Supplementary Methods

MR methods

We estimated the causal effect of GERD on IPF risk and of IPF on GERD risk by first deriving SNP-specific MR estimates using the Wald estimator, obtained by dividing the gene-outcome (G-Y) by the gene-exposure (G-X) association estimate (both expressed as logOR), with standard error obtained using the Delta method. [1] The estimate of the causal effect was then obtained by pooling the SNP-specific MR estimates using an Inverse-Variance Weighted Fixed-Effect meta-analysis (IVW-FE). [1] Although the linearity assumption underlying our MR analysis is violated when using binary variables [2], as in our case, the magnitude of the resulting bias has been shown to be negligible. [3]

Investigation of pleiotropy

The IVW-FE method used for our MR analyses is the most powerful but assumes absence of pleiotropy [4], i.e. variants chosen as instruments for the exposure cannot affect the outcome through any other independent pathways. As pleiotropy can bias MR findings [5], we investigated its possible presence through assessment of: the heterogeneity in the MR estimates across SNPs, using the I² index and the Q heterogeneity test [6].

In the presence of pleiotropy, possible pleiotropic SNPs were identified graphically based on their contribution to the overall heterogeneity (Cochran's Q statistic) as previously described [7], and we repeated the IVW-FE analysis after removing the pleiotropic SNPs. We also repeated the MR analyses on all SNPs using methods that can account for pleiotropy under different assumptions about its nature. [8] In particular, we considered the following methods:

- Inverse Variance Weighted Random-Effect (IVW-RE)[9]: This was performed in the same way as IVW-FE, but a (multiplicative) random-effects, instead of a fixed-effect, meta-analysis model was used to allow for pleiotropy. IVW-RE assumes that pleiotropic effects across SNPs are random (balanced pleiotropy), and that their magnitude is independent of the magnitude of the corresponding G-X effects (InSIDE assumption). [4]
- Weighted Median estimator (WMe) [10]: This method assumes that more than 50% of the information contributing to the MR analysis comes from genetic variants that are valid (i.e. they are not pleiotropic). [10]
- Weighted Mode estimator (WMo) [11]: This method assumes that the largest weighted contribution of "similar" (i.e. identical in infinite samples) SNP-specific MR estimates comes from valid instruments. [12]
- MR-Egger regression (MRE) [13]: In this method, G-Y estimates for the individual SNPs are regressed on their G-X estimates; the intercept of this regression model represents the overall pleiotropy, and the slope the MR estimate adjusted for pleiotropy .[14] MRE assumes an overall directional pleiotropy, and it makes the InSIDE assumption. MRE works well only in the presence of a large spread of strengths, which can be quantified by the heterogeneity in G-X estimates across

SNPs, I_{GX}^2 , with a recommended $I_{GX}^2 > 90\%$. [13] As the I_{GX}^2 was lower than 90% for both our MR analyses, we attempted to address this limitation using the SIMulation EXtrapolation (SIMEX) method that corrects for the dilution bias. [13]

The MR analyses were performed using the R packages "MendelianRandomization" (https://cran.r-project.org/web/packages/MendelianRandomization/index.html) and MR-PRESSO (https://github.com/rondolab/MR-PRESSO). The code for all the MR analyses is provided below.

```
R code
# Bi-directional Mendelian randomization analyses
# GERD and IPF
rm(list=ls())
#install.packages("MendelianRandomization")
#install.packages("simex")
#install.packages("MRPRESSO")
library(MendelianRandomization)
library(simex)
library(MRPRESSO)
A <- read.table("data.txt", sep="\t", header=T)
head(A)
dim(A)
# MR-PRESSO
mr presso(BetaOutcome = "b y", BetaExposure = "b x", SdOutcome = "se y", SdExposure
= "se_x", OUTLIERtest = TRUE, DISTORTIONtest = TRUE, data = A, NbDistribution =
1000, SignifThreshold = 0.05)
# IVW fixed effects
mr_ivw(mr_iput(bx = A\$b_x, bxse = A\$se_x, by = A\$b_y, byse = A\$se_y), model="fixed")
#IVW multiplicative random effects
mr ivw(mr input(bx = A$b x, bxse = A$se x, by = A$b y, byse = A$se y),
model="random")
# MR-Egger
```

```
mr_egger(mr_input(bx = A$b_x, bxse = A$se_x, by = A$b_y, byse = A$se_y))
# MR-Egger with simex adjustment
# dilution bias evaluation
Isq <- function(y,s){</pre>
k <- length(y)
w <- 1/s^2; sum.w <- sum(w)
mu.hat <- sum(y*w)/sum.w
Q \leftarrow sum(w*(y-mu.hat)^2)
Isq <- (Q - (k-1))/Q
lsq <- max(0, lsq)
return(Isq)
}
12_gx \leftarrow Isq(A$b_x, A$se_x)
I2_gx
bxq <- A$b x
seX <- A$se x
byg <- A$b y
seY <- A$se_y
BetaYG <- byg*sign(bxg)
BetaXG <- abs(bxg)
Fit2 <- Im(BetaYG~BetaXG,weights=1/seY^2,x=TRUE,y=TRUE)
mod.sim <- simex(Fit2,B=1000, measurement.error = seX,
SIMEXvariable="BetaXG",fitting.method ="quad",asymptotic="FALSE")
summary(mod.sim)
# Weighted MR median
mr_median(mr_i)t(bx = A$b_x, bxse = A$se_x, by = A$b_y, byse = A$se_y),
    weighting = "weighted", iterations = 10000)
# Mode-based MR
mr_mbe(mr_i)t(bx = A$b_x, bxse = A$se_x, by = A$b_y, byse = A$se_y), phi=1,
iterations=100)
QA1
```

```
BIV \leftarrow A b_y/A b_x
se_IV < -sqrt(A$se_y^2/A$b_x^2)
w < - 1/(se_IV^2)
y <- BIV
sum.w <- sum(w)
mu.hat <- sum(y*w)/sum.w
Q ivw <- w*(y-mu.hat)^2
su <- summary(Q_ivw)
plot(Q_ivw, pch = 19, ylab="", xlab = "", ylim=c(0,su[6]+1), xaxt = 'n', main="IPF-GERD")
title(ylab="Cochran Q contribution", line = 1.9)
title(xlab = "Instruments", line = 0.5)
L1 < -qchisq(1-0.05, df = 1)
L2 < -qchisq(1-(0.05/19), df = 1)
#add dotted line at 0.05
abline(L1,0,lty = 3, col = "red")
#add dotted line at 0.05/19
abline(L2,0, lty = 2, col = "red")
#Add rs names of instruments
text(4, Q ivw[4], labels=A[4,1], cex= 0.6, pos=1)
text(7, Q_ivw[7], labels=A[7,1], cex= 0.6, pos=3)
text(8, Q_ivw[8], labels=A[8,1], cex= 0.6, pos=1)
text(13, Q_ivw[13], labels=A[13,1], cex= 0.6, pos=1)
text(16, Q_ivw[16], labels=A[16,1], cex= 0.6, pos=1)
```

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