
Supplementary information

**CFTR function, pathology and
pharmacology at single-molecule resolution**

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CFTR function, pathology and pharmacology at single-molecule resolution

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8 Supplementary Methods

9 Calculations of the steady state population fractions

10 Here, we demonstrate the kinetic scheme formulation at physiologically relevant saturating ATP
11 concentrations (> 1 mM) denoted with $[ATP]$ starting with the state occupation probabilities when the
12 system is at steady state. The population fractions of the states are labeled with S_l for $l = 1, 2, \dots, 8$.
13 Temporal evolution of these population fractions is governed by the following set of equations where the
14 transition rates from state l to l' are shown with $k_{l \rightarrow l'}$, for all $l \neq l' = 1, 2, \dots, 8$

$$15 \quad \frac{dS_1}{dt} = - (k_{1 \rightarrow 2} [ATP] + k_{1 \rightarrow 8}) S_1 + k_{2 \rightarrow 1} S_2 + k_{8 \rightarrow 1} S_8,$$

$$16 \quad \frac{dS_2}{dt} = - (k_{2 \rightarrow 1} + k_{2 \rightarrow 3}) S_2 + k_{3 \rightarrow 2} S_3 + k_{1 \rightarrow 2} [ATP] S_1,$$

$$17 \quad \frac{dS_3}{dt} = - (k_{3 \rightarrow 8} + k_{3 \rightarrow 2} + k_{3 \rightarrow 4}) S_3 + k_{2 \rightarrow 3} S_2 + k_{4 \rightarrow 3} S_4 + k_{8 \rightarrow 3} [ATP] S_8,$$

$$18 \quad \frac{dS_4}{dt} = - (k_{4 \rightarrow 3} + k_{4 \rightarrow 5}) S_4 + k_{3 \rightarrow 4} S_3 + k_{5 \rightarrow 4} S_5,$$

$$19 \quad \frac{dS_5}{dt} = - (k_{5 \rightarrow 4} + k_{5 \rightarrow 6}) S_5 + k_{4 \rightarrow 5} S_4 + k_{6 \rightarrow 5} S_6,$$

$$20 \quad \frac{dS_6}{dt} = - (k_{6 \rightarrow 5} + k_{6 \rightarrow 7}) S_6 + k_{7 \rightarrow 6} S_7 + k_{5 \rightarrow 6} S_5,$$

$$21 \quad \frac{dS_7}{dt} = - (k_{7 \rightarrow 6} + k_{7 \rightarrow 8}) S_7 + k_{6 \rightarrow 7} S_6 + k_{8 \rightarrow 7} S_8,$$

$$22 \quad \frac{dS_8}{dt} = - (k_{8 \rightarrow 3} [ATP] + k_{8 \rightarrow 7} + k_{8 \rightarrow 1}) S_8 + k_{1 \rightarrow 8} S_1 + k_{8 \rightarrow 1} S_8,$$

$$23 \quad \sum_{k=1}^8 S_k = 1.$$

24 Here, the last equation imposes conservation of mass on the population fractions. We find the steady state
 25 solution for the state population fractions. steady state population fractions is used to initialize our data
 26 simulation. Below we provide the details of the data simulation.

27 **Simulation of simultaneous electrophysiology and smFRET data**

28 In our simulation setup, we imagine visualizing the single molecule conformations with smFRET and
 29 electrophysiology, simultaneously. As the single molecule transitions amongst its conformational states
 30 labeled with S_l for $l = 1, 2, \dots, 8$ where some of these states give rise the same signal in smFRET or
 31 electrophysiology measurements as summarized below in **Supplementary Table 1** with kinetic rates
 32 provided in **Supplementary Table 2**.

33 **Supplementary Table 1.** Conformational states and their associated signals in smFRET and electrophysiology
 34 measurements.

occupied conformational state	smFRET signal	electrophysiology signal
S_1	low FRET	no current
S_2	low FRET	no current
S_3	high FRET	no current
S_4	high FRET	no current
S_5	high FRET	current
S_6	high FRET	current
S_7	high FRET	no current
S_8	high FRET	no current

35
 36 Here, we simulate the trajectory reporting on the conformational dynamics of the single molecule in
 37 continuous time as a Gillespie⁶⁰ trajectory where these conformational dynamics are governed by the
 38 following generator matrix labeled with \bar{G}

	S_1	S_2	S_3	S_4	S_5	S_6	S_7	S_8
S_1	*	$k_{1 \rightarrow 2}[ATP]$	0	0	0	0	0	$k_{1 \rightarrow 8}$
S_2	$k_{2 \rightarrow 1}$	*	$k_{2 \rightarrow 3}$	0	0	0	0	0
S_3	0	$k_{3 \rightarrow 2}$	*	$k_{3 \rightarrow 4}$	0	0	0	$k_{3 \rightarrow 8}$
S_4	0	0	$k_{4 \rightarrow 3}$	*	$k_{4 \rightarrow 5}$	0	0	0
S_5	0	0	0	$k_{5 \rightarrow 4}$	*	$k_{5 \rightarrow 6}$	0	0
S_6	0	0	0	0	$k_{6 \rightarrow 5}$	*	$k_{6 \rightarrow 7}$	0
S_7	0	0	0	0	0	$k_{7 \rightarrow 6}$	*	$k_{7 \rightarrow 8}$
S_8	$k_{8 \rightarrow 1}$	0	$k_{8 \rightarrow 3}[ATP]$	0	0	0	$k_{8 \rightarrow 7}$	*

39 where the * notation shows the negative of the sum of each row.

41 Subsequently, this trajectory of the single molecule gives rise to smFRET and electrophysiology
42 measurements. For example, if the molecule has dimerized NBDs and an open pore then this conformation
43 of the molecule leads to high FRET and high current measurements in smFRET and electrophysiology,
44 respectively.

45 In a prototypical smFRET experiment, FRET efficiency (FRET) is computed based on the photons emitted
46 from donor (n_D) and acceptor dyes (n_A) that are attached to the single molecule where $FRET = \frac{n_A}{n_A + n_D}$.

47 In our simulations, we adjusted the photon emission rates of donor and acceptor dyes according to known
48 total experimentally observed photon counts such that the low and high FRET signals are equivalent to
49 $\sim 20\%$ and $\sim 55\%$ FRET, respectively. For the electrophysiology measurements, based on the occupied
50 states of the single molecule's trajectory, we generate measurements. Specifically, low (closed channel
51 conformation) and high (open channel conformation) current levels are adjusted according to the
52 experimentally observed conformational state levels in electrophysiology experiments where low and high
53 current levels are ~ 0 pA and ~ 2 pA. Both smFRET and electrophysiology measurements are acquired with
54 a camera-based detector⁶¹ thereby the measurements are subject to temporal averaging provided that the
55 conformational dynamics of the molecule are faster than the data acquisition rate labeled with $\frac{1}{\Delta t}$ where Δt
56 denotes the data acquisition period. We use Δt^F and Δt^E for smFRET and electrophysiology experiments,
57 respectively. Here, we denote the trajectory of the molecule with $\tau(t)$, for all $t \geq 0$, where photon emission

58 rates for donor and acceptor dyes that lead to low and high FRET levels are denoted with $\bar{\mu}_D = (\mu_1^D, \mu_2^D)$ and
 59 $\bar{\mu}_A = (\mu_1^A, \mu_2^A)$. We also note that for a given time t , $\tau(t) = S_l$ for some $l = 1, 2, \dots, 8$. Low and high
 60 current state levels for the electrophysiology measurements are denoted with $\bar{C} = (C_1, C_2)$. We assumed
 61 shot noise for the smFRET measurements and normally distributed measurement noise for the
 62 electrophysiology experiments.

63 Now, we summarize how simulated measurements in smFRET and electrophysiology experiments are
 64 generated.

65 Based on Gillespie simulation, we generate $\tau(\cdot) \sim \text{Gillespie}(\bar{G}, \tau(0))$, where ' \sim ' stands for sampling of $\tau(\cdot)$
 66 as a Gillespie trajectory with a given starting point denoted with $\tau(0)$ at time $t = 0$ that is determined based
 67 on the steady state probability of state occupation explained above. Subsequently, given the photon
 68 emission rates $\bar{\mu}_D$ and $\bar{\mu}_A$ of donor and acceptor dyes we can now formulate the collected photons associated
 69 with donor and acceptor dyes. The measurements are labeled with $\bar{w}_D = (w_1^D, w_2^D, \dots, w_N^D)$ and $\bar{w}_A =$
 70 $(w_1^A, w_2^A, \dots, w_N^A)$ on the donor and acceptor dyes associated detectors in smFRET experimental setup
 71 where w_n^D, w_n^A denote the n -th measurement for all $n = 1, 2, \dots, N$ with N labeling the last smFRET
 72 measurement. Then, we now formulate the n -th measurement during the data acquisition period Δt^F within
 73 the time window of $[t_{n-1}, t_{n-1} + \Delta t^F]$ such that $w_n^D \sim \text{Poisson}(\int_{t_{n-1}}^{t_{n-1} + \Delta t^F} dt \mu_{\tau(t)}^D)$ and
 74 $w_n^A \sim \text{Poisson}(\int_{t_{n-1}}^{t_{n-1} + \Delta t^F} dt \mu_{\tau(t)}^A)$ for all $n = 1, \dots, N$. Here, "Poisson" denotes the distribution to
 75 formulate the shot noise statistics in the measurements. Next, we move to the electrophysiology
 76 measurements labeled with $\bar{y} = (y_1, y_2, \dots, y_M)$ where M labels the last measurement in
 77 electrophysiology experiments. In the case of acquiring electrophysiological data, we assume that the
 78 measurement noise is governed by "Normal" distribution and thereby the m -th measurement labeled with
 79 y_m collected with data acquisition rate $\frac{1}{\Delta t^E}$ within the time window $[t_{m-1}, t_{m-1} + \Delta t^E]$ shown as

80 $y_m \sim \text{Normal}(\frac{1}{\Delta t^E} \int_{t_{m-1}}^{t_{m-1} + \Delta t^E} dt C_{\tau}(t), \sigma^2)$ for all $m = 1, 2, \dots, M$ where σ^2 (pA^2) denotes the measurement
81 noise.

82 In our current study, the only noise sources are the shot noise due to photon emissions for smFRET and
83 normally distributed measurement noise for electrophysiology. We have not considered the read-out or any
84 jittering noises dictated by the type of detector used in the experiments. Those additional improvements
85 related to the measurement models in our simulations that are left for future studies.

86 **Supplementary Table 2.** Kinetic rate parameters used in simulations. *For simulation of E1371Q gating

87 $k_{5 \rightarrow 6}$ was set to zero.

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rates	units	values
$k_{1 \rightarrow 2}$	$\mu\text{M}^{-1}\text{s}^{-1}$	1
$k_{2 \rightarrow 1}$	s^{-1}	50
$k_{2 \rightarrow 3}$	s^{-1}	10
$k_{3 \rightarrow 2}$	s^{-1}	0.3
$k_{1 \rightarrow 8}$	s^{-1}	0.3
$k_{8 \rightarrow 1}$	s^{-1}	0.3
$k_{3 \rightarrow 8}$	s^{-1}	0.6
$k_{8 \rightarrow 3}$	$\mu\text{M}^{-1}\text{s}^{-1}$	0.012
$k_{3 \rightarrow 4}$	s^{-1}	1.3
$k_{4 \rightarrow 3}$	s^{-1}	0.002
$k_{5 \rightarrow 4}$	s^{-1}	20
$k_{4 \rightarrow 5}$	s^{-1}	100
$k_{5 \rightarrow 6}$	s^{-1}	2*
$k_{6 \rightarrow 5}$	s^{-1}	0
$k_{6 \rightarrow 7}$	s^{-1}	4
$k_{7 \rightarrow 6}$	s^{-1}	0
$k_{7 \rightarrow 8}$	s^{-1}	4.5
$k_{8 \rightarrow 7}$	s^{-1}	0

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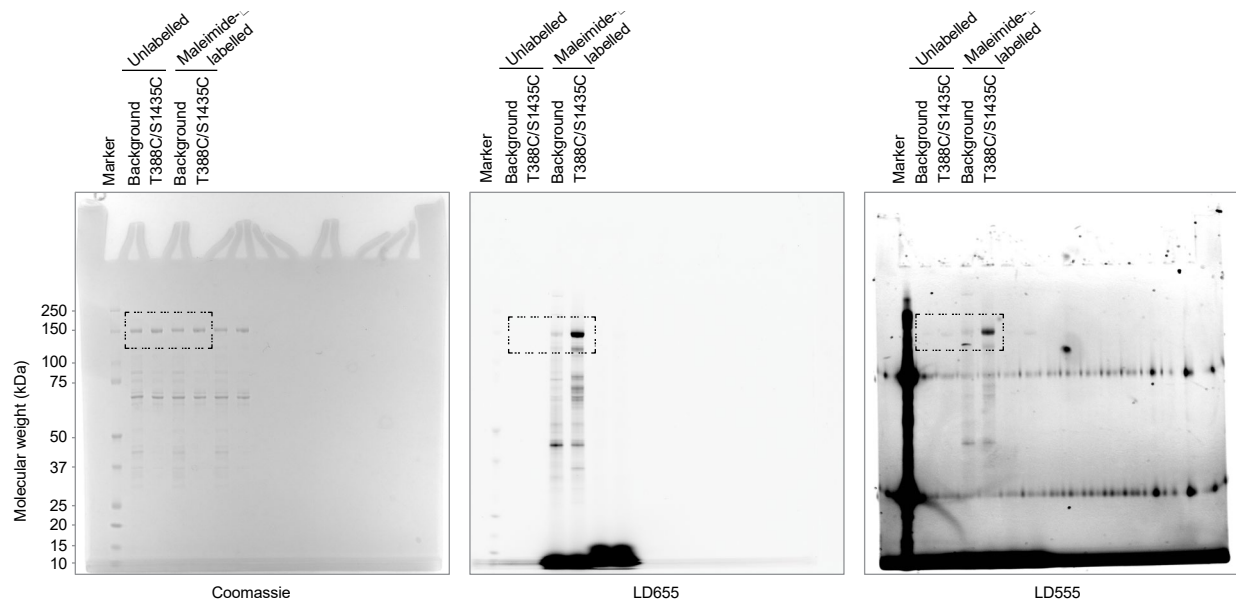
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Supplementary Figure 1 | Gel source data

Uncropped gel scans of the gel imaged in Extended Data Figure 2a. The gel was first imaged for LD555 and LD655 fluorescence, and then Coomassie-stained. The dashed boxes indicate the regions of the scans that are presented in Extended Data Figure 2a.