## **S6. IMPLEMENTING ENERGIES IN THE CIRCUIT**

In this part, we show parts of a circuit where some pair-wise energies are implemented using quantum gates (Fig. S7). Here, we have two interacting residues (Fig. S7-A), with the energy table described in Fig. S7-B. Since we have two designable sites, we require n = 6 qubits, where each residue uses 3 qubits as shown in Fig. S7-C. In the circuit shown in Fig. S7-C, parts of the energy table are implemented through *multi–control–not gates*, specifically *6-control-1-NOT* gates.



**FIG. S7**. A) representation of two interacting residues. B) energy table used in our study. C) Circuit representation of the initialization step and implementation of some of the pair-wise energies in the circuit, with g=3, n=6 and m=7.