Integrated MCDM Approaches for Exploring the Ideal Therapeutic Plastic Disposal Technology: Probabilistic Hesitant Fuzzy Domain

Ramasamy Jaisankar · Veeramuthu Murugesan · Samayan Narayanamoorthy · Ali Ahmadian · Krishnan Suvitha · Massimiliano Ferrara · Daekook Kang

Received: 5 September 2022 / Accepted: 15 November 2022 / Published online: 23 January 2023 © The Author(s), under exclusive licence to Springer Nature Switzerland AG 2023

Abstract The probabilistic hesitant fuzzy set (PHFS) is a useful extended version of the hesitant fuzzy set (HFS), which allows decision-makers greater freedom in espousing their preferences through the use of hesitant evidence in the real DM method. As the implications for individuals and global concerns have grown, efficient clinical diagnosis of medical waste has been a major challenge, particularly in developing countries. Medical waste can be disposed of in a variety of ways. The essential thing is to decide

Ramasamy Jaisankar · Veeramuthu Murugesan Department of Statistics, Bharathiar University, Coimbatore, 641 046, India e-mail: r [jaisankar@buc.edu.in](mailto:r_jaisankar@buc.edu.in)

Veeramuthu Murugesan Department of Statistics, Rajah Serfoji Government College (Autonomous), Thanjavur, India e-mail: vmurugesanstat@gmail.com

Samayan Narayanamoorthy · Krishnan Suvitha Department of Mathematics, Bharathiar University, Coimbatore, 641 046, Tamil Nadu, India e-mail: snmphd@buc.edu.in

Krishnan Suvitha e-mail: suvitha0610@gmail.com

Ali Ahmadian

Department of Computer Science and Mathematics, Lebanese American University, Beirut, Lebanon e-mail: ahmadian.hosseini@gmail.com

Ali Ahmadian

Decision Lab, Mediterranea University of Reggio Calabria, Reggio Calabria, Italy

which strategies work best. The optimal healthcare plastic waste disposal (HCPWD) option is a MCDM method involving a wide range of qualitative characteristics. The MCDM technique (ARAS) is then described, whereby the criterion weights are assessed using the recommended entropy weighted method (EWM) proportion and score function in order to increase the process utilisation. Moreover, the abovedescribed approach is used to address a real-world problem by determining the optimal treatment option for healthcare waste (HCW) disposal. Finally, a feasibility analysis is given to support the stated viewpoint on HCPWD options being prioritised.

Keywords Healthcare waste disposal collection method · Hesitant fuzzy set · Probabilistic hesitant fuzzy set · Entropy weight method · ARAS

Ali Ahmadian Department of Mathematics, Near East University, Nicosia, Mersin 10, TRNC Turkey

Massimiliano Ferrara Department of Law, Economics and Human Sciences, Mediterranea University of Reggio Calabria, Reggio Calabria, Italy e-mail: massimiliano.ferrara@unirc.it

Daekook Kang (\boxtimes) Department of Industrial and Management Engineering, Institute of Digital Anti-aging Healthcare, Inje University, 197 Inje-ro Gimhae-si, Gyeongsangnam-do, 50834, Republic of Korea e-mail: dkkang@inje.ac.kr

1 Introduction

Activities related to healthcare are ways to preserve health, treat patients, and save lives. However, they also produce trash, and 20% of that waste poses dangers for injury, infection, or exposure to chemicals or radiation. Although the dangers of handling hazardous medical waste and the methods for doing so are fairly well understood and covered in manuals and other literature, the International Committee of the Red Cross (ICRC) frequently encounters a lack of technical, financial, and legal support for the treatment and elimination methods advocated. Frequently, the personnel is ill-prepared to handle this task. Care professionals, workers who handle medical waste, patients and their relatives, and the local community can all be endangered by poor waste management. By approving its Constitution, any nation that is a United Nations member can join the WHO. When their application has been accepted by the World Health Assembly by a simple majority vote, other nations may be admitted as members. Upon application made on their behalf by the member or another entity responsible for their international relations, territories that are not in charge of the management of their international relations may be accepted as associate members. WHO members are divided into groups based on where they are located. Additionally, improper handling or disposal of such trash may pollute or contaminate the environment. Hazardous medical waste risks can be considerably decreased in unfavorable situations by taking sensible, practical steps. The goal of this document is to serve as a useful and practical tool for the normal management of hazardous hospital wastes. Under no circumstances does it take the place of any current national waste management laws or plans. Medical treatment and the disposal of healthcare waste (HCW) should be viewed as complementary processes. National Health Insurance (NHI) and the World Health Organization (WHO) have been collaborating to evaluate the clinical waste disposal of hospitals and laboratories in order to assess the quality of the hospitals because protecting plants and animals from medical waste is a significant social responsibility. The primary focus of hospital management is HCW. Environmental problems today are causing the spread of many different new diseases. Hospital trash is explicitly defined as human organs, infectious materials, fungi, bacteria, and viruses, as well as equipment used to clean blood

vessels. As a result, these tragedies must be destroyed. The environment and human health will be negatively impacted by a range of diseases brought on by fungi, viruses, and bacteria if it is not properly disposed of. The present healthcare system concentrates on manipulating contemporary disposal techniques. Waste generally has an impact on the environment. Medical waste specifically has an impact on the environment and contains infections that cause disease in other organisms. The flora and animals as well as humans are at risk from these illnesses. In addition to being unhealthy, these medical wastes pose a direct risk of infection for hospital staff members such as doctors and nurses. The choice of medical waste discharge must be made in accordance with the climatic change and infection spread of the modern world. These days, different diseases spread in different ways; thus, this method is vital to stop that from happening. Various bacteria may emerge after hospital discharge and may impact human life. The primary purpose of the management system is to prevent the spread of infection from patient to patient, patient to hospital staff, and patient to others. This HCWT approach should be an excellent strategy to stop infectious diseases brought on by contagious microbes. In recent years, there have been hazards of waste disruption in pharmacies, medical clubs, hospitals, and basic health facilities. WHO is evaluating medical waste solutions through a number of medical organisations to solve these challenges. Therefore, a particularly secure system for disposing of medical waste is required, and not just for hospital financial reasons, but also for the protection of the public, the environment, and other living things. The "bio-medical waste management and handling" regulation was published in 1998 by the Ministry of Environment and Forestry. "Everyone shall guarantee that trash created is managed without any significant effect on human health or the environment," reads this notification of Rule 4. The WHO published some regulations for the disposal of biomedical waste in 2018 and modified them in 2020. The nomenclature used in this manuscript is displayed in Table [1.](#page-2-0)

2 Literature Review

The COVID-19 pandemic epidemic has made managing healthcare waste (HCW) one of the most challenging issues facing the medical community

worldwide (Yu et al. [2020\)](#page-15-0). This may be because these HCWs may have come into contact with a variety of hazardous substances, including used needles and syringes, radioactive materials, dirty dressings, heavy metals, body parts, germs, diagnostic samples, blood, poisonous chemicals, medications, and medical equipment (Thakur & Ramesh, [2017\)](#page-14-0). Due to the disease's high contagiousness, there has been significant contamination of humans and other animals, including birds, mammals, and reptiles, which has caused a global disaster. Effective HCW management is essential to effectively stop the COVID-19 pandemic from spreading. To date, however, no research has focused on the best HCW disposal method selection for managing and controlling such pandemic epidemics. The primary reason for our concentration in this manner is the possibility that if HCWs are incorrectly handled and disposed of, COVID-19 could spread even more quickly and pose a serious risk to the lives of patients, healthcare workers, waste handlers, and members of society at large. Environmental damage is further exacerbated by improper healthcare waste disposal (Baghapour et al. [2018\)](#page-14-1). As a result, it is essential that all HCWs be correctly isolated at the time of generation, appropriately handled, and properly disposed (Badi et al. [2019\)](#page-14-2). Poor HCW treatment practises and unethical waste dumping tactics are frequently used in poor nations like India. Due to the infectious nature of the HCW, these inadequate HCW treatment practises and inappropriate waste disposal methods or procedures pose serious health risks and ecological degradation. With a population of almost

1.3 billion people and recent enormous developments in medical institutions, the problem of HCW management needs to be taken seriously (Minoglou et al. [2017\)](#page-14-3). According to studies from the Indian Society of Hospital Waste Management (ISHWM), a general practitioner's clinic and hospitals are expected to produce at least 600 g of HCW per bed per day and at least 12 kg of HCW per bed per day, respectively. At least 5 to 10% of this is thought to be dangerous or infectious trash. Given the enormous number of patients in the nation, the daily generation of HCW is a sizable number that requires adequate management (Yu et al. [2020\)](#page-15-0). In order to effectively treat and dispose of hazardous and infectious wastes, efficient HCW management systems are required. In India, fewer than 50% of medical facilities use effective waste management techniques and even separate their garbage into contagious and non-infectious waste. Hospitals are solely responsible for ensuring that their HCW treatment and disposal practises will not have any negative effects on human health or the environment. According to a WHO estimate, at least 260,000 HIV infections, 2 million hepatitis C infections, and 21 million hepatitis B infections were all caused by injections with infected needles (Thakur & Ramesh, [2017\)](#page-14-0). Therefore, it is crucial that HCW be properly handled and disposed of. This encourages us to create a tool for evaluating HCW disposal practises both before and after COVID-19 (Thakur & Ramesh A., [2015\)](#page-14-4). Healthcare waste is defined by the World Health Organization (WHO) as waste produced by healthcare events that includes all types of resources, such

as used medical instruments, injections, and toxic isotopes. According to the WHO, non-hazardous waste accounts for around 85% of HCW, and waste disposal accounts for 15%. The remaining 10%, on the other hand, is hazardous since it may contain infectious, highly contagious, and chemical waste (Patil & Shekdar, [2001\)](#page-14-5). If not properly regulated or disposed of, it can constitute a threat to the environment and human health. WHO claims that improper handling of HCW has serious environmental impacts and on the general welfare evaluates healthcare waste disposal solutions using mixed decision support frameworks (Hinduja & Pandey, [2018\)](#page-14-6). In Table [2,](#page-4-0) we give brief studies related to multi-criteria decision-making (MCDM) models for the study of HCWT disposal methods. One method for tackling problems is the MCDM procedure. The decision-situation maker's and the problem scenario's circumstances determine the decisionmaking procedures in all applications. Imagine that when determining the membership values, decisionmakers' judgments are based on ambiguous information. The following fuzzy theories are offered to address this fuzzy situation: The "father of fuzzy set theory" is Zadeh, who popularised the concept in 1965 (Zadeh, [1965\)](#page-15-1). A development of fuzzy set theory is the hesitant fuzzy set. This hesitant fuzzy set theory has produced a wide range of operations and attributes that are used to reveal the reluctant reasoning of decision-makers. The evaluation of HCWD technologies might be regarded as a MCDM problem since HCWD systems provide capabilities for the categorisation of waste produced by healthcare institutions. A rigorous and serious approach is required to properly handle this necessary topic. Several studies have shown the significance of selecting the right waste treatment technologies (Lee et al. [2016\)](#page-14-7). Jiang and Ma [\(2018\)](#page-14-8) used Frank t-norm and t-conorm to provide a number of PHFE procedures, and then subsequently applied those processes to a group decision-making problem with several criteria. Zhang et al. [\(2017\)](#page-15-2) presented two normalised hesitant fuzzy prediction models based on the invertible t-norm and t-conorm and created the PHFS concept, all of which provide case studies on the PHFE Farhadinia [\(2015,](#page-14-9) [2017\)](#page-14-10). The EWM is a well-known intelligence weighting model that has received a lot of attention (Zhi-Hong et al. [2006\)](#page-15-3). The EWM's primary advantage over other subjective weighting approaches is that it prevents human influences from distorting the weight of measures,

which improves the overall neutrality of the assessment process (Ding et al. [2017\)](#page-14-11). As a result, the EWM has been popular recently (Taheriyoun et al. [2010\)](#page-14-12). Fuzzy MCDM approaches, such as fuzzy CODAS, fuzzy VIKOR, fuzzy MULTIMOORA, fuzzy WAS-PAS, fuzzy ARAS, and fuzzy PROMETHEE, assess alternative ratings and weights of criteria based on the imprecision and vagueness conveyed by fuzzy numbers. Decision-makers are required to offer preferences in AHP and ANP instances. The first study on fuzzy AHP, published by Saaty [\(1990\)](#page-14-13), used the fuzzy (AHP) to assess excavation possibilities based on a variety of decision criteria. Numerous researchers updated and implemented these strategies to tackle selection difficulties in diverse professions.

In this research work, we introduce the concept of the PHFS-ARAS method of the MCDM problem to select the best HCWT disposal. This research paper is organised as follows: In Section [3,](#page-5-0) we present the definition of a probabilistic hesitant fuzzy set, its operations, and the score function found in the literature. In Section [4,](#page-6-0) we give proposed methodologies for weight finding and ranking algorithms. In Section [5,](#page-7-0) we select, suitable real-time application of HCW disposal treatment technology and evaluated by the proposed method. We describe the method for collecting the best healthcare plastic waste disposal method, as well as a comparison analysis and a sensitive analysis of the proposed methodology in Sections [6](#page-10-0) and [7.](#page-12-0) In Section [8,](#page-12-1) we conclude the advantages of the proposed method and determine how to select the best BMW disposal treatment.

2.1 Motivation and Objective

In this study article, we aim to select the finest HCWT disposal treatment method. We have chosen the ARAS optimisation methodology from the MCDM model's outranking method to address this issue. Additionally, we are choosing one of the MCDM model's integrated objective weight finding methods. We are prompted to expand our chosen MCDM approaches, entropy and ARAS, in a speculative fuzzy environment by the review section in Table [2](#page-4-0) that is mentioned above. Numerous writers from the literature have worked on the implementation of HCWT management in MCDM. And only a small number of authors have used fuzzy MCDM in this application. A few authors have also used PHF-MCDM to work on this **Table 2** MCDM methods for study of HCWT disposal methods

application. The tentative fuzzy integrated weighting method has not yet been used in PHF-MCDM. We suggest PHF MCDM with a probabilistic hesitant fuzzy integrated weight technique to close this knowledge gap. Decision-makers have the opportunity to pause and experience uncertainty when presented with the values for choosing the best alternative when using the proposed weight-finding process and ranking method. In addition, the HCWT management programme has a number of hesitant and ambiguous phrases, as well as some ambiguous requirements. The membership values are assigned using a probabilistic hesitant fuzzy set that contains probabilistic hesitant fuzzy components (PHFEs). Therefore, it can

be claimed that the primary motivation behind our research is the application of HCWT to PHFEs.

2.2 Contribution

This research paper's primary goal and contribution can be summed up as follows: First and foremost, the primary contribution of this study is the novel approach to multi-criteria decision-making (MCDM) methods that we propose (probabilistic hesitant fuzzy objective weight integrated approach (PHF-Entropy) and probabilistic hesitant fuzzy additive ratio assessment method (PHF-ARAS)). The approach for obtaining weights is the second contribution. The third contribution of our work is that we are implementing the methods we have suggested for the management of HCWT, i.e. we have used the methods we have suggested to determine the optimum HCW disposal treatment procedures and also determined the weights of criteria. Our fourth contribution to our work is the comparison of our outcomes with those of existing methods to demonstrate the effectiveness of our suggested methods. In this section of the comparison, we have contrasted the PHF-ARAS ranking algorithm we have presented with well-liked fuzzy MCDM (PHF-MCDM) approaches, including PHF-CODAS, PHF-WASPAS, and PHF-VIKOR. This research paper's fifth contribution from us is a discussion of our findings in light of various sensitivity analyses and variation problems. Instead of employing integrated weights in our suggested PHFS-Entropy method, we changed the objective weights in this section of the sensitivity analysis. The conclusion of the suggested probabilistic hesitant fuzzy multi-criteria decisionmaking approaches is the next step. We anticipate that the contribution of our suggested approaches will offer the finest BMW disposal treatment approach in this HCWT situation. Consequently, our work is regarded as a useful technique for choosing the appropriate treatment for BMW.

3 Preliminaries

Definition 1 (Torra, [2010\)](#page-14-23); (Xia & Xu, [2011\)](#page-15-7)

Let \Re be the universal set. Defined by the hesitant fuzzy set (HFS) on \Re in finite subset of [0, 1]. It is denoted by

 $G = \{ \langle x, g(x) \rangle / x \in \Re \}$

where $g(x) \in [0, 1]$ as the HFE, which denotes the element's possible membership degree $x \in \Re$ to the set *G*.

In the HFS, *G* can be represented in terms of

$$
G = \left\{ \left\langle x, \bigcup_{g \in g(x)} \{g\} \right\rangle / x \in \Re \right\} \tag{1}
$$

Let $g = \bigcup_{g \in g} \{g\}, g_1 = \bigcup_{g_1 \in g_1} \{g_1\}$ and $g_2 = \bigcup_{g_2 \in g_2} \{g_2\}$ are implied to be three HFEs, then the $g_2 \in g_2$ { g_2 } are implied to be three HFEs, then the following operations on them are identified.

$$
g^{c} = \bigcup_{g \in g} \{1 - g\}
$$

\n
$$
g_{1} \cup g_{2} = \bigcup_{g_{1} \in g_{1}, g_{2} \in g_{2}} \max\{g_{1}, g_{2}\};
$$

\n
$$
g_{1} \cap g_{2} = \bigcup_{g_{1} \in g_{1}, g_{2} \in g_{2}} \min\{g_{1}, g_{2}\}
$$

\n
$$
g^{k} = \bigcup_{g \in g} \{g^{k}\}; \quad \kappa g = \bigcup_{g \in g} \{1 - (1 - g)^{k}\} \quad \kappa > 0
$$

\n
$$
g_{1} \oplus g_{2} = \bigcup_{g_{1} \in g_{1}, g_{2} \in g_{2}} \{g_{1} + g_{2} - g_{1}g_{2}\};
$$

\n
$$
g_{1} \otimes g_{2} = \bigcup_{g_{1} \in g_{1}, g_{2} \in h_{2}} \{g_{1}g_{2}\}
$$

Definition 2 (He & Xu, [2019\)](#page-14-24)

The probabilistic hesitant fuzzy set (PHFS) was embraced, indicating that each possible value of HFE can be affiliated with a probability value that exists . The PHFS on \Re was defined as follows:

$$
{}^{\gamma}G = \{ \langle x, {}^{\gamma}g(x) \rangle : x \in \mathbb{R} \}
$$

=
$$
\left\{ \left\langle x, \bigcup_{\langle g(x), \gamma(x) \rangle \in {}^{\gamma}g(x)} \{ \langle g(x), \gamma(x) \rangle \} \right\rangle / x \in \mathbb{R} \right\}
$$

(2)

A PHFEs, $\gamma g(x)$ constitute both of membership degrees $x \in \Re$ being defined by $g(x)$ in addition to the probability of $\gamma(x) \in [0, 1]$, such that $\sum_{\gamma g(x)} \gamma(x) = 1$ for any $x \in \Re$.

If
$$
{}^{\gamma}g = \bigcup_{\substack{(g_1, \gamma_1) \in {}^{\gamma}g_1}} \bigcup_{\substack{\{g_1, \gamma_1\} \in {}^{\gamma}g_1}} \{ \big(g_1, \gamma_1\big) \} \begin{array}{ccc} & \text{if} & \text{if} & \text{if} \\ & \text{and} & \text{if} & \text{if} \\ & \text{if} & \text{if} & \text{if} \\ & \text{if} & \text{if} & \text{if} \\ & \text{if} & \text{if} & \text{if} \\ \end{array}
$$

Consider the three PHFEs, the presenting some operations,

$$
\gamma g^k = \bigcup_{\langle g, \gamma \rangle \in \gamma_g} \{ \langle g^k, \gamma \rangle \}
$$

$$
\kappa^{\gamma} g = \bigcup_{\langle g, \gamma \rangle \in \gamma_g} \{ \langle 1 - (1 - g)^k, \gamma \rangle \}
$$

$$
\gamma_{g_1 \oplus \gamma_{g_2}} = \bigcup_{\langle g_1, \gamma_1 \rangle \in \gamma_{g_1, \langle g_2, \gamma_2 \rangle \in \gamma_{g_2}} \{ \langle 1 - (1 - g_1)(1 - g_2), \gamma_1 \gamma_2 \rangle \}
$$

$$
\gamma_{g_1 \otimes \gamma_{g_2}} = \bigcup_{(g_1, \gamma_1) \in \gamma_{g_1, (g_2, \gamma_2) \in \gamma_{g_2}}} \{ \langle g_1 g_2, \gamma_1 \gamma_2 \rangle \}
$$

Definition 3 (Jiang & Ma, [2018\)](#page-14-8)

Let $({}^{\gamma}g(x)) = {\gamma_i (g_i) / i = 1, 2, ..., \#g}$ a PHFEs, the score (mean value) function is defined by:

$$
S(Yg(x)) = \sum_{i=1}^{Hg} \gamma_i g_i.
$$

where γ_i is the probability of possible value $\gamma_g(x)$ exhilarating Σ #*g* $i=1$ $\gamma_i = 1$, # g is the number of different PHFEs in $\gamma g(x)$.

4 Methodology

4.1 The Entropy Weight Method

In this procedure, the analysis is set up with m indicators and n samples, and the optimum value of the *i*th indicator in the *j*th instance is noted as x_{ij} . The normalisation of values obtained is the first stage (Gorgij et al. 2017). D_{ij} stands for the standardised value of the *i*th index in the *j* th sample, and it is calculated based on:

$$
\tilde{D}_{ij} = \frac{x_{ij}}{\sum_{j=1}^{n} x_{ij}}\tag{3}
$$

The entropy value F_i is defined as follows (Liu et al. [2010\)](#page-14-26):

$$
F_i = -\frac{\sum_{j=1}^{n} \tilde{D}_{ij} \cdot \ln \tilde{D}_{ij}}{\ln n}
$$
 (4)

 \tilde{D}_{ij} *ln* $\tilde{D}_{ij} = 0$ is often set when $\tilde{D}_{ij} = 0$ in the actual evaluation utilising the EWM for calculating ease. F_i has a range of [0, 1]. As more the differentiation degree of index *i*, the greater the amount of information that may be extracted. As a result, in the EWM, the weight w_i calculating method is (Zhi-Hong et al. [2006\)](#page-15-3).

$$
w_i = \frac{1 - F_i}{\sum_{i=1}^{m} (1 - F_i)}
$$
(5)

4.2 The Proposed MCDM-ARAS Method

As previously stated proposed the ARAS approach (Turskis & Zavadskas, [2010\)](#page-15-6). Forming the decision

matrix and setting, the weights of criteria are the first steps in addressing decision-making issues using the ARAS approach, as they are in the other MCDM methods. Following these first steps, the remaining part of the MCDM issue solution utilising the ARAS approach may be accurately described as follows:

Stage 1. Determine the best possible score for each criterion. The ideal performance ratings are derived as follows if the decision-maker has no priorities:

$$
x_{0j} = \begin{cases} \max_i x_{ij}, & j \in \Delta_{\max} \\ \min_i x_{ij}, & j \in \Delta_{\min} \end{cases}
$$
 (6)

where x_{0j} indicates the *j*th criterion's ideal quality performance, Δ_{max} denotes the beneficial criteria, and Δ_{min} means the non-beneficial criteria.

Stage 2. Calculate the decision matrix that has been normalised. The following formula is used to obtain the normalised performance:

$$
r_{ij} = \begin{cases} \frac{x_{ij}}{\sum_{i=1}^{m} x_{ij}}, & j \in \Delta_{\max},\\ \frac{(1/x_{ij})}{\sum_{i=1}^{m} (1/x_{ij})}, & j \in \Delta_{\min} \end{cases}
$$
(7)

Stage 3. The following equations are used to compute the weighted normalised performance in the organisation:

$$
v_{ij} = w_j * r_{ij},\tag{8}
$$

Stage 4. Evaluate each alternative's total performance rating. To calculate total performance, use the following equation:

$$
S_i = \sum_{j=1}^{n} v_{ij} \quad (i = 0, 1, 2, ..., m)
$$
 (9)

where S_i signifies the overall rating of the *i*th choice.

Stage 5. Comparing the variant under analysis with the ideal best one, *S*0, yields information about the level of alternative utility. The following equation is used to determine an alternative T_i 's utility degree K_i :

$$
Q_i = \frac{S_i}{S_0}, \quad (i = 0, 1, 2, ..., m)
$$
 (10)

where S_i and S_0 are the optimality criterion values, obtained from Eq. (9) , and S_0 is the ideal alternative's total performance.

It is obvious that the calculated values K_i are inside the range [0*,* 1] and that they may be arranged in the required order of priorities in an increasing sequence. The utility function values can be used to calculate the complicated relative efficiency of the feasible alternative.

5 Case Study of HCWT Disposal

The Biomedical Sewage Treatment and Dispatching Regulations have brought healthcare plastic waste management to the forefront in India (1998). One of the most essential aspects is the choice of HCW disposal treatment. In order to describe the current application of waste disposal treatment method selection for HCW, we take into consideration the case study reported in Liu et al. [\(2010\)](#page-14-26). We discuss five potential HCW therapy approaches that have been developed in this study work. The best treatment approach must be chosen in order to solve this issue, and the chosen treatment options must also be ranked. The current situation is being investigated based on a variety of factors, including the type and level of waste generated, how it is handled, treated, and disposed of, and some nutrition aspects. Agencies in a number of regions are failing to put in place acceptable systems owing to a lack of proper technology, economic ability, and solid waste technical programs. With the rising risks connected with this HCW disposal and flaws in the current procedure, determining the optimum methodology for the treatment of this infectious waste has become critical. In this context, utilising the ARAS approach, we suggested an MCDM technique for calculating and choosing HCW disposal options. We used the above-mentioned probabilistic hesitant fuzzy entropy and score value to evaluate the criterion weights and the suggested approach to determine the hierarchy of preferences for the HCW disposal alternatives. As shown in Fig. [1](#page-8-0) , the explanation of HCW disposal treatment techniques and alternatives is as follows:

Plasma pyrolysis (T_1) : It is a simulation technique that uses thermal plasma to convert highcalorie plastic trash into valuable bio gas. In an oxygen-deprived atmosphere, organic compounds are broken down into gases and non-leachable solid wastes using plasma pyrolysis technology.

In order to break down compounds, plasma pyrolysis makes use of a significant amount of electrons, ions, and excited molecules as well as high-energy radiation.

- **Combustion** (T_2) : In the chemical process of combustion, an object quickly combines with oxygen to produce heat. Fuel is the term for the original substance, and oxidiser refers to the source of oxygen. Although it is typically a liquid for aeroplane propulsion, the fuel can be a solid, liquid, or gas. It is a waste-to-non-combustibleresidues-and-gases conversion method that uses high temperatures. Several variables inhibit and reduce waste generation, which also depends on local circumstances. Although this method is extraordinarily successful in removing all sorts of garbage, it creates enormous volumes of harmful gases that are hazardous to public health. Hence, waste should be used or recycled wherever feasible.
- **Microwave sterilisation** (T_3) : It is a method of sterilising garbage using humid heat and steam generated by microwave radiation. It is a radiation and disposal treatment that eliminates particles and other hazardous species like bacteria, and also all substances, infected injections, and antiseptic surgical equipment, including the thermo bio indicator. Most bacteria are destroyed by microwaves with a spectrum of around 2.45 GHz and a diameter of 12.24 NM. This is a very common misinterpretation.
- **Steam disinfection** (T_4) : The gravity displacement autoclave and the high-speed prevacuum steriliser are the two fundamental varieties of steam sterilisers (autoclaves). It is made by exposing the chemicals to saturated high-pressure steam to neutralise them. It improves the ability of warmth to kill germs by reducing temperature and time, both of which serve to dehydrate microbe proteins. This is a very common misinterpretation.
- **Chemical disinfection** (T_5) : It is a chemical procedure that is used to render microorganisms inactive. A chemical using NaOCl as a sanitiser is used in this therapy method. Disinfection is a process that lowers the quantity of microbes to a point where they pose no threat. Disinfection is distinct from sterilisation, which results in the removal of all live microorganisms from the thing. Chemical disinfectants are ideally suited to the treatment of

Fig. 1 Methods for healthcare waste treatment disposal

liquid waste, such as blood, syringes, and other springy objects, urination, hospital sewage, and contaminated glassware, all of which must be treated first. Chemicals, on the other hand, can be used to sterilise solid waste, microorganism cultures, human fluids, and so on.

The following criteria are used to evaluate the above-mentioned options: (S_1) Efficiency of therapy, (*S*2) Land requirement, (*S*3) Acceptance by society, (S_4) Absorption of energy, (S_5) Disposal cost, (S_6) Level of mechanisation. The cost parameters for determining the optimum HCPWD option are (S_5) and (S_6) . A group of four debate specialists from various fields has been formed. Figure [2](#page-8-1) shows the ordered structure for Selecting the best Healthcare Treatment Waste Disposal Collection Methods approach.

5.1 The PHFEs in Entropy Weight Method

Now evaluate the following decision matrix, in which the elements are PHFEs:

$$
D = \begin{bmatrix} S_1 & S_2 & \cdots & S_n \\ T_1 & \gamma_{g_{11}} & \gamma_{g_{12}} & \gamma_{g_{1n}} \\ T_2 & \gamma_{g_{21}} & \gamma_{g_{22}} & \gamma_{g_{2n}} \\ \vdots & \vdots & \vdots & \vdots \\ T_m & \gamma_{g_{m1}} & \gamma_{g_{m2}} & \gamma_{g_{mn}} \end{bmatrix}.
$$

Fig. 2 Selecting the best healthcare treatment waste disposal collection method

Linguistic term Numerical values with PHFEs Exceptional { $(0.8, 0.5), (1.0, 0.5)$ } Very good {0*.*7*,* 0*.*6*,*0*.*8*,* 0*.*4 } Satisfactory {0*.*5*,* 0*.*4*,*0*.*7*,* 0*.*6} Average { $(0.3, 0.7), (0.5, 0.3)$ }
Insufficient { $(0.1, 0.8), (0.3, 0.2)$ } $\{\langle 0.1, 0.8 \rangle, \langle 0.3, 0.2 \rangle\}$

Table 3 Linguistic conversion scale and their corresponding PHFEs

where $\gamma_{g_{ij}}$ ($i=1,\ldots,m, j=1,\ldots,n$) indicates the score of alternative T_i comparable to the criteria S_i with the weight of w_i .

Then how to compare qualitative and quantitative data? Prioritising the factors (criteria) affecting the goal of DM and selecting the best alternative by using the linguistic conversion scale Table [3.](#page-9-0) Which are summarised in the PHF following definition (3) as shown in the Table [4](#page-9-1) decision matrix.

- **Step 1:** Definition (5) is used to calculate the probabilistic hesitant score matrix. Table [5](#page-9-2) shows the results.
- **Step 2:** The normalised matrix is created by using Eq. [3.](#page-6-2) Table [6](#page-10-1) displays the results.
- **Step 3:** Utilising (4), the probabilistic hesitant EWM is determined for all the criteria (Tables [7](#page-10-2) and [8\)](#page-10-3).

Fi = {0*.*089814882*,* 0*.*045571813*,* 0*.*062613882*,* 0*.*546841747*,* 0*.*029643991*,* 0*.*079768656}, where $i = \{1, 2, \ldots, 6\}$.

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Table 5 The PHF score matrix

- 5.2 The PHFE-Based ARAS Methodology
- **Stage 1.** Compute the optimal performance PHF score matrix for each criterion by using Eq. [\(6\)](#page-6-4). The results are shown in Table [9.](#page-11-1)
- **Stage 2** Compute the normalised PHF decision score matrix by using Eq. [\(7\)](#page-6-5). The results are shown in Table [10.](#page-11-2)
- **Stage 3** Compute the weighted normalised PHF decision matrix, using the following Eq. [\(8\)](#page-6-6). The results are shown in Table [11.](#page-11-3)
- **Stage 4** Determined the efficiency performance ranking for each alternative, using the following Eq. [\(9\)](#page-6-1). The results are shown in Table [7.](#page-10-2)

	S_1	S ₂	S_3	S_4	S_5	S_6
T_1	0.181818	0.120879	0.269388	0.063725	0.291304	0.304147465
T_2	0.033058	0.322344	0.089796	0.037255	0.23913	0.262672811
T_3	0.227273	0.117216	0.302041	0.073529	0.165217	0.262672811
T_{4}	0.322314	0.238095	0.232653	0.066667	0.191304	0.069124424
T_5	0.235537	0.201465	0.106122	0.013725	0.113043	0.101382488

Table 6 Normalised PHF score matrix

Stage 5 Compute the degree of utility for each alternative, using the following Eq. [\(10\)](#page-6-7). The results are shown in Table [8.](#page-10-3)

The options are prioritised in sorted order. To determine the proper rankings of alternatives, *ASi* results are selected from highest to lowest. The degree of the alternatives' utility, which is determined by a comparison of the variant, which is analysed with the most optimal value of T_0 . The steam disinfection (T_4) alternative is the greatest in this ranking, while the chemical disinfection (T_5) alternative is the worst as shown in Fig. [4.](#page-12-2)

$$
T_4 > T_3 > T_1 > T_2 > T_5
$$

6 Comparison Analysis

The suggested method's validity is determined by comparing the acquired findings to those obtained using PHFS-based extended CODAS, WASPAS, and VIKOR techniques for the same data set. When compared to other MCDM approaches, the ARAS method produces more realistic results and is more

Table 7 Efficiency performance ranking for each alternatives (*Si*)

Alternatives	S_i
T_0	0.254212045
T_1	0.182937076
T_2	0.133027187
T_3	0.213051806
T_{4}	0.227615128
T ₅	0.092152324

stable. The VIKOR and CODAS procedures are less effective at ranking the alternatives with an optimal solution because in the ARAS approach, results are averaged but criteria sorting is not really taken into account.

The evaluation of four feature-rich MCDM approaches:

- **WASPAS:** Problems involving multiple-criteria decision-making are straightforward and simple to solve.
- **VIKOR:** The decision-makers will be more prepared to accept compromise solutions if you maximise group advantages and reduce individual regret.
- **CODAS:** Making decisions is a useful technique for improving performance in any subject, especially one that calls for processing a lot of data and experience. Making decisions under such circumstances can frequently be challenging. The WAS-PAS method exploits the advantages of the additive ratio assessment (ARAS) method the best. Combining ARAS and WASPAS increases the ranking accuracy

Table 8 Degree of utility for each alternatives (K_i)

Alternatives	K_i
T_0	1
T_1	0.719624
T_2	0.523292
T_3	0.838087
T_4	0.895375
T_5	0.362502

Table 9 Optimal performance PHF score matrix

	S_1	S_2	S_3	S_4	S_5	S_6
T_0	0.78	0.88	0.74	0.75	3.846154	6.666667
T_1	0.44	0.33	0.66	0.65	1.492537	1.515152
T_2	0.68	0.88	0.22	0.38	1.818182	1.754386
T_3	0.55	0.32	0.74	0.75	2.631579	1.754386
T_{4}	0.78	0.65	0.57	0.68	2.272727	6.666667
T_5	0.57	0.55	0.26	0.14	3.846154	4.545455

Table 10 Normalised probabilistic hesitant score matrix

	S_1	S_2	S_3	\mathcal{S}_4	S_5	S_6
T_0	0.205263	0.243767	0.231975	0.223881	0.241785	0.291086
T_1	0.115789	0.091413	0.206897	0.19403	0.093827	0.066156
T ₂	0.178947	0.243767	0.068966	0.113433	0.114298	0.076602
T_3	0.144737	0.088643	0.231975	0.223881	0.165432	0.076602
T_4	0.205263	0.180055	0.178683	0.202985	0.142873	0.291086
T_5	0.15	0.152355	0.081505	0.041791	0.241785	0.198468

Table 11 Weighted normalised probabilistic hesitant score matrix

Fig. 4 The proposed PHF-ARAS method

of the alternatives. In that phase, WAS-PAS calculates an optimal combination parameter. Because the ARAS approach is more sector-inclusive than the other MCDM methods, we use it to choose the best healthcare waste treatment collection method. Table [12](#page-12-3) contains the results, which are visually illustrated in Fig. [5.](#page-12-4)

7 Sensitivity Analysis

Sensitivity analysis is carried out using different cases of the criteria weights. The ARAS method produces more realistic results and is more stable.

- **Case 1:** When it comes to successful criteria, assigning weights to both beneficial and nonbeneficial criteria at equal weights is 0.1667.
- **Case 2:** When it comes to assigning weights for beneficial criteria, 0.25 is the weight, and for non-beneficial criteria, 0 is the weight. The ranking displayed in Table [10](#page-11-2) indicates

 1.5 PERFORMANCE OF ALTERNATIVES $\mathbf{1}$ 0.5 VALUES $\pmb{0}$ 5 6 -0.5 -1 ALTERNATIVES -1.5 ·WASPAS ·CODAS ·VIKOR ·ARAS

Fig. 5 Comparison analysis

that T_4 is truly the greatest option and T_1 has to be the worst alternative in the creative best healthcare plastic waste disposal challenge, based on the sensitivity analysis of several conceivable settings for the fuzzy ARAS approach. When compared to two distinct circumstances, the categorisation of the options shows a high level of consistency, despite modest changes in the findings. An investigation into the validity of the proposed approaches with regard to the two cases in Table [13](#page-13-0) was conducted. Figure [6](#page-13-1) shows how the weighting of the criterion was changed to generate two unique situations.

8 Discussion and Conclusion

In this research, we have chosen an HCW disposal treatment system that will make it possible to use the five HCW disposal strategies the hospital has chosen. Based on these, we applied the MCDM approach to choose a unique HCW disposal treatment strategy for their current application. In order to deal with

	WASPAS	Rank	VIKOR	Rank	CODAS	Rank	ARAS	Rank
T_1	0.66686		O		-0.13117	4	0.7196	\mathbf{a}
T_2	0.51101	4	0.401809		-0.30767		0.5232	4
T_3	0.78452	◠	0.079449	2	0.109653		0.8380	
T_{4}	0.86688		0.580732	4	0.365326		0.8953	
T_{5}	0.35683		0.888539		-0.03178		0.3625	

Table 12 Comparison of ranking results

the complicated environment where MCDM is producing reluctant and hazy perspectives of decisionmakers, we employ the hesitant fuzzy MCDM method. The reluctant opinions of decision-makers are also appreciated. The primary procedure in hospital management is trash disposal. Different kinds of new diseases are now becoming more prevalent as a result of environmental issues. Human organs, illnesses (fungi, bacterial, and viral), and equipment used to clean blood vessels are all expressly mentioned in the context of hospital waste disposal. As a result, it is essential to get rid of these medical wastes. The autoclaving disposal method that was chosen at the conclusion of this study has been looked into with regard to environmental and human health aspects. Because of this, we think autoclaving can be the best technique of disposal treatment to prevent HCW infection. In this way, it is advised to select an appropriate and secure disposal treatment system in all medical facilities, hospitals, etc. In order to address both visible and invisible criteria and select the most appropriate disposal treatment options for the bio-medical wastes of the healthcare institution, an extension of the combined objective weight (entropy) approach and ARAS is proposed in this research study. In MCDM, numerous multi-objective optimisation techniques are employed. Here, we select the ARAS approach, which is regarded as one of the top optimisation techniques. The entropy and ARAS approaches must be developed in the probabilistic hesitant fuzzy environment of this research. Additionally, these suggested methods are less sensitive because the criteria values are highly stable. By using HCW disposal treatment, the proposed tentative approach's applicability is assessed. Based on the ranking order of alternatives, steam disinfection disposal treatment is the best disposal treatment. This ranking is based on absorption of energy, efficiency of therapy, level of mechanisation, acceptance by society, land requirements, and disposal cost risk criteria. Steam disinfection and disposal treatment reduce the risk of environmental pollution and secure human health from the effects of infections. Furthermore, patients and their attendants would be adequately informed about the advantages of using the correct HCPWD. Finally, technical advancements, government regulations, and their implementation may all be used to improve HCPWD. Moreover, we will build on the study by combining empirical and subjective data on the weight of the criterion.

Fig. 6 Sensitivity analysis

Funding This work was supported by a National Research Foundation (NRF) of Korea grant funded by the Korean Government (MSIT) Grant NRF-2022R1C1C1006671.

Data Availability All data generated or analysed during this study are included in this published article.

Compliance with Ethical Standards

Conflict of Interest The authors declare no competing interests.

Ethical Approval This article does not contain any studies with human participants or animals performed by any of the authors.

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