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Accurate prediction of aqueous free solvation energies using 3D atomic feature-based graph neural network with transfer learning

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Abstract

Graph neural networks (GNNs)-based deep learning models (DL) have been widely implemented to predict experimental aqueous solvation free energy, while its prediction accuracy has reached a plateau partly due to the scarcity of available experimental data. In order to tackle this challenge, we first build a large and diverse calculated dataset Frag20-Aqsol-100K of aqueous solvation free energy with reasonable computational cost and accuracy via electronic structure calculations with continuum solvent models. Then we develop a novel 3D atomic feature-based GNN model with the Principal Neighborhood Aggregation (PNAConv), and demonstrate that 3D atomic features obtained from molecular mechanics optimized geometries can significantly improve the learning power of GNN models in predicting calculated solvation free energies. Finally, we employ a transfer learning strategy by pre-training our deep learning model on Frag20-Aqsol-100K and fine-tuning it on the small experimental dataset, and the fine-tuned model A3D-PNAConv-FT achieves the state-of-the-art prediction on the FreeSolv dataset with a root-mean-squared error of 0.719 kcal/mol and a mean-absolute error of 0.417 kcal/mol using random data splits. These results indicate that integrating molecular modeling and deep learning would be a promising strategy to develop robust prediction models in molecular science. The source code and data are accessible at: [https://yzhang.hpc.nyu.edu/IMA.](https://yzhang.hpc.nyu.edu/IMA)

Graphical Abstract

The authors declare no competing financial interest.

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The data distribution for Frag20-Aqsol-100K with fixed data split (Figure S1); The data distribution for FreeSolv with fixed data split (Figure S2); Scatter plots for the test set of FreeSolv by A3D-PNAConv-FT (Figure S3); The bond attributes and the corresponding encoding methods that are used to build the initial 2D bond feature vectors (Table S1); The message functions and updating functions in MPNN for selected GNN modules (Table S2); The atomic attributes and the corresponding encoding methods that are used to build the initial 2D atomic feature vectors (Table S3); and some key hyper parameters used for model building and training (Table S4) ; 95% confidence interval (CI) on test set (10,000 samples) of Frag20-Aqsol-100K by each GNN under 2D and A3D featurization from bootstrapping (500,000 iterations) (Table S5); Statistical analysis between 2D-DMPNN-TS (Baseline) with other variants. The underscore bold components indicate where the difference between variant models and baseline locates (Table S6)(PDF) This material is available free of charge via the Internet at [http://pubs.acs.org.](http://pubs.acs.org/)

Introduction

Solvation free energy is defined as the energy change associated with the transfer of a molecule between gas and solvent at a certain condition¹. It is closely related to many physicochemical properties including solubility and octanol-water partition coefficient, which means it can affect the pharmacokinetic parameters such as absorption, distribution, metabolism, and excretion (usually known as ADME) in human bodies²⁻⁷. It also has tight connection with biomolecular recognition and drug discovery⁸⁻¹¹. Despite the importance of the solvation free energies, experimental data are relatively sparse because accurate measurements have been very difficult and expensive^{1,12}. Meanwhile, although significant progresses have been made to develop physics based theoretical methods to model solvation, including implicit and explicit solvent models $13-20$, those relatively rigorous approaches, such as high level electronic structure methods with explicit solvent and extensive sampling, are still computationally too expensive. Thus, there is of great interest to develop efficient computational models to predict solvation free energies accurately.

In the last few years, the applications of machine learning/deep learning tools in the prediction of solvation free energy prediction have attracted great attention 2^{1-34} . Weinreich et al. employed the Kernel Ridge Regression method to predict solvation free energy for FreeSolv based on the representations of compounds computed from an ensemble of conformers generated through short MD sampling²¹. Chen et al. proposed an algebraic graph-assisted bidirectional transformer (AGBT) framework to construct molecular representations by 3D element-specific weighted colored algebraic graphs and deep bidirectional transformers, which gives rise to some of the best predictions of molecular properties using machine learning algorithms32. Meanwhile, graph neural network-based deep learning models have been successfully implemented to predict physicochemical properties such as aqueous solubilities or hydration free energies for small molecules²²⁻²⁹. Graph neural network (GNN) models take chemical information encoded by molecular graphs as the input and learn more complex knowledge hidden in raw chemical dataset and generate powerful molecular representations for different prediction tasks. As for the solvation free energy prediction, Wu et al applied a graph neural network

named message passing neural network (MPNN) to predict experimental solvation free energy for FreeSolv dataset²³. Yang et al developed a new D-MPNN model to predict experimental solvation free energy by combining learned molecular representation with molecular features²⁶. Pathak el al. proposed a graph interaction neural network by modeling both the solute and solvent and the interaction between solute and solvent to predict solvation free energy²⁸. All these GNN models performed quite similarly with the reported RMSE of around 1.0kcal/mol or larger for the FreeSolv data set. We hypothesize that such a performance plateau for GNN models to predict aqueous solvation free energies may come from several aspects, including: 1. These GNN models all rely on the atom features such as atom type and hybridization type to initialize the features for the molecular graphs³⁵, which sometimes makes the models hard to distinguish simple molecular graph structures and thus lose some expressivity $36-37$; 2. When doing the message passing, the message aggregation is often simply chosen to be the summation or average over all neighboring node representations, which may lead to the information loss; 3. The aqueous solvation free energy dataset FreeSolv consists of 642 molecules, which is orders of magnitude smaller than many other datasets used in deep learning. As DL models greatly depend on the size and quality of the training data, they can be easily overfitting on the small solvation free energy dataset, resulting in indistinguishable prediction accuracy despite their different learning powers³⁸.

In this work, in order to address data scarcity of experimental aqueous solvation free energies, we first build a large and diverse calculated dataset Frag20-Aqsol-100K of aqueous solvation free energy with reasonable computational cost and accuracy via electronic structure calculations with continuum solvent models. Then we develop a novel DL model architecture based on graph neural network (GNN) and atomic 3D features (A3D). Based on molecular mechanics optimized geometries, A3D features were calculated by atom-centered symmetry functions $(ACSF)^{39}$ that are sets of many-body interaction functions encoding atomic environments in 3D structures. PNAConv as the GNN encoder combined with A3D features clearly demonstrate its superb learning power on the Frag20-Aqsol-100K. PNAConv is an advanced architecture combining multiple message aggregators with degree-scalers, which was originally proposed by Corso et al^{36} . Here we pre-trained the model on the Frag20-Aqsol-100K and employed the transfer learning strategy⁴⁰⁻⁴² on the experimental FreeSolv dataset. The fine-tuning performance by A3D-PNAConv-FT on FreeSolv achieved RMSE of 0.719 kcal/mol and a mean-absolute error (MAE) of 0.417 kcal/mol using multiple random data splits, which reaches the experimental uncertainty of 0.60 kcal/mol for MAE^{21} . Moreover, our proposed model architecture with transfer learning strategy can make better predictions when given a training set with very small data size.

Datasets

For the experimental aqueous solvation free energy dataset, FreeSolv has been widely employed and benchmarked by various machine learning and deep learning models $1,14,21-34$. FreeSolv consists of 642 neutral compounds, each of which is identified by the SMILES, IUPAC names along with the experimental values $1,14$. The average and standard deviation of the experimental values are −3.82 kcal/mol and 4.84 kcal/mol, respectively.

Since the data size of FreeSolv is very small, we build a large and diverse calculated dataset Frag20-Aqsol-100K for pre-training by employing a computation protocol as shown in Figure 1, which has achieved reasonable accuracy and computational cost. It should be noted that only a single conformer is used in this SMD-B3LYP computational protocol to calculate the solvation free energy, which can be further improved by considering an ensemble of conformation states. This SMD_B3LYP protocol yields an MAE of 1.28 kcal/mol in comparison with corresponding experimental aqueous solvation free energies for compounds in FreeSolv and this accuracy is comparable to other modeling studies14,18. Frag20-Aqsol-100K contains 100K diverse compounds sampled from Frag20 and CSD20^{42} , which consists of both molecular mechanics and B3LYP(6-31G*) optimized 3D geometries for molecules composed of H, B, C, O, N, F, P, S, Cl, and Br with no larger than 20 heavy atoms. The 3D geometry of each molecule in Frag20 was generated with $RDKit^{43}(ETDKG^{44})$ from Simplified Molecular-Input Line-Entry System (SMILES) representation and optimized by Merck Molecular Force Field⁴⁵ (MMFF) and then optimized and property-calculated using Density Functional Theory (DFT) method at B3LYP/6-31G* level. While for CSD20, the MMFF optimizations on the crystal structures were carried out, which was followed by DFT optimization, and molecular energy calculation.

Methods

Model architecture

The general model architecture of A3D-PNAConv is shown in Figure 2. It basically has three principal components: molecule featurization, representation learning, and prediction blocks. The molecular featurization takes SMILES as inputs to generate both 3D structures and 2D graphs with explicit hydrogen atoms that are used to subsequently generate feature vectors for atoms and bonds. The encoder layers, which are used for atom embedding learning, mainly depend on the GNNs. Meanwhile, the skip-connection is applied on each GNN module and subsequently BatchNorm and activation function are applied on it as well. The atomic readout layers consist of multiple linear layers that supports the atom-level properties read-out from atom embeddings. Lastly, the atom-wise summation on the atomlevel properties is used as the final predicted molecule-level properties such as solvation free energy in this work.

Initial featurization

In the A3D-PNAConv model, 3D atomic features (A3D) are calculated by atomic-centered symmetry functions (ACSFs) based on molecular mechanics optimized geometries. ACSFs are sets of many-body functions that encode atomic environments within a molecule³⁹ and have been used to predict molecular energy by Schutt et al^{48} . Liu et al. also used ACSF descriptors as the auxiliary prediction targets when predicting quantum properties in QM9 dataset⁴⁹. The three different two-body symmetry functions we used here are $G_i^{1, Z_1}, G_i^{2, Z_1}$, and G_i^{4, Z_1, Z_2} , as shown below. The radial functions G_i^{2, Z_1} operate on the pairwise distances between atoms and can be formulated as sum of Gaussian functions multiplied by cutoff

functions f_c , and the angular functions G_i^{4, Z_1, Z_2} incorporate angles between combinations of three atoms and can be formulated as sum of cosine functions of the angle $\theta_{ijk} = (\mathbf{R}_{ij} \cdot \mathbf{R}_{ij})$ R_{ik} / $|R_{ij}$ \cdot $|R_{ik}$ \cdot centered at atom *i* multiplied by Gaussian functions and cutoff functions f_c . All the summations on *j* for $G_i^{1, Z_1}, G_i^{2, Z_1}$ and on *j*, *k* for G_i^{4, Z_1, Z_2} run over all atoms with specific atomic number.

$$
G_i^{1, Z_1} = \sum_j^{Z_1} f_c(R_{ij})
$$

$$
G_i^{2, Z_1} = \sum_j^{Z_1} e^{-\eta(R_{ij} - R_s)^2} \cdot f_c(R_{ij})
$$

$$
G_i^{4, Z_1, Z_2} = 2^{1 - \zeta} \sum_j^{Z_1} i \sum_k^{Z_2} i (1 + \lambda cos\theta_{ijk})^{\zeta} \cdot e^{-\eta(R_{ij}^2 + R_{ik}^2 + R_{jk}^2)} \cdot f_c(R_{ij}) \cdot f_c(R_{ik}) \cdot f_c(R_{jk})
$$

$$
f_c(R_{ij}) = \begin{cases} 0.5 \cdot \left[cos\left(\frac{\pi R_{ij}}{R_c}\right) + 1 \right] \\ 0 \end{cases}
$$

For radial function, R_{ij} represents the distance between *i* and *j*, R_s is center of the Gaussian functions, η is the width of the Gaussian. For angular function, λ can have the values with +1 or −1, high values of ζ yield a narrower range, and η is used to control the radial distributions. The cutoff function ensures interactions decay to zero outside the cutoff R_c . Herein, the R_c value we adopted was always equal to 6.0. For 2D featurization on each bond, the bond attributes and the corresponding encoding methods are listed in Table S1.

Message Passing Neural Network (MPNN) and PNAConv

MPNN model works on undirected graphs G, which can be described by node attributes x_v and edge attributes e_{vw} . MPNN contains two phases: a message passing phase and a readout phase. The message passing phase incorporates information across the graphs to build a neural representation of the graphs, and the readout phase utilizes the final representation of the graphs to make predictions about the graph-level or node-level properties of interest⁵⁰.

To be specific, the message passing phase runs for T steps. At each step t, the message function M_t generates messages m_t^{t+1} for ne s, and the readout phase utilizes the final representation of
out the graph-level or node-level properties of interest⁵⁰.
g phase runs for T steps. At each step t, the message
 t_v^{t+1} for next iteration associated wit node update function U_t uses the messages to update the hidden state h_t^t at each node in the graphs. The message function and node update function are shown below and in Figure 3:

$$
m_U^{t+1} = \sum_{w \in N(v)} M_I(h_U^t, h_{uv}^t, e_{vw})
$$

$$
h_U^{t+1} = U_I(h_U^t, m_U^{t+1})
$$

where $N(v)$ means the set of neighbors of v in graph G, and the initial hidden state h_v^0 is 0_{iS} same with the initial node features x_v . The message function and updating functions for selected GNN modules that we applied are shown in Table S1. Typically, different GNN

modules use slightly different MPNN mechanism to update node embeddings. Herein as for PNAConv 36 , to construct the message function, it first applied node degree to construct a scaler that was multiplied by a combination of four aggregation methods (mean, max, min, standard deviation) to obtain the Principal Neighborhood Aggregation (PNA). The PNA works on the summation of the neighboring nodes' embeddings, connected bonds' embeddings and its own embeddings to generate the messages that are subsequently concatenated with the nodes themselves to update the node embedding. Specifically, the message function for PNAConv is:

$$
m_U^t{}^{+1} = M_t(h_U^t, h_{uv}^t, e_{vw}) = \bigoplus (h_U^t + h_{uv}^t + e_{vw})
$$

 \oplus represents PNA and is formulated as: \oplus = I $S(d, \alpha = 1)$ $S(d, \alpha = -1)$ ⊗ μ σ min max

where $S(d, a) = ((\log(d+1)/\delta)^a, d > 0, -1 \quad a \quad 1.6$ is the normalization parameter and d is the node degree. The updating function for PNA is:

$$
h_U^{t+1} = U_t(h_U^t, m_U^{t+1}) = concat(h_U^t, m_U^{t+1})
$$

where *concat* means the concatenation.

Implementation and Training Details

In this work, we compared 2D to 3D featurization on the atoms under six different GNN modules and showed their performance's difference on the calculated data. For 2D featurization on atoms, the attributes and the corresponding encoding methods are listed Table S3. All 2D features for atoms and bonds are generated by RDKit⁴³, and 3D atomic features are generated from either MMFF-optimized or DFT-optimized 3D structures by Dscribe⁵¹ with the ACSF calculations, where $g2$ params were set to [[1,1], [1,2], [1,3]] for [η , R_s] in G_i^{2, Z_1} function and g4_params were set to [[1, 1, 1], [1, 2, 1], [1, 1, -1], [1, 2, -1]] for $[\eta, \zeta, \lambda]$ in G_i^{4, Z_1, Z_2} function. The initial feature sizes for 2D atoms, 2D bonds and 3D atoms are 50, 7, and 260, respectively.

We first pre-trained our models on the larger calculated dataset Frag20-Aqsol-100K such that we determined the best featurization method and GNN module. Then we fine-tuned the model on downstream experimental dataset FreeSolv. When fine-tuning the models, we initialized the models' GNN parameters from the pre-trained models and retained the whole network. All trainings were implemented by Torch-Geometric framework⁵² and performed on RTX8000 GPU. All models were trained until it reaches 1000 epoch without early stopping, and were selected based on the smallest root-mean-squared error (RMSE) for the validation set. Hyper parameters for the model building and training are presented in Table S4. To be noted, except for the default internal hyper parameters of each GNN, we adopted

same values for all other hyper parameters such as number of encoder layers, hidden size, loss function, etc.

Results and Discussion

In order to compare different GNNs' ability to learn molecular representation for solvation free energy prediction, we first built our models based on different GNN modules and trained them on Frag20-Aqsol-100K dataset, which was split into fixed train/validation/test sets with data size of 80K/10K/10K. The data distributions are shown in Figure S1 in the supporting information. The performances on the test set are shown below in Figure 4 and the statistical significance test is shown in Table S5.

The results in Figure 4 and Table S5 clearly indicate that 3D atomic features obtained from molecular mechanics-optimized or DFT-optimized geometries can significantly improve the learning power of GNN based models in predicting calculated solvation free energies over 2D features. For all six GNN models that employ different message functions, including PNAConv³⁶, D-MPNN²⁶, GIN³⁵, GINE⁵³, NNConv⁵⁰, and superGAT⁵⁴ (see details in Table S2), they roughly showed a very similar performance of around 1.2 kcal/mol of RMSE using 2D atomic features as input, ranging from 1.168 kcal/mol for PNAConv to 1.208 kcal/mol for GINConv. As for DNN-based models, on the one hand, it is not surprising that using 2D atomic features with DNN alone would yield the worse result (RMSE = 2.805 kcal/mol) meaning that the 2D atomic feature itself encodes very little molecular information. On the other hand, using A3D features with DNN alone but without any message passing achieves a much better performance (0.944 kcal/mol for A3D_{MM} and 0.707 kcal/mol for A3DQM), which clearly demonstrates that 3D atomic features encoded by atomic-centered symmetry functions (ACSFs) are excellent representations of atomic environments within a molecule. Our new finding here is that 3D atomic features obtained from molecular mechanics-optimized or DFT-optimized geometries can significantly improve the learning power of GNN models in predicting calculated solvation free energies, resulting in the performances of 0.674 kcal/mol for A3D_{MM}-PNAConv and 0.432 kcal/mol for A3D_{OM}-PNAConv. This is probably because energy related prediction tasks are highly dependent on the 3D structures of the molecules^{$48,55$}. The 2D features can only locally depicts the molecular topology rather than the complex inter-atomic relationship. Although A3D_{OM}based models outperformed A3D_{MM}-based models because the calculated solvation free energies are based on the DFT-optimized geometries, the computational cost to obtaining DFT-optimized geometries is considerably expensive, which limits its applications in many scenarios. By comparing A3D and 2D features, it can be concluded that A3D can better help our model learn to predict aqueous solvation free energy by adequately describing the atomic environment in terms of many-body functions. Meanwhile, by using A3D features, all six GNN models achieve significant better results than A3D with DNN alone. These results indicates that message passing and edge information also play important roles in the atom embedding updating, which can further improve molecule representation learning for aqueous solvation free energy prediction. In the following parts, we use $A3D$ for $A3D_{MM}$, unless indicated otherwise.

Considering that either using 2D features or A3D features, PNAConv has achieved slightly better performance than the other five GNN modules, we have used both 2D-PNAConv and A3D-PNAConv to test the transfer learning strategy for the experimental aqueous solvation free energy prediction. Here we first built our models based on PNAConv under 2D and A3D with the calculated dataset Frag20-Aqsol-100K and subsequently fine-tuned on the experimental dataset FreeSolv. We denoted the fine-tuned models 2D-PNAConv-FT and A3D-PNAConv-FT as the ones that were pre-trained on the calculated dataset Frag20- Aqsol-100K under 3D and 2D featurization, respectively. Based on the same data split (sizes for train/validation/test sets: $513/64/65$) from the MoleculeNet²³, we removed 11 compounds in the training and 1 compound in the validation set that contain element iodine, and then used the rest 502/63/65 for our models' training/validation/evaluation. We used the same data sets to train both 2D-PNAConv and A3D-PNAConv as well as two cited models D-MPNN (from ChemProp) and MPNN (from MoleculeNet), and the results are shown in Figure 5. The data distributions are available in Figure S2 in the supporting information.

As we can see from Figure 5, the fine-tuned models 2D-PNAConv-FT and A3D-PNAConv-FT outperformed other train-from-scratch (TS) models, which indicates that the pre-training on a large, calculated data can improve the fine-tuning performance on the small, experimental data. Considering that A3D-PNAConv-FT achieved the best performance (Figure 5 $\&$ S3), we carried out the ablation studies on the selections of atomic featurization methods (2D vs A3D), GNN modules (PNAConv vs DMPNN) and training strategies (TS vs FT), as shown in Figure 6 and Table S6. We can see that the improvement of A3D-PNAConv-FT against the baseline model 2D-DMPNN-TS for FreeSolv is not due to one factor alone but is a combination of three factors. The transfer learning (fine tuning from the previously trained models on the calculate data set) looks to contribute more than the change of the other two factors.

Considering that FreeSolv is a very small dataset with experimental aqueous solvation free energy, we further tested A3D-PNAConv-FT using random data splits with ratio of 8/1/1 (data size: 504/63/63) and compared results with other reported models and frameworks in Table 1. We can see that A3D-PNAConv-FT achieved the state-of-the-art performance in terms of 10-fold cross-validation (CV) results on the test set of FreeSolv, with RMSE of 0.719 kcal/mol and MAE of 0.417 kcal/mol.

Lastly, to further examine the applicability of transfer learning strategy towards training data with even smaller size, we trained a series of fine-tuned models (A3D-PNAConv-FT) by changing the train size of FreeSolv and compared their 10-fold CV performance on the test set (63 samples) of FreeSolv using random data split of ratio 8/1/1 with corresponding training-from-scratch models (A3D-PNAConv-TS). As shown in Figure 7, when given a training set of very limited data size, A3D-PNAConv-FT can yield quite good performances. The results indicate that the fine-tuned models outperformed the train-from-scratch models on the experimental dataset with a very small data size, which points a promising direction for dealing with small experimental dataset in the future.

Conclusion

At the early stages of drug discovery pipeline, data scarcity is the most common issue in the prediction of experimental physicochemical properties by deep learning models. As for experimental aqueous solvation free energy, very limited data could be used to train on to obtain a robust and reliable deep learning model. To tackle this problem, in this study we first built a calculated dataset of aqueous solvation free energy for 100K diverse compounds based on SMD calculations with reasonable accuracy and computation cost. Then we developed a novel deep learning model that was based on PNAConv and ACSF featurization of atoms to learn atom embeddings and generate powerful molecular representations for the solvation free energies. The developed A3D-PNAConv-FT model, which is pre-trained on the calculated dataset Frag20-Aqsol-100K achieving state-of-the-art performance on the FreeSolv (RMSE of 0.719 kcal/mol and MAE of 0.417 kcal/mol using random data splits with ratio of 8/1/1). In addition, with our developed model combined with the transfer learning strategy, it clearly demonstrated that the fine-tuned models outperformed the train-from-scratch models on the experimental dataset especially with very small data size, which points a promising direction for dealing with small experimental dataset in the future. However, it should be noted that the transfer learning approach applied here requires the development of a large, computed data set with reasonable accuracy, which is still an ongoing research topic and has not been achieved for many other molecular property prediction tasks.

Data and Software Availability

The calculated dataset Frag20-Aqsol-100K and the train/validation/test sets of FreeSolv are available in<https://yzhang.hpc.nyu.edu/IMA>. The data processing, model building and training have been implemented in a python package named EzChem, and are also accessible through: [https://yzhang.hpc.nyu.edu/IMA.](https://yzhang.hpc.nyu.edu/IMA) RDKit 2020.09 version, DScribe 1.2.0 version, PyTorch 1.7.1 version and PyTorch Geometrics are used to calculate initial 2D atom/bond features, 3D atom features and model building/training, respectively.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

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Figure 1.

Computation protocol: SMD_B3LYP. Starting from the SMILE of a compound, a maximum of 300 conformers are generated by RDKit⁴³ using ETKDG⁴⁴ and optimized with MMFF94 force field⁴⁵(Step 1). The conformer *i* with the lowest MMFF energy is selected (Step 2). This conformer undergoes gas-phase optimization with B3LYP(6-31G*)⁴⁶ using Gaussian16⁴⁷ (Step 3). With the optimized geometry, the SMD¹⁵ calculation with B3LYP(6-31G*) in implicit water was carried out to calculate its aqueous solvation free energy (Step 4).

Atom

atom-level properties

Atom-wise summation

Solvation Energy

Figure 2.

A3D-PNAConv model architecture for predicting solvation free energy.

Figure 3.

Node updating in MPNN. At $t = 0$, all nodes are assigned with initial features. Then at $t =$ 1, the node v's feature gets updated by incorporating information from its neighboring nodes w. This updating is repeated several times.

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Figure 4.

Performance on the test set of Frag20-Aqsol-100K by different GNN modules and DNN under A3D and 2D featurization methods. $A3D_{QM}$ and $A3D_{MM}$ are the A3D features that are calculated from DFT-optimized geometries and MMFF-optimized geometries, respectively. The value in red atop each bar are the mean RMSE on the test set by 5 runs with random weights initialization.

Figure 5.

Performance on the fixed FreeSolv test set by different models. The values atop each bar are the mean RMSE on the test set by 5 runs with different initial weights. The error bars are the standard deviation of the mean across 5 runs. 2D-PNAConv-TS and A3D-PNAConv-TS means we trained PNAConv-based model from scratch using 2D and A3D features, respectively.

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Figure 6.

The ablation studies on the selections of atomic featurization methods (2D vs A3D), GNN modules (PNAConv vs DMPNN) and training strategies (TS vs FT). Starting from 2D-DMPNN-TS (baseline), we first changed one of the three factors (that said, atomic featurization methods, GNN modules and training strategies) and kept the other two factors constant. Then we changed two of the three factors and kept the left one constant. Lastly, we changed all the three factors. The dash cyan line shows the Baseline model's RMSE.

Figure 7.

Change of model performance on FreeSolv by A3D-PNAConv-TS and A3D-PNAConv-FT with different sizes of training set. The size of validation set was kept at 63. Each data point is the mean of 10-fold CV performance on the test set, and error bar represents its standard deviations.

Table 1.

Performance of A3D-PNAConv-FT on the test set of FreeSolv with multiple random data splits in comparison with previously published models/frameworks.

 $a_{\text{The relative position matrix}$ is designed to have the inter-atomic positions, rather than individual positions, that ensure translational invariance.

b
For a given molecular structure and its SMILES strings, AG-FPs are generated from element-specific algebraic subgraphs module and BT-FPs are generated from a deep bidirectional transformer module, and then the random forest algorithm is used to fuse, rank, and select optimal fingerprints (AGBT-FPs) for machine learning.