**Research Article** 



# Analysis of healthy and tumour DNA methylation distributions in kidney-renalclear-cell-carcinoma using Kullback–Leibler and Jensen–Shannon distance measures

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Abstract: DNA methylation is an epigenetic phenomenon in which methyl groups get bonded to the cytosines of the DNA molecule altering the expression of the associated genes. Cancer is linked with hypo or hyper-methylation of specific genes as well as global changes in DNA methylation. In this study, the authors study the probability density function distribution of DNA methylation in various significant genes and across the genome in healthy and tumour samples. They propose a unique 'average healthy methylation distribution' based on the methylation values of several healthy samples. They then obtain the Kullback–Leibler and Jensen–Shannon distances between methylation distributions of the healthy and tumour samples and the average healthy methylation distribution. The distance measures of the healthy and tumour samples from the average healthy methylation distribution are compared and the differences in the distances are analysed as possible parameters for cancer. A classifier trained on these values was found to provide high values of sensitivity and specificity. They consider this to be a computationally efficient approach to predict tumour samples based on DNA methylation data. This technique can also be improvised to consider other differentially methylated genes significant in cancer or other epigenetic diseases.

# 1 Introduction

Epigenetics is the study of heritable changes in the gene expression that cannot be explained by changes to the genetic sequence [1]. Some of the significant epigenetic mechanisms include DNA methylation, histone modifications and microRNA's. Epigenetic phenomena are known to influence several biological functions of the organism ranging from circadian rhythms to auto-immune diseases. The epigenetic mechanisms are in turn dependent on external physical factors such as environment, stress, diet and light [2].

DNA methylation is an epigenetic mechanism in which a methyl group gets bonded to the 5-carbon of the cytosine ring to result in 5-methyl cytosine (5-mC). In human somatic cells, 5-mC occurs in CpG sites and islands. A CpG site is a location within a DNA sequence in which a cytosine and guanine appear consecutively. A CpG island is a long stretch of CpG sites in DNA. When a CpG island in the promoter region of a gene is methylated, the gene expression is switched off. DNA methylation patterns are either inherited (maintenance) or developed newly (de-novo methylation) [3].

Irregular changes in DNA methylation (hypo- and hypermethylation) have been linked with many diseases. In this paper, we focus on cancer, which is considered to be caused by a multitude of genetic and epigenetic occurrences. Specifically, the methylation aberrations in the promoter regions of the tumoursuppressor genes (TSG) and oncogenes associated with the tumour type are significant in cancer genesis [4, 5]. Tumour-suppressor genes are normally active in the genome; however, the epigenetic silencing of these genes by hyper-methylation of DNA in the promoter regions causes these genes to be silenced. On the other hand, oncogenes, that are silent in the non-cancerous genomes, are found to be 'turned on' in cancer, primarily due to hypomethylation of the DNA in the promoter regions [5, 6].

Kidney-renal-clear-cell-carcinoma (KIRC) is a fatal type of cancer of the kidney and urinary tissues. There has been significant research in prediction of KIRC cancer using different parameters in the past; in [7], Yang *et al.* aim to provide an identification of the genes and pathways associated with KIRC. In the same research paper, the authors present lists of tumour-suppressor and oncogenes associated with KIRC that are differentially methylated. In [8], Liu *et al.* present an integrative model of studying KIRC stage progression. From this paper, we understand that KIRC such as most other types of cancer is caused by a series of genetic and epigenetic alternations, transcription factor modifications and other associated biological changes. In a similar research [9], information theoretic entropy is used to analyse the DNA methylation in healthy and tumour samples of KIRC. The methylation probabilities are transformed using mathematical functions to analyse the ranges of methylation that are more significant in cancer.

In the past, entropy, mutual information and even Kullback– Leibler (KL) distance have been used to study various chemical and biological parameters associated with cancer [9–13]. In [10], Hu *et al.* use mutual information to analyse the correlation between gene expression and metabolic pathways. They also use KL distance to investigate changes in relative isoenzyme expression. In [11], entropy is used as a measure to quantify the complexity, predictability and progression patterns associated with cancer. The authors also use KL distance to measure the inefficiency of using an 'all-cancer' distribution to the specific cancer type distribution. In [12], information theoretic parameters are used to obtain a significant subset of genes related to cancer, whereas in [13] KL distance is used for outlier prediction in cancer.

The Jensen–Shannon (JS) divergence and distance are other metrics that have been used in the past to study probability distributions in various fields of biology and engineering [14, 15]. The JS divergence can be considered as a symmetric and smoother form of the KL divergence [16] and is widely applied in the field of bioinformatics.

We find that though there have been several independent research on KIRC or the information theoretic techniques, there has been no significant analysis on KIRC based on the DNA methylation data using the distance measures and the average healthy methylation distribution. Our motivation is to investigate in that direction. The goal of our current research is to use the distance metrics such as the KL distance and JS distance to analyse a specific parameter in cancer (DNA methylation) with the global epigenome as well as sets of significant genes such as tumoursuppressor genes and oncogenes associated with a specific cancer type (KIRC). In that direction, we compute the 'average healthy methylation distribution' as the first step. The distance of this distribution from a given sample's methylation distribution is used for further analysis. We use the results of analysis to check if we are able to classify the normal and tumour samples using the distance measures.

A formal definition of KL distance  $D_{\text{KL}}$  between two probability distributions **P** and **Q** is given in (1)

$$D_{\mathrm{KL}}(\boldsymbol{P} \parallel \boldsymbol{Q}) = \sum_{i=1}^{N} P_i \log \frac{P_i}{Q_i}$$
(1)

The KL distance defined in (1) is non-symmetric, non-negative and has other useful properties. More details on this measure can be obtained from the texts in information theory [17].

The definition of JS distance as  $D_{\rm JS}$  between distributions P and Q can be defined as

$$D_{\rm JS}(\boldsymbol{P} \mid \boldsymbol{Q}) = \sqrt{\frac{1}{2} D_{\rm KL}(\boldsymbol{P} \parallel \boldsymbol{M}) + \frac{1}{2} D_{\rm KL}(\boldsymbol{Q} \parallel \boldsymbol{M})}$$
(2)

where

$$M = \frac{1}{2} \left( \boldsymbol{P} + \boldsymbol{Q} \right) \tag{3}$$

M can be considered as a median distribution between P and Q. The JS distance is symmetric and is non-negative.

# 2 Results

#### 2.1 Data extraction and processing

We obtained the DNA methylation data for KIRC type of cancer from the The Cancer Genomic Atlas (TCGA) database [18]. The TCGA database is the most comprehensive and publicly available cancer database [19]. They have a rigorous process involving several cooperating centres for the underlying procedures including sample collection, followed by high-throughput sequencing and sophisticated bioinformatics data analyses. According to the statistics provided in [19], as of 2014, more than 30 tumours have been analysed and the results published in prestigious journals such as *Cell* or *Nature*.

The following filter settings in the data matrix: disease: KIRC, data type - DNA methylation, data level - level 3, tumour/normal checkbox - tumour matched or normal matched for tumour/healthy samples, the other parameters were the default settings. Only the Illumina 27k DNA methylation samples were taken for our experiments. We obtained about 200 healthy and 219 tumour samples. Each sample consisted of CpG sites with their corresponding gene symbols and beta values (methylation intensities). This data was further processed into three sets: (i) one set in which all the healthy and tumour samples were processed to contain only those CpG sites corresponding to tumour-suppressor genes for KIRC, (ii) another set in which all the samples were processed to contain only the oncogenes for KIRC and (iii) the global set of healthy and tumour samples containing all the CpG sites obtained from the database. The experiments were applied to these sets of data independently. The list of oncogenes and tumoursuppressor genes for KIRC was obtained from the literature and is provided in supplementary tables S1 and S2. MATLAB was used for processing the data and extracting the relevant portions from the TCGA data.

# 2.2 Average healthy methylation probability density function

To obtain the average healthy methylation probability density function (PDF), the following steps were performed. For every healthy sample, we obtain the methylation intensities for various CpG sites to compute the methylation vector  $m_i$ , where the suffix *i* 

corresponds to the sample. This methylation vector for a sample is given by

$$\boldsymbol{m}_i = \left\{ m_{ij} \right\} \tag{4}$$

where  $m_{ij}$  represents the frequency of methylation intensities in the *j*th bin for the *i*th sample. As the next step, we obtained the histogram and the frequencies of the methylation intensities for all the healthy samples. In our experiments, the number of bins in the histogram (*j*) was varied between 5 and 35. The probabilities of methylation intensities are obtained by the ratio of the methylation intensities to the total number of CpG sites considered in the sample. Let  $p_{ij}$  represent the probability of methylation intensities in the *j*th bin for the *i*th sample. It is given by

$$p_{ij} = \frac{m_{ij}}{M} \tag{5}$$

where *M* represents the total number of CpG sites considered for computation in the samples. This quantity  $p_{ij}$  represents the probability that methylation intensity is likely to occur in a CpG site in a sample.

As a next step, we compute the average methylation intensity probabilities over all the healthy samples for the different bins as shown in (6)

$$H_{\rm m} = \frac{(\sum_{i=1}^{N_{\rm H}} m_{ij})}{N_{\rm H}}$$
(6)

In (6),  $N_{\rm H}$  represents the total number of healthy samples taken for computations. This vector  $H_{\rm m}$  represents the average healthy methylation distribution.

### 2.3 Computation of methylation distribution

To compute the methylation distribution for each sample, we obtained their probabilities of the methylation intensities as explained using (4) and (5). We then obtained the methylation distribution for every sample ( $H_i$ ) as a vector representing the methylation probabilities of the sample

$$\boldsymbol{H}_i = \left\{ p_{ij} \right\} \tag{7}$$

We denote the methylation PDF's of the healthy samples as  $\{H_{ih}\}$  and the methylation PDF's of the tumour samples as  $\{H_{it}\}$ . We then proceed to obtain the KL distance and JS distance metrics between  $H_{m}$  and  $H_{i}$  using (1) and (2).

### 2.4 Training and test data

We first consider the data processed only for the CpG sites that code for the TSG's for KIRC. The data was split into training and test data randomly with a ratio of 0.8 (80% - training data and 20% test data). To avoid bias in the computation of posterior probability distributions, equal number of healthy and tumour samples of training data were fed to the classifier. The results were averaged over five trials with randomly selected training data for each trial. We obtained the KL distances and JS distances of the healthy training samples and the tumour training samples from the average healthy methylation PDF. We then trained a Naïve Bayes classifier with the training data and obtained the results for classification for the test data. MATLAB functions were used to simulate a Naïve Bayes classifier with a combination of Gaussian/ multivariate multinomial distribution for analysis. The choice of the distribution was based on the bin size. We calculate the true positives (tp), false negatives (fn), true negatives (tn) and false positives (fp) after the classification process. The definitions for these parameters are provided in Table 1. The performance of the classifier is computed using the sensitivity and specificity defined using (8) and (9). Sensitivity can be understood as a measure of

Table 1 Definition of tp, tn, fp and fn

	Decoded as healthy	Decoded as tumour
healthy phenotype	tn	fp
tumour phenotype	Fn	tp

 

 Table 2
 Sensitivity, specificity values for the KL distance and JS distance metrics based on the Naïve Bayes classifier for the tumour-suppressor genes distributions trained with the KIRC data obtained from the TCGA database

Number of bins in PDF	Sensitivity – KL distance	Specificity – KL distance	Sensitivity – JS distance	Specificity – JS distance
5	0.8222	0.9091	0.7647	0.9474
10	0.9231	0.9091	0.9231	0.9091
15	0 5439	0.5385	0.7381	0.8125
20	0.5506	0.6364	0.7162	0.8511
25	0.5962	0.6667	0.7536	0.8462
30	0.6200	0.6875	0.7424	0.8000
35	0.5814	0.6944	0.7869	0.8000

how accurately the proposed method of classification can identify a valid case of tumour while specificity is a measure of how reliably the method can ignore the case of fp

sensitivity = 
$$\frac{\text{tp}}{(\text{tp} + \text{fn})}$$
 (8)

specificity = 
$$\frac{\text{tn}}{(\text{tn} + \text{fp})}$$
 (9)

# 3 Discussion

We have aimed to compute the average healthy methylation distribution for a data set and use the KL distance and JS distance measures to calculate the separation of individual methylation distributions from the average distribution. Furthermore, we compare the differences in KL/JS distances between the healthy and tumour samples to analyse if we can predict cancer based on these differences. From our observations, we see that the mean distance of the healthy samples is less than the mean distance of the tumour samples from the average healthy distribution. This is true for both the KL distance and the JS distance measures. For a bin size of 10 in the case of tumour-suppressor genes, the mean KL distance for the healthy samples from the average healthy distribution was computed as 76.6938, whereas the mean KL distance, the mean distance of the healthy samples was computed as 0.0155 and the mean distance for tumour samples was computed as 0.0310.

First, we consider the sensitivity and specificity measures for the tumour-suppressor genes in detail. Table 2 provides the values of sensitivity and specificity of a classifier based on the KL distance and JS distance metrics for different bin sizes of the methylation distributions for tumour-suppressor genes. From the observations, we can infer that higher values of sensitivity and specificity are obtained for lower bin sizes relatively. The higher values of sensitivity and specificity are obtained for JS distances indicating that the symmetric distance measure may be a better parameter in segregation of the healthy and tumour distributions. Fig. 1a displays the plots of the KL distance distributions of the healthy and tumour samples, whereas Fig. 1b displays the plots of the JS distance distributions of the healthy and tumour samples, both for a bin size of 10. From these figures, we observe that the JS distance plots produce less overlap than the KL distance plots that corroborates the inference that JS distance yields higher sensitivity and specificity than the KL distance.

The maximum values of sensitivity and specificity (96.7 and 97.4%) are comparable with the results obtained for segregation of healthy and tumour samples using the previously reported techniques for KIRC cancer based on RNA-seq data from the TCGA database [7] (*namely*) 96.5 and 97% and higher than the values reported by the previous DNA methylation-based cancer detection techniques [20] (*namely*) 89 and 90%. In the receiver operating characteristic (ROC) curves for these randomly selected data, we obtained a maximum value of area under the curve for



#### Fig. 1 Plots of the

(a) KL distance, (b) JS distance measures of the healthy and tumour TSG methylation distributions from the average healthy methylation distribution, for a bin size of 10. The data correspond to the KIRC samples obtained from the TCGA database



**Fig. 2** ROC curve for randomly selected data for oncogenes of the KIRC data obtained from the TCGA database. This ROC curve was obtained with a bin size of 10. The area under curve was computed as 99.05%

**Table 3** Sensitivity, specificity values for the KL distance and JS distance metrics based on the Naïve Bayes classifier for oncogenes distributions trained with the KIRC data obtained from the TCGA database

Number         Sensitivity – Specificity – Sensitivity – Specificity – of bins in KL distance KL distance JS distance JS distance           9DF         5         0.7556         0.8627         0.7778         0.8966           10         0.9200         0.9286         0.9677         0.9615           15         0.9333         0.8355         0.9333         0.8355           20         0.8571         0.7700         0.8571         0.9556           25         0.5479         0.5714         0.6234         0.7111	Ublaineu i		A ualabase		
of bins in PDF         KL distance KL distance JS distance JS distance           5         0.7556         0.8627         0.7778         0.8966           10         0.9200         0.9286         0.9677         0.9615           15         0.9333         0.8355         0.9333         0.8355           20         0.8571         0.7700         0.8571         0.9556           25         0.5479         0.5714         0.6234         0.7111	Number	Sensitivity -	Specificity -	Sensitivity -	Specificity -
PDF         5         0.7556         0.8627         0.7778         0.8966           10         0.9200         0.9286         0.9677         0.9615           15         0.9333         0.8355         0.9333         0.8355           20         0.8571         0.7700         0.8571         0.9556           25         0.5479         0.5714         0.6234         0.7111	of bins in	KL distance	KL distance	JS distance	JS distance
5         0.7556         0.8627         0.7778         0.8966           10         0.9200         0.9286         0.9677         0.9615           15         0.9333         0.8355         0.9333         0.8355           20         0.8571         0.7700         0.8571         0.9556           25         0.5479         0.5714         0.6234         0.7111	PDF				
10         0.9200         0.9286         0.9677         0.9615           15         0.9333         0.8355         0.9333         0.8355           20         0.8571         0.7700         0.8571         0.9556           25         0.5479         0.5714         0.6234         0.7111	5	0.7556	0.8627	0.7778	0.8966
15         0.9333         0.8355         0.9333         0.8355           20         0.8571         0.7700         0.8571         0.9556           25         0.5479         0.5714         0.6234         0.7111	10	0.9200	0.9286	0.9677	0.9615
20         0.8571         0.7700         0.8571         0.9556           25         0.5479         0.5714         0.6234         0.7111	15	0.9333	0.8355	0.9333	0.8355
25 0 5479 0 5714 0 6234 0 7111	20	0.8571	0.7700	0.8571	0.9556
	25	0.5479	0.5714	0.6234	0.7111
30 0.5270 0.5417 0.6667 0.7447	30	0.5270	0.5417	0.6667	0.7447
<u>35</u> 0.5125 0.5238 0.7000 0.7692	35	0.5125	0.5238	0.7000	0.7692

oncogenes (99.05%) with a corresponding bin size of 10. This value is higher than area under the curve values reported in the

previous research (96.5% in [7] and 96.1% in [20]). The ROC curve can be seen in Fig. 2.

Compared to the traditional biochemical techniques for DNA methylation-based cancer prediction (immunoassays or chromatography) which are time and cost intensive [21] or optimisation algorithms for data modelling [22], our proposed methods have the advantage of computational efficiency. The time taken to obtain the average healthy methylation distribution for 200 healthy samples is 396 s for TSG data, whereas the time taken to compute the methylation distribution for a single sample is 847 s. These values are those obtained using MATLAB software run on an Intel 2.60 GHz processor. A similar computational efficiency can be observed in the case of oncogenes and global data set.

We next discuss the results for the oncogenes. The activation of specific oncogenes by DNA hypo-methylation is known to play a significant role in carcinogenesis. Table 3 provides the sensitivity and specificity results for the KL distance and JS distance measures of the methylation distribution of the oncogenes for the healthy and tumour samples. As with the case of tumoursuppressor genes, we observe that the specificity values are by and large higher than the sensitivity values. We also observe that the JS distance with a bin size of 10 yields the highest value of sensitivity for all the cases (96.7%). Bin sizes of 15 and 5 also yield comparably high values of sensitivity and specificity indicating that they are also considerable values for experiments. Fig. 3adisplays the KL distance distributions of the healthy and tumour samples, whereas Fig. 3b shows the plots of the JS distances of the samples for a bin size of 10. We find that while there are many peaks in the tumour distance plot, there are fewer peaks in the healthy distance plot, indicating that most of the healthy samples are uniformly methylated.

In addition to specific genes, we also ran the experiments for all the CpG sites in the sample. The methylation distribution obtained thus could be considered as a global methylation vector of a given sample. The average healthy global methylation distribution was computed and the asymmetric KL distance and the symmetric JS distance measures of the healthy and tumour samples were obtained. Table 4 provides the results of classification for this data. We find that the separation between the tumour and the healthy samples is not as segregated in the global data as it was in the



### Fig. 3 Plots of the

(a) KL distance, (b) JS distance measures of the healthy and tumour oncogenes methylation distributions from the average healthy methylation distribution, for a bin size of 10. The data correspond to the KIRC samples obtained from the TCGA database



#### Fig. 4 Plots of the

(a) KL distance, (b) JS distance measures of the healthy and tumour global methylation distributions from the average healthy methylation distribution, for a bin size of 10. The data correspond to the KIRC samples obtained from the TCGA database

Table 4	Sensitivity, specificity values for the KL distance
and JS di	stance metrics based on the Naïve Bayes classifier
for global	distributions trained with the KIRC data obtained
from the	TCGA database

Number of bins in PDF	Sensitivity – KL distance	Specificity – KL distance	Sensitivity – JS distance	- Specificity – JS distance
5	0.7467	0.9500	0.7195	0.9744
10	0.6667	0.8529	0.6585	0.8529
15	0.6163	0.7778	0.6163	0.7778
20	0.5778	0.7188	0.5909	0.7353
25	0.5682	0.7308	0.5698	0.7308
30	0.5568	0.6471	0.5408	0.6667
35	0.5556	0.7391	0.5612	0.7500

oncogenes or the tumour-suppressor genes data. This can be attributed to the fact that methylation profiles of the non-cancerrelated genes are not differentially methylated in healthy and tumour samples. However, with a bin size of 5 (j = 5), we obtain the highest value of specificity (97.44%). Fig. 4*a* shows the plots of the KL distance measures of the healthy and tumour sample distributions from the average healthy methylation distribution, whereas Fig. 4*b* shows the plots of the JS distance counterparts. As in the case of tumour-suppressor genes and oncogenes, it can be observed that the healthy distance plot has peaks that are toward the left compared with the tumour distance peaks, indicating that the healthy samples are closer to the average healthy distribution than the tumour samples.

Bin size is an important parameter in the analysis since it provides a lens to view the distributions. Too small bin sizes may not provide enough details to the classifier while large bin sizes may not reflect the right nature of the distributions to the classifier. From the observations in these tables, one could generally infer that the lower bin sizes provided higher values of sensitivity/ specificity than the higher bin sizes. In particular, bin sizes of 5 and 10 yielded good results.

Additionally, we can infer that the JS distance being a symmetric measure presents better results compared with the non-symmetric KL distance. While TSG's yield good results overall for most bin sizes, the highest sensitivity was obtained with the oncogenes distributions (bin size of 10). Moreover, the global

methylation profiles, though not providing high separation values for most bin sizes yielded the highest specificity value (for a bin size of 5). This indicates that the global methylation distribution with an optimum bin size is an important factor in prediction.

# 4 Conclusion

In this research work, we have proposed techniques by which the DNA methylation distributions of healthy and tumour samples can be used in the early detection of cancer using advanced information theory techniques such as the KL distance and JS distance. We have obtained the 'average healthy distribution' of DNA methylation for the samples and computed the KL and JS distance measures of several healthy and tumour methylation distributions. We have also trained a classifier based on these results to predict the nature of test samples and obtained the sensitivity and specificity of classification. These techniques were applied to KIRC data obtained from TCGA database. We have used different sets of genes that are significant in cancer (tumour-suppressor genes, oncogenes) and global data to apply our techniques. We present this paper as a computationally efficient approach toward early prediction of cancer that can be enhanced using various parameters in epigenetics, application of mathematical transforms toward enhancing specific probabilities [9] or to study specific set of genes other than TSG's or oncogenes for other diseases.

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