1 **Supplementary information**

2 **Viral lysing can alleviate microbial nutrient limitations and**

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Supplementary Materials and Methods

 microbial resource acquisition strategies [4-5]. Vector length and angle were calculated as:

$$
31 \tV_{length} = SQRT(x^2 + y^2)
$$
\t(1)

$$
32 \quad V_{angle} \ (degree) = Degrees \ (Atan2(x, y)) \tag{2}
$$

- 2. Calculation of microbial metabolic efficiency
- 39 Microbial metabolic efficiency can be represented by $qCO₂$ and CUE, where higher metabolic efficiency equates to lower qCO2 and higher CUE [6]. Soil qCO2 41 signifies microbial respiration per unit biomass and is expressed in the units of mg $CO₂$ 42 \degree C mg⁻¹ MBC d⁻¹ [7]. According to the biogeochemical equilibrium model, CUE was
- indirectly calculated as equations (3-5).

$$
GUE = CUE_{max} \times \sqrt{\frac{S_{C:N} \times S_{C:P}}{(K_{C:N} + S_{C:N}) \times (K_{C:P} + S_{C:P})}}
$$
(3)

45
$$
S_{C:N} = B_{C:N} / L_{C:N} \times 1/EEA_{C:N}
$$
 (4)

$$
46 \t S_{C:P} = B_{C:P}/L_{C:P} \times 1/EEA_{C:P} \t\t(5)
$$

Where EEA_{C:N} and EEA_{C:P} were calculated as
$$
ln(BG)/ln(NAG + LAP)
$$
 and $ln(BG)/ln(AP)$, respectively. Lc:x is the molar C:X ratio of labile substrates (e.g., labile carbon, nitrogen and phosphorus represented by DOC, inorganic N (NH₄⁺ + NO₃⁻) and available P, respectively). Bc:x is the molar ratio of microbial biomass carbon, nitrogen

 and phosphorus. According to thermodynamic constraints of the saturating Michaelis- Menten formulation, CUEmax represents the maximum microbial growth efficiency, and 53 was set as 0.60. Kc:x was fixed to 0.50 and represents the half-saturation constant [6].

Supplementary Figures

- **Figure S1.** Cumulative CO2 fluxes during incubation at 25℃ (A) and 15℃ (B).
- **Figure S2.** Cumulative CO2 emission for incubations at three time points of 7 d (A, B),
- 28 d (C, D) and 98 d (E, F).
- **Figure S3.** Calculation of Q10 (mean ±std dev) at different groups.
- **Figure S4.** Metabolic quotient (qCO2, respiration per unit of microbial biomass, mg
- 61 CO₂–C mg⁻¹ MBC d⁻¹).
- **Figure S5.** Microbial resource acquisition strategy.
- **Figure S6.** Excitation-emission matrix (A, B, C) of DOM for three fluorescent
- components.
- **Figure S7.** Hydrophobicity of DOM after incubation as determined by SUV260.
- **Figure S8.** Correlation heatmap between microbial resource acquisition traits and
- optical properties of DOM.
- **Figure S9.** Principal coordinates analysis (PCoA) of bacterial communities in different
- 69 groups at incubation temperatures of 25 °C (A) and 15 °C (B).
- **Figure S10**. Redundancy analysis (RDA) at OTU level demonstrating the effect of soil
- physicochemical properties on bacterial communities for different groups.
-

74 **Figure S1.** Cumulative CO₂ fluxes (mean \pm std dev) during incubation at 25 °C (A) and

15 ℃ (B). SM, no added viruses; DV, added-inactive viruses; V, added-active viruses

86 represent significant differences at $p < 0.05$.

Figure S3. Calculation of Q10 (mean ±std dev) at different groups. SM, no added viruses;

90 DV, added-inactive viruses; V, added-active viruses with no dilution; 2^{-1} V, added-active

91 viruses with 2-fold dilution; 10^{-1} V, added-active viruses with 10-fold dilution.

95 biomass, mg CO2–C mg⁻¹ MBC d⁻¹). SM, no added viruses; DV, added-inactive viruses;

- 96 V, added-active viruses with no dilution; 2^{-1} V, added-active viruses with 2-fold dilution; 10^{-1} V, added-active viruses with 10-fold dilution; 25 and 15 signify the temperature (25 ℃ and 15 ℃) during the incubation. Different lowercase letters represent 99 significant differences at $p < 0.05$.
-

 Figure S5. Microbial resource acquisition strategy (mean ±std dev). The Length quantified the relative C vs. nutrient (N and P)-acquiring enzyme activities. A lower Length indicates relatively higher nutrient acquisition strategies (relative to C). SM, no 105 added viruses; DV, added-inactive viruses; V, added-active viruses with no dilution; 2-

- ¹ V, added-active viruses with 2-fold dilution; 10^{-1} V, added-active viruses with 10-fold
- dilution; 25 and 15 signify the temperature (25 ℃ and 15 ℃) during the incubation.
- 108 Different lowercase letters represent significant differences at $p < 0.05$.
-

Figure S6. Excitation-emission matrix (A, B, C) of DOM for three fluorescent

- components (Component 1: humic-like components [8-9]; Component 2: quinone-like
- components [10]; Component 3: protein-like component [11]) identified by EEM-
- 114 PARAFAC analysis.
-

Figure S7. Hydrophobicity of DOM after incubation (mean ±std dev) as determined by

SUV260. SM, no added viruses; DV, added-inactive viruses; V, added-active viruses

 Figure S8. Correlation heatmap between microbial resource acquisition traits and optical properties of DOM. Cumulation, cumulative CO2 emission; qCO2, metabolic 127 quotient, CUE, carbon use efficiency; CO₂, the CO₂ emission rate; HIX, aromaticity degree of DOM; C1 (humic-like), C2 (quinone-like), and C3 (protein-like), different 3D-fluorescence components of DOM; SUV254, represents the humification of DOM; SUV260, represents the hydrophobicity of DOM; Length, relative C:nutrient acquiring ratio; Angle, relative P:N-acquiring ratio.

Figure S9. Principal coordinates analysis (PCoA) of bacterial communities in different

135 groups at incubation temperatures of 25 °C (A) and 15 °C (B).

 Figure S10. Redundancy analysis (RDA) at OTU level demonstrating the effect of soil physicochemical properties on bacterial communities for different groups. NO3, soil nitrate-N; NH4, soil ammonium-N; AP, available phosphorus; SOC, soil organic carbon; TN, total nitrogen; DOC, dissolved organic carbon; DON, dissolved organic 142 nitrogen; N/P, the mass ratio of total nitrogen and total phosphorus; C/P, the mass ratio of soil organic carbon and total phosphorus; C/N, the mass ratio of soil organic carbon and total nitrogen; AP/MBC represents normalized enzyme activities of acid phosphatase as units/mg MBC; Ecoenzymatic vector length (length, relative C:nutrient acquiring ratio) and angle (angle, relative P:N-acquiring ratio); HIX, aromaticity degree of DOM; C1 (humic-like), C3 (protein-like), different 3D-fluorescence components of

- 148 DOM; MD, relative molecular mass of DOM; SUV260, hydrophobicity of DOM; MBC,
- microbial biomass carbon; MBP, microbial biomass phosphorus. **p* < 0.05; ***p* < 0.01.

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