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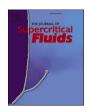
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# Solubility of favipiravir (as an anti-COVID-19) in supercritical carbon dioxide: An experimental analysis and thermodynamic modeling

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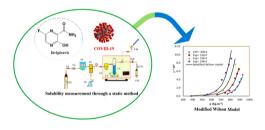
#### HIGHLIGHTS

#### GRAPHICAL ABSTRACT

- First report on solubility of favipiravir in supercritical carbon dioxide.
- Solubility data were correlated by density-based models.
- Effects of pressure and temperature were investigated on the solubility.
- Modified Wilson and K-J model can more accurately correlate experimental data.

# ARTICLE INFO

Keywords: Favipiravir solubility Supercritical carbon dioxide (SC-CO<sub>2</sub>) Empirical model Equation of state (EoS) Expanded liquid theory Simulated annealing



# ABSTRACT

Favipiravir is one of the most commonly prescribed drugs in the treatment of COVID-19 in the early stages of the disease. In this work, the solubility of favipiravir was measured in supercritical CO<sub>2</sub> at temperatures ranging from 308 to 338 K and pressures ranging from 12 to 30 MPa. The mole fraction solubility of favipiravir was in the range of  $3.0 \times 10^{-6}$  to  $9.05 \times 10^{-4}$ . The solubility data were correlated with three types of methods including; (a) density-based models (Chrastil, Garlapati and Madras, Sparks et al., Sodeifian et al., K-J and Keshmiri et al.), (b) Equations of states SRK with quadratic mixing rules) and (c) expanded liquid theory (modified Wilson model). According to the results, modified Wilson and K-J models are generally capable of providing good correlation of solubility. Finally, the approximate values of total ( $\Delta H_{total}$ ), vaporization ( $\Delta H_{vap}$ ), and solvation ( $\Delta H_{sol}$ ) enthalpies were computed.

#### 1. Introduction

In December 2019, a new coronavirus (COVID-19) emerged whose quick outbreak led to a pandemic according to the World Health

Organization (WHO) classification. COVID-19 was initially discovered in Wuhan, Hubei Province, China. Coronavirus can cause drastic acute respiratory syndrome (SARSCoV-2) [1]. SARS CoV-2 belongs to the coronaviridae family with a positive-strand RNA (+RNA) genome. An RNA-dependent RNA polymerase (RdRp) and proteases are encoded by

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Nomenc	lature	$V_s$	Volume of the collection vial (L)
		$V_L$	Volume of the sampling loop (L)
$a_0 - a_5$	Adjustable parameters of model	$v^{s}$	Solid molar volume
AARD%	Average absolute relative deviation	Ζ	Number of adjustable parameters
<b>a</b> ( <b>T</b> )	Energy parameter of the cubic EoS ( $Nm^4 mol^{-2}$ )	<b>c</b> 1	
B	Volume parameter for equations of state $(m^3 mol^{-1})$		symbols
C	Solubility of solute (g/L)	$\alpha(Tr,$	$\omega$ ) Temperature-dependent function of the considered
$c_s$	Concentration of solute (g/L) in the collection vial		parameter of the EoS
$H_f^2$	Molar heat of fusion	α	Regressed parameter of the Wilson's model
$K_{ij}$	Binary interaction parameter	β	Regressed parameter of the Wilson's model
K <sub>ii</sub>	Binary interaction parameter in the mixing rules	δ	Solubility parameter $(cal/cm^3)^{0.5}$
	Binary interaction parameter in the mixing rules	ρ	Density, kg.m <sup><math>-3</math></sup>
M <sub>w</sub>	Solute molecular weight (g/mol)	$ ho_c$	Critical density
M <sub>co</sub> ,	$CO_2$ molecular weight (g/mol)	$\rho_r$	Reduced density
N	Number of data points, dimensionless	$ ho_{ref}$	Reference density
P	Pressure	$v_1, v_2$	Volumes of the SCF and the solid solute, respectively
Pc	Critical pressure	λ	Energies of interaction between the molecules designated
Pr	Reduced pressure	~	in the subscripts
P <sub>ref</sub>	Reference pressure	$\gamma_2^{\infty}$	The activity coefficient of the solid solute at infinite
P <sub>sub</sub>	Sublimation pressure (Pa)		dilution
Q	Number of independent variables	Φ	Fugacity coefficient
$\tilde{R}$	Gas constant, $Jmol^{-1} K^{-1}$	w	Acentric factor
R <sub>adj</sub>	Adjusted correlation coefficient	Superso	cripts
S	Equilibrium solubility	Cal	Calculated
Т	Temperature, K	Exp	Experimental
T <sub>b</sub>	Boling point	i,j	Component
T <sub>c</sub>	Critical temperature	Sub	Sublimation
T <sub>r</sub>	Reduced temperature		
<i>y</i> <sub>2</sub>	Mole fraction solubility		

this single-stranded RNA beta-coronavirus [2]. Quarantine and antiviral medicines significantly reduced the ultimate size of the prevalence and peak incidence [3]. Favipiravir, remdesivir, umifenovir, oseltamivir, immune globulin, lopinavir, azithromycin, and ivermectin have been employed for the treatment of COVID-19 [4].

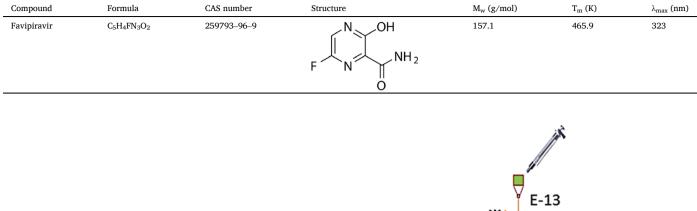
Favipiravir (FAV) was endorsed by the Food and Drug Administration (FDA) in 2014 to cure new and re-emerging influenza viruses [3]. Thanks to their antiviral features, favipiravir and its derivatives have been approved as a prodrug and support in the treatment of the influenza virus [5]. FAV belongs to class II in the Biopharmaceutics Classification System (BCS). High permeability and low water solubility are two major characteristics of favipiravir. The poor solubility of the favipiravir in the aqueous media of the human body has decreased its effectiveness and bioavailability [6]. Recently, Abd Elkodous et al. [4] reviewed nanomaterial-based drug delivery systems for the treatment of COVID-19 to increase the bioavailability of current drugs, reduce their toxicity, and increase their efficiency. They reported that favipiravir-encapsulated nano-emulsions as prospective carriers of COVID-19 drug delivery. Biodegradable nano-emulsions have a kinetically persistent structure and can be dispersed both in oil and water. Small particles with a diameter range of 5-200 nm make up nano-emulsion formulae.

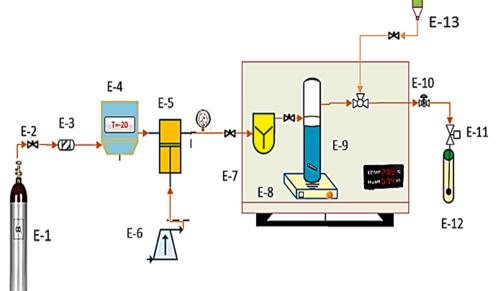
Various approaches have been developed to enhance the aqueous solubility and bioavailability of drugs among which, co-crystallization, salt formation, encapsulation/impregnation, and particle size reduction in micro/nano-scale can be mentioned. Furthermore, supercritical fluid technology could be a viable option to overcome the drawbacks of conventional techniques for enhancing the solubility of poor watersoluble formulas. Traditional processes suffer from temperature sensitivity and impurity contamination. Non-toxicity, eco-friendliness, and adaptability are among the benefits of SCF technology, making it an ideal route in green chemistry. SCF has been used to improve solubility and increase the bioavailability of poorly soluble drugs [7–10]. The bioavailability of drugs is highly dependent on their solubility and dissolution. In this regard, the production of nano/microparticles of drugs through the SCF method is of paramount significance. Concerning particle development, SCF technology is an alternative technique for particle production which can avoid most of the disadvantages associated with conventional approaches such as crushing, milling, crystallization, and precipitation. More advanced technologies, such as microencapsulation, coating, and composite particle creation, can be developed by SCF technology [11–18]. The solubility of drugs in SC-CO<sub>2</sub> is the main parameter I reduction of the particle size, highlighting the significance of measuring drug solubility. Several methods have been introduced for the measurement of solubility among which, gravimetric, spectrometric, chromatographic, and miscellaneous methods can be mentioned.

Experimental measurement of drug solubility in SC-CO2 at different temperatures and pressures is time-consuming, costly, and in some cases impossible. Therefore, various correlative models such as the equation of states (EoSs; (e.g. Peng-Robinson (PR) and Soave- Redlich-Kowang (SRK)), empirical models, and expanded liquid models (e.g. universal quasi-chemical (UNIQUAC) and modified Wilson's models) have been considered to correlate the solubility of solid at different pressures and temperatures in SC-CO2. Prediction and correlation via EoS and expanded liquid require the calculation of the physicochemical properties of solid (pharmaceutical components) such as acentric factor, critical pressure, temperature, and sublimation pressure. These properties are not in literature and are usually determined by different group contribution (GC) methods. In return, the empirical models (densitybased model), only require pressure, temperature, and SC-CO2 density. The correlative model has indicated the best fitting with the experimental data [8,9,13,19].

In the current research, the solubility of favipiravir was measured in

Structure and details of favipiravir.





**Fig. 1.** Process diagram of experimental apparatus used for measuring favipiravir solubility. E-1: CO<sub>2</sub> cylinder, E-2: Needle valve, E-3: Filter, E-4: Refrigerator unit, E-5: High-pressure pump, E-6: Compressor, E-7: Oven, E-8: Magnetic stirrer, E-9: Equilibrium cell, E-10: Backpressure, E-11: Micrometer valve, E-12: Collection vial, E-13: syringe.

the temperature range of 308 - 338 K and the pressure range of 12 - 30 MPa. For this purpose, solubility data were correlated with three types of methods including (1) Empirical density-based models (Chrastil, Garlapati and Madras, Sparks et al., Sodeifian et al., K-J, and Keshmiri et al.) (2) Equations of states (EoSs) (Soave–Redlich–Kwong (SRK) with vdW2 mixing rule), and (3) expanded liquid theory (modified Wilson model). The mentioned models were evaluated based on mean absolute deviation (AARD%) and adjusted correlation coefficient ( $R_{adj}$ ).

#### 2. Experiments

#### 2.1. Materials

Favipiravir (CAS No. 259793–96–9) has been procured through the Tofigh Darou pharmaceutical corporation (Tehran, Iran), at the minimum purity of 99%. Carbon dioxide (CO<sub>2</sub>) was prepared by Oxygen Novin Company (Shiraz, Iran) with a purity of 99.99%. Analytical-grade methanol was supplied by Merck (Darmstadt, Germany). The structure of favipiravir (drug) and the information of all components are presented in Table 1.

#### 2.2. Experimental apparatus

The applied laboratory setup with a spectrophotometer is presented

in Fig. 1 which encompassed a CO<sub>2</sub> cylinder (E-1), a needle valve (E-2), a molecular sieve filter (E-3), a refrigerator unit (E-4), a high-pressure pump (E-5, air driven liquid pump, type-M64, Shineeast Co., Shandong, China), an air compressor (E-6), an incubator (E-7, shimaz), magnetic stirrer (100 rpm) (E-8, Alfa, D-500 180,), a high-pressure equilibrium cell (E-9), a back-pressure valve (E-10, Xi'an Shelok Instrument Technology Co., Shaanxi, China), a micrometer valve (E-11), a collection vial (E-12), a Syringe (E-13). In this high-pressure system, all equipment, piping and connections were made from stainless steel 316 at 1/8'' in size. The CO<sub>2</sub> flow from the cylinder first enters the molecular sieve filter (pore size of 1 µm) to prevent impurities. It then flows to the refrigerator. The temperature inside the refrigerator is about -15 °C, liquifying the CO<sub>2</sub> flow. The liquid CO<sub>2</sub> at the pressure in the CO<sub>2</sub> tank (about 60 bar) entered the high-pressure reciprocating pump. Using the pressure gauge and transmitter, measurements were performed at a precision of  $\pm 1$  bar.

In the next step, 3000 mg favipiravir was mixed in SC-CO<sub>2</sub> using a magnetic stirrer to establish an equilibrium phase into a cell with a capacity of 300 mL. The temperature was maintained at the desired level by an oven equipped with a digital display with temperature measurements at an accuracy of  $\pm$  0.1 K. A sintered filter (1  $\mu$ m) was used on both sides of the cell to hold the drug. Carbon dioxide was pressurized and then transferred to the cell at the appropriate pressure. The static time, i.e. the time to reach equilibrium, was considered 120 min based on the preliminary experiments. After 120 min, 600  $\mu$ L of

Critical and physicochemical properties of favipiravir.

Component	T <sub>b</sub> (K)	T <sub>c</sub> (k)	P <sub>c</sub> (bar)	ω	V <sub>s</sub> (cm <sup>3</sup> /mol)	T (K)			
						308 P <sub>sub</sub> <sup>a</sup> (bar)	318	328	338
Favipiravir Carbon dioxide	589.73 <sup>b</sup>	878.71 <sup>b</sup> 304.18	66.82 <sup>b</sup> 73.8	0.5799 <sup>c</sup> 0.224	97.53 <sup>d</sup>	$2.43\times10^{\text{-8}}$	$8.86\times10^{\text{-8}}$	$2.94\times10^{\text{-7}}$	$9\times 10^{\text{-7}}$

<sup>a</sup> Estimated by Grain-Watson method.

<sup>b</sup> Marrero and Gani.

<sup>c</sup> Estimated by the Ambrose–Walton corresponding states method.

<sup>d</sup> Estimated by Immirzi–Perini method.

saturated SC-CO<sub>2</sub> was introduced into the injection loop using a threevalve two-position device. By redirecting the injection valve, the loop was depressurized into the collection vial containing a certain volume of methanol (solvent). In this part, the micrometer valve was used for controlling the flow.

In the final step, about 1 mL of solvent was injected through an external needle valve for washing the loop and the solution is collected in the vial. The final volume of the solution was 5 mL. Each experiment was repeated three times (triplicates). The favipiravir solubility values were determined by measuring the absorbance at  $\lambda_{max}$  on a Shimadzu UV-Vis spectrophotometer with a 1 cm long quartz cell. The solubility was calculated from the concentration of solute using the calibration curve (with regression coefficient 0.998) and the UV-absorbance.

At different sets of temperature and pressure, the equilibrium mole fraction,  $y_2$ , and solubility, S (g/L), in SC-CO<sub>2</sub> were computed as follows [20]:

$$y_2 = \frac{n_{solute}}{n_{solute} + n_{CO_2}},\tag{1}$$

where:

$$n_{solute} = \frac{C_s \left(\frac{g}{L}\right) V_s(L)}{M_s \left(\frac{g}{mol}\right)},\tag{2}$$

and

$$n_{CO_2} = \frac{V_l(L)\rho\left(\frac{g}{L}\right)}{M_{CO_2}\left(\frac{g}{mol}\right)}$$
(3)

where  $n_{solute}$  and  $n_{CO2}$  are moles of solute (favipiravir) and CO<sub>2</sub> in the sampling loop, respectively,  $C_s$  denotes the solute concentration (g/L) in the collection vial as obtained from the calibration curves. The volumes of the collection vial and sampling loop are Vs(L)=  $5 \times 10^{-3}$  and  $V_l$ (L)=  $600 \times 10^{-6}$  respectively.  $M_s$  also represents the molecular weight of the solute while  $M_{CO2}$  is the molecular weight of CO<sub>2</sub>. The accuracy of the mentioned volumes (500 µL and 5 mL) was 0.5% and 0.2% respectively.

The equilibrium solubility, S (g/L), of the solute in the SC-CO<sub>2</sub> can be obtained by Eq. (4):

$$S = \rho \frac{M_2}{M_1} \frac{y_2}{(1 - y_2)} \tag{4}$$

#### 3. Modeling studies

In this research, three types of models were considered to correlate the experimental solubility data of Favipiravir in SC-CO<sub>2</sub>: (1) EoS-based SRK, (2) empirical density-based models (Chrastil, Garlapati and Madras, Sparks et al., Sodeifian et al., K-J, and Keshmiri et al.,), and (3) expanded liquid theory (modified Wilson's model).

# 3.1. Equation of state-based (EoS) models

For solubility measurements of the solid (component 2) in  $SC-CO_2$  (component 1) under the thermodynamic equilibrium condition, the following equation can be used:

$$y_2 = \frac{P_2^{sub}(T)}{P} \frac{\phi_2^{sut.s}(T)}{\phi_2(T, P, y)} \exp\left[\frac{v_2^s(P - P_2^{sub}(T))}{RT}\right]$$
(5)

where P, R, T,  $P_2^{sub}(T)$ ,  $\phi_2^{sats}(T)$ ,  $\phi_2(T, P, y)$ , and  $v_2^s$  are pressure, gas constant, temperature, sublimation pressure of the drug, saturation fugacity coefficient of the solute, fugacity coefficient of the solute in supercritical phase, and the solid molar volume, respectively. According to Eq. (5), solubility (y<sub>2</sub>) depends on the physicochemical properties of the pure components. Since the physicochemical and critical properties of pharmaceutical compounds are not available in the literature; the group contribution methods were used to determine these properties. Different group contribution methods have been developed to estimate the critical and physicochemical properties of the solid compounds (drug). Table 2 reports the critical and other physicochemical properties of favipiravir. Selection of the proper mixing and combining rules to calculate the thermodynamic characteristics of the mixtures and parameters of the EoS is of crucial importance. In the current work, the quadratic mixing rules was applied for EoS.

# 3.1.1. Soave-Redlich-Kwong equation

The reduced residual Helmholtz energy of the SRK model can be expressed as follows [21]:

$$P = \frac{RT}{v-b} - \frac{a(T)}{v(v+b)}$$
(6)

Where R, T, and v are the universal gas constant, absolute temperature, and molar volume, respectively.

The parameters of a and b depend on the critical and physical properties of pure components and can be determined by the following equation (for a single-component system):

$$\mathbf{a}(\mathbf{T}) = \frac{0.42747R^2T_c^2}{P_c} \times \alpha(\mathbf{T}_{\mathbf{r},\omega})$$
(7)

$$\alpha(\mathbf{T}_{r,\omega}) = \left[1 + m(1 - \mathbf{T}_r^{0.5})\right]^2$$
(8)

$$m = 0.480 + 1.574\omega - 0.176\omega^2 \tag{9}$$

$$b = \frac{0.08664R T_c}{P_c}$$
(10)

The quadratic mixing rules in mole fraction for a(T) and b are used as follows:

$$a(T) = \sum_{i} \sum_{j} y_i y_j a_{ij}(T)$$
(11)

$$b = \sum_{i} \sum_{j} y_{i} y_{j} b_{ij} \tag{12}$$

Where  $a_{ij}(T)$  and  $b_{ij}$  are the cross energetic and the cross-co-volume parameters, respectively.  $a_{ii}(T)$  and  $b_{ii}$  can be calculated by:

$$a_{ij}(T) = \sqrt{a_{ii}(T)a_{jj}(T)} (1 - k_{ij})$$
(13)

$$b_{ij} = \frac{b_i + b_j}{2} \left( 1 - l_{ij} \right) \tag{14}$$

#### 3.2. Expanded liquid theory

The density of the supercritical fluid is very close to the typical liquid and its phase can be considered as an expanded liquid [22]. As a result, the thermodynamic phase equilibrium of solid and supercritical fluid can be defined by solid-liquid equilibrium and activity coefficients. The activity coefficients are required to calculate the solid solubility in the supercritical phases. In this regard, the equilibrium between the pure solid and the supercritical phase is expressed as follows [23,24]:

$$f_2^s = f_2^{SCF} = f_2^L \tag{15}$$

Where  $f = \frac{s}{2}$  and  $f_2^{ScF}$  are the fugacity of the solid solute in the solid phase and the supercritical phase, respectively.

The fugacity of solute in the supercritical phase can be expressed by:

$$f_2^L = \gamma_2 y_2 \quad f_2^{0L} \tag{16}$$

and

$$f_2^{os} = \gamma_2 y_2 f_2^{0L} \tag{17}$$

Where  $\gamma_2$  is the activity coefficient,  $y_2$  is the mole fraction of solid solubility and  $f_2^{OS}$  is and the fugacity of the pure solid solute in the expanded liquid phase.

According to Prausnitz et al. [25]:

$$\ln \frac{f_2^{0S}}{f_2^{0L}} = \frac{-\Delta H_2^f}{R} \left(\frac{1}{T} - \frac{1}{T_m}\right) - \frac{\Delta Cp}{RT} \left(\frac{T - T_m}{T}\right) + \frac{\Delta Cp}{R} \ln\left(\frac{T}{T_m}\right)$$
(18)

The heat capacity terms can be neglected [25], so:

$$y_2 = \frac{1}{\gamma_2} exp \quad \left(\frac{-\Delta H \frac{f}{2}}{R} \quad \left(\frac{1}{T} - \frac{1}{T_m}\right)\right)$$
(19)

Where  $\Delta H = \frac{f_2}{2}$  is the enthalpy of fusion and  $T_m$  shows the melting point of the solid (drug). The solid solubility in the supercritical fluid is very low (~ infinite dilution). Therefore, the activity coefficient of the solid solute is one at infinite dilution. Thus, Eq. (19) becomes:

$$y_2 = \frac{1}{\gamma_2^{\infty}} exp\left[\frac{-\Delta H \int_2^f}{R} \left(\frac{1}{T} - \frac{1}{T_m}\right)\right]$$
(20)

# 3.2.1. Modified Wilson model

Wilson equation can be utilized for determining the activity coefficient of the solid solute at infinite dilution. This equation consists of two parts, a combinatorial contribution based on Flory's theory, and a term based on the Gibbs excess energy, which can be written as follows [23]:

$$\frac{G^E}{RT} = -\sum_i x_i \ln\left(\sum_j x_j \Lambda_{ij}\right)$$
(21)

Where  $G^E$  is the excess Gibbs energy, and  $\Lambda_{12}$  and  $\Lambda_{21}$  represent adjustable parameters.

$$\ln \gamma_i = -\ln\left(\sum_j x_j \Lambda_{ij}\right) + 1 - \sum_k \frac{x_k \Lambda_{ki}}{\sum_j x_j \Lambda_{kj}}$$
(22)

According to the theory proposed by Assael et al., [26], Eq. (22) can be rewritten to the following form:

$$\ln \gamma_2^{\infty} = 1 - \Lambda_{12} - \ln \Lambda_{21}, \tag{23}$$

where  $\Lambda_{12}$  and  $\Lambda_{21}$  are defined at infinite dilution conditions:

$$\Lambda_{12} = v_2 \rho_c \rho_r \exp\left(-\frac{\lambda_{12}'}{T_r}\right),\tag{24}$$

and

$$A_{21} = \frac{1}{v_2 \rho_c \rho_r} \exp\left(-\frac{\lambda'_{21}}{T_r}\right)$$
(25)

Where  $\rho_c$  is the critical density of SCF,  $\rho_r(\rho_r = \frac{\rho}{\rho_c})$  represents the reduced density of the SCF,  $v_2$  denotes the molar volume of the solid solute. The dimensionless energies of interaction are as follows:

$$\lambda_{12}' = \frac{\lambda_{12}}{RT_{1c}} \tag{26}$$

and

$$\lambda'_{21} = \frac{\lambda_{21}}{RT_{1c}} \tag{27}$$

To address the effect of high pressures and simplify the prediction process, Wilson model was introduced by an empirical expression that linearly correlates the molar volume and the reduced density [23]:

$$v_2 = \alpha \quad \rho_r + \beta \tag{28}$$

where  $\alpha$ ,  $\beta$ ,  $\lambda'_{12}$  and  $\lambda'_{21}$  are the regressed parameters of the model.

#### 3.3. Semi-empirical density-based models

Density-based correlations are common techniques for modeling solid solubility in SCFs. Empirical models do not require estimation of the physicochemical properties of solid as they only depend on temperature, pressure, and density of SCF (independent variables) as well as several adjustable parameters (constants). In the current work, empirical density-based models (proposed by Chrastil, Garlapati, and Madras, Sparks et al., Sodeifian et al., K-J, and Keshmiri et al.) were applied for correlating the experimental solubility data.

The constants in the empirical models were determined by regression of experimental data. The adjustable parameters were optimized by simulated annealing (MATLAB software). The average absolute relative deviation (AARD%) was used to compare the precision of the model with experimental data which can be defined by:

$$AARD\% = \frac{100}{N_t - Z} \sum_{i=1}^{N_t} \frac{\left| y_2^{cal} - y_2^{exp} \right|}{y_2^{exp}}$$
(29)

Where Z and  $N_t$  are the number of fitted parameters for each model and the number of data points in each set, respectively. As another criterion for comparing different models,  $R_{adj}$  has the following expression [27, 28]:

$$R_{adj} = \sqrt{\left|R^2 - \left(Q(1-R^2)/(N-Q-1)\right)\right|}$$
(30)

Where N shows the number of data points in each set, Q is the number of independent variables in each equation.

The favipiravir solubility experimental data in SC-C	D <sub>2</sub> . The v <sub>2</sub> and S are mole fractions and solubility	ty of solute in the SC-CO <sub>2</sub> , respectively. <sup>a</sup> .

Temperature (K)	Pressure (MPa)	Density (kg/ m <sup>3</sup> )	Binary				
(R)	(mi a)		$y_2  imes 10^4$ (Mole Fraction)	Standard deviation of the mean, SD $(\bar{y})$ $\times$ $(10^4)$	Expanded uncertainty $\times 10^4$	$S \times 10^1$ (Solubility (g/L))	
308	12	768.42	0.53	0.014	0.027	1.46	
	15	816.06	0.87	0.041	0.047	2.54	
	18	848.87	1.44	0.023	0.017	4.37	
	21	874.40	2.31	0.023	0.011	7.22	
	24	895.54	3.42	0.046	0.014	10.95	
	27	913.69	4.09	0.023	0.007	13.35	
	30	929.68	5.13	0.069	0.014	17.04	
318	12	659.73	0.37	0.041	0.110	0.87	
	15	743.17	0.80	0.014	0.018	2.13	
	18	790.18	1.30	0.046	0.036	3.67	
	21	823.70	2.72	0.047	0.018	8.01	
	24	850.10	4.29	0.093	0.022	13.03	
	27	872.04	5.41	0.047	0.010	16.86	
	30	890.92	6.48	0.116	0.018	20.63	
328	12	506.85	0.08	0.001	0.019	0.15	
	15	654.94	0.60	0.003	0.008	1.41	
	18	724.13	1.39	0.047	0.034	3.60	
	21	768.74	3.21	0.070	0.022	8.82	
	24	801.92	4.75	0.068	0.015	13.61	
	27	828.51	6.58	0.117	0.018	19.48	
	30	850.83	7.65	0.092	0.012	23.26	
338	12	384.17	0.03	0.008	0.270	0.04	
	15	555.23	0.37	0.014	0.037	0.74	
	18	651.18	1.32	0.023	0.018	3.07	
	21	709.69	3.92	0.070	0.019	9.95	
	24	751.17	5.6	0.043	0.009	15.03	
	27	783.29	7.57	0.115	0.016	21.19	
	30	809.58	9.05	0.163	0.018	26.18	

The experimental standard deviation and the experimental standard deviation of the mean (SD) were calculated by  $S(y_k) = \sqrt{\frac{\sum_{j=1}^n (y_i - y)^2}{n-1}}$  and  $SD(\bar{y}) = \frac{S(y_k)}{\sqrt{n}}$  respectively. The relative combined standard uncertainty was obtained by  $U_{combined}/y = \sqrt{\sum_{i=1}^N (P_iU(x_i)/x_i)^2}$ . The expanded uncertaint U is  $k \times U_{combined}$ . <sup>b</sup>Standard uncertainty u are (T) = 0.1 K; u(p) = 0.1 MPa. The relative standard uncertainties are calculated below 0.05 for solubilities and mole fractions. <sup>c</sup> Data from the

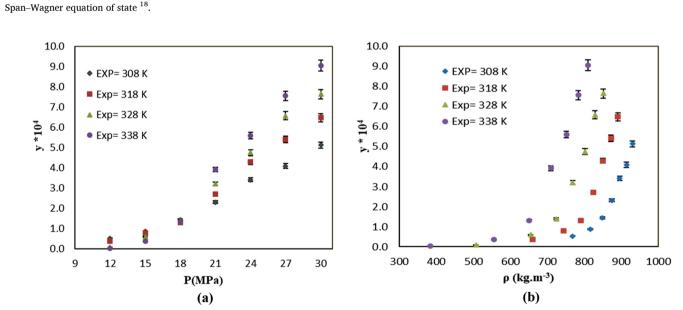


Fig. 2. The influence of (a) pressure and (b) density of SC-CO<sub>2</sub> on favipiravir solubility at different temperatures.

# 4. Results and discussion

#### 4.1. Experimental data

Solubility of favipiravir in SC-CO<sub>2</sub> was experimentally measured at the temperature range of 308–338 K and pressure range of 10–30 MPa. Solubility data of favipiravir is collected in Table 3. The SC-CO<sub>2</sub> density

was calculated by Span-Wanger EoS [29]. Furthermore, each data point was repeated three times to increase the reliability of the measurements; relative standard uncertainties were lower than 5%. The expanded uncertainty with the mole fractions is also reported in Table 3.

Fig. 2 shows the mole fraction solubility of favipiravir vs. pressure and density at different temperatures. In general, the density of  $SC-CO_2$  and its solvating power increased with increasing the pressure.

Review of some articles on the crossover points of various pharmaceutical compound in SC-CO<sub>2</sub>.

Compound	Pressure range (MPa)	Temperature range (K)	Crossover (MPa)	Mole fraction (y)	Ref
Clobetasol Propionate (C <sub>25</sub> H <sub>32</sub> ClFO <sub>5</sub> )	15.5-30.5	315–345	24.5	$1\times 10^{-6}$ to $2.1\times 10^{-5}$	[30]
Desoxycorticosterone acetate ( $C_{21}H_{30}O_3$ )	15.5-30.5	315-345	24.5	$5 imes 10^{-6}$ to $1.03 imes 10^{-4}$	[30]
Esomeprazole ( $C_{17}H_{19}N_3O_3S$ )	12-27	308.2-338.2	22	$1.11  imes 10^{-5}$ to $9.10  imes 10^{-4}$	[31]
Amiodarone hydrochloride (C <sub>25</sub> H <sub>29</sub> I <sub>2</sub> NO <sub>3</sub> . Hcl)	12-30	313.2-343.2	19	$2.510 imes10^{-5}$ to	[32]
				$1.012\times 10^{-3}$	
Ketotifen fumarate (C <sub>23</sub> H <sub>23</sub> NO <sub>5</sub> S)	12-30	308.2-338.2	20	$2.11  imes 10^{-5}$ to $1.07  imes 10^{-3}$	[33]
Aprepitant $(C_{23}H_{21}F_7N_4O_3)$	12-33	308.15-338.15	15-18	$4.50\times 10^{-6}$ to $7.67\times 10^{-5}$	[34]
Imatinib mesylate (C <sub>30</sub> H <sub>35</sub> N <sub>7</sub> O <sub>4</sub> S)	12-27	308.2-338.2	18-21	$1.0 imes 10^{-7}$ to $4.4 imes 10^{-6}$	[35]
Coumarin-7 $(C_{20}H_{19}N_3O_2)$	9–33	308-338	13-16	$4.15 \times 10^{-6}$ to $1.00 \times 10^{-5}$	[36]
Loratadine (C <sub>22</sub> H <sub>23</sub> N <sub>2</sub> O <sub>2</sub> Cl)	12-27	308.15-338.15	18-21	$4.50 imes10^{-6}$ to $1.30 imes10^{-3}$	[37]
Cefixime trihydrate ( $C_{16}H_{15}N_5O_7S_2$ .3 $H_2O$ )	18.3-33.5	308-328	NO	$1.6 \times 10^{-7}$ to $3.02 \times 10^{-7}$	[38]
Oxymetholone (C <sub>21</sub> H <sub>32</sub> O <sub>3</sub> )	18.3-33.5	308-328	18	$1.6 imes 10^{-5}$ to $1.49 imes 10^{-4}$	[38]
Atorvastatin (C <sub>33</sub> H <sub>33</sub> FN <sub>2</sub> O <sub>4</sub> )	12.16-35.46	308-348	17	$1.12  imes 10^{-6}$ to $1.45  imes 10^{-3}$	[39]
Simvastatin (C <sub>25</sub> H <sub>38</sub> O <sub>5</sub> )	12.16-35.46	308-348	17	$2 imes 10^{-6}$ to $5.35 imes 10^{-4}$	[39]
Lovastatin (C <sub>24</sub> H <sub>36</sub> O <sub>5</sub> )	12.16-35.46	308-348	17	1. $10 \times 10^{-5}$ to 1.14 $\times 10^{-4}$	[39]
Rosuvastatin (C <sub>22</sub> H <sub>28</sub> FN <sub>3</sub> O <sub>6</sub> S)	12.16-35.46	308-348	17	$3 imes 10^{-6}$ to 2.44 $ imes 10^{-4}$	[39]
Fluvastatin (C <sub>24</sub> H <sub>26</sub> FNO <sub>4</sub> )	12.16-35.46	308-348	17	$5\times 10^{-6}$ to $6\times 10^{-4}$	[39]
Azithromycin (C <sub>38</sub> H <sub>72</sub> N <sub>2</sub> O <sub>12</sub> )	12.2-35.5	308-348	13.8-14	$6.9 imes10^{-5}$ to $2.73 imes10^{-4}$	[40]
Erythromycin (C <sub>37</sub> H <sub>67</sub> NO <sub>13</sub> )	12.2-35.5	308-348	16.8-17	$4.3 imes10^{-5}$ to $3.12 imes10^{-4}$	[40]
Clindamycin (C <sub>18</sub> H <sub>33</sub> ClN <sub>2</sub> O <sub>5</sub> S)	12.2-35.5	308-348	14.8-15.2	$1.77  imes 10^{-4}$ to $1.146  imes 10^{-3}$	[40]
Clarithromycin ( $C_{38}H_{69}NO_{13}$ )	12.2-35.5	308-348	15-15.2	$1.31  imes 10^{-4}$ to $3.28  imes 10^{-4}$	[40]
Loxoprofen ( $C_{15}H_{18}O_3$ )	12-40	308-338	20	$1.04  imes 10^{-5}$ to $1.28  imes 10^{-3}$	[41]
Cyproheptadine $(C_{21}H_{21}N)$	16-40	308-338	20	$3.35  imes 10^{-5}$ to $3.09  imes 10^{-3}$	[42]
2,4,7-Triamino-6-phenylpteridine (Triamterene) (C <sub>13</sub> H <sub>13</sub> N <sub>7</sub> )	12-27	308-338	19.2-19.5	$0.03  imes 10^{-5}$ to $2.89  imes 10^{-5}$	[43]
Tolmetin (C <sub>15</sub> H <sub>15</sub> NO <sub>3</sub> )	12-40	308-338	16	$5.00 imes10^{-5}$ to $2.59 imes10^{-3}$	[44]
Busulfan( $C_6H_{14}O_6S_2$ )	12-40	308-338	16	$3.27 imes10-5 extrm{-8.65} imes10-4$	[45]
Sunitinib malate ( $C_{26}H_{33}FN_4O_7$ )	12-27	308-338	NO	$0.5\times 10^{-5}$ to $8.56\times 10^{-5}$	[46]
Fenoprofen ( $C_{15}H_{14}O_3$ )	12-40	308-338	16	$2.01  imes 10^{-5}$ to $4.20  imes 10^{-3}$	[47]
Azathioprine ( $C_9H_7N_7O_2S$ )	12-27	308-338	12-15	$0.27  imes 10^{-5}$ to $1.83  imes 10^{-5}$	[48]
Sorafenib tosylate (C <sub>28</sub> H <sub>24</sub> ClF <sub>3</sub> N <sub>4</sub> O <sub>6</sub> S)	12-27	308-338	NO	$0.68  imes 10^{-6}$ to $12.57  imes 10^{-6}$	[49]
spiroindolinonaphthoxazine photochromic dye (1,3-dihydro-3,3-dimethyl-1- isopropyl-6 -(2,3)- (dihydroindole-1-yl)spiro[2 H-indole-2,3 – 3 H-naphtho [2,1- b][1,4]oxazine])	10–26	308–328	17	$2.2\times10^{7}$ to $5.05\times10^{6}$	[50]
Flurbiprofen( $C_{15}H_{13}FO_2$ )	8–25	303-323	12	$2.170 imes10^{-5}$ to $19.683 imes10^{-5}$	[51]
Artemisinin( $C_{15}H_{22}O_5$ )	10-25	303-328	13-17	10 <sup>-4</sup> to 10 <sup>-3</sup>	[52]
Juglone (5-hydroxy-1,4-naphthoquinone) ( $C_{10}H_6O_3$ )	9.2-24.4	308.2-328.2	21-22	$2.0 imes10^{-5}$ to $1.6 imes10^{-3}$	[53]
Diflunisal (5-(2,4-difluorophenyl)– 2-hydroxybenzoic acid)( C <sub>13</sub> H <sub>8</sub> F <sub>2</sub> O3)	9–25	308.2-328.2	15	$0.54  imes 10^{ ext{-6}}$ to $8.07  imes 10^{ ext{-6}}$	[54]
Norfloxacin ( $C_{16}H_{18}FN_3O_3$ )	10-30.3	308.2-328.2	NO	$1.4 imes10^{-6}$ to $24.4 imes10^{-6}$	[55]
Ofloxacin ( $C_{18}H_{21}$ ClFN <sub>3</sub> O <sub>4</sub> )	10-30.3	308.2-328.2	NO	$0.4  imes 10^{-6}$ to $1.3  imes 10^{-6}$	[55]
Meloxicam sodium ( $C_{14}H_{12}N_3NaO_4S_2$ )	14.9-25.5	303–323	15–17	$4.41 imes10^{-6}$ to $12.76 imes10^{-6}$	[56]
CIBA photoinitiator Irgacure® 2959 2-Hydroxy-4'-(2-hydroxyethoxy)– 2- methylpropiophenone(C <sub>12</sub> H <sub>16</sub> O <sub>4</sub> )	10–26	308.2–328.2	14	$5.17 \times 10^{-6}$ to $2.83 \times 10^{-4}$	[57]

Therefore, favipiravir solubility in SC-CO<sub>2</sub> rose with increasing pressure (Table 3 and Fig. 2). As indicated in Fig. 2, at the pressure range of 12-18 MPa, the solubility of favipiravir in SC-CO2 decreased with increasing the temperature. At pressures below 18 MPa, favipiravir solubility showed a decremental trend with increasing temperature. Above this pressure (18 MPa), the solubility increased with elevating the temperature. The mentioned trend can be also observed in Fig. 2, where the solubility curve showed the crossover region between 15 and 18 MPa. At pressures lower than the crossover region, the density effect is predominant and as a result, the solubility increases with decreasing temperature. However, at pressures above the crossover point, the vapor pressure of the solution was the main factor and the solubility increased at higher temperatures. The crossover point of various pharmaceutical compounds in SC-CO<sub>2</sub> have been investigated by some other researchers, that crossover point of some of these compounds was reported in Table 4.

The crossover pressure was investigated by several articles which proposed some methods to predict the crossover pressure region [58–61]. Investigation of these methods showed the crossover region depends on the critical properties of solutes, sublimation pressure, enthalpy of sublimation, partial molar enthalpy, and molar volume of the solute. Minimum and maximum favipiravir solubility were seen at the temperature of 338 K and pressures of 12 and 30, respectively. As indicated in Table 3, the mole fraction of favipiravir in the binary system (favipiravir-SC-CO<sub>2</sub>) ranged in  $3.0 \times 10^{-6}$ -9.05  $\times 10^{-4}$ . The mole

#### Table 5

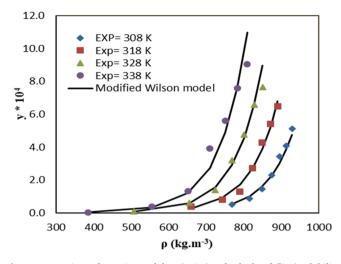
Modified Wilson model parameters for solubility of favipiravir in SC-CO2.

α	β	$\lambda'_{12}$	$\lambda'_{21}$	AARD%	R <sub>adj</sub>
-0.000027	0.000929	0.2525	15.021	10.09	0.9658

fraction of drugs in Table 4 shows a wide range of values. These values were reported between  $10^{-3}$  and  $10^{-7}$  according to the experimental conditions. The mole fraction of favipiravir also was in this range. The results present that high mole fraction values were obtained in the order of  $10^{-4}$ . As above mentioned some researchers reported that the solubility of solutes in SC-CO<sub>2</sub> can be dependent on the critical properties of solutes, sublimation pressure values, enthalpy of sublimation, partial molar enthalpy, and molar volume of solute. This experimental data can be used to develop the method for the production of favipiravir nanoparticles using SCF. This information can be also employed for the incorporation of polar co-solvent to increase the solubility.

#### 4.2. Expanded liquid theory - Modified Wilson model

The modified Wilson model was studied to model the favipiravir solubility in SC-CO<sub>2</sub>. The modified Wilson model parameters ( $\alpha$ ,  $\beta$ ,  $\lambda'_{12}$  and  $\lambda'_{21}$ ) were optimized for binary system favipiravir-SC-CO<sub>2</sub>. The results on the solubility of favipiravir in SC-CO<sub>2</sub> are listed in Table 5.



**Fig. 3.** Comparison of experimental data (point) and calculated (line) solubility of favipiravir in SC-CO<sub>2</sub> based on modified Wilson model.

Table 6 Semi-empirical modela

Semi-empirical inc	Jucia.
Name	Formula
Chrastil	$\ln S = a_0 \ln \rho + a_1 + \frac{a_2}{T}$
K-J	$\ln y_2 = a_0 + a_1 \rho + \frac{a_2}{r}$
Keshmiri et al.	$\ln y_2 = a_0 + \frac{a_1}{T} + a_2 P^2 + (a_3 + \frac{a_4}{T}) \ln \rho$
Sparks et al.	$S_{2}^{*} = \rho_{r,1}^{(a_{0}+a_{1}\rho_{r,1}+a_{2}\rho_{r,1}^{2})} exp\left(a_{3} + \frac{a_{4}}{T_{r}} + \frac{a_{5}}{T_{r}^{2}}\right) S_{2}^{*} = \frac{S}{\rho_{c,1}} S =$
	$\rho M_{w \text{ solute}} y_2$
Sodeifian et al.	$ \begin{array}{c} \overline{M_w \ _{SCF}(1-y_2)} \\ lny_2 \ = a_0 \ + a_1 \frac{P^2}{T} + a_2 ln(\rho T) \ + a_3(\rho ln\rho) \ + a_4 PlnT \ + a_5 \frac{ln\rho}{T} \end{array} $
Garlapati and Madras	$lny_{2}=a_{0}+(a_{1}+a_{2}\rho)ln\rho+\frac{a_{3}}{T}+a_{4}ln(\rho T)$

a  $a_0 - a_5$ , adjustable parameters of models.

Fig. 3 shows the experimental data and model of solubility of favipiravir in SC-CO<sub>2</sub>. As indicated in Fig. 3, the model exhibited a proper agreement with experimental solubility data of favipiravir in SC-CO<sub>2</sub>. According to Table 5, the values of AARD% and R<sub>adj</sub> were 10.09% and 0.9658. Therefore, the modified Wilson model can correlate the solubility of favipiravir at proper accuracy.

#### 4.3. Correlation of the solubility data with semi-empirical models

As presented in Table 6, six empirical density-based models (Chrastil, K-J, Keshmiri et al., Sparks et al., Sodeifian et al., and Garlapati-Madras) were used to correlate favipiravir solubility experimental data in a binary system (favipiravir-SC-CO<sub>2</sub>). The results and adjustable parameters of each empirical model are listed in Table 7.

The equation developed by K-J (AARD = 10.55%) presented the best fit compared to the other equation with three parameters namely

Chrastil (AARD = 18.61%). K-J provided a relationship between the logarithm of the mole fraction of a solute has a linear dependence on the density of the SCF phase. On the other hand, Chrastil described one of the first density-based models, based on the solvato complex formed between the solute and solvent molecules at equilibrium. However, it has some limitations in high solubility [62]. Therefore, the model described by Chrastil underwent several modifications, deriving in different equations like Adachi-Lu [63] and del Valle and Aguilera [64]. Moreover, Sparks et al. combined Adachi-Lu and del Valle- Aguilera models considering the effect of the density in the association number k and the change of the enthalpy of vaporization with the temperature. The results in Table 7 showed that Sparks et al. (AARD = 11.10%) was more adequate than Chrastil model.

Keshmiri et al. introduced a semi-empirical model based on the effect of pressure, density, and temperature. This model is expressed by a linear relationship between the logarithm of the solid solubility and the density of the  $CO_2$  and it has a strong relationship with pressure. Keshmiri's model (AARD= 15.55%) with more parameters, but the fit was worse compared to K-J and better than Chrastil. In this model, the relationship of solubility to pressure, density, and temperature are complicated.

Sodeifian et al. and Garlapti- Madras models were developed by reviewing the laboratory data and models presented. Both of them included more combined terms than K-J, but the AARDs obtained with these models were 13.45% and 11.31% respectively. The main conclusion obtained from Table 7 is that the best models for correlating favipiravir solubility were the equation developed by K-J and Sparks et al."

Furthermore, experimental data and favipiravir solubility calculated by empirical models are compared in Fig. 4. As seen, the models showed satisfactory agreement with experimental data. Using the model, total heat ( $\Delta$ Htotal = 70.09 KJ mol<sup>-1</sup>), vaporization heat ( $\Delta$ Hvap = 90.12 KJ mol<sup>-1</sup>), and solvation heat ( $\Delta$ Hsol = 20.04 KJ mol<sup>-1</sup>) can be calculated for binary system.

#### 4.4. Solubility correlation with EoS model

In this study, the SRK EoS with quadratic mixing rules was employed. Interaction parameters ( $k_{ij}$ ,  $l_{ij}$ ) are used to calculate the parameters of the SRK equation for the binary system. As previously mentioned, different group contribution (GC) methods are used to calculate the physico-chemical and critical properties of solids (drug), which can affect the correlation results (AARD) for solubility data in SC-CO<sub>2</sub> by EoS, but in many cases the results were not significantly different [65]. In the current research, the Ambrose-Walton equation [66], Immirzi and Perini [67], Edmister [66] and Marrero and Gani [68], methods were applied to determine the sublimation pressure, solid molar volume, acentric factor, critical temperature and pressure, respectively. The results of estimating of drug properties are presented in Table 2.

Moreover, interaction parameters can be written as a function of temperature:

$$l_{ij} = AT + B \tag{32}$$

$$k_{ij} = CT + D \tag{33}$$

Table 7

The correlation result	ts of the favipiravir – C	O <sub>2</sub> system provided	by semi-empirical models. <sup>a</sup> .

Model	a <sub>0</sub>	a <sub>1</sub>	a <sub>2</sub>	a <sub>3</sub>	a <sub>4</sub>	a <sub>5</sub>	a <sub>6</sub>	AARD%	R <sub>adj</sub>
Chrastil	10.01	-8267.85	-40.35	-	_	-	-	18.61	0.966
K-J	7.35	-8593.17	0.014	-	-	-	-	10.55	0.957
Keshmiri et al.	-43.11	-4486.03	0.0000129	7.99	-253.79	-	-	15.55	0.954
Sparks et al.,	4.98	2.74	16.41	-29.65	4358.15	11.14	-	11.10	0.976
Sodeifian et al.,	-16.03	-0.00506	1.58	0.0021	0.012	-1177.91	-	13.45	0.966
Garlapati and Madras	-61.13	-8.1	0.0016	-5595.52	9.29	-	-	11.31	0.956

<sup>a</sup>  $a_0 - a_6$ , adjustable parameters of models.

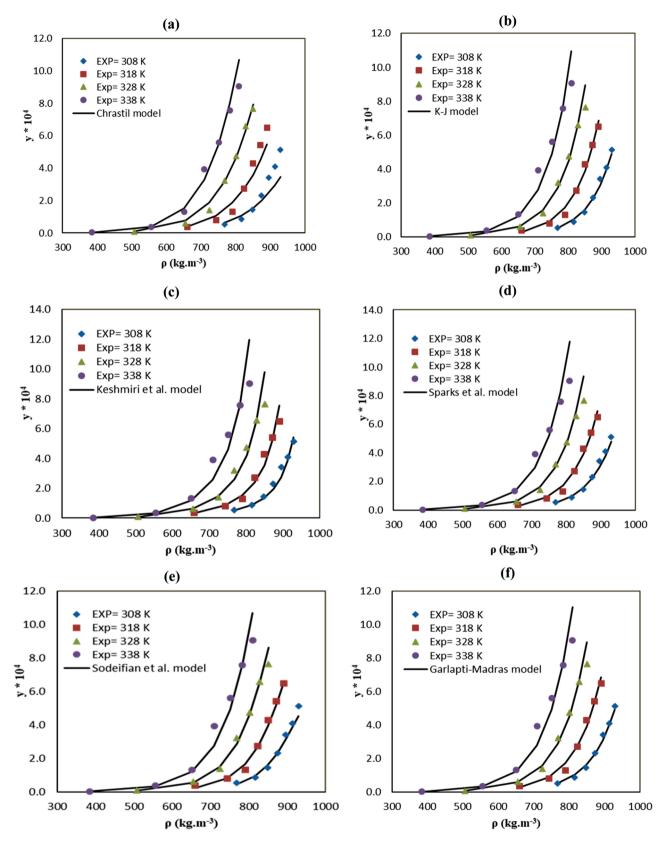
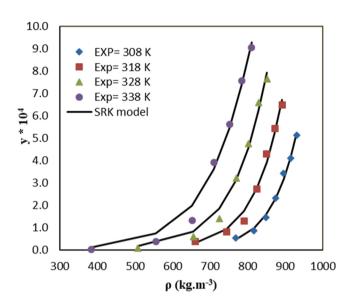


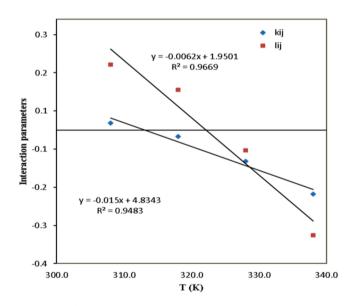
Fig. 4. Comparison of experimental (points) and calculated (line) values of favipiravir solubility based on the (a) Chrastil, (b) K-J, (c) Keshmiri (d) Sparks et al., (e) Sodeifian et al., and (f) Garlapati and Madras models at different temperatures.

Correlation results of the SRK for solubility of favipiravir in SC-CO<sub>2</sub>, interaction parameters.

Model	Parameter	$T=308\;K$	$T=318\;K$	$T=328\;K$	$T=338\;K$
SRK	k <sub>12</sub>	0.018	-0.0168	-0.0818	-0.168
	112	0.1717	0.1052	-0.053	-0.2758
	AARD	6.08	11.59	15.04	17.65
	R <sub>adj</sub>	0.996	0.986	0.975	0.965



**Fig. 5.** Comparison of experimental and calculated solubilities of favipiravir base on SRK- with quadratic mixing rules EoS.



**Fig. 6.** The influence of temperature on the binary interaction parameters for the favipiravir SC–CO<sub>2</sub> system, SRK model.

The corresponding values of interaction parameters were optimized by the simulated annealing (SA) method. The correlation results obtained with the SRK-EoS and quadratic mixing rules at four temperatures are reported in Table 8. According to AARD% values in Table 8, the interaction parameters were calculated with acceptable accuracy. However, it can be said that the accuracy of the data obtained at low temperatures (308 K) is higher than those determined at high temperatures (338 K). Fig. 5 shows the experimental solubility of favipiravir in SC-CO<sub>2</sub> at four temperatures (308, 318, 328, and 338 K) and those predicted by SRK-EoS. As indicated in Fig. 5, the SRK EoS with quadratic mixing rules was capable of corrolating solubility data. The coefficients of A, B, C, and D (Eq. (33), (34)) were calculated via linear regression analysis (Fig. 6).

#### 5. Conclusion

Proper knowledge of drug's solubility in a supercritical fluid is essential in the production of pharmaceutical micro and nanoparticles using supercritical fluids. In this study, the solubility of favipiravir in SC-CO2 was explored at the temperature range 308 - 338 K and pressure range 12-30 MPa. The solubility of favipiravir in SC-CO<sub>2</sub> varying from 0.004 to 2.618 g/L was obtained. The minimum and maximum values for favipiravir solubility were observed in the temperature of 338 K and pressures of 12 and 30 MPa. After experimental measurement of the solubility, three models including expanded liquid theory (modified Wilson model), semi-empirical density-based models (Chrastil, K-J, Keshmiri et al., Sparks et al., Sodeifian et al., and Garlapati- Madras), and equation of state (SRK with quadratic mixing rules) were used to correlate the generated solubility data. According to the results, K-J (AARD% = 10.55), Sparks et al. (AARD% = 11.1), and Garlapati and Madras (AARD% = 11.31) showed a better agreement with solubility data of favipiravir compared to SRK model (12.59%). Comparison of the models showed that the best model for correlating favipiravir solubility is the modified Wilson (AARD% = 10.09) and K-J (AARD% = 10.55).

#### **Declaration of Competing Interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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