Supplementary Material - Modeling the impact of school reopening and contact tracing strategies on Covid-19 dynamics in different epidemiologic settings in Brazil

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1 Introduction

This model framework was first introduced in Águas et al.^{[1](#page-6-0)} and modified to account for brazilian hospital structure and percolation effects in Franco et al.^{[2](#page-6-1)}. The code is available at [https://github.com/covid19br/](https://github.com/covid19br/school_reopening_manuscript) school reopening [manuscript.](https://github.com/covid19br/school_reopening_manuscript) In Section [2](#page-6-1) we introduce our modifications in the Brazilian model structure² to account for contact tracing strategies. Section [2.1](#page-1-1) describes the equations, along with the explanation and sources of the parameters used. Section [2.2](#page-2-0) describes how the force of infection for quarantined and nonquarantined work in the model. Section [2.5](#page-3-0) thoroughly describes our contact tracing model. Section [3](#page-4-0) lists the interventions used in the main paper. Finally, Section [4](#page-5-0) shows the procedure used to fit the model to data and Section [5](#page-6-2) describes our approach to sensitivity analysis.

2 Model structure

2.1 Model equations

The model consists of an expanded age-structured SEIR model to account for asymptomatic individuals, a detailed structure of the Brazilian health system, transmission in different settings, and non-pharmaceutical interventions, including contact tracing strategies. The model was simulated by solving its deterministic differential equations and implemented in R with the package deSolve Soetaert, Petzoldt, Setzer [\[3\]](#page-6-3). We write

$$
\frac{dS}{dt} = -\lambda S + \omega R + A_{G} \cdot S + \mu_{b} - \mu_{d}S - (Q_{in} + Q_{in,2})S + Q_{d}QS
$$
\n
$$
\frac{dE}{dt} = \lambda S - \gamma E + A_{G} \cdot E - \mu_{d}E - (Q_{in} + Q_{in,2})E + Q_{d}QE
$$
\n
$$
\frac{dA}{dt} = \gamma (1 - P_{clin})(1 - \sigma)E - \nu_{i}A + A_{G} \cdot A - \mu_{d}A - (Q_{in} + Q_{in,2})A + Q_{d}QI
$$
\n
$$
\frac{dI}{dt} = (1 - Q_{cov}T_{I})\gamma P_{clin}(1 - P_{selfis})(1 - \sigma)E - \nu_{i}I + A_{G} \cdot I - \mu_{d}I + Q_{d}QC
$$
\n
$$
\frac{dX}{dt} = \gamma P_{selfis}P_{clin}(1 - \sigma)E - \nu_{i}X + A_{G} \cdot X - \mu_{d}X
$$
\n
$$
\frac{dH}{dt} = \gamma \sigma (1 - P_{icu})(1 - \phi_{H})(E + QE) - \nu_{s}H + A_{G} \cdot H - \mu_{d}H
$$
\n
$$
\frac{dICU}{dt} = \gamma \sigma (1 - P_{icu})\phi_{H}(E + QE) - \nu_{sc}HC + A_{G} \cdot HC - \mu_{d}HC
$$
\n
$$
\frac{dICU}{dt} = \gamma \sigma P_{icu}(1 - \phi_{c})(E + QE) - \nu_{icu}ICU + A_{G} \cdot ICU - \mu_{d}ICU
$$
\n
$$
\frac{dICUH}{dt} = \gamma \sigma P_{icu}\phi_{c}(1 - \phi_{cH})(E + QE) - \nu_{icu}ICUH + A_{G} \cdot ICUL - \mu_{d}ICUH
$$
\n
$$
\frac{dICUC}{dt} = \gamma \sigma P_{icu}\phi_{c} \phi_{cH}(E + QE) - \nu_{icu}ICUC + A_{G} \cdot ICUC - \mu_{d}ICUC
$$
\n
$$
\frac{dR}{dt} = \nu_{i}A - \omega R + \nu_{i}X + \nu_{i}I + A_{G} \cdot R - \mu_{d}R + \nu_{s}(1 - P_{d}\mu_{H})H - (Q_{in} + Q_{in,2})R + Q_{d}QR + \nu
$$

$$
\frac{d\mathbf{Q}\mathbf{S}}{dt} = -\lambda_q \mathbf{Q}\mathbf{S} + \omega \mathbf{Q}\mathbf{R} + \mathbf{A}_{\mathbf{G}} \cdot \mathbf{Q}\mathbf{S} - \mu_d \mathbf{Q}\mathbf{S} + (Q_{in} + Q_{in,2})\mathbf{S} - Q_d \mathbf{Q}\mathbf{S}
$$
\n
$$
\frac{d\mathbf{Q}\mathbf{E}}{dt} = \lambda_q \mathbf{Q}\mathbf{S} - \gamma \mathbf{Q}\mathbf{E} + \mathbf{A}_{\mathbf{G}} \cdot \mathbf{Q}\mathbf{E} - \mu_d \mathbf{Q}\mathbf{E} + (Q_{in} + Q_{in,2})\mathbf{E} - Q_d \mathbf{Q}\mathbf{E}
$$
\n
$$
\frac{d\mathbf{Q}\mathbf{I}}{dt} = \gamma (1 - P_{olin})(1 - \sigma) \mathbf{Q}\mathbf{E} - \nu_i \mathbf{Q}\mathbf{I} + \mathbf{A}_{\mathbf{G}} \cdot \mathbf{Q}\mathbf{I} - \mu_d \mathbf{A} + (Q_{in} + Q_{in,2})\mathbf{A} - Q_d \mathbf{Q}\mathbf{I}
$$
\n
$$
\frac{d\mathbf{Q}\mathbf{R}}{dt} = \nu_i (\mathbf{Q}\mathbf{I} + \mathbf{Q}\mathbf{C}) + \mathbf{A}_{\mathbf{G}} \cdot \mathbf{Q}\mathbf{R} - \omega \mathbf{Q}\mathbf{R} + (Q_{in} + Q_{in,2})\mathbf{R} - Q_d \mathbf{Q}\mathbf{R}
$$
\n
$$
\frac{d\mathbf{Q}\mathbf{C}}{dt} = Q_{cov}T_I \gamma P_{clip}(1 - P_{selfis})(1 - \sigma)\mathbf{E} + \gamma P_{clip}(1 - \sigma)\mathbf{Q}\mathbf{E}
$$
\n
$$
-\nu_i \mathbf{I} + \mathbf{A}_{\mathbf{G}} \cdot \mathbf{I} - \mu_d \mathbf{I} - Q_d \mathbf{Q}\mathbf{C}
$$
\n
$$
\frac{d\mathbf{C}}{dt} = r\gamma (1 - \sigma)(1 - P_{clip})(\mathbf{E} + \mathbf{Q}\mathbf{E}) + r_c \gamma (1 - \sigma) P_{clip}(\mathbf{E} + \mathbf{Q}\mathbf{E}) + r_h \gamma \sigma (\mathbf{E} + \mathbf{
$$

$$
\frac{dC_{\text{ML}}}{dt} = \nu_s P_{dh} \mu_H \mathbf{H} + \nu_{sc} P_{dhc} \mu_H \mathbf{H} \mathbf{C} + \nu_{icu} P_{dicu} \mu_H \mathbf{ICU} + \nu_{icuc} P_{dicu} \mu_H \mathbf{ICUC}
$$
\n
$$
+ \nu_{icuh} P_{dicuh} \mu_H \mathbf{ICU} \mathbf{H} + \mu_d (\mathbf{H} + \mathbf{HC} + \mathbf{ICU} + \mathbf{ICU} \mathbf{H} + \mathbf{I} + \mathbf{X})
$$
\n
$$
\frac{dCMC}{dt} = \nu_{sc} P_{dhc} \mu_H \mathbf{HC} + \nu_{icuc} P_{dicu} \mu_H \mathbf{ICUC}
$$
\n
$$
+ \nu_{icuh} P_{dicuh} \mu_H \mathbf{ICU} \mathbf{H} + \mu_d (\mathbf{HC} + \mathbf{ICUC})
$$

where each of the dynamic variables (corresponding to the compartments shown in Table [1\)](#page-7-0) is further subdivided in 19 age classes consisting of 5 years age bins $(0-4,5-9,$ up to $90+)$. Thereby, each of the parameters written in the model, aside from A_G (ageing matrix), should be thought of as diagonal matrices containing parameter values corresponding to each age class. Take, as an example, the natural mortality rate, given by

$$
\hat{\mu}_d = \text{diag}(\mu_{d1}, \mu_{d2}, ..., \mu_{dD}) = \text{diag}(\vec{\mu}_d).
$$

Note that, in the system of equations presented above, we drop the hats/bolds from all diagonal matrices to avoid an overloaded notation, but keep them in all variables. Thus, each of them actually represents $D = 19$ different ODEs, and therefore the number of equations is D multiplied by the number of compartments. A description of each parameter from the model is available at table [2.](#page-8-0)

Finally, A_G implements ageing of the population, and it is defined as a 19×19 matrix given by:

$$
A_G = \frac{1}{1826.25} \begin{pmatrix} -1 & 0 & 0 & 0 & \dots & 0 & 0 & 0 \\ 1 & -1 & 0 & 0 & \dots & 0 & 0 & 0 \\ 0 & 1 & -1 & 0 & \dots & 0 & 0 & 0 \\ \vdots & & & & & \ddots & & \vdots \\ 0 & 0 & 0 & 0 & \dots & 1 & -1 & 0 \\ 0 & 0 & 0 & 0 & \dots & 0 & 1 & 0 \end{pmatrix}
$$
(1)

where the denominator accounts for the time to transition between age bins in a 5-year division in units of days.

2.2 Force of infection

Our model assumes two different forces of infection, one for the non-quarantined individuals λ and other for quarantined individuals λ_q . Non-quarantined individuals can be infected by non-quarantined infected individuals in four locations: school, work, home, and in the community. They can also be infected by interacting with quarantined familiars in the "home" setting, and quarantined individuals in other households through the "community" matrix setting. The later considers that transmission by occasional contacts with quarantined individuals in their households may occur, such as in food delivery contexts, for instance. Assuming that \hat{c} is the total contact matrix with percolation effect and non-pharmaceutical interventions described in Franco et al.^{[2](#page-6-1)}, and \hat{c}_i being the other matrices with the "cocooning of older adults" intervention, with $i = \{\text{home, school, work, community}\},\$ we have:

$$
\lambda = (1 - mask(t))p\hat{c}(\rho \mathbf{E} + \mathbf{A} + \mathbf{I} + imports + \rho_s(\mathbf{H} + \mathbf{ICU} + \mathbf{ICUH}))/N
$$
\n
$$
+ (1 - mask(t))p(1 - f_{perc})\hat{c}_{home}(\rho \mathbf{QE} + \mathbf{Q}\mathbf{I} + \mathbf{QC} + \mathbf{X} + \mathbf{HC} + \mathbf{ICUC})/N
$$
\n
$$
+ (1 - mask(t))p(1 - Q_{eff,com})\hat{c}_{com}(\rho \mathbf{QE} + \mathbf{Q}\mathbf{I} + \mathbf{QC} + \mathbf{X} + \mathbf{HC} + \mathbf{ICUC})/N
$$
\n(2)

where $Q_{eff,com}$ is a parameter of reduction in mean contacts between quarantined and non-quarantined by the "community" contact matrix, imports is the value of new imported cases added by day (see Section [3](#page-4-0) for details), N is the population size per age group, and f_{perc} and $mask(t)$ are the percolation effect and the usage of mask intervention, respectively, described in Franco et al.^{[2](#page-6-1)}.

Similarly, a quarantined susceptible individual can be infected by an infected person inside the household, or be infected by interacting through the "community" contact matrix, as follows:

$$
\lambda_q = (1 - mask(t))p(1 - f_{perc})\hat{c}_{home}(\rho \mathbf{QE} + \mathbf{Q}\mathbf{I} + \mathbf{QC} + \mathbf{X} + \mathbf{HC} + \mathbf{ICUC})/\mathbf{N}
$$

+ (1 - mask(t))p(1 - Q_{eff,com})\hat{c}_{com}(\rho \mathbf{E} + \mathbf{A} + \mathbf{I} + imports + \rho_s(\mathbf{H} + \mathbf{ICU} + \mathbf{ICU}\mathbf{H}))/\mathbf{N}(3)

2.3 Computing the birth rate

To compute the birth rate, we consider that half of the population is females. With this, we compute the birth rate per female per age b_i using the data described in Table [5.](#page-11-0) Therefore our birth rate is given by:

$$
\mu_b(t) = (\mu_{b,0-4}(t), 0, \dots, 0) = \left(\sum_{j=0-4}^{85+} b_j \frac{N_j(t)}{2}, 0, \dots, 0\right)
$$
\n(4)

2.4 Computing the probability of dying when unattended

To be able to simulate an age-varying risk of death when an individual does not receive proper health assistance, we do the following: First, we consider the age-stratified risk of dying when the individuals are properly assisted. We then renormalize this vector \hat{v} by the highest value P (pdeath h and pdeath icu, for common bed and ICU, respectively). Thus, the age with the highest risk will have a value of 1. Naturally, we can recover the probability of dying when attended simply by doing $P\hat{v}$. To consider the risk of dying when not receiving attendance, we multiply \hat{v} by the highest risk of dying in each case (pdeath hc if not receiving common bed if needed, pdeath icuh if needing ICU bed, but receiving a common one and pdeath icuc if needing ICU bed, but not receiving any attendance). This will naturally be age-stratified, as \hat{v} is. The actual values of the maximum probability of dying are given in Table [4.](#page-10-0)

2.5 Contact tracing

In our definition, individuals quarantined by contact tracing are the ones that were quarantined not by direct testing, but being detected as contacts of tested (and infected) individuals. We use the contact matrices from [\[4\]](#page-6-4) as a proxy for the contact network of each infected individual, while still assuming a well-mixed model. To implement the contact tracing strategy, we assume that individuals from compartments S, E, A, I, HC, ICUH, ICUC, and R can be transferred to their respective "quarantined" compartments where their remain isolated, thus, decreasing the chance of infecting other individuals. Isolation occurs after being positively diagnosed as infected by testing, and quarantining occurs when you are traced as a contact of a positively diagnosed individual. For simplicity, we refer to all individuals isolated by the contact tracing strategy as "quarantined". Our model supports two ways of testing, one fixing the probabilities PT_i for each compartment or supplying a number of tests applied per day n_t . While the implementation of the first case is trivial, for the second one, we first calculate the entrance rate F_i from the exposed (quarantined and non-quarantined) compartment to the compartment studied (for example, $F_H = \gamma IHR(1-P_{icu})(1-H_c)(\mathbf{E}+\mathbf{QE}))$, with i following the given sequence of priority $i = \{ICU, ICUH, H, ICUC, HC, X+CL\}$ (here assuming that non-symptomatic individuals are not tested in first place). The index ℓ represents the age group. This gives us the daily number of new cases in each compartment. Then, the probability of testing the compartment j (that follows the same sequence of i) is given by:

$$
x = \frac{n_t - \sum_{\ell} \sum_{i}^{j-1} F_{i\ell}}{\sum_{\ell} F_{j\ell} + 1}
$$

\n
$$
PT_j = \begin{cases} 0, & \text{if } x < 0 \\ 1, & \text{if } x > 1 \\ x, & \text{otherwise.} \end{cases}
$$
 (5)

where we add 1 to the denominator to avoid division by zero. The term $n_t - \sum_{i=1}^{j-1} F_i$ calculates the number of tests that are available to be used in compartment j after being used in higher priority compartments. The ratio between the number of tests available and the number of new daily cases in the j compartment then gives the probability of a new case being detected by testing, assuming a completely random testing strategy within the population (but still assuming a priority rule to allocate the tests). Of course, if there are more tests available than needed, the probability will be 1, and if there are no tests left, it will be zero.

Consider again the entrance rate F_i , but this time only considering non-quarantined exposed individuals. Then, the entrance rate from a compartment to the corresponding quarantined one is given by:

$$
\mathbf{Q}_{in} = \frac{Q_{cov}\tau_{w}}{P - Q} \left(\sum_{k} E_{k}\hat{c}_{k}\right) \sum_{j} PT_{j} F_{j}
$$
(6)

where Q_{cov} is the adherence to quarantine, τ_w is the time window of traced contacts, $P - Q$ is the total (alive) population discounted for the already quarantined individuals, and E_k is the estimated reduction of contacts due to the contact tracing in each k contact matrix (ie. home, work, school, or community; for the results concerning this paper, the only non-zero reduction of contacts is the one related to school contacts). Notice that the entrance rates are age-stratified, thus the entrance rate to quarantine is also stratified.

Finally, if there are still tests available, they are applied to asymptomatic, exposed, recovered, and susceptible individuals who were identified as contacts of already tested individuals:

$$
x = \frac{n_{t,2}}{1 + \sum_{\ell} Q_{in,\ell} (\mathbf{S}_{\ell} + \mathbf{E}_{\ell} + \mathbf{A}_{\ell} + \mathbf{R}_{\ell})}
$$

\n
$$
PT_{sec} = \begin{cases} 0, & \text{if } x < 0 \\ 1, & \text{if } x > 1 \\ x, & \text{otherwise.} \end{cases}
$$
 (7)

where we add 1 to the fraction to avoid division by zero, $n_{t,2} = n_t - \sum_{i,\ell} F_{i,\ell} > 0$ is the number of remaining tests. The ratio between the number of tests available per day and the number of new quarantined individuals per day then gives us the probability of a new case being detected by testing, assuming a completely random testing strategy within the population. Notice that $PT_E = PT_A$ (which we call PT_{sec} since we do not distinguish between them, and $PT_S = PT_R = 0$ as we assume there are no false positives. Once again, these probabilities have to remain between 0 and 1.

Then the rate of quarantining of second-order contacts is given by:

$$
\mathbf{Q}_{in,2} = \frac{Q_{cov}\tau_w}{P - Q} \left(\sum_k E_k \hat{c}_k\right) PT_{sec} \mathbf{Q}_{in}(\mathbf{E} + \mathbf{A})
$$
\n(8)

Table [6](#page-11-1) shows the contact tracing parameters assumed for this study:

3 List of interventions

Here we describe the interventions used as input of the model, reproducing (with permission) Franco et al.^{[2](#page-6-1)}. Tables [7,](#page-13-0) [8](#page-14-0) and [9](#page-15-0) comprises all interventions used in the fitting of the model. Figures [1,](#page-9-1) [2](#page-12-0) and [3](#page-12-1) show the timeline of these interventions.

• Self-Isolation: Symptomatic individuals that do not require hospitalization voluntarily isolate themselves during the time of infection and reduce the chance of infecting others. The beginning and end period of this intervention is defined by $\theta_{selfis}(t)$ and represents the days t when the population adheres to this behavior. The impact of this NPI depends on its adherence to self-isolation $selfis_{cov}$ and estimated reduction in contacts by self-isolation $selfis_{eff}$ values, where

$$
P_{selfis} = selfis_{cov}(t) selfis_{eff} \theta_{selfis}(t)
$$
\n(9)

• Social Distancing: the population avoids or reduces contacts in the community setting (\hat{c}_{com}) . This intervention comprises reduction of contacts on churches, markets, social events and gatherings, shopping activities, gyms, and others. The beginning and end period of this intervention is defined by $\theta_{dist}(t)$. The impact of this NPI depends on its adherence to social distancing at community level $(dist_{cov})$ and reduction of contacts in the community among those adhering to social distancing $(distr_{eff})$ values, where:

$$
dist(t) = dist_{cov}(t)dist_{eff}\theta_{dist}(t); \qquad (10)
$$

• Use of masks: This intervention comprises individual protection measures, given by the adoption of mask usage. The beginning and end period of this intervention is defined by $\theta_{mask}(t)$. The impact of this NPI depends on its adherence to mask usage $(mask_{cov})$ and the proportion in the reduction of contacts $(mask_{eff})$, where

$$
mask(t) = mask_{cov}(t) mask_{eff} \theta_{mask}(t); \qquad (11)
$$

• Work from home: This intervention reduces contacts in the work environment (\hat{c}_{work}) as workers perform their activities from their home. The beginning and end period of this intervention is defined by $\theta_{work}(t)$. The impact of this NPI depends on the adherence to home-office (work_{cov}) and reduction of contacts at work among those adhering to home-office $(wordk_{eff})$, where:

$$
work(t) = work_{cov}(t)work_{eff}\theta_{work}(t);
$$
\n(12)

• School closure: This intervention reduces the contacts in the school setting (\hat{c}_{school}) due to limitation of in-school activities or school closures. The beginning and end period of this intervention is defined by $\theta_{school}(t)$. The effectiveness of this NPI depends on the adherence to online (not in-person) school activities (school_{cov}) and the estimated reduction of contacts in school upon school closure (school_{eff}), where:

$$
school(t) = school_{cov}(t) school_{eff} \theta_{school}(t); \qquad (13)
$$

Note that in the main text, $school_{cov}$ is also referred as PCS (potential contacts in school).

- cocooning of older adults: This intervention reduces the contacts to a proportion of the older adult population, given a minimum age D^{\dagger} . The beginning and end period of this intervention is defined by $\theta_{cocon}(t)$. The effectiveness of this NPI depends on the adherence to cocooning of older adults ($cocon_{cov}$) and the estimated reduction of contacts with older adults in all settings as a results of cocooning older adults ($cocon_{eff}$). Additional details of this implementation is described in Franco et al.^{[2](#page-6-1)}.
- Travel ban: This intervention models the interruption of travel flow from outside the city and the isolation of cases coming from outside, which reduces or eliminate import cases. This intervention is given by:

$$
imports = (1 - travel_{eff}) mean_imports
$$
\n(14)

where (mean imports) is the mean value of imported cases, $travel_{eff}$ the effectiveness of this intervention, and imports the number of new cases that are added to the population per day.

4 Model Fitting

To fit the model onto epidemiological data, we used consolidated time series from Severe Acute Respiratory Infection (SARI) hospitalisations and deaths in São Paulo, Goiânia and Porto Alegre from the SIVEP-Gripe $database⁵$ $database⁵$ $database⁵$ between the dates described in table [10.](#page-15-1)

In Brazil, SARI case notification is compulsory (leading to high reporting rates) and SARS-CoV-2 is included as a SARI category. Due to the lack of extensive testing, we assume that using only SARS-CoV-2 confirmed cases would lead to an underestimation of the actual number of cases. Hence, we assume that SARI cases are a better approximation to the number of SARS-CoV-2, rather than only cases confirmed by PCR tests. Since SIVEP-Gripe reports only severe cases that require hospitalisation, we fit SARI cases to the sum over all hospitalised compartments of the model.

Following Franco et al.^{[2](#page-6-1)}, we chose to use weekly time series for new cases and new deaths to avoid carrying past information into future values, which occurs when using time series of cumulative data.

Based on data from SIVEP^{[5](#page-6-5)}, we were able to estimate the COVID-19 In-Hospital Fatality Rate (IHFR) and Intensive Care mortality rate (ICMR) for each city (Table [3\)](#page-9-0). Other local parameters are described in Table [4,](#page-10-0) and local demographic rates per age group in Table [5.](#page-11-0)

Our model included four free parameters: p, startdate, T_{perc} , and h_{steep} . The parameter p indicates the probability of transmission per contact, and startdate is the date of onset of the pandemic, that is, the introduction of the first infected individual. The last two parameters are related to the assumption of a non-linear effect of reducing transmission when increasing social distancing measures in households, following the implementation by [\[2\]](#page-6-1). Based on a phenomenological approach, after a critical threshold of adherence to social distancing, the underlying network of transmission composed of a fully connected cluster collapses and breaks down into multiple smaller clusters. As a consequence, the probability of infection decreases drastically after this point. Thus, T_{perc} indicates this threshold, which represents the value of adherence to the social distancing intervention that results in the percolation effect. The parameter h_{steep} , in turn, indicates the steepness of the effect caused by the percolation: while values closer to zero indicate a more linear relationship between the intervention adherence and the reduction of contacts, higher values indicate a steeper change in the reduction of contacts after the percolation effect.

To perform a nonlinear least squares fitting of the free parameters $(p, T_{perc}, h_{steep}, startedate)$ to the data, we used the Levenberg-Marquardt algorithm implemented in the minpack. Im R package^{[6](#page-6-6)}.

To fit both new cases (C) and new deaths (D) , we had to account for residuals in different scales. One way to do that was by normalising each of the variables in respect to their total sum. Therefore, the resulting residual (R) is given by:

$$
R = \frac{\sum (C_{model} - C_{observed})}{\sum C_{observed}} + \frac{\sum (D_{model} - D_{observed})}{\sum D_{observed}}
$$
(15)

The algorithm minimises the square of this quantity, while evaluating the respective negative log-likelihood and minimising it.

To perform the non-linear optimisation, the algorithm requires a series of initial guesses. We tested a wide range of startdate values (from $2020 - 01 - 01$ to $2020 - 02 - 24$) and for each one we ran the fitting algorithm using several reasonable initial guesses for the other free parameters. Hence, this method gives us fitted p , T_{perc} and h_{steep} for each startdate considered.

With the goal to find a probability distribution for the fitted parameters^{[7](#page-7-1)}, we selected the run which returned the lowest residual for each *startdate*, with its respective (p, T_{perc}, h_{steep}) set. We then computed the negative log-likelihood for each start date, L_t :

$$
L_t = N \ln \left(\frac{1}{N} \sum_{i=1}^{N} R_{i,t}^2, \right) \tag{16}
$$

from which we can derive the probability for each startdate, given by

$$
P_t = \frac{exp(-L_t + min(\{L_t\}))}{\sum_t exp(-L_t + min(\{L_t\}))}.
$$
\n(17)

Finally, maximising the probability (which is equivalent to minimising the negative log-likelihood), we find sets of best fitted parameters for each of the cities considered (See Table [11\)](#page-16-0)

5 Sensitivity analysis

For the sensitivity analysis, we evaluated how changes in a parameter of interest can qualitatively and quantitatively alter the simulation results for the different scenarios evaluated for the reopening of schools. We set each parameter of interest to be fitted together with the main parameters, sampling uniformly the initial conditions in the range described in [12](#page-16-1) and choosing the best fit as result (see tables [13,](#page-16-2) [14](#page-16-3) and [15\)](#page-17-0). Each parameter was fit independently of the others. Since the adherence to the NPI varies in time, the parameter with "cov" were varied by a scaling factor, maintaining the variation in time.

We then compared the final difference in the incidence of cases and deaths in relation to a baseline scenario without school reopening. The simulations were repeated for the different school reopening values (PCS) and compared with the original simulation (see main text).

References

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Table 1: List of model variables in equations on supplementary material and in the code. Variables written in the main text may be different for readability, here, we stick to the nomenclature used throughout the code to help reproducibility.

Table 2: List of model parameters in equations on supplementary material and in the code. These variables are restricted to epidemiological variables (not the NPI-related ones).

| Age group | Goiânia-GO | | Porto Alegre-RS | | São Paulo-SP | | prob_icu | $\overline{\sigma^1}$ |
|-----------|-------------|-------------|-----------------|-------------|--------------|-------------|----------|-----------------------|
| | ICMR | IHFR | ICMR | IHFR | ICMR | IHFR | | |
| $0 - 4$ | 0.29 | 0.034 | 0.26 | 0.028 | 0.14 | 0.014 | 0.45 | 0.1 |
| $5-9$ | 0.29 | 0.034 | 0.26 | 0.028 | 0.14 | 0.014 | 0.45 | 0.1 |
| 10-14 | 0.29 | 0.034 | 0.26 | 0.028 | 0.14 | 0.014 | 0.52 | 0.1 |
| 15-19 | 0.29 | 0.034 | 0.26 | 0.028 | 0.14 | 0.014 | 0.52 | 0.1 |
| 20-24 | 0.29 | 0.034 | 0.26 | 0.028 | 0.14 | 0.014 | 0.25 | $0.5\,$ |
| 25-29 | 0.29 | 0.034 | 0.26 | 0.028 | 0.14 | 0.014 | 0.25 | 0.5 |
| 30-34 | 0.25 | 0.036 | 0.21 | 0.013 | $0.2\,$ | 0.028 | 0.32 | 1.1 |
| 35-39 | 0.25 | 0.036 | 0.21 | 0.013 | $0.2\,$ | 0.028 | 0.32 | 1.1 |
| 40-44 | 0.36 | 0.049 | 0.25 | 0.031 | 0.24 | 0.045 | 0.34 | 1.4 |
| 45-49 | 0.36 | 0.049 | 0.25 | 0.031 | 0.24 | 0.045 | 0.34 | 1.4 |
| 50-54 | 0.42 | 0.075 | 0.35 | 0.05 | 0.36 | 0.087 | 0.40 | 2.9 |
| 55-59 | 0.42 | 0.075 | 0.35 | 0.05 | 0.36 | 0.087 | 0.40 | $2.9\,$ |
| 60-64 | 0.59 | 0.166 | 0.56 | 0.109 | 0.52 | 0.162 | 0.48 | 5.8 |
| 65-69 | 0.59 | 0.166 | 0.56 | 0.109 | 0.52 | 0.162 | 0.48 | 5.8 |
| 70-74 | 0.69 | 0.194 | 0.71 | 0.262 | 0.62 | 0.248 | 0.54 | 9.3 |
| 75-79 | 0.69 | 0.194 | 0.71 | 0.262 | 0.62 | 0.248 | 0.54 | 9.3 |
| 80-84 | 0.76 | 0.295 | 0.82 | 0.498 | 0.69 | 0.459 | 0.47 | 26.2 |
| 85-89 | 0.76 | 0.295 | 0.82 | 0.498 | 0.69 | 0.459 | 0.47 | 26.2 |
| $90 +$ | 0.76 | 0.295 | 0.82 | 0.498 | 0.69 | 0.459 | 0.47 | 26.2 |

Table 3: National COVID-19 infection-hospitalization rate (IHR), and COVID-19 In-Hospital Fatality Rate (IHFR) and Intensive Care mortality rate (ICMR) in the 3 study sites, by age sub-groups. Brazil, 2020. σ : IHR ¹ Source: 11

Figure 1: Diagram of adherence, reduction of contacts and their product for each of the considered non-pharmaceutical interventions considered in the model for S˜ao Paulo, SP.

Table 4: Model Parameter Values used for analysis of COVID-19 school reopening scenarios in Goiânia, Porto Alegre and São Paulo, 2020

Table 5: Demographic data used to calculate the birth and mortality rate in Brazil, 2020.

¹ Source: 16

² Source:[8](#page-7-2) ³ Source:^{[9](#page-7-3)}

Parameter Description Value of the Contract of the Contract of the Value of the Value of the Value of the Valu $\begin{array}{lll} n_t & \qquad \text{Number of tests available at time t}\\ n_{t.2} & \qquad \text{Number of tests available at time t for second order testing} \end{array} \qquad \begin{array}{lll} \text{Var} & \qquad \text{Var} \\ \text{Var} & \qquad \text{Var} \\ \end{array}$ $n_{t,2}$ Number of tests available at time t for second order testing Varies Vari Probability of case of compartment i being detected Varies of compliance to the contact tracing strategy 1 Q_{cov} Level of compliance to the contact tracing strategy τ_w Time window of the contact tracing strategy 2 days E_{home} Estimated reduction of contacts due to the strategy in tracing contacts from "home" environment 0 E_{school} Estimated reduction of contacts due to the strategy in tracing contacts from "school" environment 1 E_{work} Estimated reduction of contacts due to the strategy in tracing contacts from "work" environment 0 E_{com} Estimated reduction of contacts due to the strategy in tracing contacts from "community" environment 0

Table 6: List of model parameters in equations on supplementary material and in the code. These variables are restricted to epidemiological variables (not the NPI-related ones).

Figure 2: Diagram of adherence, reduction of contacts and their product for each of the considered non-pharmaceutical interventions considered in the model for Goiânia, GO.

Figure 3: Diagram of adherence, reduction of contacts and their product for each of the considered non-pharmaceutical interventions considered in the model for Porto Alegre, RS.

| | | Self Isolation | | |
|------------|------------|---------------------------|-----------------------|--|
| Start date | End date | Adherence | Reduction of Contacts | |
| 2020-03-24 | 2020-08-31 | 0.70 | 0.80 | |
| 2020-09-01 | 2020-10-08 | 0.55 | 0.80 | |
| 2020-10-09 | 2021-03-01 | 0.20 | 0.80 | |
| | | Social Distancing | | |
| Start date | End date | Adherence | Reduction of Contacts | |
| 2020-03-18 | 2020-05-31 | 0.70 | 0.95 | |
| 2020-06-01 | 2020-06-30 | 0.59 | 0.95 | |
| 2020-07-01 | 2020-10-08 | 0.45 | 0.95 | |
| 2020-10-09 | 2020-10-31 | 0.25 | 0.95 | |
| 2020-11-01 | 2020-03-01 | 0.15 | 0.95 | |
| | | School Closure | | |
| Start date | End date | Adherence | Reduction of Contacts | |
| 2020-03-21 | 2020-10-06 | 0.95 | 1.00 | |
| 2020-10-07 | 2020-12-17 | 0.80 | 1.00 | |
| 2020-12-18 | 2021-03-01 | 0.95 | 1.00 | |
| | | Use of Mask | | |
| Start date | End date | Adherence | Reduction of Contacts | |
| 2020-03-19 | 2020-05-31 | 0.20 | 0.85 | |
| 2020-06-01 | 2020-06-30 | 0.35 | 0.85 | |
| 2020-07-01 | 2020-10-31 | 0.42 | 0.85 | |
| 2020-11-01 | 2020-03-01 | 0.37 | 0.85 | |
| | | Work from Home | | |
| Start date | End date | Adherence | Reduction of Contacts | |
| 2020-03-16 | 2020-05-31 | 0.60 | 0.95 | |
| 2020-06-01 | 2020-06-30 | 0.48 | 0.95 | |
| 2020-07-01 | 2020-10-08 | 0.36 | 0.95 | |
| 2020-10-09 | 2020-10-31 | 0.20 | 0.95 | |
| 2020-11-01 | 2021-03-01 | 0.15 | 0.95 | |
| | | cocooning of older adults | | |
| Start date | End date | Adherence | Reduction of Contacts | |
| 2020-03-14 | 2020-05-31 | 0.10 | 0.95 | |
| 2020-06-01 | 2020-06-30 | 0.40 | 0.95 | |
| 2020-07-01 | 2020-07-31 | 0.50 | 0.95 | |
| 2020-08-01 | 2020-08-31 | 0.60 | 0.95 | |
| 2020-09-01 | 2020-10-06 | 0.70 | 0.95 | |
| 2020-10-07 | 2020-11-01 | 0.80 | 0.95 | |
| 2020-11-02 | 2021-03-01 | 0.75 | 0.95 | |
| | | Travel Ban | | |
| Start date | End date | Mean imports | Reduction of Contacts | |
| 2020-02-19 | 2020-03-18 | 0.20 | 0.0 | |
| 2020-03-19 | 2021-03-01 | 0.20 | 0.70 | |

Table 7: List of interventions used for model fitting in the case of São Paulo, SP.

| | | Self Isolation | | |
|------------|------------|---------------------------|-----------------------|--|
| Start date | End date | Adherence | Reduction of Contacts | |
| 2020-03-17 | 2020-11-14 | 0.70 | 0.80 | |
| 2020-11-15 | 2020-03-01 | 0.35 | 0.80 | |
| | | Social Distancing | | |
| Start date | End date | Adherence | Reduction of Contacts | |
| 2020-03-17 | 2020-04-30 | 0.70 | $0.95\,$ | |
| 2020-05-01 | 2020-07-13 | 0.65 | 0.95 | |
| 2020-07-14 | 2020-08-31 | 0.50 | 0.95 | |
| 2020-09-01 | 2020-11-14 | 0.55 | 0.95 | |
| 2020-11-15 | 2020-03-01 | 0.20 | 0.95 | |
| | | School Closure | | |
| Start date | End date | Adherence | Reduction of Contacts | |
| 2020-03-18 | 2020-11-10 | 0.95 | $1.00\,$ | |
| 2020-11-11 | 2020-12-17 | 0.80 | 1.00 | |
| 2020-12-18 | 2021-01-31 | 0.95 | $1.00\,$ | |
| 2021-02-01 | 2021-03-01 | 0.30 | $1.00\,$ | |
| | | Use of Mask | | |
| Start date | End date | Adherence | Reduction of Contacts | |
| 2020-03-17 | 2020-07-13 | 0.16 | 0.85 | |
| 2020-07-14 | 2020-08-31 | 0.38 | 0.85 | |
| 2020-09-01 | 2020-11-14 | 0.49 | 0.85 | |
| 2020-11-15 | 2021-03-01 | 0.29 | 0.85 | |
| | | Work from Home | | |
| Start date | End date | Adherence | Reduction of Contacts | |
| 2020-03-20 | 2020-07-13 | 0.60 | $\rm 0.95$ | |
| 2020-07-14 | 2020-11-14 | 0.48 | 0.95 | |
| 2020-11-15 | 2021-03-01 | 0.40 | 0.95 | |
| | | cocooning of older adults | | |
| Start date | End date | Adherence | Reduction of Contacts | |
| 2020-03-14 | 2021-03-01 | 0.25 | 0.95 | |
| | | Travel Ban | | |
| Start date | End date | Mean imports | Reduction of Contacts | |
| 2020-02-19 | 2020-03-18 | 0.20 | 0.0 | |
| 2020-03-19 | 2021-03-01 | 0.20 | 0.70 | |

Table 8: List of interventions used for model fitting in the case of Goiânia, GO.

| | Self Isolation | | |
|-----------------------|---------------------------|------------|------------|
| Reduction of Contacts | Adherence | End date | Start date |
| 0.80 | 0.70 | 2020-12-18 | 2020-03-19 |
| | Social Distancing | | |
| Reduction of Contacts | Adherence | End date | Start date |
| 0.95 | 0.65 | 2020-05-10 | 2020-03-17 |
| 0.95 | 0.60 | 2020-06-22 | 2020-05-11 |
| 0.95 | 0.55 | 2020-09-28 | 2020-06-23 |
| 0.95 | 0.50 | 2020-12-18 | 2020-09-29 |
| | School Closure | | |
| Reduction of Contacts | Adherence | End date | Start date |
| 1.00 | 0.95 | 2020-09-07 | 2020-03-19 |
| 1.00 | 0.80 | 2020-12-17 | 2020-09-08 |
| $1.00\,$ | 0.95 | 2021-12-18 | 2020-12-18 |
| | Use of Mask | | |
| Reduction of Contacts | Adherence | End date | Start date |
| 0.85 | 0.16 | 2020-05-10 | 2020-03-19 |
| 0.85 | 0.38 | 2020-06-22 | 2020-05-11 |
| 0.85 | 0.57 | 2020-09-28 | 2020-06-23 |
| 0.85 | 0.49 | 2020-12-18 | 2020-09-29 |
| | Work from Home | | |
| Reduction of Contacts | Adherence | End date | Start date |
| 0.95 | $0.60\,$ | 2020-05-10 | 2020-03-19 |
| 0.95 | 0.45 | 2020-06-22 | 2020-05-11 |
| 0.95 | 0.55 | 2020-09-28 | 2020-06-23 |
| 0.95 | 0.40 | 2020-11-30 | 2020-09-29 |
| 0.95 | 0.50 | 2020-12-18 | 2020-12-01 |
| | cocooning of older adults | | |
| Reduction of Contacts | Adherence | End date | Start date |
| 0.95 | 0.30 | 2020-12-18 | 2020-03-14 |
| | Travel Ban | | |
| Reduction of Contacts | Mean imports | End date | Start date |
| 0.0 | 0.20 | 2020-03-18 | 2020-02-19 |
| 0.70 | 0.20 | 2021-03-01 | 2020-03-19 |

Table 9: List of interventions used for model fitting in the case of Porto Alegre, RS.

| City | Start date | End date |
|--------------|------------|------------|
| São Paulo | 2020-03-22 | 2020-12-18 |
| Goiânia. | 2020-03-22 | 2021-03-05 |
| Porto Alegre | 2020-03-22 | 2020-12-18 |

Table 10: Time interval of new hospitalizations from SIVEP-Gripe that were fitted for each city.

| City | Parameter | Estimate | Std. Error | t value | Pr(> t) |
|--------------|--|---|----------------------------------|----------------------------------|--|
| São Paulo | \mathcal{p} T_{perc} h_{steep} startdate | 0.04184 0.55151 4.58545 2020-01-26 | 0.00010 0.00152 0.02065 | 397.8866 362.8879 222.0186 | $7.318e-155$ 4.578e-151 8.082e-131 |
| Porto Alegre | \boldsymbol{p} T_{perc} h_{steep} startdate | 0.04565 0.48442 0.00243 2020-02-18 | 0.00019 0.34299 0.00062 | 239.8034 1.4123 3.8858 | 1.701e-107 0.16209 0.00022 |
| Goiânia | \mathcal{p} T_{perc} h_{steep} startdate | 0.02890 0.72814 15.0106 2020-01-27 | $5.5e-0.5$ 0.00307 0.05038 | 523.3179 237.4351 297.9735 | 3.664e-166 1.389e-133 6.097e-143 |

Table 11: Best fit results for each of the cities studied.

Table 13: Sensitivity analysis of the fitting for São Paulo, SP.

Table 14: Sensitivity analysis of the fitting for Porto Alegre, RS.

Table 15: Sensitivity analysis of the fitting for Goiânia, GO.