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## Live-cell fluorescence spectral imaging as a data science challenge

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#### Abstract

Live-cell fluorescence spectral imaging is an evolving modality of microscopy that uses specific properties of fluorophores, such as excitation or emission spectra, to detect multiple molecules and structures in intact cells. The main challenge of analyzing live-cell fluorescence spectral imaging data is the precise quantification of fluorescent molecules despite the weak signals and high noise found when imaging living cells under non-phototoxic conditions. Beyond the optimization of fluorophores and microscopy setups, quantifying multiple fluorophores requires algorithms that separate or unmix the contributions of the numerous fluorescent signals recorded at the single pixel level. This review aims to provide both the experimental scientist and the data analyst with a straightforward description of the evolution of spectral unmixing algorithms for fluorophores in a pixel progressively evolved into matrix factorization, clustering, and deep learning approaches. We outline potential future trends on combining fluorescence spectral imaging with label-free detection methods, fluorescence lifetime imaging, and deep learning image analysis.

Keywords Fluorescence · Spectral imaging · Live-cell imaging · Data science · Cell biology

## Introduction

Fluorescence spectral imaging (FSI) in cell biology is an advanced type of fluorescence microscopy that generates images from a sample at different wavelengths across the electromagnetic spectrum (Hiraoka et al. 2002; Zimmermann, 2005). The set of images produced by FSI contains extensive information about the sample's fluorescent properties, which can be used to simultaneously identify several molecules or structures, given that their fluorescence signatures are different. FSI has been used to study fixed biological

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samples, such as fluorescently stained tissues, fixed cells, and microarrays (Tsurui et al. 2000; Samarov et al. 2012; Fereidouni et al. 2018; Lichten et al. 2014). However, one of the most promising applications of FSI is the simultaneous visualization and quantification of the multitude of biochemical reactions and cellular structures in living cells (Valm et al. 2017; Arguello-Miranda et al. 2018; Chen et al. 2021). The further development of live-cell fluorescence spectral imaging could hold the key to tracking entire networks or intracellular structures in real-time as cells grow and divide during healthy and disease conditions (Argüello-Miranda et al. 2021; Hedde et al. 2021; Valm et al. 2017).

Spectral imaging has been implemented in a wide range of fields including biomedical diagnostics (Campos-Delgado et al., 2019; Schröck et al. 1996; Ortega et al. 2020), quality control in crop or food science (Elmasry et al. 2012; Su and Xue 2021), multidimensional cytometry (Jiménez-Sánchez et al. 2019; Schraivogel et al. 2022), and object detection in astronomy, remote sensing, and satellite imagery (Pauca et al. 2006). However, live-cell fluorescence spectral imaging has remained exceedingly challenging due to the specific requirements of working with living cells and, crucially, the lack of specific algorithms to optimize and analyze data produced from live-cell fluorescence imaging.

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This work aims to introduce both the wet lab experimentalist and the dry-lab data analyst to the algorithmic approaches used to analyze live-cell fluorescence spectral data. This is a balancing act of finding a middle ground in the depth in which fluorescence microscopy or data science concepts are discussed. A general explanation of fluorescence or the design of spectral microscopes is omitted since excellent reviews already describe the principles of fluorescence microscopy (Lichtman and Conchello 2005; Rino et al. 2009) and the general design of spectral imaging systems (Hiraoka et al. 2002; Li et al. 2013). We focus instead on providing a unified description of the evolution of spectral unmixing approaches used in live-cell fluorescence spectral imaging. Using a preamble on the basics of live-cell fluorescence microscopy, we then discuss how the analysis of live-cell fluorescence spectral imaging can be understood as a data science challenge.

## **Basics and current limits of FSI**

In cell biology, fluorescence spectral images are produced from samples containing combinations of fluorophores, which are molecules that absorb photons at a specific wavelength and then emit photons at a longer wavelength that contain less energy (Lichtman and Conchello 2005; Rino et al. 2009). Common fluorophores in cell biology include dyes (Haraguchi et al. 2002), nanostructures (Jaiswal and Simon 2015), fluorescent biomolecule analogs (Sinkeldam et al. 2010), and fluorescent proteins (Chamberlain and Hahn 2000; Lansford et al. 2001b; Shaner et al. 2005).

The information acquired by FSI constitutes a multidimensional data set composed of wavelength-specific images (Fig. 1A). An image in this context is an array or matrix of pixels whose values depend on the fluorescence intensity of the sample at the imaging wavelength (Waters 2009). The values of a pixel at each different imaging wavelength create a single pixel spectrum (Fig. 1B), and the array of wavelength-specific images creates a data cube that has the images' length and width dimensions and a third dimension defined by the imaging wavelengths (Fig. 1C) (Deal et al. 2019; Chen et al. 2021; Li et al. 2013).

In samples containing two or more fluorophores, the images acquired at a specific wavelength can present pixels containing mixtures of fluorescent signals. The presence of mixed pixels in an image prevents the direct quantification of individual fluorophores, which requires calculating the proportion of each fluorophore in the mixed pixels by analyzing the information contained in the single-pixel spectra. This approach, known as spectral unmixing, processes fluorescent images with mixed pixels acquired at a certain wavelength to generate fluorophore-specific images for further quantitative analysis (Keshava and Mustard 2002; Zimmermann 2005; Lansford et al. 2001b).

By using spectral unmixing, the number of different features that can be simultaneously imaged is in principle equal to the number of fluorophores that can be unequivocally identified. Given that the available fluorophores for cell biology span the ultraviolet (UV), visible, and infrared (IR) portion of the electromagnetic spectrum (Shaner et al. 2005; Balleza et al. 2018), one could imagine that a high number of fluorophores could be used to study several processes or structures in living cells simultaneously. However, live-cell fluorescence microscopy is usually reduced to blue, green, and red detection channels (Ettinger and Wittmann 2014).

Why has live-cell fluorescence microscopy remained limited to three fluorescent channels? We consider that at



Fig. 1 Schematic definition of spectral imaging, pixel spectrum, and data cube. A Schematic representation of three images acquired at different  $\lambda$  wavelengths (colors) using a spectral imaging setup. The intensity value of pixel number one is shown to ease comparison.

**B** Representation of the single pixel spectrum as the values of pixel number one arranged as a vector. **C** Schematic representation of a data cube in which, besides their length and width dimensions, the images acquire a third dimension along their  $\lambda$  values

least four factors have prevented live-cell imaging from using numerous fluorophores simultaneously: (1) the requirement of customized optical equipment in spectral microscopes (Favreau et al. 2013; Abuleil and Abdulhalim 2016; Hedde et al. 2021); (2) the phototoxic effects of illuminating cells with different excitation wavelengths (Ettinger and Wittmann 2014; Icha et al. 2017; Kiepas et al. 2020); (3) the complexity of stably expressing or delivering three or more fluorophores in living cells (which is feasible in organisms such as the yeast Saccharomyces cerevisiae (Arguello-Miranda et al. 2018), but remains challenging in mammalian and plant cells despite recent advances in tandem protein expression systems (Abdeladim et al. 2019; Boone et al. 2019; Cai et al. 2013; Yang et al. 2021) or CRISPR-based approaches (Kim et al. 2021; Willems et al. 2020); and (4) the fact that algorithms for spectral unmixing of fluorophores are beyond the formal training of many cell biologists and, conversely, live-cell imaging is beyond the formal training of many data scientists (Sommer and Gerlich 2013; Noorbakhsh et al. 2019).

This review focuses on the evolution of spectral unmixing algorithms in a language that appeals to the wet lab experimental cell biologist and the computational data analyst. We emphasized the analysis of spectral fluorescence data derived from fluorescent proteins, which are the most common fluorophores used in live-cell imaging.

## Fluorescent proteins used in live-cell spectral imaging

Fluorescence microscopy in cell biology heavily relies on a wide range of dyes or fluorophores that label cellular structures or biomolecules (Vida and Emr 1995). However, despite the increase of new probes, such as quantum dots (Jaiswal and Simon 2015) and organelle-specific dyes (Tamura et al. 2020), the most common class of fluorophores in live-cell imaging are genetically encoded fluorescent proteins (Tsien 1998; Zhao et al. 2021).

Genetic engineering techniques create organisms producing genetically encoded fluorescent proteins by fusing a DNA sequence carrying the information for synthesizing a protein to a DNA sequence carrying the information for synthesizing a fluorophore (Chalfie et al. 1994; Thorn 2017). Genetically encoded protein fluorophores started with the discovery of green fluorescent protein (GFP) in jellyfish (Prasher et al. 1992) and the realization that GFP's DNA sequence could be fused to almost any protein DNA sequence (Chalfie et al. 1994).

Imaging GFP-tagged proteins in living cells quickly revealed that GFP fluorescence properties, such as intensity, spectral shape, and anisotropy, are sensitive to intracellular acidity (pH), viscosity, redox state, ionic strength, and molecular crowding (Tsien 1998; Germond et al. 2016). The performance of GFP was improved, for instance, by creating a monomeric version called mEGFP (Zacharias et al. 2002) or a "superfolder" version, called sfGFP, that reduced the time required between its initial synthesis and its proper three-dimensional folding, known as maturation time (Balleza et al. 2018; Pédelacq et al. 2006). However, these GFP variants were spectrally indistinguishable, and new fluorophores were required to answer key cell biology questions such as whether two or more proteins colocalize or act in the same biochemical pathway (Lichtman and Conchello 2005).

The search for fluorophores with a different spectral signature from GFP led to engineering GFP's DNA sequence to generate blue (Heim et al. 1994) and yellow (Ormö et al. 1996) fluorescent proteins. Eventually, new fluorescent proteins were discovered in organisms such as corals (Matz et al. 1999), algae (Nagel et al. 2003), crustaceans (Evdokimov et al. 2006), bacteria (Bellini and Papiz 2012), lancelets (Shaner et al. 2013), fish (Kumagai et al. 2013), and plants (Rodríguez-Pulido et al., 2016). Genetic and computer-aided engineering of fluorescent proteins has now produced fluorophores spanning the UV, visible, and IR range (Ai et al. 2006; Bindels et al. 2017; Chu et al. 2016; Bajar et al. 2016; Tsutsui et al. 2008). Thus, nowadays, the major constraint to visualizing multiple processes in living cells is not the lack of different fluorophores but the capacity to accurately quantify each fluorescent protein independently.

### Fluorophore properties used in FSI

Differences in excitation and emission spectra are the most utilized properties to identify and quantify fluorophores in live-cell imaging (Deal et al., 2019). The excitation spectrum corresponds to the propensity of a fluorophore to absorb photons across multiple wavelengths. The emission spectrum corresponds to the propensity of a fluorophore to emit a photon at a certain wavelength. Fluorescence microscopy setups are usually optimized to illuminate the sample at the wavelength that matches the peak of the fluorophore's excitation spectrum, while the detection system matches the peak of the emission spectrum. This strategy can detect several fluorophores with significantly different excitation/ emission spectra; however fluorescent proteins have broad excitation/emission spectra (Chen et al. 2021; Lansford et al. 2001b; Schröck et al. 1996), especially compared with the excitation or emission spectra of other fluorophores used in cell biology, such as some BODIPY dyes or quantum dots (Fig. 2A) (Loudet and Burgess 2007). Broad excitation/ emission spectra frequently overlap, leading fluorophores to be co-excited or co-detected, a problem called crosstalk or bleed-through (Fig. 2B). Co-detection of fluorescent

Fig. 2 Emission spectra comparison among common fluorophores and fluorescent proteins used in cell biology. A Reference emission spectra comparison of three fluorophores with similar emission peaks used in cell biology applications: the red fluorescent protein, mNeptune2.5 (Chu et al. 2014); the red lipid-conjugated BODIPY dye, CellTrace<sup>™</sup> BODIPY® TR methyl ester (NCBI 2021); and Invitrogen<sup>TM's</sup> streptavidinconjugated red quantum dot, Qdot® 655. Notice mNeptune2.5's broader spectrum. B Reference emission spectra comparison of superfolder green fluorescent protein (sfGFP) (Pédelacq et al. 2006), mNeon-Green (Shaner et al. 2013), and Citrine (Griesbeck et al. 2001), three green/yellow fluorophores commonly used as genetically encoded tags to fluorescently label proteins. Despite the differences in their emission peaks, the fluorophores' spectra significantly overlap, potentially leading to co-detection and preventing their simultaneous use in fluorescence microscopy. Spectra obtained from SearchLight Spectra Viewer from Semrock accessed on 11/29/2021



proteins produces images with pixels that contain a mixture of fluorescent signals preventing direct quantitative analysis of individual fluorophores (Chen et al. 2021; Zimmermann et al. 2003; Haraguchi et al. 2002; Schröck et al. 1996). Thus,

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although the number of fluorescent proteins has expanded steadily, the overlap in their excitation/emission spectra has remained a challenge for quantifying individual fluorophores in cells expressing several fluorescent proteins.

Beyond the identification of fluorophores based on their excitation/emission spectra, other fluorophore's properties could be exploited for FSI including the time between the initial excitation of a fluorophore and its return to a relaxed state, known as fluorescence lifetime (Scipioni et al. 2021; Zhao et al. 2014), the capacity of a fluorophore to directly excite a second fluorophore, known as Förster resonance energy transfer (FRET) (Tsutsui et al. 2008; Haraguchi et al. 2002; Yang et al. 2021), the reduction of the fluorophore's emission intensity under constant illumination, known as photobleaching or photostability (Orth et al. 2018), and the differential emission intensity along polarization axes, known as fluorescence anisotropy (Esposito and Venkitaraman 2019). All of the previous properties could be combined to identify multiple fluorescent targets simultaneously (Esposito and Venkitaraman 2019); however, the excitation/emission spectra are by far the most utilized fluorophore properties used in live-cell imaging.

# Experimental optimization to deal with fluorophores' spectral overlap

The detection of multiple fluorophores with overlapping excitation/emission spectra can be achieved, in part, by careful design of the spectral imaging setup (see Fig. 1 in Hiraoka et al. (2002) for schematics of FSI designs and table 3 in Li et al. (2013) for an extensive list of spectral imaging setups). Multiple fluorophores can be excited by light sources that match their excitation peaks, such as arrays of wavelength-specific LEDs (Arguello-Miranda et al. 2018), arrays of wavelength-specific lasers (Cohen et al. 2018), or tunable lasers that can generate several different wavelengths (Esposito and Venkitaraman 2019). The specificity of fluorophore excitation is also enforced by selecting wavelengths or altering light source properties using devices such as optical filters (Valm et al. 2016; Orth et al. 2018; Jeffet et al. 2021), interferometers (Schröck et al. 1996; Zhao et al. 2014), polarizers, gratings, and prisms (Valm et al. 2017; Wang et al. 2019c; Esposito and Venkitaraman 2019). Combinations of optical filters, such as bandpass filters or tunable filters, can increase the specificity of fluorophore excitation/detection by selecting specific wavelengths from the excitation or emission light source (Arguello-Miranda et al. 2018; Argüello-Miranda et al. 2022). Thin-film tunable filters (TFTF) (Favreau et al. 2013; Vissa et al. 2020), acousto-optic tunable filters (AOTF) (Chen et al. 2021; Garbacik et al. 2018), and liquid crystal tunable filters (LCTF) (Lansford et al. 2001; St-Georges-Robillard et al. 2018) are commonly used in spectral imaging because, unlike wavelength-fixed bandpass filters, several excitation wavelengths can be produced by a single tunable filter (Deal et al. 2019).

Optimized FSI setups, however, seldom prevent the co-detection of fluorescent proteins in live-cell imaging because, beyond overlapping excitation/emission spectra, the imaging process is further constrained by noise, background fluorescence, cellular autofluorescence, and phototoxicity (Icha et al. 2017; Oheim 2010; Rino et al. 2009). In most cases, even after considering the previous factors, the quantification of individual fluorophores is only possible after a proper deployment of spectral unmixing algorithms.

# Image acquisition constraints in live-cell fluorescence spectral imaging

#### Phototoxicity

Avoiding phototoxicity is the first general challenge of live-cell fluorescence imaging (Kilian et al. 2018; Kiepas et al. 2020). For this purpose, imaging wavelengths are usually set above 400 nm to prevent UV-driven deleterious reactions in biomolecules, which can trigger stress responses and activate cell surveillance mechanisms such as the DNA damage checkpoint (Icha et al. 2017; Olivieri et al. 2020). In addition, the irremediable oxidative damage produced by light-generated free radicals, such as reactive oxygen species (ROS), must be kept in check by reducing the light source intensity and exposure times (Laissue et al. 2017).

#### Weak signals

The use of dim light sources and reduced exposure times to prevent phototoxicity (Kiepas et al. 2020), and the use of optical filters to achieve specific fluorophore excitation/emission, constraint live-cell fluorescent microscopy to produce weak signals (Mandracchia et al. 2020; Mafi et al. 2019). Thus, spectral unmixing algorithms for live-cell imaging can be thought of as approaches to identify weak fluorescent signals in a noisy environment affected by background fluorescence and cellular autofluorescence (Shi et al. 2020b).

A common strategy to detect weak signals in FSI setups is the use of very sensitive detectors such as electronmultiplying, intensified, or electron-bombarded chargecoupled devices (CCDs) (Gómez-García et al. 2018; Chen et al. 2021; Cubeddu et al. 2002; Hirvonen et al. 2015), complementary metal–oxide–semiconductor (CMOS) cameras coupled to image intensifiers (Görlitz et al. 2017; Yoon et al. 2009), single-photon avalanche diodes (SPADs) devices (Garbacik et al. 2018; Connolly et al. 2021), and photomultiplier tubes (PMTs) (Valm et al. 2017; Abdeladim et al. 2019; McRae et al. 2019). These devices, however, cannot control most sources of noise, background fluorescence, and cellular autofluorescence, which must be addressed experimentally or algorithmically.

#### Noise

Noise in fluorescence microscopy can be classified as shot noise, which is signal-dependent and follows a Poisson distribution, and read noise, which is signal-independent and follows a gaussian distribution (Foi et al. 2008). Read noise has a constant variation that depends on factors such as thermal fluctuations and inaccuracies in the detectors (Waters 2009). On the other hand, shot noise is the square root of the average detected photons (Garini et al. 1999). Both types of noise have a stronger effect on weak signals, which can be illustrated by calculating the signal-to-noise ratio (SNR) given by the total number of photons divided by the noise (Garini et al. 1999; McRae et al. 2019; Okada et al. 2016). For instance, assuming only shot noise in a pixel, a signal with an average of 4 photons has a SNR  $(4/\sqrt{})$ 4) of 2, indicating that the value in the pixel is half noise, whereas a signal of 64 photons has a SNR (64/ $\sqrt{64}$ ) of 8, indicating that the value in the pixel is only 12.5% noise.

Prevention of phototoxicity, however, forces livecell spectral imaging to produce weak signals, and noise sources must be controlled by post-acquisition image filtering algorithms that model noise using Poisson/Gaussian mixtures (Foi et al. 2008), hidden Markov models (Yang and Lee 2015), or generalized threshold assessment (Luisier et al. 2011), among others.

#### Background fluorescence and autofluorescence

When imaging cells in vitro conditions, background fluorescence could be considered a source of noise generated by the cell culture medium, exchanges of cell culture medium, and the material of the structure used for cell culture such as glass slides, Petri dishes, and microfluidic devices (Ettinger and Wittmann 2014; Cordina et al. 2018; Gharia et al. 2020). Background fluorescence can be alleviated by using low-autofluorescence cell culture medium (Ettinger and Wittmann 2014; Cordina et al. 2018) and assessing the fluorescent properties of the device for cell culture (Shi et al. 2020b). When imaging cells in tissues, dedicated experimental and algorithmic approaches must be used to control the non-homogenous fluorescent background produced by out-of-focus cells and scattered light (Helmchen and Denk 2005; Mansfield et al. 2005).

Cellular autofluorescence could be considered another source of noise generated by fluorescent molecules in living cells such as aromatic amino acids (Monici 2005), metabolites (García-Plazaola et al. 2015), protein aggregates (Tikhonova et al. 2018), and certain enzymes and cofactors (Kolenc and Quinn 2019). Cellular autofluorescence is a double-edged sword; on the one hand, autofluorescence can be used for label-free tracking of cellular metabolism and the stress status of cells (Kolenc and Quinn 2019; Surre et al. 2018). On the other hand, autofluorescence signals can outcompete fluorescently tagged proteins and are hard to model since they are affected by the cell culture medium and the stress or differentiation status of the cell (Surre et al. 2018; Walsh et al. 2021; Bertolo et al. 2019; Miranda-Lorenzo et al. 2014). Autofluorescence can be experimentally quantified by simultaneously imaging a mixed population of blank cells (without any of the target fluorophores) and cells carrying fluorophores (Argüello-Miranda et al. 2022).

Measuring individual fluorophores in the presence of background fluorescence, autofluorescence, and Poisson/ gaussian noise, while preventing phototoxicity, is the essence of live-cell spectral fluorescence microscopy. Under these conditions, identifying and unmixing the signals of single fluorophores requires data-driven or computational tools (Smith et al. 2020a; Wang et al. 2019c; Garbacik et al. 2018; St-Georges-Robillard et al. 2018; Valm et al. 2017).

## The analysis of single-pixel spectra and multidimensional images or data cubes

The judicious selection of fluorophores, light sources, and optical filters can maximize the capacity of spectral microscopy to detect images corresponding to single fluorophores (Arguello-Miranda et al. 2018; Valm et al. 2017). However, even carefully designed imaging setups are unable to prevent crosstalk and bleed-through between excitation/detection channels when imaging more than five fluorophores (Argüello-Miranda et al. 2022). Once the imaging system surpasses its capacity to produce fluorophore-specific images, data-driven approaches are necessary to reveal the proportion of fluorophores contained in a pixel and reconstruct approximations of fluorophore-specific images (Orth et al. 2018; Seo et al. 2021; Rehman and Qureshi 2021; Ozkan et al. 2019).

The problem of assessing bleed-through between detection channels in fluorescence microscopy has been traditionally solved by experimentalists' careful visual inspection of whole images taken at different wavelengths. In FSI, however, distinguishing fluorophores using single-pixel spectra at multiple wavelengths escapes a human-based approach (Sommer and Gerlich 2013), and automated strategies for single-pixel analysis are necessary (Silva et al. 2019; Noorbakhsh et al. 2019; Zhao et al. 2021; Megjhani et al. 2017).

Most approaches to identify single fluorophores in spectral imaging use single-pixel spectra information to express the value registered at a single pixel as a precise mixture of different fluorophores. Such methods have evolved from linear models (Zimmermann et al. 2002; Montcuquet et al. 2010) into clustering algorithms for single-pixel classification (Rehman and Qureshi 2021; McRae et al. 2019) and deep learning approaches for spectral data cube analysis (Manifold et al. 2021; Rehman and Qureshi 2021; Smith et al. 2020a; Bhatt and Joshi 2020).

#### Data preprocessing

FSI often requires tailored raw data preprocessing to account for variable background fluorescence or illumination, autofluorescence, and noise (Lansford et al. 2001). Image preprocessing can include normalization or scaling pixel values (Zimmermann et al. 2002), the use of noise-canceling algorithms (Okada et al. 2016), foreground detection through thresholding (Leavesley et al. 2012), flat-field correction when uniform illumination is not possible (Waters 2009; Wolf 2003), and deconvolution of maximum intensity projections (Webb and Brown 2013). In the following sections, proper image preprocessing is assumed before the use of spectral unmixing algorithms.

#### Linear unmixing

The simplest model to identify the fluorophores present at a single pixel is linear unmixing (Cohen et al. 2018; Zimmermann 2005). This method assumes that the intensity value of a pixel p, in a wavelength-specific image, is the sum of the contributions of each fluorophore expressed as algebraic terms of the form  $a_{(\lambda)} \cdot f + n$  where f corresponds to the relative concentration of a fluorophore in the pixel,  $a_{(\lambda)}$  corresponds to the expected intensity of a fluorophore at the imaging  $\lambda$  wavelength, and n represents noise (Zimmermann 2005; Hiraoka et al. 2002). For simplicity, noise terms are initially ignored in the following explanation.

A single pixel p in an image containing three fluorophores acquired at  $\lambda_1$  wavelength, can be represented as follows:

$$\boldsymbol{p}_{(\lambda_1)} = \boldsymbol{a}_{1(\lambda_1)} \bullet \boldsymbol{f}_1 + \boldsymbol{a}_{2(\lambda_1)} \bullet \boldsymbol{f}_2 + \boldsymbol{a}_{3(\lambda_1)} \bullet \boldsymbol{f}_3 \tag{1}$$

Assuming three wavelength-specific images, the pixel values at each  $\lambda$  wavelength produce the following system of algebraic linear equations:

$$p_{(\lambda_1)} = a_{1(\lambda_1)} \bullet f_1 + a_{2(\lambda_1)} \bullet f_2 + a_{3(\lambda_1)} \bullet f_3$$
  

$$p_{(\lambda_2)} = a_{1(\lambda_2)} \bullet f_1 + a_{2(\lambda_2)} \bullet f_2 + a_{3(\lambda_2)} \bullet f_3$$
  

$$p_{(\lambda_3)} = a_{1(\lambda_3)} \bullet f_1 + a_{2(\lambda_3)} \bullet f_2 + a_{3(\lambda_3)} \bullet f_3$$
(2)

In this equation system, the values of the pixel p and the expected fluorophore's intensities a change in each  $\lambda$  wavelength-specific image, but the relative concentration of fluorophores  $f_1, f_2, f_3$  should be the same (Lansford et al. 2001). The equation system can be solved by entering the pixel values  $p_{(\lambda_1)}, p_{(\lambda_2)}, p_{(\lambda_3)}$  and the expected intensities of the fluorophores a at each  $\lambda$  imaging wavelength, which returns

the relative concentration of fluorophores in the pixel (Zimmermann 2005).

Importantly, solving the linear equation system involves at least two scaling operations. First, all fluorophores' spectra must be scaled between 0 and 1 and their expected intensities must be entered at unit concentration, that is, all expected fluorophores intensities in a pixel at a imaging wavelength must add to 1 (Lansford et al. 2001). Second, the solutions for each fluorophore's relative concentration are also scaled so that their sum is one (Zimmermann 2005).

While pixel values are obtained experimentally during image acquisition (Fig. 3A and B), the expected intensity of a fluorophore at a specific wavelength must be derived from a reference spectrum (Fig. 3A–C) or by determining the fluorophore's spectrum under experimental conditions (Valm et al. 2011; Mylle et al. 2013).

The linear unmixing equation system does not have a single solution; that is, different relative concentrations of fluorophores could produce similar pixel values, and the best approximation can be found using methods such as least squares (Lloyd 1982b). Solving the linear unmixing equation system reveals the proportions of each fluorophore contained in each pixel (Fig. 3D–F), producing fluorophore-specific images in which the original pixel intensity value is replaced by the calculated relative fluorophore concentration (Fig. 3G) (Zimmermann et al. 2003).

In linear unmixing methods, homogeneous background fluorescence can be treated as an "extra" fluorophore (Zimmermann 2005), and Gaussian or Poisson noise terms can be directly added to the linear equation terms (Wang and Chang 2006). For a pixel containing two fluorophores, homogenous spectral background and, for instance, an additive mixture of Poisson-Gaussian noise at the  $\lambda$  imaging wavelength, the linear unmixing equation becomes:

$$\boldsymbol{p}_{(\lambda_1)} = \boldsymbol{a}_{1(\lambda_1)} \bullet \boldsymbol{f}_1 + \boldsymbol{a}_{2(\lambda_1)} \bullet \boldsymbol{f}_2 + \boldsymbol{a}_{bg(\lambda_1)} \bullet \boldsymbol{f}_{bg} + \boldsymbol{n}$$
(3)

where  $a_{bg}$  equals the intensity of background at  $\lambda$  wavelength,  $f_{bg}$  equals the relative proportion of spectrally homogenous background fluorescence, and the term n is the result of adding Poisson and Gaussian noise. However, accurate treatments of autofluorescence or spectrally uniform background are seldom reported or assumed to be controlled by algorithms such as the maximum noise fraction transformation (Green et al. 1988).

Several methods have attempted to improve the efficiency of linear unmixing models, including vertex component analysis (VCA) (Nascimento and Dias 2005), the N-FINDR algorithm (Winter 1999), independent component analysis (ICA) (Wang and Chang 2006), and alternating projected subgradients (APS) (Zymnis



**Fig. 3** Linear unmixing model for spectral imaging data. **A–B, left** Schematic image acquisition showing the reference emission spectra of monomeric teal fluorescent protein one, mTFP1 (Ai et al. 2006), and the monomeric green fluorescent protein mNeonGreen (Shaner et al. 2013). The shaded area indicates the wavelength range of the detection channel generated using the bandpass filters **A** FF01-488/6–25 (light blue) and **B** FF01-530/11–25 (light green) from Semrock. **A–B, right** Schematic matrix representation of the mixed images collected by the wavelength-specific channels. For simplicity, only the intensity value of pixel one is shown. **C** Normalized fluorophores' expected intensities at each detection channel are derived by calculating the approximated fluorophore spectrum area that falls in the

et al. 2007). However, these methods assume that pixels' intensities originate from linear mixtures and that reference spectra remain unchanged and independent from other fluorophores under experimental conditions, which might not always be the case (Mylle et al. 2013; Balleza et al. 2018). A solution to these limitations is to determine the spectrum of each fluorophore under experimental conditions, which is the base for methods such as spectral deconvolution (Ricard and Debarbieux 2014). Nonetheless, the experimental determination of spectra is a time-consuming task when handling large numbers of fluorophores or in time-lapse experiments (Valm et al. 2016; Zimmermann 2005). For large data sets, linear unmixing might also be computationally intensive, and its accuracy decreases due to strong spectral overlap, inaccurate spectral information, low-SNR acquisitions, and the presence of nonlinear effects such as quenching, FRET, photobleaching, or multiphoton excitation (Li et al. 2013; Smith et al. 2020a; Tsurui et al. 2000). Crucially, linear unmixing does not provide a threshold criterion to classify single pixels according to fluorophores which must be addressed by data post-processing (Lansford et al. 2001).

wavelength range allowed by the filter set (shaded areas in A). **D** Linear model showing the intensity value of pixel number one as a linear combination of the multiplication of each fluorophore's expected intensity a by each fluorophore's relative concentration f at the imaging wavelength range  $\lambda$ . **E** Linear equation system to solve the relative concentration of fluorophores f in pixel number one. **F** Matrix factorization representation of the linear equation system to solve the relative concentration of fluorophores f in pixel number one. **G** Schematic unmixed fluorophore-specific images showing the linear unmixing solution of pixel number one as approximated by the least squares method (Lloyd 1982a) using the Python function *numpy.linalg.lstsq()* 

#### Nonnegative matrix factorization

The search for more computationally efficient methods to unmix fluorescent spectral imaging data led to the realization that the linear unmixing equation can be represented as a matrix multiplication problem (Pauca et al. 2006; Montcuquet et al. 2010). In fact, the terms on the right side of the linear unmixing equation system in Eq. 2 are a matrix multiplication operation in which a matrix containing the expected fluorophores' intensities at each wavelength a is multiplied by a vector containing the relative fluorophore concentrations f (compare also Fig. 3E and F). Equation 2 can be written in matrix notation as follows:

$$\begin{bmatrix} \boldsymbol{p}_{(\lambda_1)} \\ \boldsymbol{p}_{(\lambda_2)} \\ \boldsymbol{p}_{(\lambda_3)} \end{bmatrix} = \begin{bmatrix} \boldsymbol{a}_{1(\lambda_1)} & \boldsymbol{a}_{2(\lambda_1)} & \boldsymbol{a}_{3(\lambda_1)} \\ \boldsymbol{a}_{1(\lambda_2)} & \boldsymbol{a}_{2(\lambda_2)} & \boldsymbol{a}_{3(\lambda_2)} \\ \boldsymbol{a}_{1(\lambda_3)} & \boldsymbol{a}_{2(\lambda_3)} & \boldsymbol{a}_{3(\lambda_3)} \end{bmatrix} \cdot \begin{bmatrix} \boldsymbol{f}_1 \\ \boldsymbol{f}_2 \\ \boldsymbol{f}_3 \end{bmatrix}$$
(4)

For simplicity, in the previous example (Eq. 4), the factorization of a single pixel spectrum without noise is shown. However, when dealing with multiple images acquired at multiple wavelengths, the spectra of individual pixels can be represented as the columns of a matrix P which can be expressed as the multiplication of the matrix representing the expected intensities of each fluorophore at each wavelength A by a matrix representing the relative concentration of the fluorophores F, or for short:

$$\boldsymbol{P} \approx \boldsymbol{A} \boldsymbol{\bullet} \boldsymbol{F} \tag{5}$$

When represented as a matrix operation, spectral unmixing is equivalent to a matrix factorization problem (Fig. 4A–D) that consists in finding two matrices ( the expected spectra intensities A and the relative fluorophore concentrations F) whose multiplication produces a good approximation of the matrix containing the P pixel values (Wei and Wang 2020).

As with linear unmixing models, matrix factorization can take advantage of theoretical or experimental determination of the fluorophores spectra to calculate P, a case known as semi-blind matrix factorization because the fluorophore spectra information defines matrix A a priori (Rossetti et al. 2020). Blind matrix factorization algorithms have also been proposed, which can generate both the fluorophores' intensities matrix and the fluorophores' relative concentration matrix without precise a priori knowledge about the fluorophores' spectra (Pengo et al. 2013; Montcuquet et al. 2010; Seo et al. 2021; Jiménez-Sánchez et al. 2019; Neher et al. 2009). In principle, blind matrix factorization algorithms could bypass the linear unmixing models' need for reference spectra (which is an example of a general problem known as blind source separation (Sawada et al. 2019)). However, most blind matrix factorization algorithms tend to become less efficient as the number of fluorophores or spectral overlap increases; in addition, the number of fluorophores should not outnumber the detection channels (Wei and Wang 2020; Seo et al. 2021).

Examples of matrix factorization deployed in fluorescence spectral unmixing include approaches based on singular value decomposition (SVD) (Tsurui et al. 2000) and nonnegative matrix factorization (NMF) (Lee and Seung 1999). In general, these approaches iteratively optimize the values in the matrices of relative fluorophore concentrations F and expected fluorophore intensity A until their product approximates the values in the pixel spectrum matrix P (Huang et al. 2015). However, the process to approximate P can generate a high number of solutions, and optimization constraints must be imposed on the matrix factorization algorithms to efficiently find the best solution without creating high computational complexity or requiring large amounts of a priori knowledge (Ertürk 2020; Huck et al. 2010; Qian et al. 2011).

Nonnegative matrix factorization has arisen as the basis of a large number of spectral unmixing algorithms because it embodies natural constraints of spectral imaging, such as the fact that the intensity and concentration of a fluorophore are invariably positive numbers (Montcuquet et al. 2010; Pauca et al. 2006; Yokota et al. 2015). NMF algorithms can easily incorporate a priori optimization constraints, such as the expected abundance of the fluorophores (Ertürk 2020; Horisaki and Tanida 2010; Peharz and Pernkopf 2012), and assumptions about the structure of the matrices, such as their sparsity, which refers to the number of non-zero elements contained in a matrix (He et al. 2016; Aggarwal and



D) Example nonnegative matrix factorization of the form  $P \approx A \cdot F$  for spectral unmixing of the images displayed in C

Pixel values at each $\lambda$ (detection channel)						Emission intensity of each fluorophore in each detection channel						Fluorophores relative concentration in each pixel			
	Pixel 1	Pixel 2	Pixel 3	Pixel 4			mTFP1	mNG	mNer	ot		Pixel 1	Pixel 2	Pixel 3	Pixel 4
Channel 1 Channel 2 Channel 3	10 53 145	20 55 170	15 50 150	10 65 180	=	Channel 1 Channel 2 Channel 3	$\begin{bmatrix} a1_{\scriptscriptstyle(\lambda_1)}\\ a1_{\scriptscriptstyle(\lambda_2)}\\ a1_{\scriptscriptstyle(\lambda_3)} \end{bmatrix}$	$\begin{array}{l} a2_{_{(\lambda_1)}}\\ a2_{_{(\lambda_2)}}\\ a2_{_{(\lambda_3)}}\end{array}$	$\begin{bmatrix} a3_{(\lambda_1)} \\ a3_{(\lambda_2)} \\ a3_{(\lambda_3)} \end{bmatrix}$	•	mTFP1 mNG mNept	f <sub>mTFP1</sub> f <sub>mNG</sub> f <sub>mNept</sub>			

**Fig. 4** Schematic nonnegative matrix factorization spectral unmixing. **A** Generic diagram of a  $2 \times 2$  pixels image. **B** Fluorophores assumed to be present in the image. **C** Spectral image acquisition using three different detection channels showing individual pixel values. **D** 

Example of a nonnegative matrix factorization algorithm that could calculate the relative fluorophore concentration in each pixel. Notice how, in this approach, each  $2 \times 2$  image is "unraveled" into a  $1 \times 4$  row vector whose concatenation creates the matrix to be factorized

Majumdar 2016). Sparsity constraints can be implemented by assuming that mixed pixels only combine a few fluorophores (He et al. 2016). For instance, in a sample containing six fluorescent markers, an NMF sparsity constraint could state that mixed pixels can only be the combination of two fluorophores, implying that the values of the remaining four fluorophores will be equated to zero. Matrices with great sparsity can be rapidly processed using algorithms derived from fields such as compressed sensing (Liu et al. 2016). In addition, spatial information from the sample can be used as a constraint by specifying the coordinates of pixels expected to contain a precise mixture of fluorophores, for instance, when fluorescently labeled proteins interact or colocalize in a specific intracellular location (Wang et al. 2019c; Megjhani et al. 2017; Horisaki and Tanida 2010).

Spectral unmixing NMF algorithms can also include noise sources, such as Poisson/Gaussian noise (Theis et al. 2009; Qin et al. 2016), by adding a noise term N to Eq. 5:

$$\boldsymbol{P} \approx \boldsymbol{A} \boldsymbol{\cdot} \boldsymbol{F} + \boldsymbol{N} \tag{6}$$

Background fluorescence can be quantified using regularized NMF (Qin et al. 2016) or affine NMF (aNMF,(Rossetti et al. 2020)) approaches. In contrast to linear unmixing models, in aNMF background fluorescence is not treated as another fluorophore, but it is assumed to be an "offset" of the noise term (Rossetti et al. 2020) obtained by multiplying a vector composed of the background's fluorescence spectrum *b* by a row vector of ones 1:

$$\boldsymbol{P} \approx \boldsymbol{A} \boldsymbol{\cdot} \boldsymbol{F} + \boldsymbol{b} \boldsymbol{\cdot} \boldsymbol{1} + \boldsymbol{N} \tag{7}$$

Autofluorescence signals can also be separated by advanced NMF approaches, such as the semi-blind sparse affine spectral unmixing (SSASU) algorithm (Rossetti et al. 2020), sparse constrained NMF (Montcuquet et al. 2011), and specific read noise considerations (Woolfe et al. 2011). However, the use of more complicated NMF algorithms to deal with fluorescent signals, noise, background, and autofluorescence can become computationally demanding (Theis et al. 2009).

#### **Clustering algorithms**

Constrained NMF is actually a widely used clustering algorithm in machine learning (Lee and Seung 1999). This insight leads to the realization that the problem of spectral unmixing is indistinguishable from clustering and classification tasks in data science. In fact, NMF applied to spectral imaging can be understood as a clustering task in which pixels are classified as belonging to different fluorophore clusters based on similarities of spectral signatures (Montcuquet et al. 2010). The interpretation of NMF unmixing as clustering (Li et al. 2017; Oh et al. 2021) bears a crucial implication: clustering algorithms could classify the pixels of spectral images into clusters corresponding to fluorophores without reference spectra information and independently of the number of imaging channels (Fig. 5C).

Learning unsupervised means of spectra (LUMoS, McRae et al. 2019) is an example of an unmixing algorithm based on clustering that does not require reference spectra or a precise number of imaging channels. LUMoS uses a staple machine learning algorithm known as k-means (Arthur and Vassilvitskii 2007) to separate pixels into clusters corresponding to fluorophores, autofluorescence, or background. "Means of Spectra" does not refer to spectral data but to the center (centroid) of the clusters corresponding to the fluorophores that are used to classify pixels. Interestingly, LUMoS assumes that neighboring pixels often belong to the same structure and applies a median filter to the raw image, fusing neighboring pixels, before clustering. Furthermore, LUMoS assumes that each pixel is occupied by a single fluorophore and classifies mixed pixels as new clusters. Although this approach makes the affiliation of a pixel to a cluster unambiguous, it could lead to the generation of many clusters when multiple fluorophores are highly colocalized (McRae et al. 2019). A solution to this problem is to generate a predictive clustering model based on previously classified data.

A trained clustering model is an algorithm that has been optimized using past clustered results that are known to be correct and constitute a "ground truth" (Sommer and Gerlich 2013). The initial algorithm is iteratively forced to improve until its results recapitulate the clustering in the ground truth data set (Chicco 2017). Assuming that the number of clusters in a spectral imaging data set is equivalent to the number of fluorophores, spectral clustering algorithms could be classified as follows: (1) supervised, if the number of fluorophores is known a priori; (2) semi-supervised, if the number of fluorophores is specified within a range, for instance, by including background fluorescence, noise, or bona fide colocalized signals as potential additional clusters; and (3) blind or unsupervised, if the number of fluorophores is not defined before the clustering task. Although blind clustering algorithms hold the promise of revealing unsuspected correlations in a spectral data set, for instance, by showing that two fluorescent signals always colocalize, there is no universal approach to determine the optimum number of clusters in a data set (Strehl and Ghosh 2003; Senbabaoğlu et al. 2014). Although some approaches such as the silhouette method (Rousseeuw 1987), the Caliński-Harabasz criterion (Caliński and Harabasz 1974), and consensus or ensemble clustering (Monti et al. 2003) can provide an educated guess of the maximum number of clusters in a data set, the final decision can depend on empiric factors and experimental context.

A) Linear Unmixing

Requires as many imaging channels as fluorophores and the fluorophores' spectrum

Finds the relative contribution f of each fluorophore to the pixel intensity value

Solution is optimized by methods such as least squares



 $P(\lambda_1) = a_1(\lambda_1) \bullet f_1 + a_2(\lambda_1) \bullet f_2 + a_3(\lambda_1) \bullet f_3$ 

 $P(\lambda_2) = a_1(\lambda_2) \bullet f_1 + a_2(\lambda_2) \bullet f_2 + a_3(\lambda_2) \bullet f_3$ 

 $P(\lambda_2) = a_1(\lambda_2) \bullet f_1 + a_2(\lambda_2) \bullet f_2 + a_3(\lambda_2) \bullet f_3$ 

Fig. 5 Evolution of spectral unmixing models. A System of linear equations to solve the relative concentration of three fluorophores in a mixed pixel p. The pixel intensity value is assumed to be the sum of terms composed of each fluorophore's expected intensity a multiplied by each fluorophore's relative concentration f at the imaging wavelength  $\lambda$ . B Matrix factorization representation of a linear equation system to solve the relative concentration of fluorophores in a pixel. The pixel values matrix P is assumed to result from multiplying the fluorophore expected intensities matrix A by the fluorophore relative concentration approach for assigning a single pixel spectrum to a particular fluorophore that is represented as a data cluster. Notice how the single pixel spectrum

A general workflow for creating a trained clustering algorithm for spectral imaging could include the following steps (Chicco 2017; Sommer and Gerlich 2013): (1) data points (pixels groups, pixel spectra) are normalized and their index randomized; (2) data points are split into three data sets: 50% for training, 30% for validation, and 20% for testing; (3) the training data set is initially clustered using different algorithms, such as *k*-means (McRae et al. 2019) or support vector machines (SVM) (Yang et al. 2016; Shi et al. 2020a), which in turn can be optimized by changing

could be compressed to a single value in the clustering space (solid arrow) before being affiliated to a cluster by calculating, for instance, the minimum Euclidean distance between the pixel spectrum data point and the center (centroid) of the clusters representing different fluorophores (red dotted arrows). **D** Deep learning approach to spectral unmixing. Instead of assuming linearity or focusing on the single pixel spectrum, deep learning approaches use the entire data cube to find relevant features or patterns for single pixel classification into fluorophores. Green arrows represent an oversimplified information flow in a deep learning architecture designed to extract features (feature extraction) from a data cube and classify pixels (classification) according to fluorophores

their specific parameters (also known as hyperparameters) such as including spatial information, number of clusters, and criterium or distance metric to determine cluster affiliation of a data point; (4) the validation data set is labeled by experienced researchers and becomes "ground truth"; (5) clustering algorithms are iteratively optimized by comparing their clustering solutions to the "ground truth" using a measure of classification quality such as a multiclass Matthews's coefficient or a loss function; (6) the best-performing clustering model is deployed for



clustering the test data set and cross-validated with orthogonal approaches if possible; and (7) the best-performing trained algorithm is used to classify future data points, which in this case correspond to pixels from new images. In this approach, the success of the clustering algorithm heavily depends on the quality of the training data and the correctness of the ground truth (Rajkomar et al. 2019; Silva et al. 2019). Since human-classified data or humandefined features usually define the ground truth, the clustering results will recapitulate subject biases (Sommer and Gerlich 2013). **√Fig. 6** Schematic representation of a convolutional neural network (CNN) for data cube analysis using 2D convolution. A A data cube, or any other multidimensional representation of the spectral imaging data, is used as input for deep learning approaches. B The schematic CNN uses three feature extraction layers to produce feature maps of the data cube. The feature extraction process through convolution is continued in each layer using the feature maps produced by the previous layer as input. C Minimalistic schematic of feature extraction through convolution in which a kernel, or defined area in pixels, is used to scan a feature map image using two different oversimplified operations, "sum" and "average." Notice how the original feature map image has two rows and four columns, whereas, after convolution, it is reduced to one row of three pixels containing the result of the scanning process. The deep learning algorithms can find pixel classification-relevant features by selecting the feature maps that lead to successful pixel classification based on training data. D Based on features found to be good predictors of a pixel's fluorophore affiliation, pixels in the data cube are assigned to fluorophores or combinations of fluorophores

#### **Deep learning**

Deep learning offers a significant expansion of clustering models for spectral unmixing (Bhatt and Joshi 2020; Belthangady and Royer 2019). In contrast to most clustering algorithms that use human-defined features for data cube analysis, such as pixel intensity, deep learning automatically identifies classification-relevant features (Manifold et al. 2021). A deep learning system of algorithms, or architecture, uses a set of correctly classified training data to identify the pixel-or image-features that lead to successful classification (Fig. 5D) (Belthangady and Royer 2019; Wang et al. 2019a; Smith et al. 2020). Different types of deep learning architectures, such as convolutional neural networks (CNN) (Ochoa et al. 2020), autoencoders (Wang et al. 2019b; Ozkan et al. 2019), and deep belief networks (DBN) (Chen et al. 2015), could be potentially applied for spectral unmixing in live-cell imaging, as they have been deployed in remote-sensing applications (Aggarwal and Majumdar 2016; Bhatt and Joshi 2020; Bioucas-Dias et al. 2012; Ozkan et al. 2019).

Deep learning algorithms are composed of layers of operations that reduce the matrix representing an image or a data cube to a compressed matrix called *feature map*. Successful algorithms for image analysis, such as CNNs (Fig. 6A–B), are composed of layers of iterative matrix operations that reduce an image or data cube to its key features (Bhatt and Joshi 2020). Convolution refers to compressing a section of the original image to a single pixel in the feature map matrix. This operation scans the original matrix, sliding the image section, or kernel, to be compressed, for instance, one pixel at a time (Fig. 6C). The resulting "layer" comprises different feature maps resulting from different convolution operations that scanned the original matrix (Fig. 6C). The "depth" of the network depends on how many times the same process is applied to the feature maps. Deep learning algorithms first produce feature maps of the image and then *feature maps* of the feature maps and use this highly distilled information to predict pixel classification. By using training data to evaluate the importance, or weight, of each feature map for successful classification, this process can identify highly efficient, although also highly abstracted, features for single pixel classification (Fig. 6D). Although deep learning spectral unmixing does not require any prior information about the fluorophores or the imaging setup, it is in most cases limited by the availability of training data and the researchers' acceptance that after the initial feature extraction layers, the feature extraction process is hard to follow and becomes "hidden" (Tajbakhsh et al. 2016).

Unmix multiple emissions (UNMIX-ME) (Smith et al. 2020a) exemplifies an unmixing algorithm for fluorescence microscopy that uses both spectral and fluorescence lifetime imaging microscopy (FLIM) data for fluorophore unmixing. UNMIX-ME uses a CNN architecture with 2D (for images) and 3D (for data cubes) convolution layers for feature extraction. Interestingly, UNMIX-ME was trained on simulated data sets, which overcame the need for collecting a large amount of experimental training data. The algorithm was validated by processing and unmixing in vitro and in vivo data sets, including FRET and infrared spectral imaging information.

The capacity to use any pixel-associated data to identify fluorophores is the most significant promise of deep learning for spectral unmixing (Smith et al. 2020; Rehman and Qureshi 2021). As seen in remote sensing, the classification of pixels in a data cube improves by combining features beyond the spectral information, such as spatial information (Xu et al. 2020; Chen et al. 2015). A combination of spectral information and other fluorophore properties, such as fluorescence lifetime, could result in a new generation of deep learning–driven unmixing approaches for imaging multiple fluorophores in living cells.

## Outlook

We envision that future trends in live-cell fluorescence spectral imaging will include (1) the use of spectral imaging data sets to train deep learning algorithms for label-free detection of intracellular structures (Ounkomol et al. 2018; Manifold et al. 2021); (2) the use of spectral imaging to track entire biochemical pathways directly (Argüello-Miranda et al. 2022) or to in silico reconstruct biochemical pathways based on in vivo spectral fluorescence data (Yang et al. 2021); (3) the combination of spectral imaging with FLIM to enlarge the specificity, sensitivity, and combinations of fluorophores for live-cell imaging (Poland et al. 2015; Görlitz et al. 2017; Scipioni et al. 2021; Zhao et al. 2014). Recent advances in detectors and algorithms to obtain and process FLIM data using representations such as phasors (Hedde et al. 2021; Scipioni et al. 2021; Vu et al. 2022) make this approach highly relevant for creating richer data cubes for spectral unmixing or for achieving fluorophore identification independently of spectral properties (Bruschini et al. 2019; Scipioni et al. 2021; Zhao et al. 2014; Ochoa et al. 2020; Rehman and Qureshi 2021; Smith et al. 2020). However, regardless of new fluorophores, better detectors, and the inclusion of FLIM, live-cell fluorescence spectral imaging's crucial question of assigning pixels to their corresponding fluorophores is likely to remain a challenge for data science.

Author contribution JAR, JPMV, and OAM conceived the idea, performed literature research, and wrote the manuscript.

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#### Declarations

Conflict of interest The authors declare no competing interests.

### References

- Abdeladim L, Matho KS, Clavreul S, Mahou P, Sintes JM, Solinas X, Arganda-Carreras I, Turney SG, Lichtman JW, Chessel A, Bemelmans AP, Loulier K, Supatto W, Livet J, Beaurepaire E (2019) Multicolor multiscale brain imaging with chromatic multiphoton serial microscopy. Nat Commun 10:1662. https://doi. org/10.1038/s41467-019-09552-9
- Abuleil M, Abdulhalim I (2016) Narrowband multispectral liquid crystal tunable filter. Opt Lett 41:1957–1960. https://doi.org/10.1364/ OL.41.001957
- Aggarwal HK, Majumdar A (2016) Hyperspectral unmixing in the presence of mixed noise using joint-sparsity and total variation. IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing 9:4257–4266. https://doi.org/10.1109/ JSTARS.2016.2521898
- Ai HW, Henderson JN, Remington SJ, Campbell RE (2006) Directed evolution of a monomeric, bright and photostable version of Clavularia cyan fluorescent protein: structural characterization and applications in fluorescence imaging. Biochem J 400:531–540. https://doi.org/10.1042/bj20060874
- Arguello-Miranda O, Liu Y, Wood NE, Kositangool P, Doncic A (2018) Integration of multiple metabolic signals determines cell fate prior to commitment. Mol Cell 71:733-744.e11. https://doi. org/10.1016/j.molcel.2018.07.041
- Argüello-Miranda O, Marchand AJ, Kennedy T, Russo M, Noh J (2022) Cell cycle–independent integration of stress signals by Xbp1 promotes non-G1/G0 quiescence entry. J Cell Biol. 221(1): e202103171. https://doi.org/10.1083/jcb.202103171
- Arthur D, Vassilvitskii S (2007) k-means++: the advantages of careful seeding. Proceedings of the eighteenth annual ACM-SIAM

symposium on Discrete algorithms. New Orleans, Louisiana: Society for Industrial and Applied Mathematics

- Bajar BT, Wang ES, Lam AJ, Kim BB, Jacobs CL, Howe ES, Davidson MW, Lin MZ, Chu J (2016) Improving brightness and photostability of green and red fluorescent proteins for live cell imaging and FRET reporting. Sci Rep 6:20889. https://doi.org/10.1038/ srep20889
- Balleza E, Kim JM, Cluzel P (2018) Systematic characterization of maturation time of fluorescent proteins in living cells. Nat Methods 15:47–51. https://doi.org/10.1038/nmeth.4509
- Bellini D, Papiz MZ (2012) Structure of a bacteriophytochrome and light-stimulated protomer swapping with a gene repressor. Structure 20:1436–1446. https://doi.org/10.1016/j.str.2012.06.002
- Belthangady C, Royer LA (2019) Applications, promises, and pitfalls of deep learning for fluorescence image reconstruction. Nat Methods 16:1215–1225. https://doi.org/10.1038/s41592-019-0458-z
- Bertolo A, Baur M, Guerrero J, Pötzel T, Stoyanov J (2019) Autofluorescence is a reliable in vitro marker of cellular senescence in human mesenchymal stromal cells. Sci Rep 9:2074. https://doi. org/10.1038/s41598-019-38546-2
- Bhatt JS, Joshi MV (2020) Deep learning in hyperspectral unmixing: a review. IGARSS 2020 - 2020 IEEE International Geoscience and Remote Sensing Symposium, 26 Sept.-2 Oct. 2020. 2189–2192
- Bindels DS, Haarbosch L, Van Weeren L, Postma M, Wiese KE, Mastop M, Aumonier S, Gotthard G, Royant A, Hink MA, Gadella TW Jr (2017) mScarlet: a bright monomeric red fluorescent protein for cellular imaging. Nat Methods 14:53–56. https://doi.org/ 10.1038/nmeth.4074
- Bioucas-Dias JM, Plaza A, Dobigeon N, Parente M, Du Q, Gader P, Chanussot J (2012) Hyperspectral unmixing overview: geometrical, statistical, and sparse regression-based approaches. IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing 5:354–379. https://doi.org/10.1109/JSTARS. 2012.2194696
- Boone PG, Rochelle LK, Ginzel JD, Lubkov V, Roberts WL, Nicholls PJ, Bock C, Flowers ML, Von Furstenberg RJ, Stripp BR, Agarwal P, Borowsky AD, Cardiff RD, Barak LS, Caron MG, Lyerly HK, Snyder JC (2019) A cancer rainbow mouse for visualizing the functional genomics of oncogenic clonal expansion. Nat Commun 10:5490. https://doi.org/10.1038/s41467-019-13330-y
- Bruschini C, Homulle H, Antolovic IM, Burri S, Charbon E (2019) Single-photon avalanche diode imagers in biophotonics: review and outlook. Light: Sci Appl 8:87. https://doi.org/10.1038/ s41377-019-0191-5
- Cai D, Cohen KB, Luo T, Lichtman JW, Sanes JR (2013) Improved tools for the Brainbow toolbox. Nat Methods 10:540–547. https:// doi.org/10.1038/nmeth.2450
- Caliński T, Harabasz J (1974) A dendrite method for cluster analysis. Commun Stat 3:1–27. https://doi.org/10.1080/0361092740 8827101
- Campos-Delgado DU, Gutierrez-Navarro O, Rico-Jimenez JJ, Duran E, Fabelo H, Ortega S, Callicó GM, Jo JA (2019) Extended blind end-member and abundance extraction for biomedical imaging applications. IEEE Access 7:178539–178552. https://doi.org/10. 1109/access.2019.2958985
- Chalfie M, Tu Y, Euskirchen G, Ward WW, Prasher DC (1994) Green fluorescent protein as a marker for gene expression. Science 263:802–805. https://doi.org/10.1126/science.8303295
- Chamberlain C, Hahn KM (2000) Watching proteins in the wild: fluorescence methods to study protein dynamics in living cells. Traffic 1:755–762. https://doi.org/10.1034/j.1600-0854.2000. 011002.x
- Chen K, Yan R, Xiang L, Xu K (2021) Excitation spectral microscopy for highly multiplexed fluorescence imaging and quantitative biosensing. *Light: Science & Applications*, 10:97. https://doi. org/10.1038/s41377-021-00536-3

- Chen Y, Zhao X, Jia X (2015) Spectral-Spatial classification of hyperspectral data based on deep belief network. IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing 8:2381–2392. https://doi.org/10.1109/JSTARS.2015. 2388577
- Chicco D (2017) Ten quick tips for machine learning in computational biology. BioData Mining 10:35. https://doi.org/10.1186/ s13040-017-0155-3
- Chu J, Haynes RD, Corbel SY, Li P, González-González E, Burg JS, Ataie NJ, Lam AJ, Cranfill PJ, Baird MA, Davidson MW, Ng HL, Garcia KC, Contag CH, Shen K, Blau HM, Lin MZ (2014) Non-invasive intravital imaging of cellular differentiation with a bright red-excitable fluorescent protein. Nat Methods 11:572–578. https://doi.org/10.1038/nmeth.2888
- Chu J, Oh Y, Sens A, Ataie N, Dana H, Macklin JJ, Laviv T, Welf ES, Dean KM, Zhang F, Kim BB, Tang CT, Hu M, Baird MA, Davidson MW, Kay MA, Fiolka R, Yasuda R, Kim DS, Ng HL, Lin MZ (2016) A bright cyan-excitable orange fluorescent protein facilitates dual-emission microscopy and enhances bioluminescence imaging in vivo. Nat Biotechnol 34:760–767. https://doi.org/10.1038/nbt.3550
- Cohen S, Valm AM, Lippincott-Schwartz J (2018) Multispectral live-cell imaging. Curr Protoc Cell Biol 79:e46. https://doi. org/10.1002/cpcb.46
- Connolly PWR, Valli J, Shah YD, Altmann Y, Grant J, Accarino C, Rickman C, Cumming DRS, Buller GS (2021) Simultaneous multi-spectral, single-photon fluorescence imaging using a plasmonic colour filter array. J Biophotonics 14:e202000505. https://doi.org/10.1002/jbio.202000505
- Cordina NM, Sayyadi N, Parker LM, Everest-Dass A, Brown LJ, Packer NH (2018) Reduced background autofluorescence for cell imaging using nanodiamonds and lanthanide chelates. Sci Rep 8:4521. https://doi.org/10.1038/s41598-018-22702-1
- Cubeddu R, Comelli D, D'andrea C, Taroni P, Valentini G (2002) Time-resolved fluorescence imaging in biology and medicine. J Phys D Appl Phys 35:R61–R76. https://doi.org/10.1088/0022-3727/35/9/201
- Deal J, Britain A, Rich T, Leavesley S (2019) Excitation-scanning hyperspectral imaging microscopy to efficiently discriminate fluorescence signals. J vis Exp. https://doi.org/10.3791/59448
- Elmasry G, Barbin DF, Sun DW, Allen P (2012) Meat quality evaluation by hyperspectral imaging technique: an overview. Crit Rev Food Sci Nutr 52:689–711. https://doi.org/10.1080/10408 398.2010.507908
- Ertürk A (2020) Constrained nonnegative matrix factorization for hyperspectral change detection. 2020 Mediterranean and Middle-East Geoscience and Remote Sensing Symposium (M2GARSS), 9–11 March 2020. 49–52
- Esposito A, Venkitaraman AR (2019) Enhancing biochemical resolution by hyperdimensional imaging microscopy. Biophys J 116:1815–1822. https://doi.org/10.1016/j.bpj.2019.04.015
- Ettinger A, Wittmann T (2014) Fluorescence live cell imaging. Methods Cell Biol 123:77–94. https://doi.org/10.1016/B978-0-12-420138-5.00005-7
- Evdokimov AG, Pokross ME, Egorov NS, Zaraisky AG, Yampolsky IV, Merzlyak EM, Shkoporov AN, Sander I, Lukyanov KA, Chudakov DM (2006) Structural basis for the fast maturation of Arthropoda green fluorescent protein. EMBO Rep 7:1006– 1012. https://doi.org/10.1038/sj.embor.7400787
- Favreau P, Hernandez C, Lindsey A, Alvarez D, Rich T, Prabhat P, Leavesley S (2013) Thin-film tunable filters for hyperspectral fluorescence microscopy. Journal of Biomedical Optics 19:011017
- Fereidouni F, Griffin C, Todd A, Levenson R (2018) Multispectral analysis tools can increase utility of RGB color images in histology. J Opt 20. https://doi.org/10.1088/2040-8986/aab0e8

- Foi A, Trimeche M, Katkovnik V, Egiazarian K (2008) Practical Poissonian-Gaussian noise modeling and fitting for single-image rawdata. IEEE Trans Image Process 17:1737–1754. https://doi.org/ 10.1109/TIP.2008.2001399
- Garbacik ET, Sanz-Paz M, Borgman KJE, Campelo F, Garcia-Parajo MF (2018) Frequency-encoded multicolor fluorescence imaging with single-photon-counting color-blind detection. Biophys J 115:725–736. https://doi.org/10.1016/j.bpj.2018.07.008
- García-Plazaola JI, Fernández-Marín B, Duke SO, Hernández A, López-Arbeloa F, Becerril JM (2015) Autofluorescence: biological functions and technical applications. Plant Sci 236:136–145. https://doi.org/10.1016/j.plantsci.2015.03.010
- Garini Y, Gil A, Bar-Am I, Cabib D, Katzir N (1999) Signal to noise analysis of multiple color fluorescence imaging microscopy. Cytometry 35:214–226. https://doi.org/10.1002/(sici)1097-0320(19990301)35:3%3c214::aid-cyto4%3e3.0.co;2-d
- Germond A, Fujita H, Ichimura T, Watanabe TM (2016) Design and development of genetically encoded fluorescent sensors to monitor intracellular chemical and physical parameters. Biophys Rev 8:121–138. https://doi.org/10.1007/s12551-016-0195-9
- Gharia A, Papageorgiou EP, Giverts S, Park C, Anwar M (2020) Signal to noise ratio as a cross-platform metric for intraoperative fluorescence imaging. Mol Imaging 19:1536012120913693. https:// doi.org/10.1177/1536012120913693
- Gómez-García PA, Garbacik ET, Otterstrom JJ, Garcia-Parajo MF, Lakadamyali M (2018) Excitation-multiplexed multicolor superresolution imaging with fm-STORM and fm-DNA-PAINT. Proc Natl Acad Sci U S A 115:12991–12996. https://doi.org/10.1073/ pnas.1804725115
- Görlitz F, Corcoran DS, Garcia Castano EA, Leitinger B, Neil MAA, Dunsby C, French PMW (2017) Mapping molecular function to biological nanostructure: combining structured illumination microscopy with fluorescence lifetime imaging (SIM + FLIM). Photonics 4:40
- Green AA, Berman M, Switzer P, Craig MD (1988) A transformation for ordering multispectral data in terms of image quality with implications for noise removal. IEEE Trans Geosci Remote Sens 26:65–74. https://doi.org/10.1109/36.3001
- Griesbeck O, Baird GS, Campbell RE, Zacharias DA, Tsien RY (2001) Reducing the environmental sensitivity of yellow fluorescent protein. Mechanism and Applications. J Biol Chem 276:29188– 29194. https://doi.org/10.1074/jbc.M102815200
- Haraguchi T, Shimi T, Koujin T, Hashiguchi N, Hiraoka Y (2002) Spectral imaging fluorescence microscopy. Genes Cells 7:881– 887. https://doi.org/10.1046/j.1365-2443.2002.00575.x
- He W, Zhang H, Zhang L (2016) Sparsity-regularized robust nonnegative matrix factorization for hyperspectral unmixing. IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing 9:4267–4279. https://doi.org/10.1109/JSTARS. 2016.2519498
- Hedde PN, Cinco R, Malacrida L, Kamaid A, Gratton E (2021) Phasorbased hyperspectral snapshot microscopy allows fast imaging of live, three-dimensional tissues for biomedical applications. Commun Biol 4:721. https://doi.org/10.1038/s42003-021-02266-z
- Heim R, Prasher DC, Tsien RY (1994) Wavelength mutations and posttranslational autoxidation of green fluorescent protein. Proc Natl Acad Sci 91:12501. https://doi.org/10.1073/pnas.91.26.12501
- Helmchen F, Denk W (2005) Deep tissue two-photon microscopy. Nat Methods 2:932–940. https://doi.org/10.1038/nmeth818
- Hiraoka Y, Shimi T, Haraguchi T (2002) Multispectral imaging fluorescence microscopy for living cells. Cell Struct Funct 27:367–374. https://doi.org/10.1247/csf.27.367
- Hirvonen LM, Jiggins S, Sergent N, Zanda G, Suhling K (2015) Photon counting imaging with an electron-bombarded CCD: towards wide-field time-correlated single photon counting (TCSPC).

Nucl Instrum Methods Phys Res, Sect A 787:323–327. https:// doi.org/10.1016/j.nima.2015.01.031

- Horisaki R, Tanida J (2010) Multi-channel data acquisition using multiplexed imaging with spatial encoding. Opt Express 18:23041– 23053. https://doi.org/10.1364/oe.18.023041
- Huang S, Zhao Y, Qin B (2015) Two-hierarchical nonnegative matrix factorization distinguishing the fluorescent targets from autofluorescence for fluorescence imaging. Biomed Eng Online 14:116. https://doi.org/10.1186/s12938-015-0107-4
- Huck A, Guillaume M, Blanc-Talon J (2010) Minimum dispersion constrained nonnegative matrix factorization to unmix hyperspectral data. IEEE Trans Geosci Remote Sens 48:2590–2602. https://doi. org/10.1109/TGRS.2009.2038483
- Icha J, Weber M, Waters JC, Norden C (2017) Phototoxicity in live fluorescence microscopy, and how to avoid it. BioEssays 39. https://doi.org/10.1002/bies.201700003
- Jaiswal JK, Simon SM (2015) Imaging live cells using quantum dots. Cold Spring Harb Protoc 2015:619–625. https://doi.org/10.1101/ pdb.top086322
- Jeffet J, Ionescu A, Michaeli Y, Torchinsky D, Perlson E, Craggs TD, Ebenstein Y (2021) Multimodal single-molecule microscopy with continuously controlled spectral resolution. Biophysical Reports 1:100013. https://doi.org/10.1016/j.bpr.2021.100013
- Jiménez-Sánchez D, Ariz M, Morgado JM, Cortés-Domínguez I, Ortiz-De-Solórzano C (2019) NMF-RI: blind spectral unmixing of highly mixed multispectral flow and image cytometry data. Bioinformatics 36:1590–1598. https://doi.org/10.1093/bioin formatics/btz751
- Keshava N, Mustard JF (2002) Spectral unmixing. IEEE Signal Process Mag 19:44–57. https://doi.org/10.1109/79.974727
- Kiepas A, Voorand E, Mubaid F, Siegel PM, Brown CM (2020) Optimizing live-cell fluorescence imaging conditions to minimize phototoxicity. J Cell Sci 133. https://doi.org/10.1242/jcs.242834
- Kilian N, Goryaynov A, Lessard MD, Hooker G, Toomre D, Rothman JE, Bewersdorf J (2018) Assessing photodamage in live-cell STED microscopy. Nat Methods 15:755–756. https://doi.org/10. 1038/s41592-018-0145-5
- Kim S, Ren E, Casanova PM, Piddini E, Salas RC (2021) Multiplexed live visualization of cell fate dynamics in hPSCs at single-cell resolution. *bioRxiv*, 2021.01.30.428961. https://doi.org/10.1101/ 2021.01.30.428961
- Kolenc OI, Quinn KP (2019) Evaluating cell metabolism through autofluorescence imaging of NAD(P)H and FAD. Antioxid Redox Signal 30:875–889. https://doi.org/10.1089/ars.2017.7451
- Kumagai A, Ando R, Miyatake H, Greimel P, Kobayashi T, Hirabayashi Y, Shimogori T, Miyawaki A (2013) A bilirubin-inducible fluorescent protein from eel muscle. Cell 153:1602–1611. https://doi.org/10.1016/j.cell.2013.05.038
- Laissue PP, Alghamdi RA, Tomancak P, Reynaud EG, Shroff H (2017) Assessing phototoxicity in live fluorescence imaging. Nat Methods 14:657–661. https://doi.org/10.1038/nmeth.4344
- Lansford R, Bearman G, Fraser SE (2001) Resolution of multiple green fluorescent protein color variants and dyes using two-photon microscopy and imaging spectroscopy. J Biomed Opt 6:311–318. https://doi.org/10.1117/1.1383780
- Leavesley SJ, Annamdevula N, Boni J, Stocker S, Grant K, Troyanovsky B, Rich TC, Alvarez DF (2012) Hyperspectral imaging microscopy for identification and quantitative analysis of fluorescently-labeled cells in highly autofluorescent tissue. J Biophotonics 5:67–84. https://doi.org/10.1002/jbio.201100066
- Lee DD, Seung HS (1999) Learning the parts of objects by non-negative matrix factorization. Nature 401:788–791. https://doi.org/ 10.1038/44565
- Li Q, He X, Wang Y, Liu H, Xu D, Guo F (2013) Review of spectral imaging technology in biomedical engineering: achievements

and challenges. J Biomed Opt 18:100901. https://doi.org/10. 1117/1.Jbo.18.10.100901

- Li X, Cui G, Dong Y (2017) Graph regularized non-negative low-rank matrix factorization for image clustering. IEEE Trans Cybern 47:3840–3853. https://doi.org/10.1109/tcyb.2016.2585355
- Lichten CA, White R, Clark IBN, Swain PS (2014) Unmixing of fluorescence spectra to resolve quantitative time-series measurements of gene expression in plate readers. BMC Biotechnol 14:11. https://doi.org/10.1186/1472-6750-14-11
- Lichtman JW, Conchello JA (2005) Fluorescence microscopy. Nat Methods 2:910–919. https://doi.org/10.1038/nmeth817
- Liu Z, Tan S, Wu J, Li E, Shen X, Han S (2016) Spectral camera based on ghost imaging via sparsity constraints. Sci Rep 6:25718. https://doi.org/10.1038/srep25718
- Lloyd S (1982) Least squares quantization in PCM. IEEE Trans Inf Theory 28:129–137. https://doi.org/10.1109/TIT.1982.1056489
- Loudet A, Burgess K (2007) BODIPY dyes and their derivatives: syntheses and spectroscopic properties. Chem Rev 107:4891–4932. https://doi.org/10.1021/cr078381n
- Luisier F, Blu T, Unser M (2011) Image denoising in mixed Poisson-Gaussian noise. IEEE Trans Image Process 20:696–708. https:// doi.org/10.1109/TIP.2010.2073477
- Mafi M, Martin H, Cabrerizo M, Andrian J, Barreto A, Adjouadi M (2019) A comprehensive survey on impulse and Gaussian denoising filters for digital images. Signal Process 157:236–260. https:// doi.org/10.1016/j.sigpro.2018.12.006
- Mandracchia B, Hua X, Guo C, Son J, Urner T, Jia S (2020) Fast and accurate sCMOS noise correction for fluorescence microscopy. Nat Commun 11:94. https://doi.org/10.1038/ s41467-019-13841-8
- Manifold B, Men S, Hu R, Fu D (2021) A versatile deep learning architecture for classification and label-free prediction of hyperspectral images. Nature Machine Intelligence 3:306–315. https:// doi.org/10.1038/s42256-021-00309-y
- Mansfield JR, Gossage KW, Hoyt CC, Levenson RM (2005) Autofluorescence removal, multiplexing, and automated analysis methods for in-vivo fluorescence imaging. J Biomed Opt 10:41207. https://doi.org/10.1117/1.2032458
- Matz MV, Fradkov AF, Labas YA, Savitsky AP, Zaraisky AG, Markelov ML, Lukyanov SA (1999) Fluorescent proteins from nonbioluminescent Anthozoa species. Nat Biotechnol 17:969–973. https://doi.org/10.1038/13657
- Mcrae TD, Oleksyn D, Miller J, Gao YR (2019) Robust blind spectral unmixing for fluorescence microscopy using unsupervised learning. PLoS ONE 14:e0225410. https://doi.org/10.1371/journal. pone.0225410
- Megjhani M, Correa De Sampaio P, Leigh Carstens J, Kalluri R, Roysam B (2017) Morphologically constrained spectral unmixing by dictionary learning for multiplex fluorescence microscopy. Bioinformatics 33:2182–2190. https://doi.org/10.1093/ bioinformatics/btx108
- Miranda-Lorenzo I, Dorado J, Lonardo E, Alcala S, Serrano AG, Clausell-Tormos J, Cioffi M, Megias D, Zagorac S, Balic A, Hidalgo M, Erkan M, Kleeff J, Scarpa A, Sainz B Jr, Heeschen C (2014) Intracellular autofluorescence: a biomarker for epithelial cancer stem cells. Nat Methods 11:1161–1169. https://doi.org/10.1038/ nmeth.3112
- Monici M (2005) Cell and tissue autofluorescence research and diagnostic applications. Biotechnol Annu Rev 11:227–56. https:// doi.org/10.1016/s1387-2656(05)11007-2
- Montcuquet AS, Hervé L, Navarro F, Dinten JM, Mars JI (2010) Nonnegative matrix factorization: a blind spectra separation method for in vivo fluorescent optical imaging. J Biomed Opt 15:056009. https://doi.org/10.1117/1.3491796

- Montcuquet AS, Hervé L, Navarro F, Dinten JM, Mars JI (2011) In vivo fluorescence spectra unmixing and autofluorescence removal by sparse nonnegative matrix factorization. IEEE Trans Biomed Eng 58:2554–2565. https://doi.org/10.1109/tbme.2011. 2159382
- Monti S, Tamayo P, Mesirov J, Golub T (2003) Consensus clustering: a resampling-based method for class discovery and visualization of gene expression microarray data. Mach Learn 52:91–118. https://doi.org/10.1023/A:1023949509487
- Mylle E, Codreanu M-C, Boruc J, Russinova E (2013) Emission spectra profiling of fluorescent proteins in living plant cells. Plant Methods 9:10. https://doi.org/10.1186/1746-4811-9-10
- Nagel G, Szellas T, Huhn W, Kateriya S, Adeishvili N, Berthold P, Ollig D, Hegemann P, Bamberg E (2003) Channelrhodopsin-2, a directly light-gated cation-selective membrane channel. Proc Natl Acad Sci U S A 100:13940–13945. https://doi.org/10. 1073/pnas.1936192100
- Nascimento JMP, Dias JMB (2005) Vertex component analysis: a fast algorithm to unmix hyperspectral data. IEEE Trans Geosci Remote Sens 43:898–910. https://doi.org/10.1109/TGRS. 2005.844293
- Ncbi (2021) PubChem Compound Summary for CID 25164039, BODIPY TR methyl ester [Online]. Available: https://pubch em.ncbi.nlm.nih.gov/compound/BODIPY-TR-methyl-ester. Accessed 8 Dec 2021
- Neher RA, Mitkovski M, Kirchhoff F, Neher E, Theis FJ, Zeug A (2009) Blind source separation techniques for the decomposition of multiply labeled fluorescence images. Biophys J 96:3791–3800. https://doi.org/10.1016/j.bpj.2008.10.068
- Noorbakhsh J, Chandok H, Karuturi RKM, George J (2019) Machine learning in biology and medicine. Advances in Molecular Pathology 2:143–152. https://doi.org/10.1016/j.yamp.2019. 07.010
- Ochoa M, Rudkouskaya A, Yao R, Yan P, Barroso M, Intes X (2020) High compression deep learning based single-pixel hyperspectral macroscopic fluorescence lifetime imaging in vivo. Biomed Opt Express 11:5401–5424. https://doi.org/10.1364/BOE.396771
- Oh S, Park H, Zhang X (2021) Hybrid clustering of single-cell gene expression and spatial information via integrated NMF and *k*-means. Front Genet 12:763263. https://doi.org/10.3389/fgene. 2021.763263
- Oheim M (2010) Instrumentation for live-cell imaging and main formats. Methods Mol Biol 591:3–16. https://doi.org/10.1007/ 978-1-60761-404-3\_1
- Okada M, Ishikawa T, Ikegaya Y (2016) A computationally efficient filter for reducing shot noise in low S/N data. PLoS ONE 11:e0157595. https://doi.org/10.1371/journal.pone.0157595
- Olivieri M, Cho T, Álvarez-Quilón A, Li K, Schellenberg MJ, Zimmermann M, Hustedt N, Rossi SE, Adam S, Melo H, Heijink AM, Sastre-Moreno G, Moatti N, Szilard RK, Mcewan A, Ling AK, Serrano-Benitez A, Ubhi T, Feng S, Pawling J, Delgado-Sainz I, Ferguson MW, Dennis JW, Brown GW, Cortés-Ledesma F, Williams RS, Martin A, Xu D, Durocher D (2020) A genetic map of the response to DNA damage in human cells. Cell 182:481-496. e21. https://doi.org/10.1016/j.cell.2020.05.040
- Ormö M, Cubitt AB, Kallio K, Gross LA, Tsien RY, Remington SJ (1996) Crystal structure of the Aequorea victoria green fluorescent protein. Science 273:1392–1395. https://doi.org/10.1126/ science.273.5280.1392
- Ortega S, Halicek M, Fabelo H, Callico GM, Fei B (2020) Hyperspectral and multispectral imaging in digital and computational pathology: a systematic review [Invited]. Biomed Opt Express 11:3195–3233. https://doi.org/10.1364/BOE.386338
- Orth A, Ghosh RN, Wilson ER, Doughney T, Brown H, Reineck P, Thompson JG, Gibson BC (2018) Super-multiplexed

fluorescence microscopy via photostability contrast. Biomed Opt Express 9:2943–2954. https://doi.org/10.1364/boe.9.002943

- Ounkomol C, Seshamani S, Maleckar MM, Collman F, Johnson GR (2018) Label-free prediction of three-dimensional fluorescence images from transmitted-light microscopy. Nat Methods 15:917– 920. https://doi.org/10.1038/s41592-018-0111-2
- Ozkan S, Kaya B, Akar GB (2019) EndNet: sparse autoencoder network for endmember extraction and hyperspectral unmixing. IEEE Trans Geosci Remote Sens 57:482–496. https://doi.org/ 10.1109/TGRS.2018.2856929
- Pauca VP, Piper J, Plemmons RJ (2006) Nonnegative matrix factorization for spectral data analysis. Linear Algebra Appl 416:29–47. https://doi.org/10.1016/j.laa.2005.06.025
- Pédelacq JD, Cabantous S, Tran T, Terwilliger TC, Waldo GS (2006) Engineering and characterization of a superfolder green fluorescent protein. Nat Biotechnol 24:79–88. https://doi.org/10.1038/ nbt1172
- Peharz R, Pernkopf F (2012) Sparse nonnegative matrix factorization with *l*0-constraints. Neurocomputing 80:38–46. https://doi.org/ 10.1016/j.neucom.2011.09.024
- Pengo T, Muñoz-Barrutia A, Zudaire I, Ortiz-De-Solorzano C (2013) Efficient blind spectral unmixing of fluorescently labeled samples using multi-layer non-negative matrix factorization. PLoS ONE 8:e78504. https://doi.org/10.1371/journal.pone.0078504
- Poland SP, Krstajić N, Monypenny J, Coelho S, Tyndall D, Walker RJ, Devauges V, Richardson J, Dutton N, Barber P, Li DD, Suhling K, Ng T, Henderson RK, Ameer-Beg SM (2015) A high speed multifocal multiphoton fluorescence lifetime imaging microscope for live-cell FRET imaging. Biomed Opt Express 6:277–296. https://doi.org/10.1364/boe.6.000277
- Prasher DC, Eckenrode VK, Ward WW, Prendergast FG, Cormier MJ (1992) Primary structure of the Aequorea victoria greenfluorescent protein. Gene 111:229–233. https://doi.org/10.1016/ 0378-1119(92)90691-H
- Qian Y, Jia S, Zhou J, Robles-Kelly A (2011) Hyperspectral unmixing via L1/2 sparsity-constrained nonnegative matrix factorization. IEEE Trans Geosci Remote Sens 49:4282–4297. https://doi.org/ 10.1109/TGRS.2011.2144605
- Qin B, Hu C, Huang S (2016) Target/background classification regularized nonnegative matrix factorization for fluorescence unmixing. IEEE Trans Instrum Meas 65:874–889. https://doi.org/10.1109/ TIM.2016.2516318
- Rajkomar A, Dean J, Kohane I (2019) Machine learning in medicine. N Engl J Med 380:1347–1358. https://doi.org/10.1056/NEJMr a1814259
- Rehman AU, Qureshi SA (2021) A review of the medical hyperspectral imaging systems and unmixing algorithms' in biological tissues. Photodiagn Photodyn Ther 33:102165. https://doi.org/10.1016/j. pdpdt.2020.102165
- Ricard C, Debarbieux F (2014) Six-color intravital two-photon imaging of brain tumors and their dynamic microenvironment. Front Cell Neurosci 8. https://doi.org/10.3389/fncel.2014.00057
- Rino J, Braga J, Henriques R, Carmo-Fonseca M (2009) Frontiers in fluorescence microscopy. Int J Dev Biol 53:1569–1579. https:// doi.org/10.1387/ijdb.072351jr
- Rodríguez-Pulido A, Cortajarena AL, Torra J, Ruiz-González R, Nonell S, Flors C (2016) Assessing the potential of photosensitizing flavoproteins as tags for correlative microscopy. Chem Commun (camb) 52:8405–8408. https://doi.org/10.1039/c6cc0 3119f
- Rossetti BJ, Wilbert SA, Mark Welch JL, Borisy GG, Nagy JG (2020) Semi-blind sparse affine spectral unmixing of autofluorescencecontaminated micrographs. Bioinformatics 36:910–917. https:// doi.org/10.1093/bioinformatics/btz674

- Rousseeuw PJ (1987) Silhouettes: A graphical aid to the interpretation and validation of cluster analysis. J Comput Appl Math 20:53– 65. https://doi.org/10.1016/0377-0427(87)90125-7
- Samarov DV, Clarke ML, Lee JY, Allen DW, Litorja M, Hwang J (2012) Algorithm validation using multicolor phantoms. Biomed Opt Express 3:1300–1311. https://doi.org/10.1364/BOE.3. 001300
- Sawada H, Ono N, Kameoka H, Kitamura D, Saruwatari H (2019) A review of blind source separation methods: two converging routes to ILRMA originating from ICA and NMF. APSIPA Transactions on Signal and Information Processing 8:e12. https:// doi.org/10.1017/ATSIP.2019.5
- Schraivogel D, Kuhn TM, Rauscher B, Rodríguez-Martínez M, Paulsen M, Owsley K, Middlebrook A, Tischer C, Ramasz B, Ordoñez-Rueda D, Dees M, Cuylen-Haering S, Diebold E, Steinmetz LM (2022) High-speed fluorescence image-enabled cell sorting. Science 375:315–320. https://doi.org/10.1126/ science.abj3013
- Schröck E, Manoir SD, Veldman T, Schoell B, Wienberg J, Ferguson-Smith MA, Ning Y, Ledbetter DH, Bar-Am I, Soenksen D, Garini Y, Ried T (1996) Multicolor spectral karyotyping of human chromosomes. Science 273:494–497. https://doi.org/10. 1126/science.273.5274.494
- Scipioni L, Rossetta A, Tedeschi G, Gratton E (2021) Phasor S-FLIM: a new paradigm for fast and robust spectral fluorescence lifetime imaging. Nat Methods 18:542–550. https://doi.org/10.1038/ s41592-021-01108-4
- Şenbabaoğlu Y, Michailidis G, Li JZ (2014) Critical limitations of consensus clustering in class discovery. Sci Rep 4:6207. https:// doi.org/10.1038/srep06207
- Seo J, Sim Y, Kim J, Kim H, Cho I, Yoon Y-G, Chang J-B (2021) PICASSO: Ultra-multiplexed fluorescence imaging of biomolecules through single-round imaging and blind source unmixing. bioRxiv 2021.01.27.428247. https://doi.org/10.1101/2021.01.27. 428247.
- Shaner NC, Lambert GG, Chammas A, Ni Y, Cranfill PJ, Baird MA, Sell BR, Allen JR, Day RN, Israelsson M, Davidson MW, Wang J (2013) A bright monomeric green fluorescent protein derived from *Branchiostoma lanceolatum*. Nat Methods 10:407–409. https://doi.org/10.1038/nmeth.2413
- Shaner NC, Steinbach PA, Tsien RY (2005) A guide to choosing fluorescent proteins. Nat Methods 2:905–909. https://doi.org/10. 1038/nmeth819
- Shi H, Shi Q, Grodner B, Lenz JS, Zipfel WR, Brito IL, De Vlaminck I (2020) Highly multiplexed spatial mapping of microbial communities. Nature 588:676–681. https://doi.org/10.1038/ s41586-020-2983-4
- Shi W, Koo DES, Kitano M, Chiang HJ, Trinh LA, Turcatel G, Steventon B, Arnesano C, Warburton D, Fraser SE, Cutrale F (2020) Pre-processing visualization of hyperspectral fluorescent data with spectrally encoded enhanced representations. Nat Commun 11:726. https://doi.org/10.1038/s41467-020-14486-8
- Silva JCF, Teixeira RM, Silva FF, Brommonschenkel SH, Fontes EPB (2019) Machine learning approaches and their current application in plant molecular biology: a systematic review. Plant Sci 284:37–47. https://doi.org/10.1016/j.plantsci.2019.03.020
- Sinkeldam RW, Greco NJ, Tor Y (2010) Fluorescent analogs of biomolecular building blocks: design, properties, and applications. Chem Rev 110:2579–2619. https://doi.org/10.1021/cr900301e
- Smith JT, Ochoa M, Intes X (2020) UNMIX-ME: spectral and lifetime fluorescence unmixing via deep learning. Biomed Opt Express 11:3857–3874. https://doi.org/10.1364/BOE.391992
- Sommer C, Gerlich D (2013) Machine learning in cell biology teaching computers to recognize phenotypes. J Cell Sci 126. https:// doi.org/10.1242/jcs.123604

- St-Georges-Robillard A, Masse M, Cahuzac M, Strupler M, Patra B, Orimoto AM, Kendall-Dupont J, Péant B, Mes-Masson A-M, Leblond F, Gervais T (2018) Fluorescence hyperspectral imaging for live monitoring of multiple spheroids in microfluidic chips. Analyst 143:3829–3840. https://doi.org/10.1039/C8AN00536B
- Strehl A, Ghosh J (2003) Cluster ensembles -- a knowledge reuse framework for combining multiple partitions. J Mach Learn Res 3:583–617. https://doi.org/10.1162/153244303321897735
- Su W-H, Xue H (2021) Imaging spectroscopy and machine learning for intelligent determination of potato and sweet potato quality. Foods (basel, Switzerland) 10:2146. https://doi.org/10.3390/ foods10092146
- Surre J, Saint-Ruf C, Collin V, Orenga S, Ramjeet M, Matic I (2018) Strong increase in the autofluorescence of cells signals struggle for survival. Sci Rep 8:12088. https://doi.org/10.1038/ s41598-018-30623-2
- Tajbakhsh N, Shin JY, Gurudu SR, Hurst RT, Kendall CB, Gotway MB, Jianming L (2016) Convolutional neural networks for medical image analysis: full training or fine tuning? IEEE Trans Med Imaging 35:1299–1312. https://doi.org/10.1109/tmi.2016.25353 02
- Tamura T, Fujisawa A, Tsuchiya M, Shen Y, Nagao K, Kawano S, Tamura Y, Endo T, Umeda M, Hamachi I (2020) Organelle membrane-specific chemical labeling and dynamic imaging in living cells. Nat Chem Biol 16:1361–1367. https://doi.org/10. 1038/s41589-020-00651-z
- Theis FJ, Neher R, Zeug A (2009) Blind Decomposition of Spectral Imaging Microscopy: A Study on Artificial and Real Test Data. In: Adali, T., Jutten, C., Romano, J. M. T. and Barros, A. K., eds. Independent component analysis and signal separation. Berlin, Heidelberg. Springer Berlin Heidelberg, 548–556
- Thorn K (2017) Genetically encoded fluorescent tags. Mol Biol Cell 28:848–857. https://doi.org/10.1091/mbc.e16-07-0504
- Tikhonova TN, Rovnyagina NR, Zherebker AY, Sluchanko NN, Rubekina AA, Orekhov AS, Nikolaev EN, Fadeev VV, Uversky VN, Shirshin EA (2018) Dissection of the deep-blue autofluorescence changes accompanying amyloid fibrillation. Arch Biochem Biophys 651:13–20. https://doi.org/10.1016/j.abb.2018.05.019
- Tsien RY (1998) The green fluorescent protein. Annu Rev Biochem 67:509–544. https://doi.org/10.1146/annurev.biochem.67.1.509
- Tsurui H, Nishimura H, Hattori S, Hirose S, Okumura K, Shirai T (2000) Seven-color fluorescence imaging of tissue samples based on Fourier spectroscopy and singular value decomposition. J Histochem Cytochem 48:653–662. https://doi.org/10.1177/00221 5540004800509
- Tsutsui H, Karasawa S, Okamura Y, Miyawaki A (2008) Improving membrane voltage measurements using FRET with new fluorescent proteins. Nat Methods 5:683–685. https://doi.org/10.1038/ nmeth.1235
- Valm AM, Cohen S, Legant WR, Melunis J, Hershberg U, Wait E, Cohen AR, Davidson MW, Betzig E, Lippincott-Schwartz J (2017) Applying systems-level spectral imaging and analysis to reveal the organelle interactome. Nature 546:162–167. https:// doi.org/10.1038/nature22369
- Valm AM, Mark Welch JL, Rieken CW, Hasegawa Y, Sogin ML, Oldenbourg R, Dewhirst FE, Borisy GG (2011) Systems-level analysis of microbial community organization through combinatorial labeling and spectral imaging. Proc Natl Acad Sci U S A 108:4152–4157. https://doi.org/10.1073/pnas.1101134108
- Valm AM, Oldenbourg R, Borisy GG (2016) Multiplexed spectral imaging of 120 different fluorescent labels. PLoS ONE 11:e0158495. https://doi.org/10.1371/journal.pone.0158495
- Vida TA, Emr SD (1995) A new vital stain for visualizing vacuolar membrane dynamics and endocytosis in yeast. J Cell Biol 128:779–792. https://doi.org/10.1083/jcb.128.5.779

- Vissa A, Giuliani M, Kim PK, Yip CM (2020) Hyperspectral superresolution imaging with far-red emitting fluorophores using a thin-film tunable filter. Rev Sci Instrum 91:123703. https://doi. org/10.1063/1.5143319
- Vu T, Vallmitjana A, Gu J, La K, Xu Q, Flores J, Zimak J, Shiu J, Hosohama L, Wu J, Douglas C, Waterman ML, Ganesan A, Hedde PN, Gratton E, Zhao W (2022) Spatial transcriptomics using combinatorial fluorescence spectral and lifetime encoding, imaging and analysis. Nat Commun 13:169. https://doi.org/10. 1038/s41467-021-27798-0
- Walsh AJ, Mueller KP, Tweed K, Jones I, Walsh CM, Piscopo NJ, Niemi NM, Pagliarini DJ, Saha K, Skala MC (2021) Classification of T-cell activation via autofluorescence lifetime imaging. Nature Biomedical Engineering 5:77–88. https://doi.org/10. 1038/s41551-020-0592-z
- Wang H, Rivenson Y, Jin Y, Wei Z, Gao R, Günaydın H, Bentolila LA, Kural C, Ozcan A (2019) Deep learning enables cross-modality super-resolution in fluorescence microscopy. Nat Methods 16:103–110. https://doi.org/10.1038/s41592-018-0239-0
- Wang J, Chang C (2006) Applications of independent component analysis in endmember extraction and abundance quantification for hyperspectral imagery. IEEE Trans Geosci Remote Sens 44:2601–2616. https://doi.org/10.1109/TGRS.2006.874135
- Wang M, Zhao M, Chen J, Rahardja S (2019) Nonlinear unmixing of hyperspectral data via deep autoencoder networks. IEEE Geosci Remote Sens Lett 16:1467–1471. https://doi.org/10.1109/LGRS. 2019.2900733
- Wang Y, Yang B, Feng S, Pessino V, Huang B (2019) Multicolor fluorescent imaging by space-constrained computational spectral imaging. Opt Express 27:5393–5402. https://doi.org/10.1364/ oe.27.005393
- Waters JC (2009) Accuracy and precision in quantitative fluorescence microscopy. J Cell Biol 185:1135–1148. https://doi.org/10.1083/ jcb.200903097
- Webb DJ, Brown CM (2013) Epi-fluorescence microscopy. Methods Mol Biol 931:29–59. https://doi.org/10.1007/ 978-1-62703-056-4\_2
- Wei J, Wang X (2020) An overview on linear unmixing of hyperspectral data. Math Probl Eng 2020:3735403. https://doi.org/10.1155/ 2020/3735403
- Willems J, De Jong APH, Scheefhals N, Mertens E, Catsburg LAE, Poorthuis RB, De Winter F, Verhaagen J, Meye FJ, Macgillavry HD (2020) ORANGE: A CRISPR/Cas9-based genome editing toolbox for epitope tagging of endogenous proteins in neurons. PLoS Biol 18:e3000665. https://doi.org/10.1371/journal.pbio. 3000665
- Winter M (1999) N-FINDR: an algorithm for fast autonomous spectral end-member determination in hyperspectral data. Proc. SPIE 3753, Imaging Spectrometry V. https://doi.org/10.1117/ 12.366289
- Wolf DE (2003) Quantitative digital and video microscopy. Methods Cell Biol 72:319–336. https://doi.org/10.1016/s0091-679x(03) 72015-9
- Woolfe F, Gerdes M, Bello M, Tao X, Can A (2011) Autofluorescence removal by non-negative matrix factorization. IEEE Trans Image Process 20:1085–1093. https://doi.org/10.1109/tip.2010.2079810

- Xu Q, Xiao Y, Wang D, Luo B (2020) CSA-MSO3DCNN: multiscale octave 3D CNN with channel and spatial attention for hyperspectral image classification. Remote Sensing 12:188. https://doi.org/ 10.3390/rs12010188
- Yang JM, Chi WY, Liang J, Takayanagi S, Iglesias PA, Huang CH (2021) Deciphering cell signaling networks with massively multiplexed biosensor barcoding. Cell. https://doi.org/10.1016/j.cell. 2021.11.005
- Yang Q, Zou H-Y, Zhang Y, Tang L-J, Shen G-L, Jiang J-H, Yu R-Q (2016) Multiplex protein pattern unmixing using a non-linear variable-weighted support vector machine as optimized by a particle swarm optimization algorithm. Talanta 147:609–614. https://doi.org/10.1016/j.talanta.2015.10.047
- Yang S, Lee B-U (2015) Poisson-Gaussian noise reduction using the hidden Markov model in contourlet domain for fluorescence microscopy images. PLoS ONE 10:e0136964. https://doi.org/ 10.1371/journal.pone.0136964
- Yokota T, Zdunek R, Cichocki A, Yamashita Y (2015) Smooth nonnegative matrix and tensor factorizations for robust multi-way data analysis. Signal Process 113:234–249. https://doi.org/10. 1016/j.sigpro.2015.02.003
- Yoon H, Itoh S, Kawahito S (2009) A CMOS image sensor with inpixel two-stage charge transfer for fluorescence lifetime imaging. IEEE Trans Electron Devices 56:214–221. https://doi.org/ 10.1109/TED.2008.2011678
- Zacharias DA, Violin JD, Newton AC, Tsien RY (2002) Partitioning of lipid-modified monomeric GFPs into membrane microdomains of live cells. Science 296:913–916. https://doi.org/10.1126/scien ce.1068539
- Zhao M, Li Y, Peng L (2014) Parallel excitation-emission multiplexed fluorescence lifetime confocal microscopy for live cell imaging. Opt Express 22:10221–10232. https://doi.org/10.1364/oe.22. 010221
- Zhao T, Hao H, Wang Z, Liang Y, Feng K, He M, Yun X, Bianco PR, Sun Y, Yao B, Lei M (2021) Multi-color structured illumination microscopy for live cell imaging based on the enhanced image recombination transform algorithm. Biomed Opt Express 12:3474–3484. https://doi.org/10.1364/boe.423171
- Zimmermann T (2005) Spectral imaging and linear unmixing in light microscopy. Adv Biochem Eng Biotechnol 95:245–265. https:// doi.org/10.1007/b102216
- Zimmermann T, Rietdorf J, Girod A, Georget V, Pepperkok R (2002) Spectral imaging and linear un-mixing enables improved FRET efficiency with a novel GFP2-YFP FRET pair. FEBS Lett 531:245–249. https://doi.org/10.1016/s0014-5793(02)03508-1
- Zimmermann T, Rietdorf J, Pepperkok R (2003) Spectral imaging and its applications in live cell microscopy. FEBS Lett 546:87–92. https://doi.org/10.1016/s0014-5793(03)00521-0
- Zymnis A, Kim S, Skaf J, Parente M, Boyd S (2007) Hyperspectral image unmixing via alternating projected subgradients. 2007 Conference Record of the Forty-First Asilomar Conference on Signals, Systems and Computers 4–7:1164–1168. https://doi.org/ 10.1109/ACSSC.2007.4487406

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