^{2+} - \text{O}_{\text{dp}}} ;$ $p_4 + p_3 = 1$
	Adjusted	1, 0	$1p_1 = N_{\text{Be}^{2+} - \text{O}_{\text{dp}}} ;$ $p_0 + p_1 = 1$
	Lipid FF**	3, 2	$3p_3 + 2p_2 = N_{\text{Be}^{2+} - \text{O}_{\text{dp}}} ;$
	Adjusted	1, 0	$1p_1 = N_{\text{Be}^{2+} - \text{O}_{\text{dp}}} ;$ $p_0 + p_1 = 1$

* N_{SM} = number of associated molecules; $N_{\text{Be}^{2+} - \text{O}_{\text{dp}}}$ = number of associated free oxygens; p_i = probability of associating with i small molecules.

** New soluble acetate model for Lipid FF. See supplemental information appendix S1.

Table 2.

Thermodynamic Parameters of Binding Obtained from ITC Experiments

Reaction	K_r^{eq} (1/M)	H (cal/mol)	N	S (cal/mol ^o C)
Be ²⁺ + DMP	48050 ± 8800	4530 ± 193	0.19 ± 0.03	36.43 ± 0.26
Be ²⁺ + Acetate	320 ± 15	5946 ± 130	0.82 ± 0.02	31.03 ± 0.32

Table 3.Be²⁺ Interactions with Bulk Water

	Simulation	Target Result from Exp. or QM	Difference
		Exp. ^{14, 21, 39}	
ΔG_{hyd} (kcal/mol)	-522.0 ± 0.3	-572	8.7 %
$g(r)$ Peak Position* (Å)	1.55	1.66 – 1.67	-6.60 %
Coordination Number*	3.94 ± 0.08	4 QM model results ⁴⁰	-1.6 %
Monohydrate Energy (kcal/mol)	-131.9	-139.4, -146.1	9.3 %
Monohydrate Separation (Å)	1.37	1.51 Å	-9.27 %

* 5.3 molal aqueous BeCl₂ at 298.15 K.

Table 4.Final $2r_{ij}^{\min}$ [Å] Interaction Parameters with Be^{2+} .

Atom Type	Small Molecule	r_{ij}^{\min}
O2L	phosphoryl, DMP	2.92
OG2D2	carboxylate, CGEN FF	3.20
OCL	carboxylate, Lipid FF	3.07

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Table 5.

Configuration States and Probabilities.

Small Molecule		$N_{\text{Be}^{2+} - \text{O}_{\text{dp}}}$	N_{SM}	P_i
DMP	Lipid FF	3.1	4, 3	0.10, 0.90
	Adjusted	1.31	2, 1	0.31, 0.69
Acetate	CGEN FF	3.5	4, 3	0.50, 0.50
	Adjusted	0.53	1, 0	0.53, 0.47
	Lipid FF*	2.93	3, 2	0.93, 0.07
	Adjusted	0.37	1, 0	0.37, 0.63

* New soluble acetate model for Lipid FF. See supplemental information Appendix S1.

Table 6. G_r from Experiment and Simulation.

Small Molecule	Original $r_{ij}^{\min}/\Delta G_r$ (kcal/mol)	Final Fit $r_{ij}^{\min}/\Delta G_r$ (kcal/mol)	Exp. ΔG_r (kcal/mol)	Error, Fit/Exp.
DMP Lipid FF	2.51/-56.6 ± 0.8	2.92/-7.09 ± 0.45	-6.49 ± 0.12	-9.5 %
Acetate CGEN FF	2.51/ -72.9 ± 1.5	3.20/ -3.38 ± 0.31	-3.47 ± 0.03	-2.6 %
Lipid FF*	2.51/ -54.3 ± 0.8	3.07/ -3.76 ± 0.44	-3.47 ± 0.03	-7.8 %

* New soluble acetate model for Lipid FF. See supplemental information appendix S1.

Table 7.

DOPS monolayer surface tensions. Units of dyn/cm.

	65.3 Å ² /lipid	71.6 Å ² /lipid	80 Å ² /lipid
Be²⁺			
Sim.	52.8 ± 5.8	58.9 ± 4.7	-
Exp. ¹⁰	51.2	57.9	-
K⁺			
Sim.	35.9 ± 6.3	46.6 ± 5.4	53.5 ± 6.1
Exp. ¹⁰	41.3	47.5	54.7

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Table 8.

Ion-oxygen associations in DOPS monolayer simulations.

	Phosphate	Carboxylate	Water	Total
Be²⁺				
65.3 Å ² /lipid	1.69	0.15	2.22	4.05
71.6 Å ² /lipid	1.64	0.00	2.35	4.00
K⁺				
65.3 Å ² /lipid	0.34	0.75	5.67	6.76
71.6 Å ² /lipid	0.27	0.70	5.89	6.86

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Table 9.
Residence times and expected occupancy for various oxygen-ion associations in DOPS monolayer simulations.

Computed from 30 – 120 ns. Associations through water bridging included only for Be^{2+} . (Residence times are given in ps or ns timescale.)

	65.3 Å ² /lipid				71.6 Å ² /lipid			
	Phosphoryl	Phosphoryl + water	Carboxylate	Carboxylate + water	Phosphoryl	Phosphoryl + water	Carboxylate	Carboxylate + water
Be²⁺								
Residence time	23.7 ± 1.2 ns	14.3 ± 0.4 ps	4.4 ± 0.5 ns	21.7 ± 0.7 ps	18.2 ± 1.0 ns	14.7 ± 0.3 ps	None	21.0 ± 0.8 ps
Occupancy	0.42	0.14	0.04	0.53	0.40	0.13	None	0.55
K⁺								
Residence time	22.8 ± 0.6 ps	-	30.5 ± 0.1 ps	-	21.0 ± 0.4 ps	-	27.7 ± 0.2 ps	-
Occupancy	0.18	-	0.39	-	0.14	-	0.36	-