

Supplementary Material

Table S1. Adsorption energy for the d-CH₄, u-CH₄, t-CH₄ and u-CH₄-IP, obtained at the PBE-TS level ($E_{ads,TS}$), PBE-MBD level ($E_{ads,MBD}$) and their energetic difference (ΔE_{ads}). Equilibrium distance between methane and the Z1 adsorption site, obtained at the PBE-TS level ($D_{e,TS}$), PBE-MBD level ($D_{e,MBD}$) and their difference (ΔD_e).

| | $E_{ads,TS}$ (eV) | $E_{ads,MBD}$ (eV) | ΔE_{ads} | $D_{e,TS}$ | $D_{e,MBD}$ | ΔD_e |
|-----------------------|-------------------|--------------------|------------------|------------|-------------|--------------|
| d-CH ₄ | -0.089 | -0.070 | 0.019 | 2.750 | 2.960 | 0.210 |
| u-CH ₄ | -0.120 | -0.089 | 0.032 | 3.510 | 3.790 | 0.280 |
| t-CH ₄ | -0.113 | -0.072 | 0.041 | 3.610 | 3.950 | 0.340 |
| u-CH ₄ -IP | -0.073 | -0.070 | 0.003 | 2.810 | 2.800 | -0.010 |

Table S2. Adsorption energies in eV for different orientations of CH₄ on Z1, Z2, Z3 and Z4 sites on the 12-ZGNR.

| | Z1 | Z2 | Z3 | Z4 |
|-------------------|--------|--------|--------|--------|
| u-CH ₄ | -0.120 | -0.136 | -0.180 | -0.186 |
| d-CH ₄ | -0.089 | -0.115 | -0.133 | -0.136 |
| t-CH ₄ | -0.113 | -0.140 | -0.177 | -0.180 |

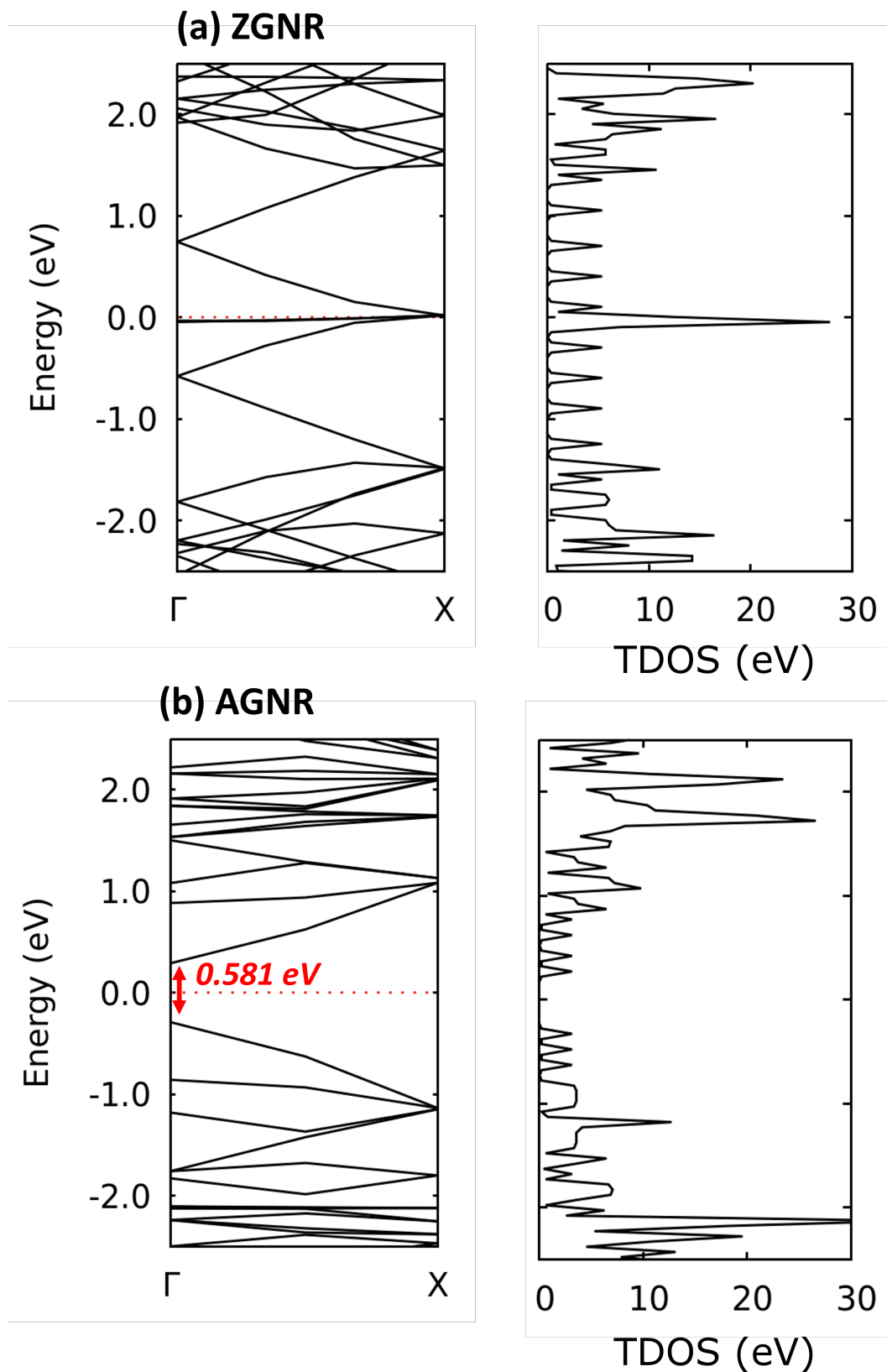


Figure S1. Band structure (left) and total density of states (right) of (a) pristine 12-ZGNR and (b) pristine 12-AGNR. A uniform ($10 \times 1 \times 1$) k-point sampling grid was adopted for the band structure calculations

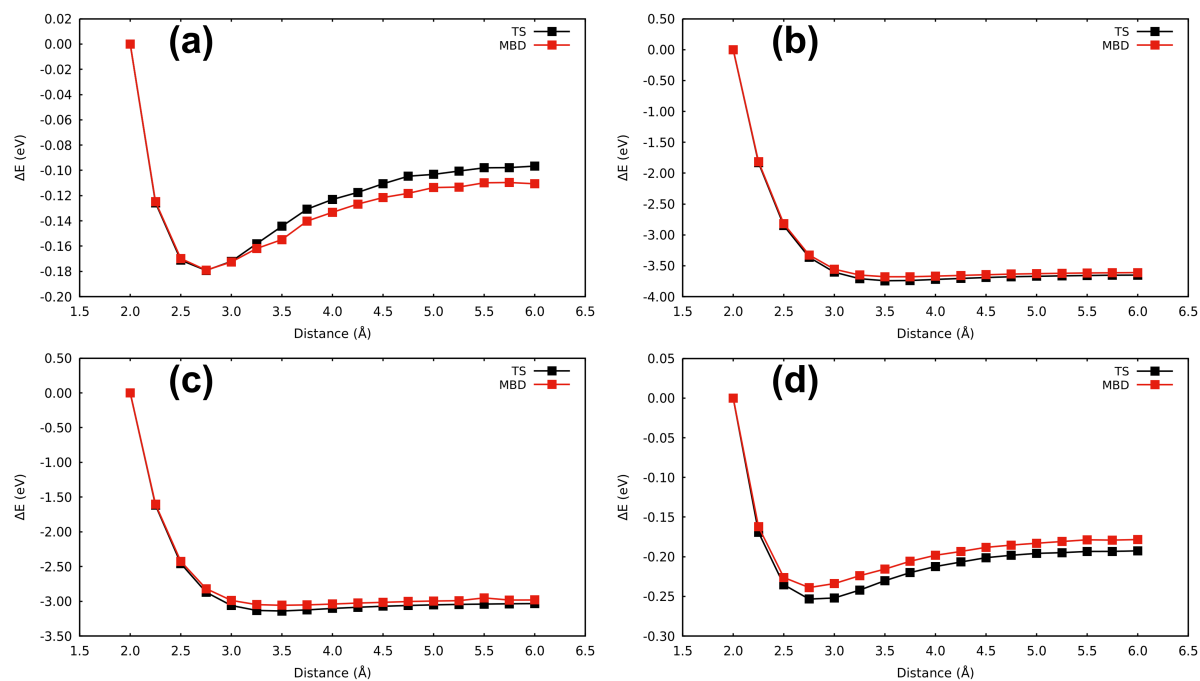


Figure S2. Potential energy surface as a function from the CH₄ distance from the Z1 adsorption site on 12-ZGNR, adopting the TS and MBD dispersion corrections. The PES were constructed in respect to the (a) d-CH₄ conformation; (b) t-CH₄ conformation; (c) u-CH₄ conformation physisorbed on Z1 site and (d) on the Z1-IP site.

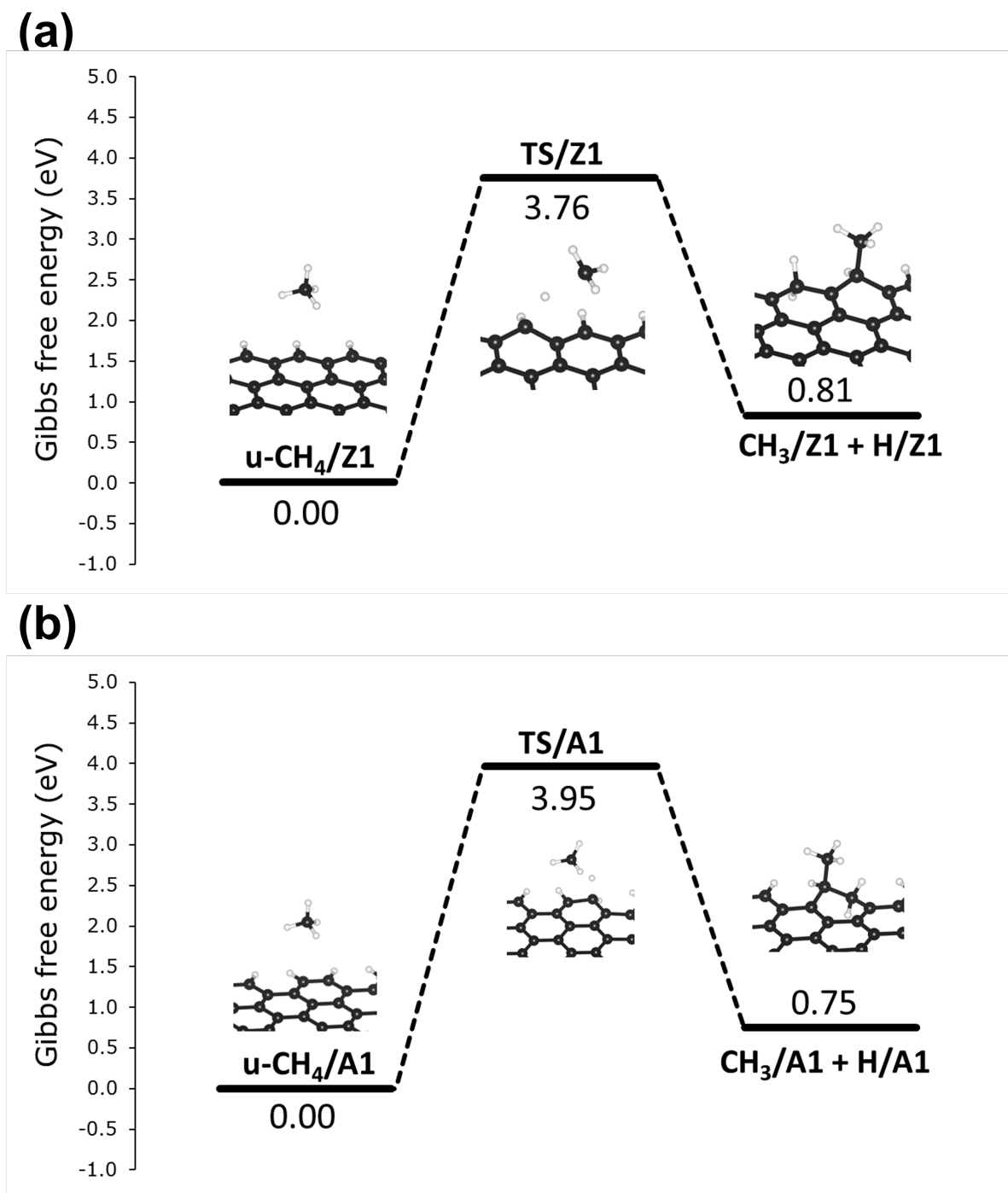


Figure S3. Gibbs free energy reaction profile of the u-CH₄ adsorption on the Z1 and A1 sites of the 12-ZGNR and 12-AGNR, respectively.

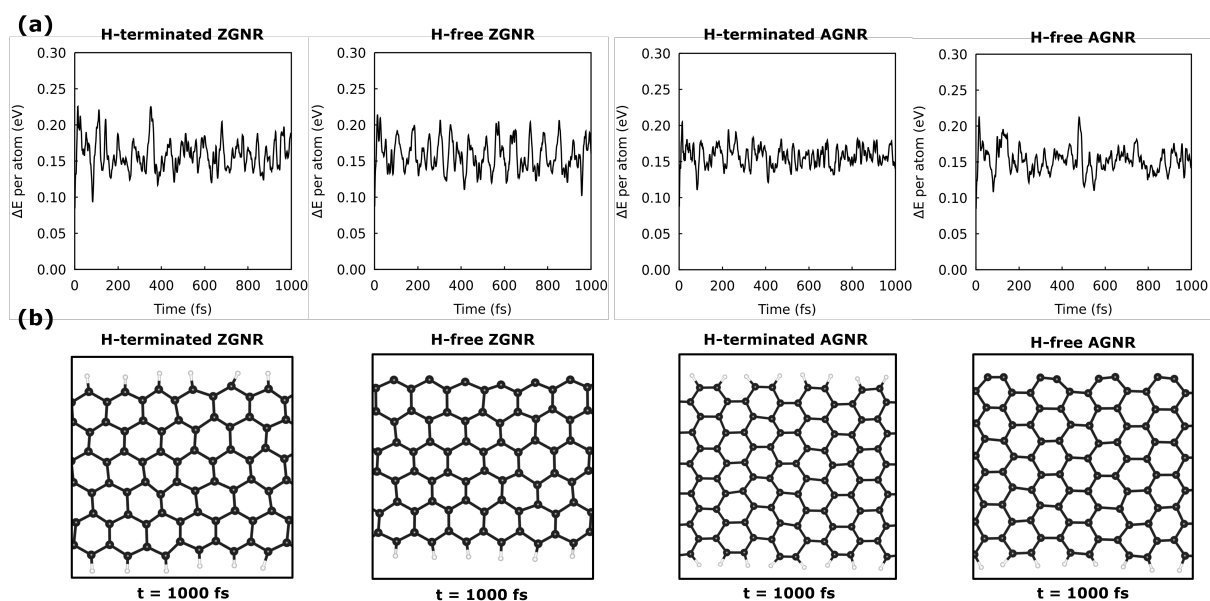


Figure S4. (a) Variation of electronic energy per atom, in respect to the minimum energy structure, against the time, upon AIMD simulations at 1200 K for the H-terminated and H-free ZGNR and AGNR (b) Snapshot of the each ZGNR and AGNR structures after 1000 fs simulation time.

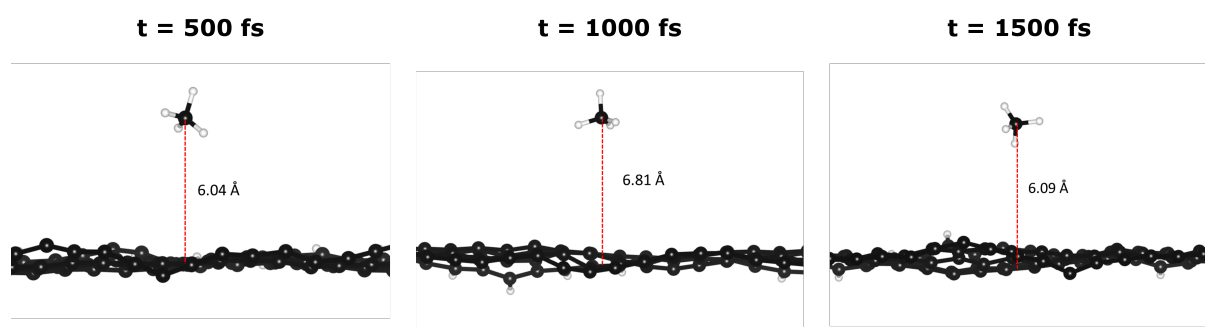


Figure S5. Snapshot of AIMD simulations of methane physisorbed on H-free ZGNR at 500 fs, 1000 fs and 1500 fs

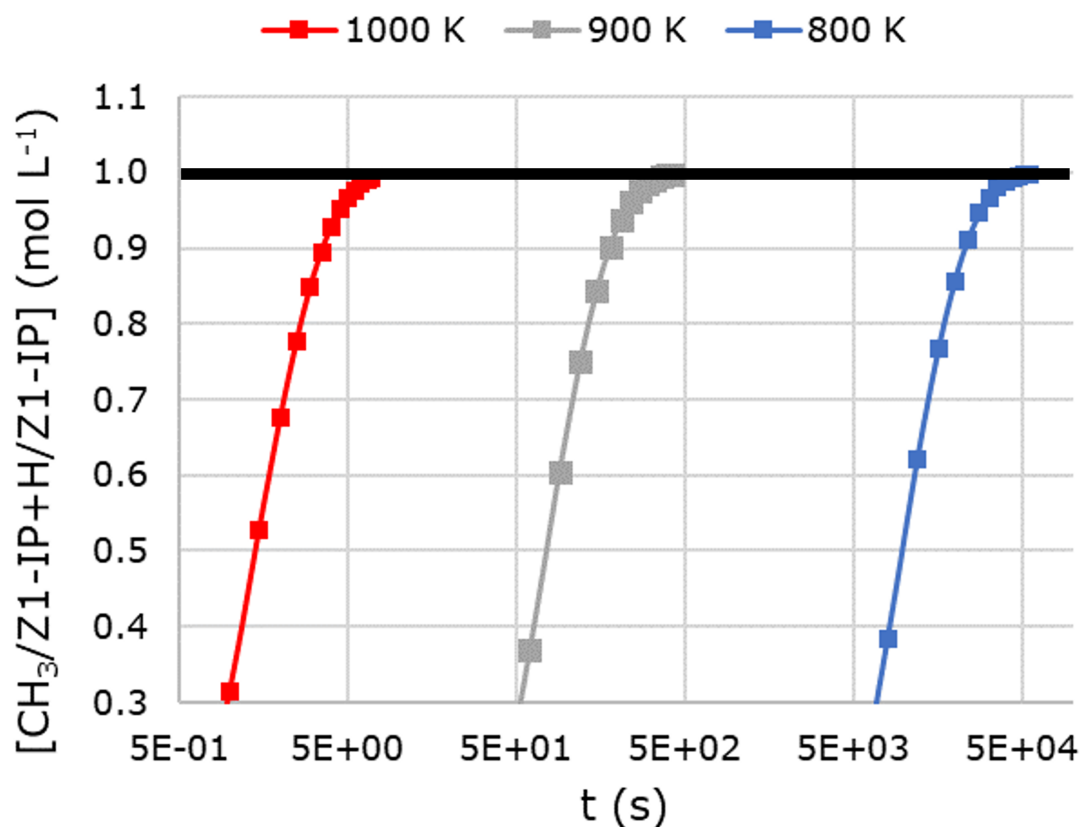


Figure S6. Concentration in mol L⁻¹ as a function of time of the most thermodynamic favourable chemisorption product, CH₃/Z1 + H/Z1, from methane (u-CH₄/Z2). Rate coefficients were obtained by means of the Transition State Theory, at the temperatures of 800 K, 900 K and 1000 K. The lattice-gas thermodynamic model was adopted in all calculations. Simulations were made considering the reaction mechanisms (ii) and (iii) of the main manuscript, i.e., we considered u-CH₄/Z2 as the intermediate, and CH₃-H/Z₁ and CH₃/Z1 + H/Z1 as the initial and final states, respectively. Numerical simulations were done considering the steady-state approximation, in which $d[u\text{-CH}_4/\text{Z2}]/dt \approx 0$.