## Heterogeneous mechanisms for synchronization of networks

## of resonant neurons under different  $E/I$  balance regimes

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## **Supplemental Material**

In this Supplemental Material we present results showing how synaptic inhibitory strength qualitatively modulates the results shown in the main text. We track the trajectories of  $E/I$  ratio and the difference between  $E$  and I currents (total current) as excitatory synaptic strength  $w_E$  is varied for three different values of inhibitory synaptic strength  $w_I$  (Fig. S1a). We compare the shape of the trajectory loops for three different values of  $w<sub>I</sub>$  when the network is driven with external oscillatory current input in the resonant frequency range  $(5Hz)$  to when it is not driven  $(0Hz)$ . We observe that increased inhibitory synaptic strength limits the maximum  $E/I$  ratio and thus the domain of the trajectory loop, which is further diminished if the resonant drive is present.

The trajectory loops for all three  $w<sub>I</sub>$  values illustrate the two synchronization regimes discussed in the manuscript. In the resonance regime for lower  $w_E$  values, resonant oscillatory drive constrains the trajectory around E=I balance points with smaller trajectory loop sizes (dashed lines) than when no drive is given (solid lines). In the network-driven PING-like synchronization regime for higher  $w_E$  values, external oscillatory drive does not have pronounced effects.

At the same time, the trajectories with various  $w_1$  values show marked differences. First, the size of the trajectory loop in the resonance regime decreases with stronger inhibition. For  $w_1=3mS/cm^2$ , the stronger inhibition affects the activity of inhibitory cells diminishing overall inhibitory signaling, so that the network does not exhibit single spike bursting activity even at the strongest  $w_E$  range. In addition, the network does not enter the inhibition-dominant regime for highest  $w_E$  values (total current < 0 and  $E/I$  ratio <1) even though  $w<sub>I</sub>$  is high. This indicates that the excitatory and inhibitory signals interact in a recurrent, non-linear way.

Figures S2 and S3 depict sample raster plots for higher inhibitory synaptic strength values,  $w_1=1 \text{mS/cm}^2$  and  $w_1=3 \text{mS/cm}^2$ , respectively. In both cases, similarly as for  $w_1=0.3 \text{mS/cm}^2$  in the main text, when  $w_E$  is weak, the resonant oscillatory drive mediates ordered spiking within synchronous bursts (middle row, left side). For slightly higher  $w_E$ , resonant oscillatory drive increases the spiking synchrony through phase locking. The colored markers (stars and dots) denote parametric locations from Fig. S1.

However, in the PING-regime, the behavior of the networks for different inhibition  $w<sub>I</sub>$  values diverges. For  $w<sub>I</sub>=1mS/cm<sup>2</sup>$  (Fig. S2, right side), with the increase of  $w_E$ , the network firing pattern changes from wide (multi-spike) bursts to narrow, often single spike bursts. When  $w_E$  has medium values ( $w_E$ =1.5mS/cm<sup>2</sup>, right side, first column), cells fire randomly at a high rate during network bursts rather than synchronously, due to the weakened inhibitory signal. For higher  $w_E$  ( $w_E=3mS/cm^2$ , right side,  $2<sup>nd</sup>$  column), inhibitory cells get higher excitatory signaling and generate stronger inhibition, which causes shorter network bursts. For higher inhibitory synaptic strength  $(w_1=3mS/cm^2)$ , Fig. S3, right side), however, due, to strong inhibitory-to-inhibitory connections, inhibitory signaling is not strong enough to generate single spike bursts, and network bursts are long-lasting. For both levels of inhibitory synaptic strength  $(w_1=1 \text{mS/cm}^2$  and  $w_1=3 \text{mS/cm}^2$ , Figs. S2 and S3, right sides), resonant (5Hz) external oscillatory drive phase-locks the onset of network bursts. 



Figure S1. Trajectories of E/I ratio and E – I total current as excitatory synaptic strength  $w_E$  is increased for networks with different inhibitory synaptic strength  $w<sub>I</sub>$  values. In panel (a), trajectories are shown for  $w_1=0.3$ mS/cm<sup>2</sup> (blue, same curve as Fig.1),  $w_1=1$ mS/cm<sup>2</sup> (red) and  $w_1$ =3mS/cm<sup>2</sup> (black) with no external oscillatory drive (solid lines) and with 5Hz drive (dashed lines). The details around E=I balance are displayed in the inset. The magnified curves for  $w_1$ =1mS/cm<sup>2</sup> and  $w_1$ =3mS/cm<sup>2</sup> are shown in panel (b) and (c), respectively; markers label the data points for which raster plots are displayed in Figs. S2, S3.



Figure S2. Example raster plots for networks with  $w_1=1 \text{mS/cm}^2$  at parameter points marked on the trajectory in Fig S1b. Top row: no external oscillatory drive; middle row: resonant (5Hz) drive; Bottom row: 40Hz (non-resonant) drive (not shown in Fig. S1b).



Figure S3. Example raster plots for networks with  $w_1=3 \text{mS/cm}^2$  at parameter points marked on the trajectory in Fig S1c. Top row: no external oscillatory drive; middle row: resonant (5Hz) drive; Bottom row: 40Hz (non-resonant) drive (not shown in Fig. S1b).